A visualization of the cosmic web, showing a complex network of filaments and clusters of galaxies. The background is a deep blue, with the filaments and clusters appearing in shades of purple, magenta, and bright yellow-orange. A horizontal scale bar is positioned in the upper middle of the image.

31.25 Mpc/h

Astrophysics III

Formation and Evolution of galaxies

Michaela Hirschmann, Fall-Winter semester 2024

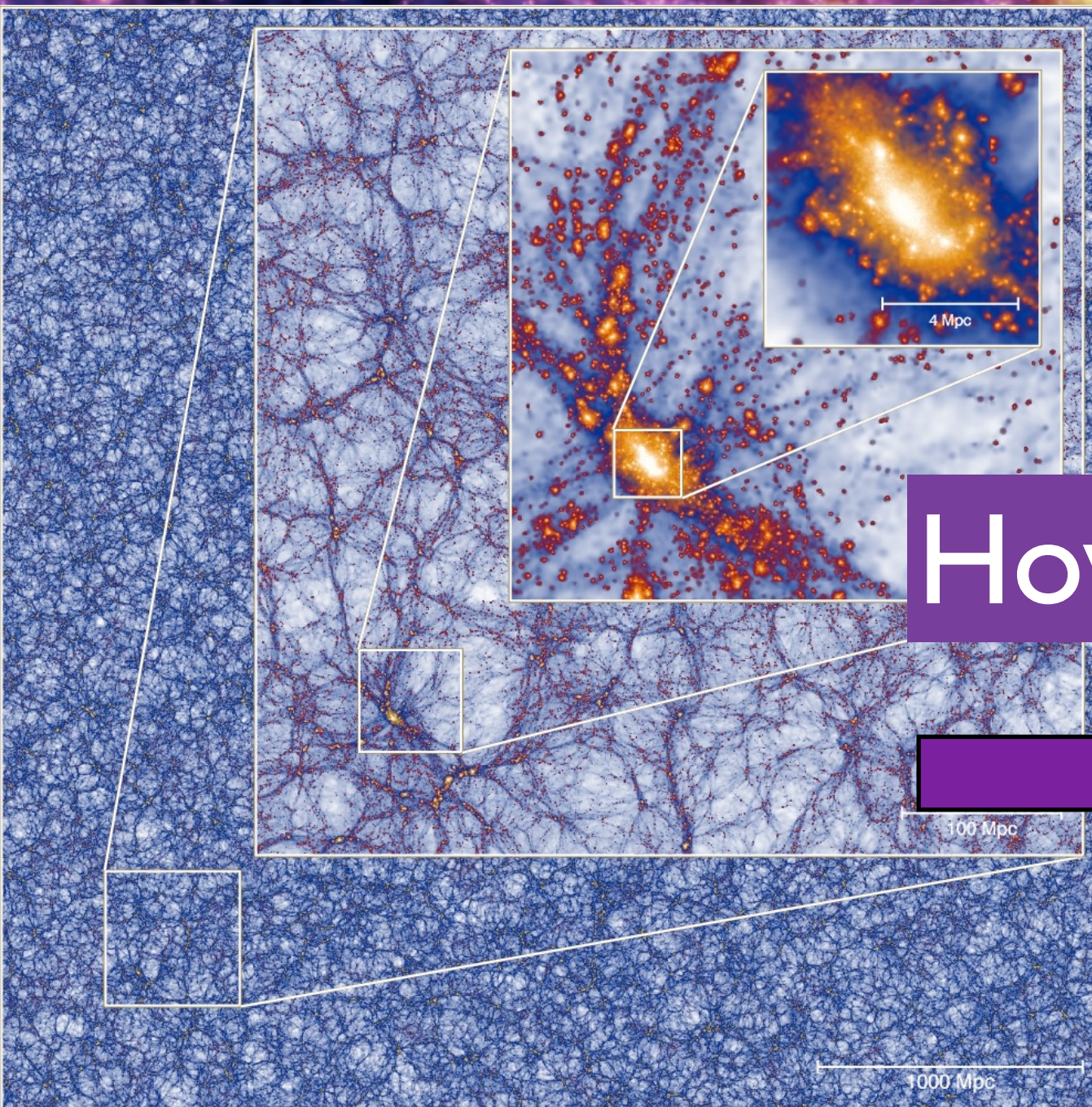
Lecture content and schedule

- *Chapter 1:* Introduction (galaxy definition, astronomical scales, observable quantities — repetition of Astro-I)
- *Chapter 2:* Brief review on stars
- *Chapter 3:* Radiation processes in galaxies and telescopes;
- *Chapter 4:* The Milky Way
- *Chapter 5:* The world of galaxies I
- *Chapter 6:* The world of galaxies II
- *Chapter 7:* Black holes and active galactic nuclei
- *Chapter 8:* Galaxies and their environment;
- *Chapter 9:* High-redshift galaxies
- *Chapter 10:*
 - Cosmology in a nutshell; Linear structure formation in the early Universe
- *Chapter 11:*
 - Dark matter and the large-scale structure
 - Cosmological N-body simulations of dark matter
- *Chapter 12:* Populating dark matter halos with baryons: Semi-empirical & semi-analytical models
- *Chapter 13:* Modelling the evolution of gas in galaxies: Hydrodynamics
- *Chapter 14:* Gas cooling/heating and star formation
- *Chapter 15:* Stellar feedback processes
- *Chapter 16:* Black hole growth & AGN feedback processes
- *Chapter 17:* Modern simulations & future prospects

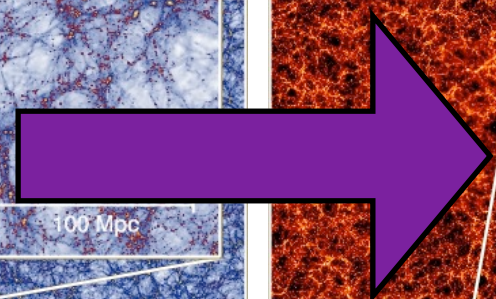
Part I:
Observational
basics & facts of
galaxies
first 7 lectures

Part II:
Theory & models
of
galaxy evolution
processes
second 7 lectures

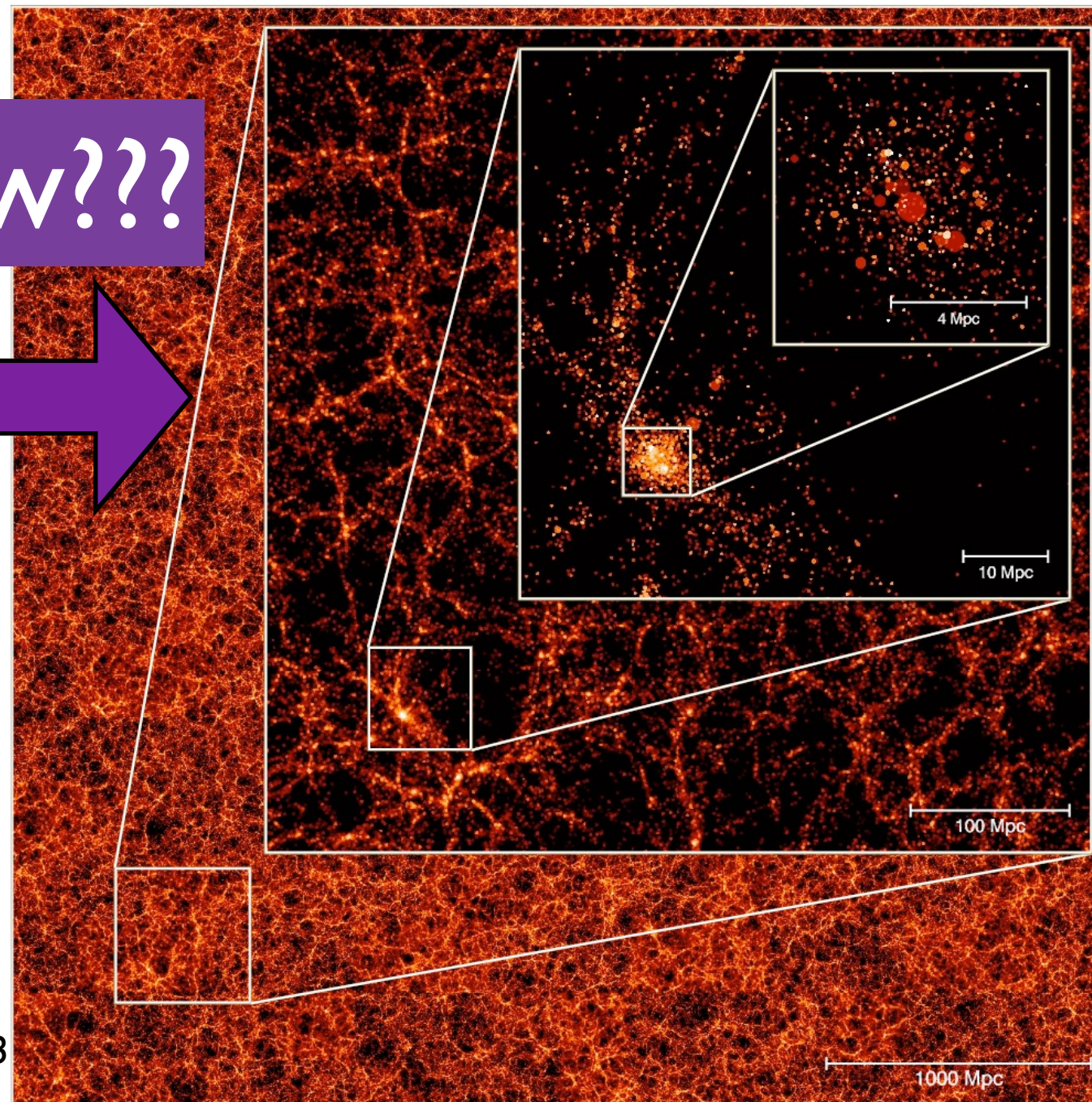
How to populate halos with galaxies?



How???



Galaxy distribution



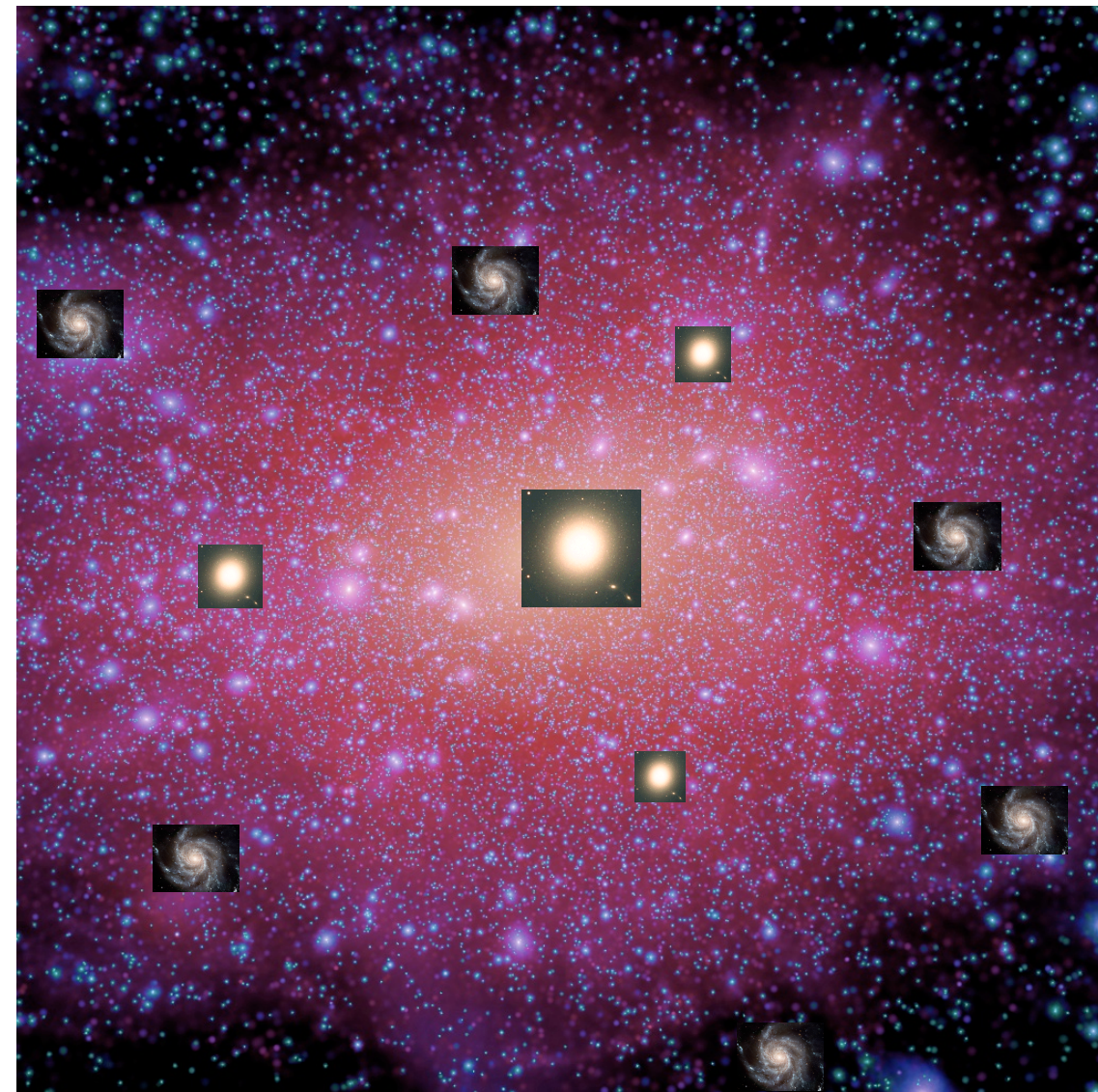
Dark matter distribution
halo catalogues and halo
merger trees

Outline of this lecture

- Different modelling approaches for baryons
- Semi-empirical models
 - Linking DM halos to observed galaxies
 - Main results
- Semi-analytic models
 - Physical models for baryons
 - Main results
 - Challenges and limitations

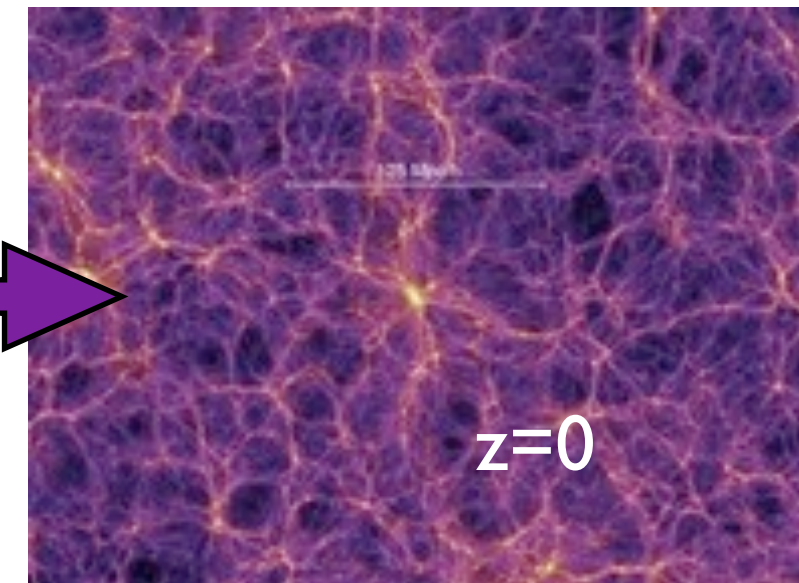
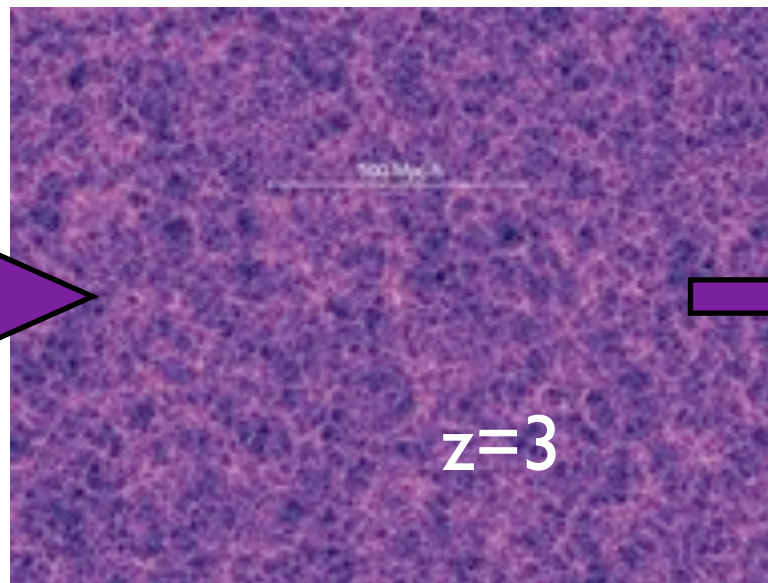
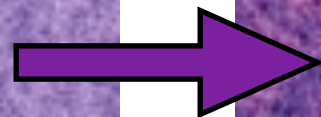
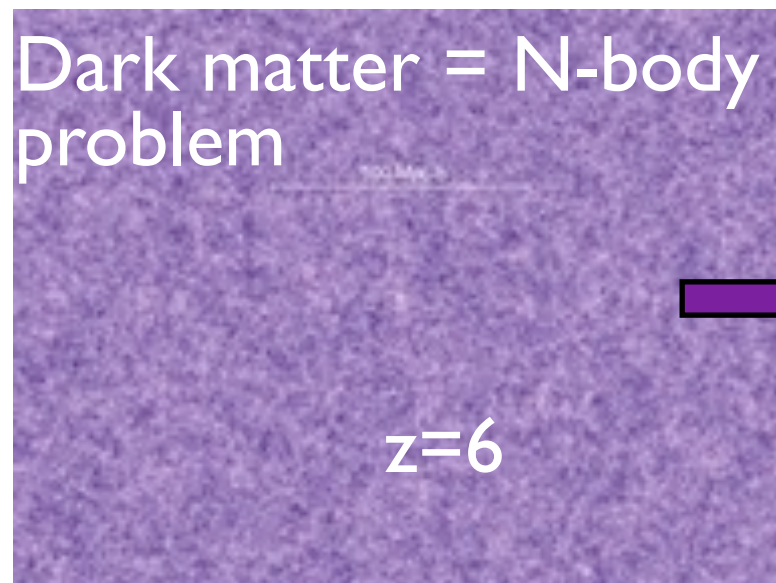
How to model baryons?

- Based on hierarchical evolution of DM halos in a CDM paradigm: due to gravitational interactions, **baryons follow the evolution of dark matter**
- **Evolution of baryons much more complex** due to gas-dynamical processes and variety of other baryonic processes
- Galaxy formation is a **complex, self-regulated network of reactions and back-reactions**
- **What are the main processes affecting galaxy evolution?**



Cosmological galaxy formation simulations

Cosmological model + initial conditions + N-body simulation code = DM halos

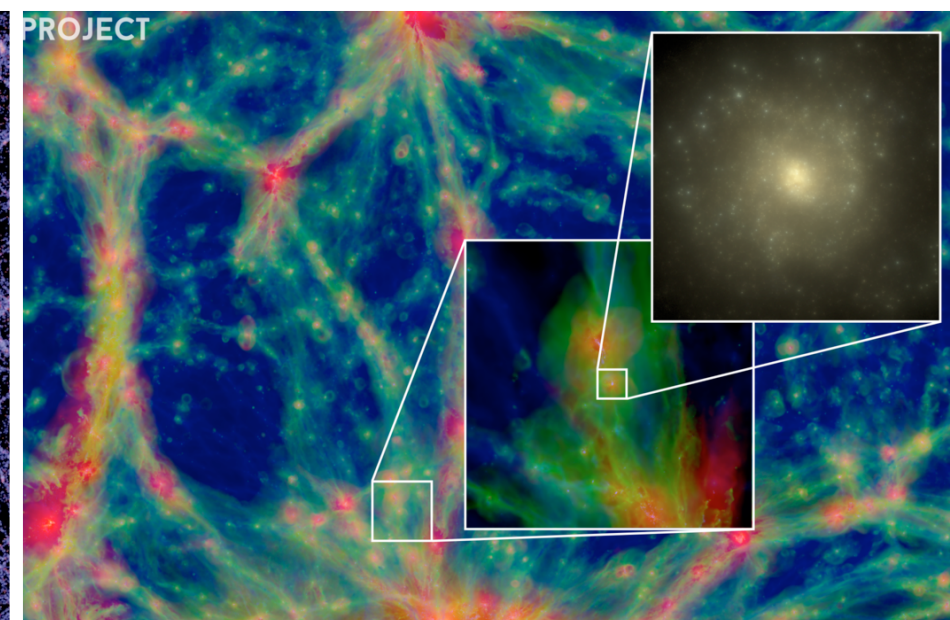
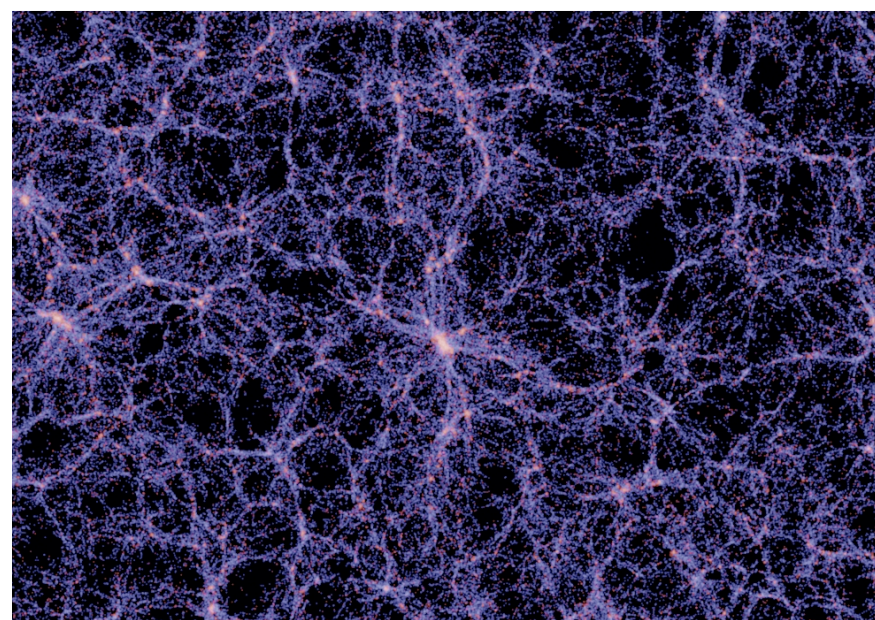
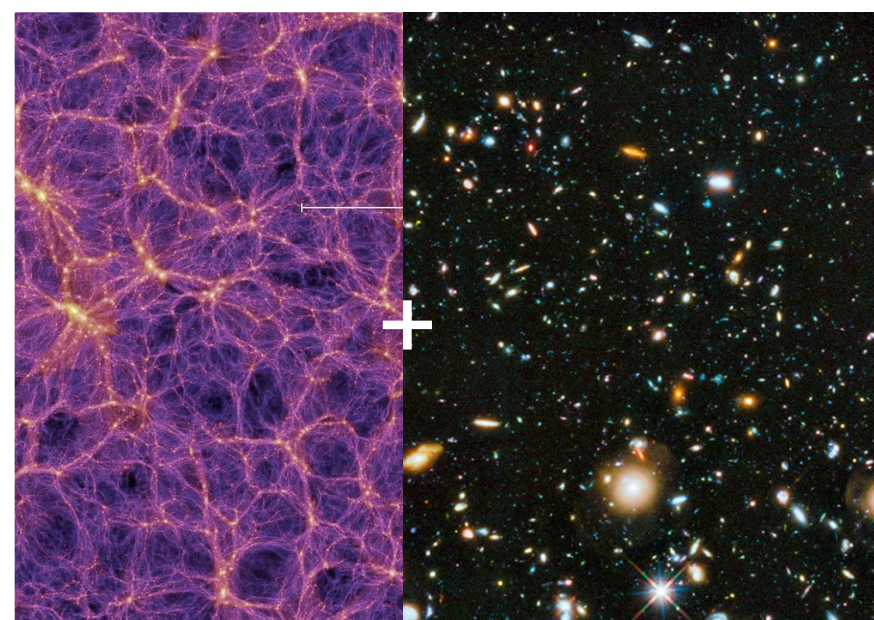


To populate DM halos with galaxies: model baryon physics via

Semi-empirical models

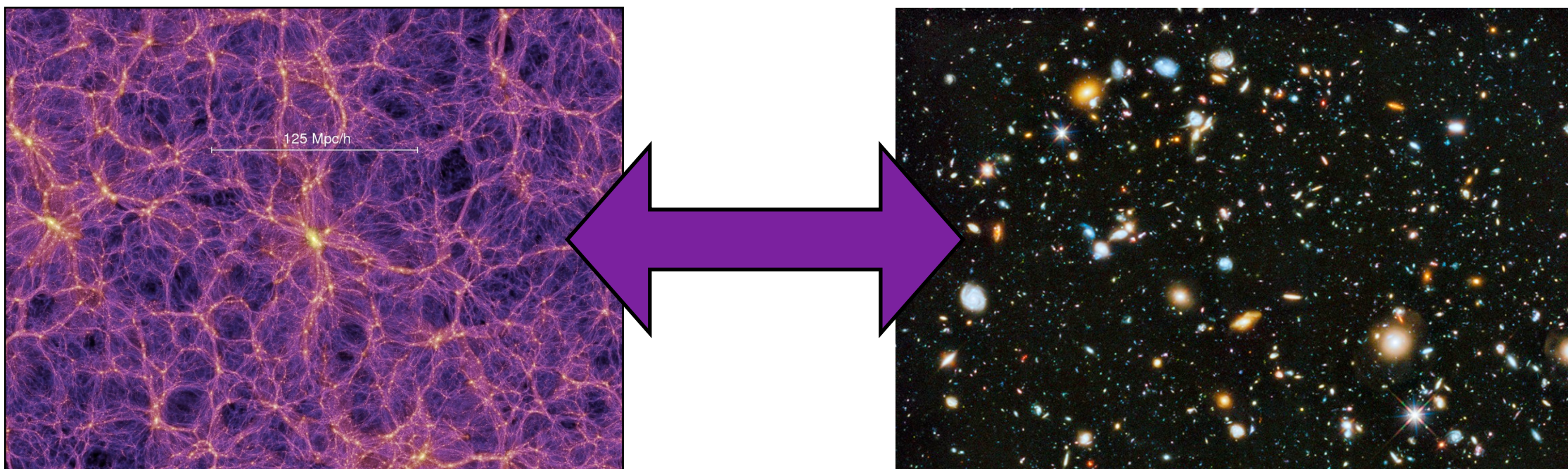
Semi-analytic models

Hydrodynamic simulations



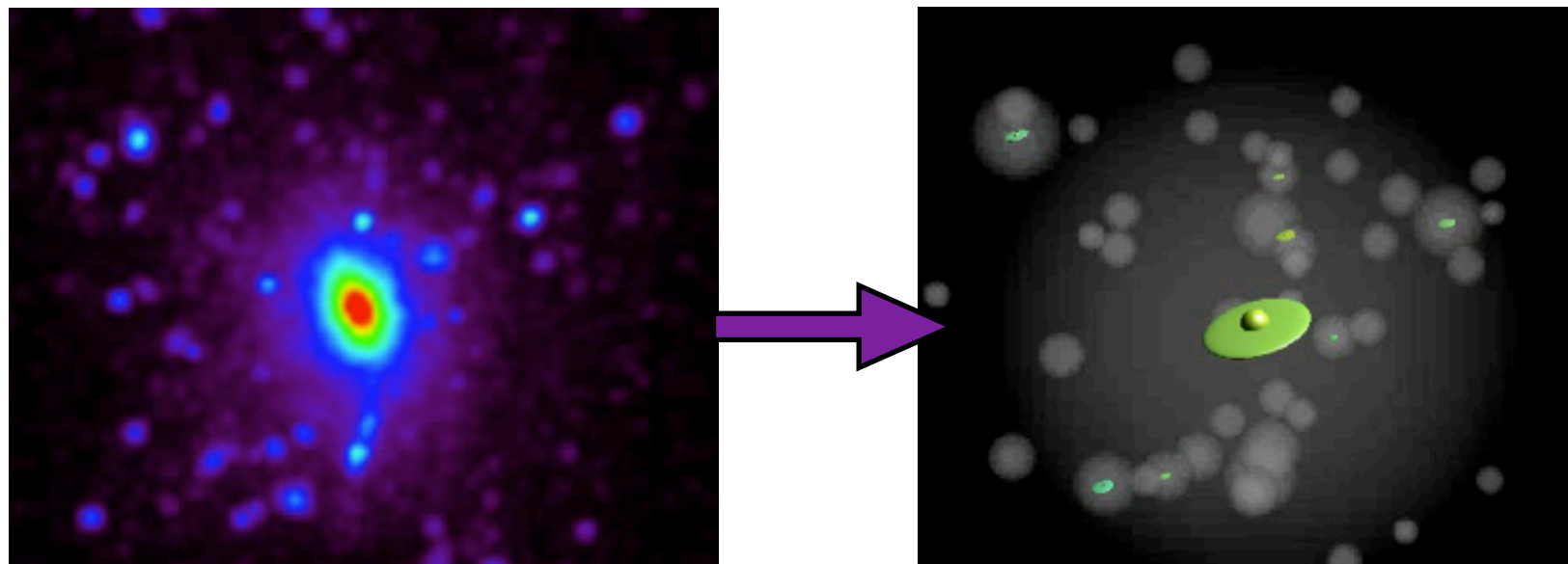
Different approaches for modelling baryons

- Mostly based on N-body simulations of dark matter
- Semi-empirical/abundance matching models:
 - Observed galaxy properties are coupled to depth of potential well of simulated halo mass
 - **No direct modelling of baryonic physics**
 - Using statistical observations of galaxies and statistically link halo masses (simulated) to (observed) galaxy masses or luminosities
 - Idea of how galaxies may evolve in the framework of hierarchically growing DM halos
 - **“Quasi”-observations with “undetectable” halo mass**



Different approaches for modelling baryons

- Mostly based on N-body simulations of dark matter
- Semi-empirical models
- Semi-analytic models:
 - **Approximation with physically motivated, but phenomenological analytic laws** to trace different baryonic reservoirs of a galaxy (cold gas, stars, hot gas, BH mass etc.)
 - Solving coupled sets of differential equations
 - + Powerful approach to assess *statistical galaxy properties*
 - + Low computational costs
 - + Perfect for a first *testing of different physical processes*
 - — But Simplified models with a large free parameter space
 - — No spatial resolution, other than spherical symmetry of profiles

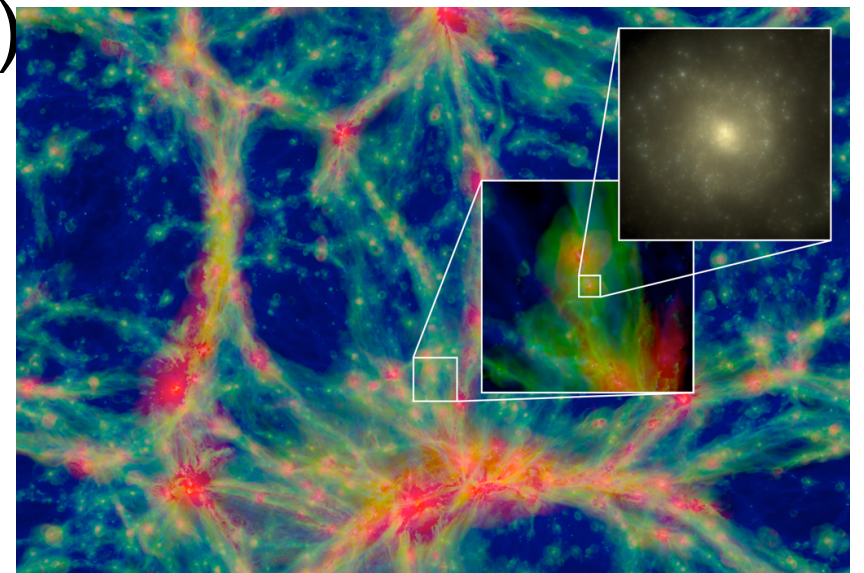


Different approaches for modelling baryons

- Mostly based on N-body simulations of dark matter
- Semi-empirical models
- Semi-analytic models
- (Cosmological) hydrodynamic simulations:
 - **Explicitly solving gas dynamical equations:** conservation laws for mass, momentum & energy, solved with Mesh-based/SPH techniques, see Chapter 13
 - + Most precise approach for modelling baryons up to now
 - + Spatial information accessible and self-consistently modelled
 - — High computational costs —> difficult to explore the effect of different physical processes and their parameter space
 - — Multi-scale problem: sub-resolution models very uncertain and strongly affect the results (see chapter 14-16)

$$\frac{\partial U}{\partial t} + \nabla \cdot \mathbf{F} = 0 \quad U = \begin{pmatrix} \rho \\ \rho \mathbf{v} \\ \rho e \end{pmatrix} = \begin{pmatrix} \rho \\ \rho \mathbf{v} \\ \rho u + \frac{1}{2} \rho \mathbf{v}^2 \end{pmatrix}$$

$$\mathbf{F}(U) = \begin{pmatrix} \rho \mathbf{v} \\ \rho \mathbf{v} \mathbf{v}^T + P \\ (\rho e + P) \mathbf{v} \end{pmatrix} \quad P = (\gamma - 1) \rho u$$



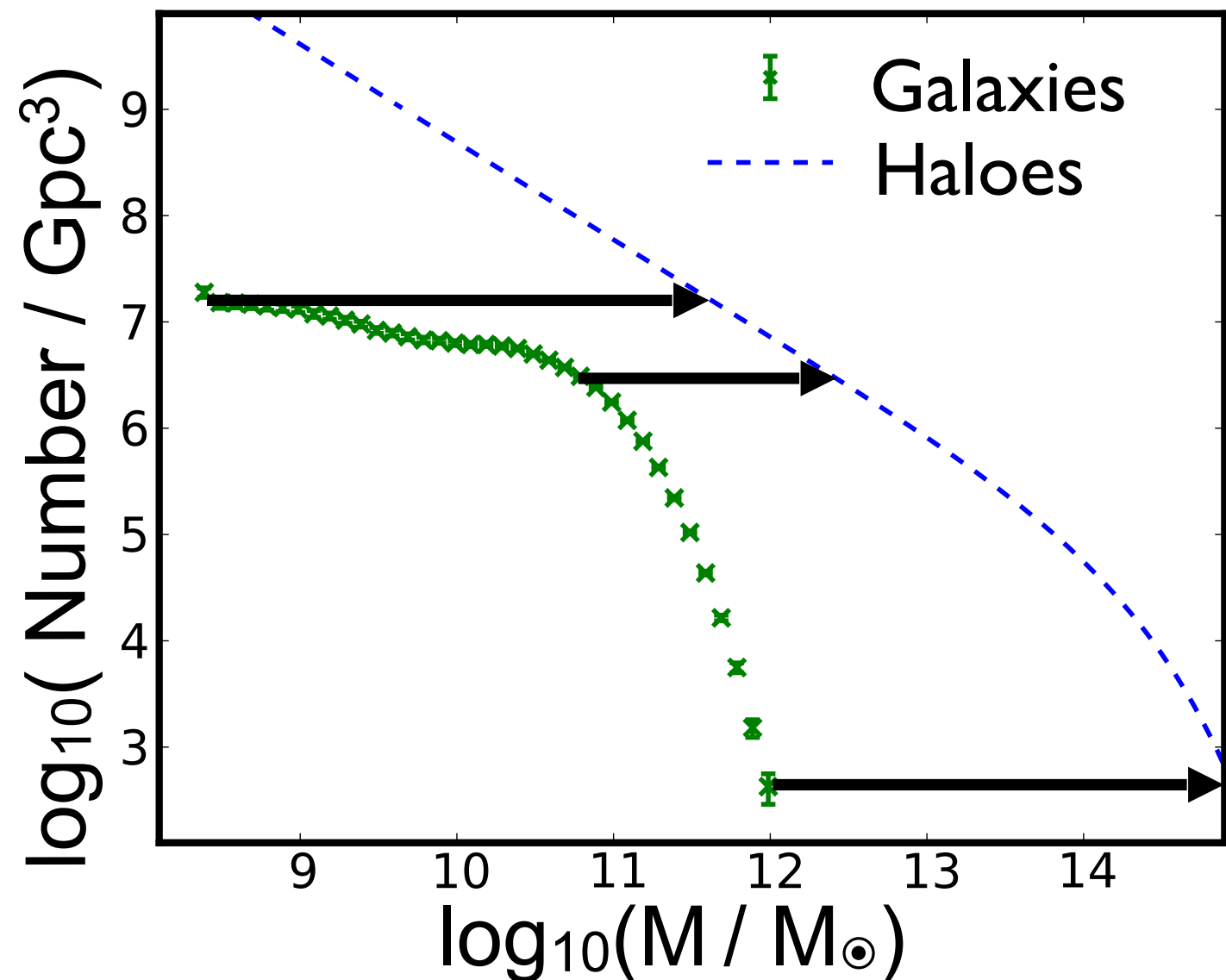
Outline of this lecture



- Different modelling approaches for baryons
- Semi-empirical models
 - Description
 - Main results
- Semi-analytic models
 - Physical models
 - Main results
 - Challenges and limitations

Abundance matching

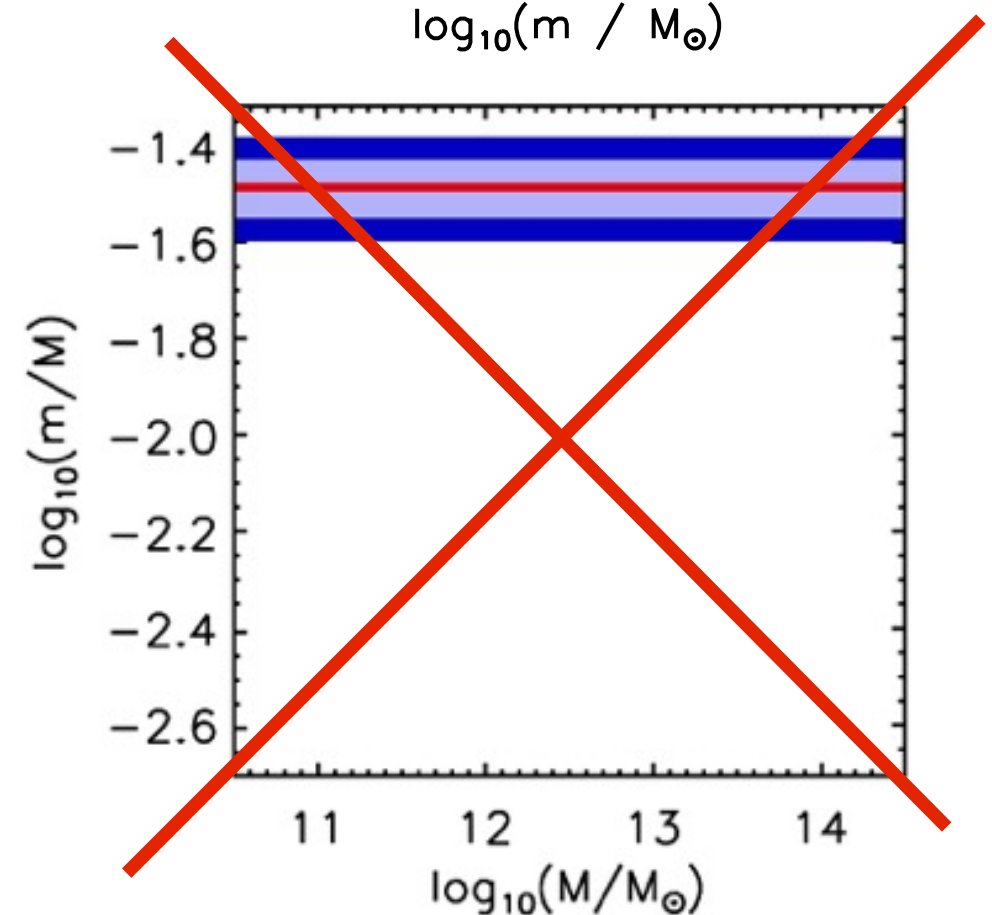
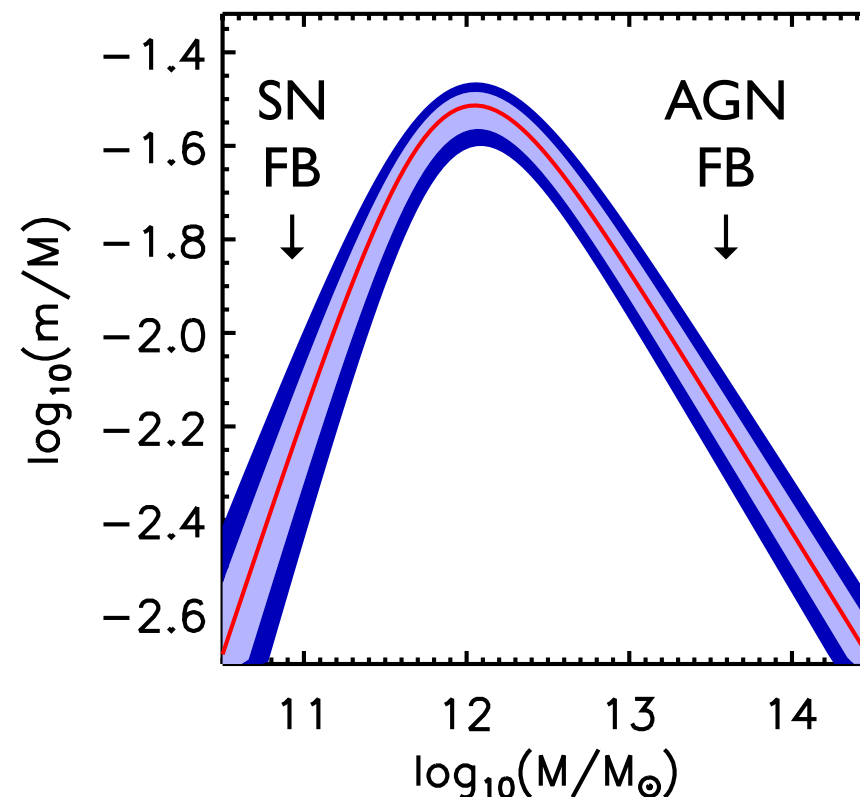
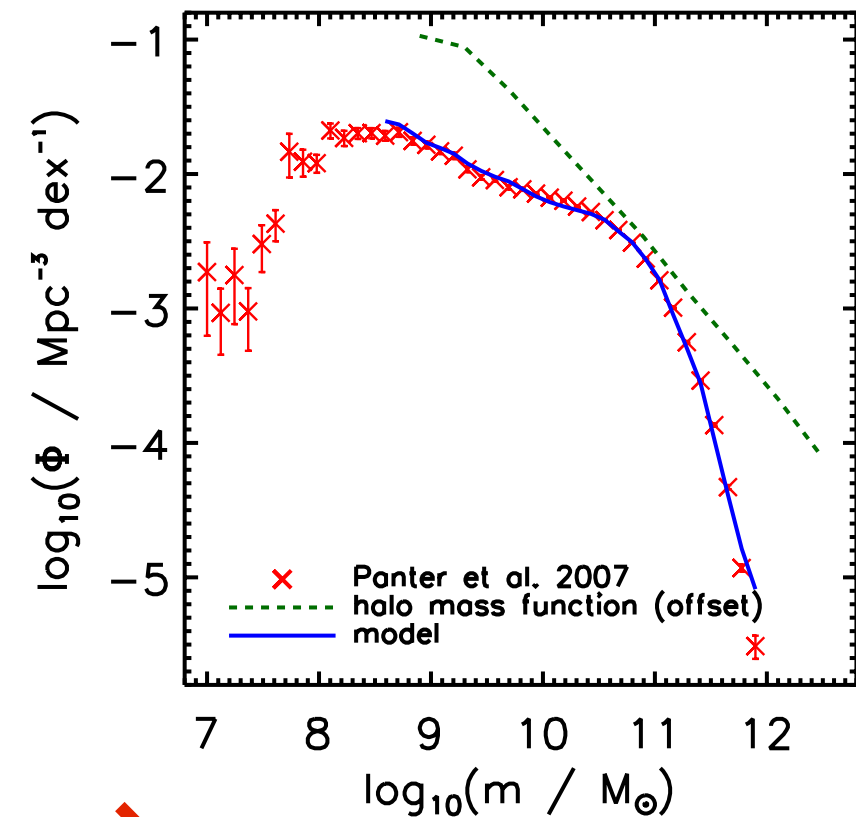
- Extract positions and masses of **halos from N-body simulations**
- Take **observed stellar mass function** (SMF) of galaxies
- **Link galaxies and halos** using a simple assumption: most massive galaxies live in most massive halos
- Rank order halos by mass
- Generate galaxy catalogue from observed SMF and rank order galaxies by mass
- Link galaxies one-to-one
- Connection of stellar to halo mass can be done in two ways:
 - assuming a non-parametric monotonic relation
 - assuming parameterised functions



Populating halos

- Populate halos and subhalos
- Constant stellar-to-halo mass ratio **does not work**
- Use non-constant ratio like:

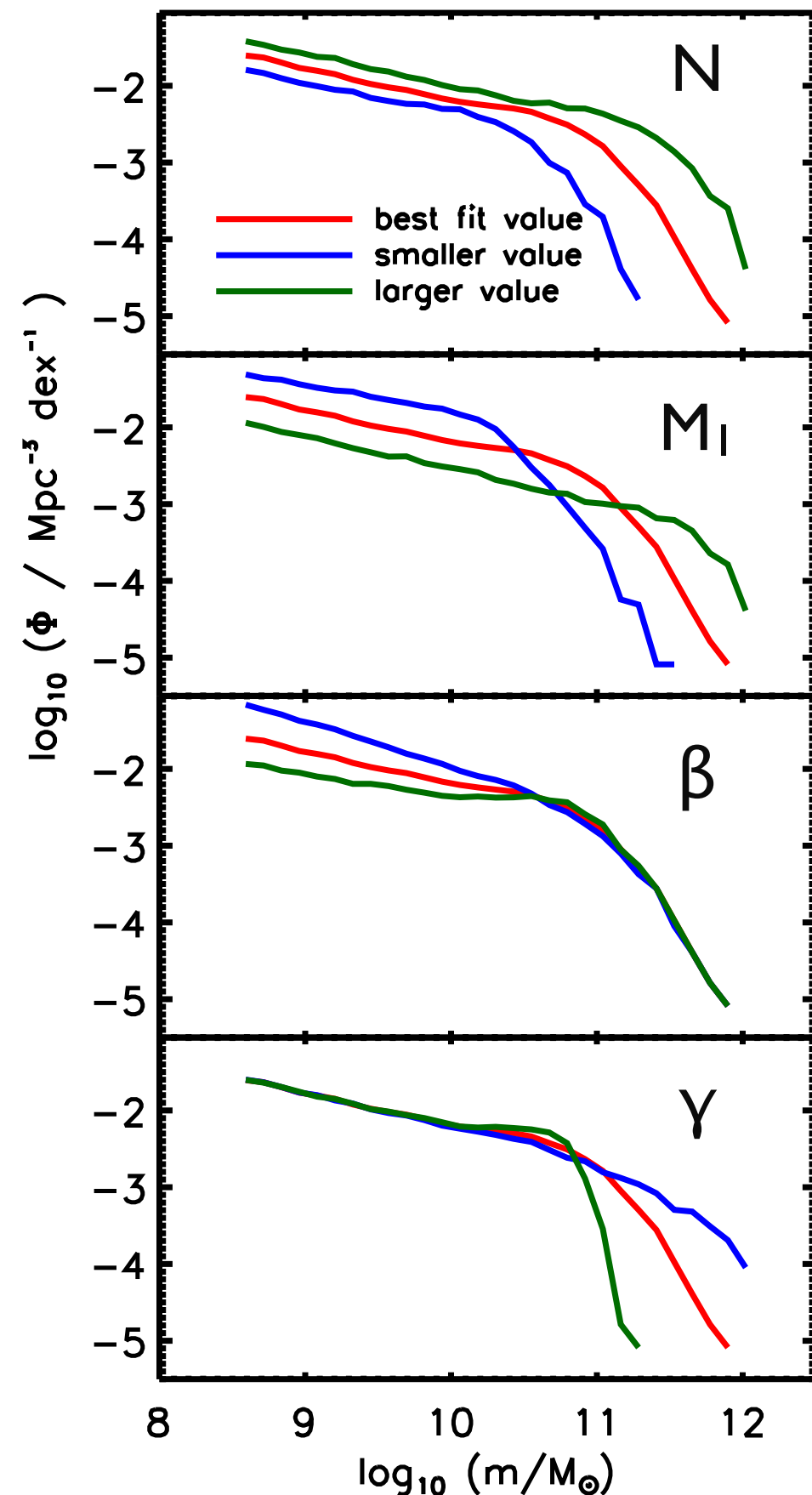
$$\frac{m_*}{M}(M) = 2N \left[\left(\frac{M}{M_1} \right)^{-\beta} + \left(\frac{M}{M_1} \right)^{\gamma} \right]$$
- Contains two slopes, characteristic mass and a normalisation
- Fit parameters to SMF



Meaning of parameters

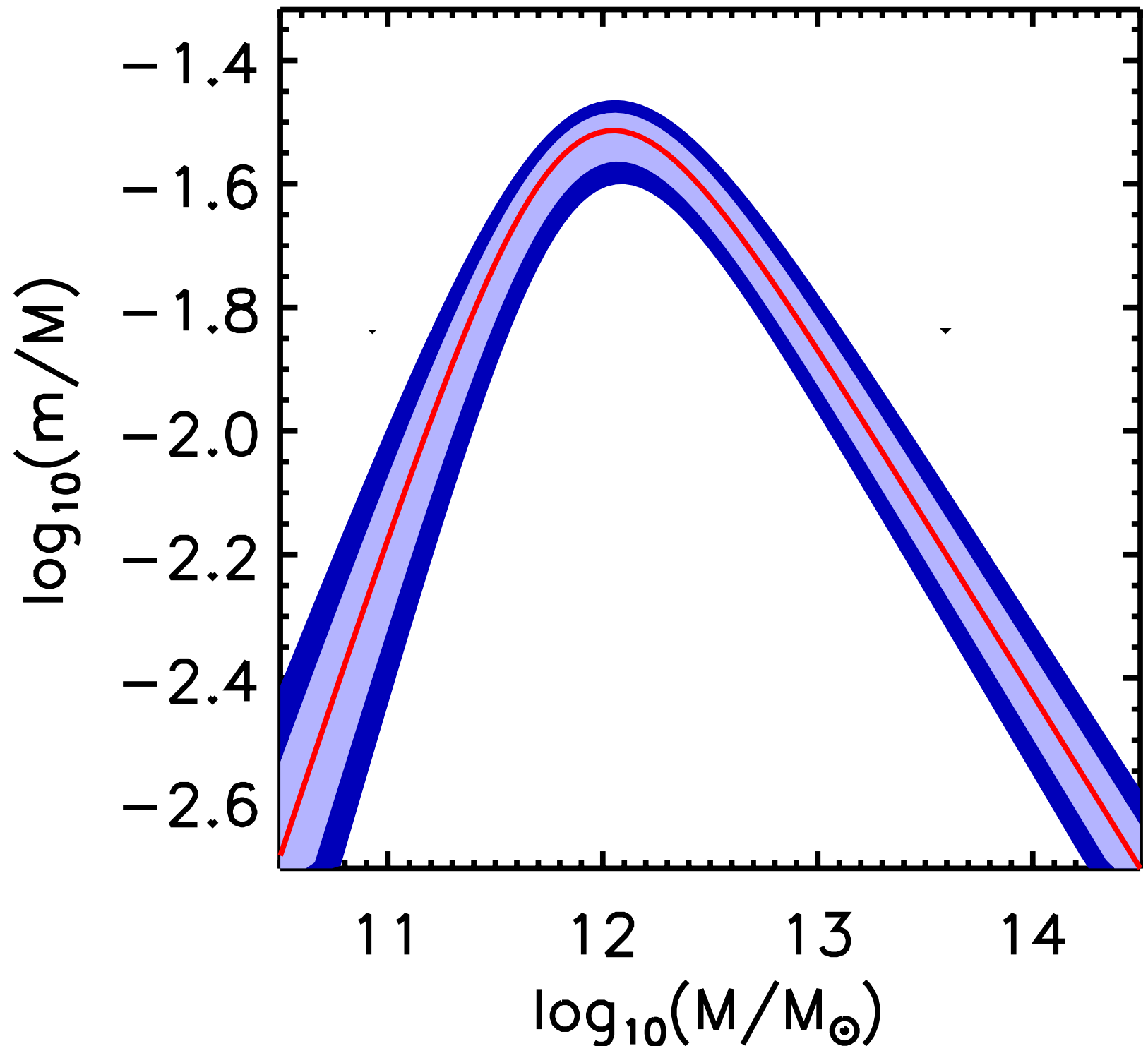
$$\frac{m_*}{M}(M) = 2N \left[\left(\frac{M}{M_1} \right)^{-\beta} + \left(\frac{M}{M_1} \right)^{\gamma} \right]$$

- Leave all parameters constant and change only one:
- **Normalization N** determines the position on stellar mass axis
- **Characteristic mass M_1** sets the knee of the SMF
- **Low mass slope β** affects the slope α of the Schechter fct
- **High mass slope γ** determines the exponential “cut-off” of the SMF

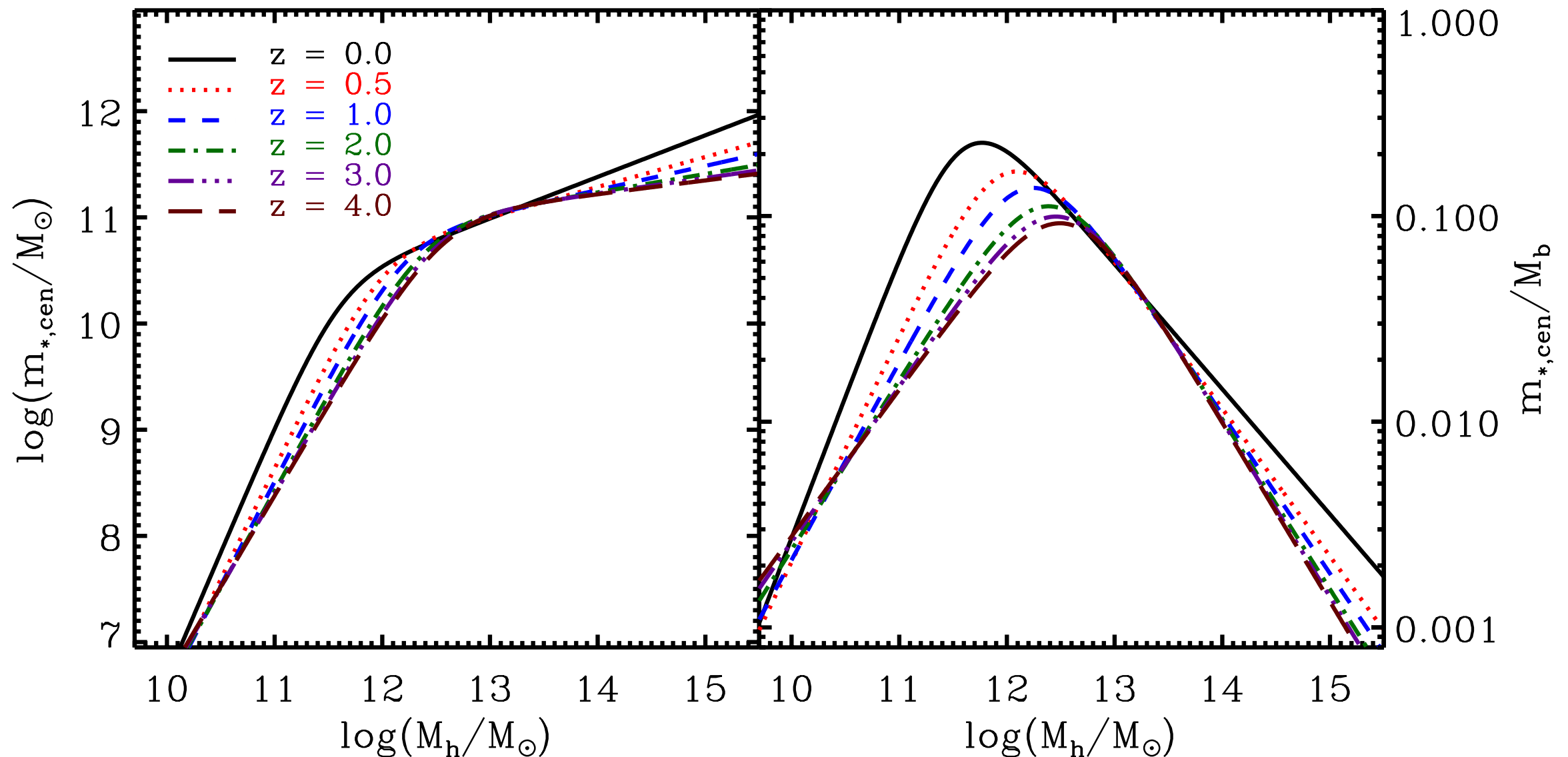


Stellar mass content versus halo mass

- At maximum, only 3-4% of matter in halo consists of luminous stars
- Implying that at maximum only ~20-30% of the universally expected baryon content is converted into stars
- lower efficiencies for low-mass and high-mass halos!



Results of the best-fit model



- Little evolution at high z (>2), moderate evolution at low z
- “Antihierarchical” trend visible: at higher z , baryon conversion efficiencies peak in more massive halos than at lower z
- Why is the stellar baryon conversion efficiency so low?
 - gas prevented from infall? — gas not forming stars? — gas ejected?
- ➡ Semi-empirical models **cannot answer** this question!

Constraints and predictions

Semi-empirical (abundance matching) models helpful for

- Predictions unbiased by assumption on baryon physics
- Getting an idea of how galaxies grow and assemble in hierarchically growing dark matter halos
- “Observational-like” constraints for semi-analytic models and hydro simulations to test their models for baryon physics within DM halos

BUT: Semi-empirical models only provide us with some trends with halos mass, but they **DO NOT PROVIDE ANY PHYSICAL EXPLANATION!**

Outline of this lecture



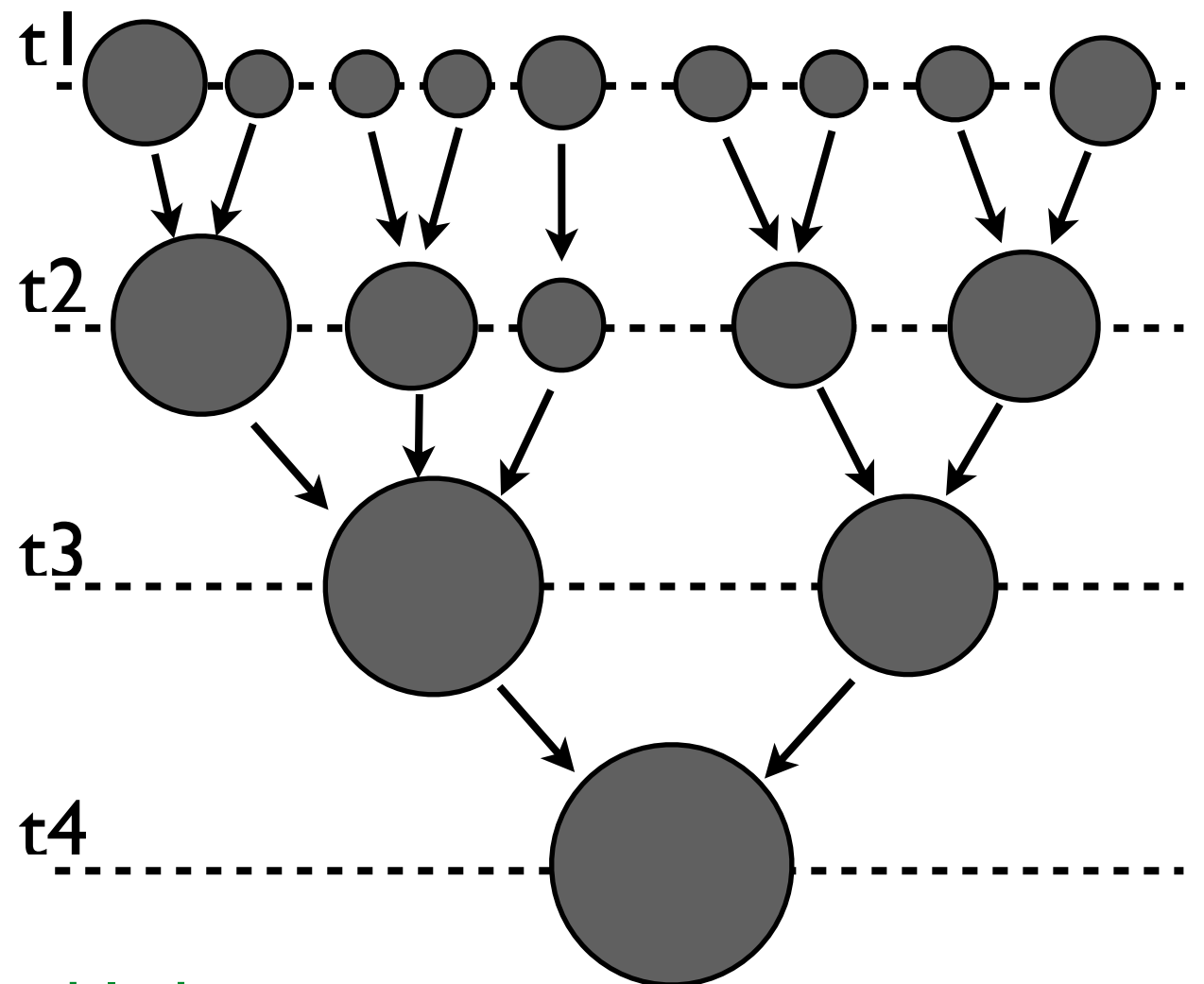
- Different modelling approaches for baryons
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A bit of history...

- Original “idea” by Fred Hoyle (1949): “Stellar evolution and the expanding Universe”
- White & Rees 1978: Galaxy formation as a two stage process
 - First, dark matter halos collapse and assemble
 - Then, gas cools in these halo potential, condenses in the center and forms stars
- Frenk & White 1991: “Grandparent” model for all future SAMs: further development, first semi-analytic model with cooling, SF, feedback, mergers etc.
- Since then, further refinement of physically motivated models and development of many different semi-analytic models

Reminder: Merger trees

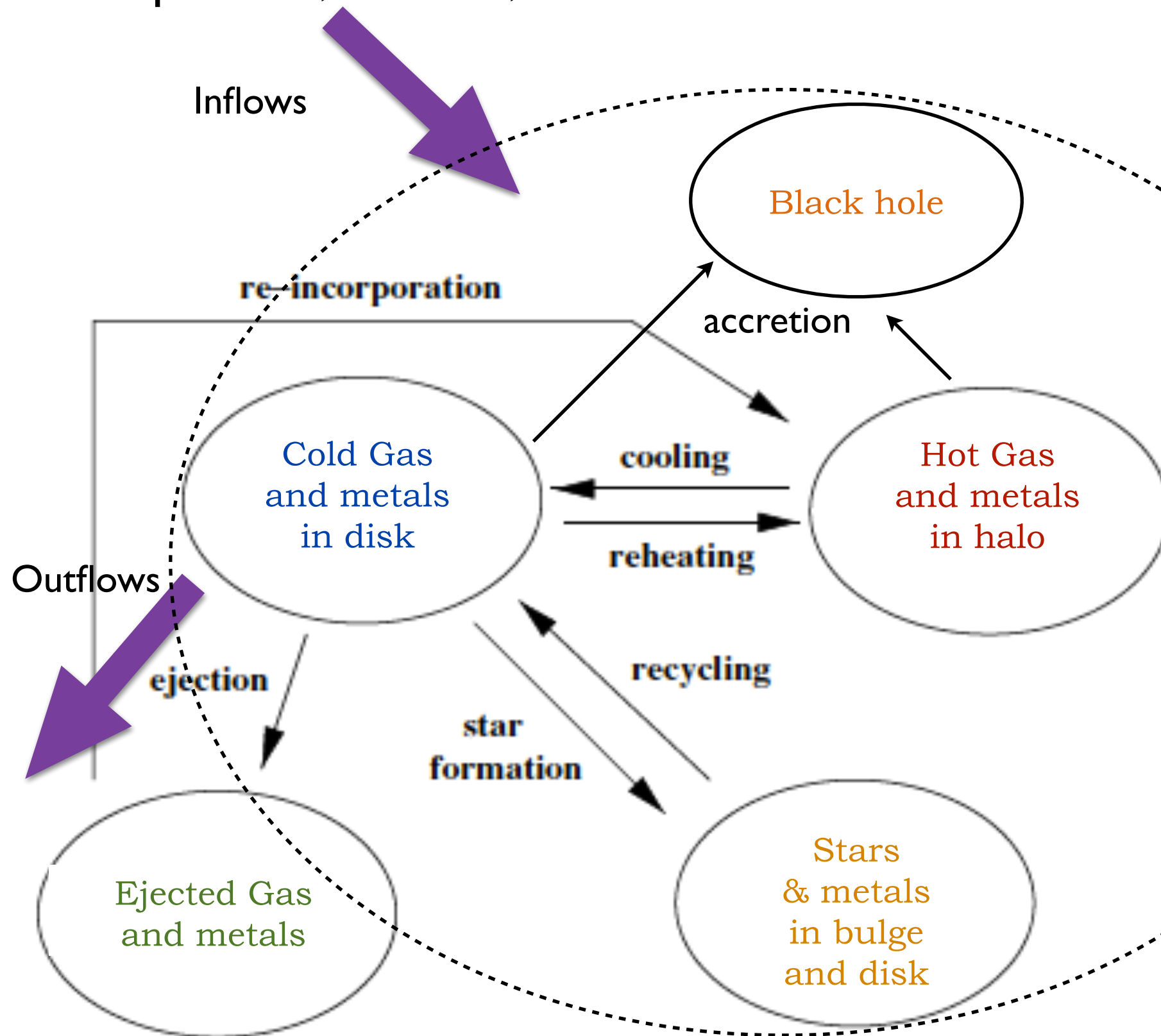
- Backbone is **HIERARCHICAL structure formation**, merging into larger and larger objects



- **SAMs are built up-on the DM assembly history**
 - When a halo for the first time “appears”, **hot gas is put in according to the universal baryon fraction of a halo** of a given mass
 - Smooth accretion rate in dark matter is transformed into one for baryons (according to the universal baryon fraction)
 - Mergers are considered, and accretion onto larger halos (->sub-halos)

Baryon reservoirs in SAMs

- In practice, in SAMs, we follow the evolution of different baryonic reservoirs



- Recipes empirically motivated by observations
- **Problem:** small-scale physical processes not well understood → free parameters
- Free parameters are “tuned” to match basic statistical galaxy properties at $z \sim 0$
- Predictions of other statistical galaxy properties and confront them to observations

Gas cooling

- For simplicity, always **assume spherical symmetry** of halos and galaxies
- Gas is assumed to fall into DM halos and to shock heat to the virial temperature
- The **gas density profile** is assumed to follow an isothermal sphere

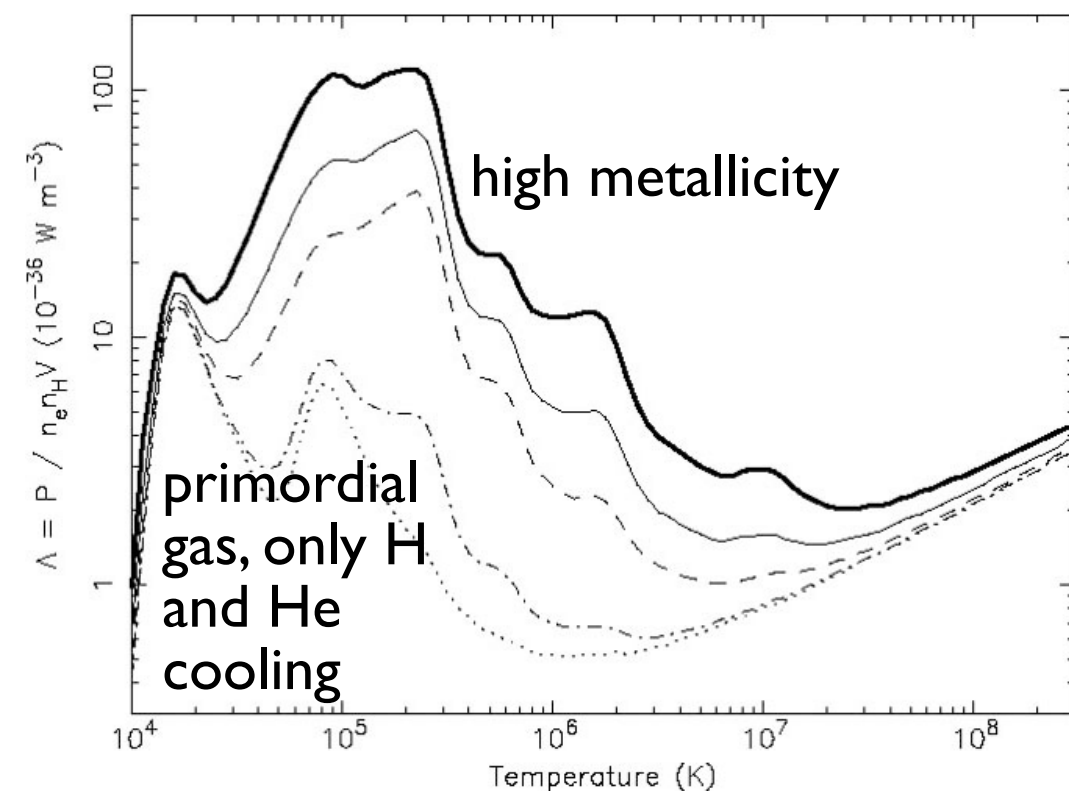
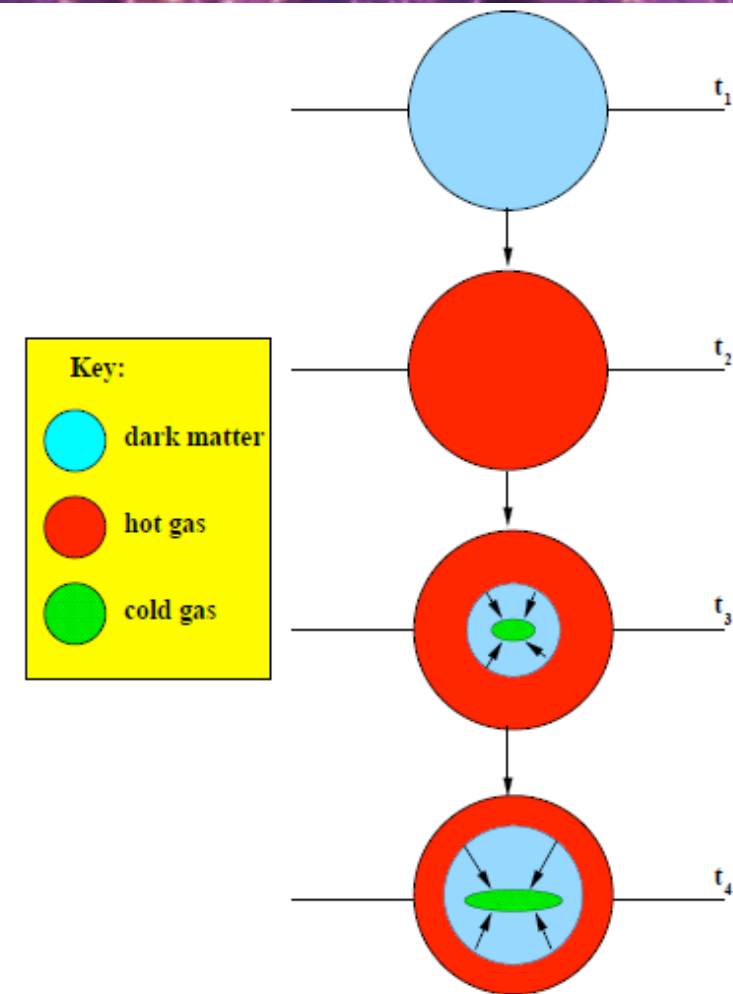
$$\rho_g(r) = m_{\text{hot}} / (4\pi r_{\text{vir}} r^2)$$

- **Gas cools from this hot halo**, loses P support, falls to the centre and forms a disc

$$t_{\text{cool}} = \frac{3/2 \mu m_p k T}{\rho_g(r) \Lambda(T, Z_h)}$$

- Putting the density into the above equation, one can solve for the cooling radius r_{cool} with t_{cool}
- Writing expression of the mass within r_{cool} and differentiate it \rightarrow rate at which gas can cool

$$\frac{dm_{\text{cool}}}{dt} = \frac{1}{2} m_{\text{hot}} \frac{r_{\text{cool}}}{r_{\text{vir}}} \frac{1}{t_{\text{cool}}}$$



Star formation

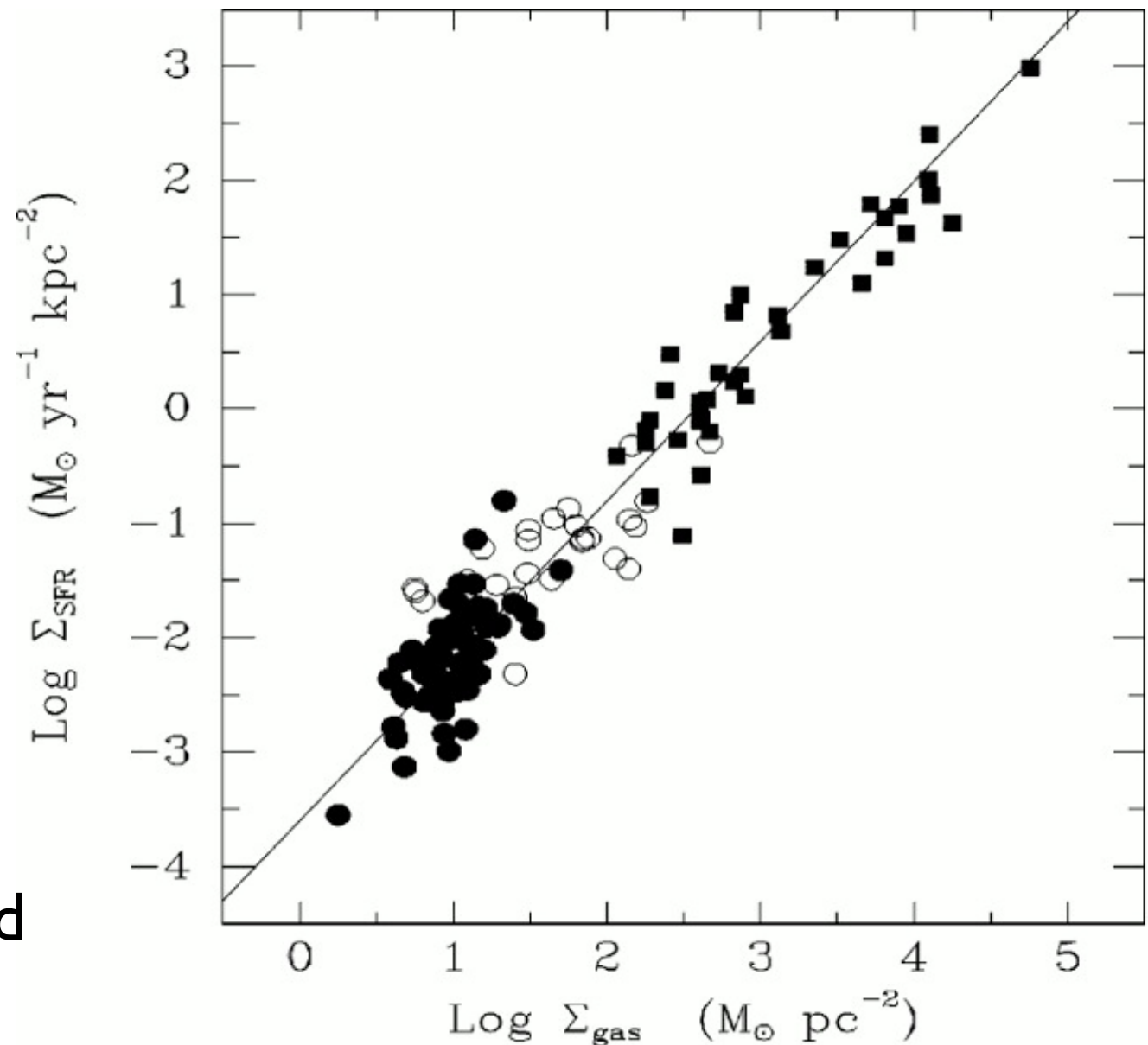
- No full theory of star formation that gives SFR as a function of the ISM
- **Phenomenological approach**: calculate SFR following the observed Schmidt-Kennicutt relation

- **SFR surface density is related to the cold gas surface density**

$$\Sigma_{\text{SFR}} = A_{\text{Kenn}} \Sigma_{\text{gas}}^{N_K}$$

- Stars and cold gas are assumed to be distributed in an exponential disc
- Adopt a critical gas surface density, and calculate the corresponding critical SF radius (inside which gas is SF)

$$SFR = \int_0^{r_{\text{crit}}} \dot{\Sigma}_* 2\pi r dr$$



- **Remove mass of formed stars from cold gas reservoir and add it to the stellar component**
- Details can vary from model to model...

Stellar feedback

- Due to **Supernova explosions**, a certain amount of energy is released

$$\dot{E}_{\text{thermal}} = \epsilon \eta_{\text{SN}} E_{\text{SN}} \cdot SFR = \dot{M}_{\text{reheated}} V_{\text{max}}^2$$

- Thus, some cold gas is assumed to be **re-heated**

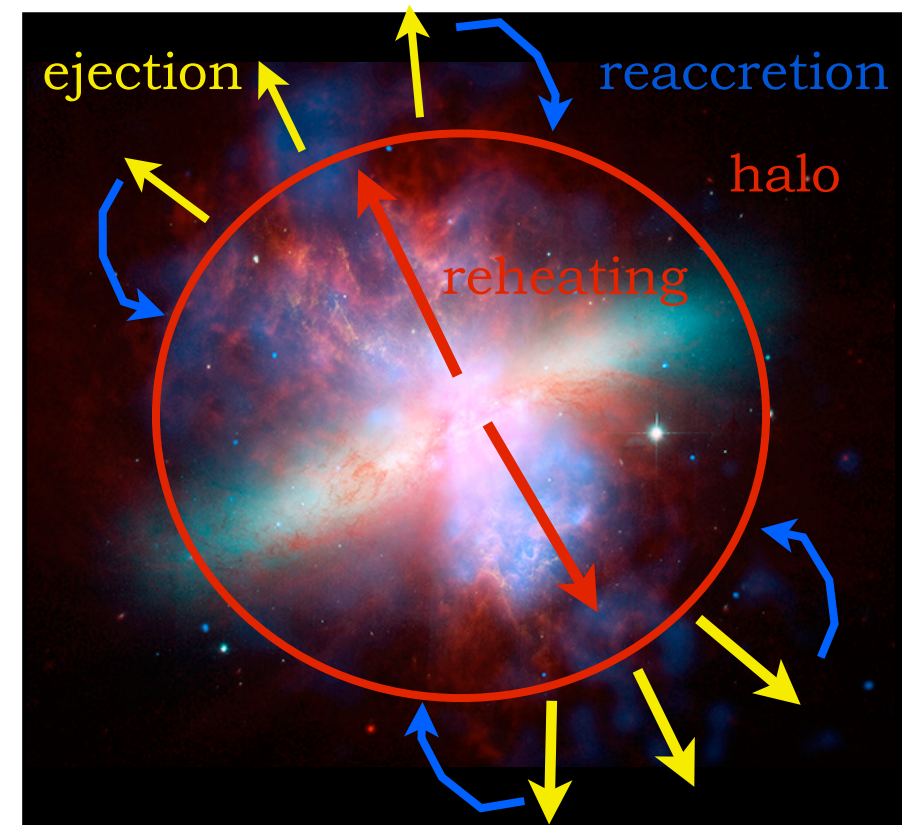
$$\dot{M}_{\text{reheated}} = \epsilon \frac{\eta_{\text{SN}} E_{\text{SN}}}{V_{\text{max}}^2} SFR$$

- In addition, a fraction of re-heated gas **can be expelled out of the halo** so that it is not available for cooling for some time

$$f_{\text{eject}}(V_{\text{vir}}) = \left[1 + \left(\frac{V_{\text{vir}}}{V_{\text{eject}}} \right)^{\alpha_{\text{eject}}} \right]^{-1}$$

- After some time (typically a halo dynamical time scale), a fraction of the ejected gas **is reincorporated back** onto the halo

$$\dot{M}_{\text{reinc}} = \gamma \dot{M}_{\text{ejected}} / t_{\text{dyn}} = \gamma \dot{M}_{\text{ejected}} \frac{V_{\text{Vir}}}{R_{\text{Vir}}}$$



- Again, exact parametrisations vary from model to model due to our poor understanding of the underlying physics
- Other processes like radiation pressure, stellar winds may contribute to heating/expelling gas

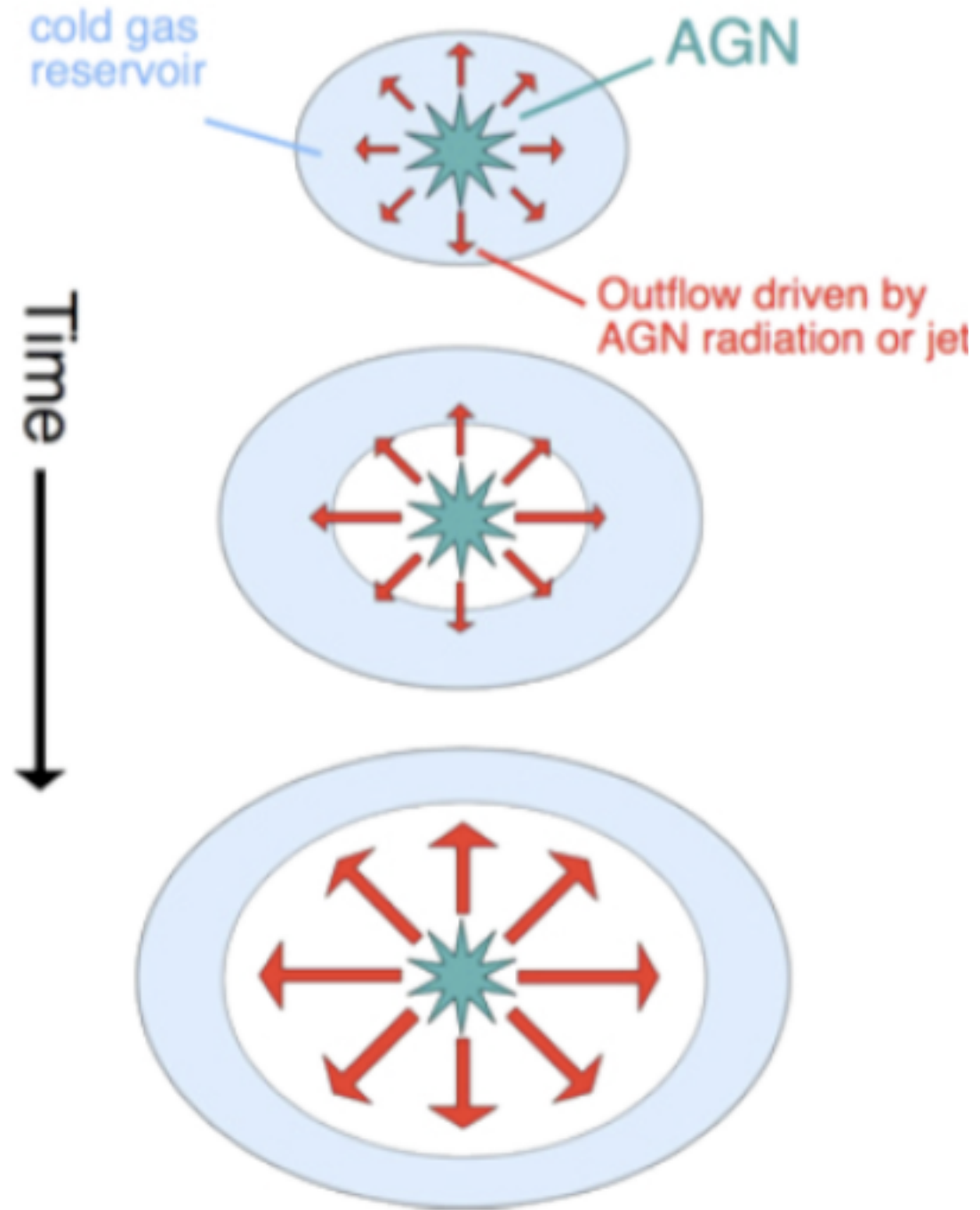
BH growth & “quasar-mode” AGN feedback

- Every top-level halo contains a seed BH of $100\text{--}10^5 M_\odot$
- Mostly assumed that BH grow via gas inflows **through mergers** (and secular evolution processes like disk instabilities)
- Accretion rates related to **cold gas content and merger mass ratio**, sometimes recipes for merger simulations used
- Some (but not many) SAMs account for **quasar-driven outflows** during phases of heavy gas accretion

$$f_{\text{eject}} \propto L_{\text{quasar}},$$

$$\text{where } L_{\text{quasar}} = \epsilon_r \dot{M}_\bullet c^2$$

conversion efficiency
of the loss of
gravitational energy
into radiation



“Jet-mode” AGN feedback

- Less efficient “hot gas accretion” once a static hot halo is present

$$\dot{m}_{\text{radio}} = \pi (G M_{\text{BH}})^2 \rho_0 c_s^{-3}$$

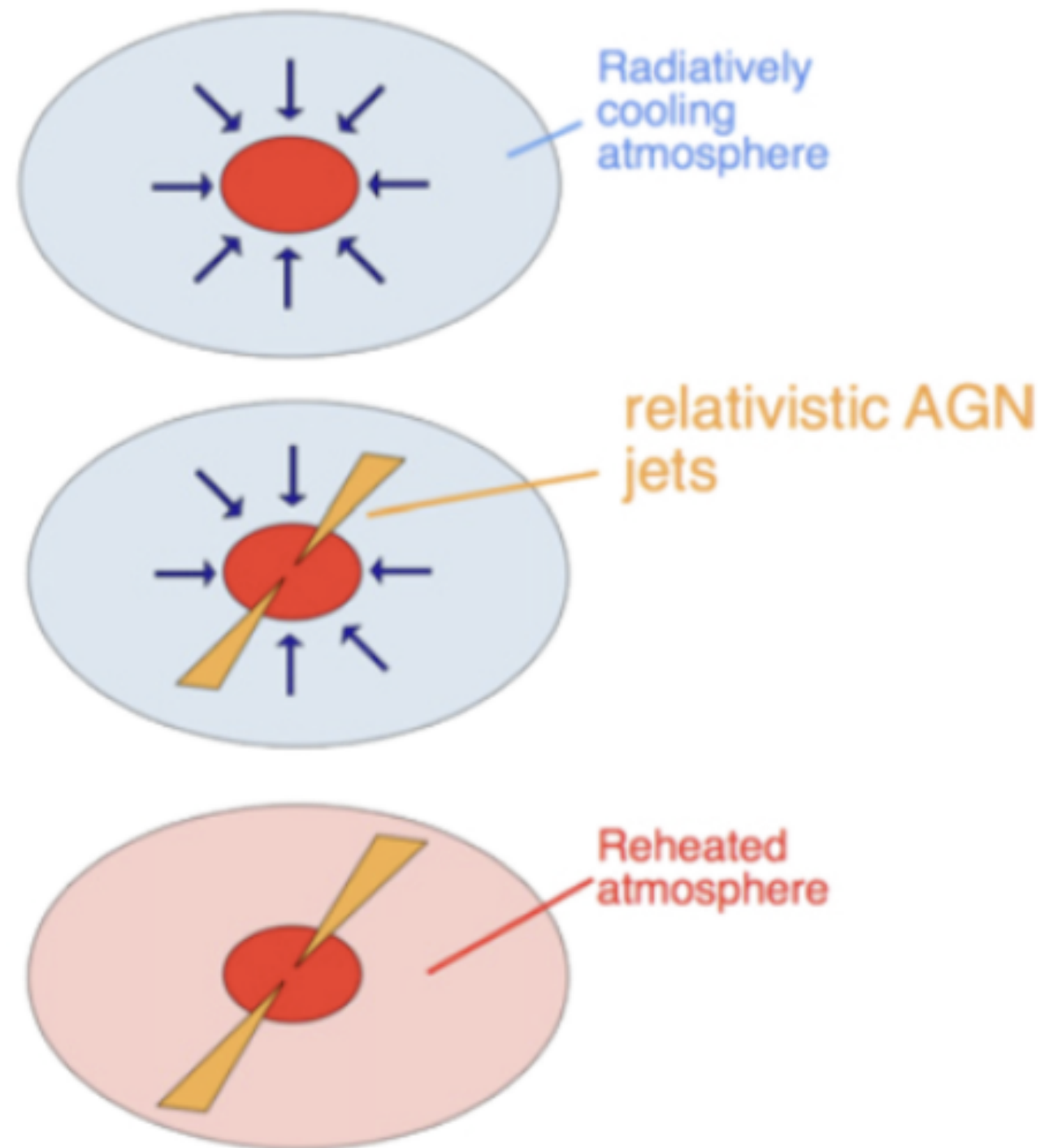
- “Radio-mode” feedback: energy due to jets released into hot halo
 - Mechanical heating power generated by BH accretion

$$L_{\text{heat}} = \kappa_{\text{heat}} \eta_{\text{rad}} \dot{m}_{\text{radio}} c^2$$
$$\rightarrow \dot{m}_{\text{heat}} \propto L_{\text{heat}}$$

- Modified, reduced cooling rate:

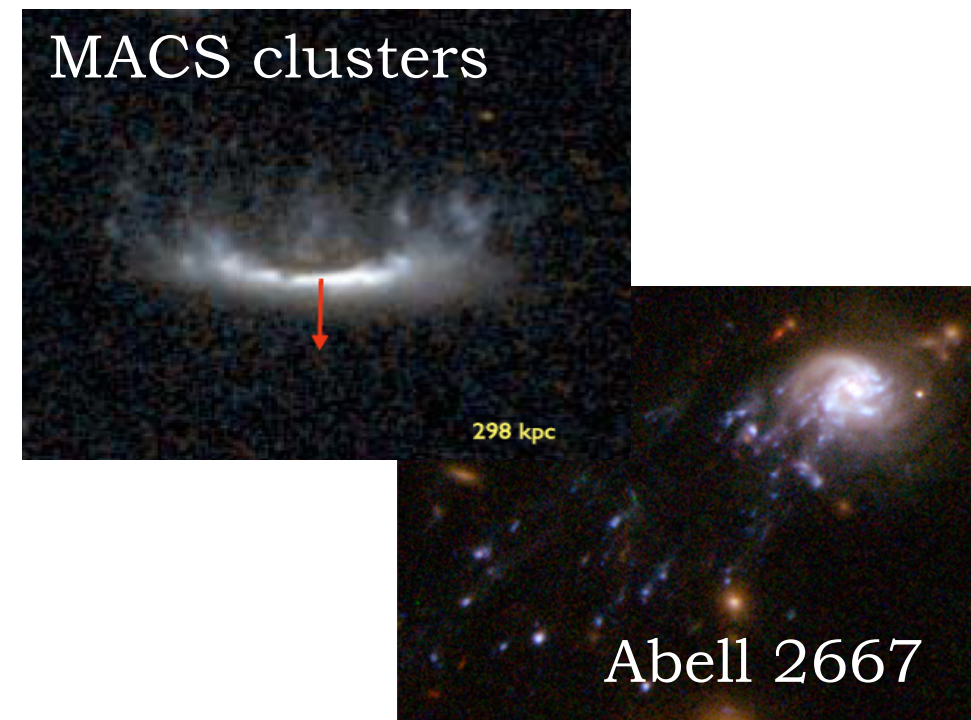
$$\dot{m}_{\text{cool,new}} = \dot{m}_{\text{cool}} - \dot{m}_{\text{heat}}$$

Croton+06 explains the first implementation of such a scheme

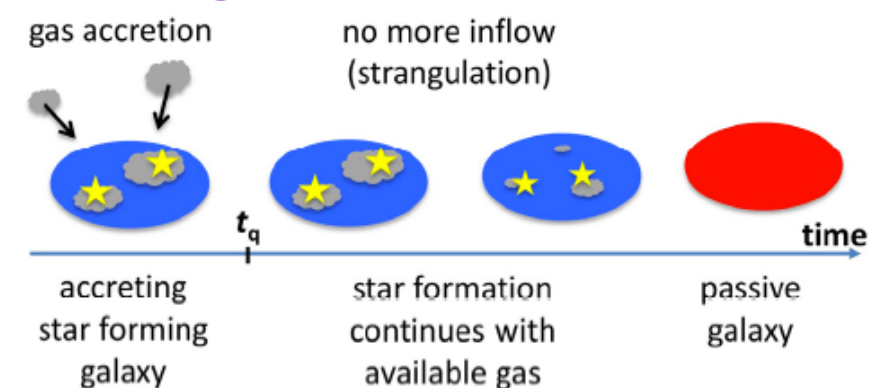


Mergers and environmental effects

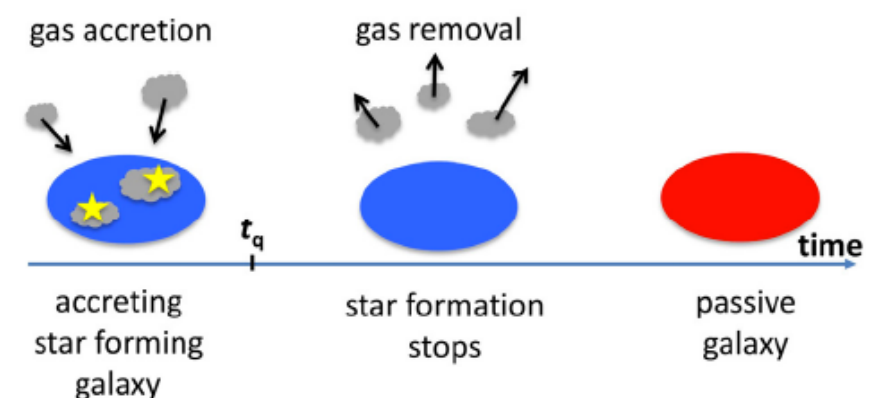
- **Mergers** lead to starbursts and morphological transformation
- **Environmental effects** mostly affecting satellites residing in dense regions:
 - **Strangulation, Ram-pressure stripping:**
Interaction with hot/cold gas due to ram-pressure
- SAMs often assume an **instantaneous strangulation**, i.e. as soon as a galaxy becomes a satellite, its hot gaseous halo is entirely stripped (i.e. no further cooling)
- Sometimes more sophisticated approaches of **delayed strangulation/stripping** based on hydro-simulations



Strangulation



Ram-pressure stripping



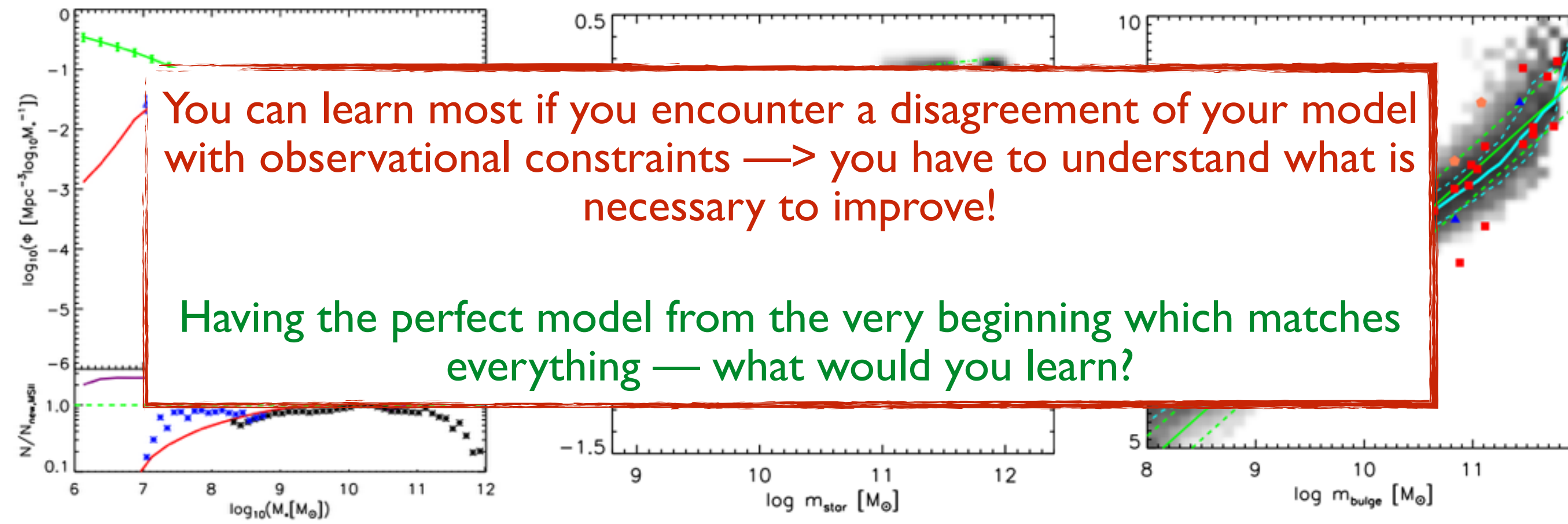
Free parameters for a typical SAM...

Parameter	Description
<i>Quiescent star formation</i>	
A_{KS}	Normalization of Kennicutt law
N_K	Power-law index in Kennicutt law
Σ_{crit}	Critical surface density
<i>Burst star formation</i>	
μ_{crit}	Critical mass ratio for burst activity
<i>SN feedback</i>	
ϵ_{SN}^0	Normalization of reheating fct
α_{rh}	Power-law slope of reheating fct
V_{eject}	Velocity scale for ejecting gas
$\chi_{\text{re-infall}}$	Time-scale for re-infall of ejected gas
<i>Chemical evolution</i>	
y	Chemical yield
<i>Black hole growth</i>	
η_{rad}	Efficiency of conversion of rest mass to radiation
M_{seed}	Mass of seed black hole
$f_{\text{BH,final}}$	Scaling factor for mass after merger
$f_{\text{BH,crit}}$	Scaling factor for critical BH mass
<i>AGN-driven winds</i>	
ϵ_{wind}	Coupling factor for AGN-driven winds
<i>Radio-mode feedback</i>	
κ_{radio}	Normalization of 'radio mode' accretion rate
κ_{heat}	Coupling efficiency of radio jets with hot gas

- This SAM (Somerville+08) has 16 free parameters

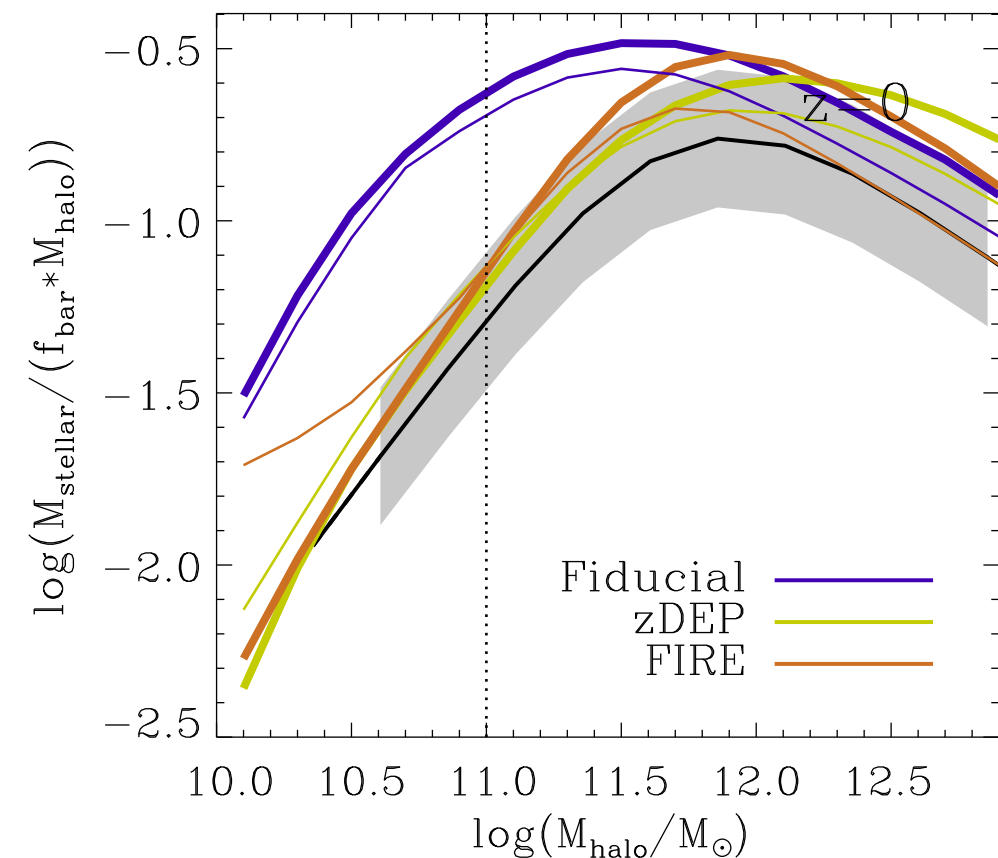
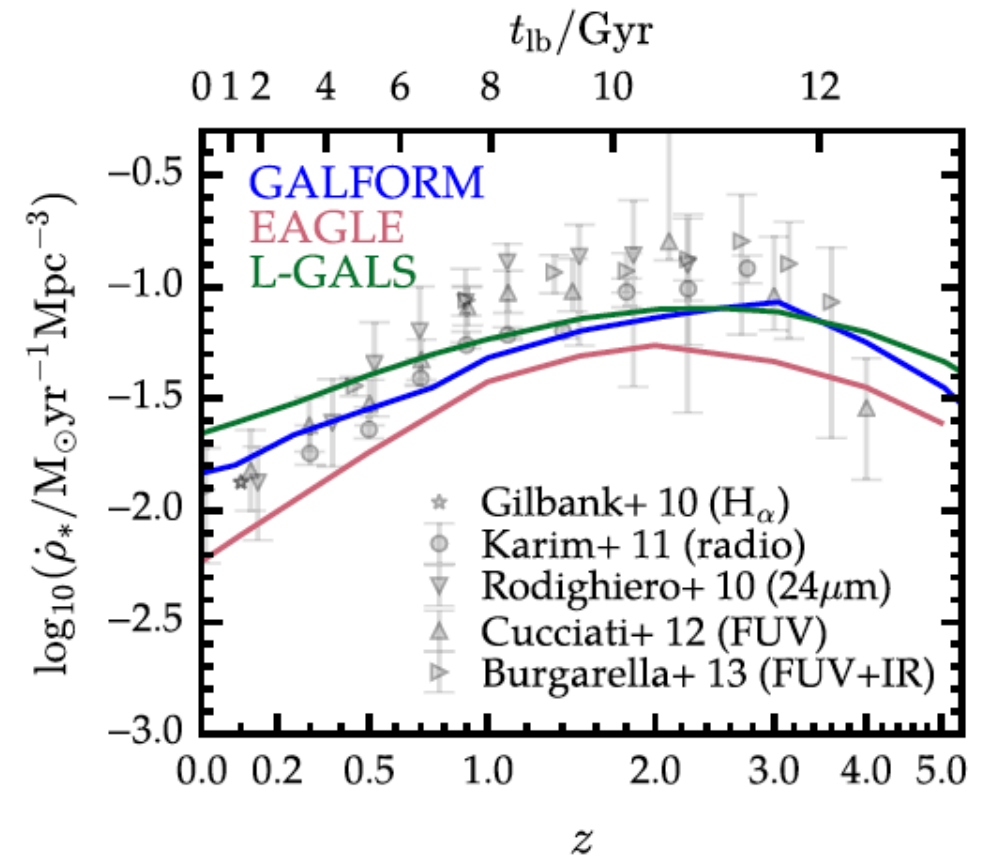
...tuned to...

- ...match a number of different observational data, mostly at the low redshift Universe, as SMF, BH-bulge mass relation, stellar metallicity
- Either tuned “by hand”, or more modern SAMs use Monte-Carlo-Markov-Chains to explore all different combinations of free parameters
- Investigate predictions for other galaxy properties
- Sometimes tuning to some observational data set not possible (i.e. one cannot reproduce “everything” just by re-tuning free parameters)
 - ➡ This indicates the need for more fundamental modifications for some physical models

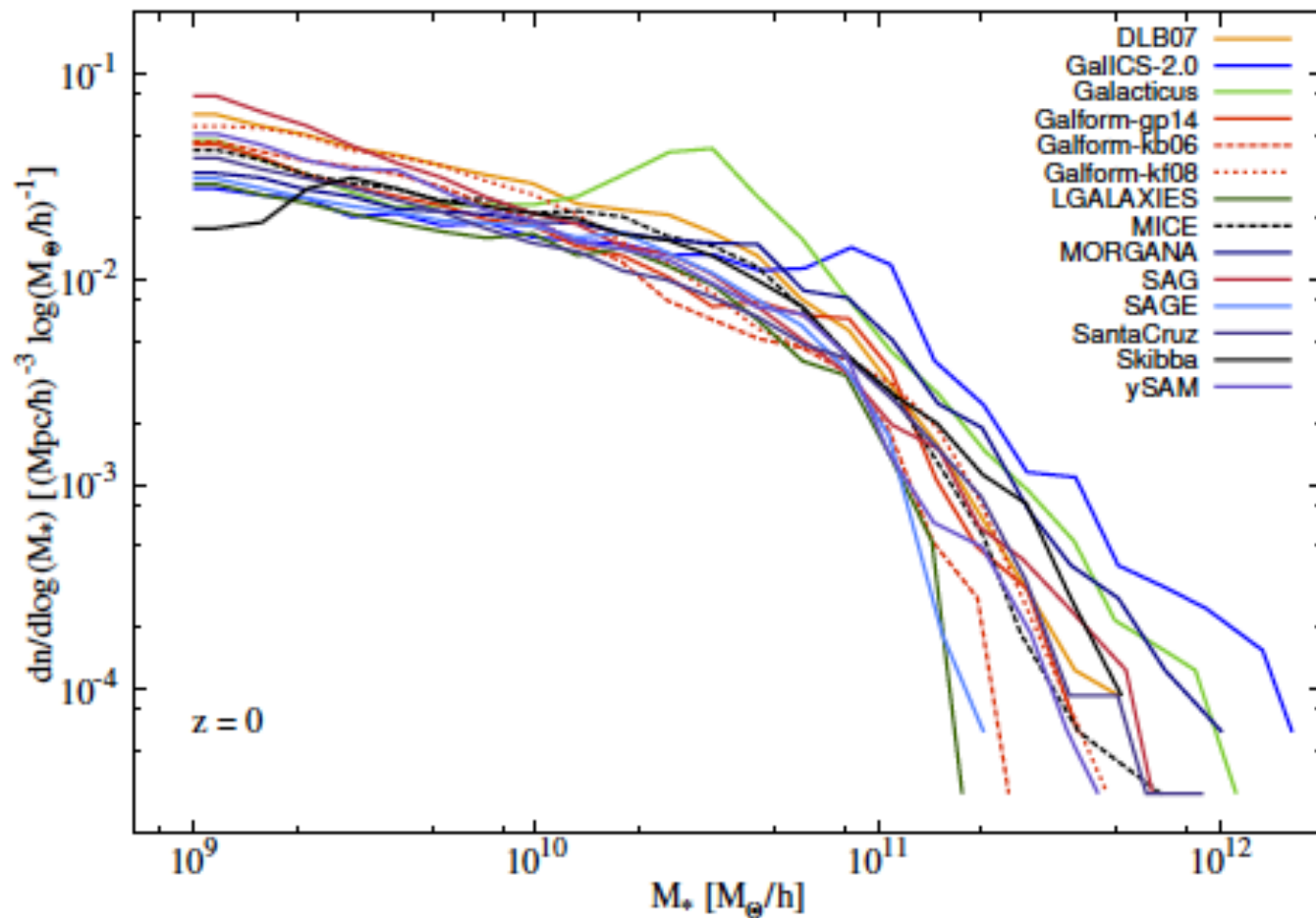


Lessons learned from SAMs...

- Without any mechanism which prevents gas from cooling in massive halos (like jet-mode feedback), SAMs cannot be brought into agreement with the massive end of the stellar mass function and decline of SFR density at $z < 0$
- In addition, SAMs show that stellar feedback is a possibility to suppress SF in low mass halos

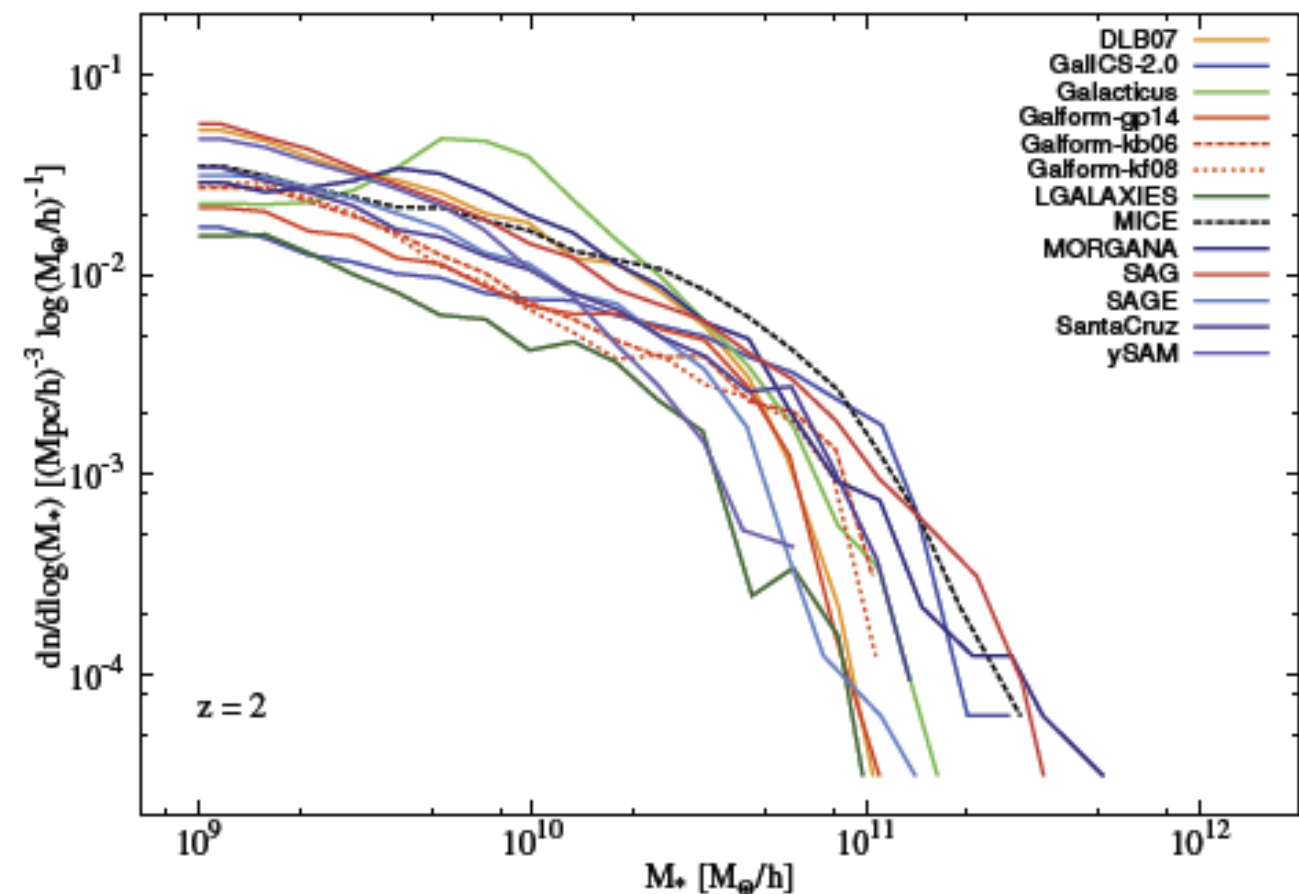


Comparison studies of different SAMs



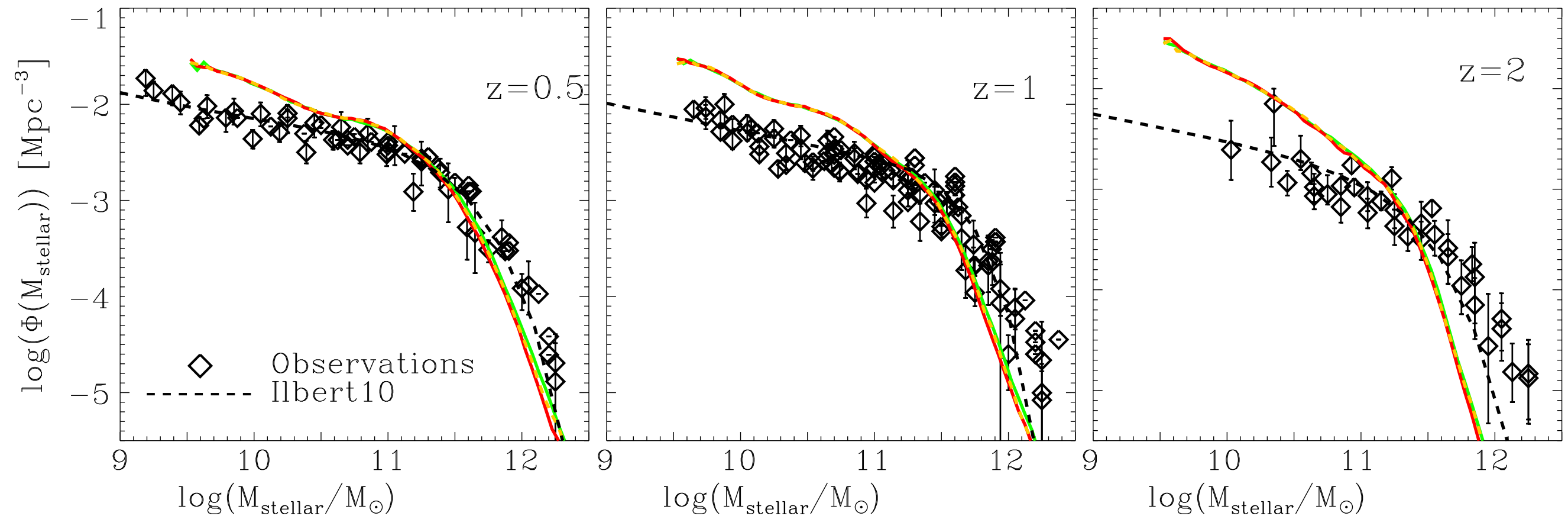
- Different SAMs applied to same merger trees based on same DM simulation
- Stellar mass function at $z=0$ and at $z=2$
- Large scatter at the massive end at $z=0$ and at all masses at $z=2$

- Origin of large scatter is
 - the tuning to different observational data sets
 - **the uncertainty of how to model baryon physics**



are the past and current main
challenges to SAMs?

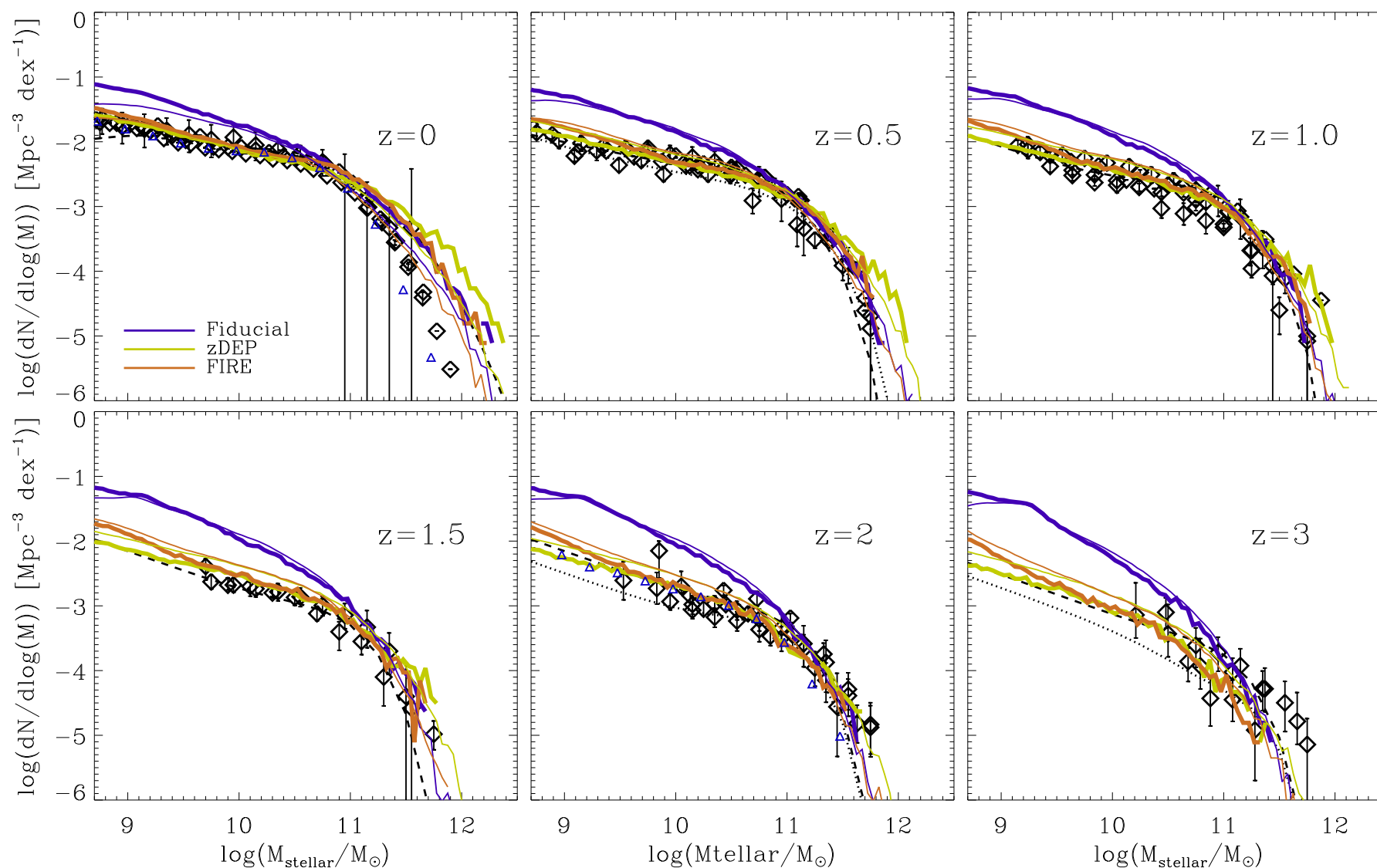
Past challenges... Evolution of the SMF



- Most SAMs (and simulations!!) had/have the problem that they **over-estimate the amount of low-mass galaxies towards higher redshifts**
- Observations instead indicate an antihierarchical behaviour
- Evolution of baryons too tightly coupled to hierarchical evolution of dark matter halos

Past challenges... Evolution of the SMF

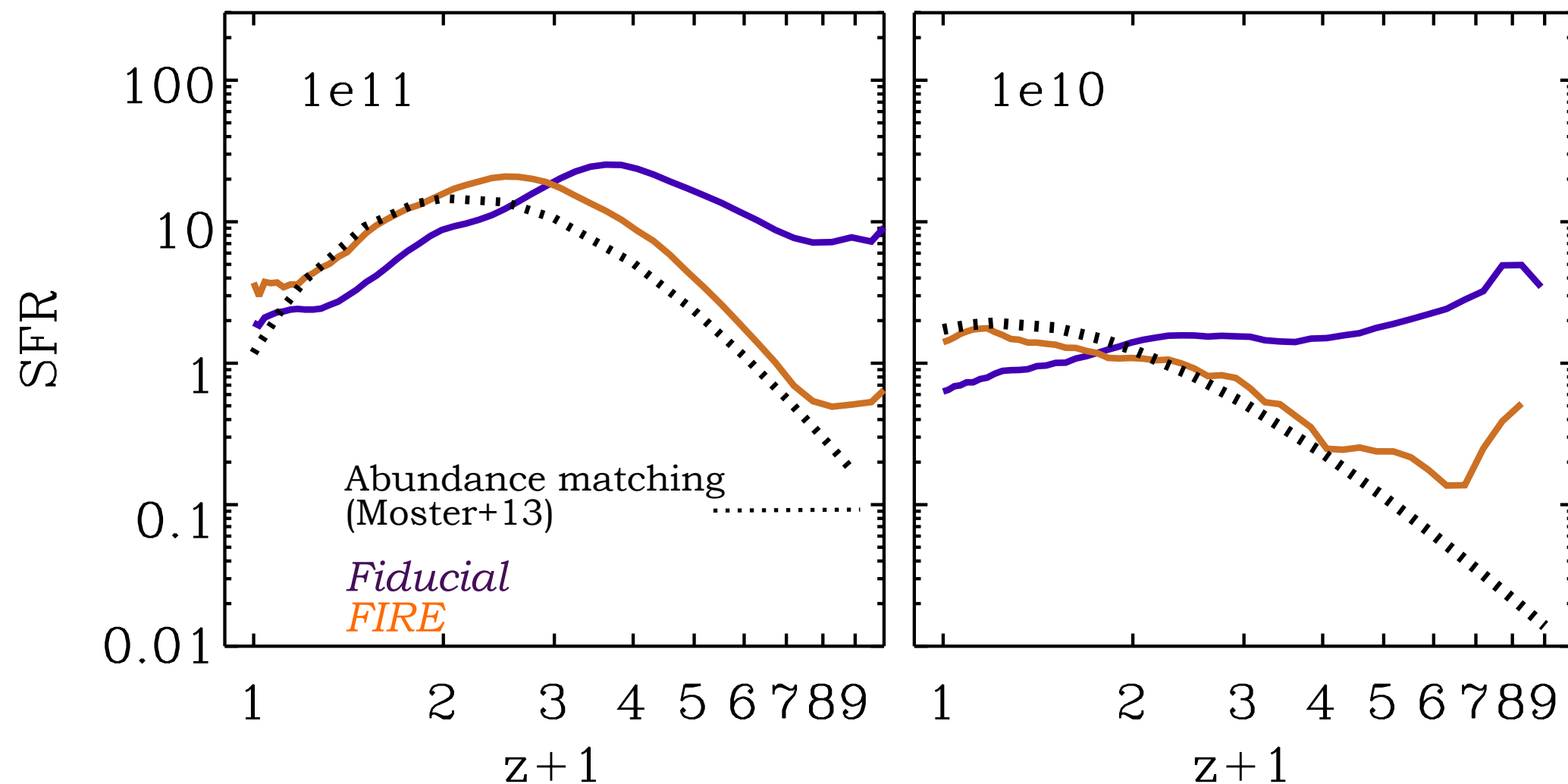
- Different solutions have been proposed over the past decade
- **Strong stellar feedback**: different scalings for re-heating and ejection following hydro-simulations



- Such mechanisms can help to de-couple the evolution of baryons from that of DM halos and to reproduce the anti-hierarchical trend

Past challenges... Evolution of the SFR

- This delayed stellar mass growth in case of **strong stellar feedback** can also be seen when looking at SFR:
 - SFRs of low mass galaxies peak at lower redshift than that of more massive galaxies (anti-hierarchical trend)
 - Consistent with abundance matching constraints/semi-empirical models

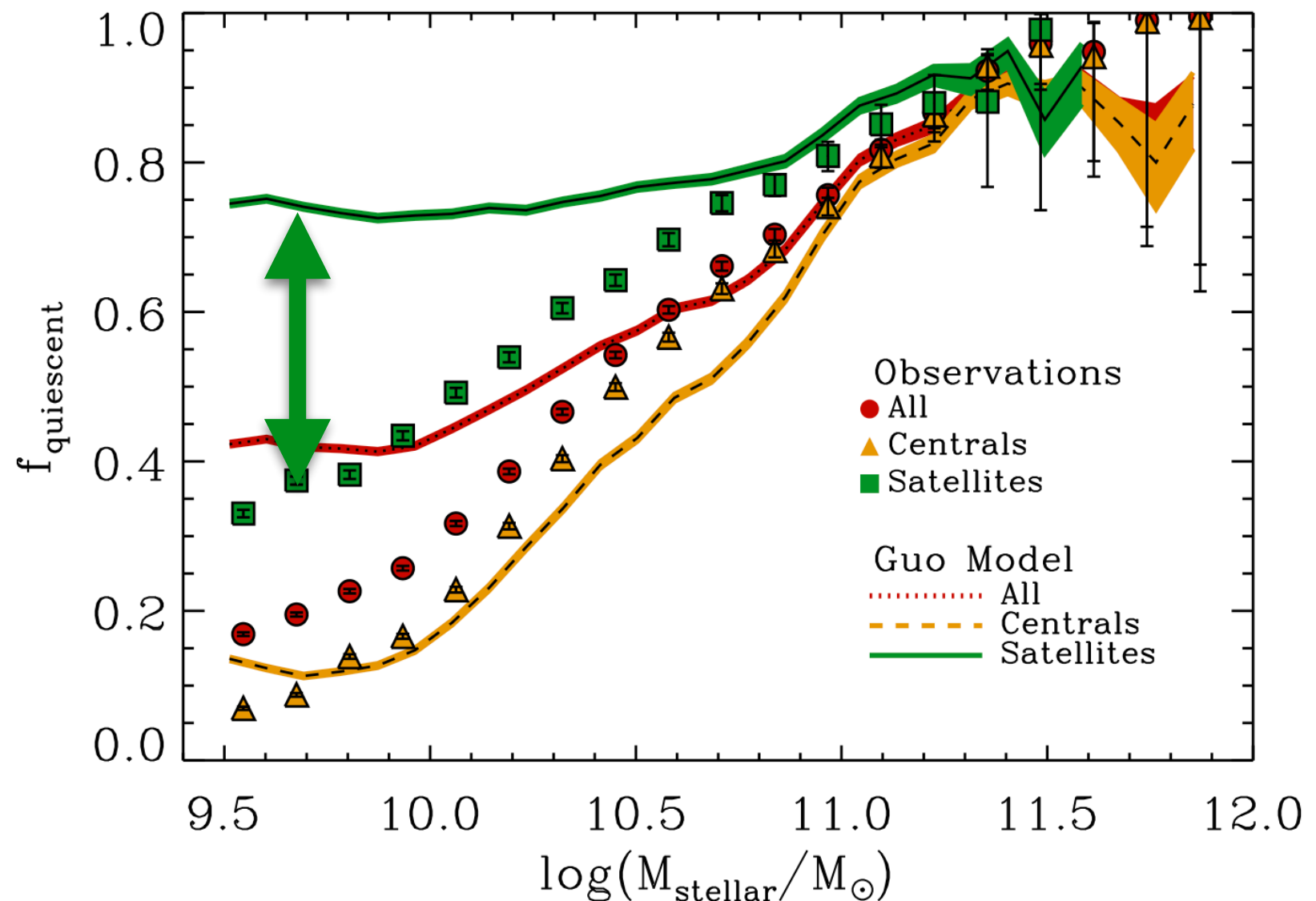


• **With SAMs, no conclusion on origin for strong outflows possible**

Past challenges... Quiescent fractions of sats

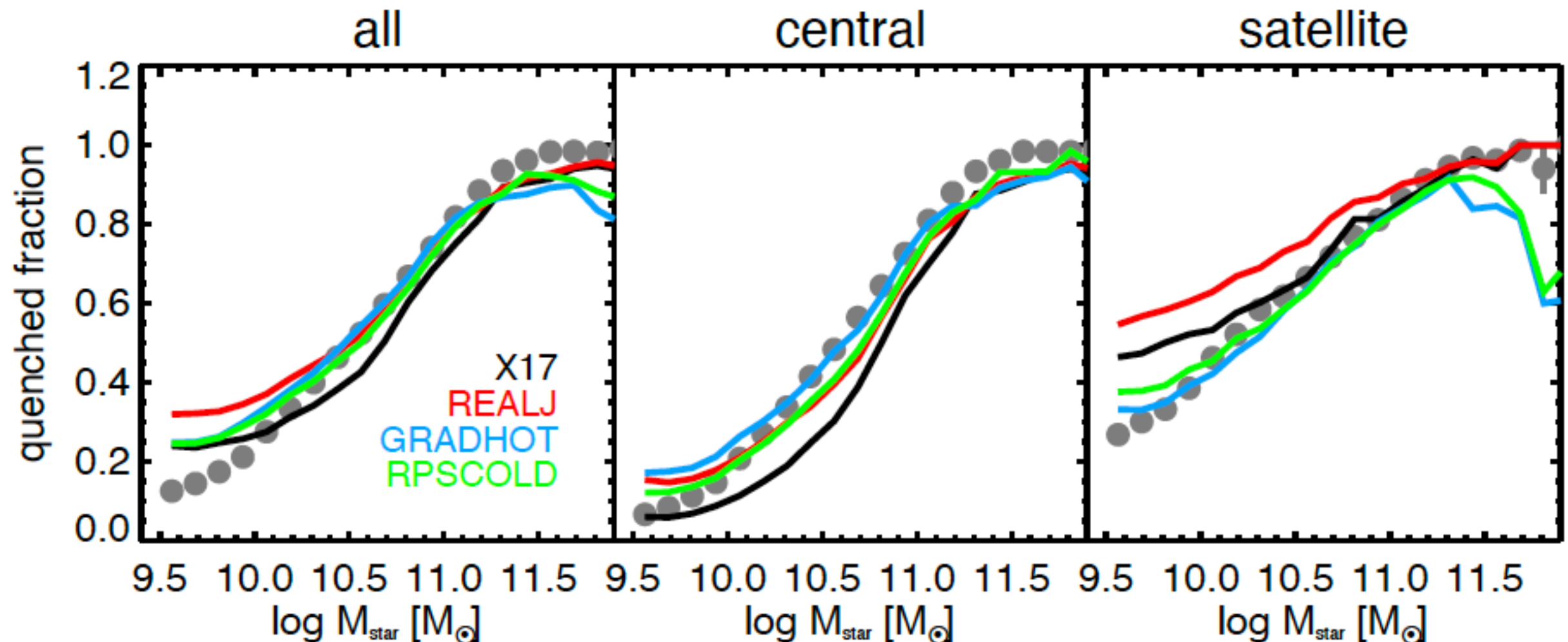
Another long-standing problem of most SAMs:

- Select quiescent galaxies according to their sSFR
- Quiescent fraction of (low-mass) satellites is significantly over-estimated
- Star formation is too fast quenched when a galaxy becomes a satellite \rightarrow too short quenching time-scales
- Partly related to the simplified assumptions of instantaneous strangulation



Past challenges... Quiescent fractions of sats

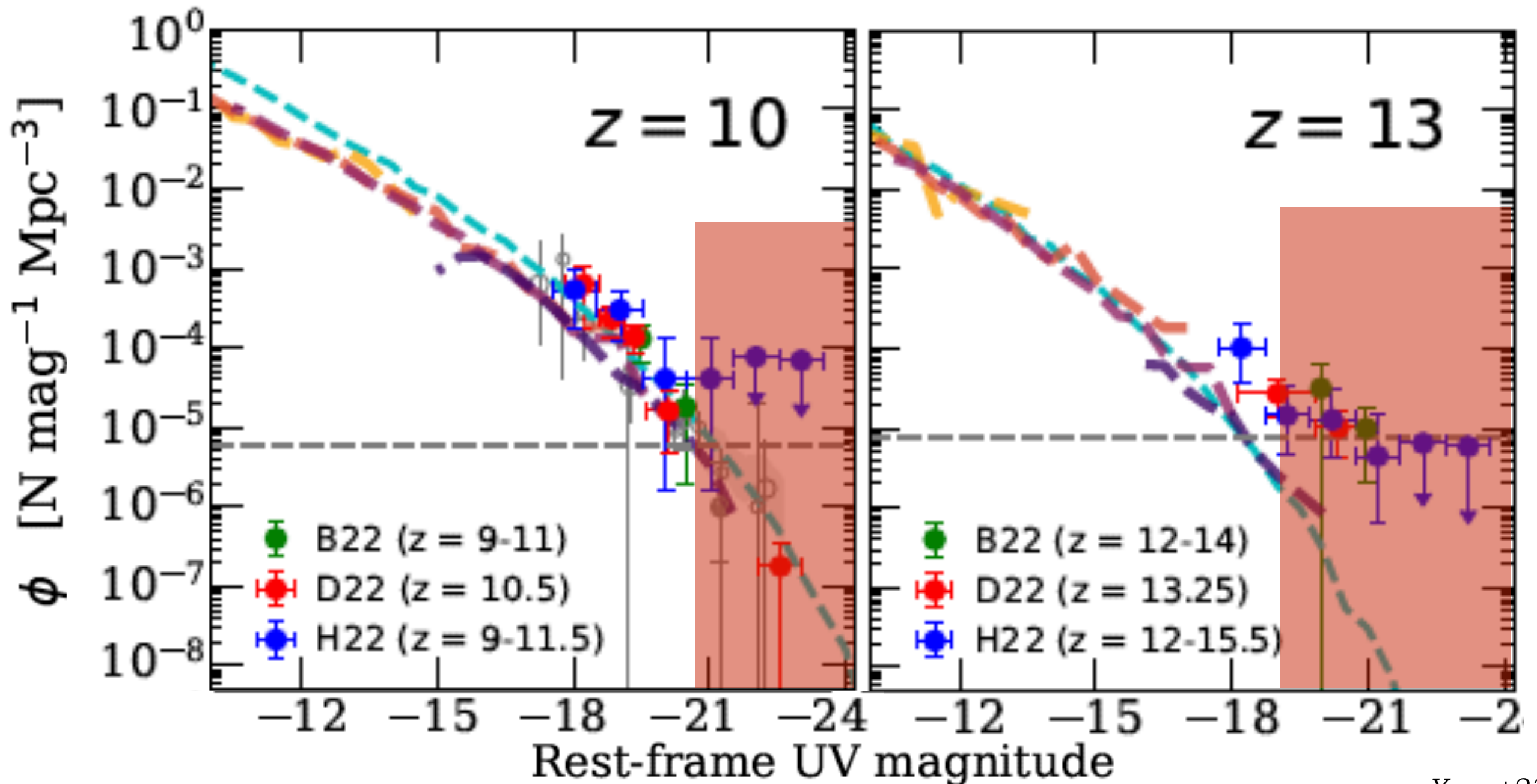
- Changing models stellar feedback and environment in GAEA reduces quiescent satellite fractions, in a better agreement with that observed



- Strong early stellar feedback makes the galaxies more gas-rich at time of infall \rightarrow longer/more SF while being a satellite
- *Gradual* stripping of hot gas, ram-pressure stripping of cold gas instead of *instantaneous* removal of hot gas when becoming a satellite

Challenges... UV luminosity function at $z > 10$

- One of the main current challenges:
- SAMs fail to predict bright galaxies above $z=10$ newly observed with JWST!

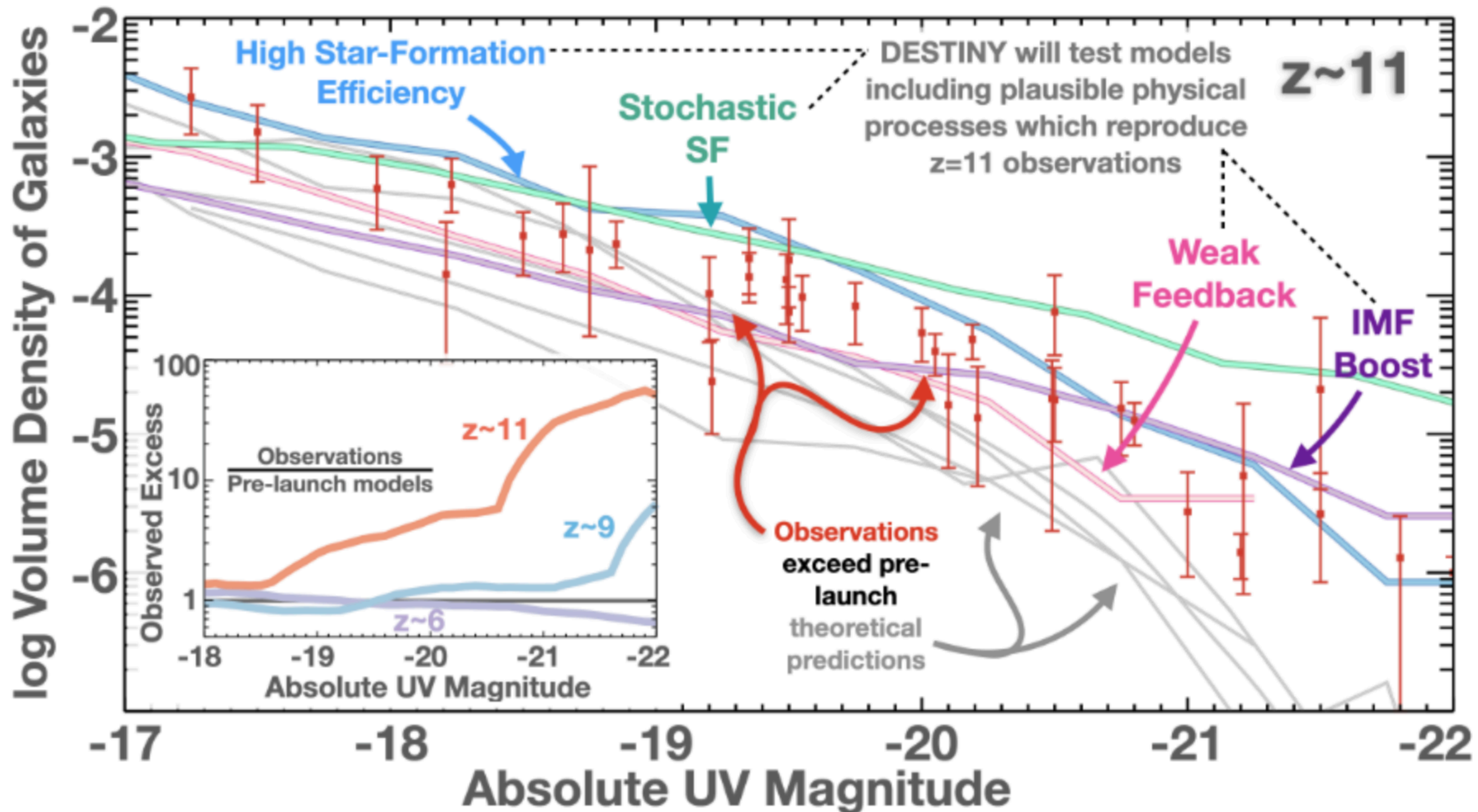


Yung+23

- What could be the reason for this mismatch?

Challenges... UV luminosity function at $z > 10$

- Possible reasons: model deficiencies (SF efficiency, stochastic SF, weak stellar feedback, top-heavy IMF and/or observational uncertainties)



➡ Continuous on-going improvement, but also higher level of complexity...

Pro's and con's of SAMs

PRO:

- SAMs are **flexible** in testing different recipes for different physical processes
- SAMs are **fast** in running over the merger trees
- and thus, they allow for large **statistics with low computational costs**

CON:

- Little to **no spatial information**
- **Simplified approximations**, no direct modelling of a gas fluid
- Many (often degenerate) **free parameters**
- No possibility of understanding the underlying physical processes leading to different, partly more successful recipes
- We can just **capture “global trends”**, no physically based recipes available yet

Summary

- **Galaxies form in the potential wells of DM halos: gas gets trapped due to gravity, cools, condenses form stars...**
- **Galaxy evolution processes:** gas cooling, SF, stellar feedback, BH growth and feedback, mergers, environmental processes etc.
- **Semi-empirical models** helpful to interpret observations in the framework of hierarchically growing DM halos
 - Useful “observational-like” constraints for models with detailed baryon physics
 - No insights in the physical processes at all
- **Semi-analytic models** based on the DM halo merger trees and the evolution of baryons is estimated via phenomenologically motivated differential equations
 - Consistent with many observational constraints, but some unresolved issues remain
 - Information about *global* trends of baryon processes, but underlying physical driving mechanisms often unclear
 - Excellent for a fast testing physical processes in a large cosmological volume

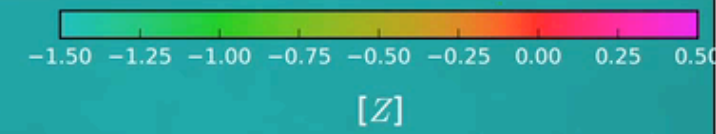
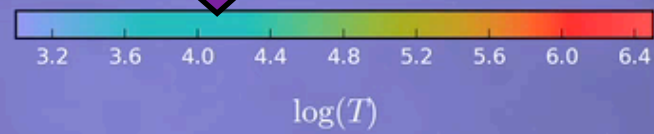
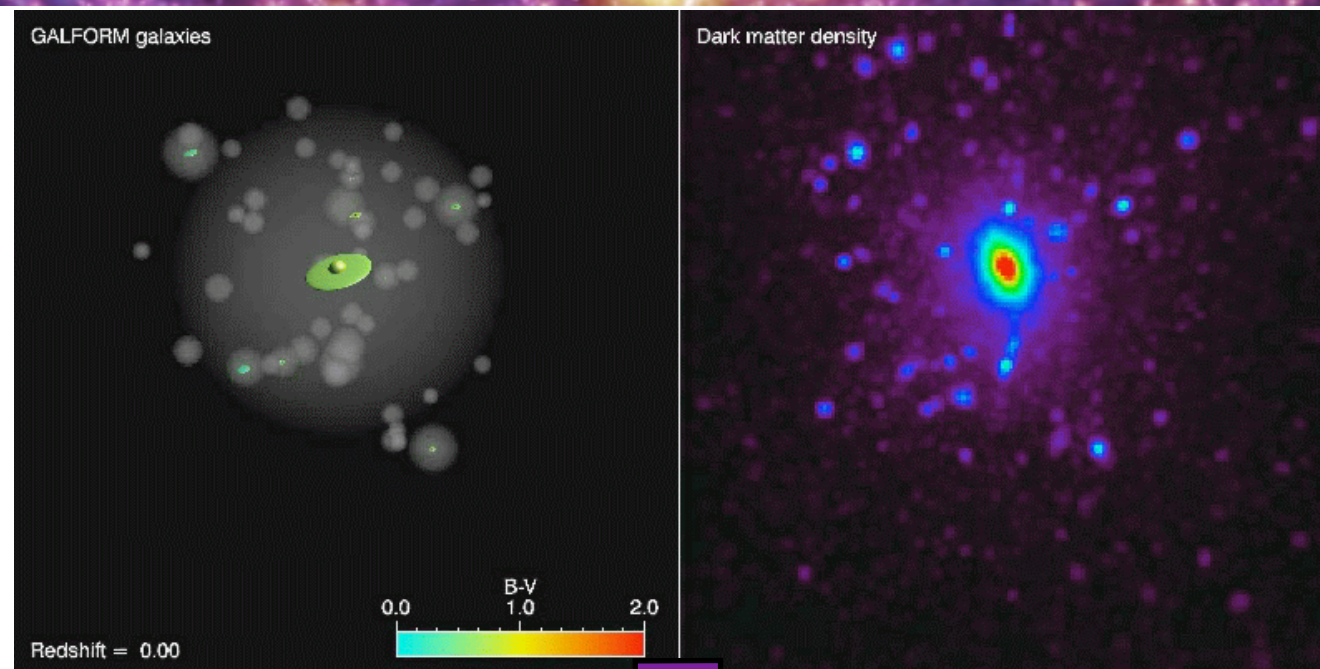
Up next...

- *Chapter 1:* Introduction (galaxy definition, astronomical scales, observable quantities — repetition of Astro-I)
- *Chapter 2:* Brief review on stars
- *Chapter 3:* Radiation processes in galaxies and telescopes;
- *Chapter 4:* The Milky Way
- *Chapter 5:* The world of galaxies I
- *Chapter 6:* The world of galaxies II
- *Chapter 7:* Black holes and active galactic nuclei
- *Chapter 8:* Galaxies and their environment;
- *Chapter 9:* High-redshift galaxies
- *Chapter 10:*
 - Cosmology in a nutshell; Linear structure formation in the early Universe
- *Chapter 11:*
 - Dark matter and the large-scale structure
 - Cosmological N-body simulations of dark matter
- *Chapter 12:* Populating dark matter halos with baryons: Semi-empirical & semi-analytical models
- *Chapter 13:* Modelling the evolution of gas in galaxies: Hydrodynamics
- *Chapter 14:* Gas cooling/heating and star formation
- *Chapter 15:* Stellar feedback processes
- *Chapter 16:* Black hole growth & AGN feedback processes
- *Chapter 17:* Modern simulations & future prospects

Part I:
Observational
basics & facts of
galaxies
first 7 lectures

Part II:
Theory & models
of
galaxy evolution
processes
second 7 lectures

Cosmological hydrodynamic simulation



50 kpc

$t = 0.261$ Gyr
 $z = 15.67$

50 kpc

50 kpc