

INTEGRATED NONLINEAR PHOTONICS

Concepts, methods and research



AARHUS
UNIVERSITY
DEPARTMENT OF ELECTRICAL AND COMPUTER
ENGINEERING

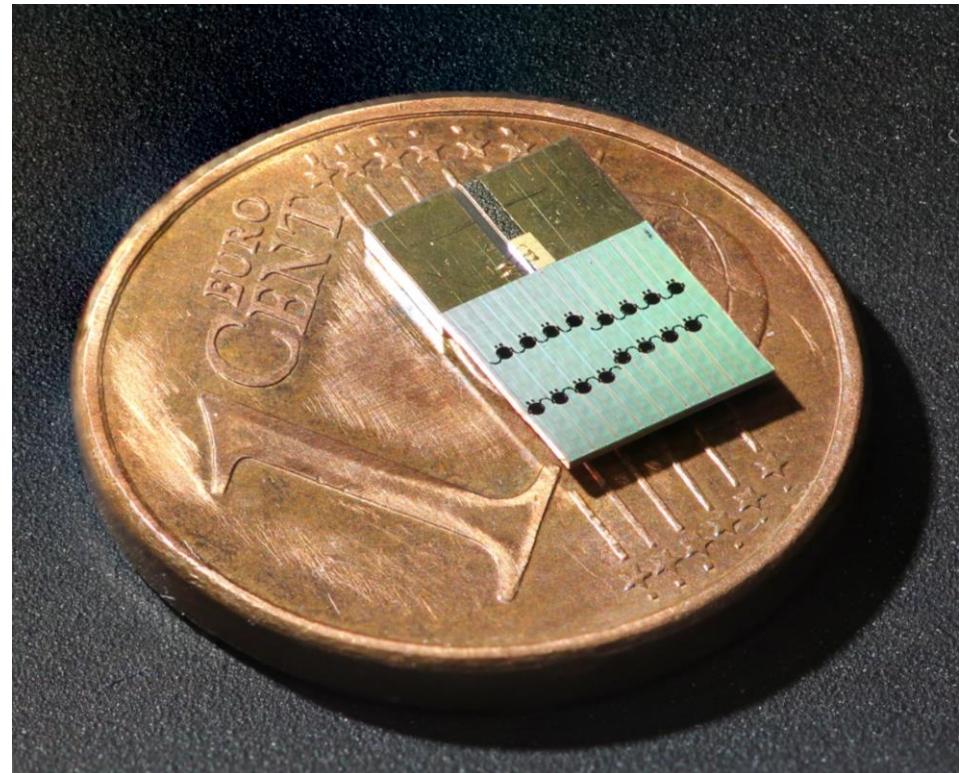
GUEST LECTURE
8 MAY 2025

ASGER BRIMNES GARDNER
PHD STUDENT



AGENDA

- Integrated nonlinear photonics:
 - What?
 - Why?
 - How?
 - Who?
- Example: quantum frequency conversion
- Example: deep-UV generation



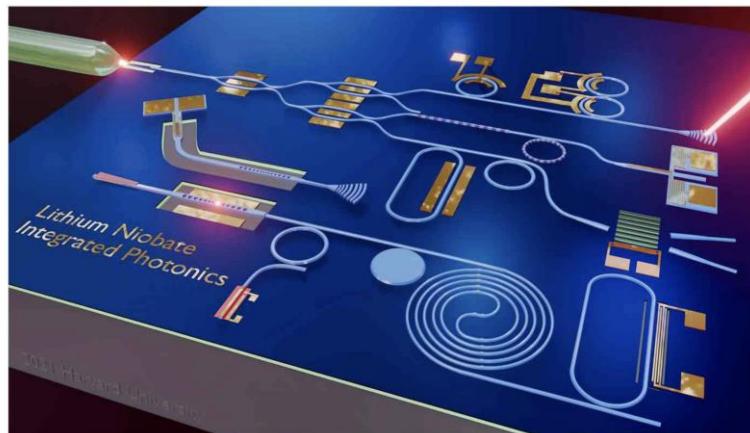
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What?

- **Complex** optical systems on a chip
- Transferral of **laboratory** optical systems to **mass-producible** devices: Photonic Integrated Circuits (**PICs**)
- Comparison: Electronic Integrated Circuits (**EICs**)



European XFEL

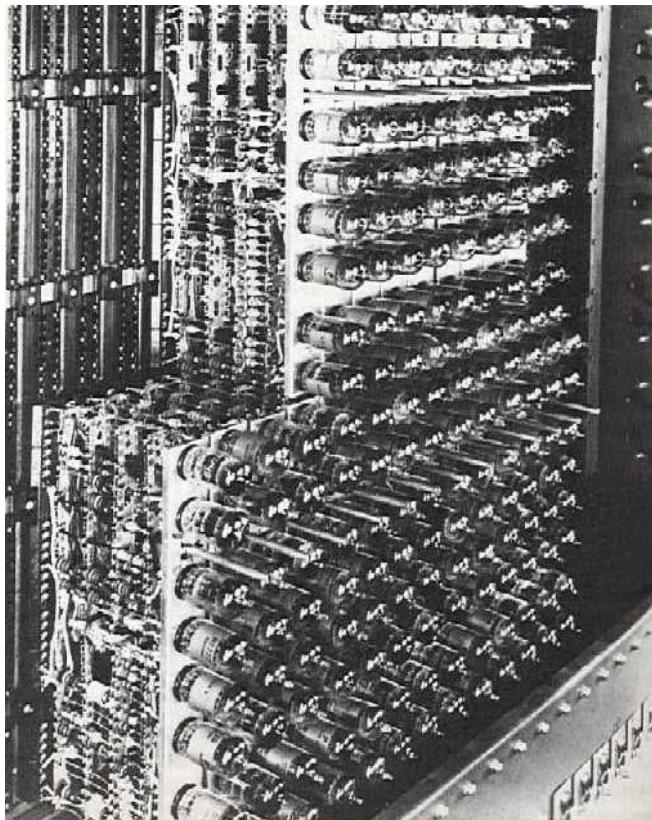


Di Zhu et. Al., "Integrated photonics on thin-film lithium niobate," Adv. Opt. Photon. 13, 242-352 (2021)

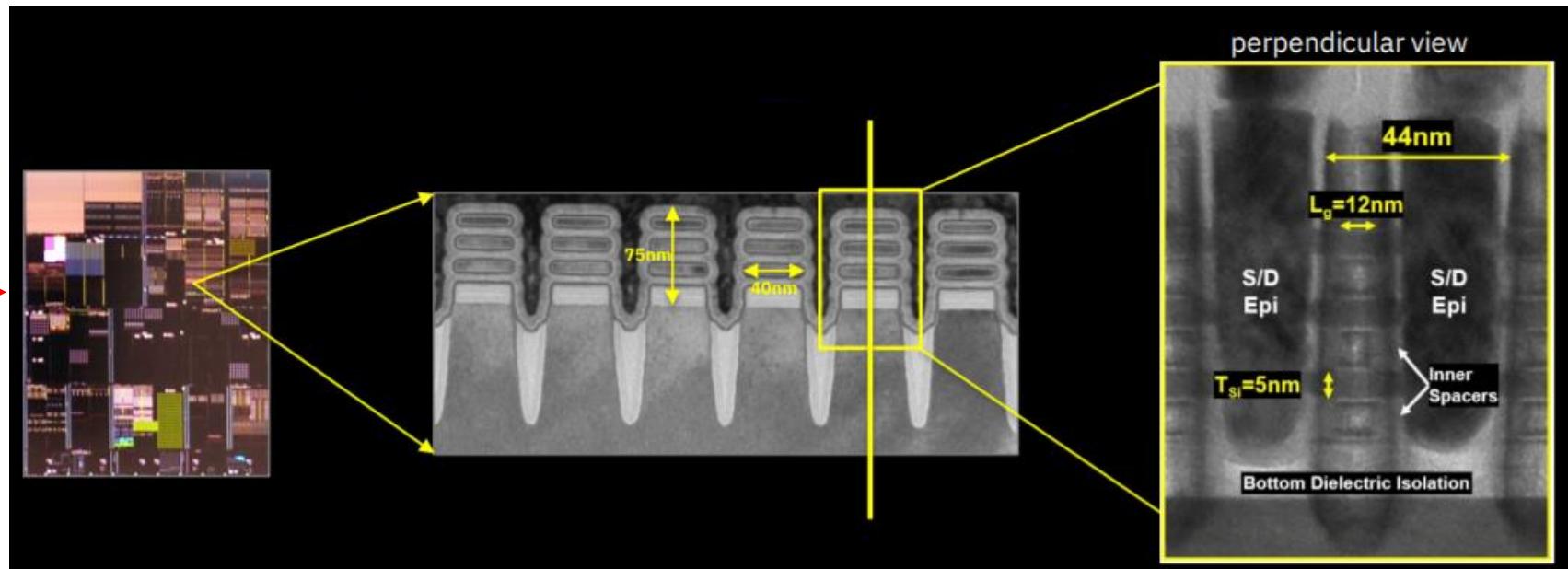


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IBM 701 (1953)



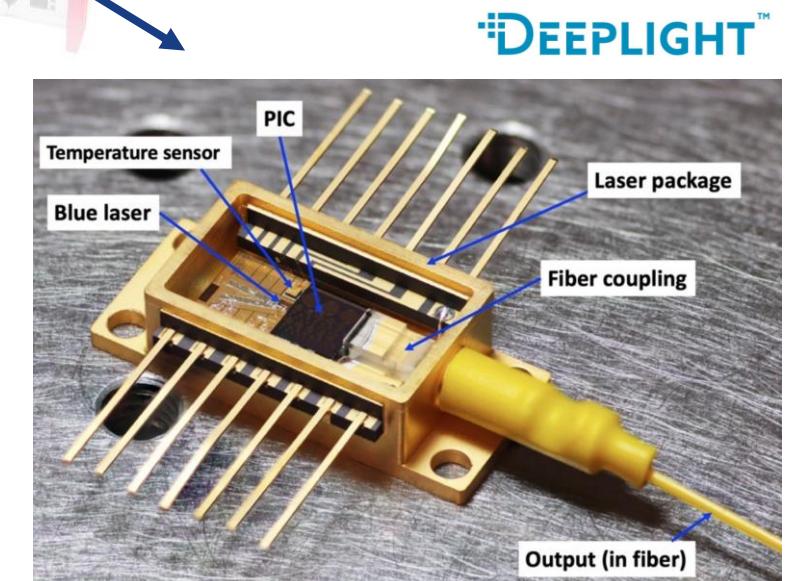
IBM 2 nm node transistors (2021)



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Why?

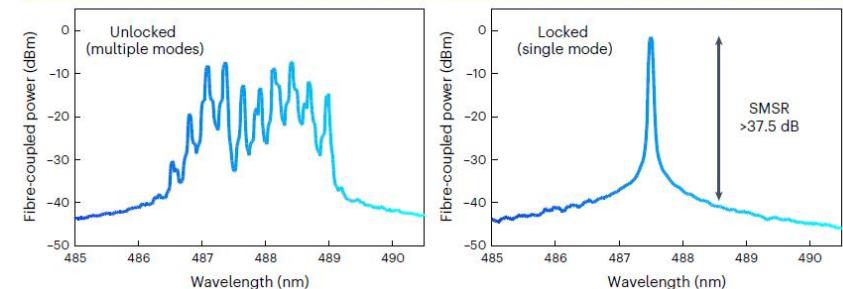
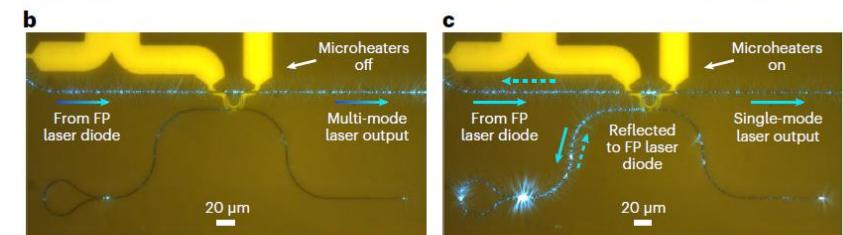
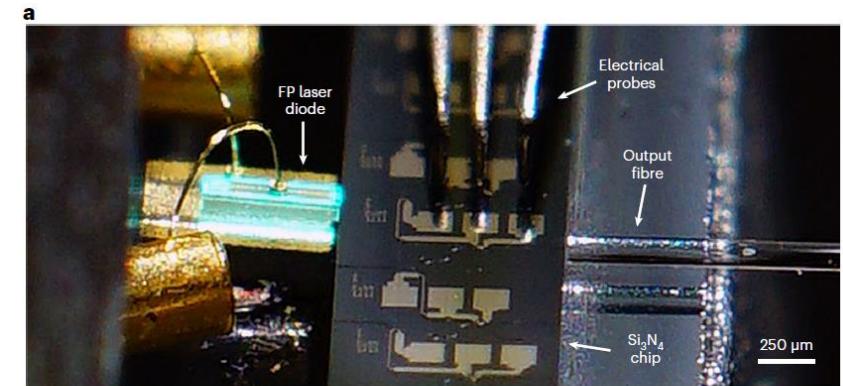
- SWaP: **S**ize, **W**eight **a**nd **P**ower
- Use cases include:
 - the Internet
 - data centers
 - sensing
 - (quantum) computing



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How?

- Confining light to **micro/nanoscale** structures opposed to **free-space** beams

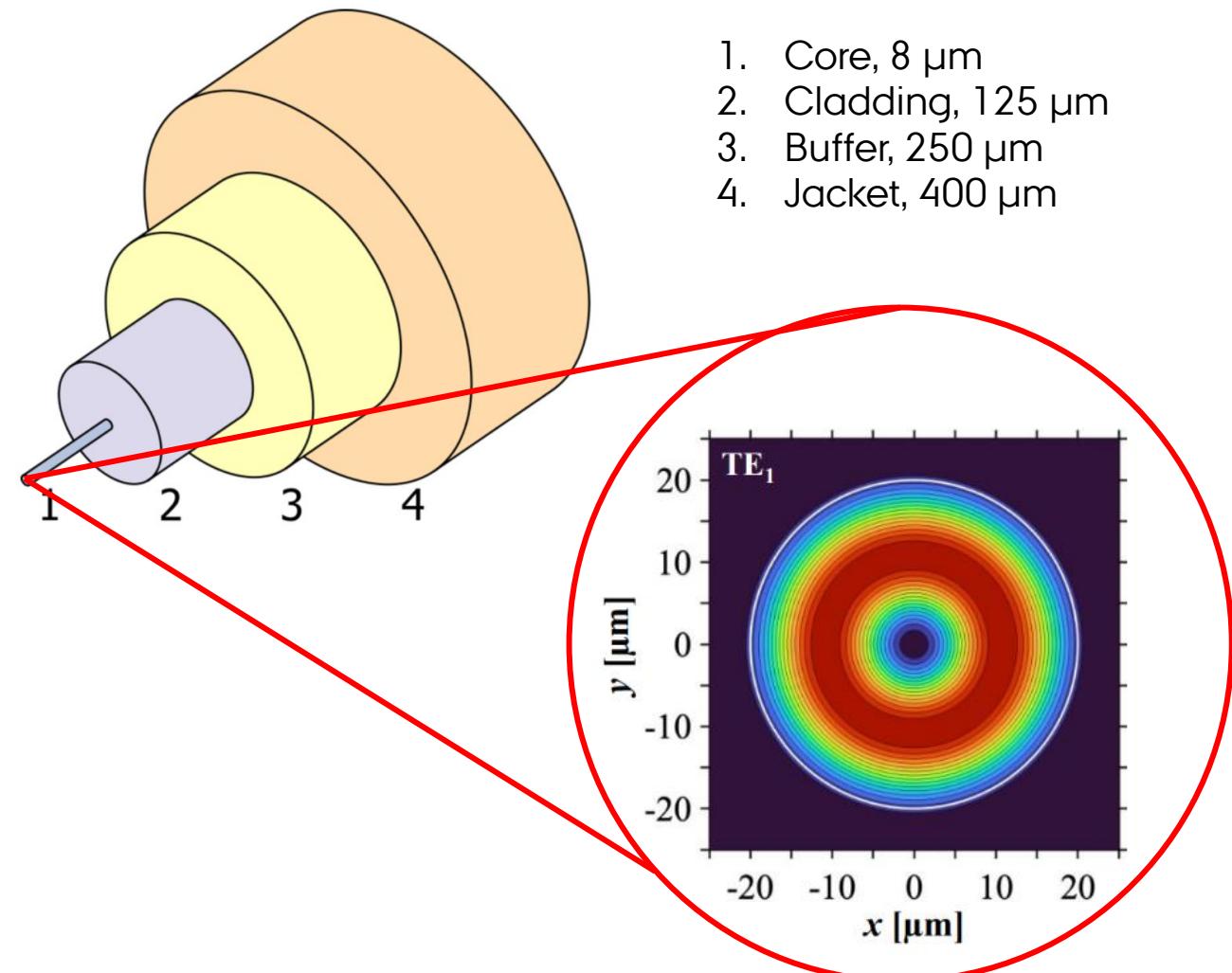


Corato-Zanarella *et al.* Widely tunable and narrow-linewidth chip-scale lasers from near-ultraviolet to near-infrared wavelengths. *Nat. Photon.* **17**, 157–164 (2023).

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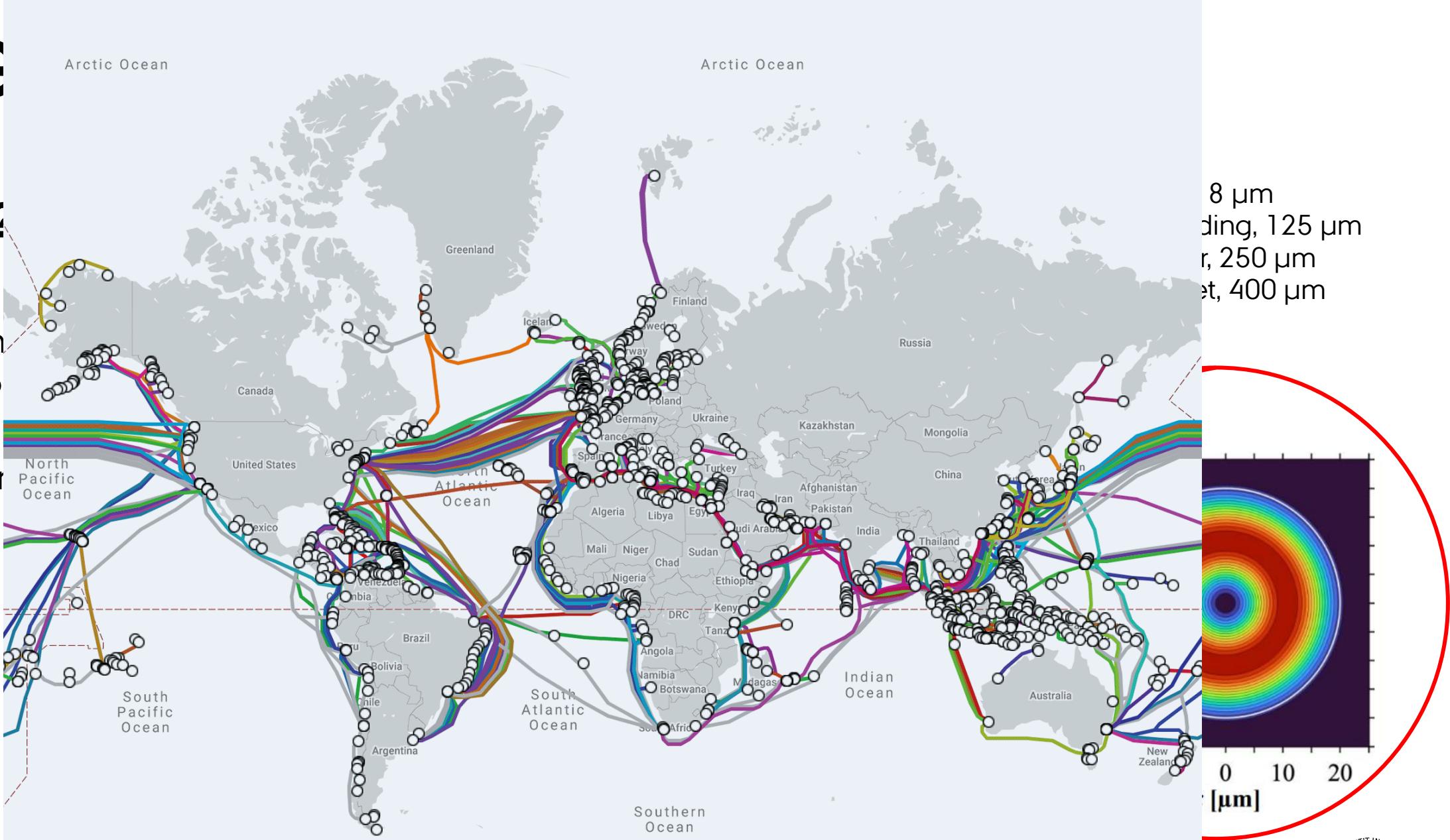
How?

- Confining light to **micro/nanoscale** structures opposed to **free-space** beams
- Example: **optical fibers**



1. Core, 8 μm
2. Cladding, 125 μm
3. Buffer, 250 μm
4. Jacket, 400 μm

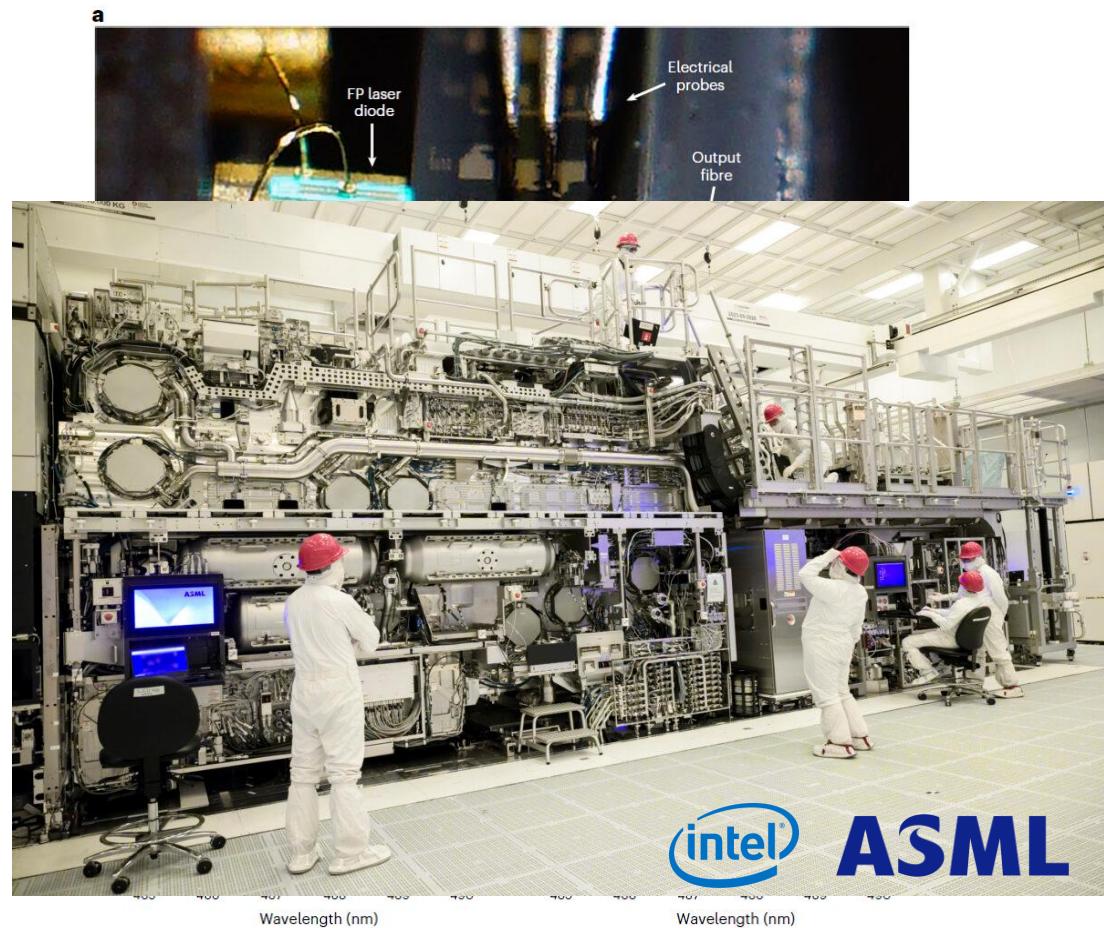
- Consider opportunities
- Examples



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How?

- Confining light to **micro/nanoscale** structures opposed to **free-space** beams
- Designing analogues of mirrors, resonators, filters etc. at the **chip-scale**
- Leveraging the nanofabrication expertise of the Silicon-based **CMOS** industry



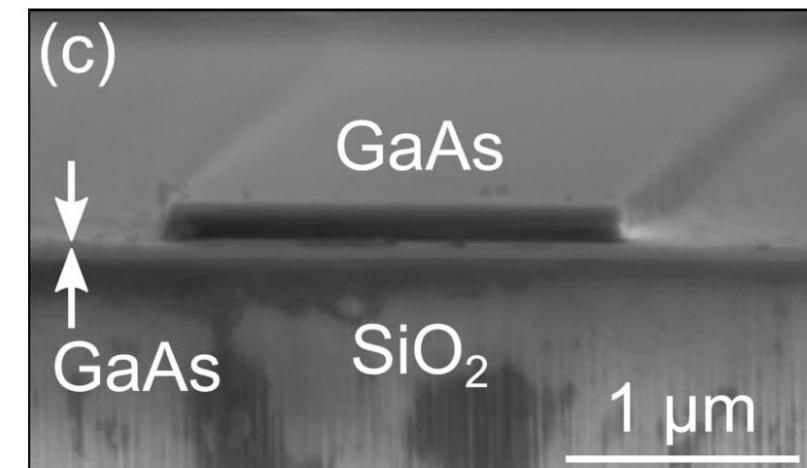
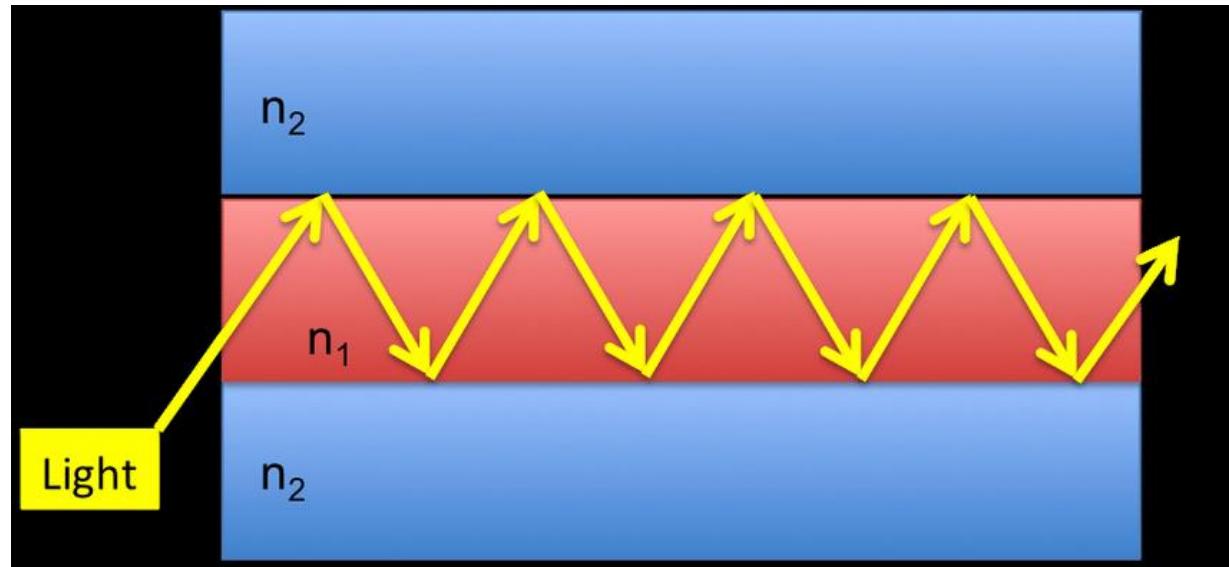
Corato-Zanarella *et al.* Widely tunable and narrow-linewidth chip-scale lasers from near-ultraviolet to near-infrared wavelengths. *Nat. Photon.* **17**, 157–164 (2023).



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Key concept: optical modes

- Linear **solutions to Maxwell's equations** in a material cross-section
- **Spatial** distribution of electric and magnetic fields
- Calculated **numerically** to design and evaluate PICs **before** fabrication



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Who?

Data centers:

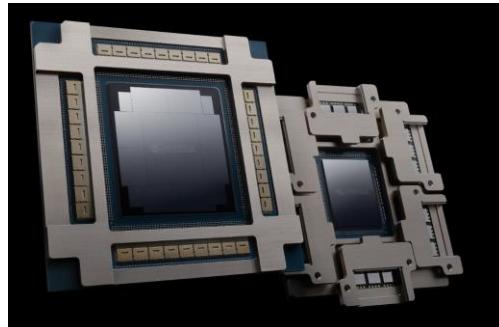


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Sensing:



Compute/quantum:

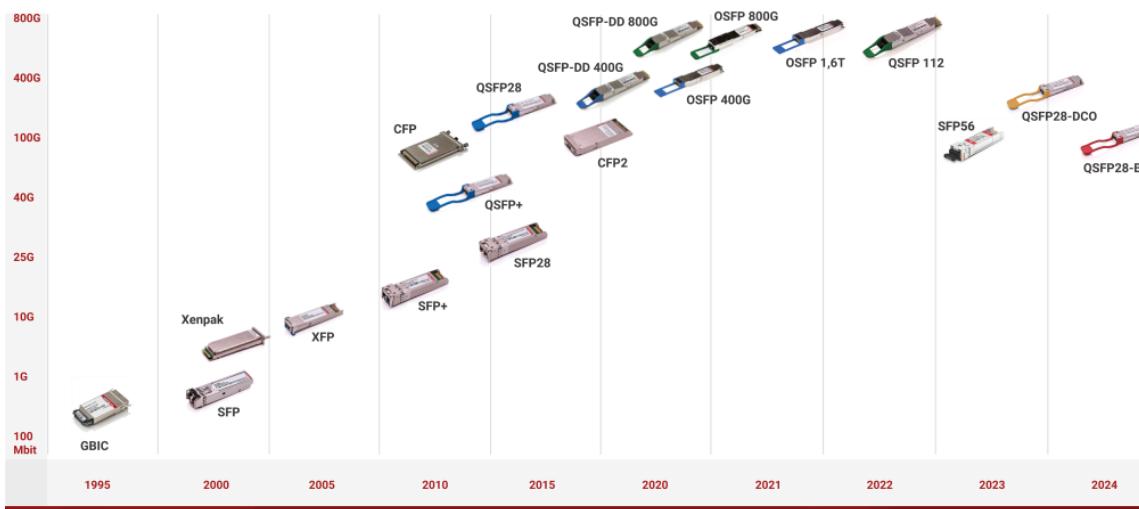
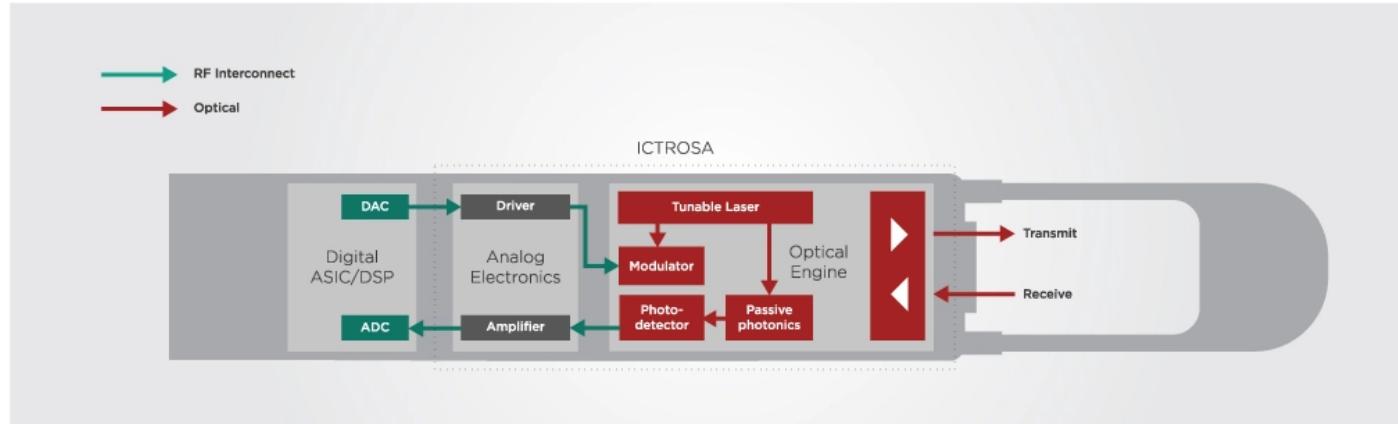
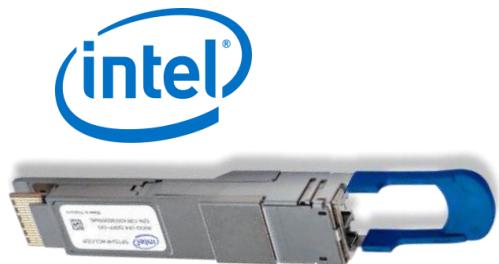


PsiQuantum



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Who?



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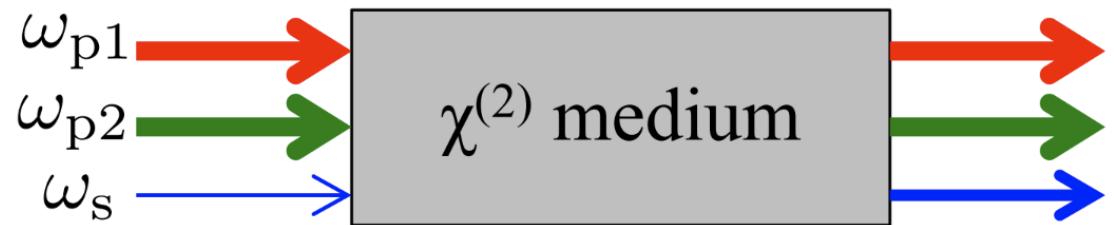
Key takeaways:

- Advanced optical systems at the **chip-scale**: PICs
- Based mainly on **Silicon**: CMOS-compatibility
- Enabling technology for the modern **Internet**,
sensors, and (coming) **quantum computers**

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What, why and how:

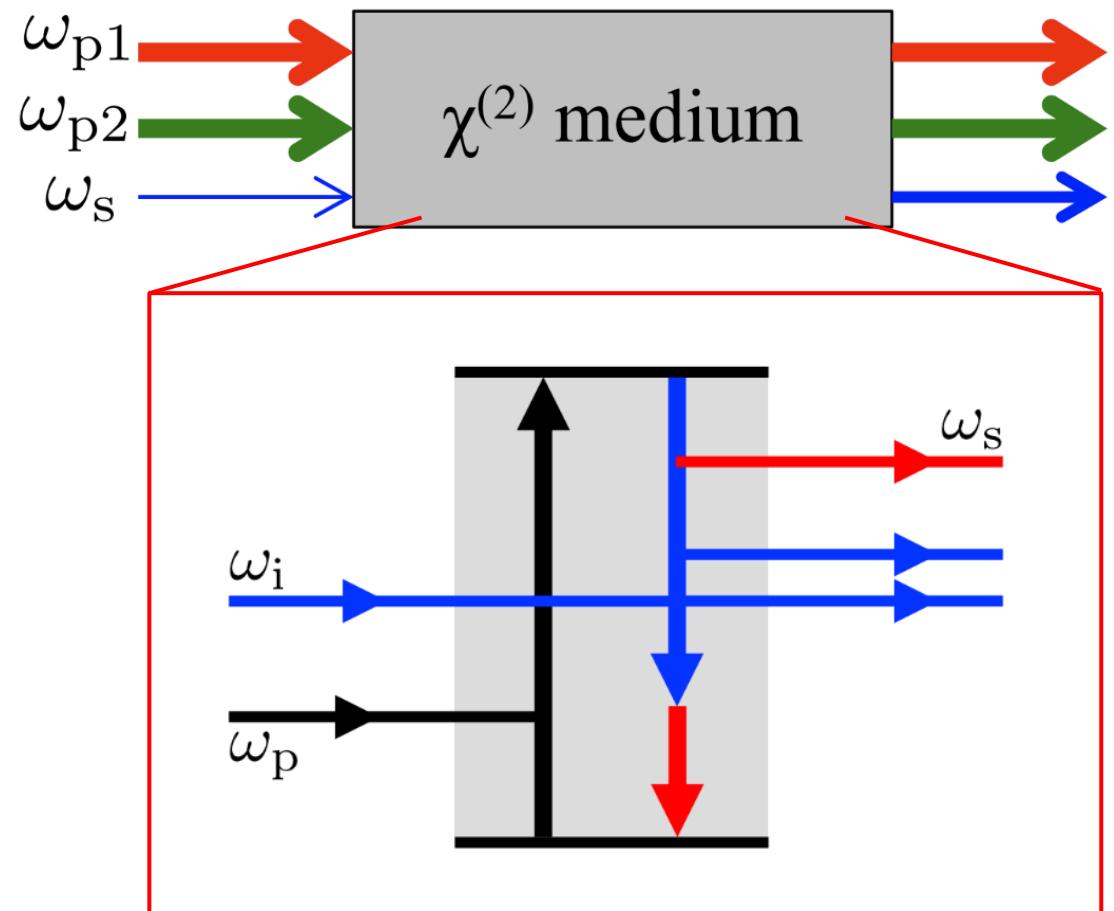
- Integrated photonics on a platform with a **nonlinear** optical response:
SiN, LiNbO₃, LiTaO₃, **GaAs**, InGaP ...
- Access to useful optical effects:
 - frequency conversion
 - frequency comb generation
 - supercontinuum generation
 - optical switching
 - etc.
- Depends on the **type** of nonlinearity: $\chi^{(2)}$ or $\chi^{(3)}$



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Example: $\chi^{(2)}$ -nonlinearity

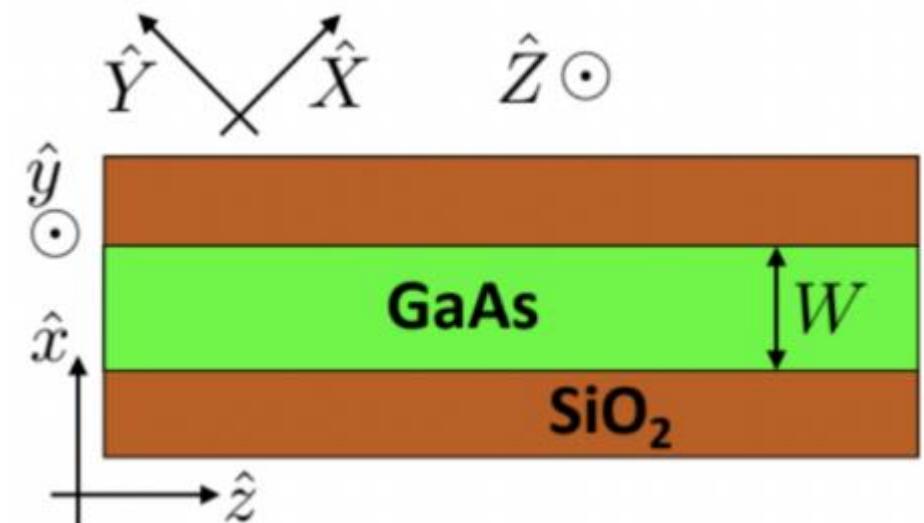
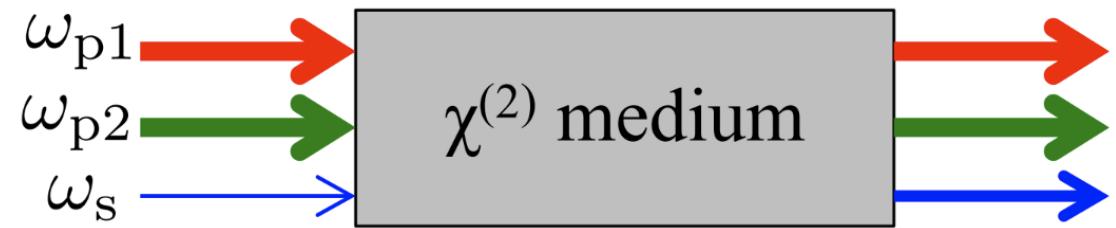
- Three-wave mixing
- Second-harmonic, difference-frequency and sum-frequency generation (SHG, DFG, SFG)



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Example: $\chi^{(2)}$ -nonlinearity

- Interaction is **mediated** by the **nonlinear polarization** of the medium
- Quantified by the nonlinear **tensor**, which depends on **crystal** geometry: $\hat{x}, \hat{y}, \hat{z} \neq \hat{X}, \hat{Y}, \hat{Z}$
- The tensor is a **material** property; **only** non-zero elements for **non-centrosymmetrical** crystals



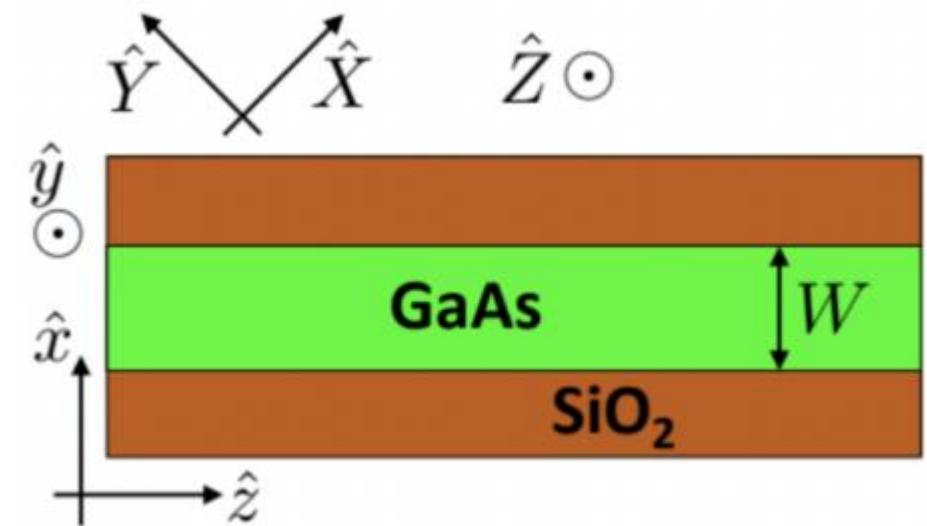
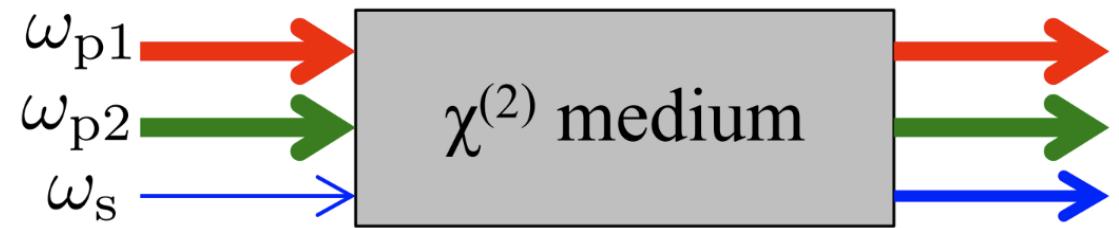
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Example: $\chi^{(2)}$ -nonlinearity

- Equation for the **generated** light:

$$\partial_z \mathcal{Z} = i \frac{\omega}{4Q} e^{-i\varphi} \iint_{\mathbb{R}^2} \vec{\mathcal{P}}^{\text{NL}} \cdot \vec{\epsilon}^* dx dy$$

- The **generated amplitude along z** results from **normalized signal mode** interaction with the **pump mode** and **nonlinear tensor** in the **waveguide cross-section** reliant on **phase matching**



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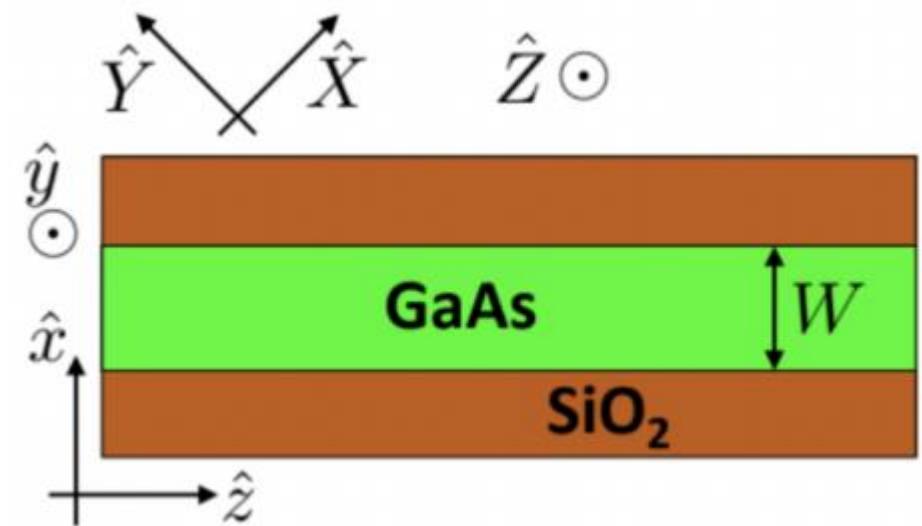
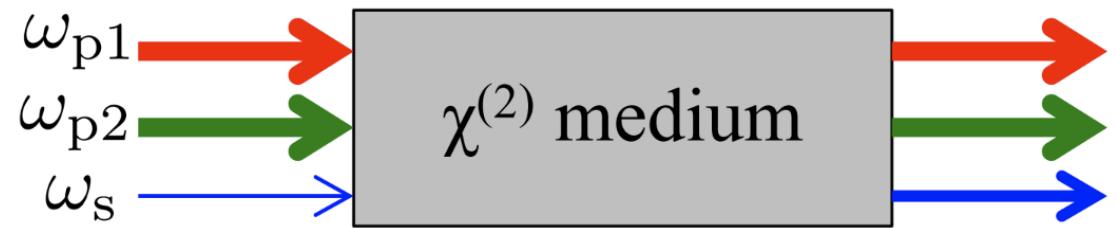
Example: $\chi^{(2)}$ -nonlinearity

- Factorize equation with $p1 = p2$:

$$\partial_z Z_s = i \frac{\omega_s}{c} \kappa e^{-i\Delta kz} Z_p^2$$

- The **strength** of the **nonlinear coupling** is quantified by:

$$\kappa_\nu \equiv \frac{c\varepsilon_0}{2Q} \iint_{\mathbb{R}^2} (D\vec{v}_\nu) \cdot \vec{\epsilon}_\nu^* \, dx \, dy$$



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$$\frac{\partial_z Z_s}{Z_p} = i \frac{\omega_s}{c} \kappa e^{-i\Delta kz} Z_p^2$$

$$\underline{\kappa_\nu} \equiv \frac{c\varepsilon_0}{2Q} \iint_{\mathbb{R}^2} (\underline{D\vec{v}_\nu}) \cdot \underline{\vec{\epsilon}_\nu^*} dx dy$$

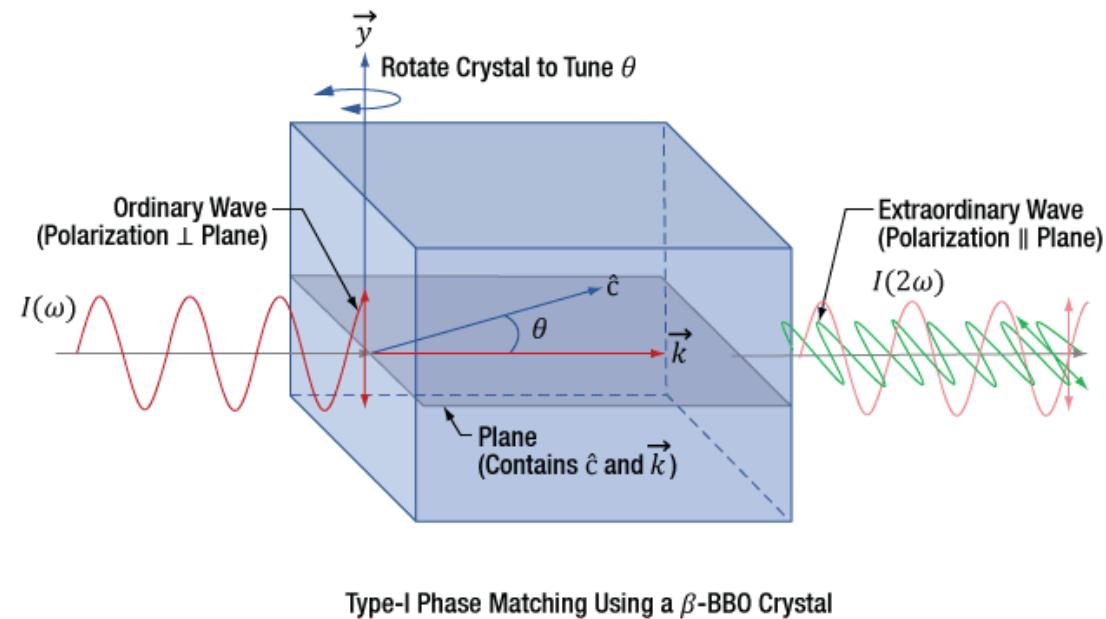
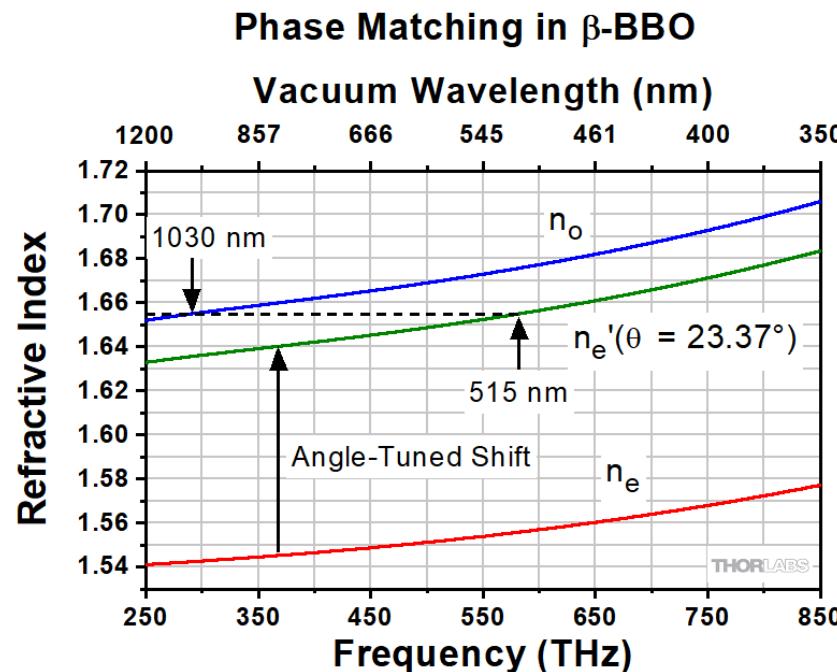
- The **signal generated** along **z** depends on the **coupling coefficient**, the **phase matching** and the **pump amplitude squared**
- The **coupling coefficient** is **static** and depends on the **normalized cross-sectional interaction** between the **pump mode** and **signal mode** through the **nonlinear tensor**

From Prof. Galland's notes:

$$\frac{\partial A_\alpha}{\partial z} = \frac{i\omega_\alpha c}{2n_\alpha} \chi_{\text{eff}}^{(n)} A_1^{(*)}(z) \dots A_n^{(*)}(z) e^{i\Delta k z}$$

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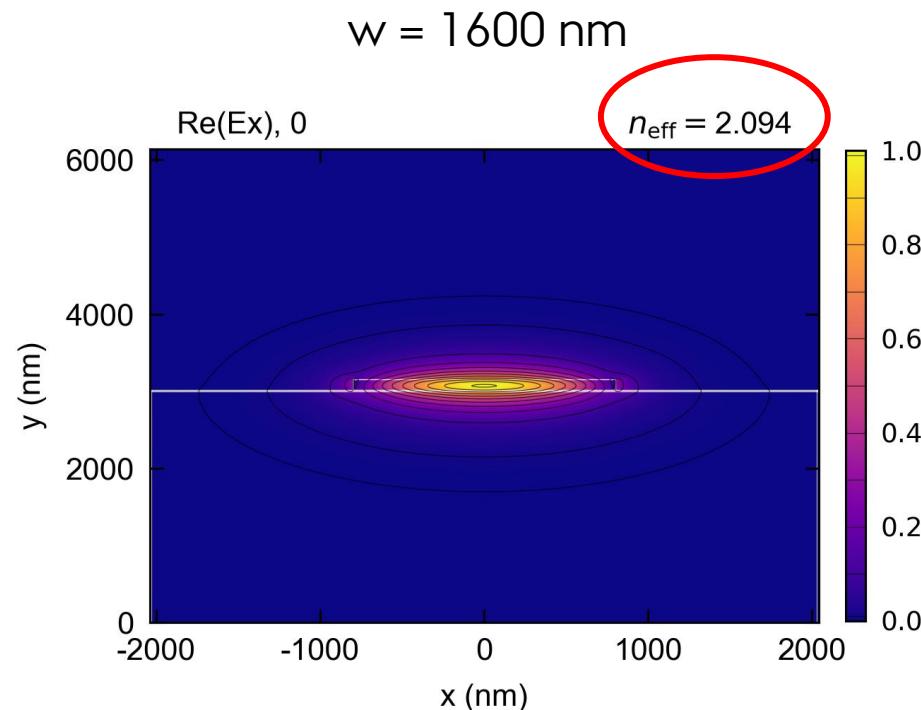
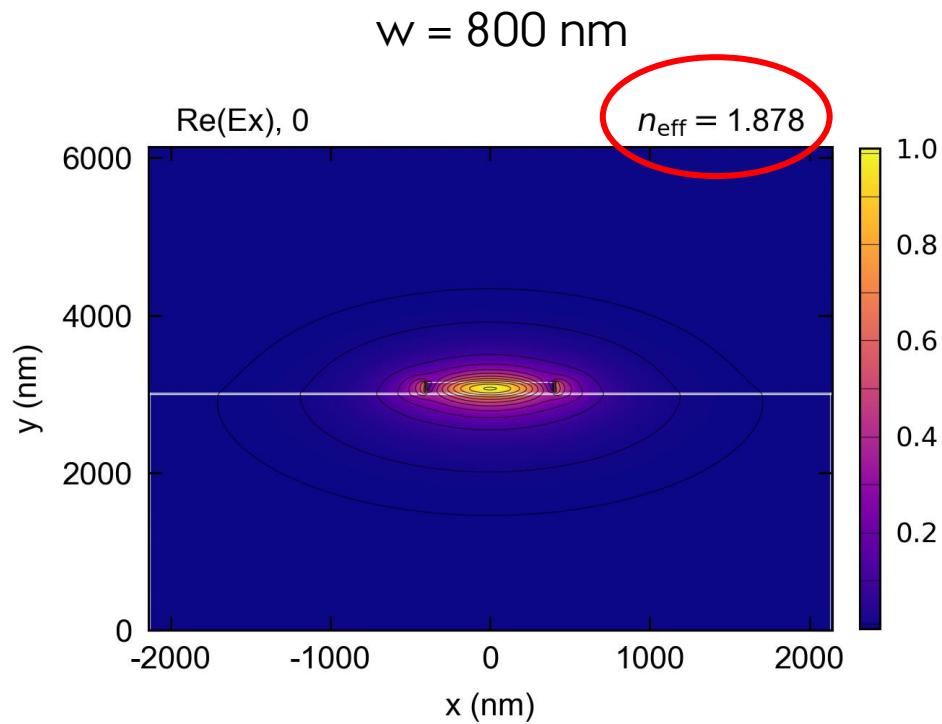
Key concept: phase matching



Thorlabs: BBO Crystals for Second Harmonic Generation:
https://www.thorlabs.com/newgroupage9.cfm?objectgroup_id=15444

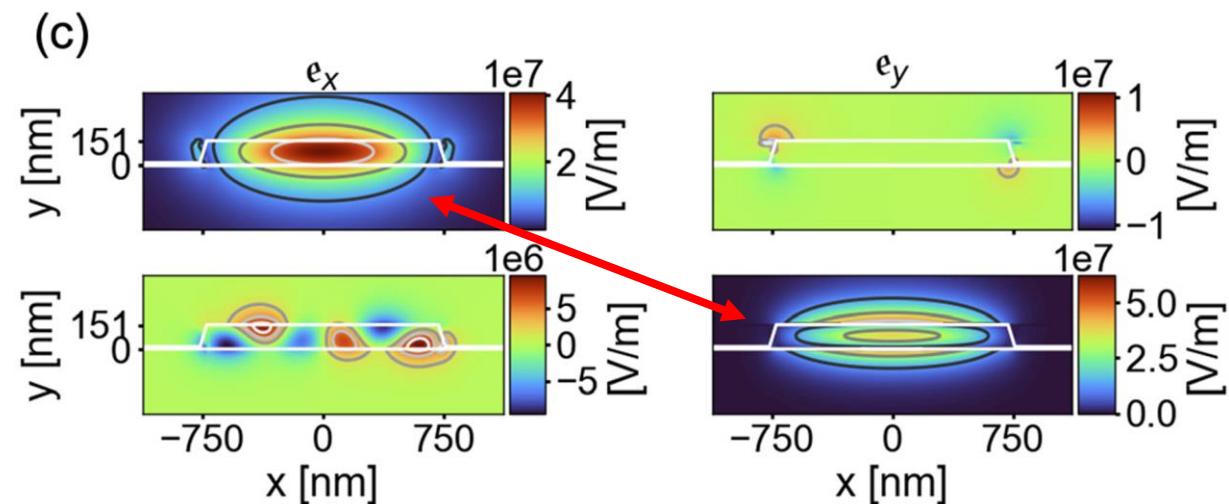
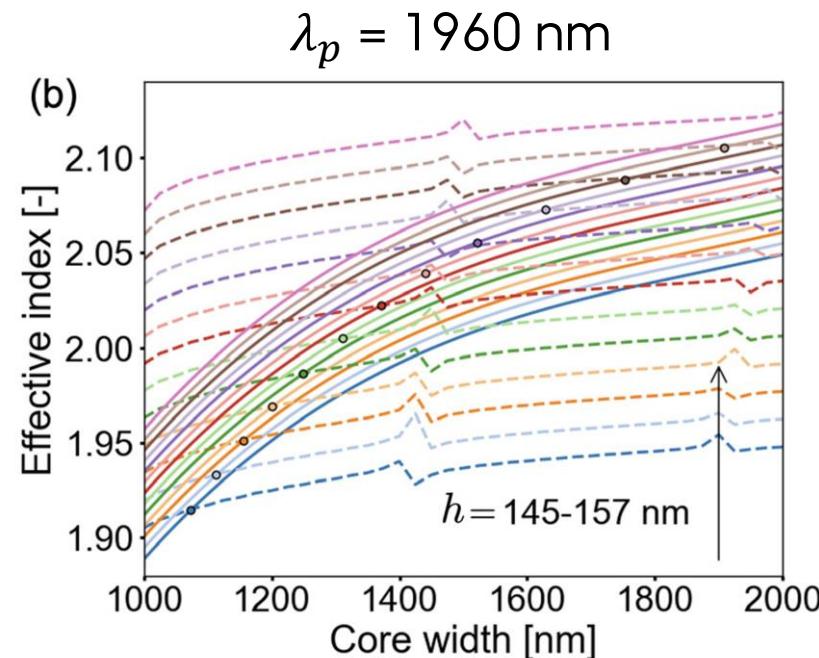
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- Dispersion engineering to adjust **effective** refractive index



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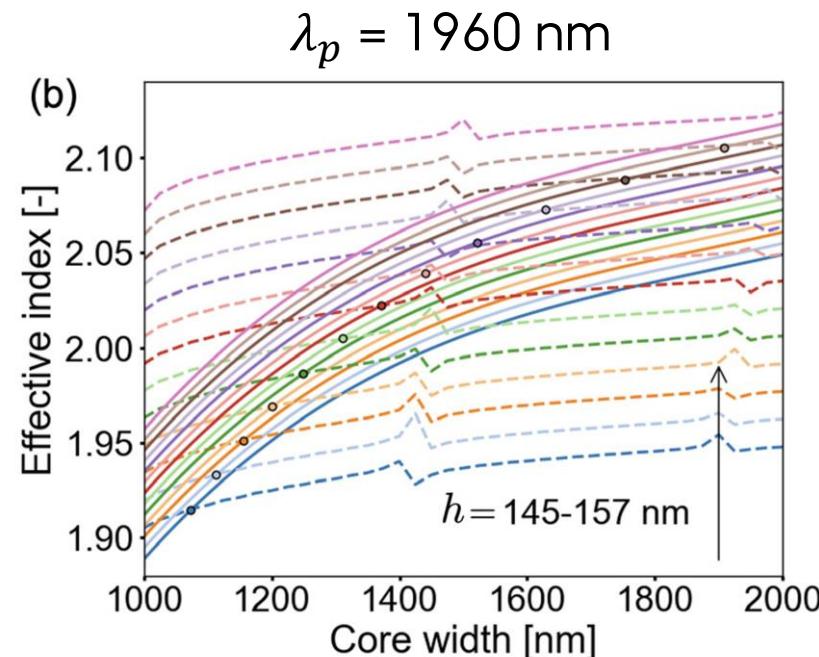
Key concept: phase matching



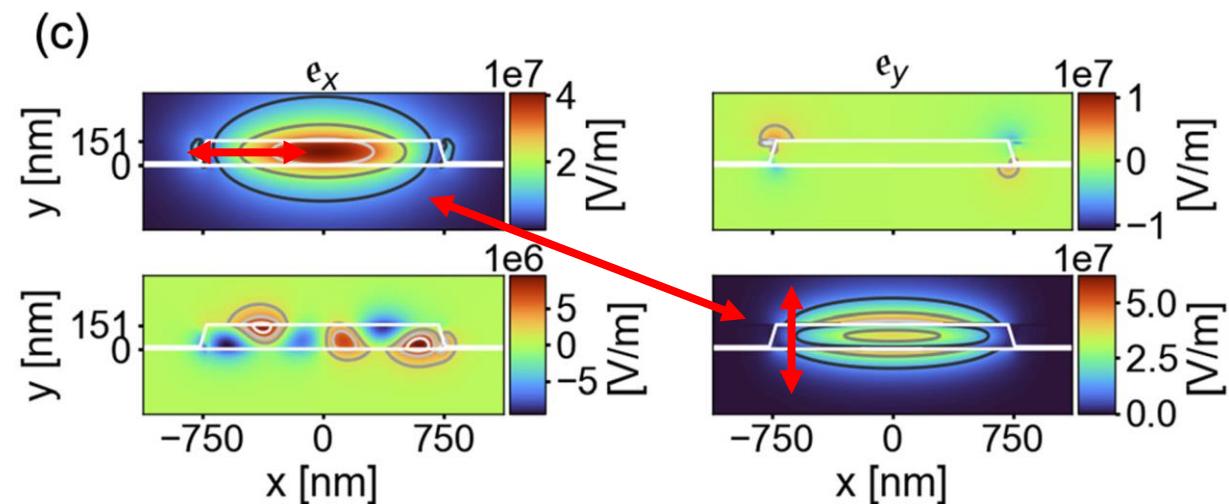
Emil Z. Ulsig *et. al.*, "Efficient and widely tunable mid-infrared sources using GaAs and AlGaAs integrated platforms for second-order frequency conversion," Opt. Express 32, 36986-37000 (2024)

INTEGRATED NONLINEAR PHOTONICS

Key concept: phase matching



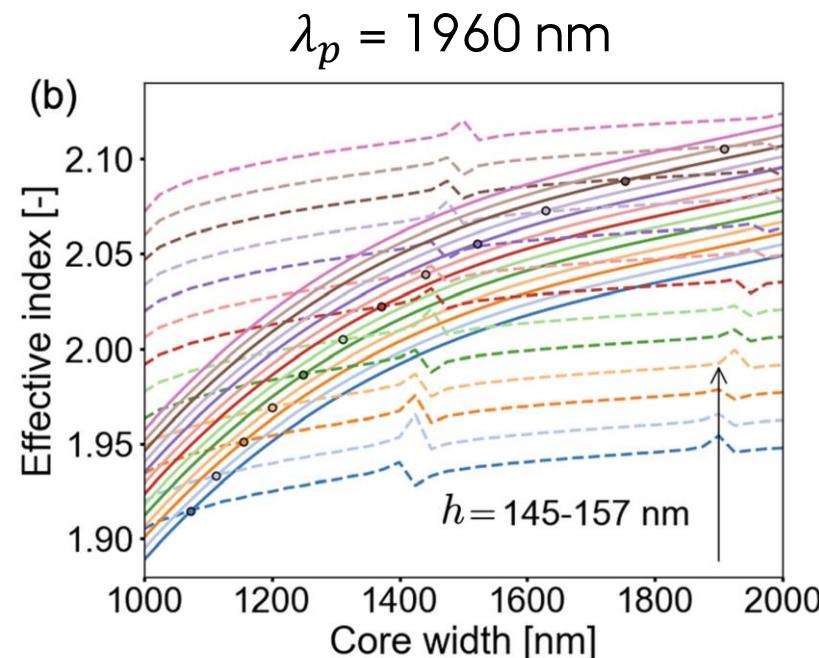
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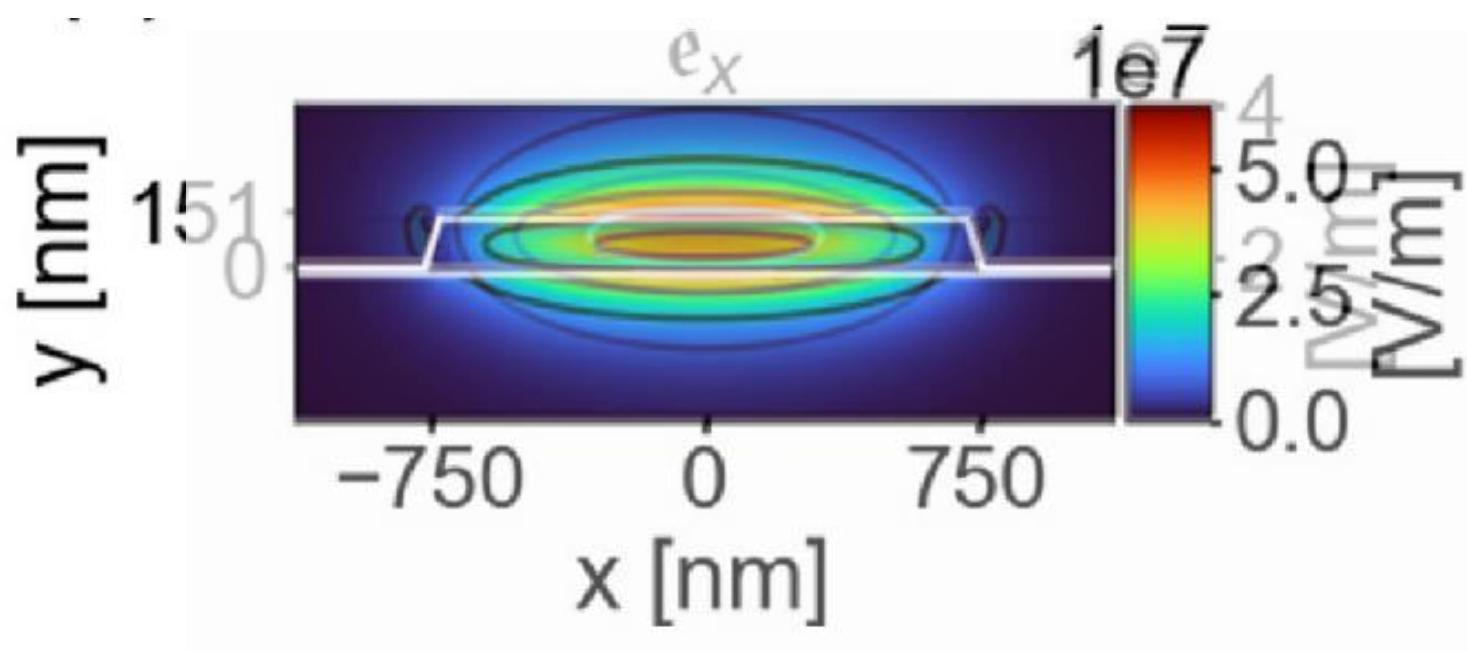
$$\kappa_\nu \equiv \frac{c\epsilon_0}{2Q} \iint_{\mathbb{R}^2} (D\vec{v}_\nu) \cdot \vec{e}_\nu^* \, dx \, dy$$

INTEGRATED NONLINEAR PHOTONICS

Key concept: phase matching



Emil Z. Ulsig *et. al.*, "Efficient and widely tunable mid-infrared sources using GaAs and AlGaAs integrated platforms for second-order frequency conversion," Opt. Express 32, 36986-37000 (2024)

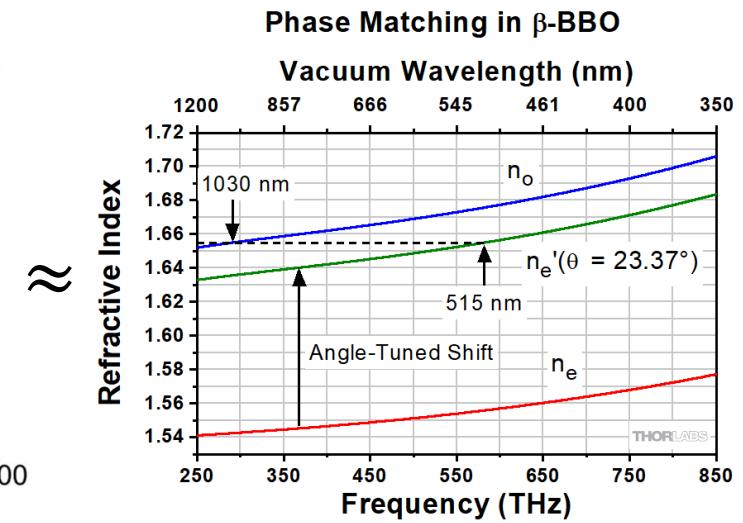
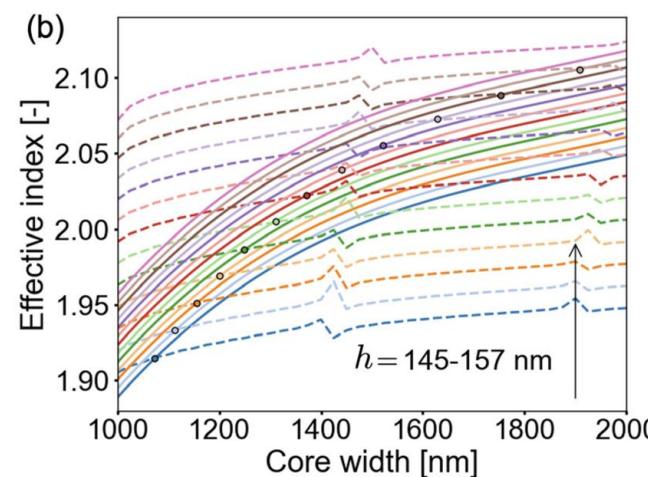


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INTEGRATED NONLINEAR PHOTONICS

Key concept: phase matching

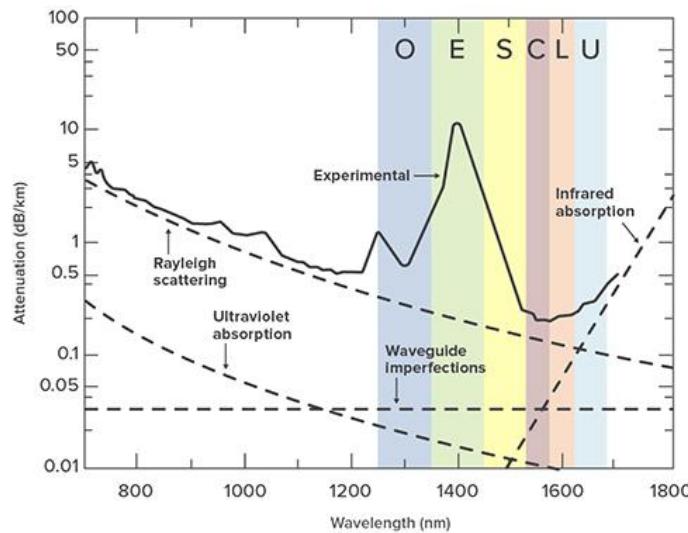
- In integrated photonics: **independent** of birefringence
- Conversion **strength** depends on **mode overlap**
- Enables **more** materials for frequency conversion, e.g. **GaAs**



Emil Z. Ulsig *et. al.*, "Efficient and widely tunable mid-infrared sources using GaAs and AlGaAs integrated platforms for second-order frequency conversion," Opt. Express 32, 36986-37000 (2024)

EXAMPLE: C-BAND SINGLE PHOTONS

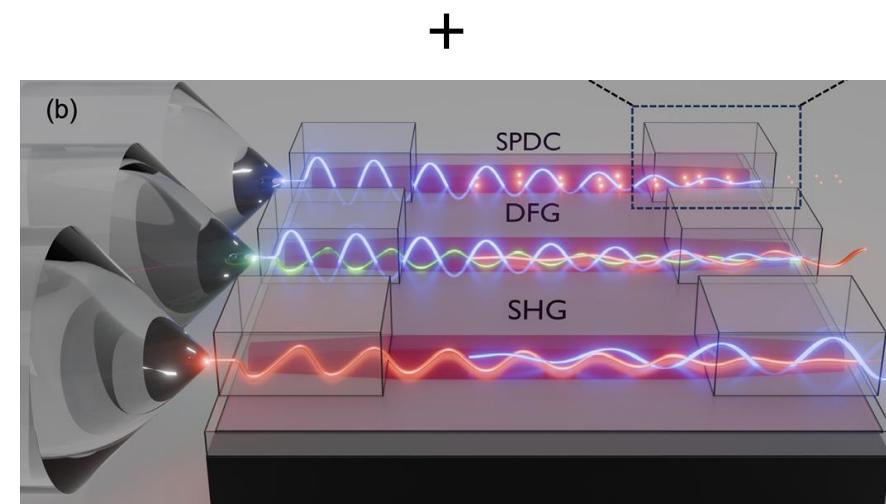
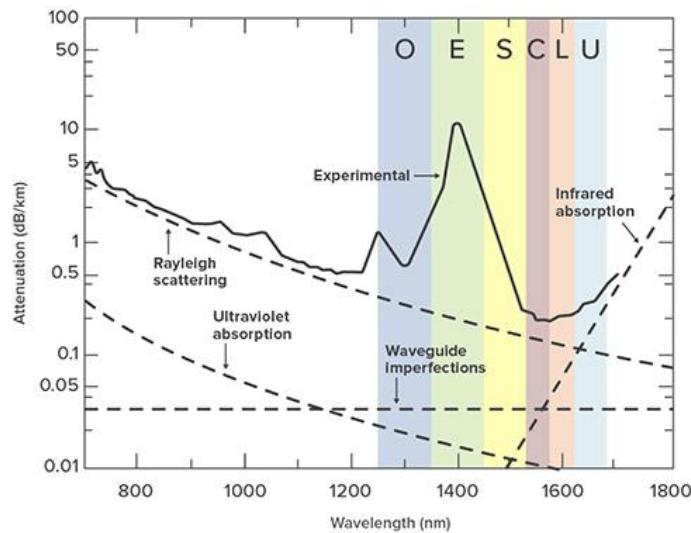
- Danish propaganda:
commercially available single-photon source
- Based on a **photonic integrated circuit (PIC)**
- Emission wavelength: **920-980 nm**



<https://sparrowquantum.com/>

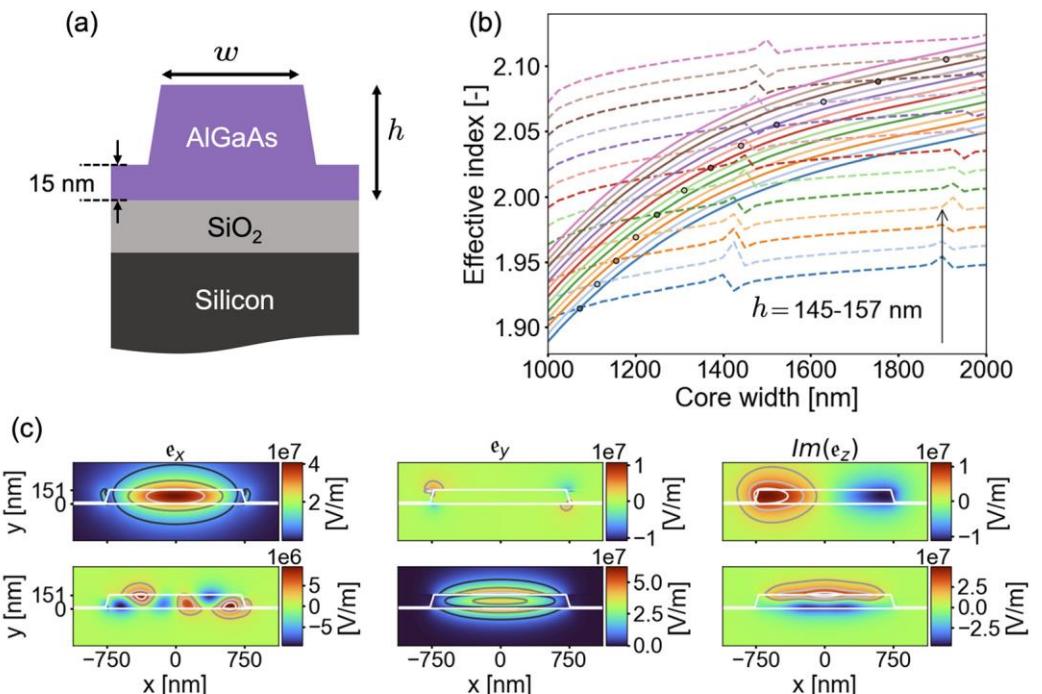
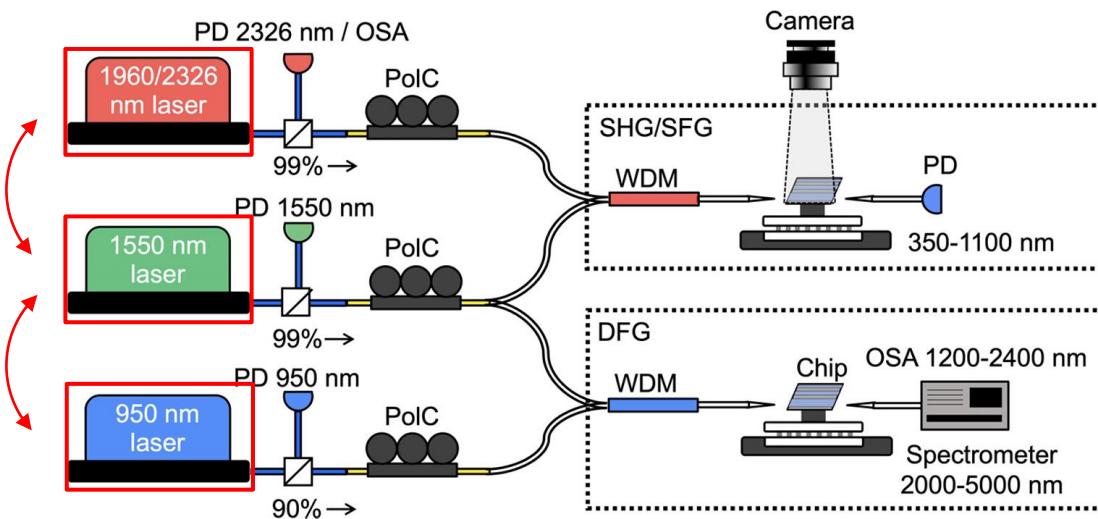
EXAMPLE: C-BAND SINGLE PHOTONS

- Retain **efficient & pure** single-photon generation
- Enable integration with **telecom** networks
- **Single-platform** integration (GaAs)



EXAMPLE: C-BAND SINGLE PHOTONS

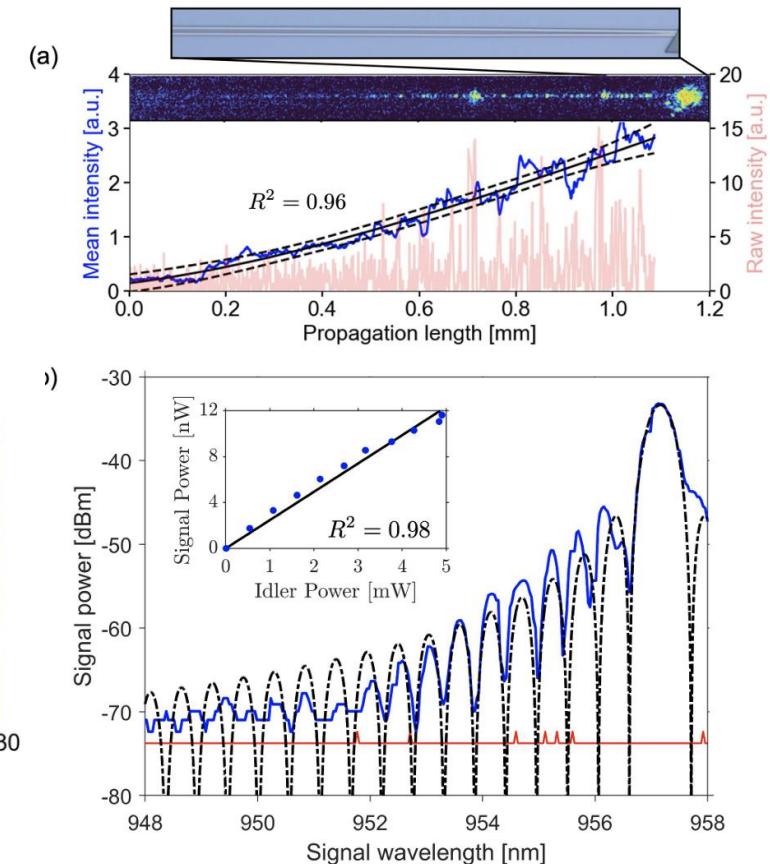
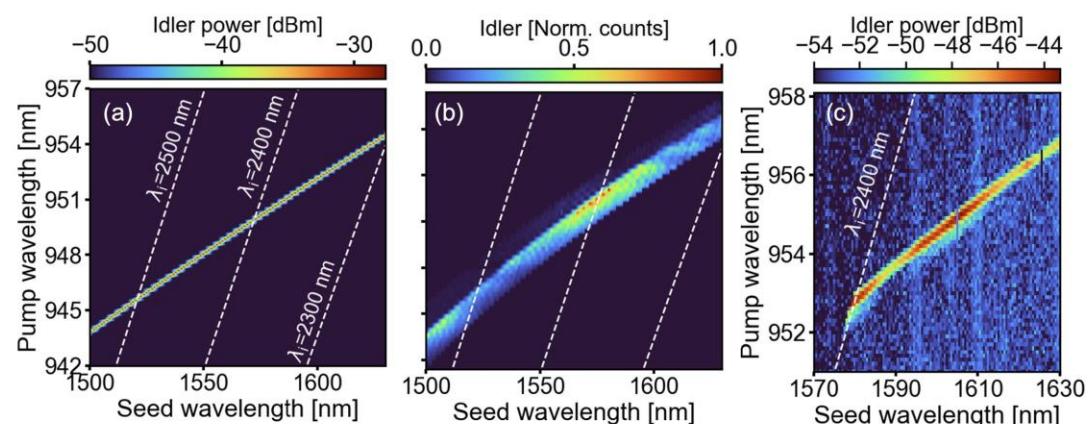
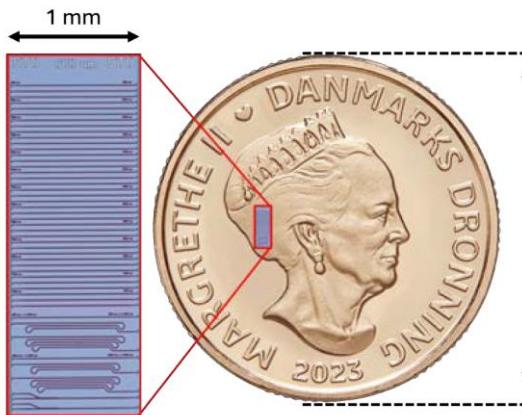
- **Sum and difference-frequency** generation (S/D FG):
Three-wave mixing: P(ump), S(ignal), I(dler)
- **Modal phase matching:** $n_s = n_p$



Emil Z. Ulsig *et. al.*, "Efficient and widely tunable mid-infrared sources using GaAs and AlGaAs integrated platforms for second-order frequency conversion," Opt. Express 32, 36986-37000 (2024)

EXAMPLE: C-BAND SINGLE PHOTONS

- **DFG** and **SFG** between ~ 950 nm and 1550 nm
- Exercise: SHG in GaAs waveguides



Emil Z. Ulsig *et. al.*, "Efficient and widely tunable mid-infrared sources using GaAs and AlGaAs integrated platforms for second-order frequency conversion," Opt. Express 32, 36986-37000 (2024)

EXAMPLE: DEEP-UV GENERATION

- 2014 Nobel Prize: Nakamura, Amano & Akasaki
"for the invention of efficient blue light-emitting diodes which has enabled bright and energy-saving white light sources"

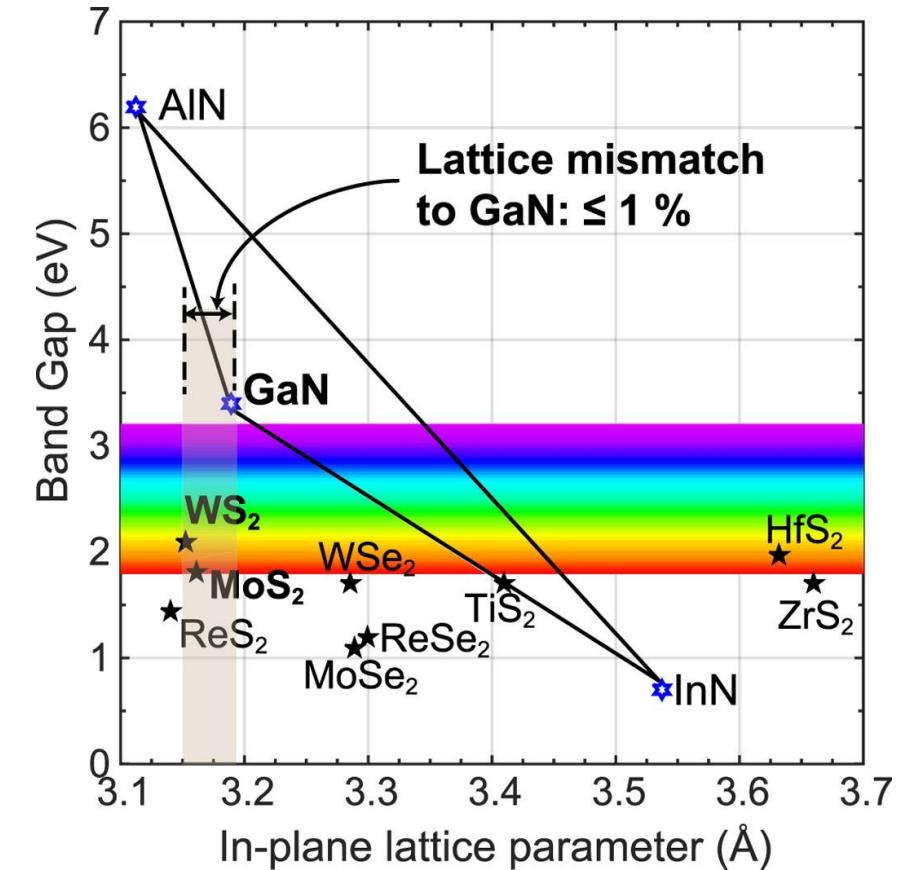


Veritasium: "Why it was almost impossible to make the blue LED":
<https://www.youtube.com/watch?v=AF8d72mA41M>



EXAMPLE: DEEP-UV GENERATION

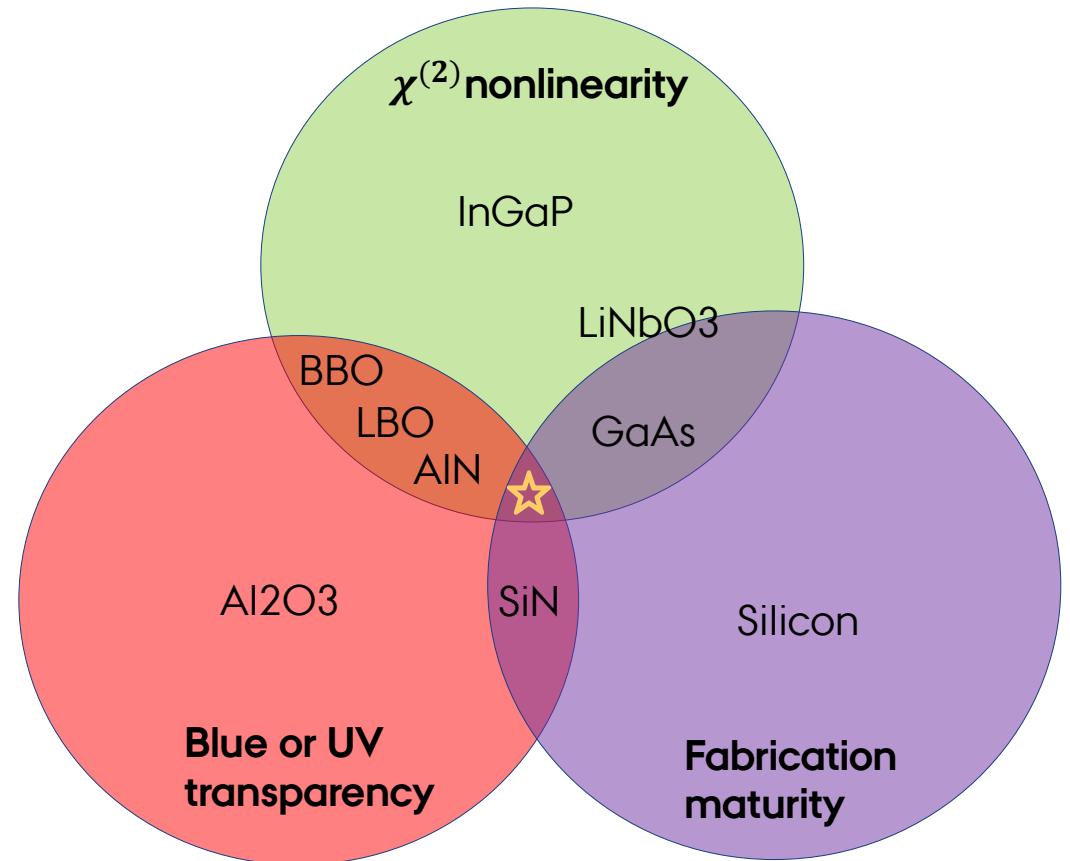
- AlInGaN-based compounds:
Cover the **entire visible range** down to the deep-UV
- Demonstrated WPE (wall-plug efficiency) of >80%
- World record for laser emission: **271.8 nm**
By laureate Amano's group
- Immense difficulties at very short wavelengths
 - growth defects
 - p-type doping
 - light extraction
 - etc.



Gupta, P., Rahman, A., Subramanian, S. *et al.* Layered transition metal dichalcogenides: promising near-lattice-matched substrates for GaN growth. *Sci Rep* **6**, 23708 (2016).

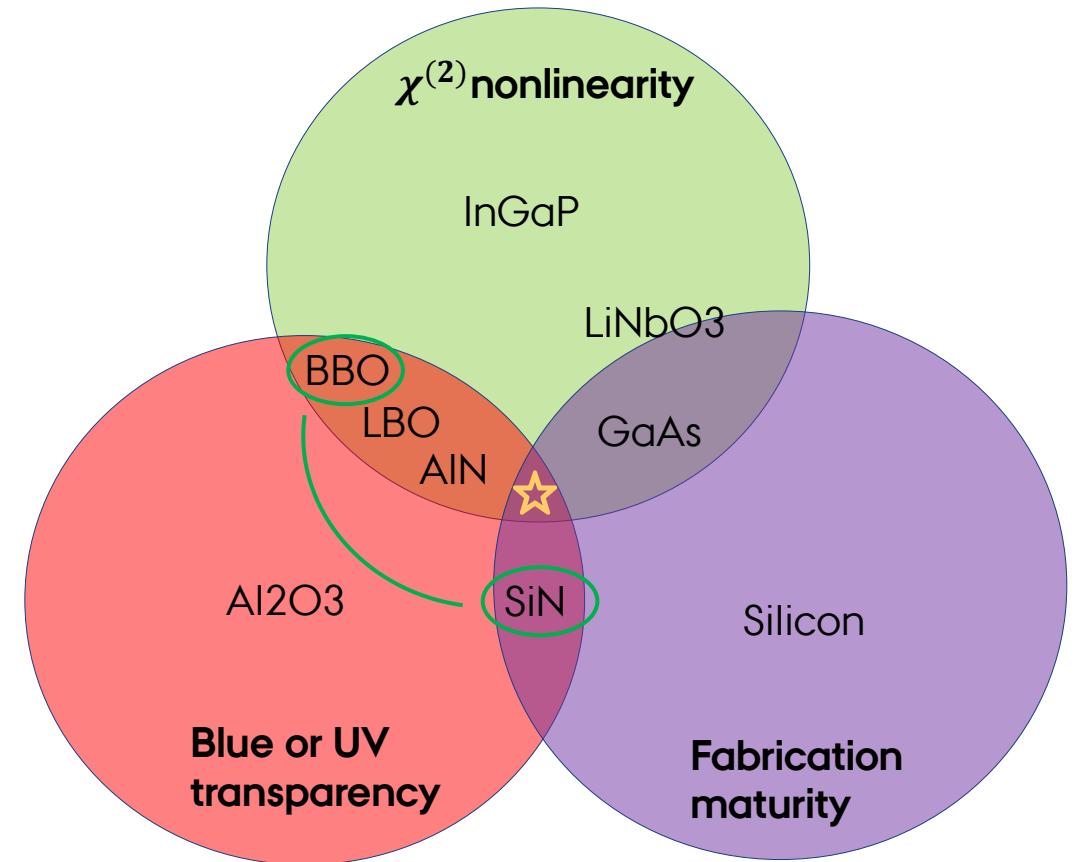
EXAMPLE: DEEP-UV GENERATION

- Potential solution: **nonlinear photonics**
- Allows for **compact** form-factor while “cheating” the bandgap
- **Photonic integration** of (active) pump laser and (passive) conversion chip
- Challenge: suitable **platform**

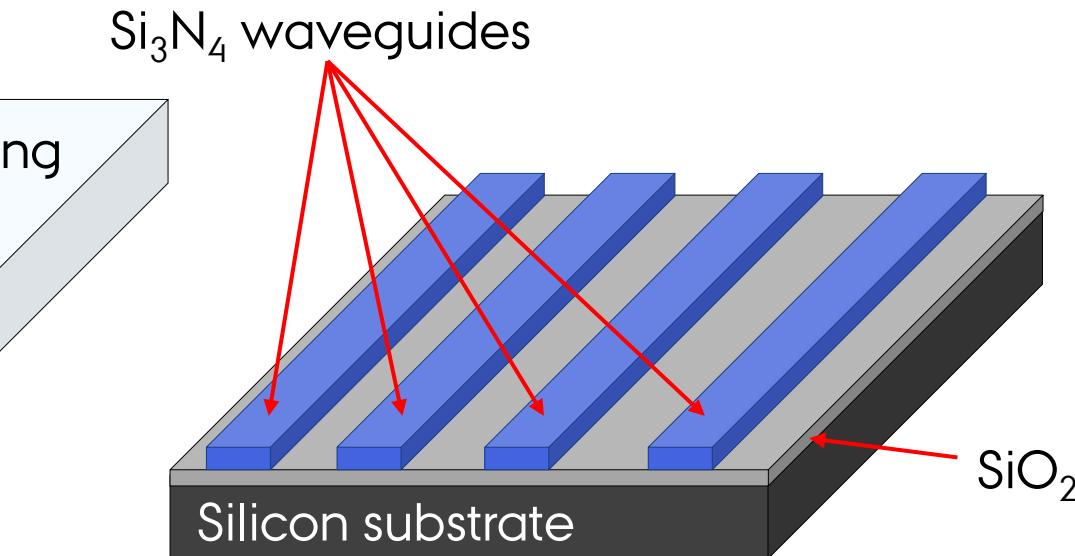
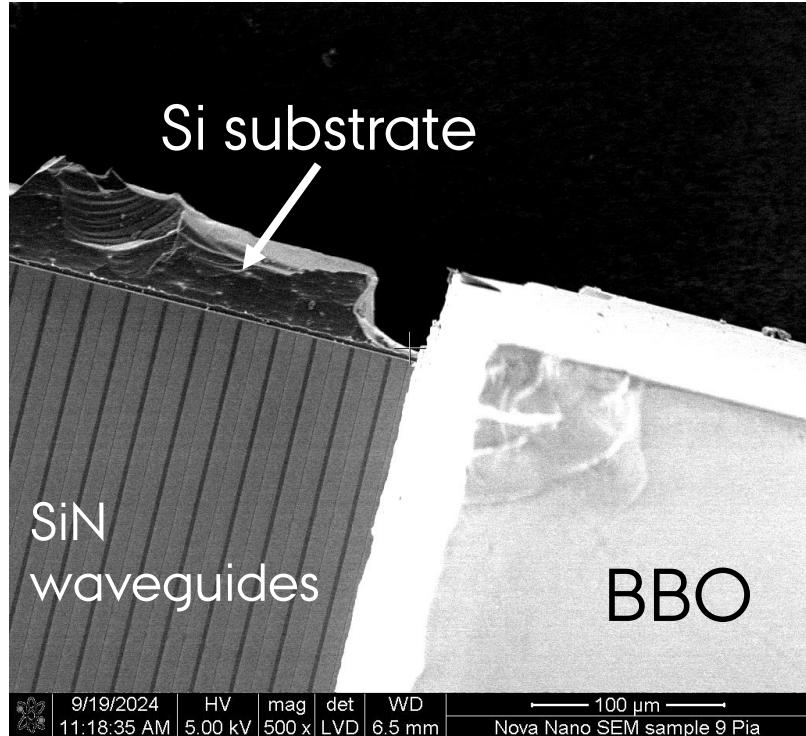


EXAMPLE: DEEP-UV GENERATION

- Solution: **heterogeneous** integration:
Combine **BBO** with **SiN**
- Leverage complimentary properties:
BBO: $\chi^{(2)}$ **nonlinearity**, **UV** transparency
SiN: Mature fabrication, **blue** transparency



EXAMPLE: DEEP-UV GENERATION

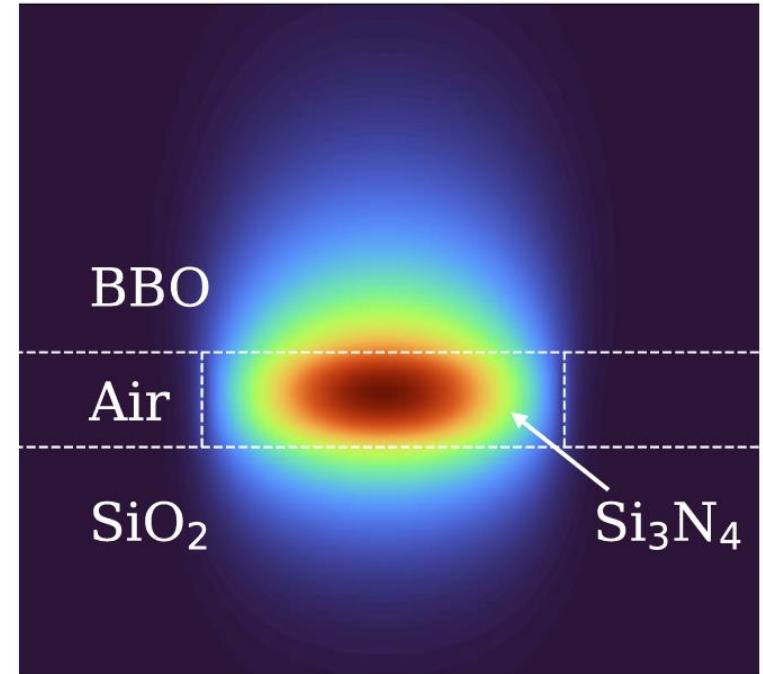
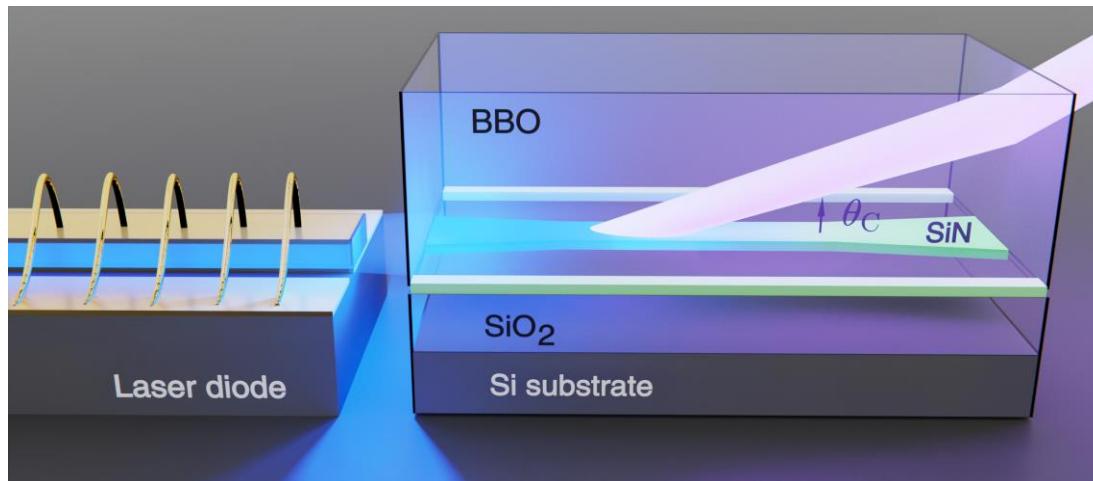


EXAMPLE: DEEP-UV GENERATION

- Challenge: **no** $\chi^{(2)}$ in waveguides

- Solution: **Cerenkov-type** SHG:

$$\cos(\theta_C) = \frac{n_p}{n_s}, \quad n_p < n_s$$



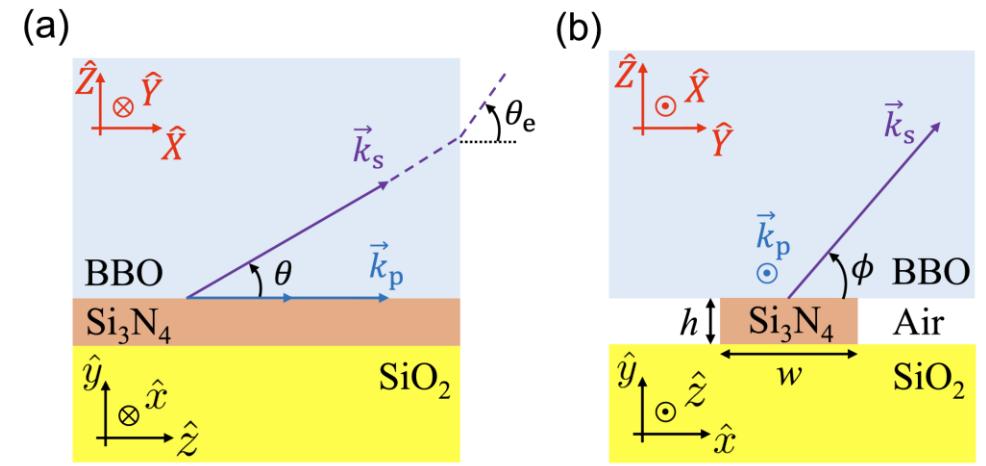
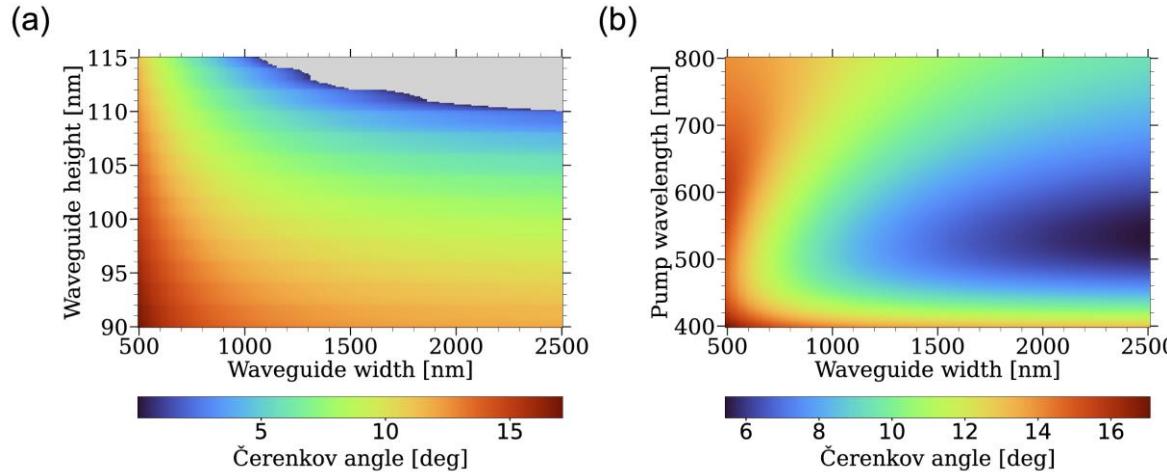
Asger B. Gardner *et. Al.*, "Robust and broadband UV laser utilizing Čerenkov phase matching on a hybrid photonic chip," Opt. Express 33, 19330-19341 (2025)



EXAMPLE: DEEP-UV GENERATION

- Maintains phase matching over a **broad** parameter space:

$$\cos(\theta_C) = \frac{n_p}{n_s}, \quad n_p < n_s$$

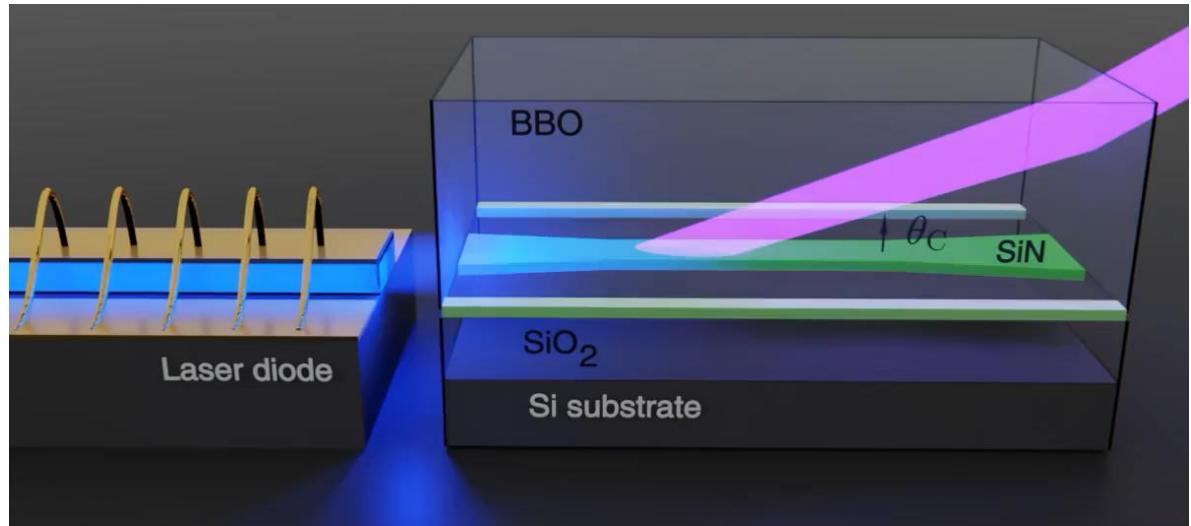
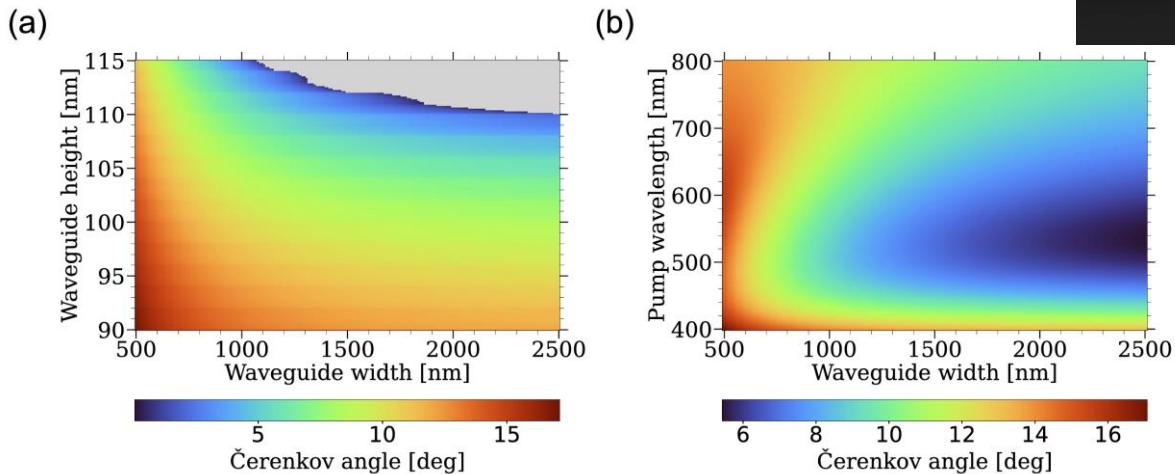


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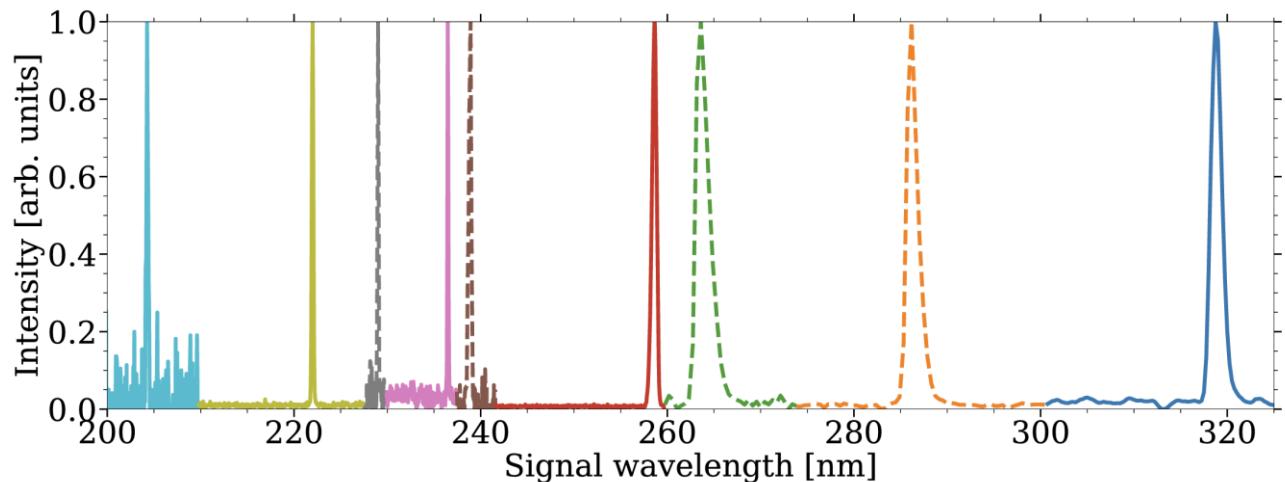
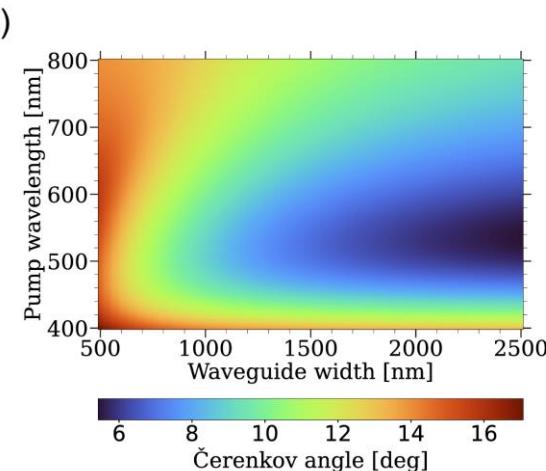
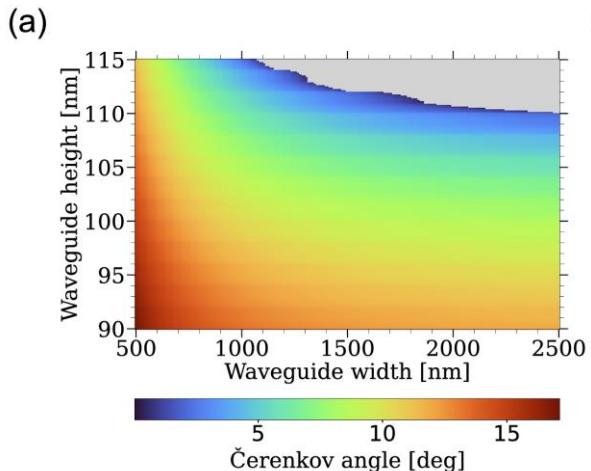
Asger B. Gardner *et. Al.*, "Robust and broadband UV laser utilizing Čerenkov phase matching on a hybrid photonic chip," Opt. Express 33, 19330-19341 (2025)



EXAMPLE: DEEP-UV GENERATION

- Maintains phase matching over a **broad** parameter space:

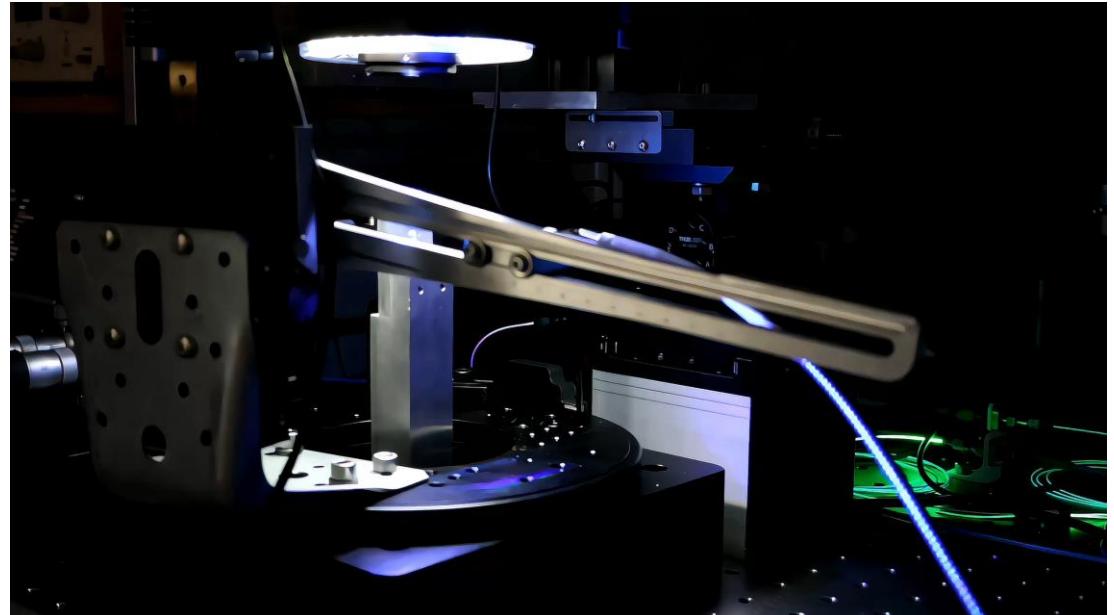
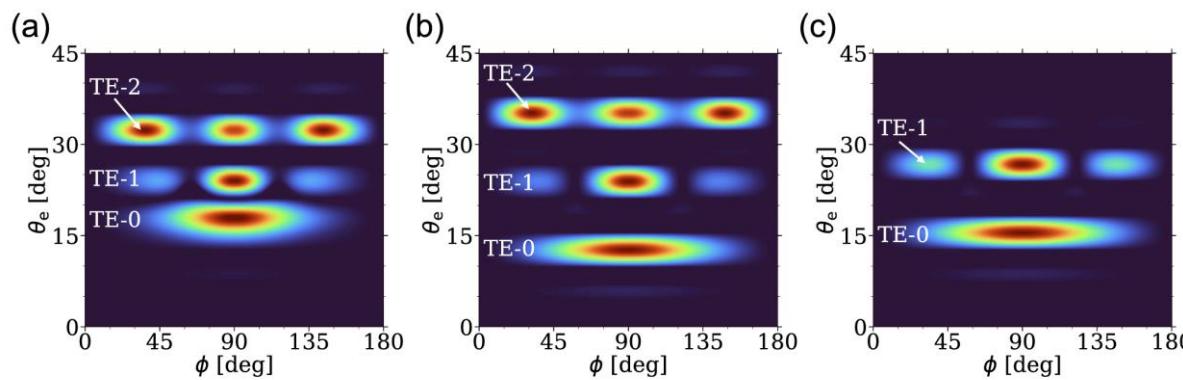
$$\cos(\theta_C) = \frac{n_p}{n_s}, \quad n_p < n_s$$



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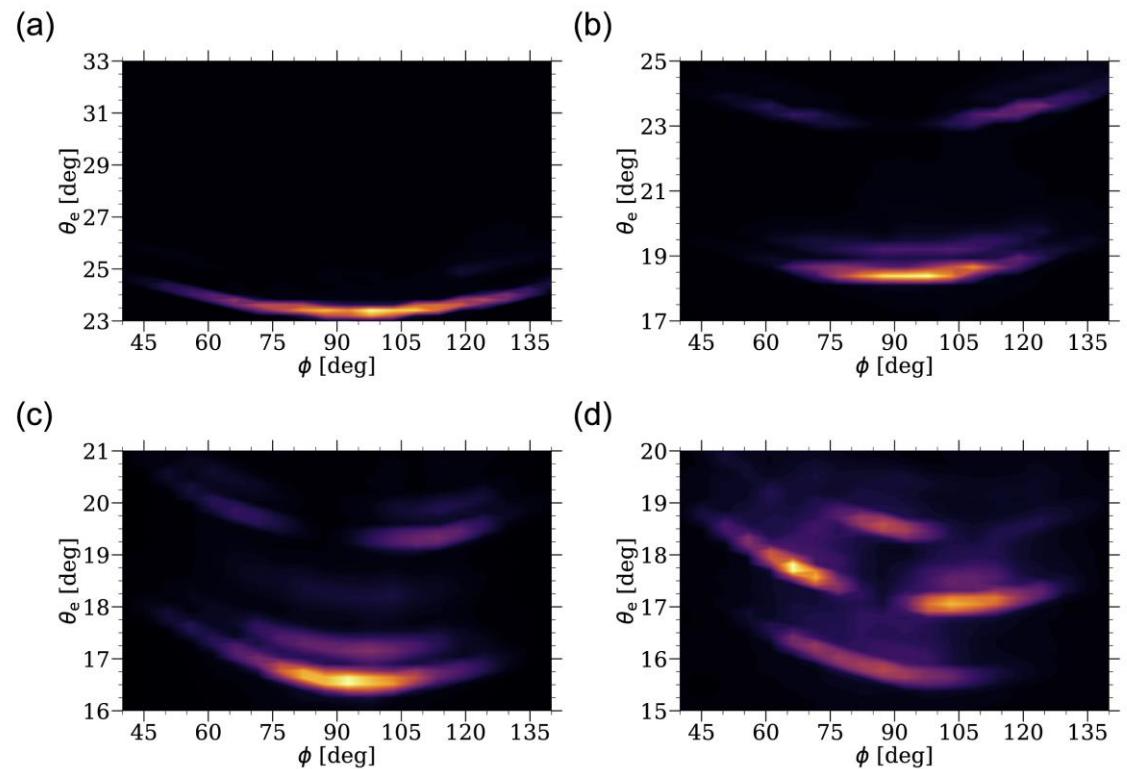
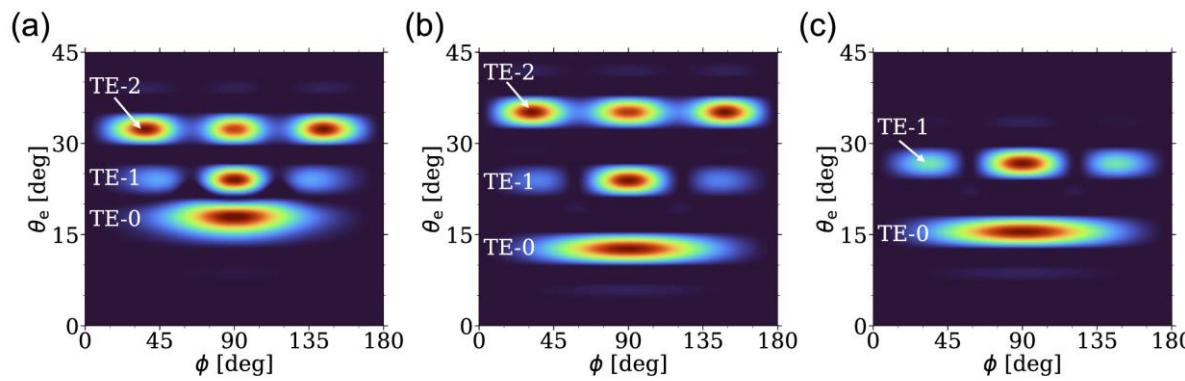
- Generated light is **free-space**
- Results in complex output distribution



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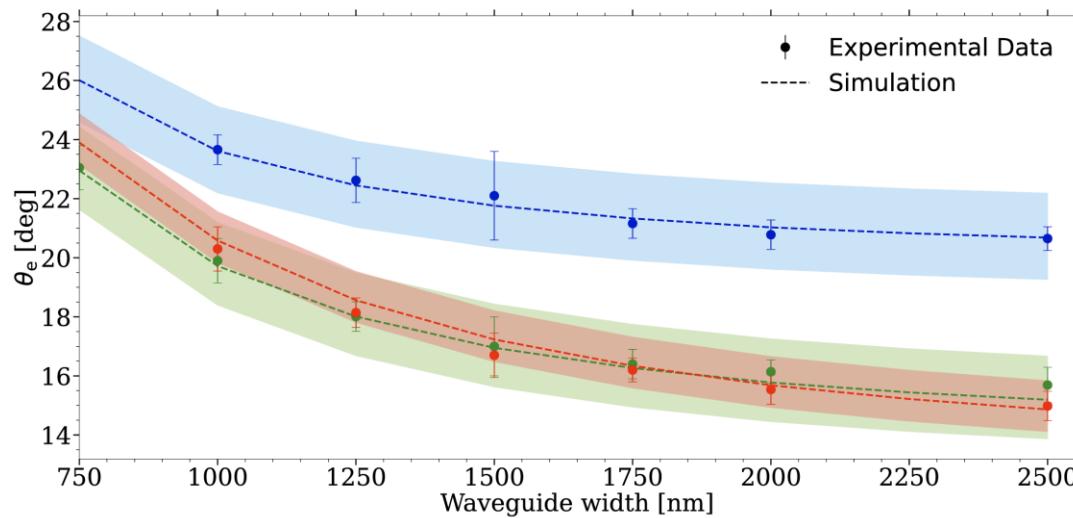


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EXAMPLE: DEEP-UV GENERATION

- Extremely **robust** phase matching process
- Broadband coverage from single waveguides



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WRAP-UP

- Introduction to **integrated photonics**
- Introduction to **nonlinear** effects in photonic integrated circuits
- Two examples:
 - Frequency conversion for quantum applications
 - Deep-UV generation
- **Exercise** on SHG in a GaAs waveguide





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