

Electron Matter Interactions in Transmission Electron Microscopy PHYS-637

Week 1- Introduction

Course Schedule

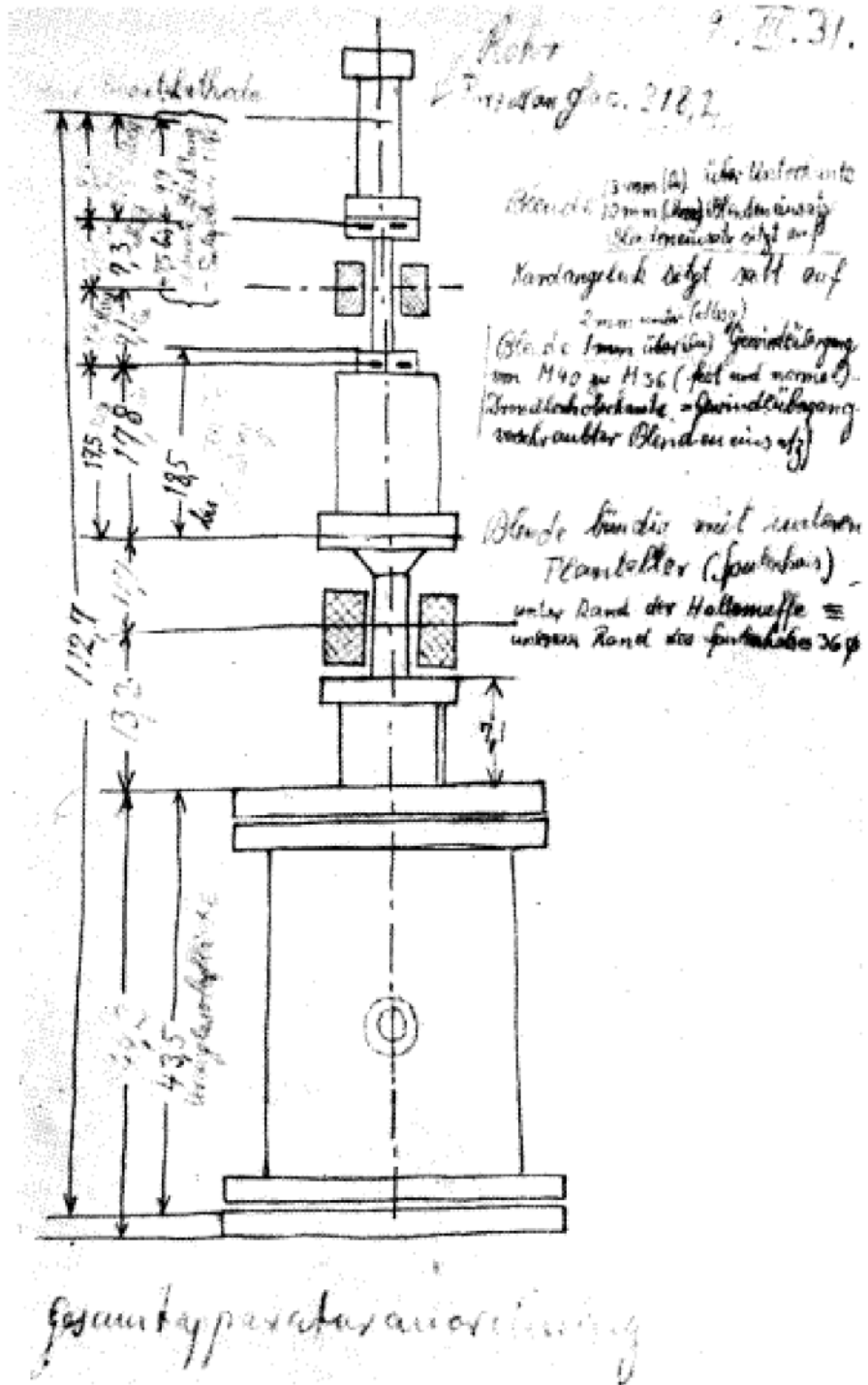
- **Week 1: Introduction (CH)**
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Week 1: Introduction

- A few words of history
- The Instrument
- Orders of magnitude
- Prerequisites: crystallography

History of TEM

- 1931: Knoll & Ruska build the first prototype
- 1933: The TEM surpasses the light microscope in resolution
- 1939: first commercial instrument
- 1986 E. Ruska is awarded the Nobel prize

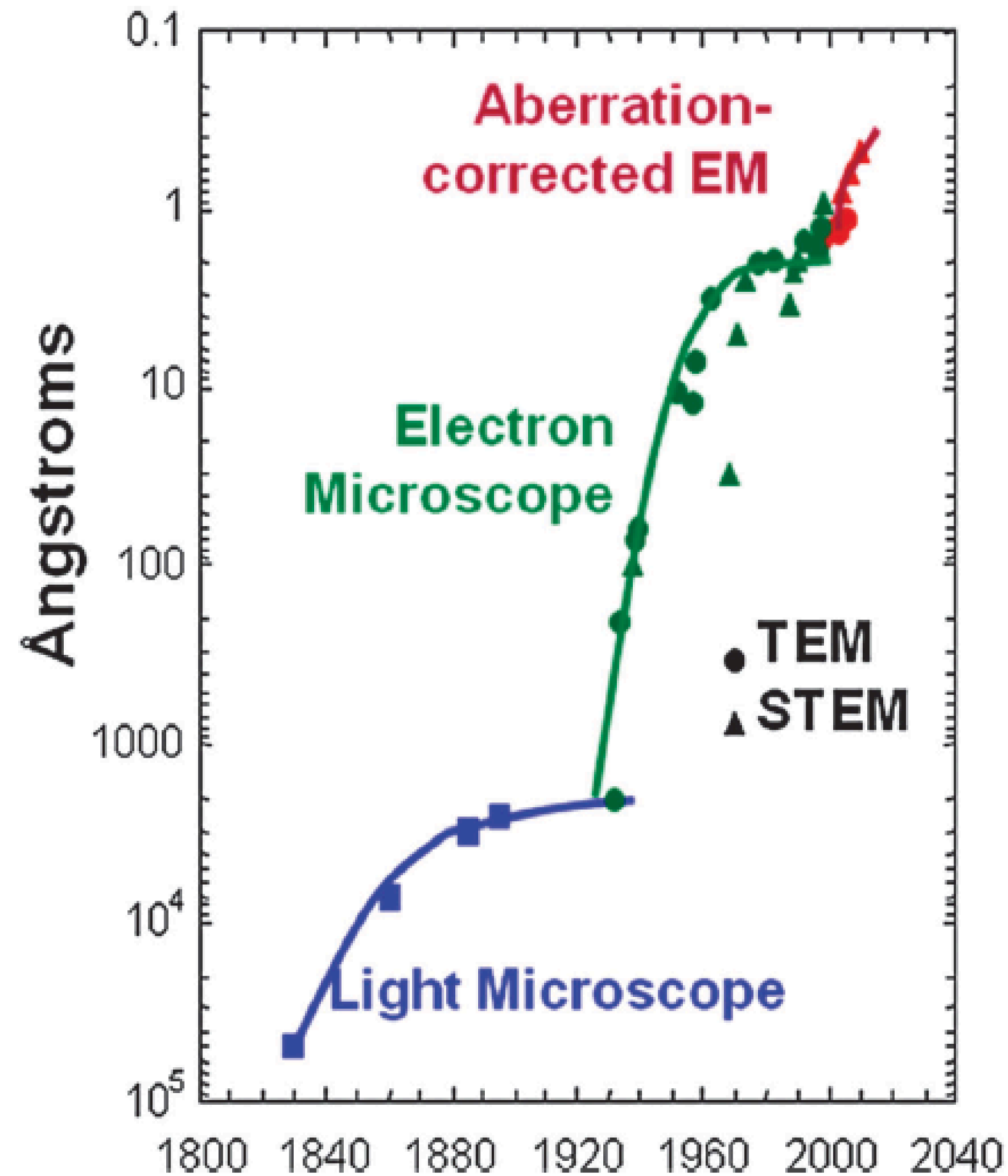


E. Ruska

Sketch of first TEM by Ruska, 1931

From [Nobel Lectures, Physics 1981-1990](#), Editor-in-Charge Tore Frängsmyr, Editor Gösta Ekspong, World Scientific Publishing Co., Singapore, 1993

History of TEM



- Abbe diffraction limit for the light microscope

$$d = \frac{\lambda}{2n\sin\theta}$$

- Equivalent for the electron microscope

$$d = \frac{1.2\lambda}{\sin\theta}$$

$$\lambda = 2.5 \cdot 10^{-12} \text{ m @ 200 kV;}$$

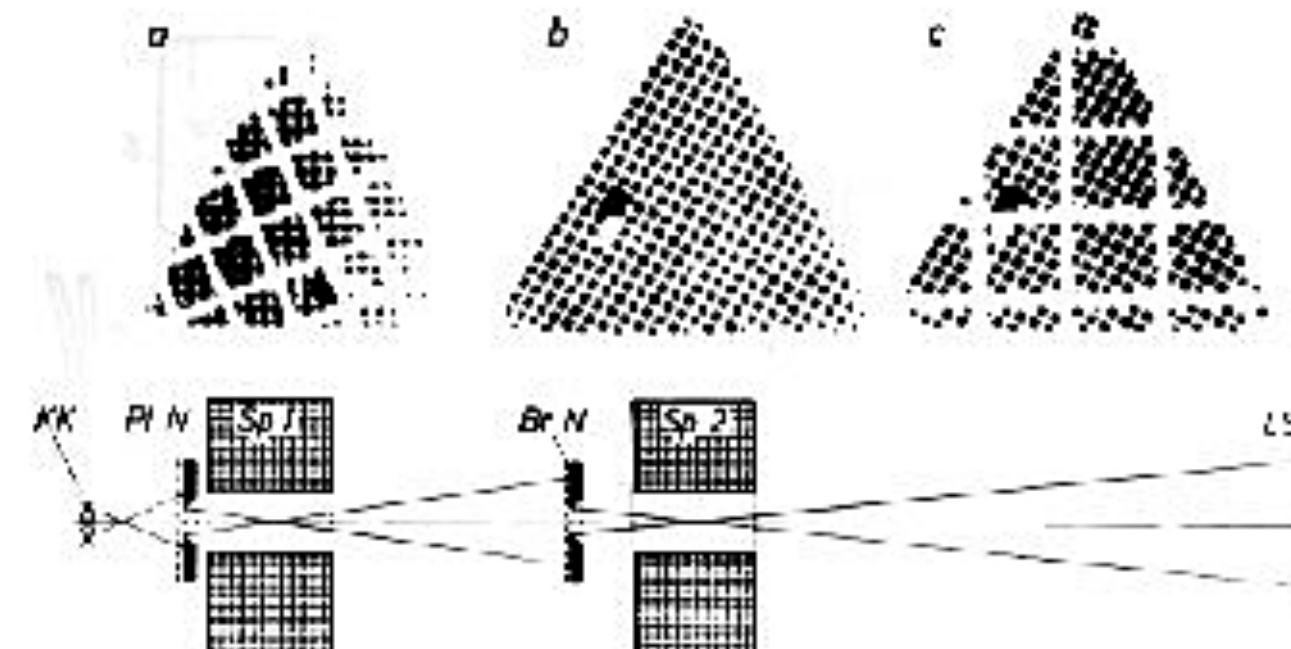
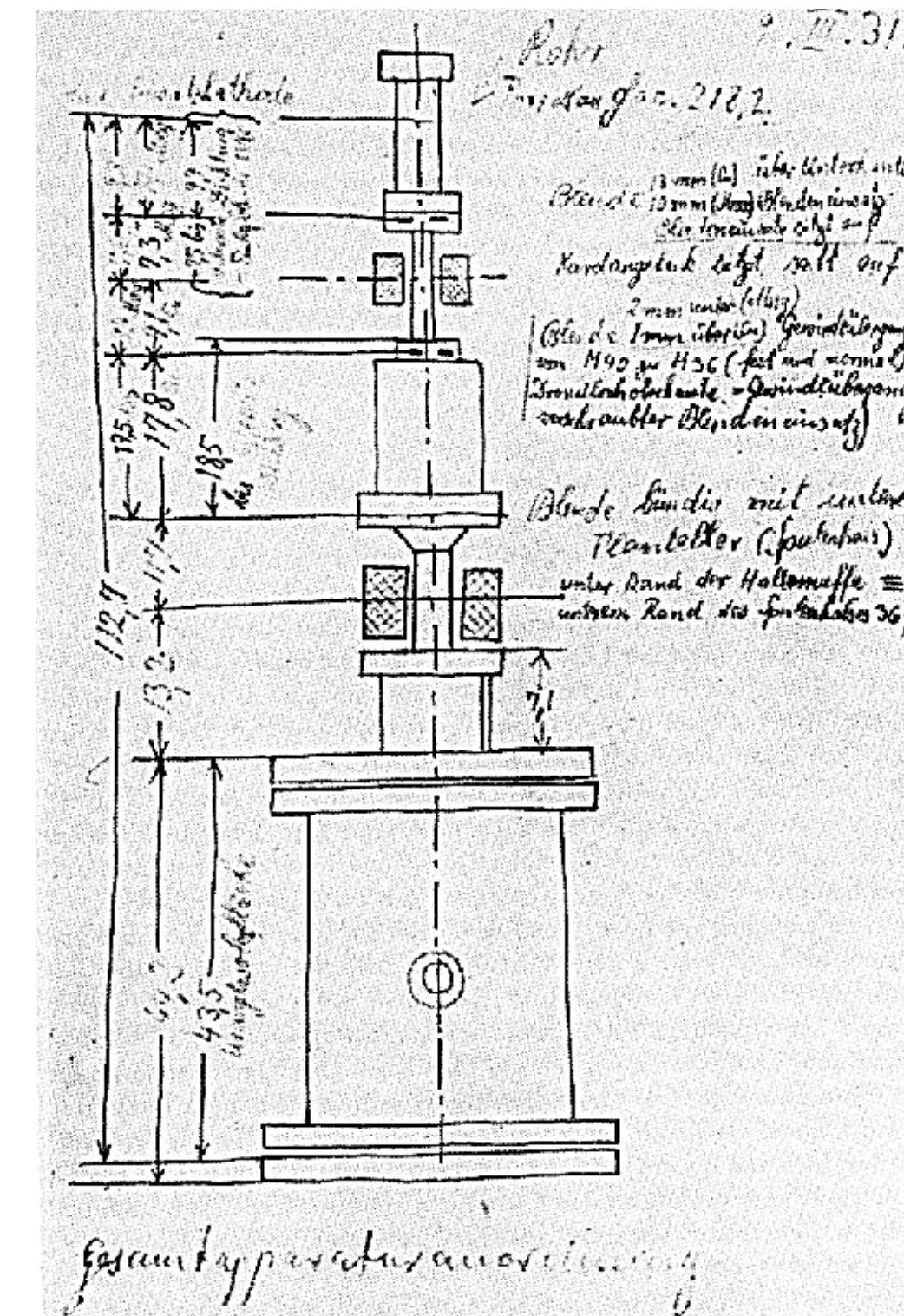
$$\theta \approx 10 - 20 \text{ mrad}$$

$$\Rightarrow d \text{ 1.5 to 3 \AA}$$

S. J. Pennycook & al., in: The Oxford Handbook of Nanoscience and Nanotechnology, ed. A. V. Narlikar and Y. Y. Fu, Oxford University Press, Oxford, United Kingdom, 2010, p. 205.

History of (corrected) TEM

- 1931: Ernst Ruska & Max Knoll invent the TEM



Hope... and disappointment

- Wavelength of electrons at 200 kV: 2.5 pm

Über einige Fehler von Elektronenlinsen.

Von **O. Scherzer** in Darmstadt.

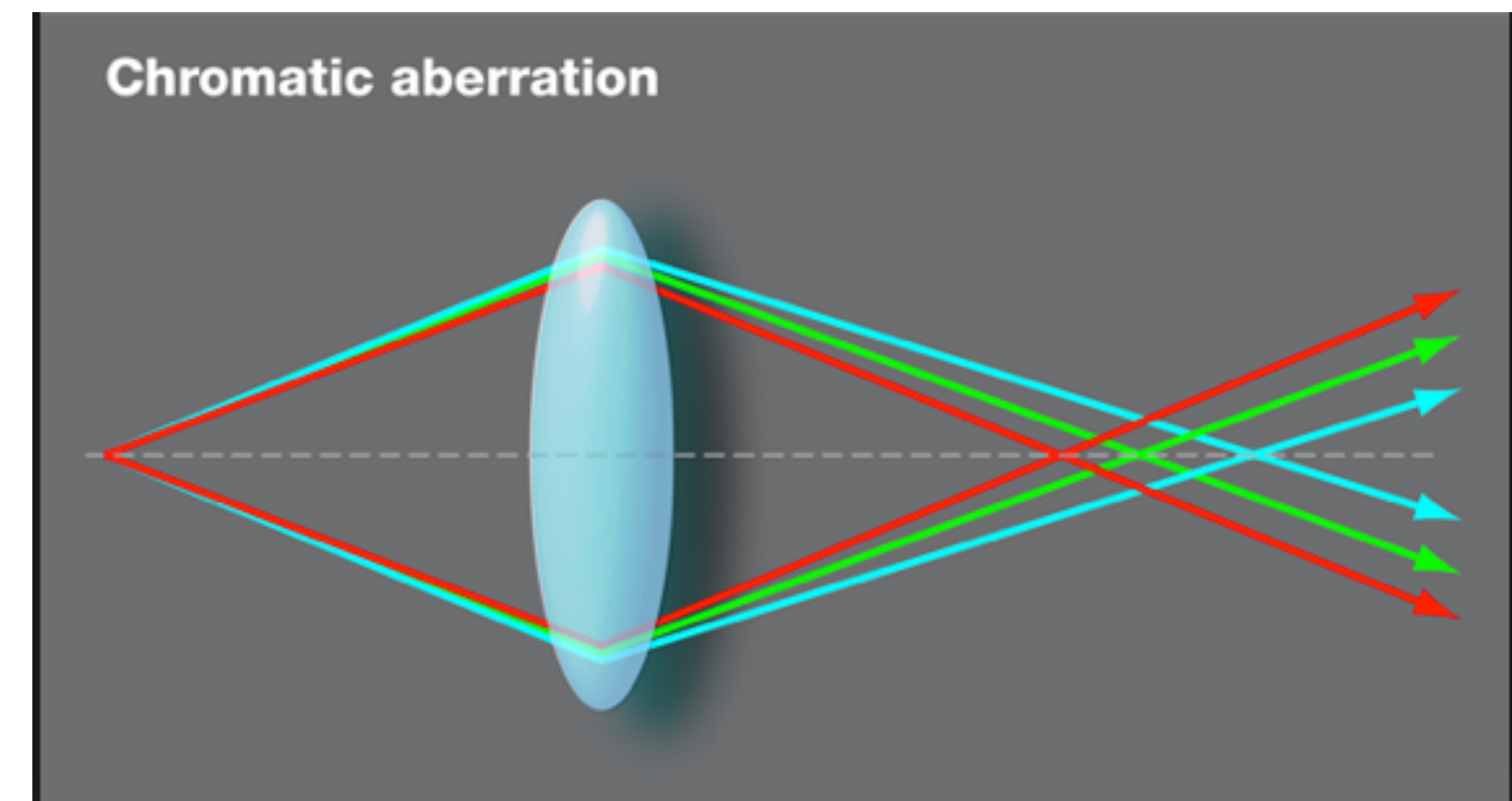
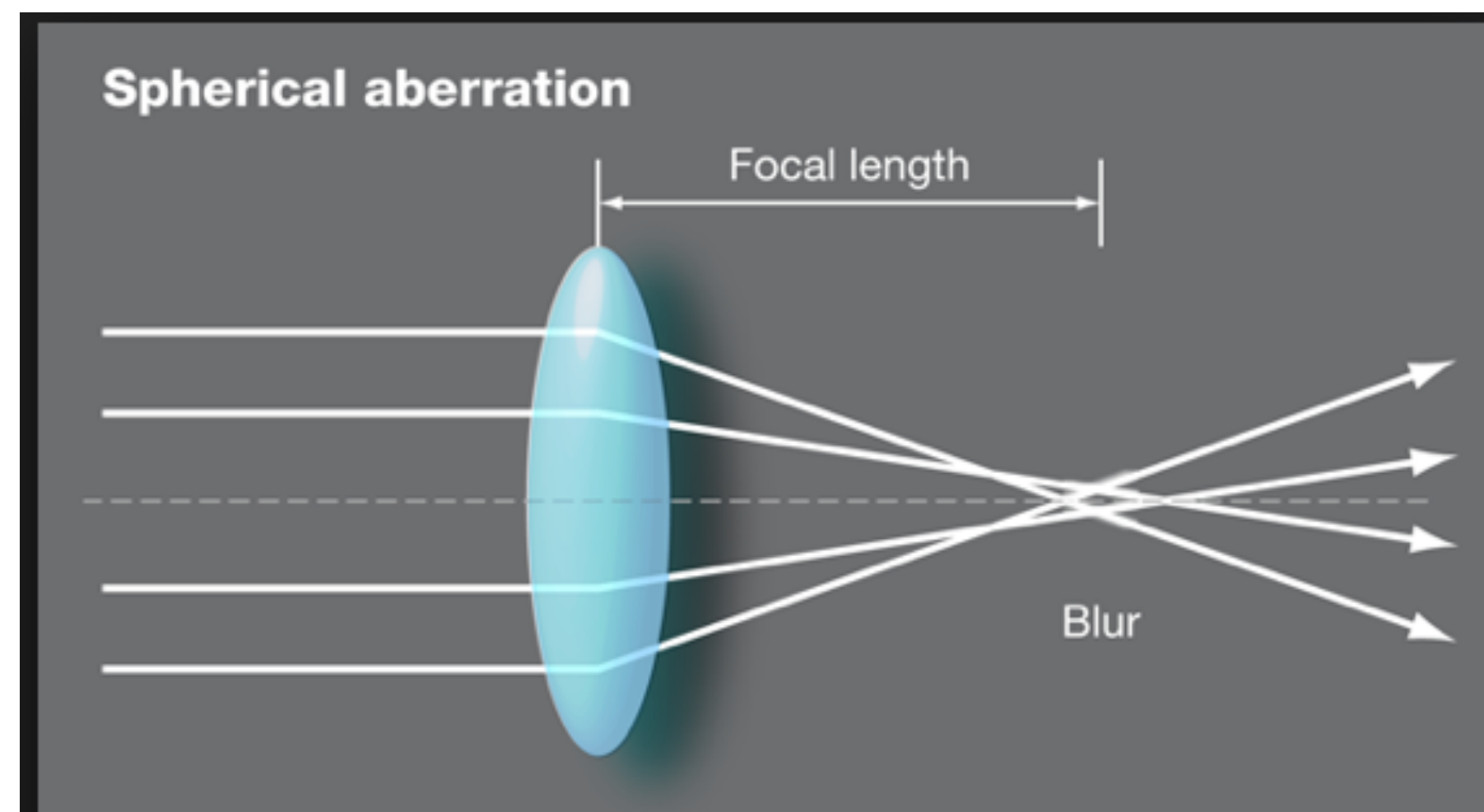
Mit 3 Abbildungen. (Eingegangen am 4. Juni 1936.)

Unmöglichkeit des Achromaten. Die Bildfehler dritter Ordnung. Unvermeidbarkeit der sphärischen Aberration.

Zusammenfassung. Chromatische und sphärische Aberration sind unvermeidbare Fehler der raumladungsfreien Elektronenlinse. Verzeichnung (Zerdehnung wie Zerdrehung) und (alle Arten von) Koma lassen sich prinzipiell beseitigen. Durch die Unvermeidbarkeit der sphärischen Aberration ist eine praktische, nicht aber eine prinzipielle Schranke für das Auflösungsvermögen der Elektronenmikroskope gegeben.

Aberration are the limitation

- Electron lenses with a cylindrical symmetry have a positive C_s and C_c coefficient



- 2 options:
 - 1 Correct the aberration of the TEM
 - 2 Design lenses with the smallest possible aberration & “correct the images”

2- design lenses with small Cs and Cc

- Small pole piece gap
- High tension
- “Straightforward” and successful route to HRTEM from 1931 to (very) late 90s
- Correct the image, not the TEM (image simulation; exit wave reconstruction)

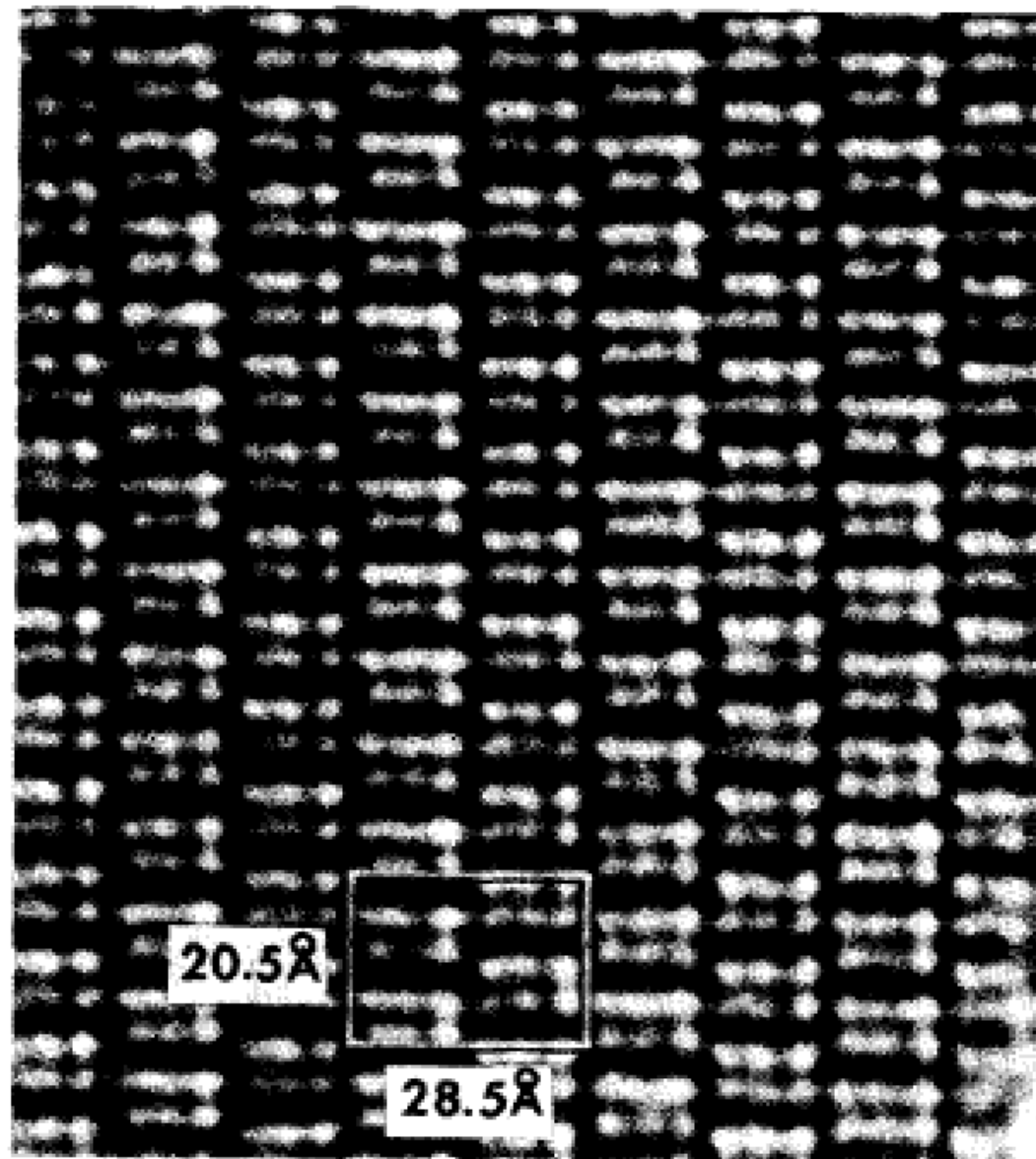
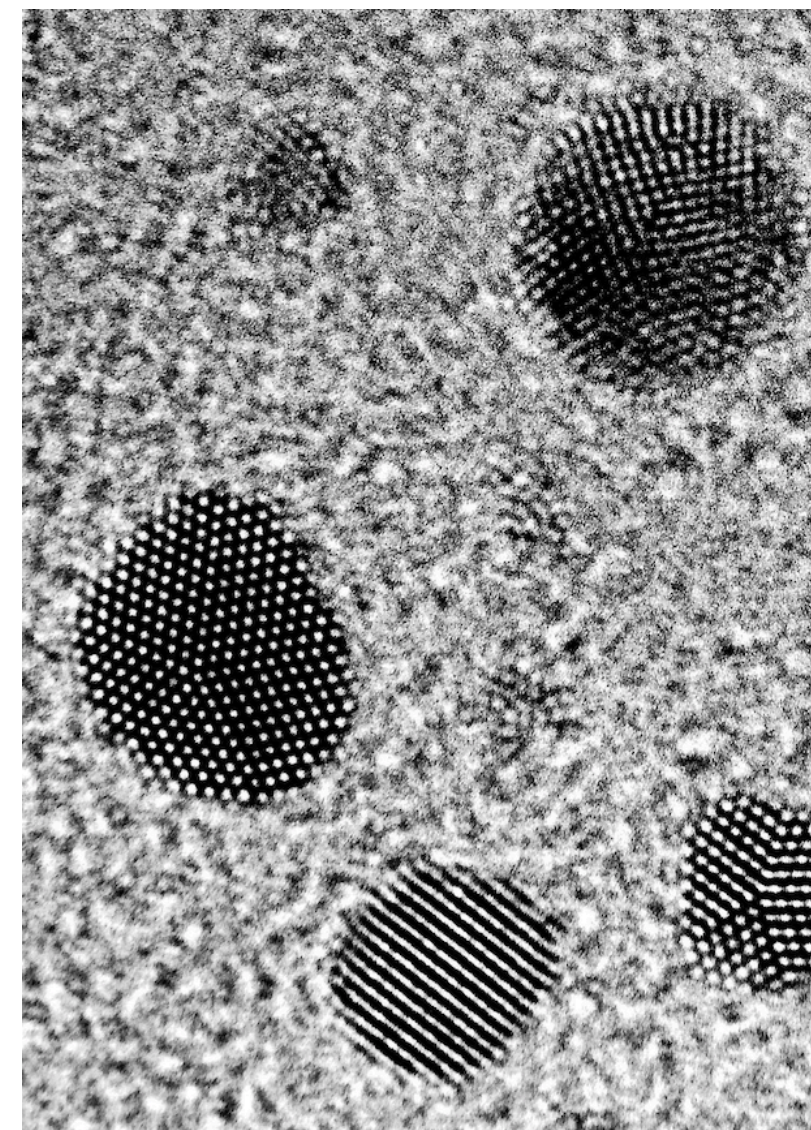
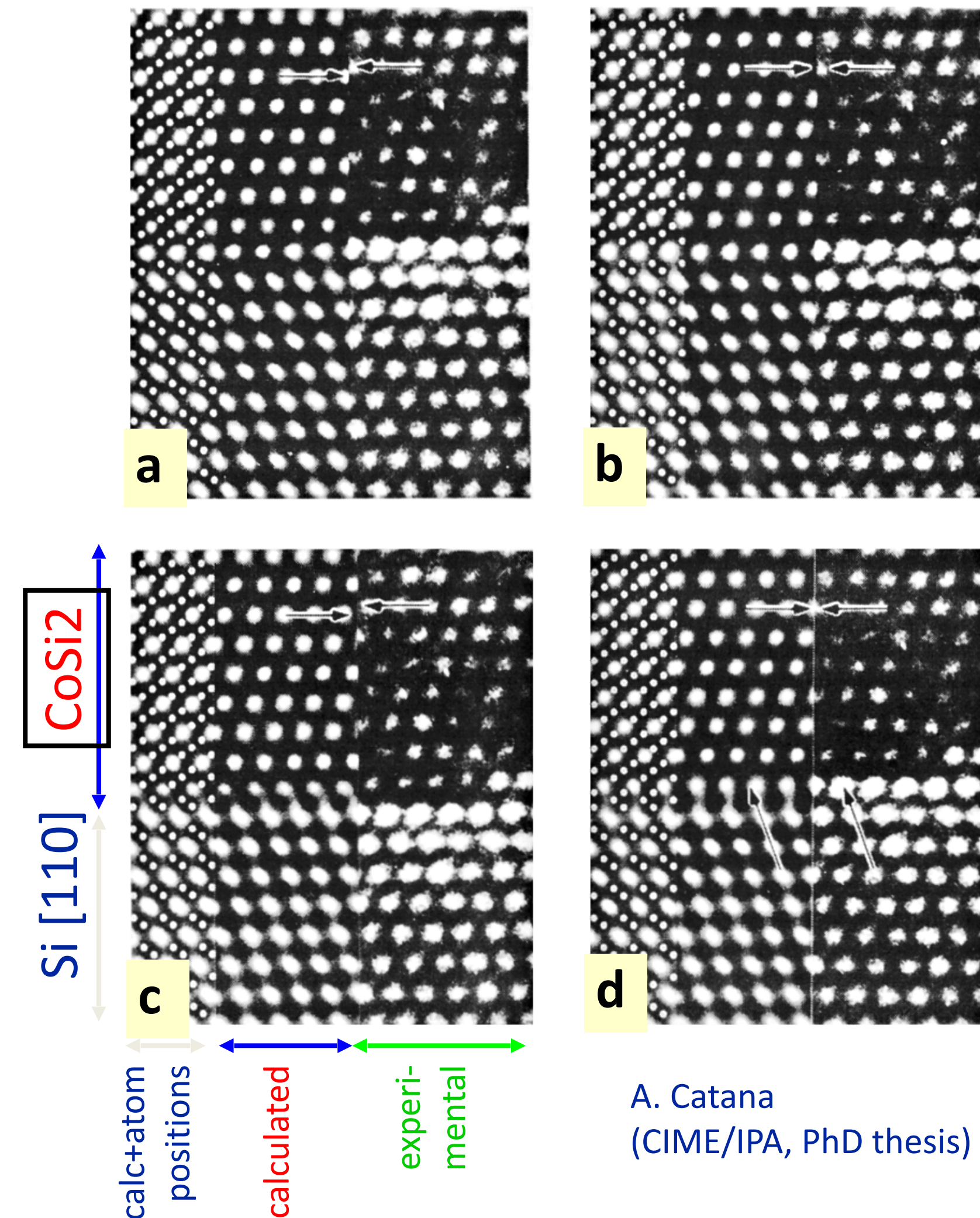


FIG. 1. Two-dimensional lattice image of orthorhombic $\text{Ti}_2\text{Nb}_{10}\text{O}_{29}$ obtained with electron beam incident parallel to the b axis. The unit cell projection is shown by white lines ($a = 28.5 \text{ \AA}$, $c = 20.5 \text{ \AA}$).

S. Iijima, APL, 1971



EM430@CIME: Au NPs, Flueli



A. Catana
(CIME/IPA, PhD thesis)

1- correct lens aberrations



Sphärische und chromatische Korrektur von Elektronen-Linsen.

Von O. Scherzer, z. Zt. USA.

(Aus den Süddeutschen Laboratorien in Mosbach.)

(Mit 7 Textabbildungen.)

Die Brauchbarkeit des Elektronenmikroskops bei hohen Vergrößerungen wird durch den Öffnungsfehler und die chromatische Aberration beeinträchtigt. Beide Fehler sind unvermeidlich, solange die abbildenden Felder rotations-symmetrisch, ladungsfrei und zeitlich konstant sind. Die vorliegende Untersuchung soll zeigen, daß die Aufhebung irgendeiner dieser drei Einschränkungen genügt, um den Weg zur sphärischen und chromatischen Korrektur und damit zu einer erheblichen Steigerung des Auflösungsvermögens freizugeben.

Solange nicht klar zu sehen ist, welche Art Linsen das beste Mikroskop ergibt, müssen alle sich bietenden Wege verfolgt werden. Es scheint daher angebracht, etwas ausführlicher auf die verschiedenen Arten korrigierter Linsen einzugehen.

Optik, 1947

One “just” need to relax one of the following constraint: cylindrical symmetry of the lens, permanent fields, no space charge.

1- correct lens aberrations

Aberration correction past and present

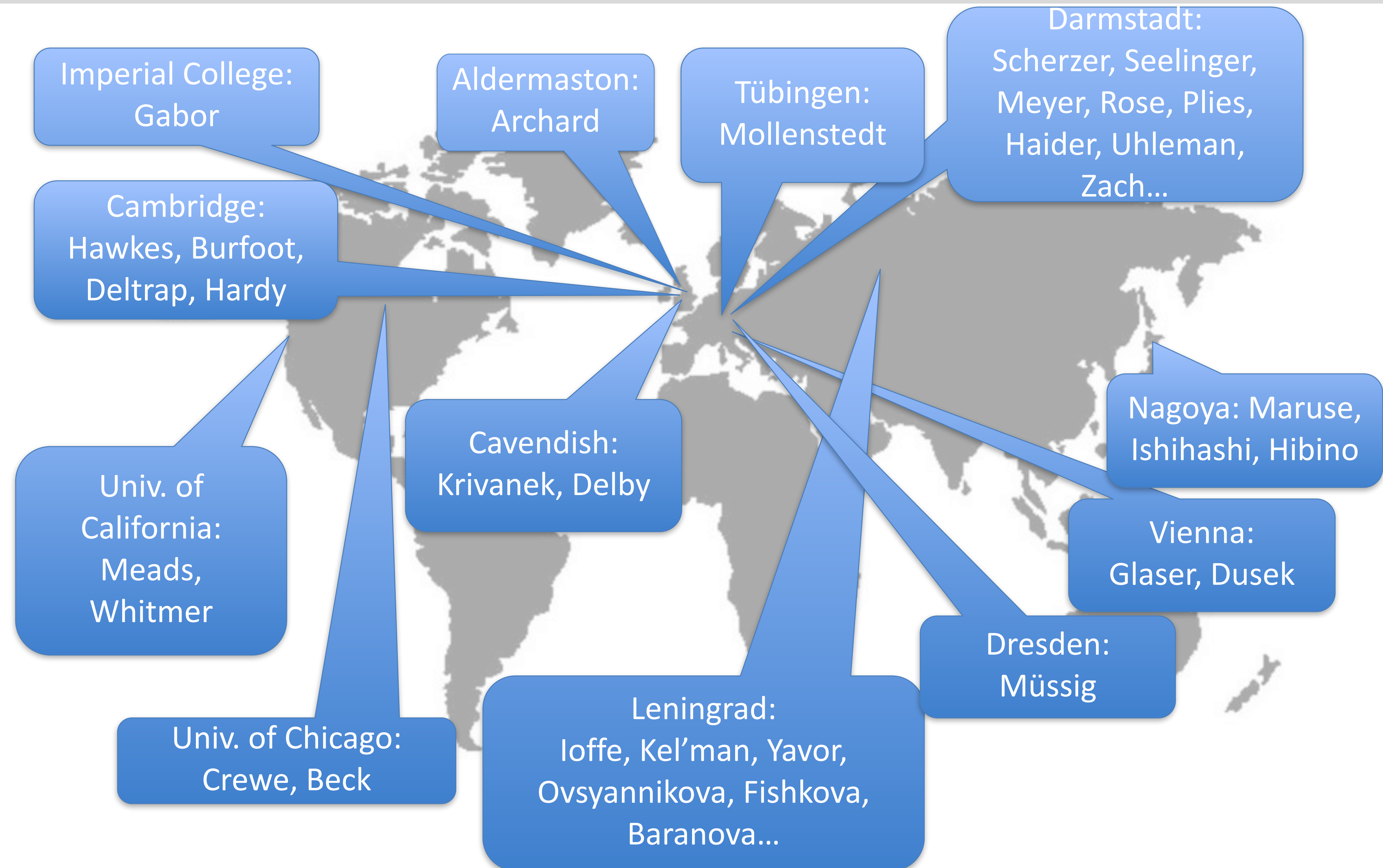
P. W. Hawkes

Phil. Trans. R. Soc. A 2009 **367**, doi: 10.1098/rsta.2009.0004, published 17 August 2009

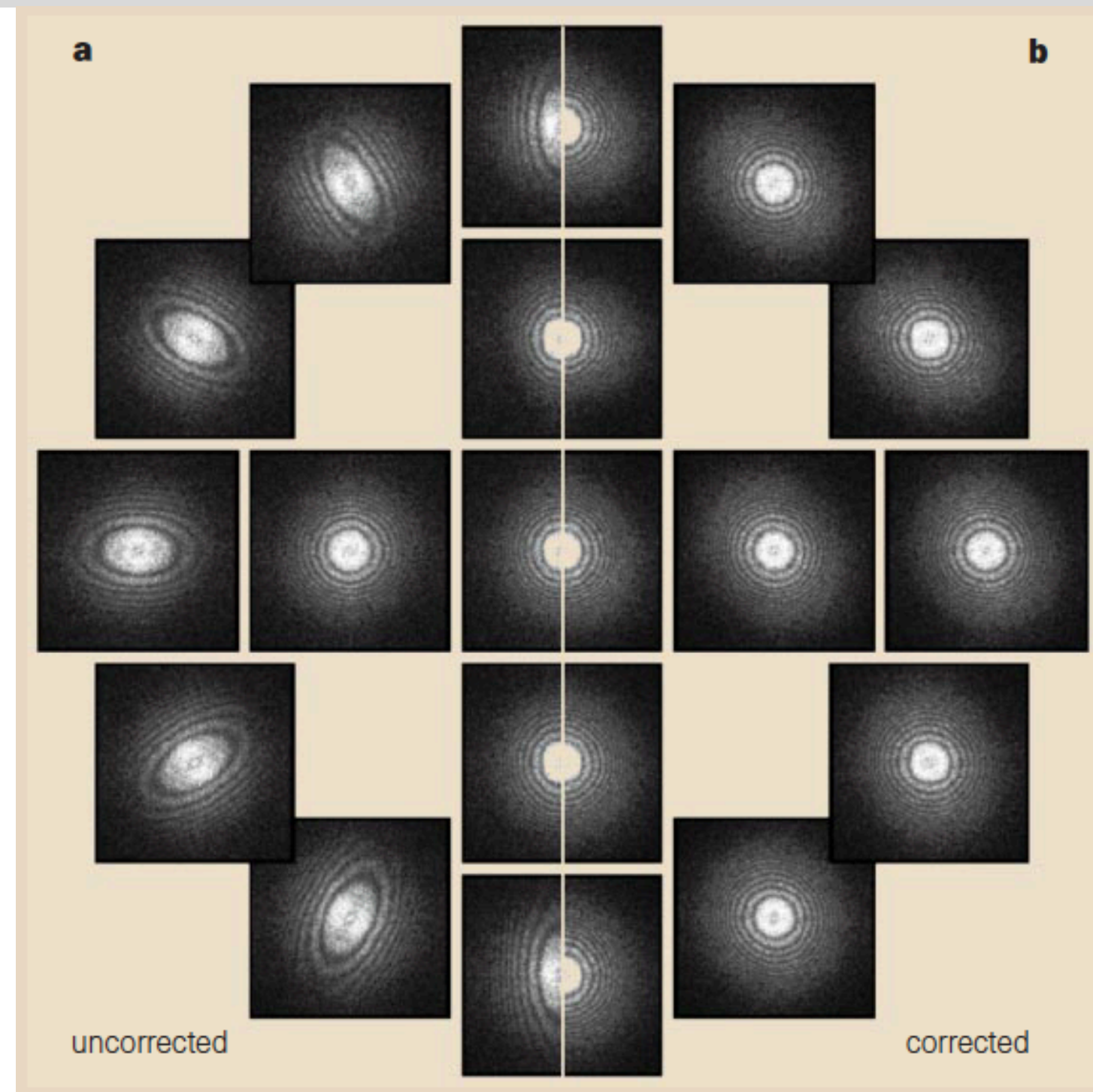
2. Forty disappointing years

During the next four decades, all of the four major families of correction methods attracted considerable attention. Here, we can only provide a representative selection; some other projects and the corresponding references are to be found in earlier surveys (Hawkes 1980, 2007, 2008; Hawkes & Kasper 1989, ch. 41; Rose 2008*a,b*).

“40 disappointing years”

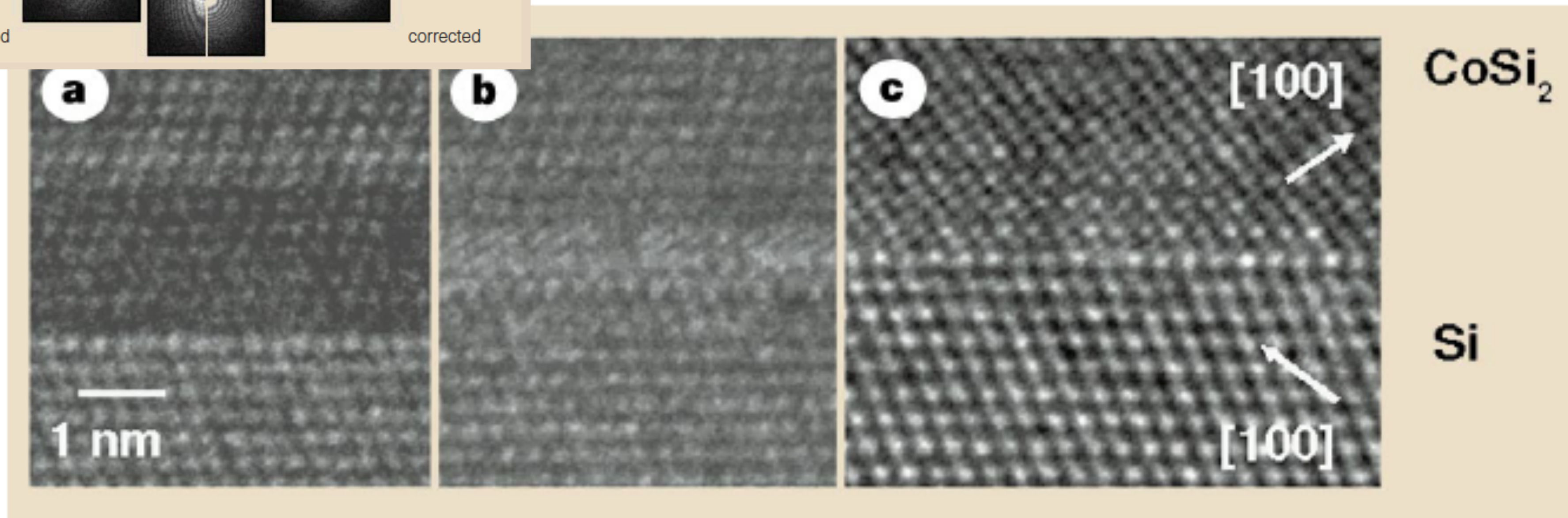


1997: Success



Haider, Uhlemann, Schwan, Rose, Kabius, Urban
Nature, 392 (1998), p. 268

Project funded by the Volkswagen Foundation

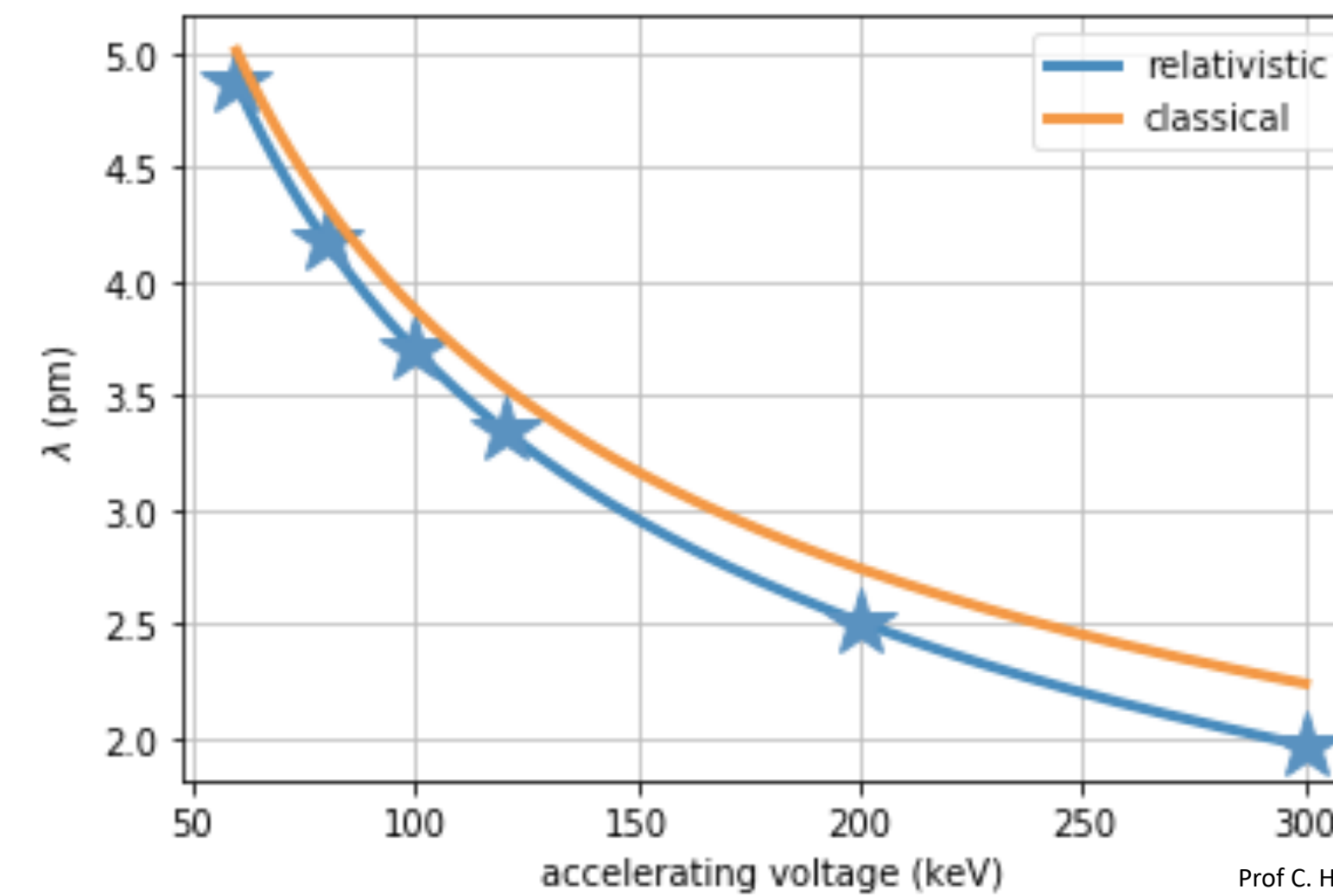
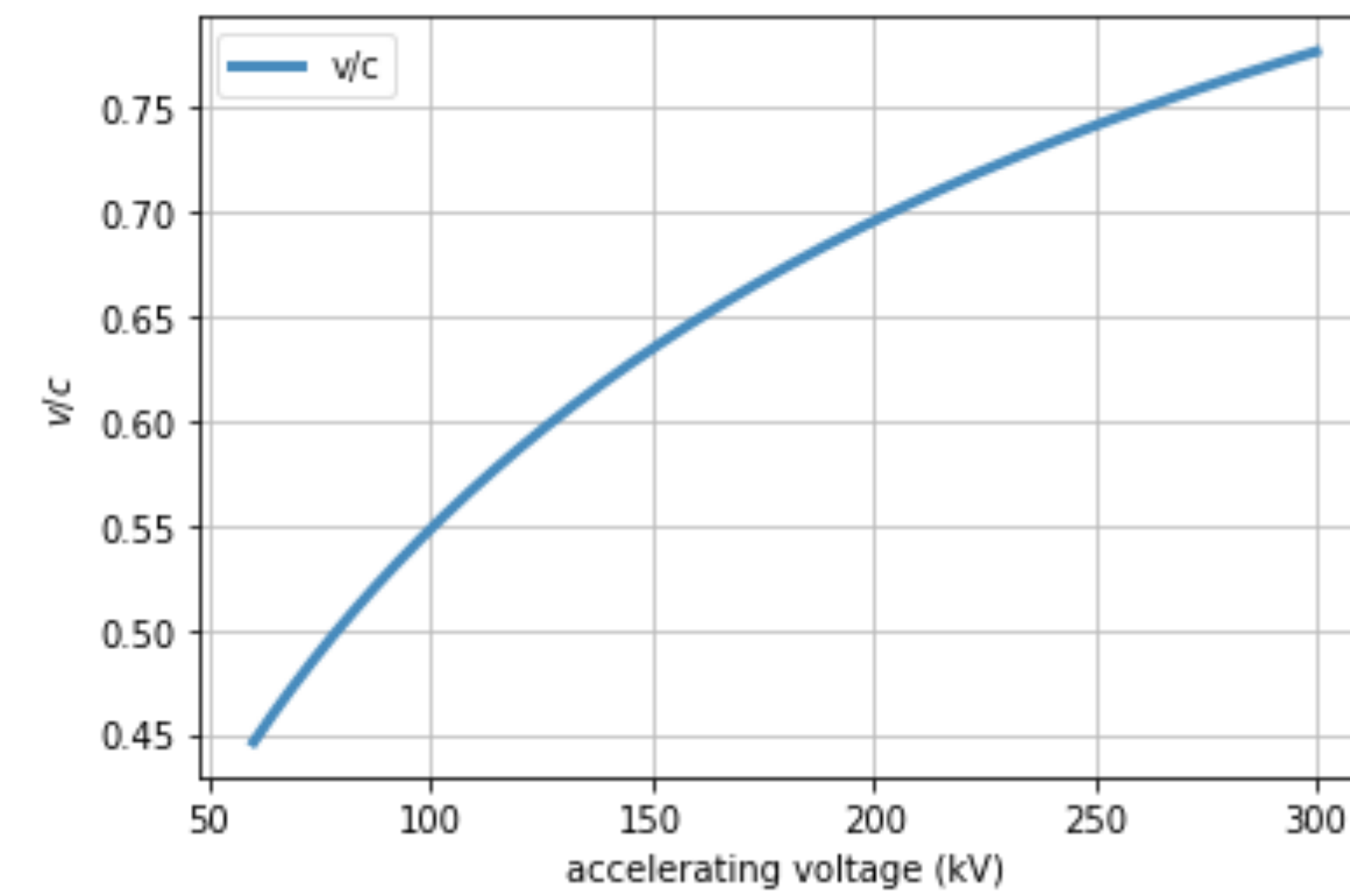


Presentation of the instrument



The electron source

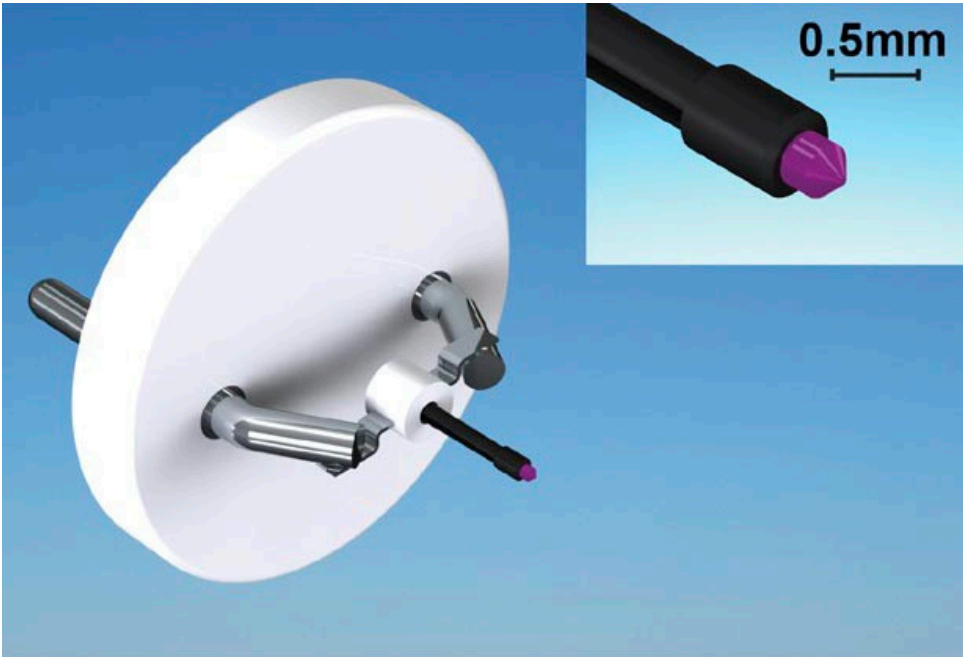
Typical high tensions: 60-300 kV





The electron source

Type of sources
Coherence; energy spread



	W	LaB ₆	Schottky	cold field emission
work function [eV]	4.5	2.7	2.5	4.5
emiss. current [μ A]	100	20-50	< 100	20
temperature[$^{\circ}$ C]	2500	< 1800	< 1500	20
brightness [$\text{A m}^{-2} \text{sr}^{-1}$]	10^9	$< 5 \cdot 10^{10}$	$< 10^{13}$	$5 \cdot 10^{12}$
crossover [μm]	50	10	0.02-0.05	≤ 0.01
energy width[eV]	1-3	0.5-2	0.3-0.8	0.2-0.7

The objective lens

- Aberration
- Contrast transfer function
- magnification

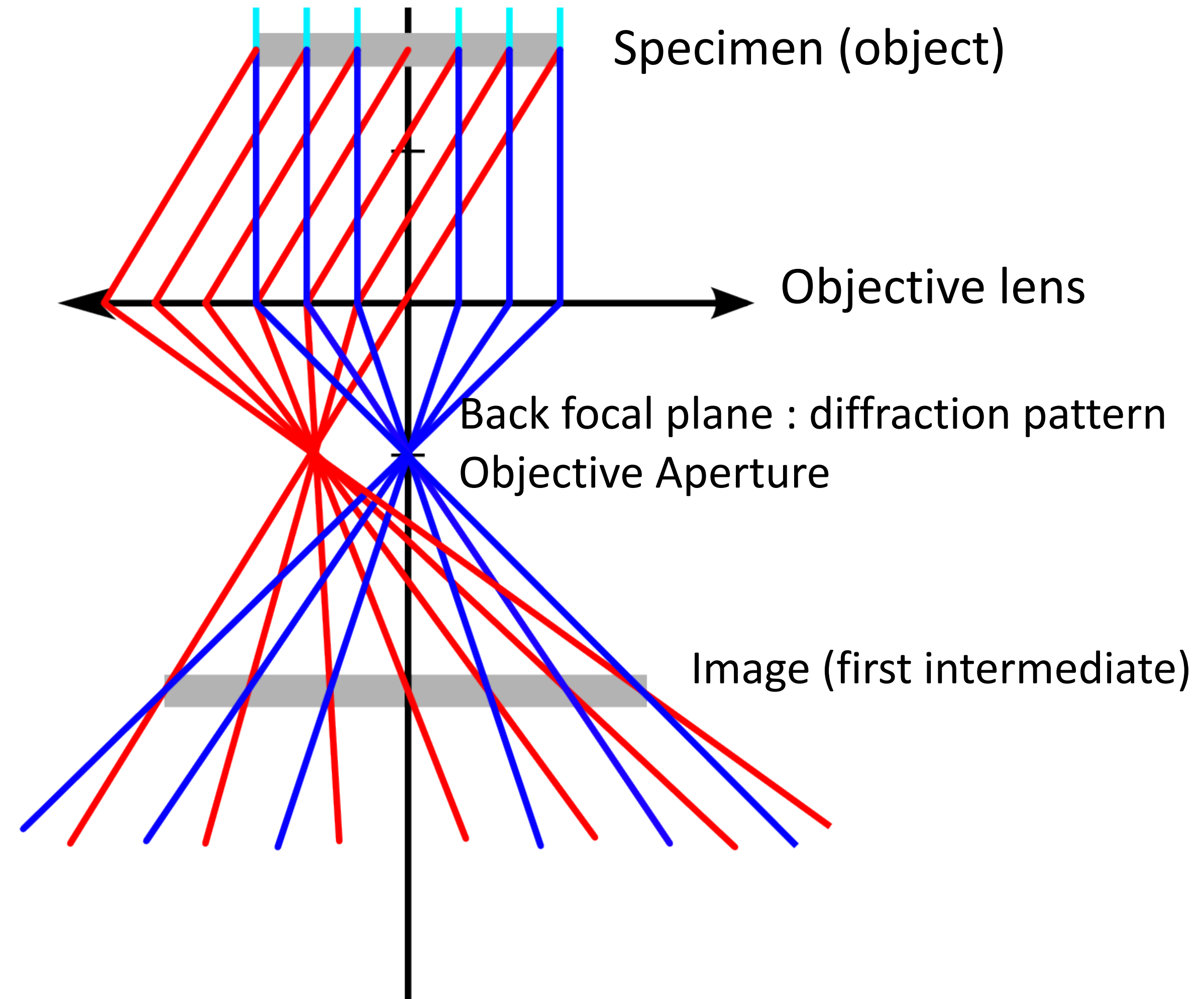
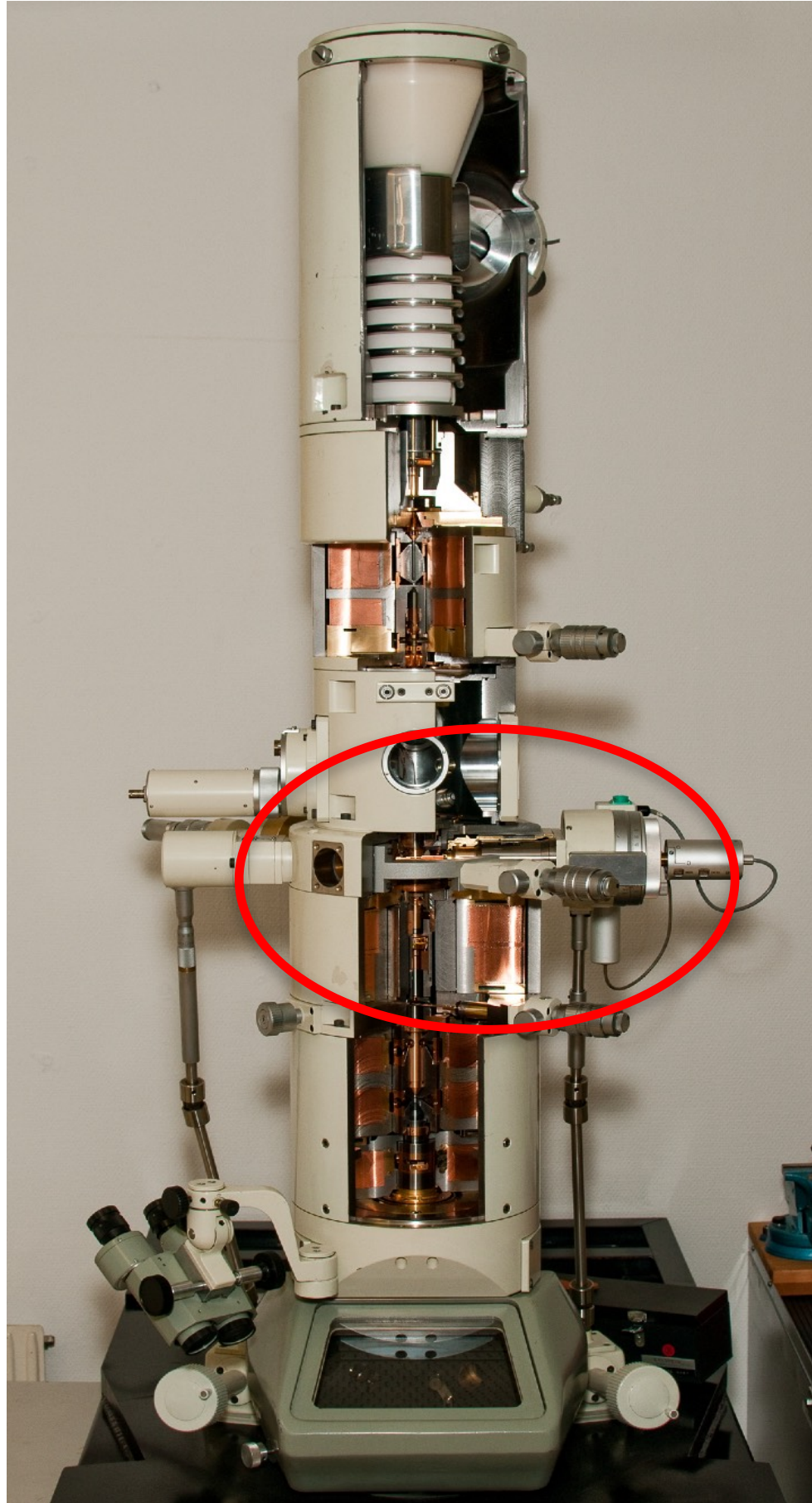


The intermediate and projector lenses

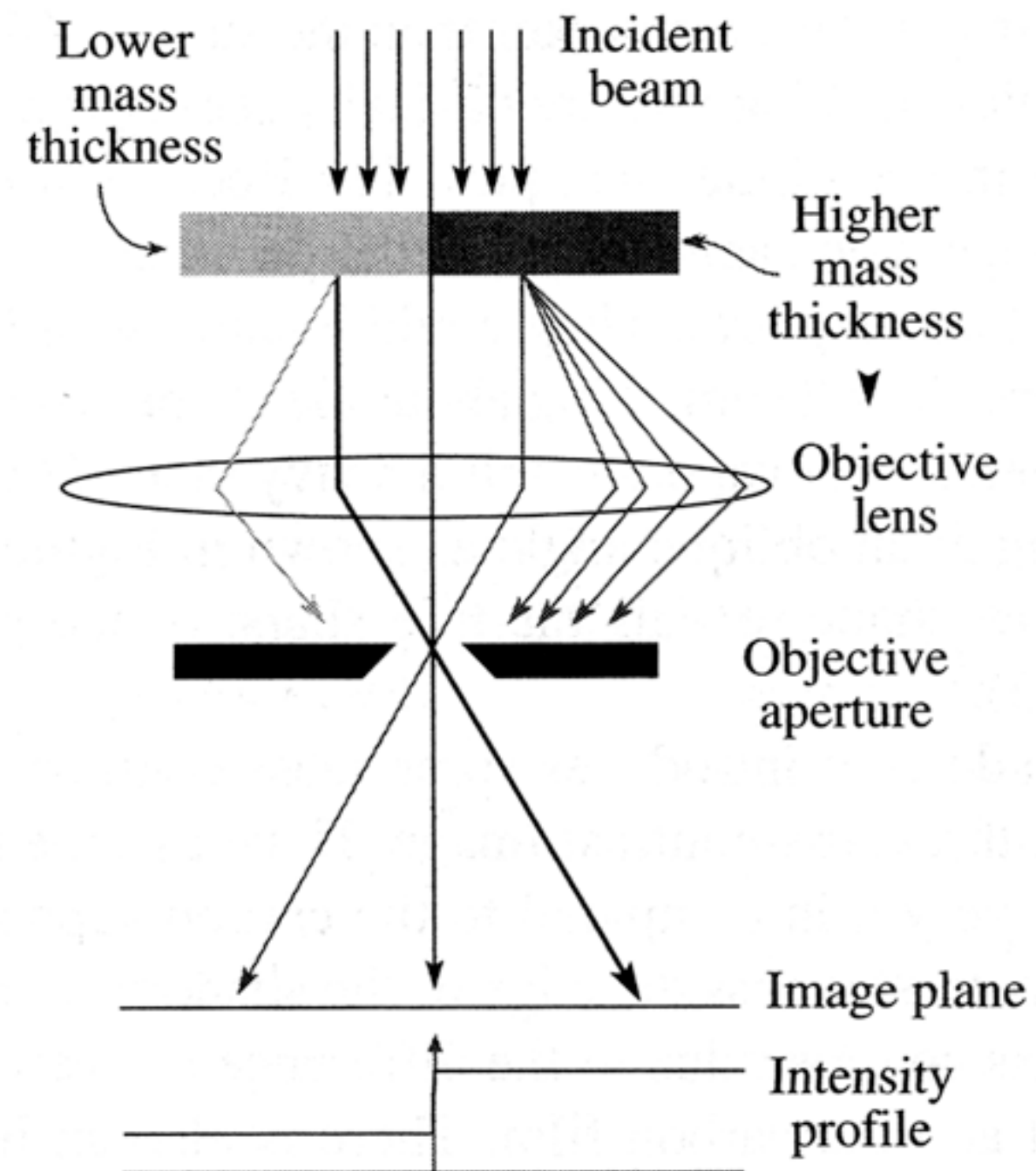
- Further magnification
- Switch between imaging and diffraction



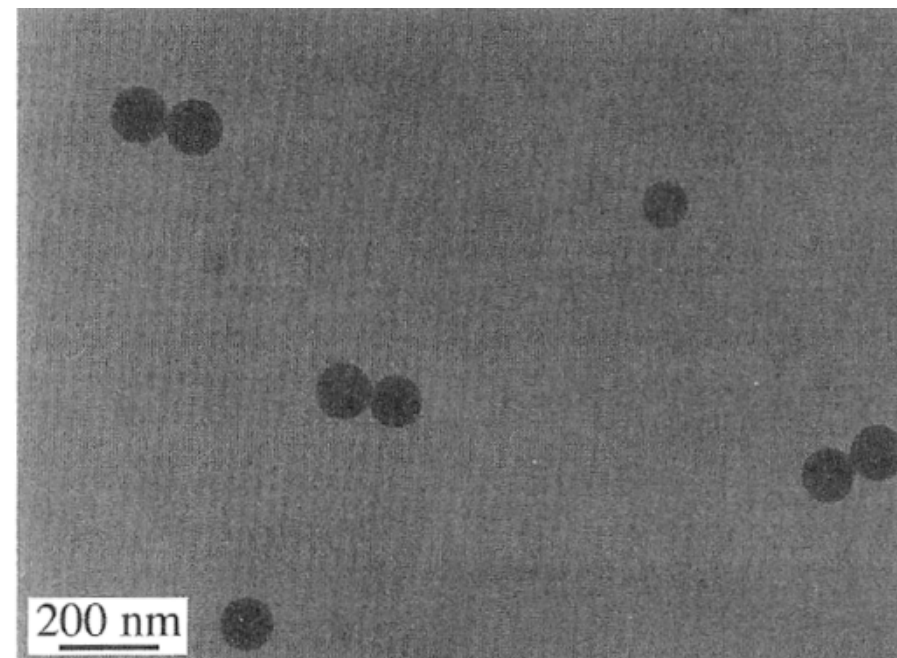
The type of contrasts



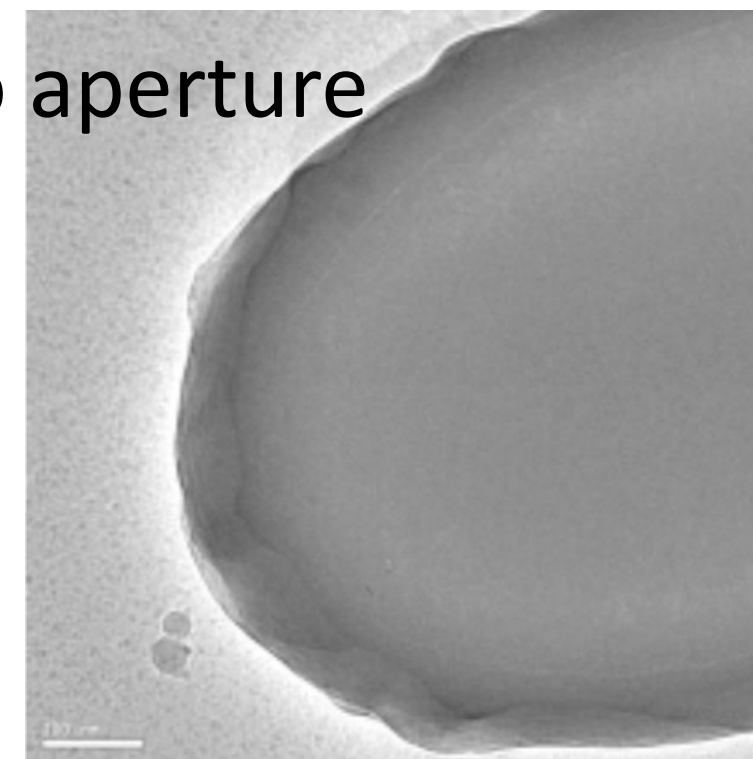
TEM mass-thickness contrast



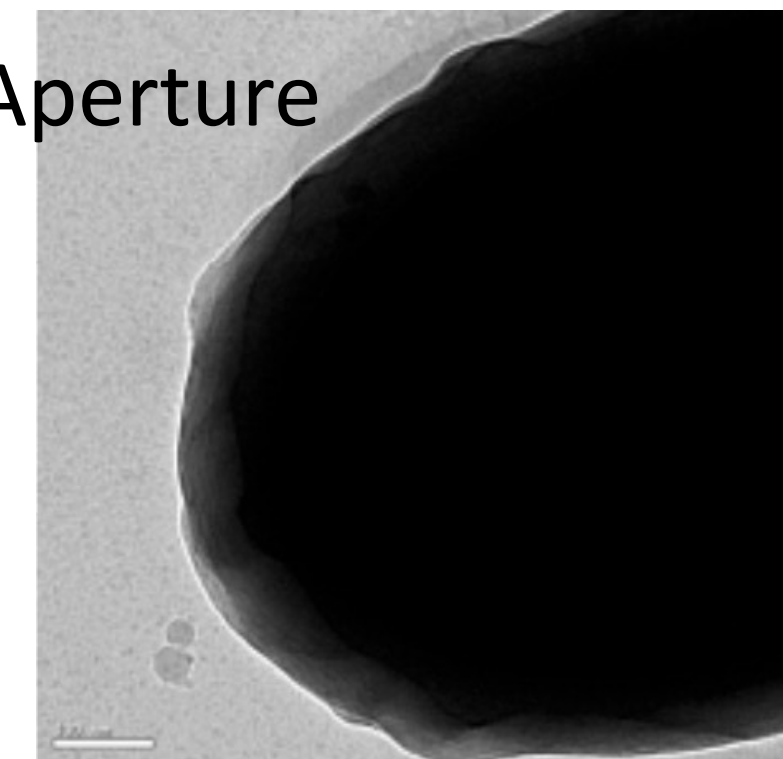
- Areas of higher mass thickness scatter electrons more than others
- Electrons are captured by the aperture and lost from the beam path
- Areas of higher mass thickness will therefore appear dark in the image
- This is known as
 - mass thickness contrast,
 - scattering contrast,
 - aperture contrast or
 - amplitude contrast!



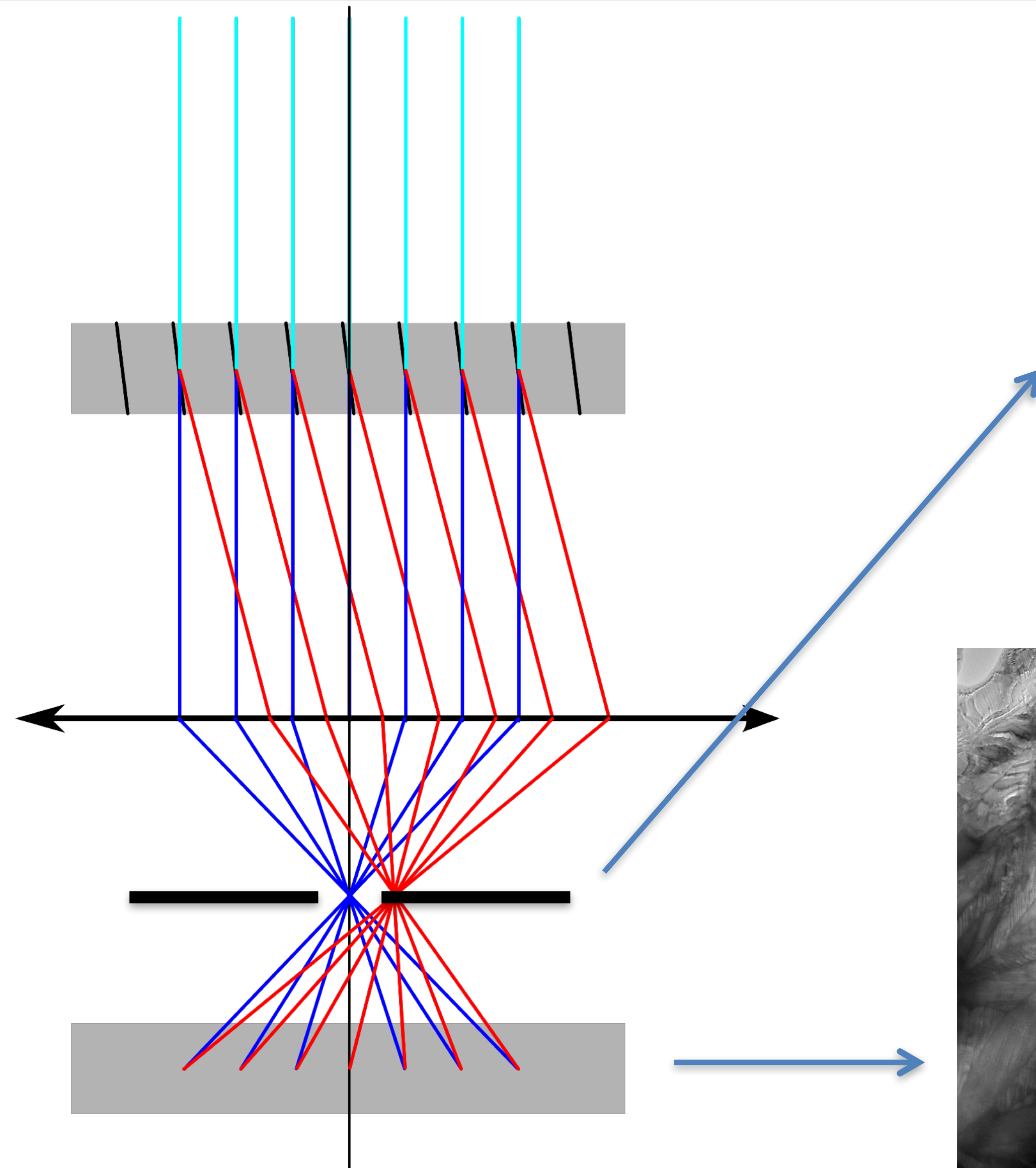
No aperture



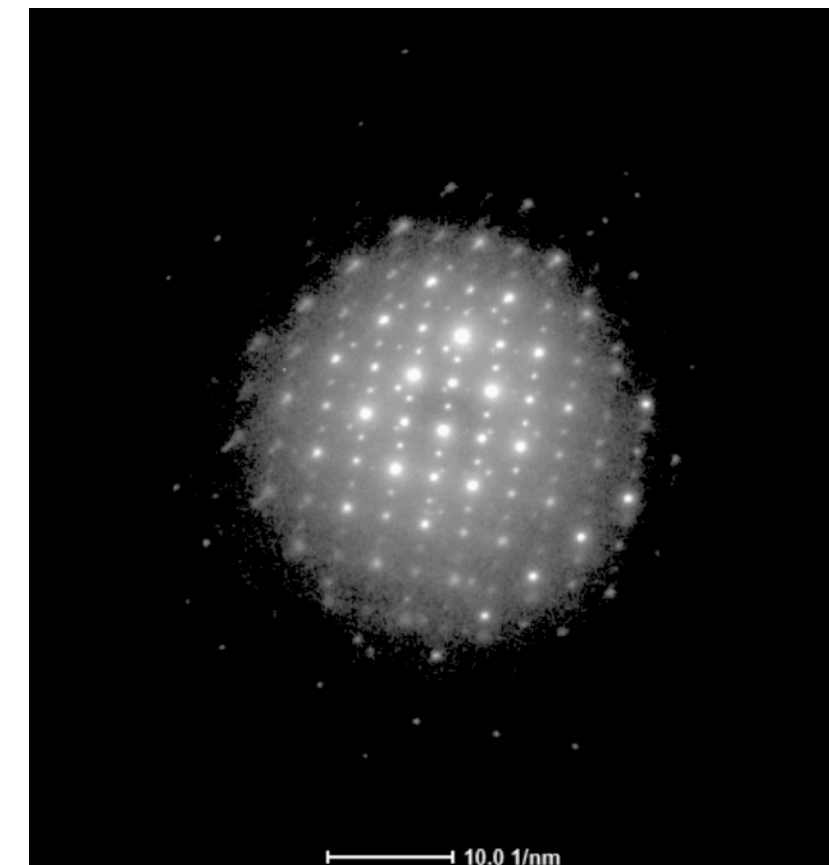
Aperture



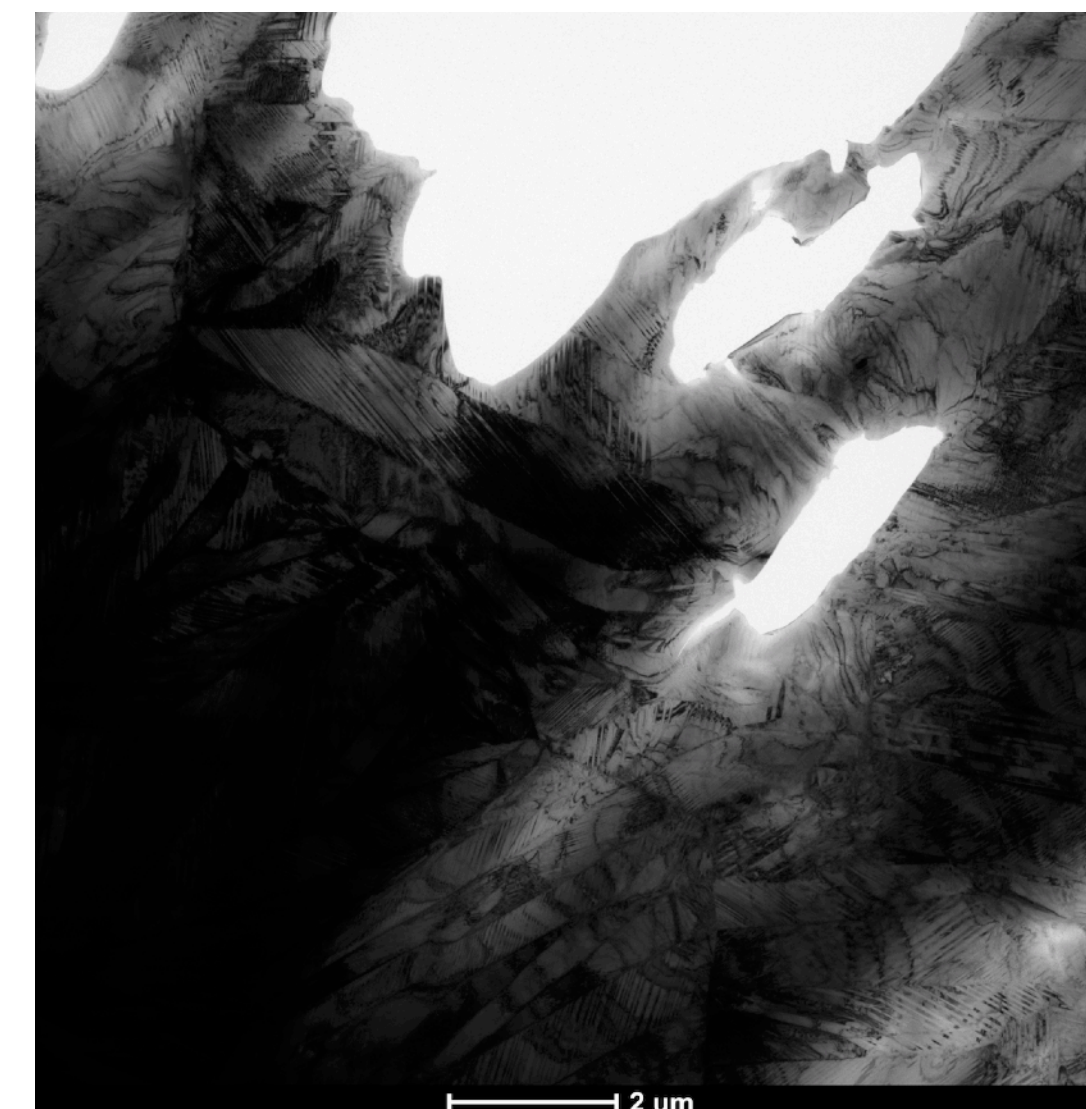
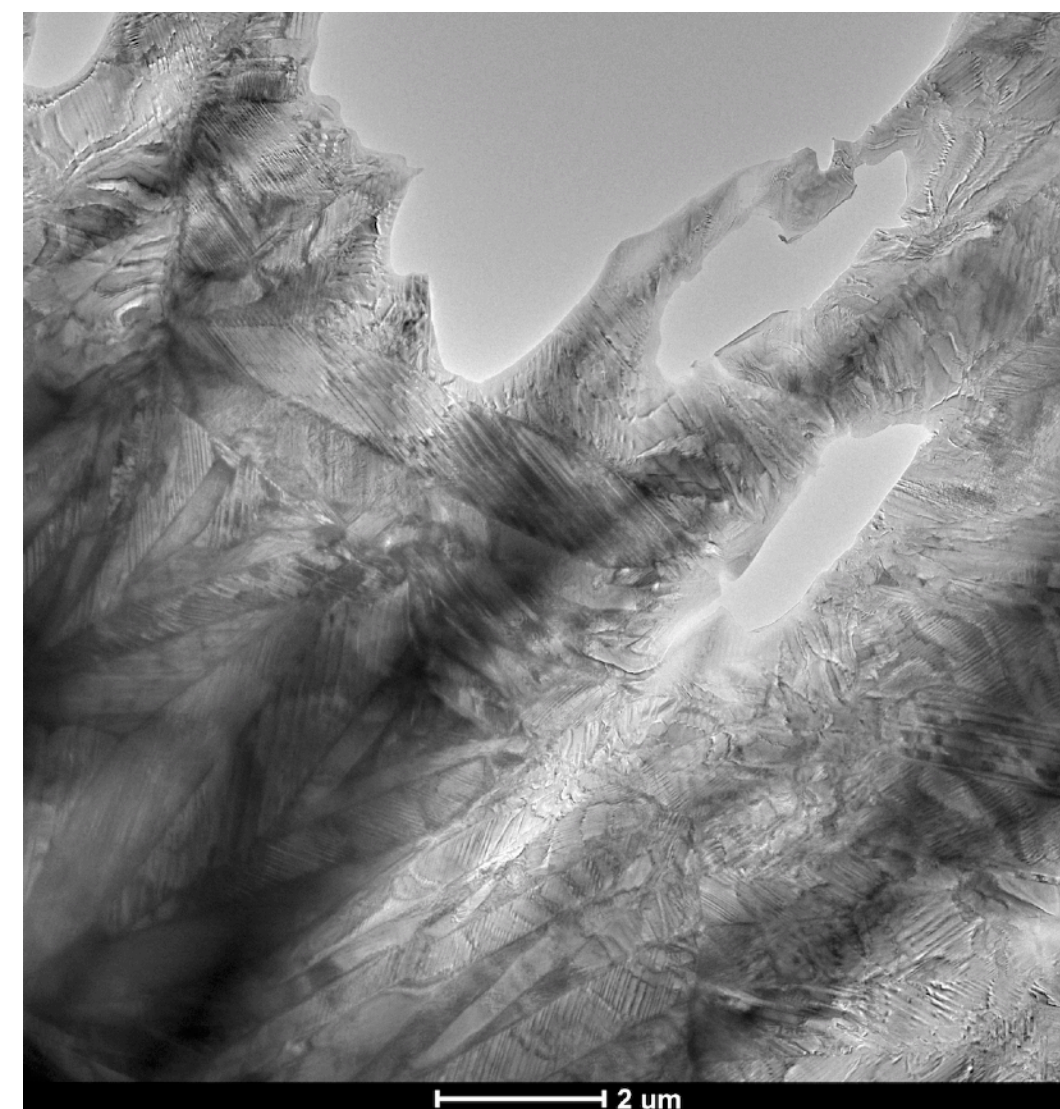
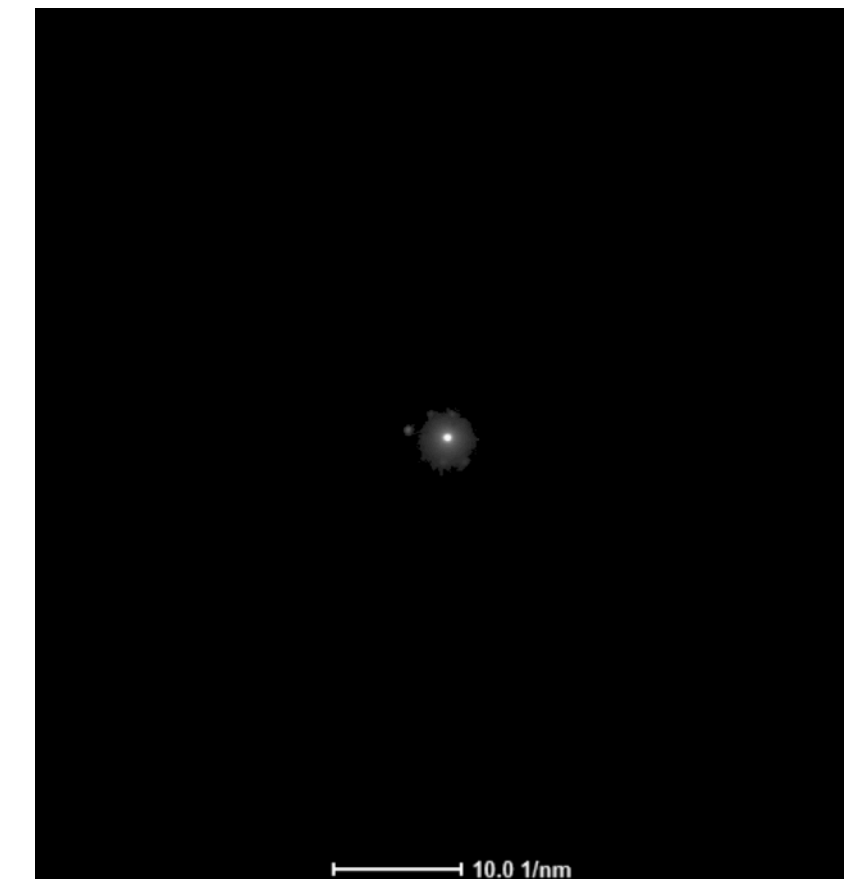
Diffraction contrast



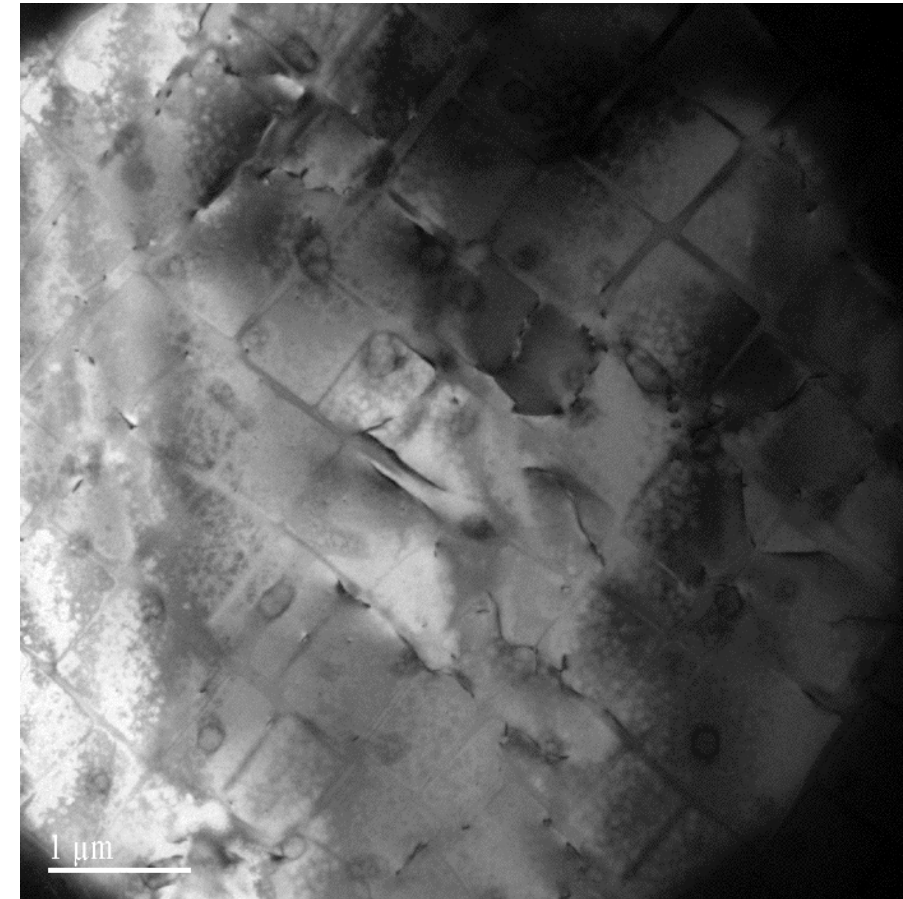
No aperture



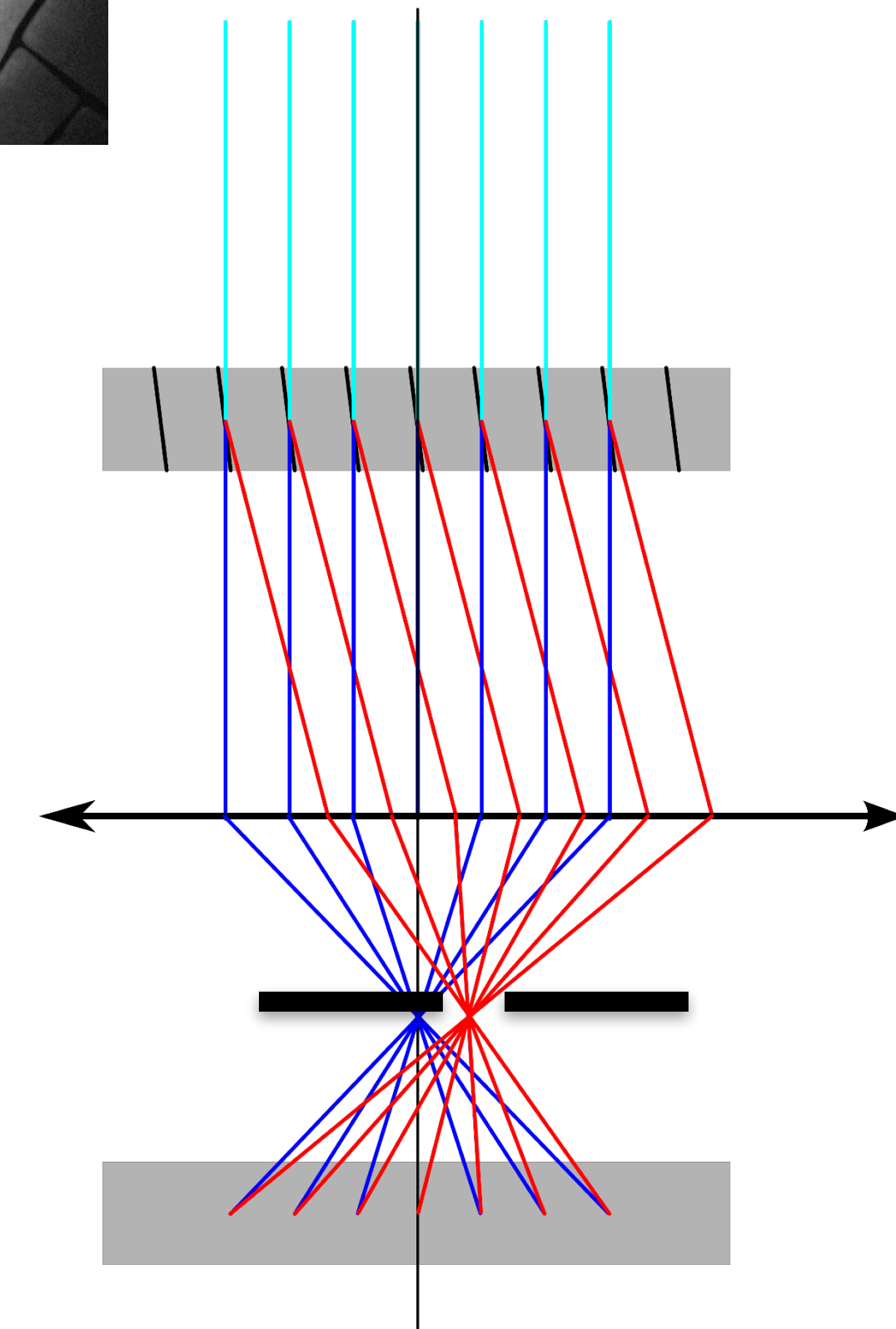
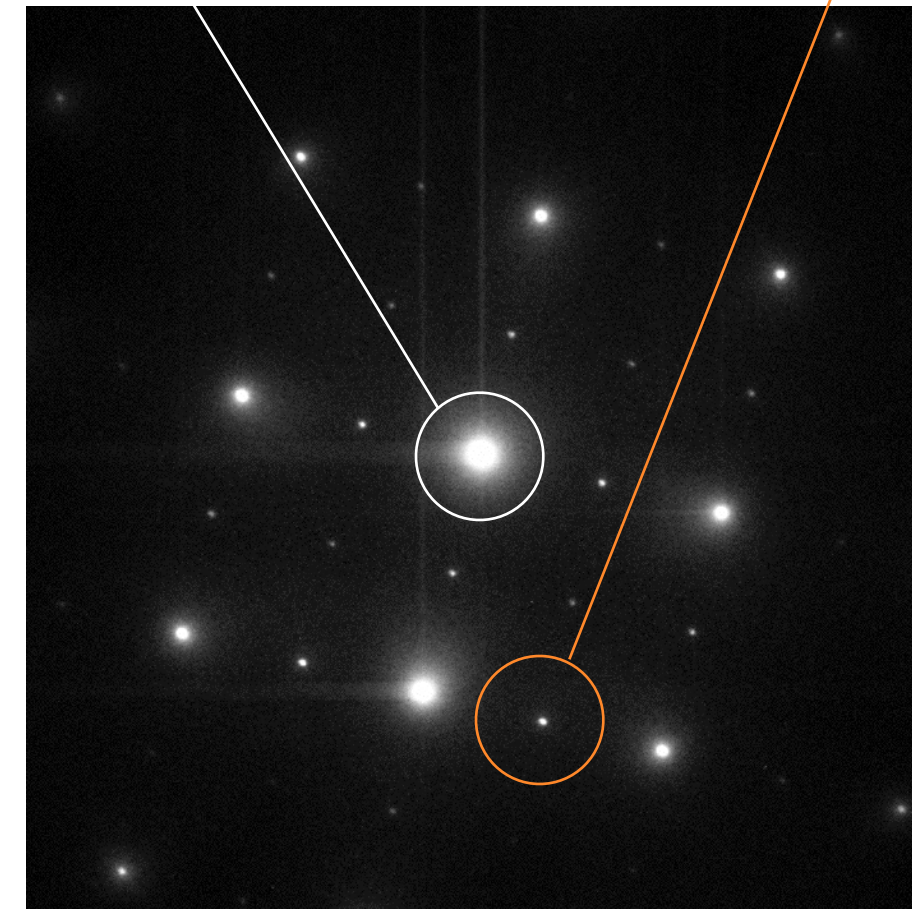
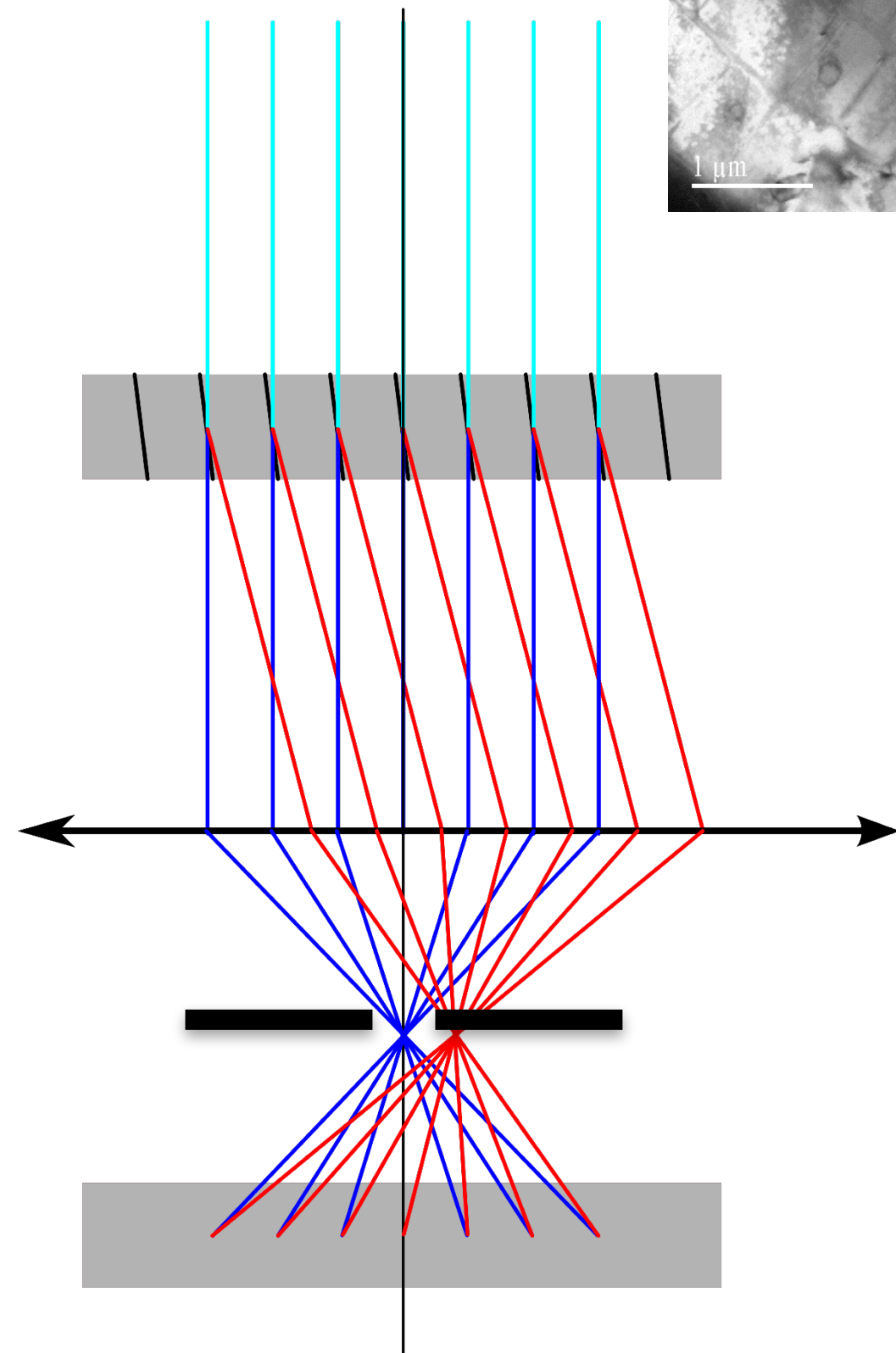
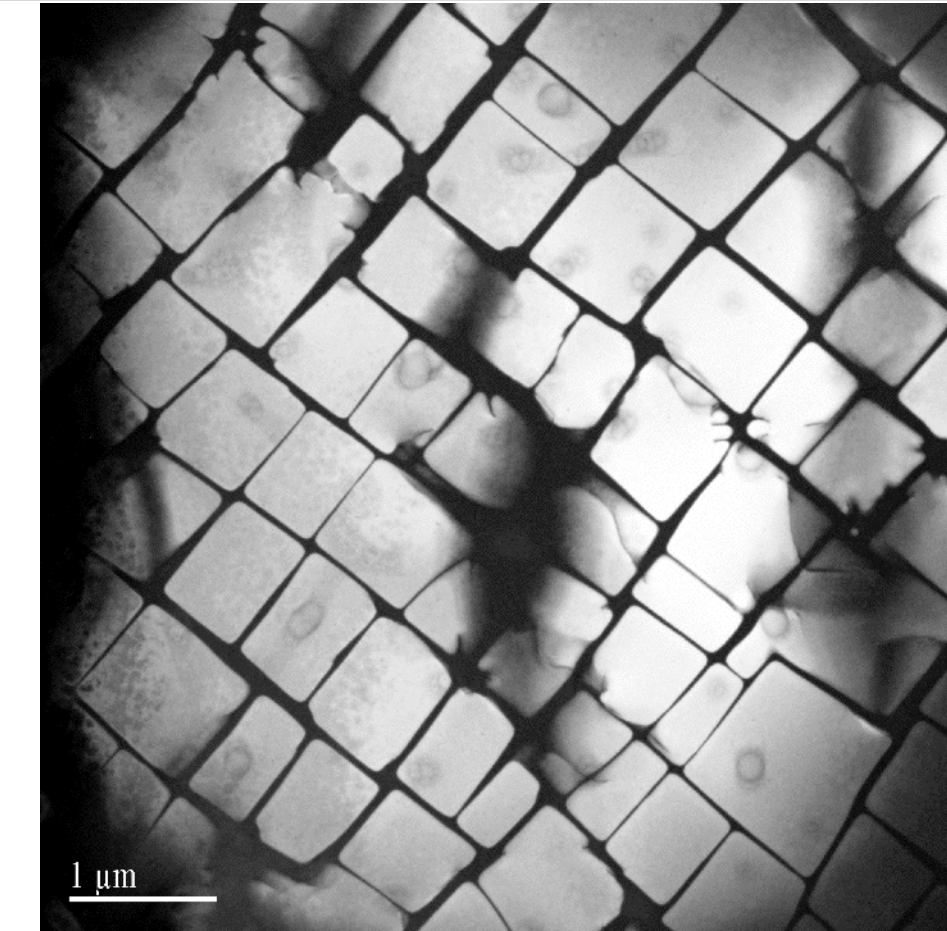
Objective aperture



Bright-field/dark-field imaging



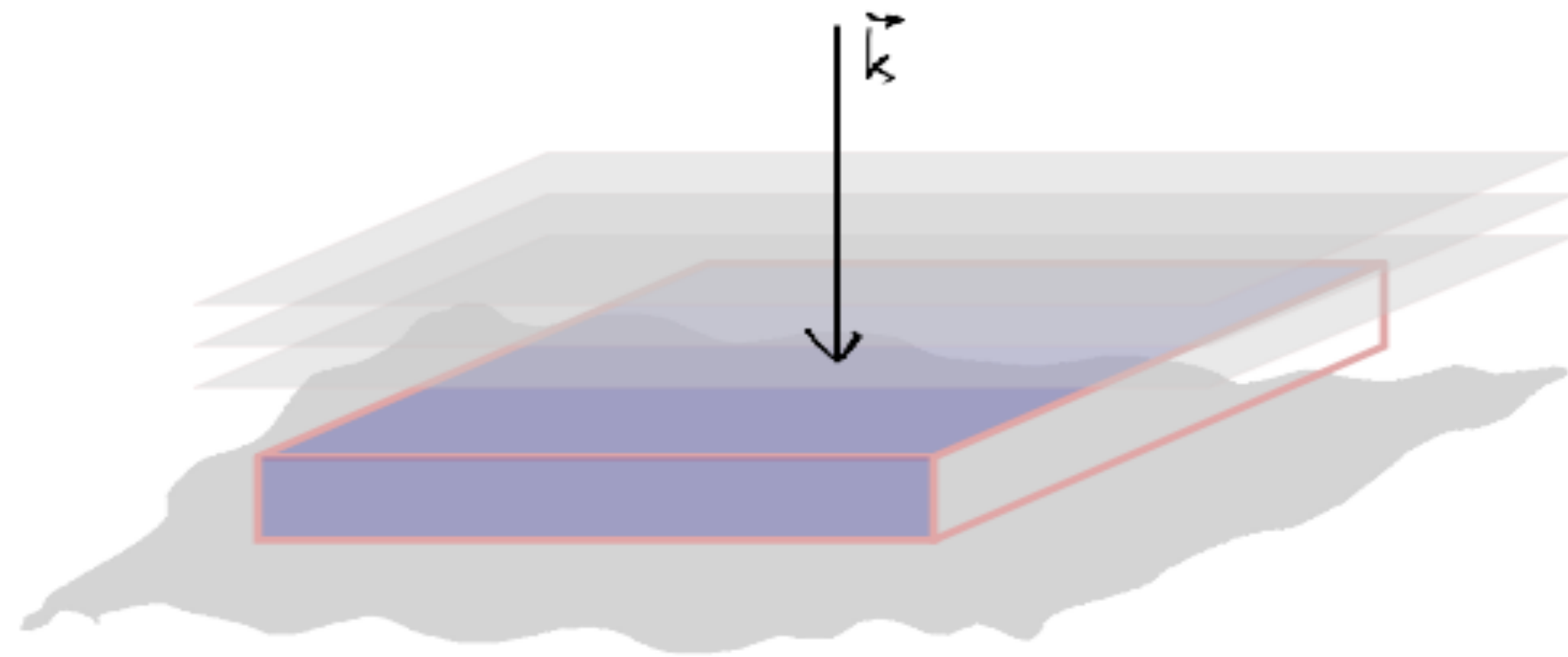
Nickel based superalloys
Contrast γ/γ'



Diffraction in this lecture

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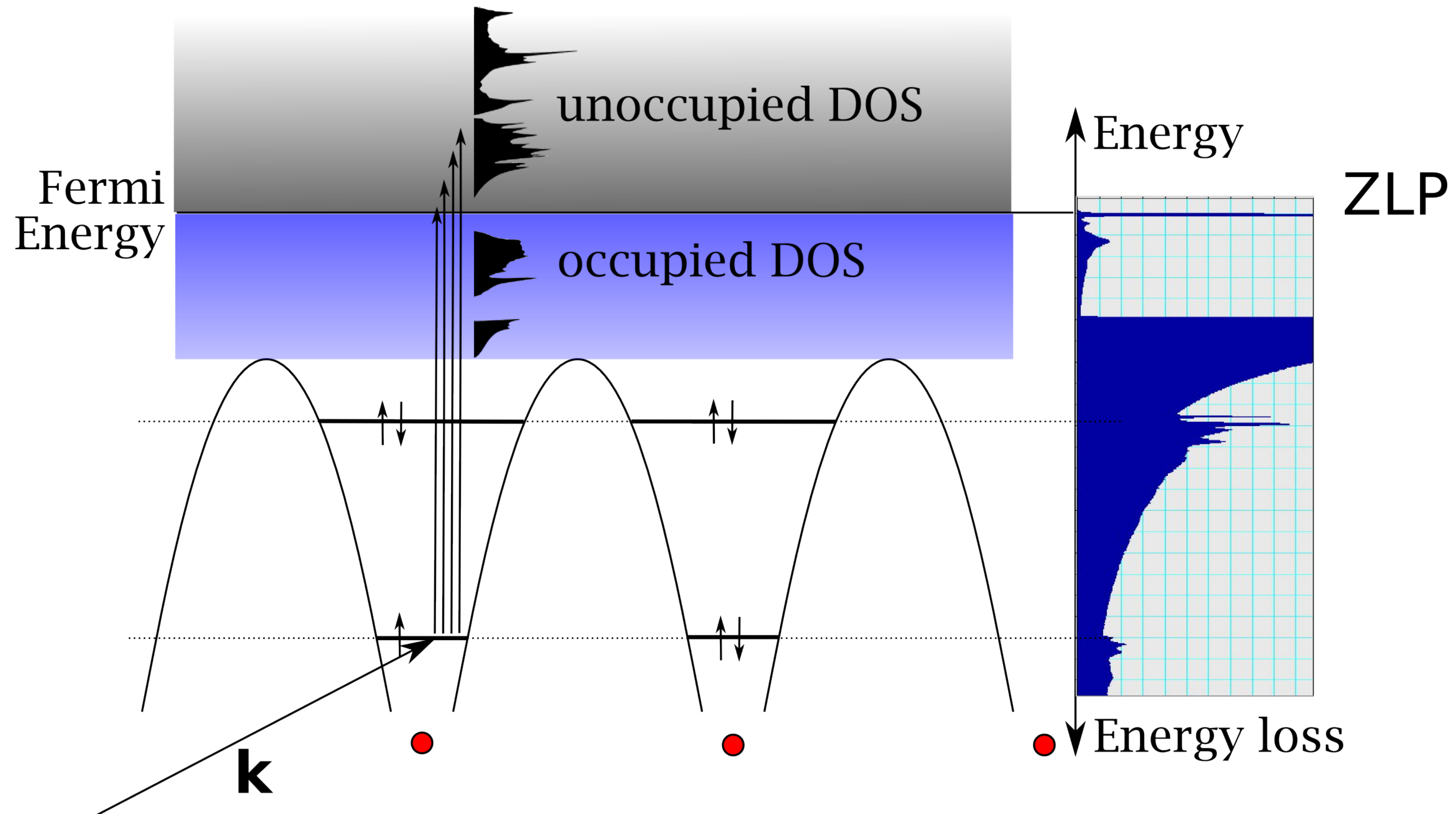
Phase contrast



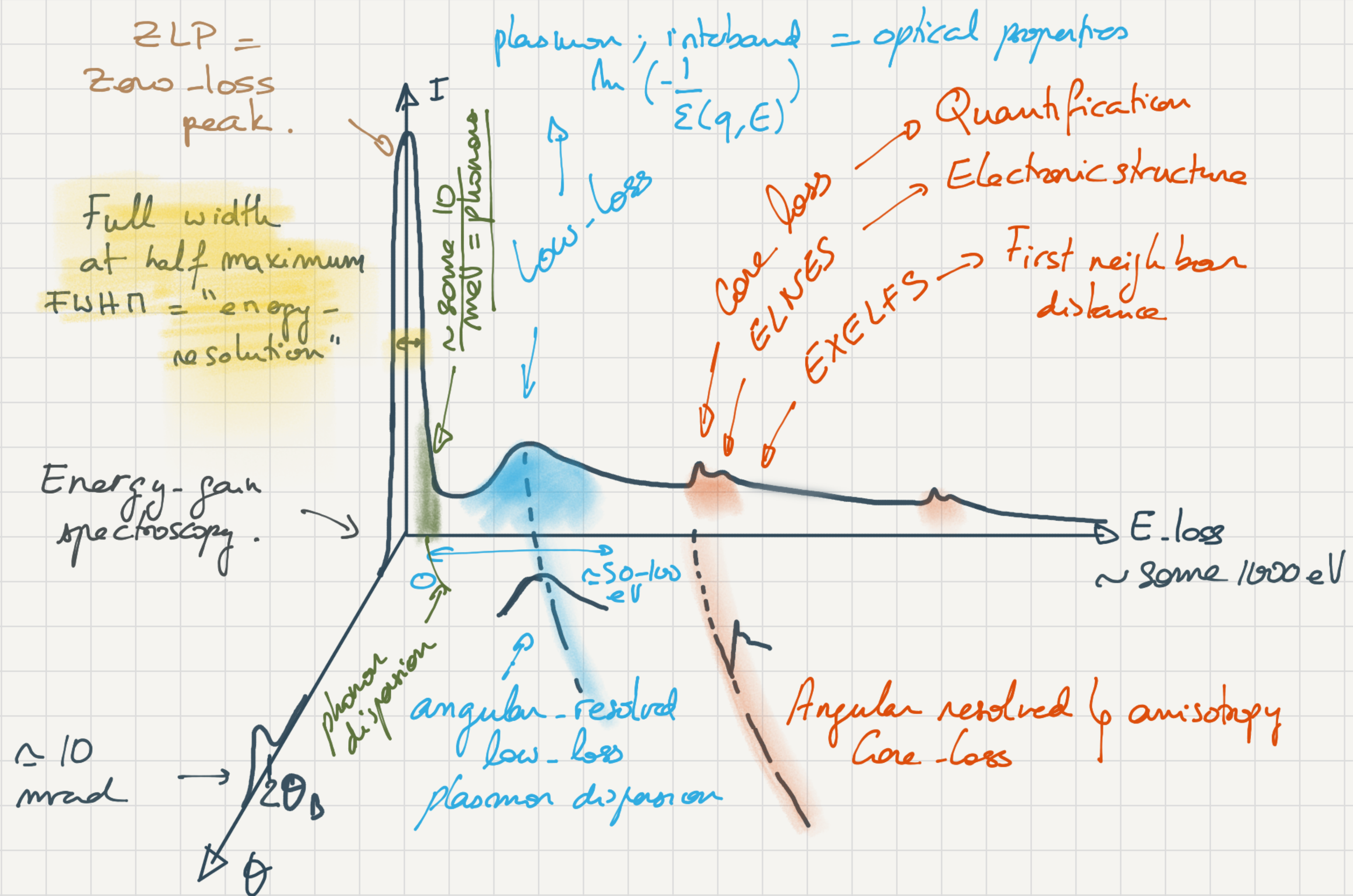
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EELS :Excitation process



EELS: accessible information



EELS: geometry

θ : scattering angle

$\theta \ll 1$ & $k' \simeq k_0$

$\Rightarrow q^2 \simeq q_{||}^2 + q_{\perp}^2$

$q_{\perp}^2 = k_0^2 \theta^2$

$q_{||}^2 = k_0^2 \theta_E^2$ (def)

$\Rightarrow q^2 \simeq k_0^2 (\theta^2 + \theta_E^2)$

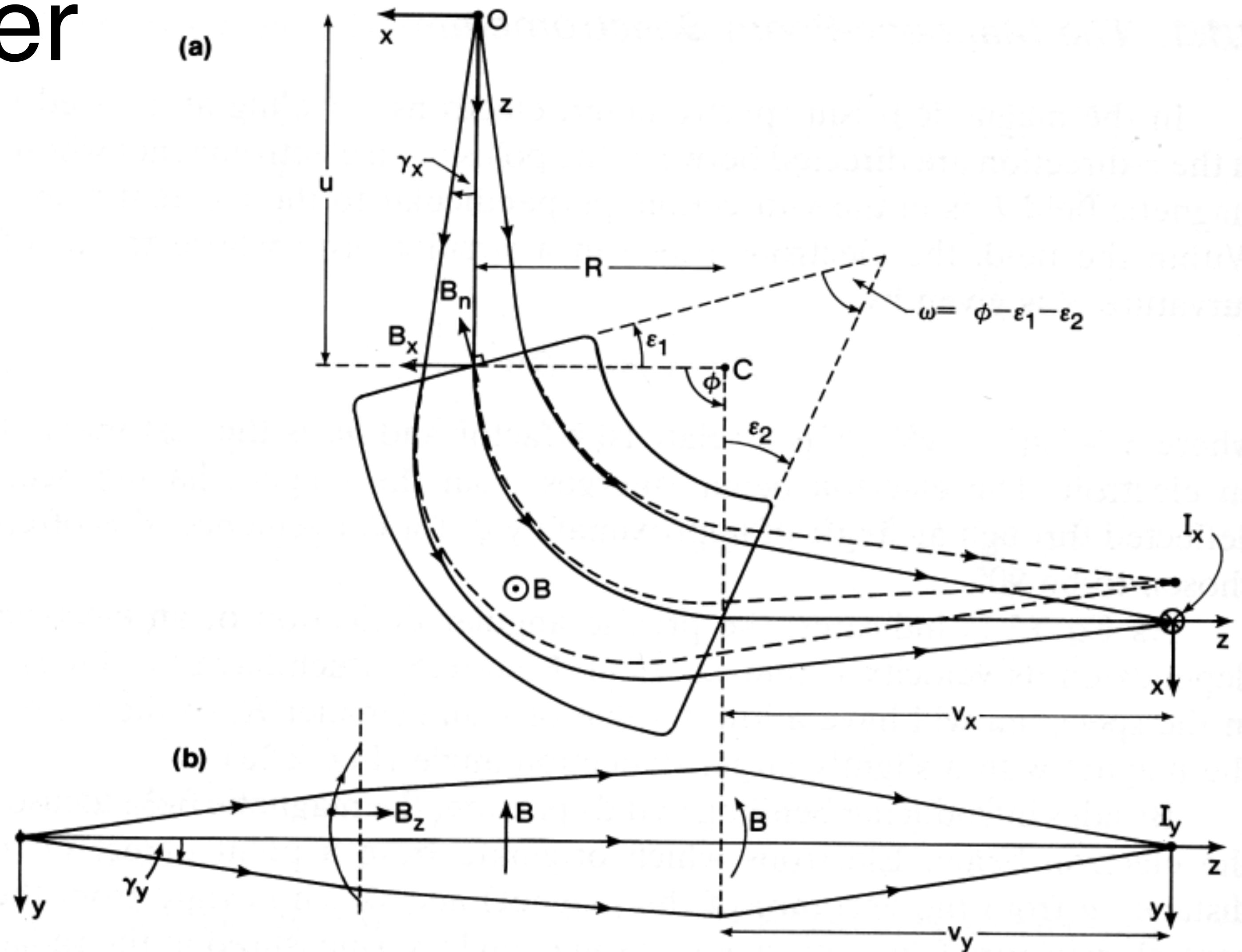
θ & $\theta_E \ll 1$

$\theta_E = \frac{E m_0 \gamma}{\hbar^2 k_0^2} \simeq \frac{E}{2 E_0}$ E : Energy loss

The diagram illustrates the geometry of Electron Energy Loss Spectroscopy (EELS). It shows an incident electron with wave vector \vec{k}_0 and a scattered electron with wave vector \vec{k}' . The scattering angle θ is the angle between \vec{k}_0 and \vec{k}' . The momentum transfer \vec{q} is the vector from the tip of \vec{k}_0 to the tip of \vec{k}' . This vector \vec{q} is decomposed into a parallel component $q_{||}$ (along the direction of \vec{k}_0) and a perpendicular component q_{\perp} . The perpendicular component q_{\perp} is labeled as 'negligible' in orange. The parallel component $q_{||}$ is labeled as 'shortening of k' in orange. The energy loss E is related to the scattering angle θ_E by the equation $\theta_E = \frac{E m_0 \gamma}{\hbar^2 k_0^2} \simeq \frac{E}{2 E_0}$, where E_0 is the initial energy of the electron. The final boxed equation is $q^2 \simeq k_0^2 (\theta^2 + \theta_E^2)$.

Instrumentation for EELS

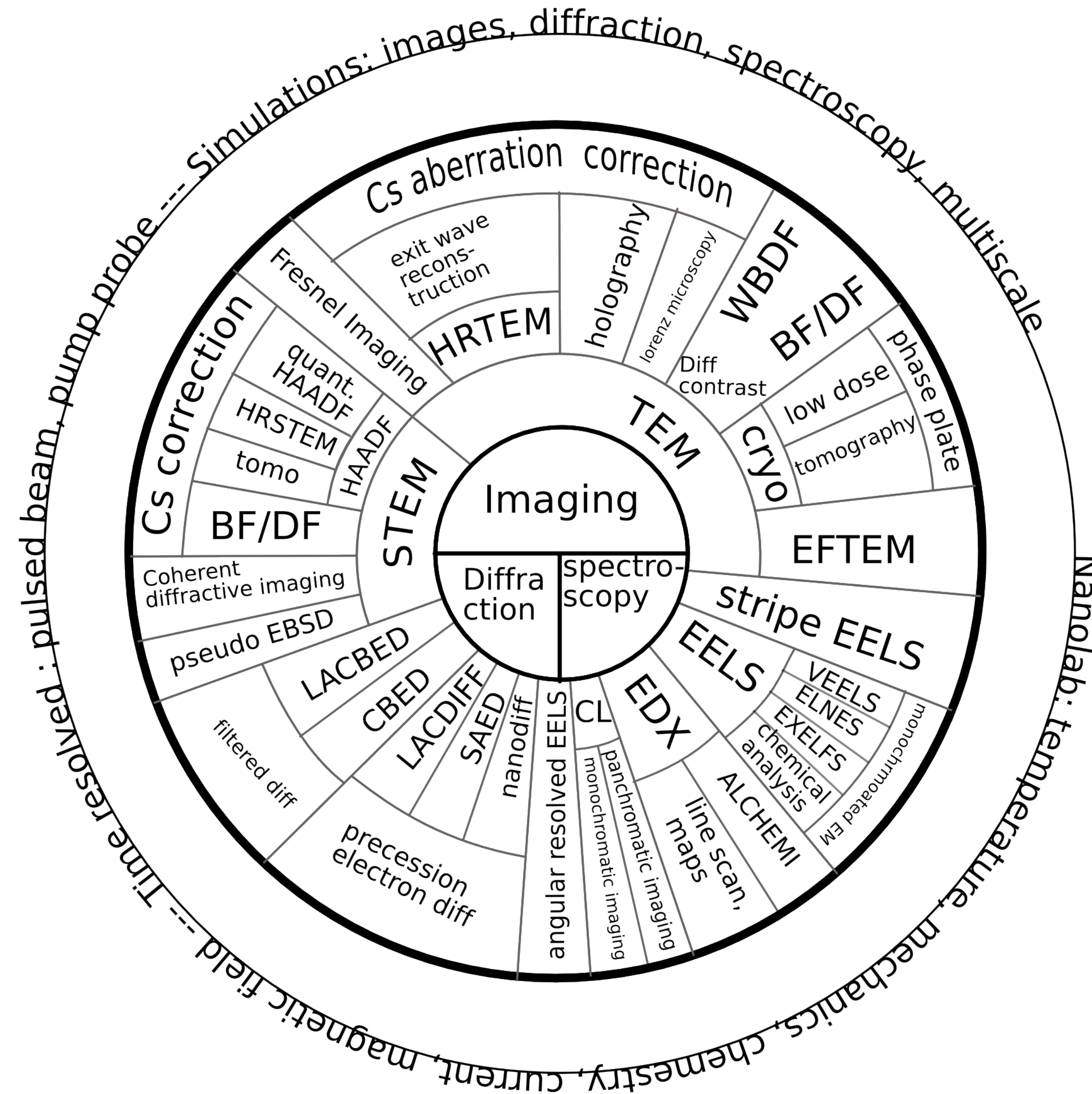
Spectrometer



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Techniques in Microscopy



The (crystalline) specimen

A large part of the investigated specimens are crystals (even sometimes in biology: e.g proteins can be crystallised!)

Many imaging techniques make use of the interaction of the beam with the crystal: High resolution, diffraction, dark field, weak beam, convergent beam diffraction, large angle convergent beam diffraction...

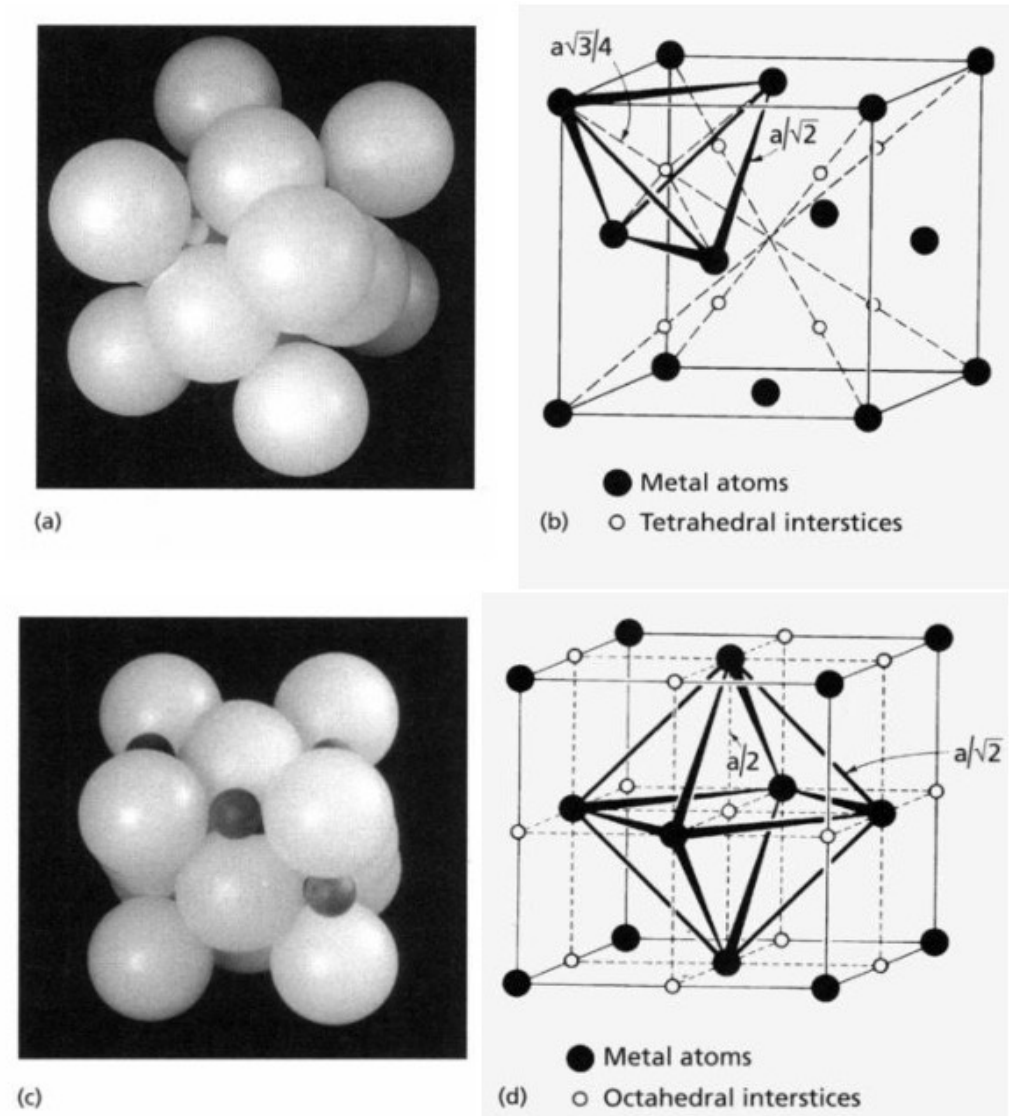
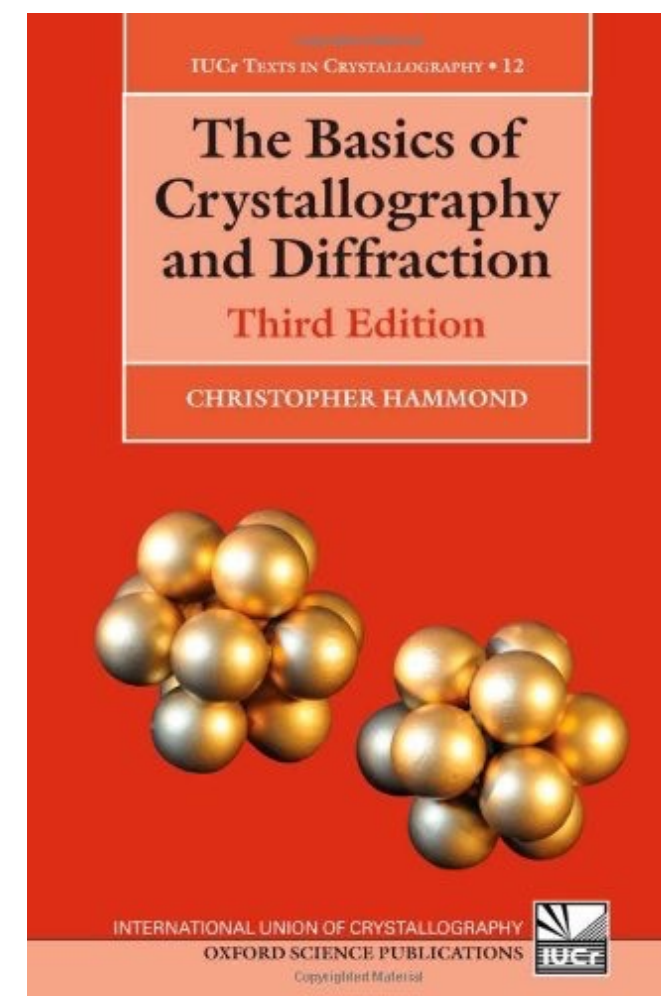
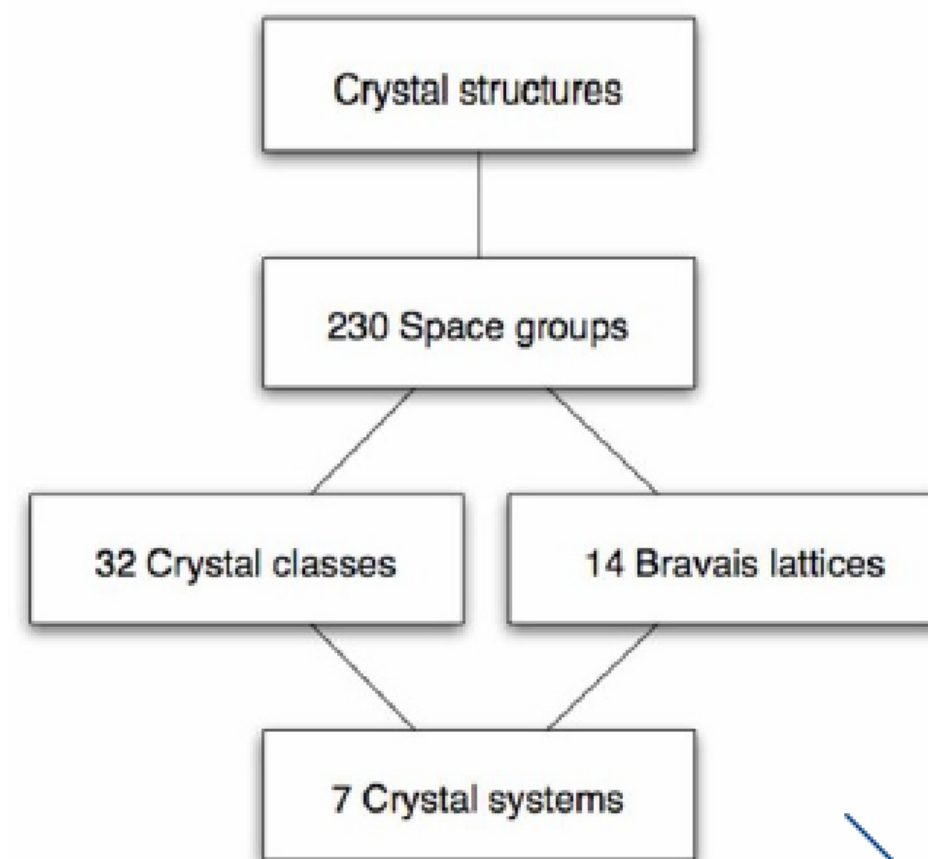


Fig. 1.10. (a) An atom in a tetrahedral interstitial site, $r_X/r_A = 0.225$ within the ccp unit cell and (b) geometry of a tetrahedral site, showing the dimensions of the tetrahedron in terms of the unit cell edge length a . (c) Atoms or ions in some of the octahedral interstitial sites, $r_X/r_A = 0.414$ within the ccp unit cell and (d) geometry of an octahedral site, showing the dimensions of the octahedron in terms of the unit cell edge length a . (From *The Structure of Metals*, 3rd edn, by C. S. Barrett and T. B. Massalski, Pergamon, 1980.)

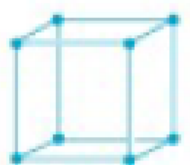
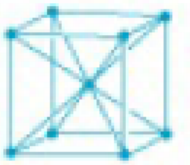
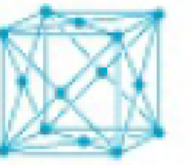
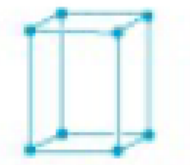


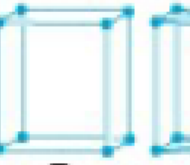

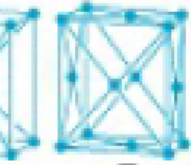
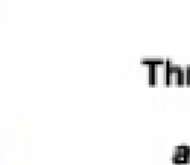
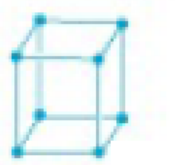
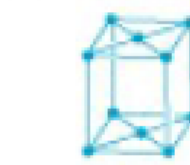


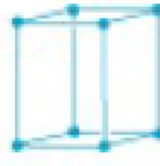


The (crystalline) specimen



There are :

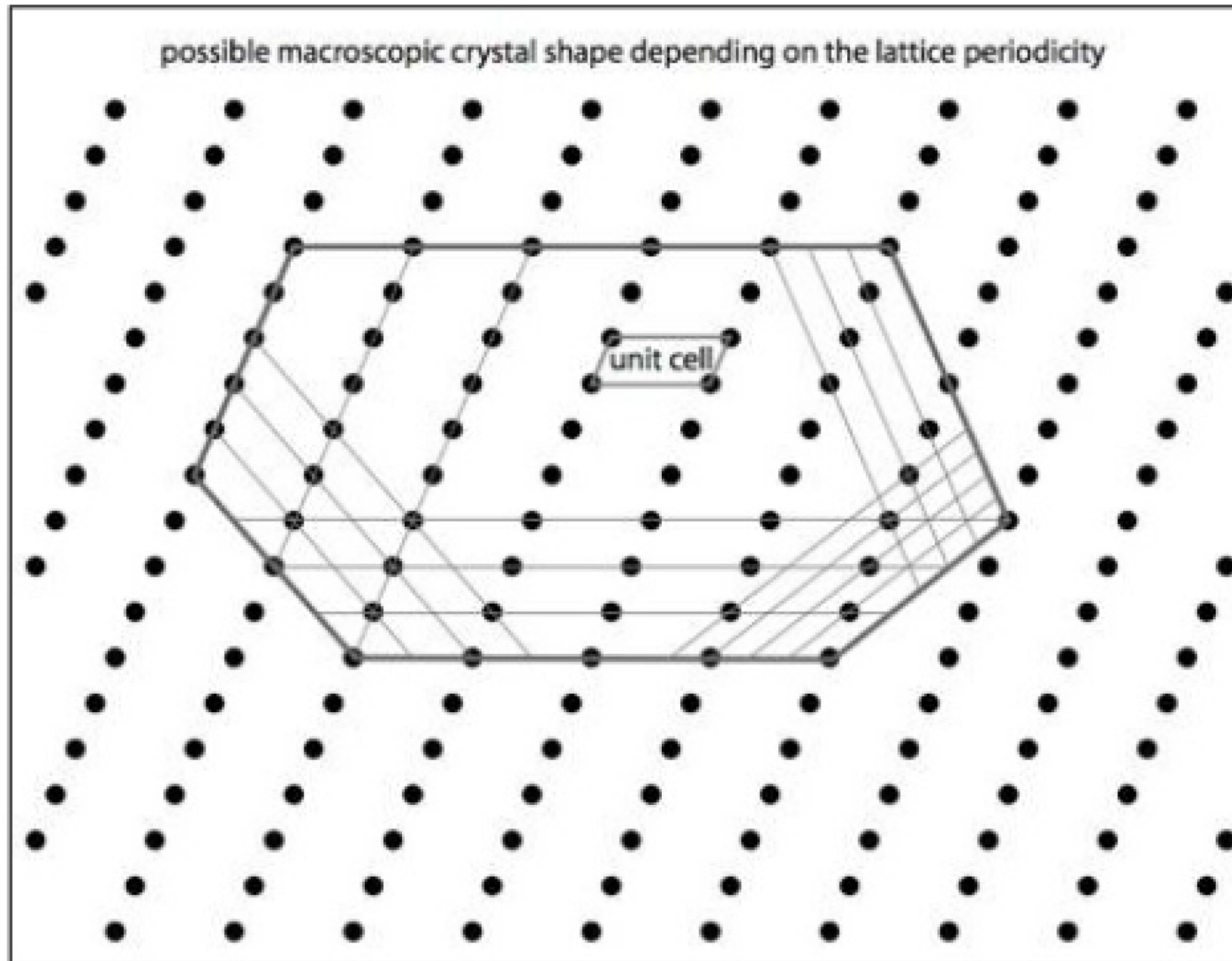
- the cubics
- the others...

Bravais lattice cells	Axes and interaxial angles	Examples
   Cubic P Cubic I Cubic F	Three axes at right angles; all equal: $a = b = c; \alpha = \beta = \gamma = 90^\circ$	Copper (Cu), silver (Ag), sodium chloride (NaCl)
   Tetragonal P Tetragonal I	Three axes at right angles; two equal: $a = b \neq c; \alpha = \beta = \gamma = 90^\circ$	White tin (Sn), rutile (TiO ₂), β -spodumene (LiAlSi ₂ O ₆)
    P C I F Orthorhombic	Three axes at right angles; all unequal: $a \neq b \neq c; \alpha = \beta = \gamma = 90^\circ$	Gallium (Ga), perovskite (CaTiO ₃)
  Monoclinic P Monoclinic C	Three axes, one pair not at right angles, of any lengths: $a \neq b \neq c; \alpha = \gamma = 90^\circ \neq \beta$	Gypsum (CaSO ₄ • 2H ₂ O)
 Triclinic P	Three axes not at right angles, of any lengths: $a \neq b \neq c; \alpha \neq \beta \neq \gamma \neq 90^\circ$	Potassium chromate (K ₂ CrO ₇)
 Trigonal R (rhombohedral)	Rhombohedral: three axes equally inclined, not at right angles; all equal: $a = b = c; \alpha = \beta = \gamma \neq 90^\circ$	Calcite (CaCO ₃), arsenic (As), bismuth (Bi)
 Trigonal and hexagonal C (or P)	Hexagonal: three equal axes coplanar at 120°, fourth axis at right angles to these: $a_1 = a_2 = a_3 \neq c; \alpha = \beta = 90^\circ, \gamma = 120^\circ$	Zinc (Zn), cadmium (Cd), quartz (SiO ₂) [P]

The (crystalline) specimen

Planes, directions and families of those. Miller indices.

- Electrons are waves ... and articles



In 2D, we can draw families of lines parallel to each other, containing the same linear arrangement of atoms. In 3D these are **planes**.

They are called lattice planes

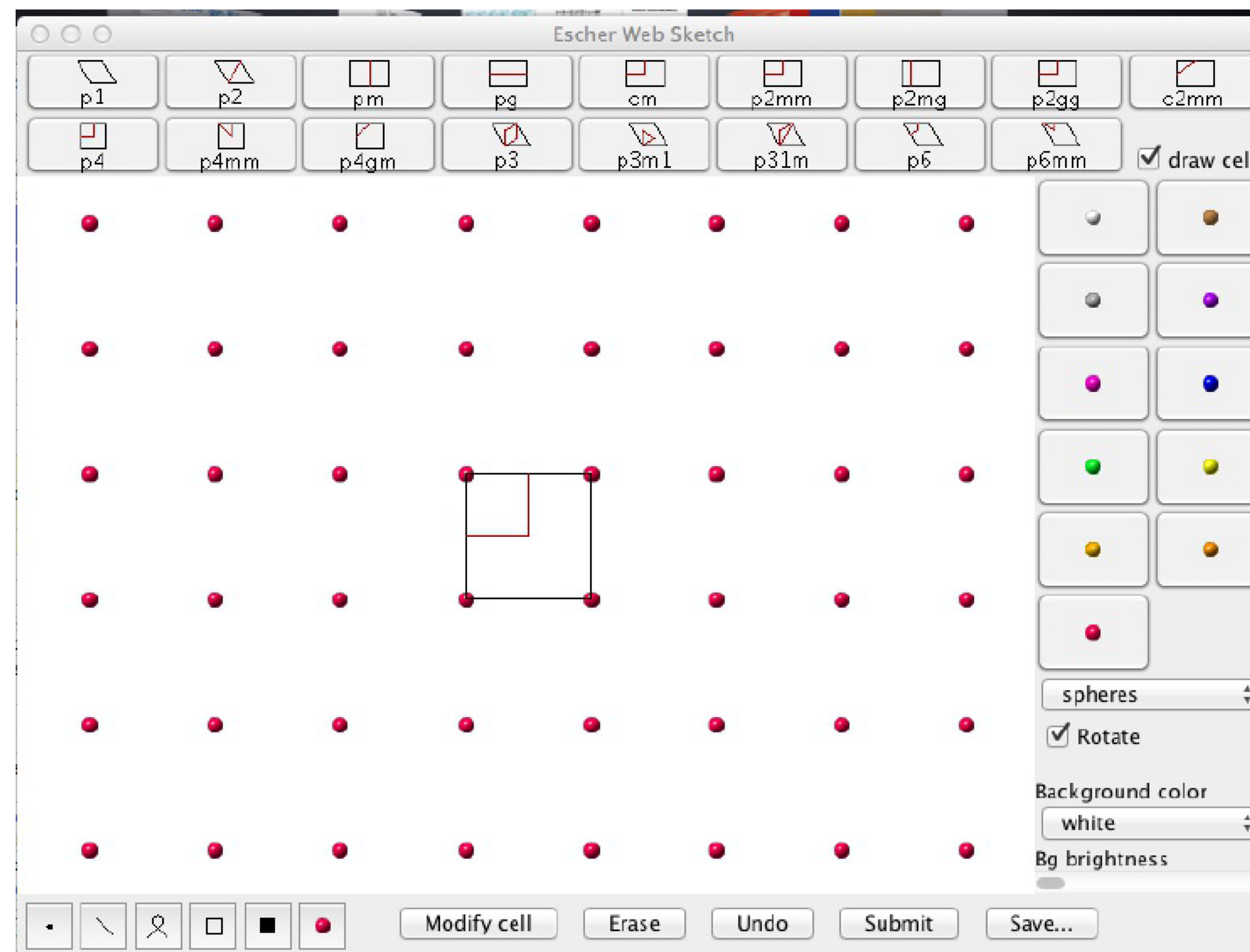
We can also look at vectorial directions with respect to the unit cell.

How do we label those ?

The (crystalline) specimen

We use miller indices for planes and directions for the vectors.

They are taken in the referential system of the unit cell. For a cubic system, it is an orthonormal one. For any other system, it is not. Be careful, some « intuitive evidences » will be WRONG!



Direction: end point of the vector.

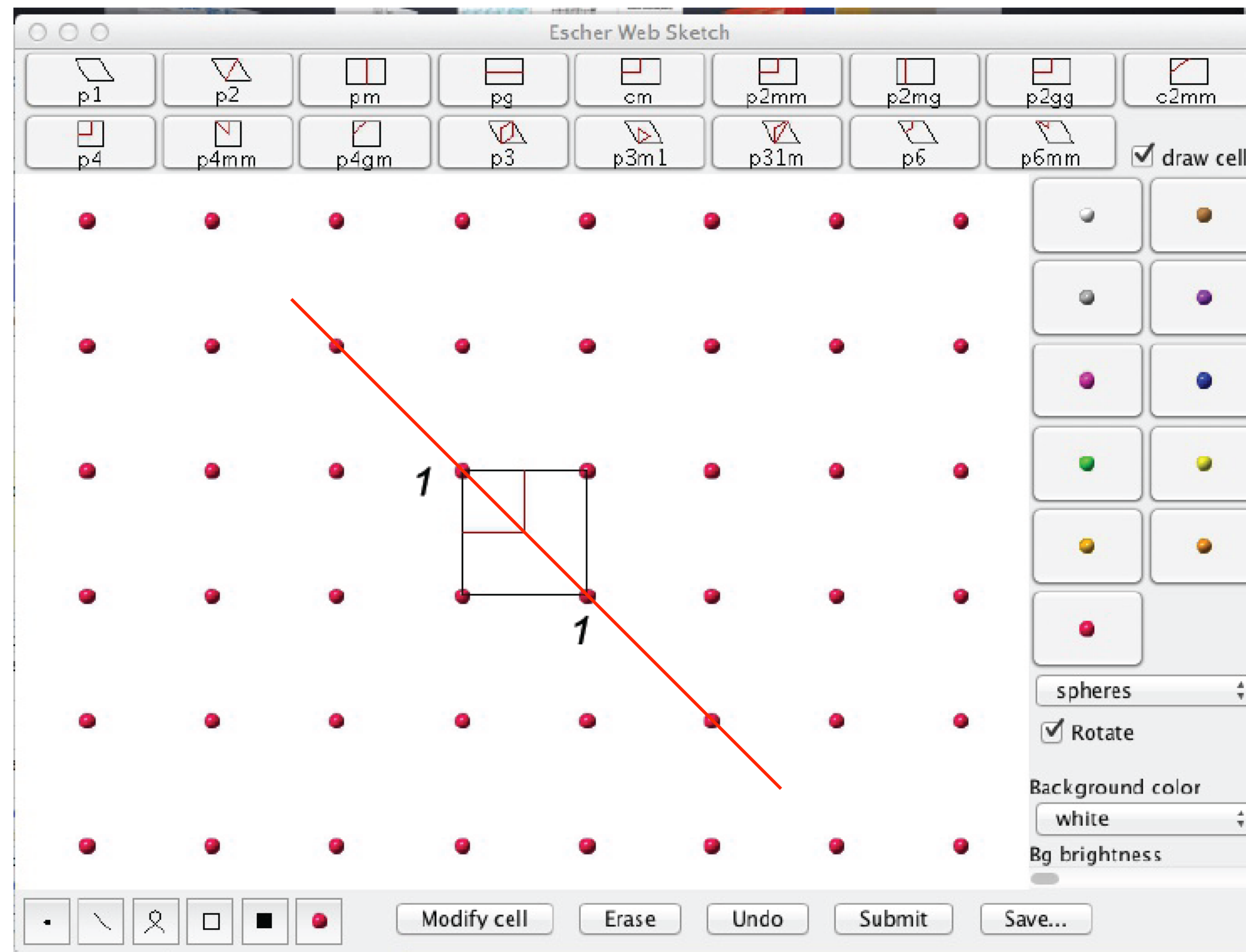
e.g. :

- // to a: 1,0
- on the diagonal: 1,1
- it can point down: 1,-1

Directions are given in squared brackets in 3D they are labelled u,v,w $[u,v,w]$

The (crystalline) specimen

Lines (planes) are given by the miller indices h,k,l .
The line (plane) intercepts the crystal at $a/h, b/k, (c/l)$



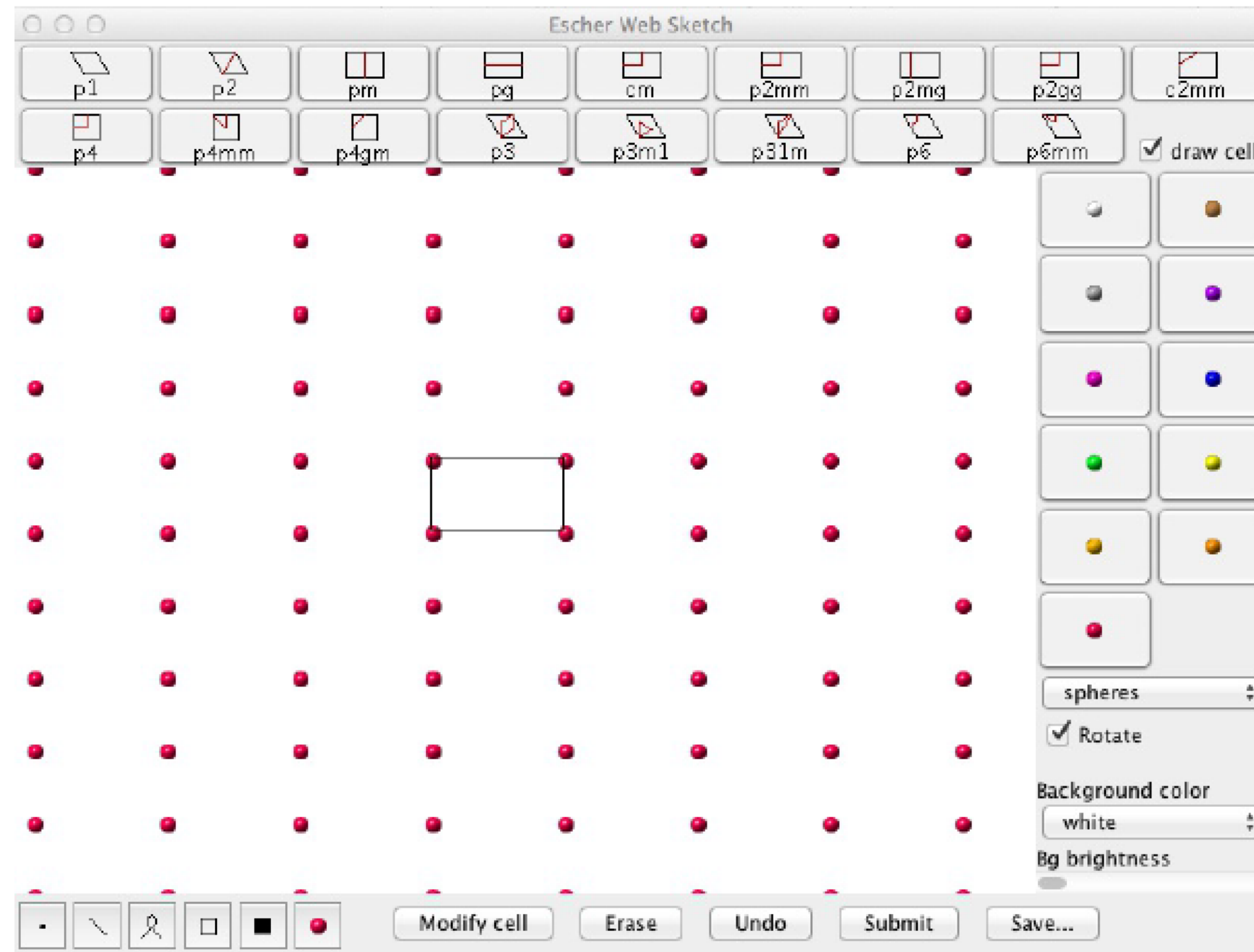
Here, we have the 1,1 line

Planes are given in round brackets (h,k,l)

Families of planes are given in curled brackets $\{h,k,l\}$

The (crystalline) specimen

Draw the (2,1) line and the [2,1] direction



The (crystalline) specimen

Zone and zone axis

A **zone** is a set of plane whose intersections in a crystal are parallels.

The **zone axis** is the direction of those intersections

Therefore zone and directions are equivalent.

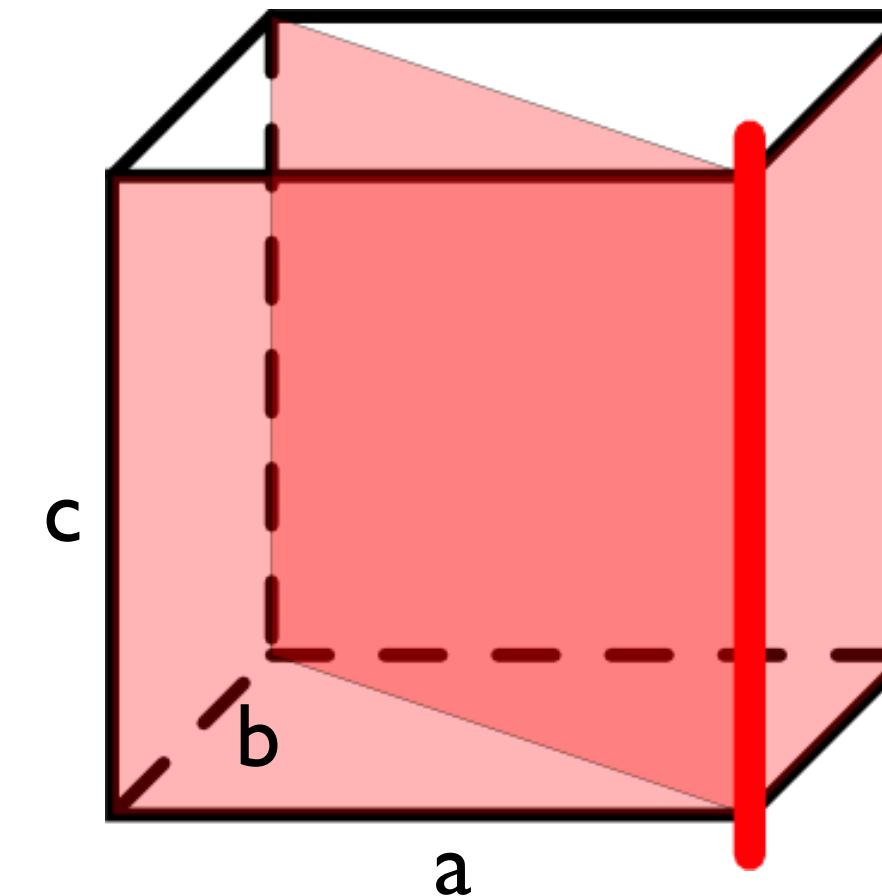
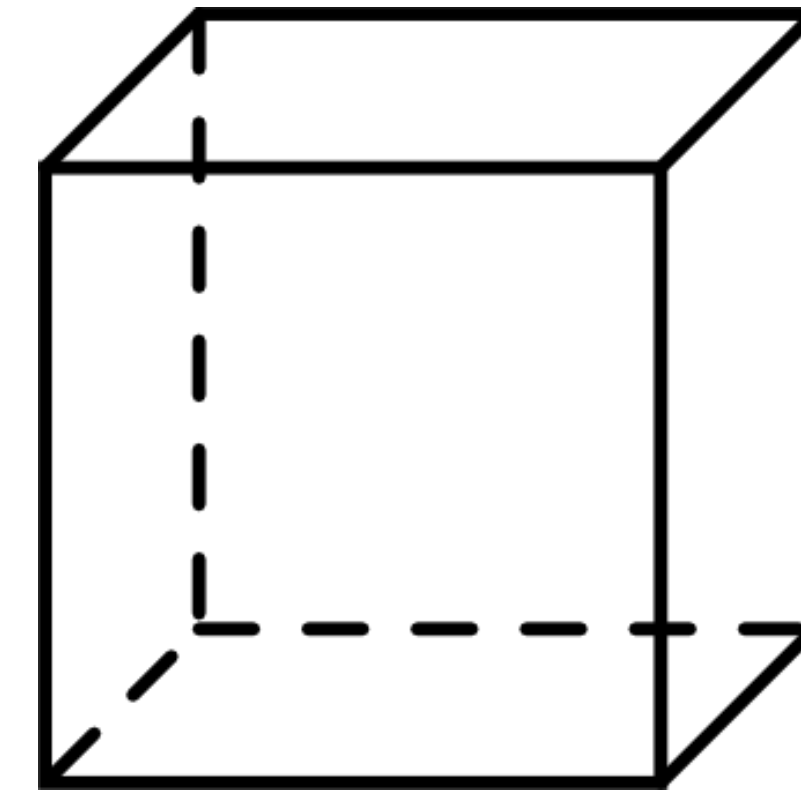
Zone and zone axis are then noted in squared brackets $[u,v,w]$

In TEM, you will commonly read « The crystal is oriented in the $[u,v,w]$ zone axis.

This means the optical axis of the microscope is // to this zone axis

Zone law or Weiss zone law:

if a plane (hkl) lies in a zone $[uvw]$ $hu+kv+lw=0$



The (crystalline) specimen

Reciprocal space

a^* is perpendicular to b and c
 b^* is perpendicular to a and c
 c^* is perpendicular to a and b

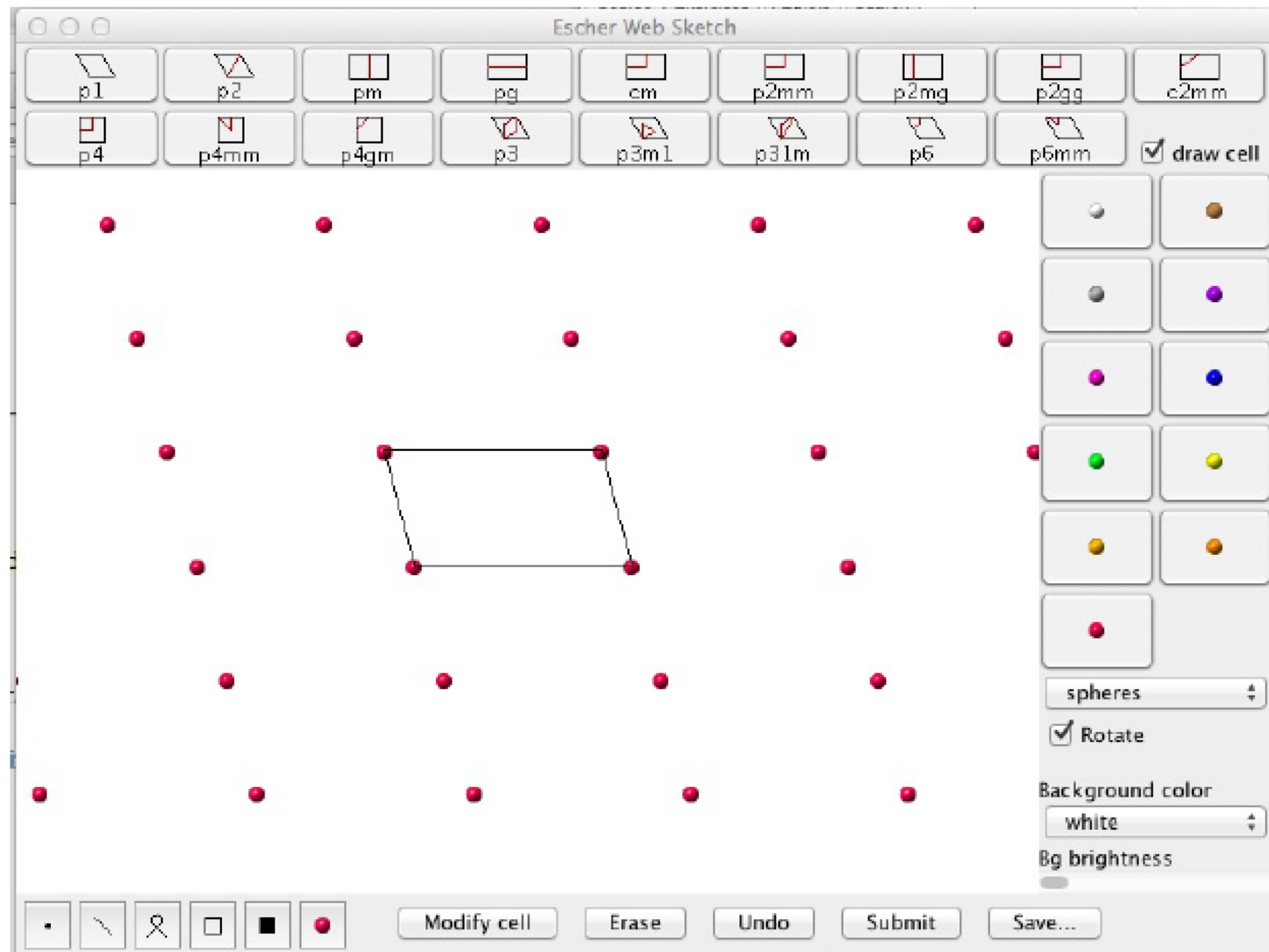
$$a^* \cdot a = b^* \cdot b = c^* \cdot c = 1$$

similarly to real space, the reciprocal vectors define the reciprocal unit cell.

thus we have directions in reciprocal space. They are identified by h k and l
An hkl direction in reciprocal space is perpendicular to the (hkl) plane in real space.

a reciprocal space vector $\mathbf{d}_{hkl}^* = h\mathbf{a}^* + k\mathbf{b}^* + l\mathbf{c}^*$ has a length d_{hkl}^* $d_{hkl}^* = 1/d_{hkl}$ with d_{hkl} the interplane distance of planes (hkl)

The reciprocal space vector's length gives the **spacial frequency** of the planes (hkl)



Draw the a^* and b^* reciprocal unit vectors; draw the $||$ reciprocal direction and the $(||)$ line

The (crystalline) specimen

2 π or not 2 π ?

A word of caution: investigated volume

One TET sample : $\xleftrightarrow{1\mu m} 100\text{ nm}$ $(10^{-6})^2 \cdot 10^{-7} = 10^{-19} \text{ m}^3$


Average TET-day : 5 samples }
Average day/year 200 } 1000 samples / y

$10^{-16} \text{ m}^3 / \text{year}$ 8 TET

EPFL	5 TET	10'000 students	TU Graz	16'000
			4 TET	
ENAT	6 TET	20'000 students	...	

Take 5 TET per 20'000 students

$\sim 200 \cdot 10^6$ students worldwide \rightarrow 10'000 TET worldwide

$\Rightarrow 10^{-12} \text{ m}^3$ water / year $\sim 80 \text{ y}$  linear increase $\Rightarrow \sim 50 \text{ y}$
 $5 \cdot 10^{-11} \text{ m}^3$ matter $0,05 \text{ mm}^3$