

Introduction to RAPT DR

Kinetic Equilibrium Prediction & pulse design for TCV

Cassandre Contré (*cassandre.contre@epfl.ch*)



What is RAPTOR?

What is a Kinetic Equilibrium Prediction (KEP)?

Application to TCV experiments

Summary

RApid Plasma Transport simulatOR^[1,2]

- **Rapid** transport solver of 1D tokamak plasma profiles

Why? → Turbulent transport is obtained via reduced models or NN regressions

- Designed for **real-time control...**

Why? → Written in Matlab, easily transferable to Simulink
→ Feedback controllers can be used for any actuator
→ Any diagnostics can be included as additional information into RT simulation

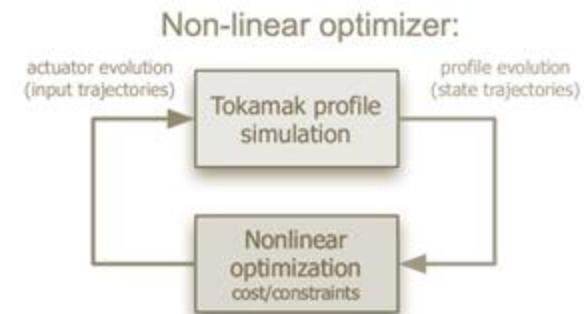
- ... and inter-discharge **optimization**

Why? → Knowledge of the analytical Jacobians $\frac{\partial \tilde{f}}{\partial x}, \frac{\partial \tilde{f}}{\partial u}$

DISCLAIMER

👎 Not made for:

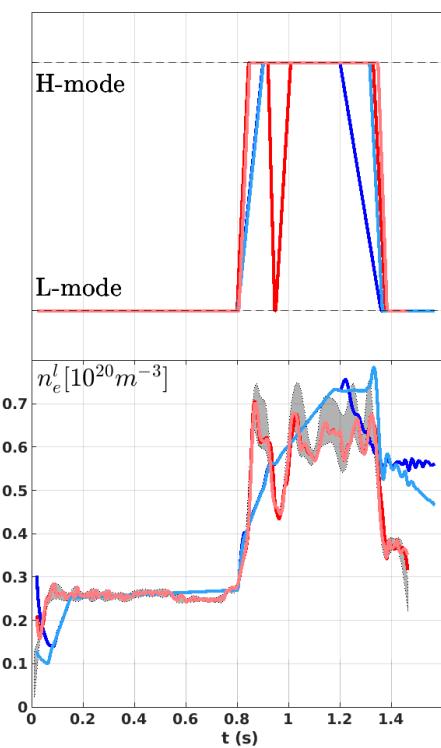
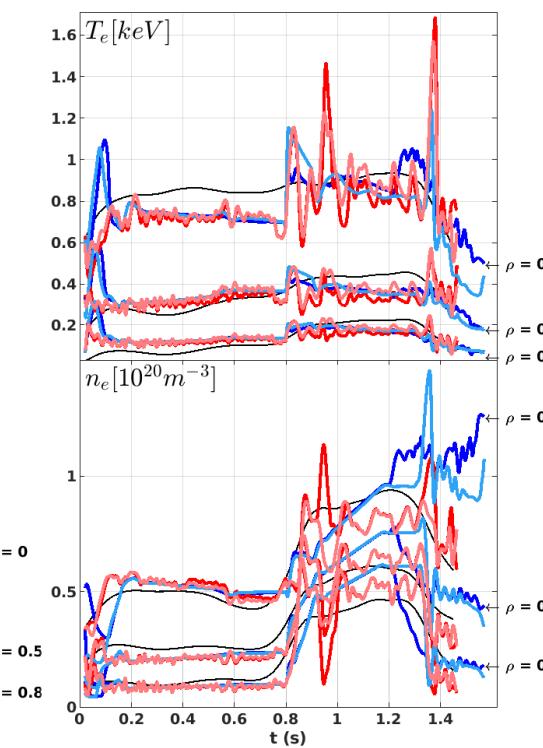
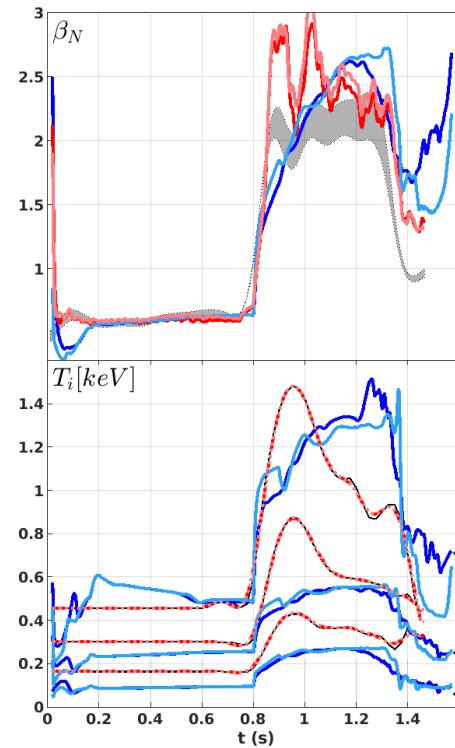
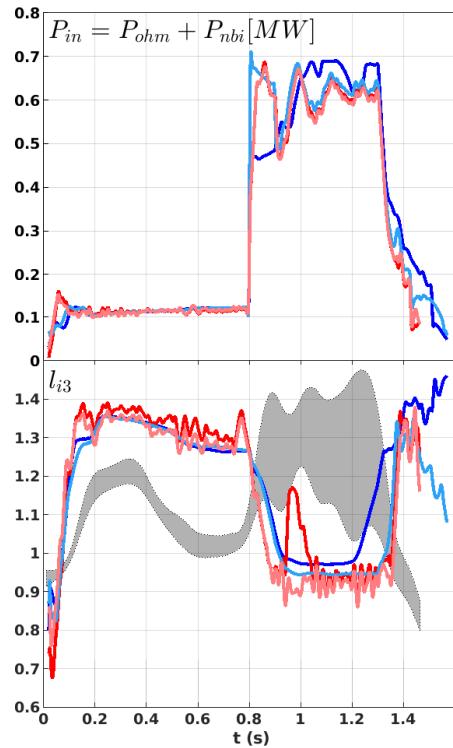
- predicting the performance of a scenario from scratch
- giving high fidelity predictions



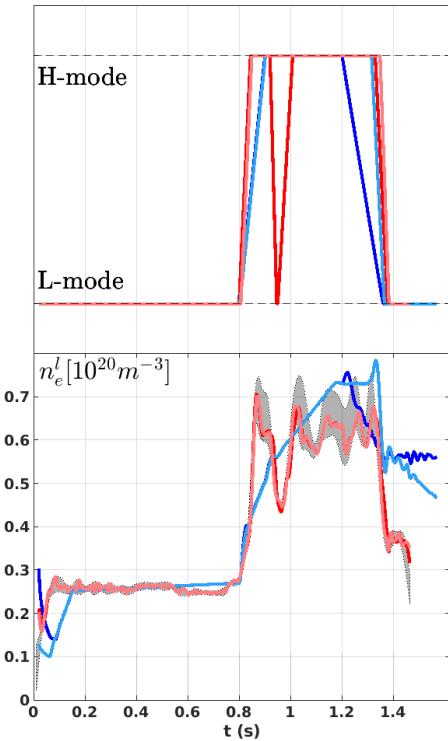
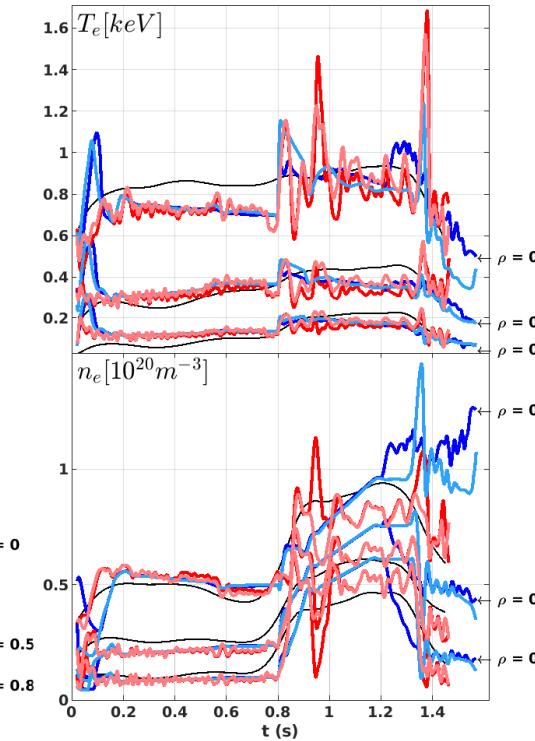
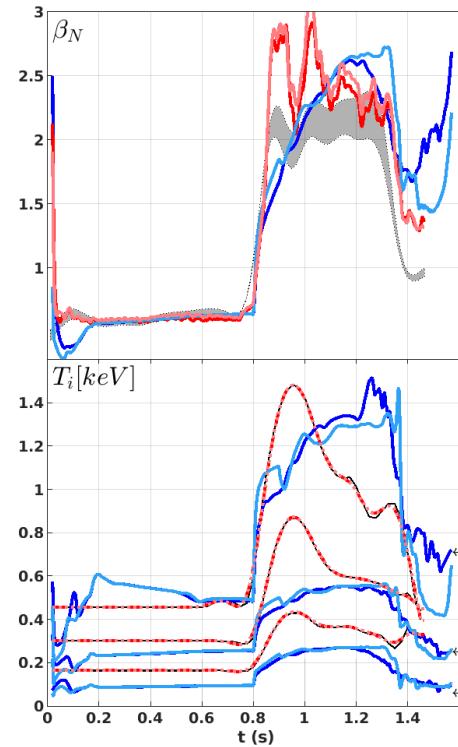
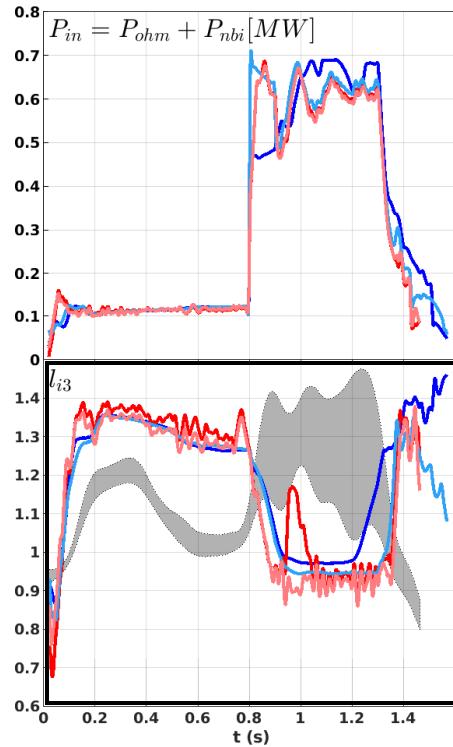
[1] F. Felici et al 2011 Nucl. Fusion 51 083052

[2] F. Felici et al 2018 Nucl. Fusion 58 096006

RAPTOR



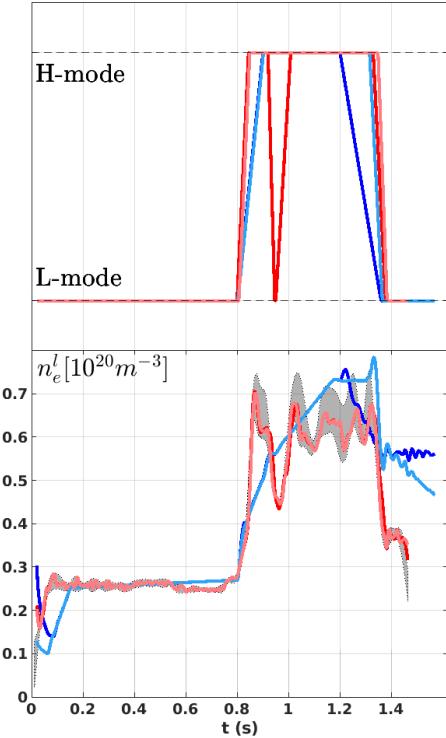
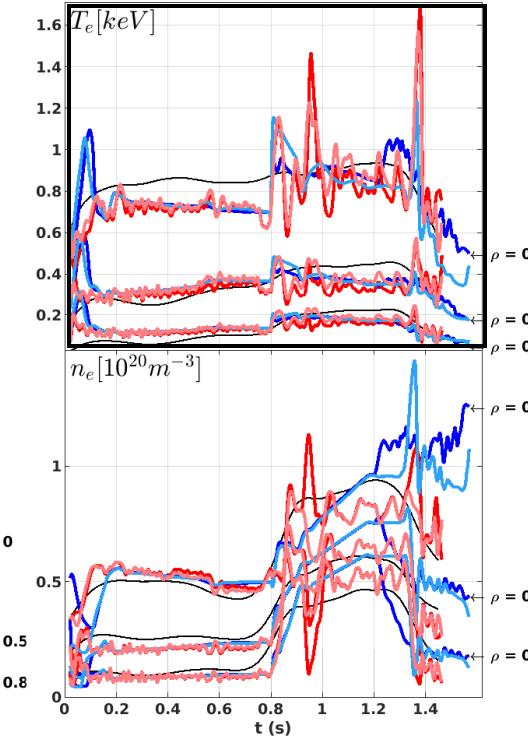
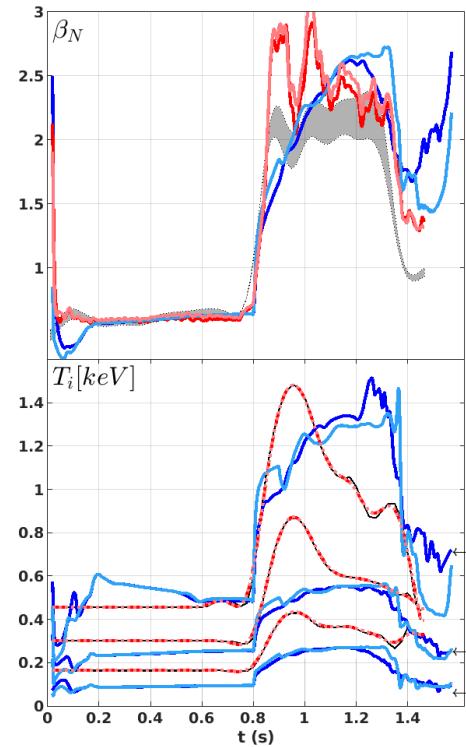
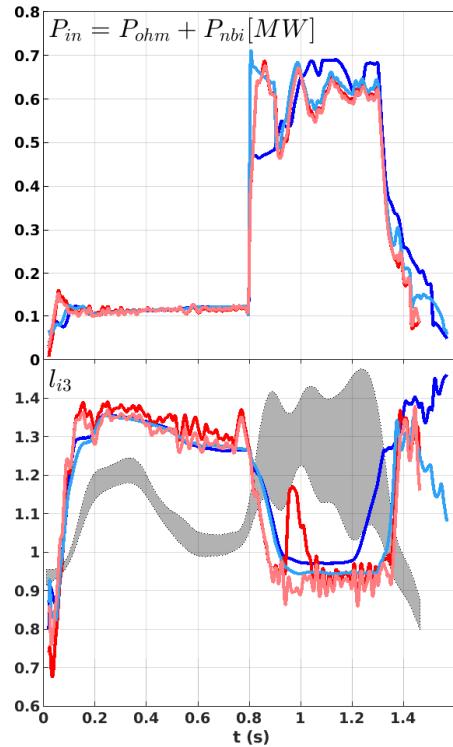
RAPTOR solves for ψ



$$\sigma_{\parallel} \left(\frac{2\Phi_b \rho}{V'_\rho} \frac{\partial \psi}{\partial t} \Big|_\rho - \frac{\rho^2 \dot{\Phi}_b}{V'_\rho} \frac{\partial \psi}{\partial \rho} \right) = \frac{F^2}{8\pi^2 \mu_0 \Phi_b V'_\rho} \frac{\partial}{\partial \rho} \left[\frac{g_2 g_3}{\rho} \frac{\partial \psi}{\partial \rho} \right] - \langle \mathbf{j}_{ni} \cdot \mathbf{B} \rangle \quad (current^*)$$

*See lecture: Plasma profiles and their control, eq.12

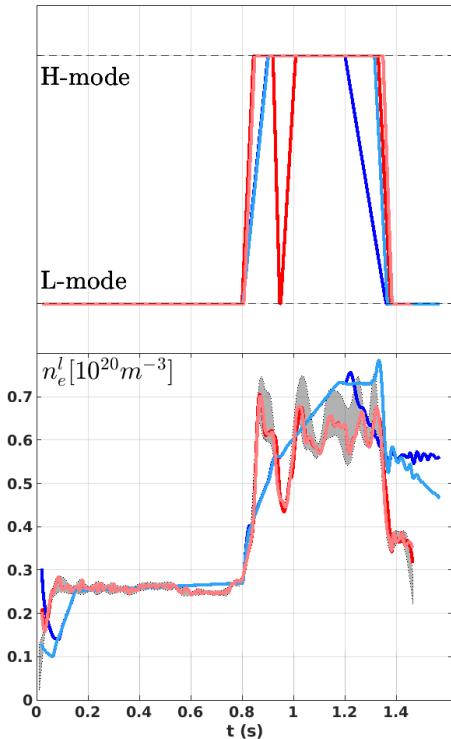
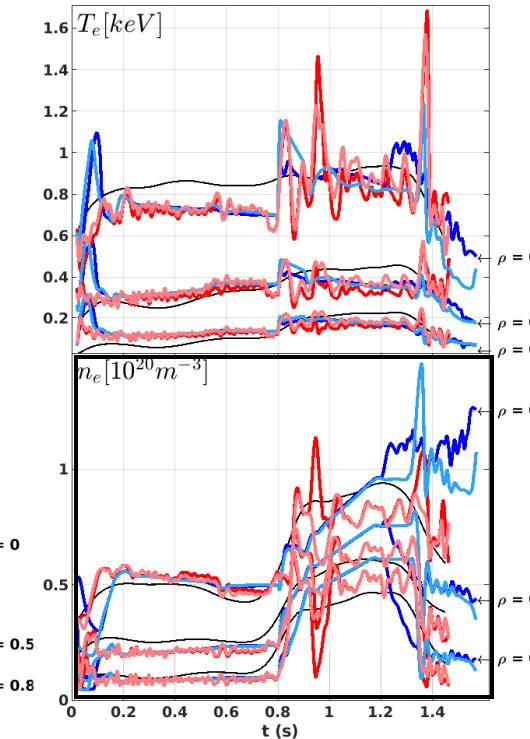
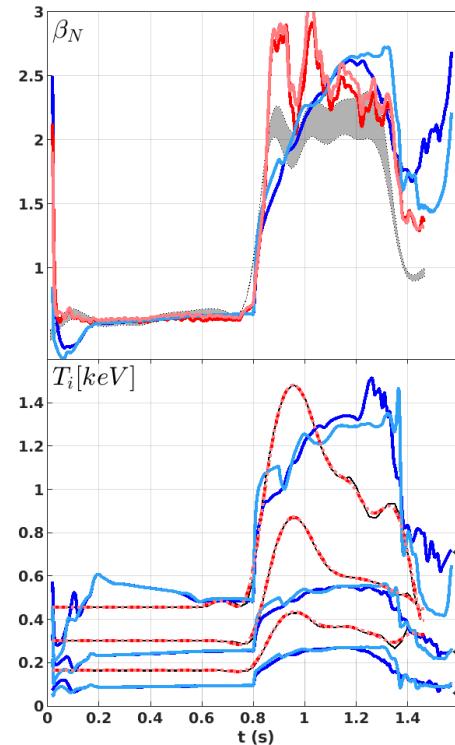
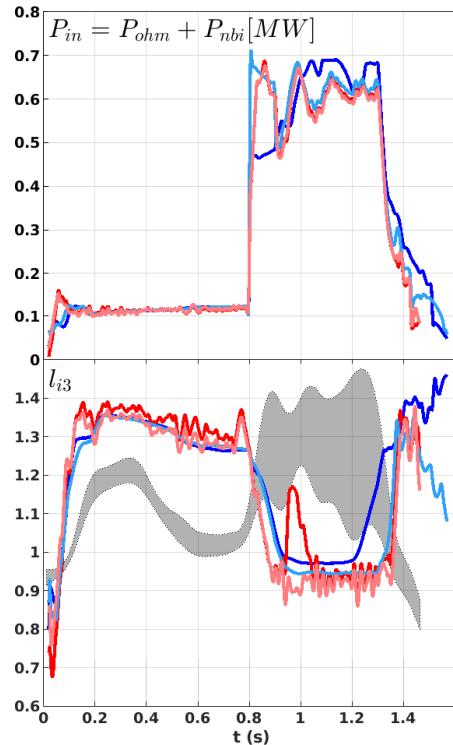
RAPTOR can solve for T_e



$$\frac{3}{2}(V'_\rho)^{-5/3} \left(\frac{\partial}{\partial t} \Big|_\rho - \frac{\dot{\Phi}_b}{2\Phi_b} \frac{\partial}{\partial \rho} \rho \right) [(V'_\rho)^{5/3} n_{e,i} T_{e,i}] + \frac{1}{V'_\rho} \frac{\partial}{\partial \rho} \left(-\frac{g_1}{V'_\rho} n_{e,i} \chi_{e,i} \frac{\partial T_{e,i}}{\partial \rho} + \frac{5}{2} T_{e,i} \Gamma_{e,i} g_0 \right) = P_{e,i} \quad (\text{temperature})$$

*See lecture: Plasma profiles and their control, eq.22

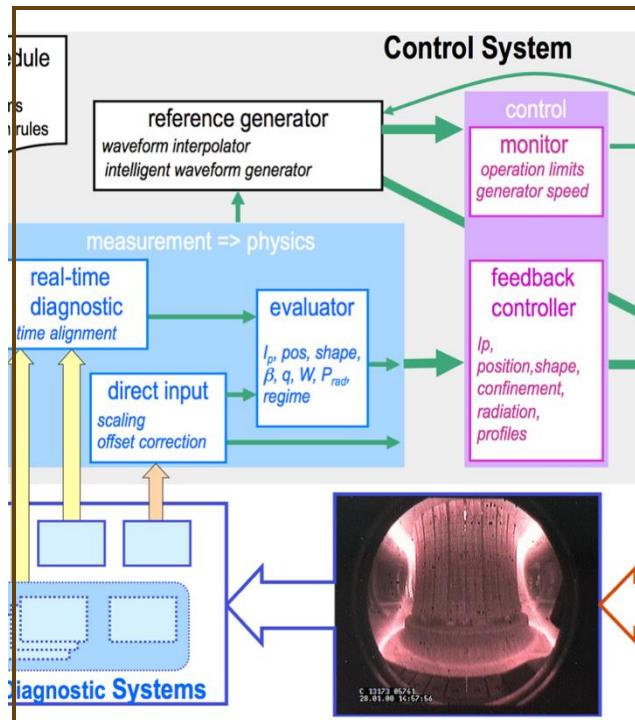
RAPTOR can solve for n_e



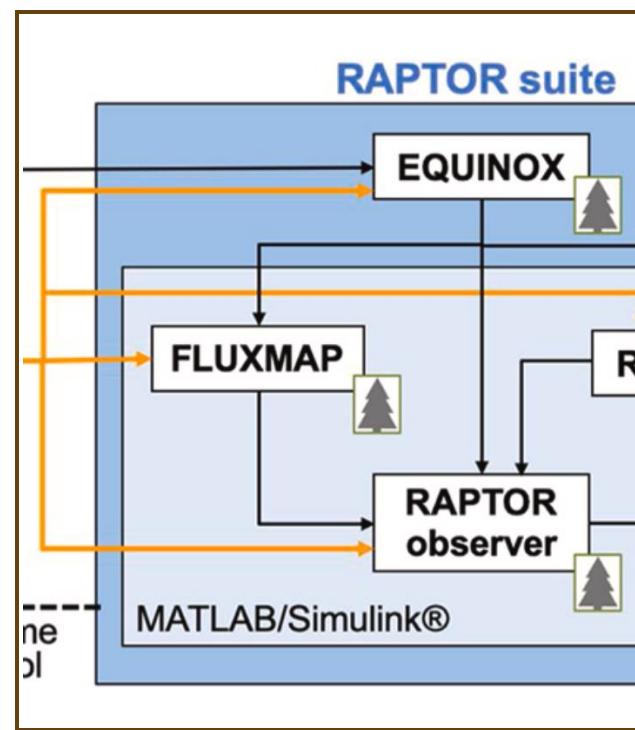
$$\frac{1}{V'_{\hat{\rho}}} \left(\frac{\partial}{\partial t} \Big|_{\hat{\rho}} - \frac{\dot{\Phi}_b}{2\Phi_b} \frac{\partial}{\partial \hat{\rho}} \hat{\rho} \right) [V'_{\hat{\rho}} n_e] = - \frac{1}{V'_{\hat{\rho}}} \frac{\partial}{\partial \hat{\rho}} \Gamma_e + S_e$$

(density)

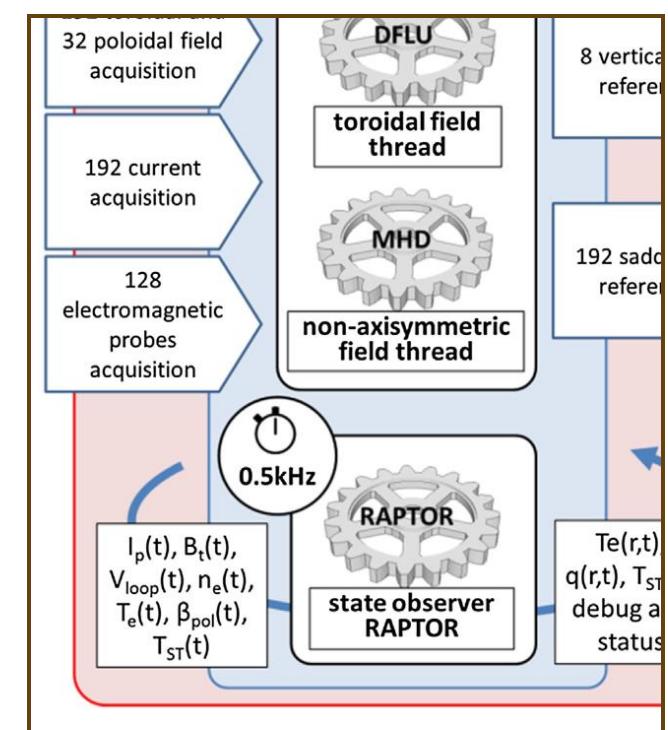
RAPTOR is implemented in RT at



AUG

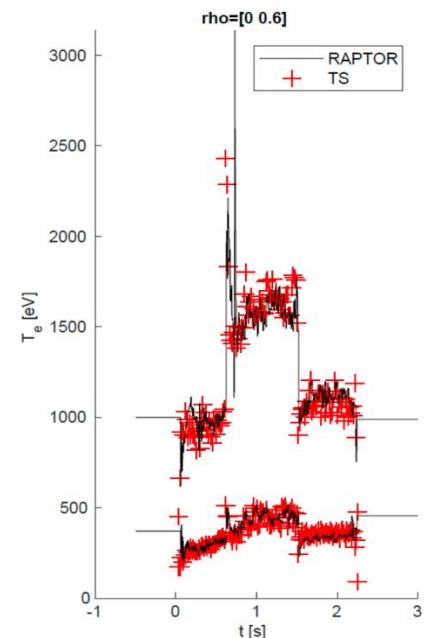
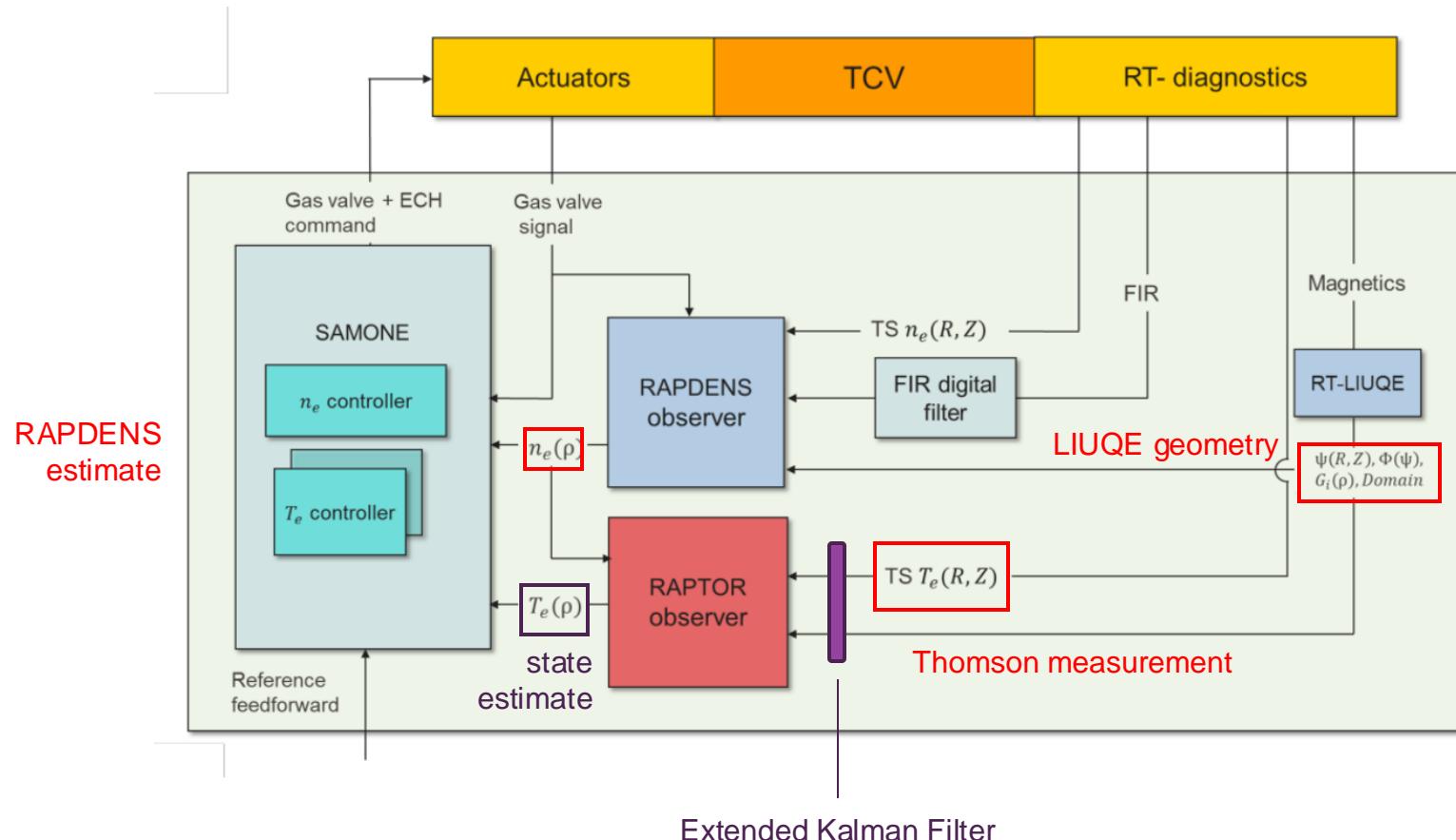


JET



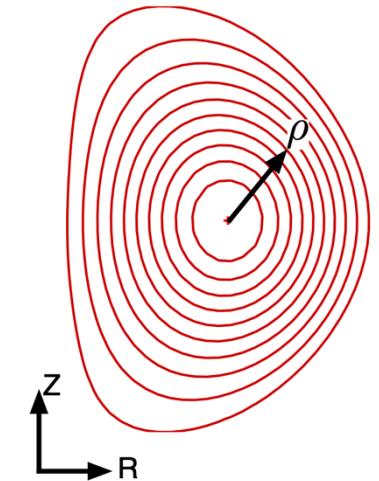
RFX

RAPTOR is implemented in RT at TCV



Reminder

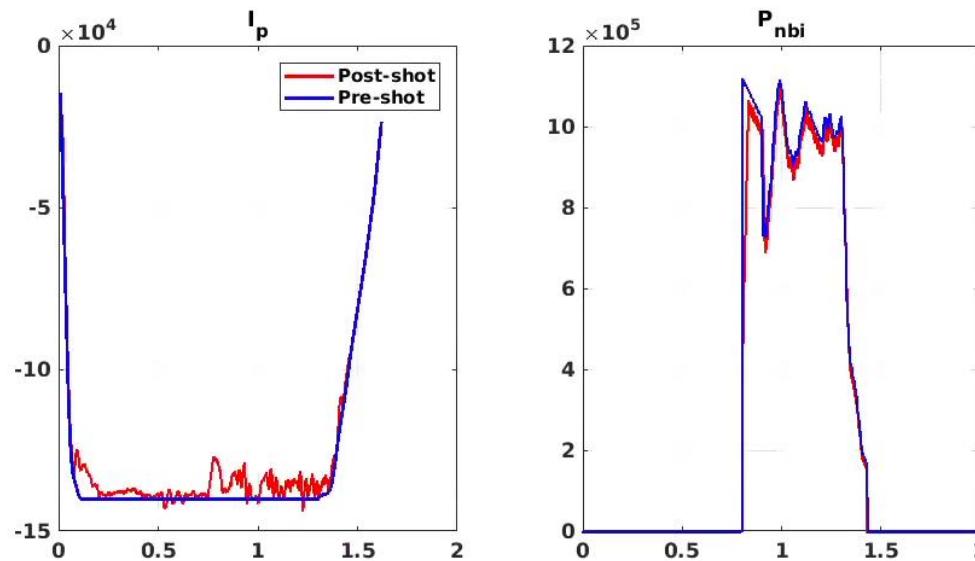
- As said in previous course*, 1D transport solvers require a **2D equilibrium** from an external Grad-Shafranov solver
- Historically, RAPTOR is run with **CHEASE**, a fixed-boundary equilibrium solver
 - *can re-compute Grad-Shafranov from almost any free-boundary code and any machine, if given in an EQDSK format*
- But it can also be coupled to a **free-boundary equilibrium** solver directly



Kinetic Equilibrium Prediction

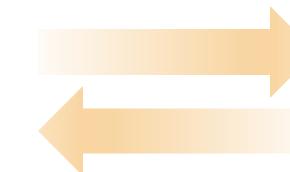
What is a pre-shot simulation?

What is a Kinetic Equilibrium Prediction (KEP)?



In post-shot, one can do a **KER**

LIUQE
equilibrium
reconstruction



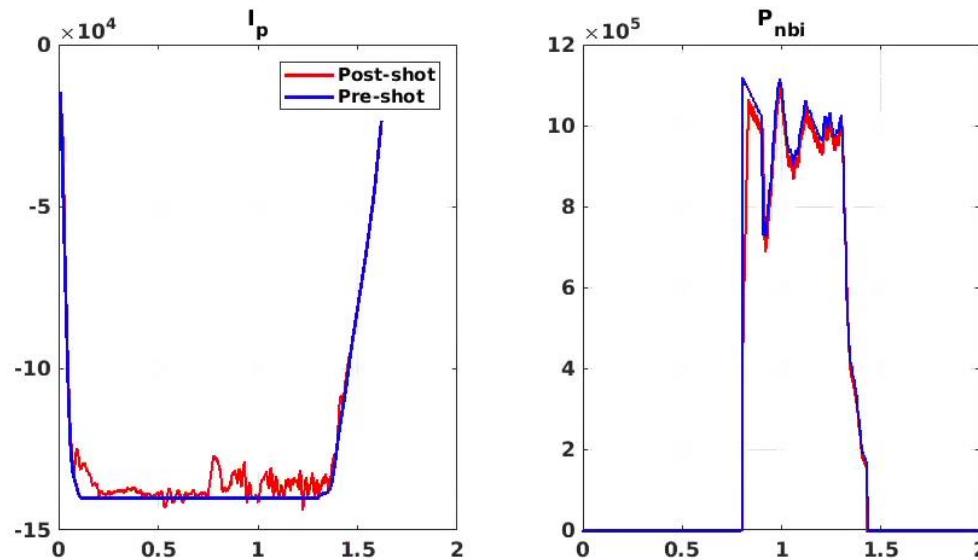
RAPTOR
post-shot
transport
simulation

Post-shot available inputs:

- LIUQE 2D equilibrium
- TS mesurement for pedestal top $\rightarrow T_e, n_e$ boundary conditions at $\rho = \rho_{ped}$
- Actuators ($I_p, P_{NBI}, P_{EC} \dots$) actions, as observed in experiment
- Obtained line-averaged density $n_{e,l}$, current drive j_{ec} , confinement... etc.
- L-H transition, MHD events... etc.

→ we don't have all
this information
pre-shot!

What is a Kinetic Equilibrium Prediction (KEP)?



In pre-shot, equivalent is a **KEP**

FBT
inverse
equilibrium
solution



RAPTOR
pre-shot
transport
simulation

Pre-shot available inputs:

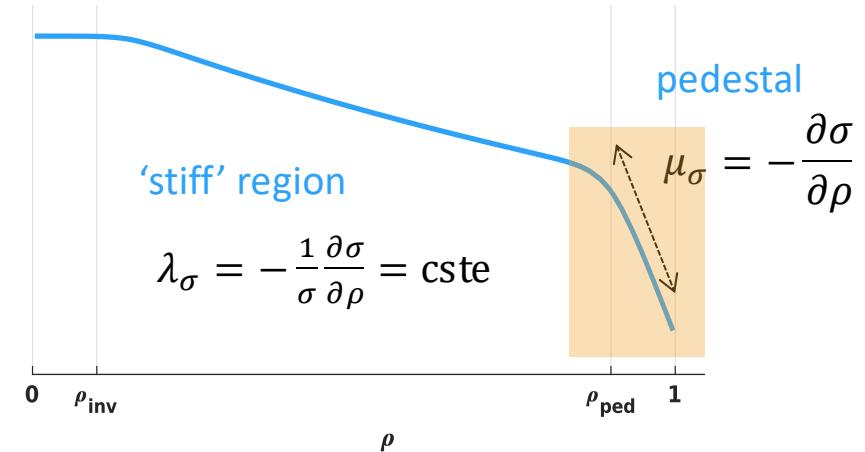
- FBT 2D equilibrium
- No a-priori information on the pedestal
- Actuators (I_p , P_{NBI} , P_{EC} ...) programming
- Gas valve reference, ECRH angles... etc.
- No a-priori information on the L-H transition

What is a Kinetic Equilibrium Prediction (KEP)?

For this, we use the **gradient-based model**^[1]

based on the observation that for $\sigma = \{T_e, n_e\}$

- the logarithmic gradients remain stiff^[2] in an intermediate region between $\rho_{inv} \sim 0.1$ and $\rho_{ped} \sim 0.8$
- while the pedestal gradient μ_σ varies with the shot confinement^[3]



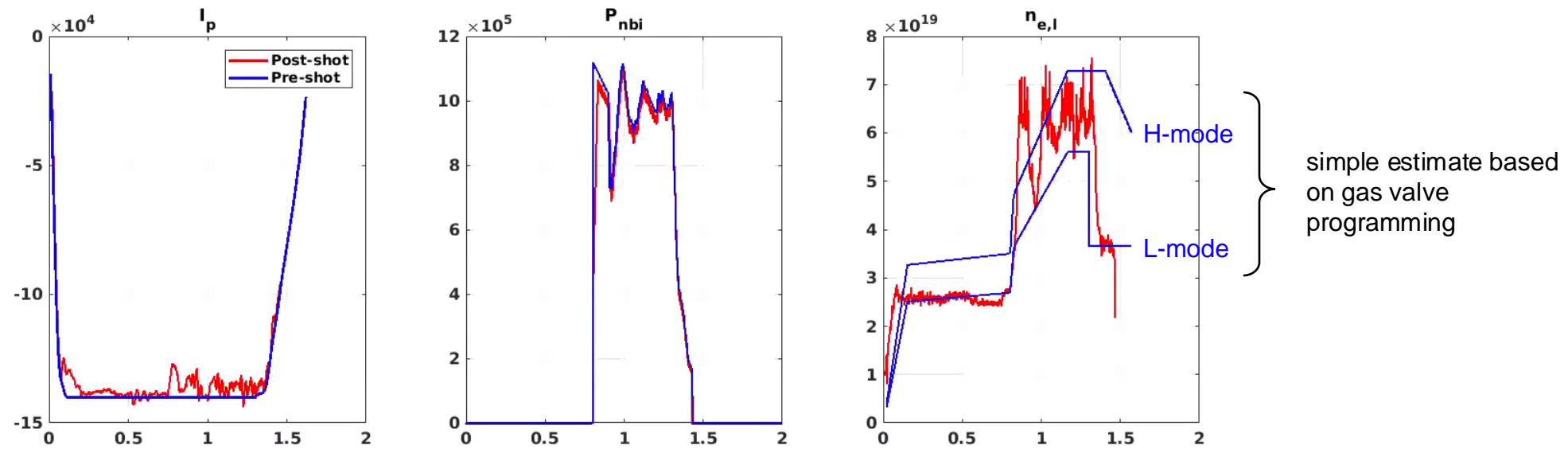
Coupled to a L-H transition prediction, following **Y. Martin's scaling law**^[4]

$$P_{LH} = \frac{2}{A_i} 2.15 \cdot 10^6 n_e^{l,20^{0.782}} B_0^{0.772} a^{0.975} R_0^{0.999}$$

$$P_{sep} > \alpha P_{LH}$$

$$P_{sep} = P_{oh} + P_{aux} - P_{rad} - \frac{dW}{dt}$$

What is a Kinetic Equilibrium Prediction (KEP)?



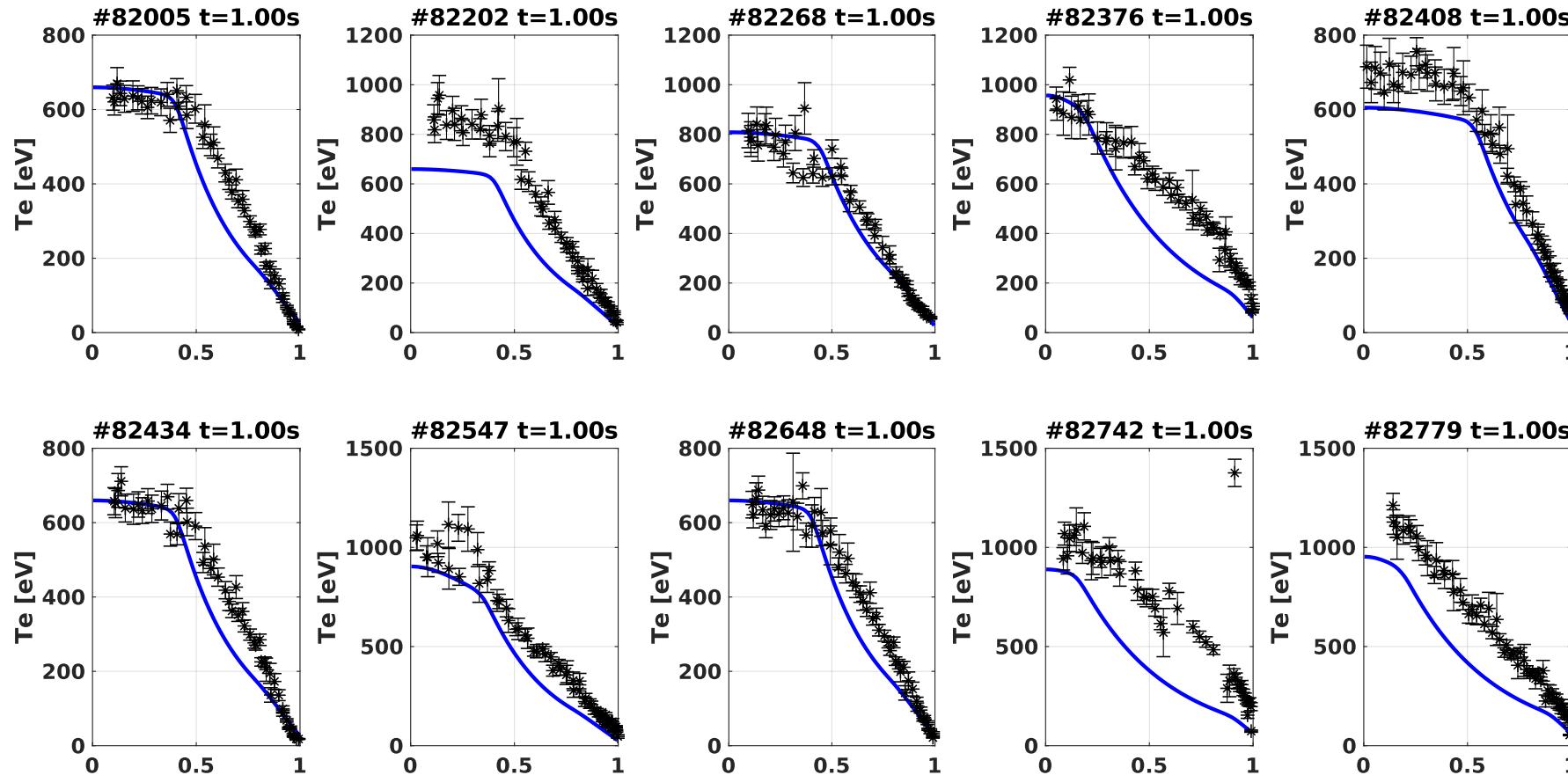
This model requires:

- Line-averaged density $n_{e,l}$ to control μ_{ne}
- Electron confinement quality^[1] H_e^{98} to control μ_{Te}
- Logarithmic gradients λ_{ne} and λ_{Te}

Mode	Triangularity	λ_{Te}	λ_{ne}	H_e^{98}
L	PT	3.3	3	0.4
H	PT	2.7	2	0.5
L	NT	3	3	0.5

What is a Kinetic Equilibrium Prediction (KEP)?

- Pre-shot RAPTOR simulations for ohmic shots with/without NBI is almost automatised

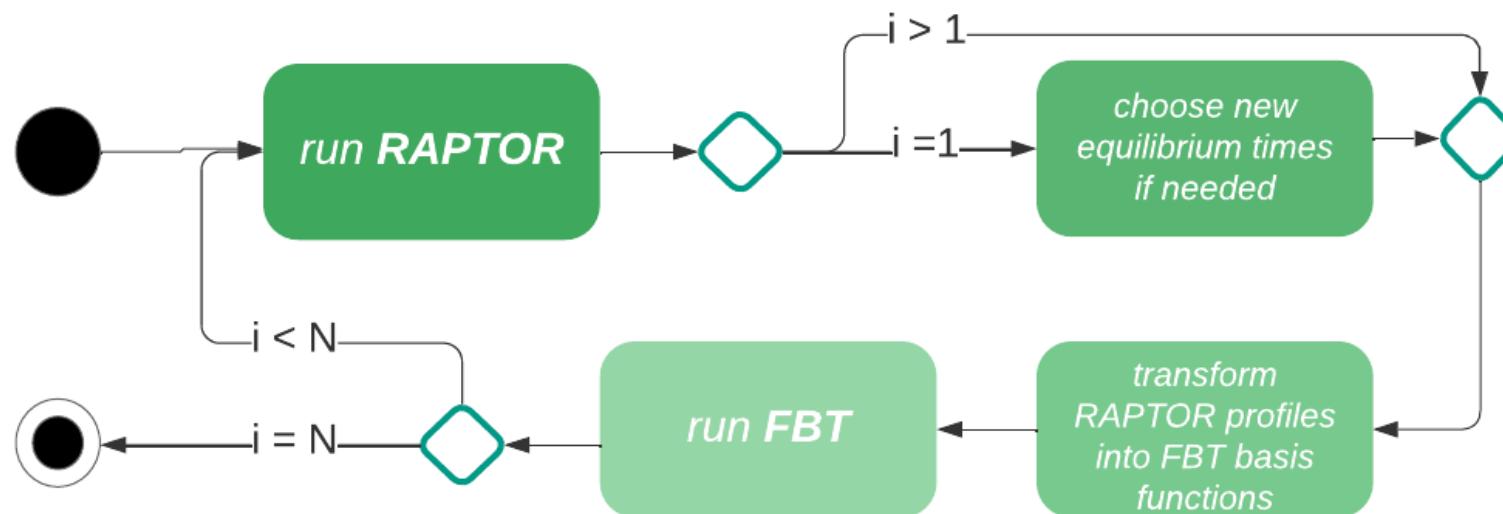


Kinetic-Equilibrium Prediction

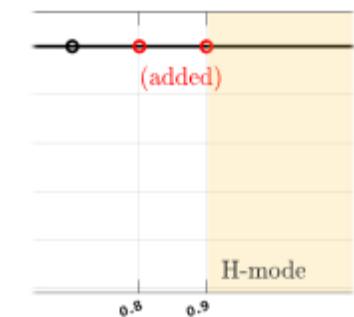
About the Kinetic-Equilibrium coupling...

Methodology

1. Prepare an initial FBT equilibrium on the standard GUI
2. Using information available prior to the shot, launch a RAPTOR simulation
3. If result is validated, launch coupling



RAPTOR informs us on the scenario dynamics



Methodology

1. Prepa
2. Using
3. If resu

Inputs:

Desired boundary shape
Internal p' , TT' profiles

FBT

Outputs:

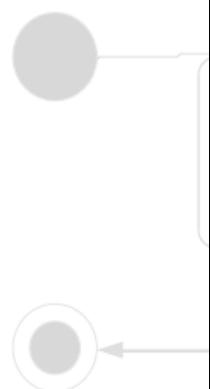
Required PF coil currents I_a
equilibrium flux mapping

When solving for Grad-Shafranov,

FBT is given one degree of freedom to match I_p :

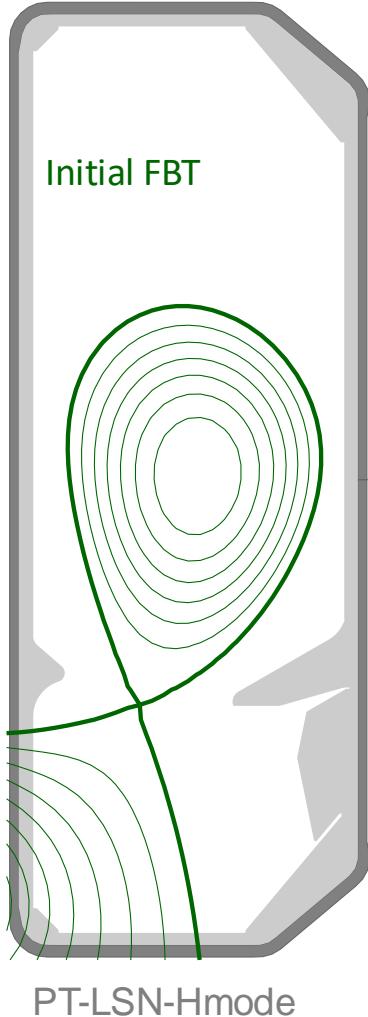
- $TT'_{FBT} = TT'_{RAP}$
- $p'_{FBT} = \alpha p'_{RAP}$

RAPTOR informs
us on the scenario
dynamics



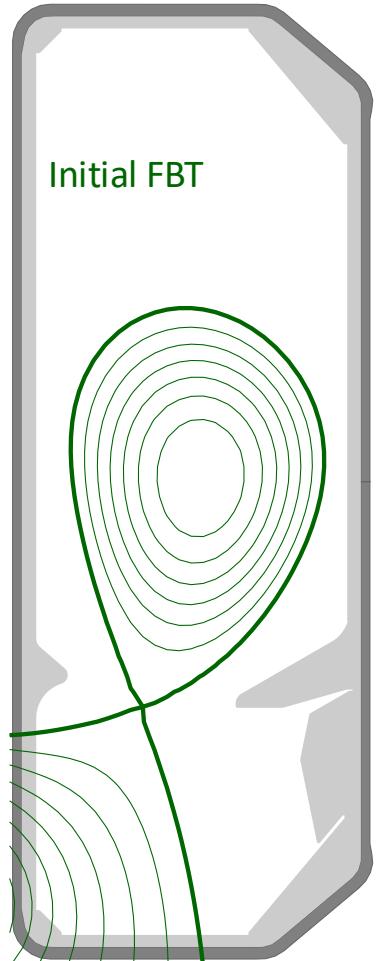
Convergence

- generally good for $I_p > 10\% I_p^{\max}$
- difference between p'_{RAP} and p'_{FBT} ($\alpha - 1$) decreases with iterations & falls rapidly below 5%
- 3-4 iterations often sufficient



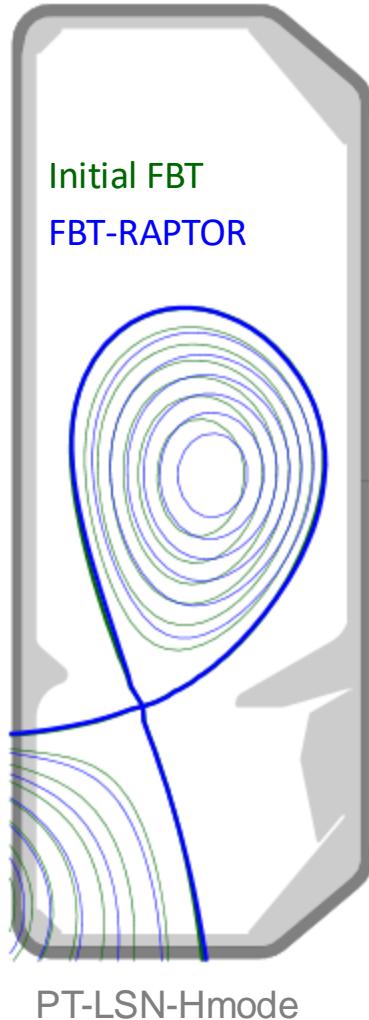
We start from a set of initial FBT equilibria prepared through the usual GUI,
assuming completely wrong values were chosen for q_A and β_p .

Then, a first RAPTOR simulation is launched.

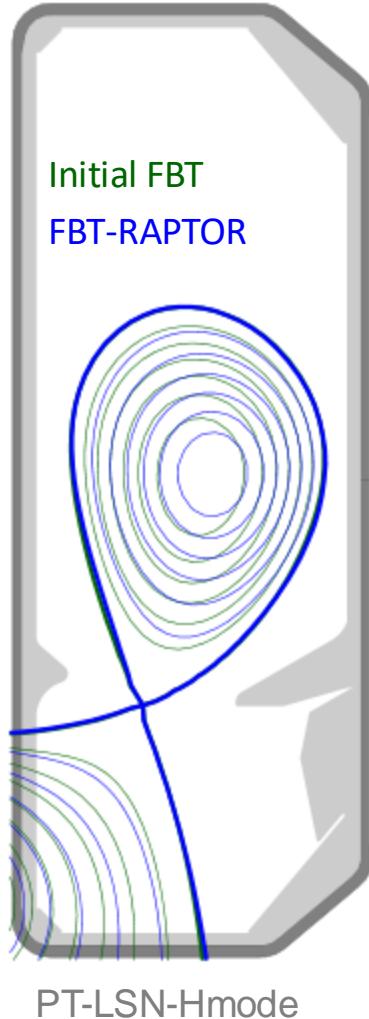


After 3 iterations between RAPTOR and FBT

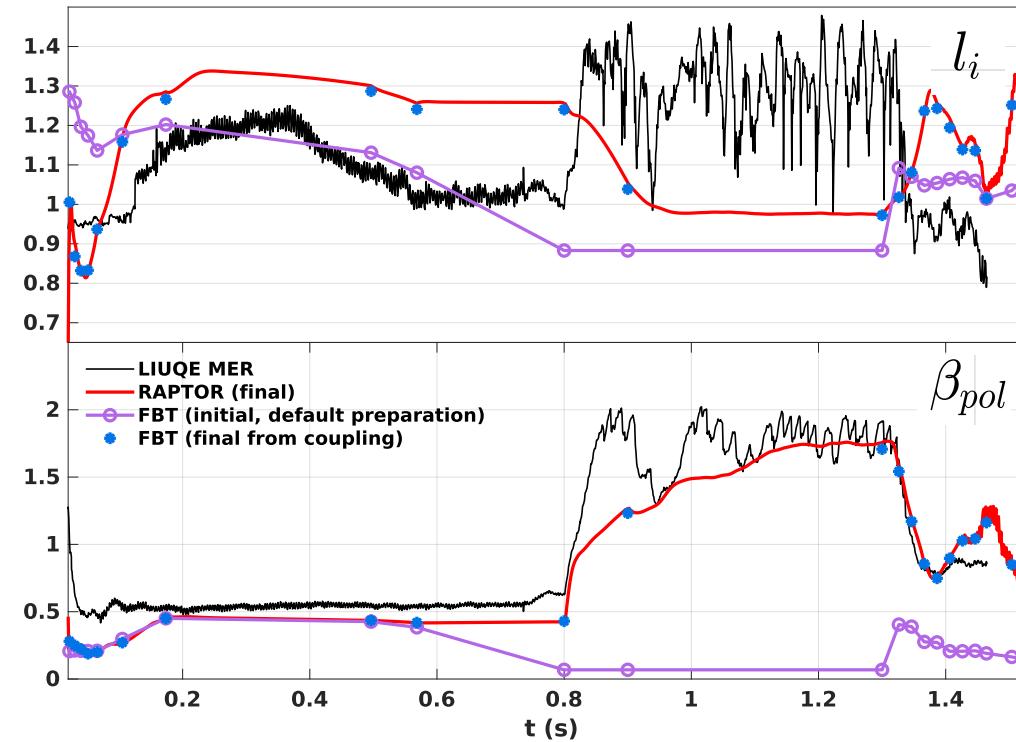
PT-LSN-Hmode

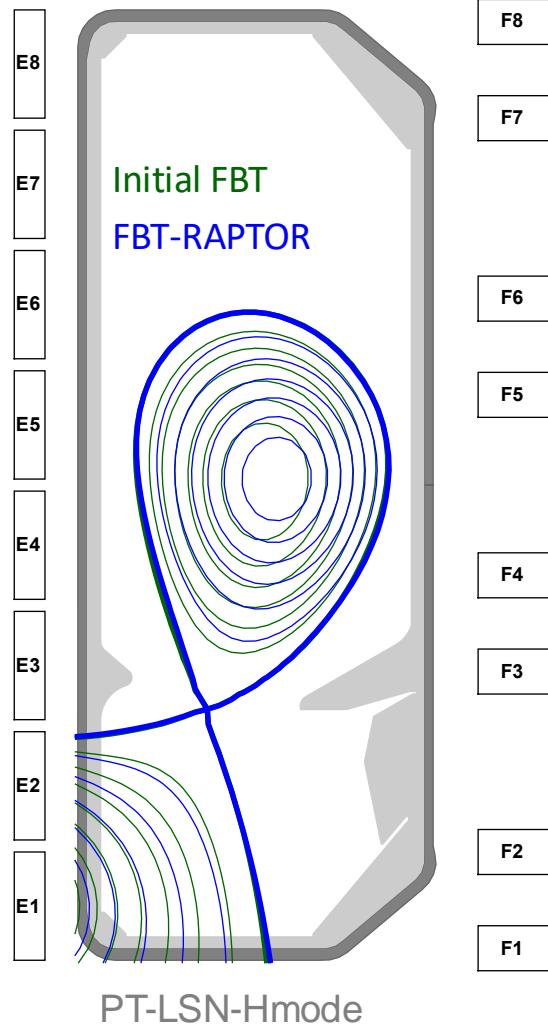


After 3 iterations between RAPTOR and FBT,
we get a new equilibrium.



After 3 iterations between RAPTOR and FBT,
we get a new equilibrium.



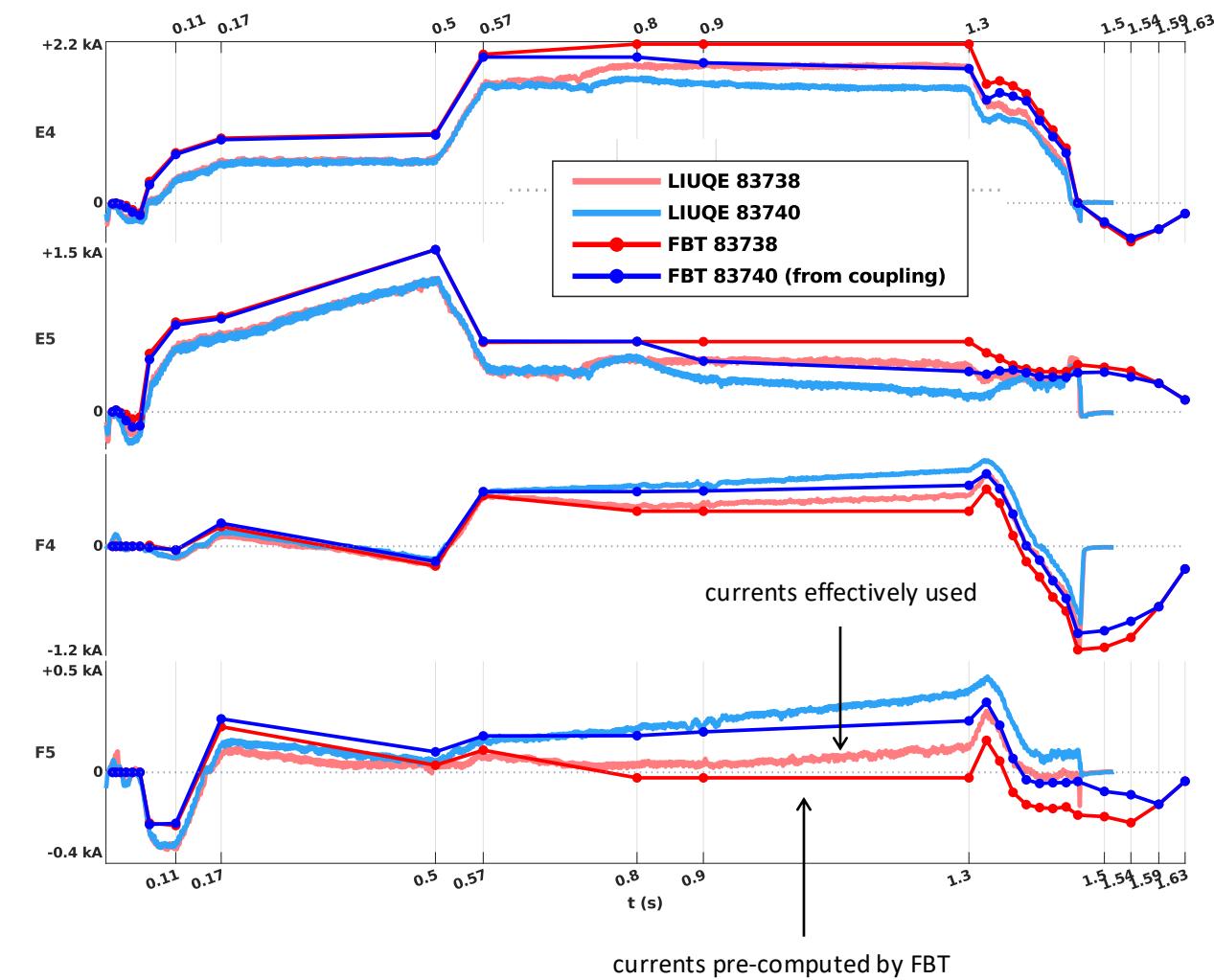
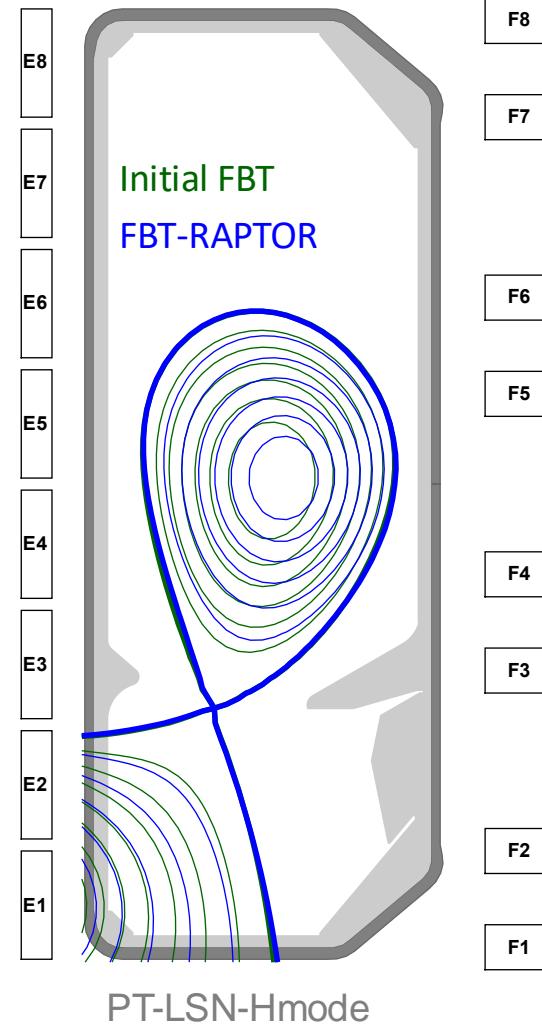


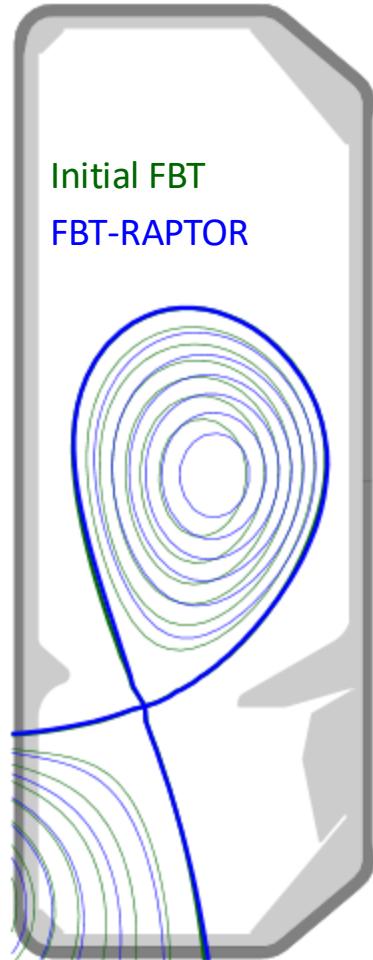
TCV has 16 PF coil currents (E1-8, F1-8) for shaping,
all individually controlled with an hybrid system.

It traditionnally uses FBT to compute reference for the shape alone,
to which is added:

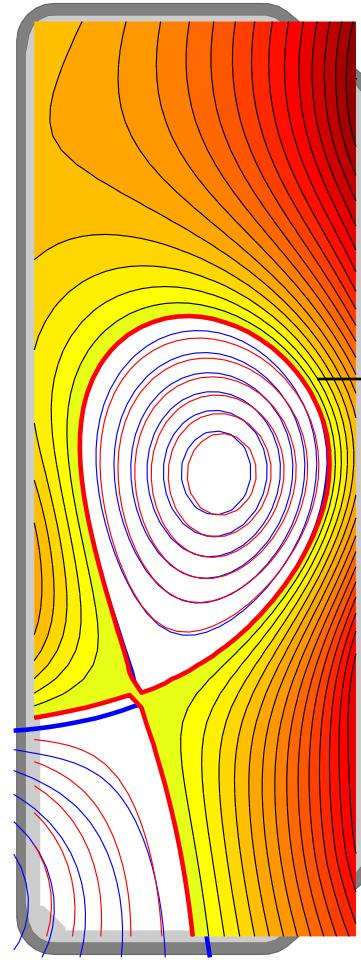
- reference for the central solenoid (to generate I_p)
- extra control polices, including control for RZ position

So we replicated the same shot two times in a row,
only changing the reference for shaping:
• #83738 using the initial FBT
• #83740 using FBT-RAPTOR



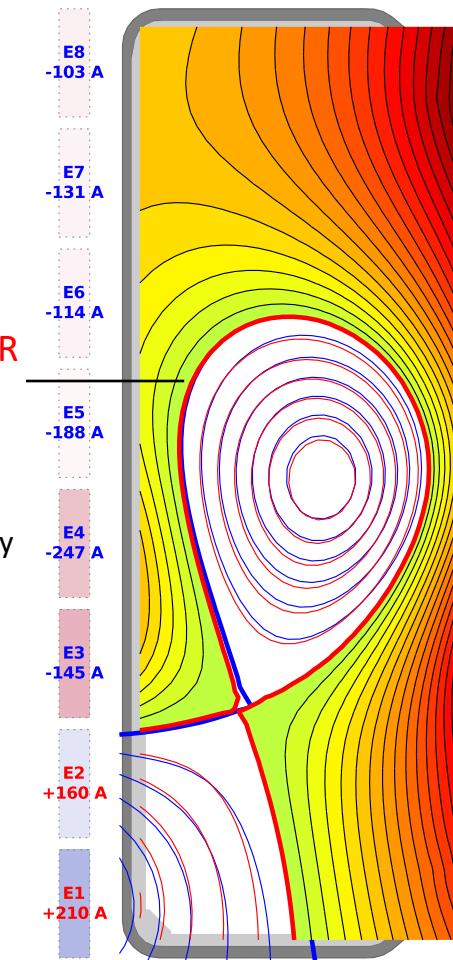


PT-LSN-Hmode



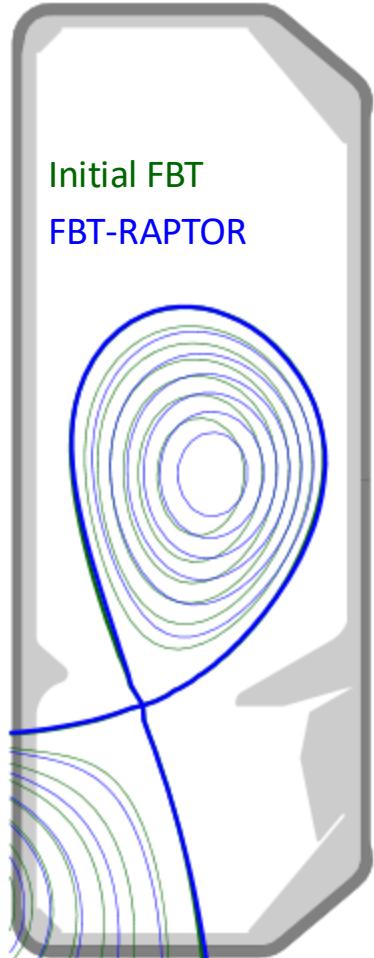
Shot prepared with FBT

LIUQE-ASTRA KER
Good agreement
with the inner
 $\psi(R, Z)$ predicted by
FBT-RAPTOR

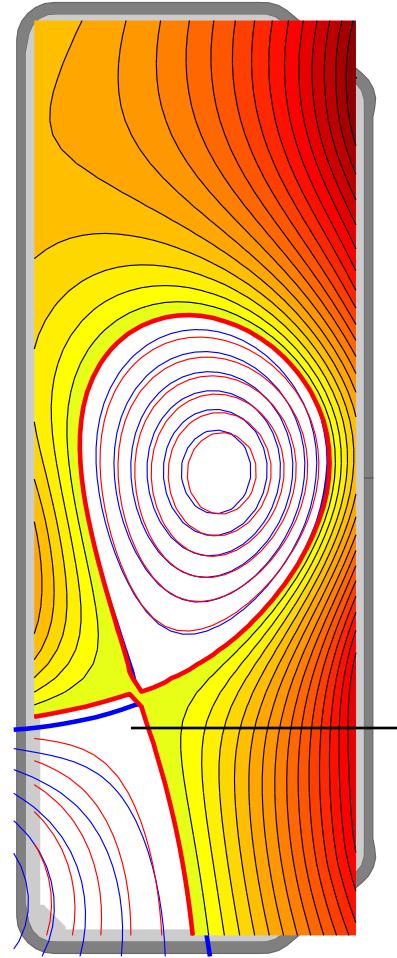


Shot prepared with FBT-RAPTOR



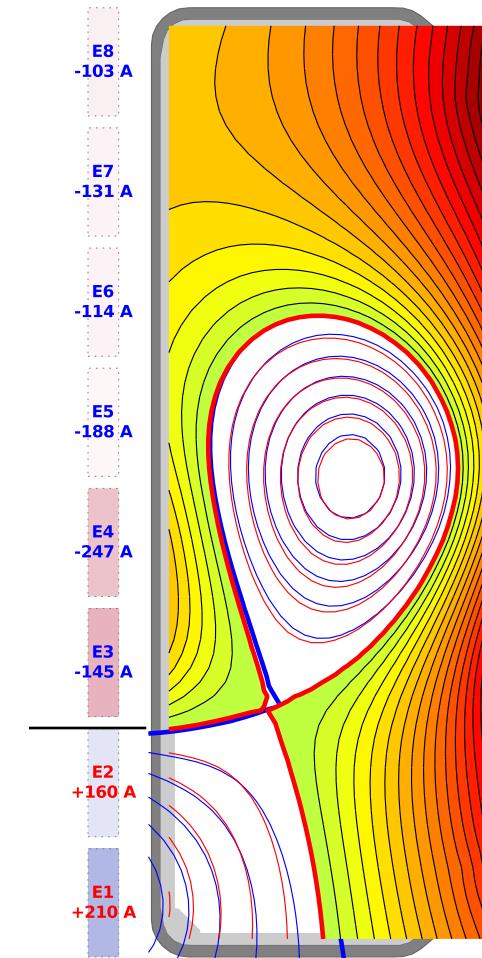


PT-LSN-Hmode



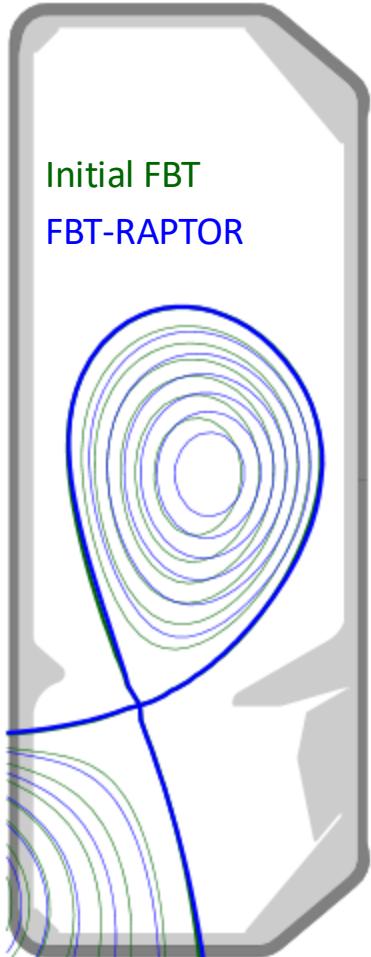
Shot prepared with FBT

Shot prepared with
FBT-RAPTOR
shows a better
alignment with X-
point target

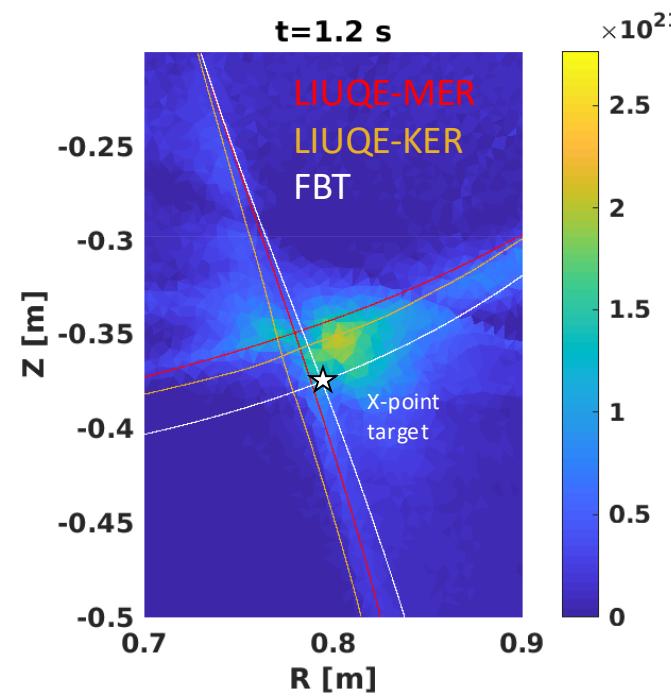


Shot prepared with FBT-RAPTOR

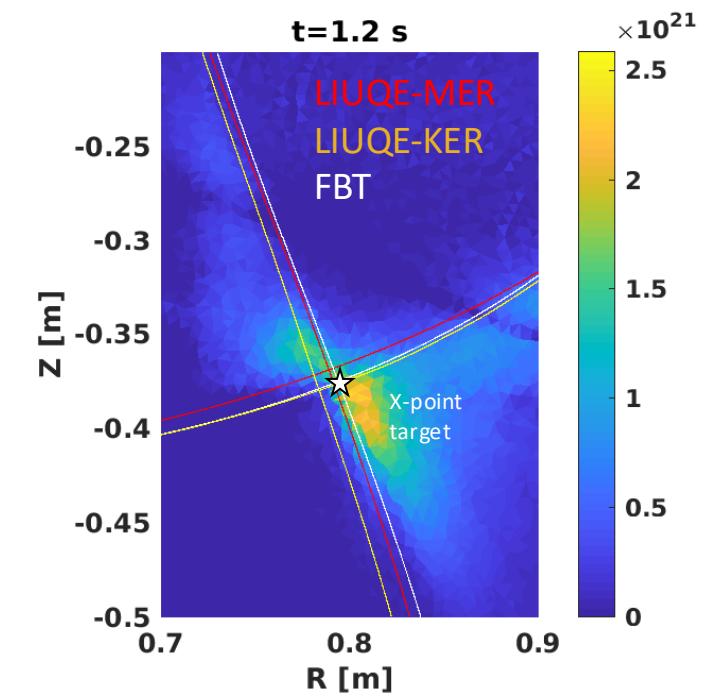
F8 -44 A
F7 -213 A
F6 -109 A
F5 +167 A
F4 +187 A
F3 -106 A
F2 -258 A
F1 -61 A



MANTIS tomographic inversion

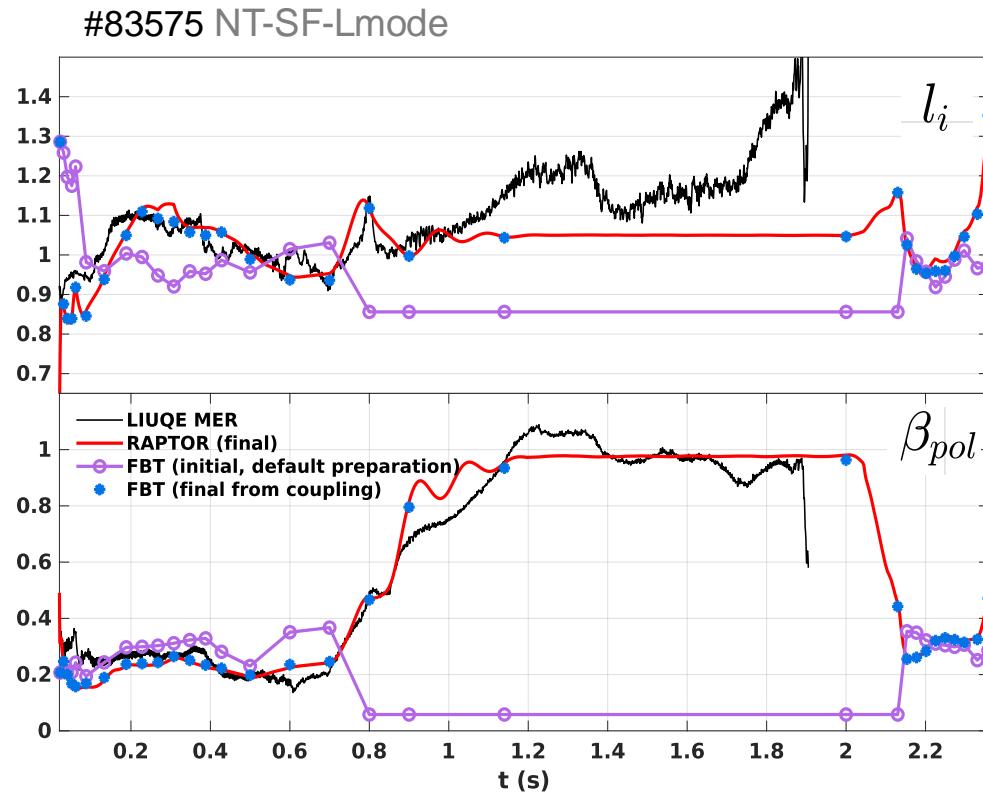


Shot prepared with FBT



Shot prepared with FBT-RAPTOR

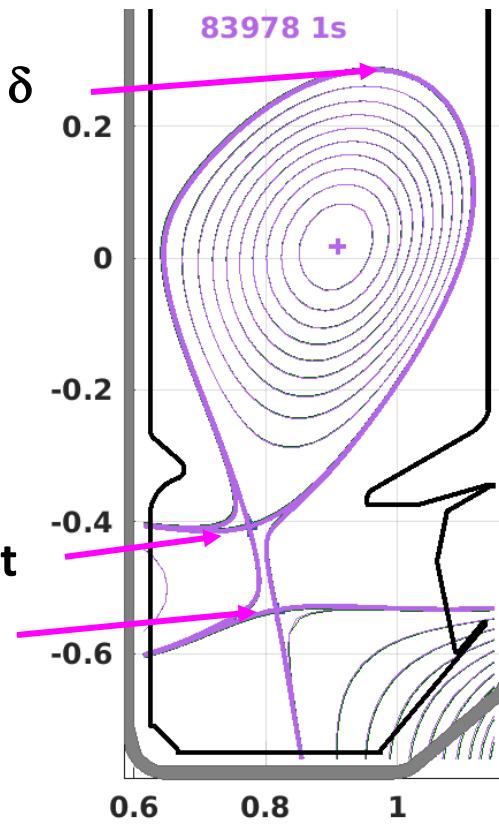
Application to a **Negative Triangularity** (NT) plasma with **Snowflake** (SF)

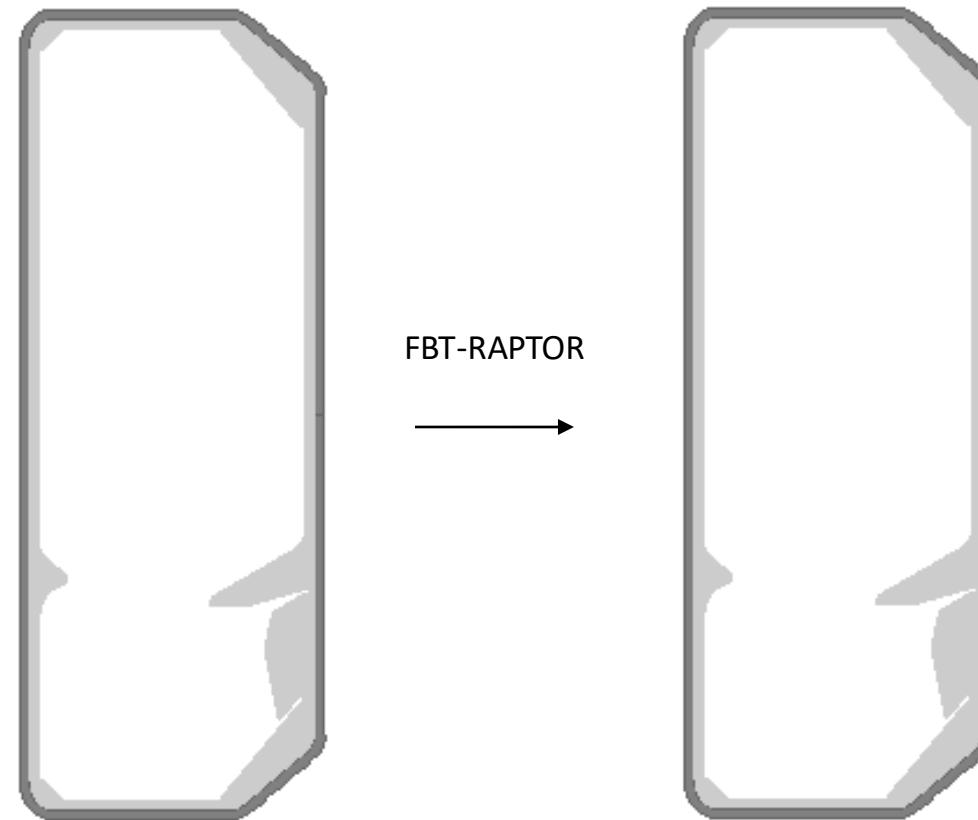


Top negative δ

Primary X-point

2nd X-point





- RAPTOR is a fast transport solver of 1D tokamak plasma profiles, designed for **real-time control** and inter-discharge **optimization**
- Coupling can be performed between a transport code and an equilibrium code to inform the Grad-Shafranov equilibrium with p' and TT' estimates
- **KEP**: coupling between an inverse equilibrium solver (FBT) and a predict-first transport simulator
- FBT-RAPTOR results successfully integrated into the TCV shot preparation system, showing a significant improvement of the shape

Questions?