

# Nuclear Fusion and Plasma Physics

## Lecture 9

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Ohmic heating

The need for auxiliary heating

ITER auxiliary heating systems

Neutral beam heating

Heating by waves

Electron Cyclotron

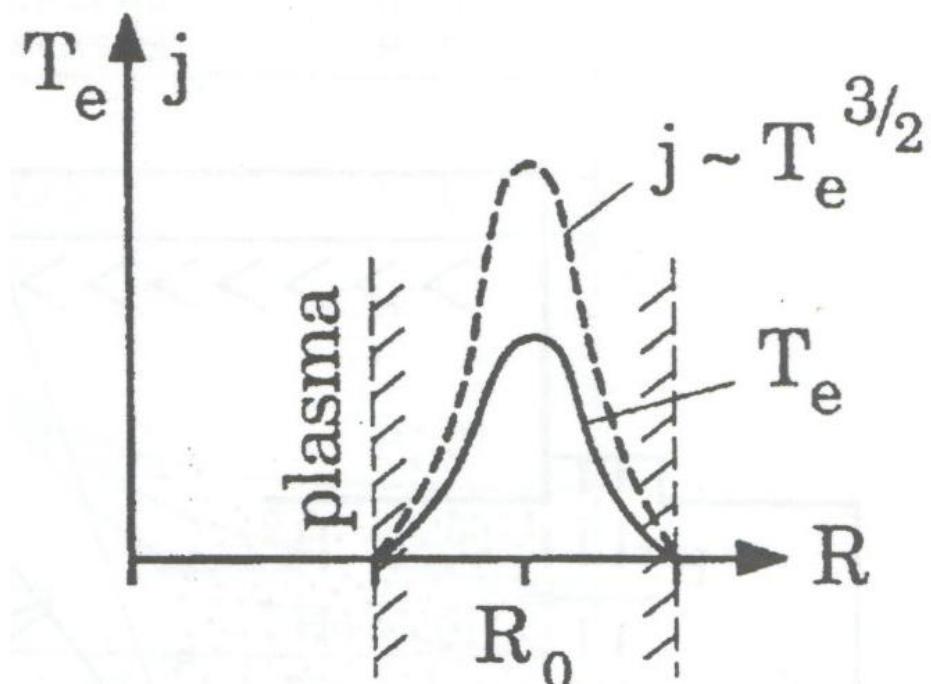
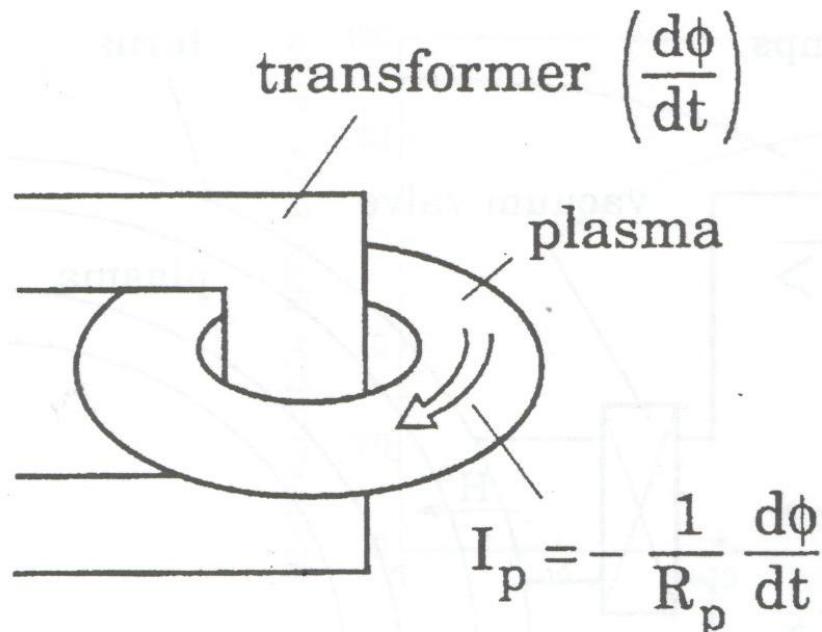
Ion Cyclotron

Lower Hybrid

Discussion

Pros and cons of the different methods

# Ohmic heating

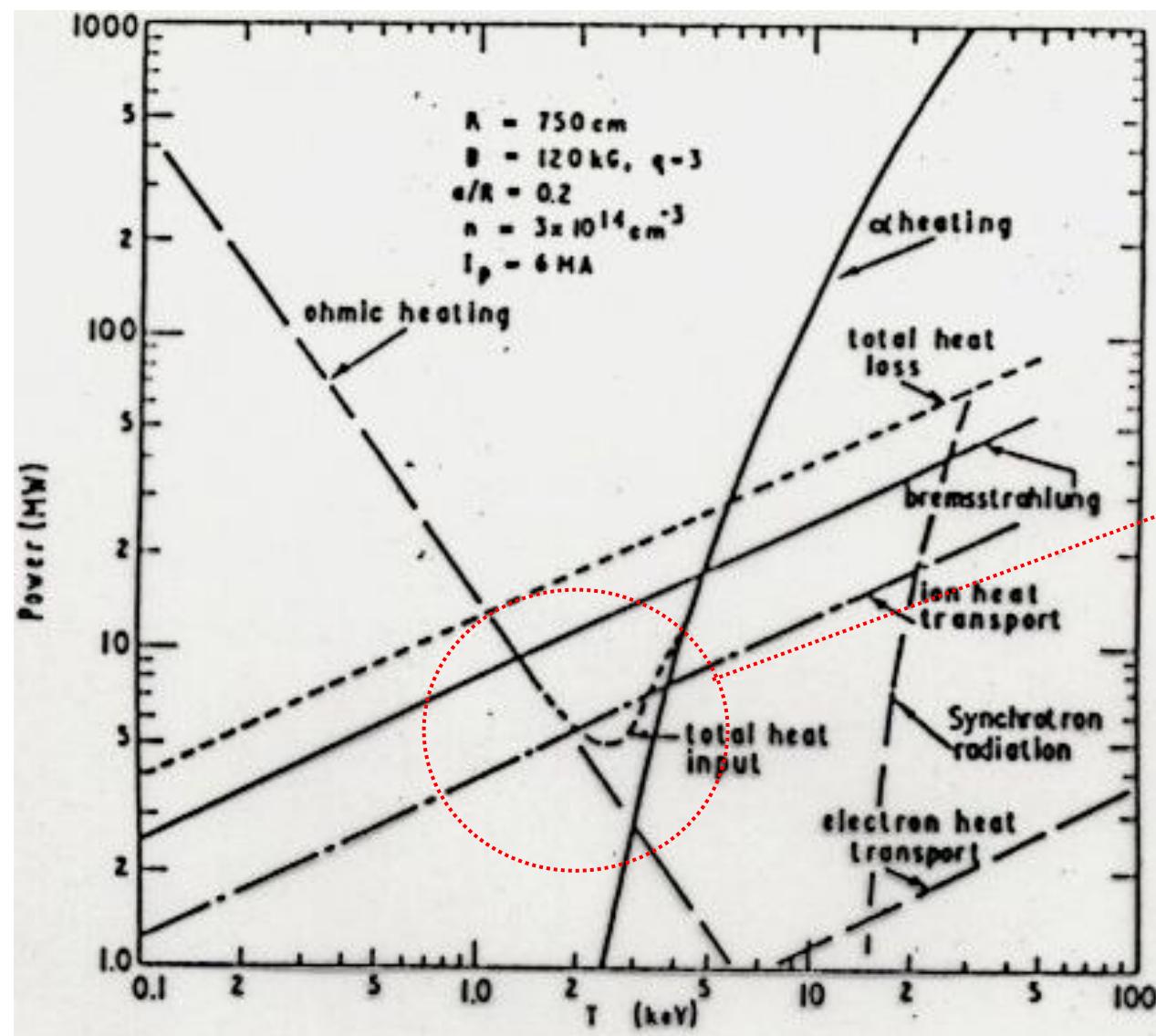


$$P_{\text{ohmic}} = V_{\text{loop}} \times I_p = R_p \times I_p^2 = \eta j^2$$

$$\eta = \frac{\sqrt{2}}{\pi^{3/2}} \frac{m_e^{1/2} Z e^2 \ln \Lambda}{12 \epsilon_0^2 T_e^{3/2}} \propto T_e^{-3/2}$$

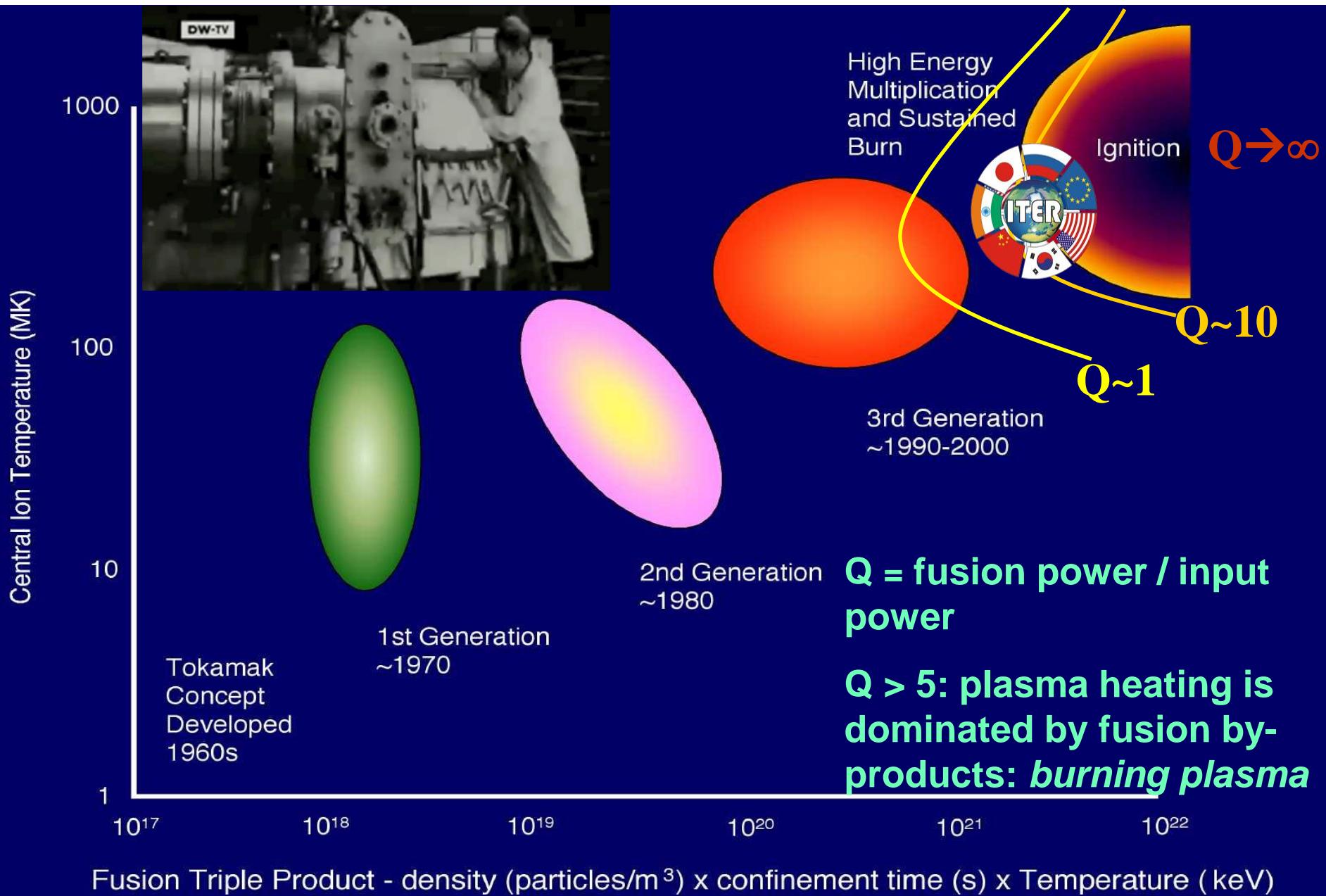
*OH heating becomes less and less effective at high  $T_e$*

# The need for additional plasma heating



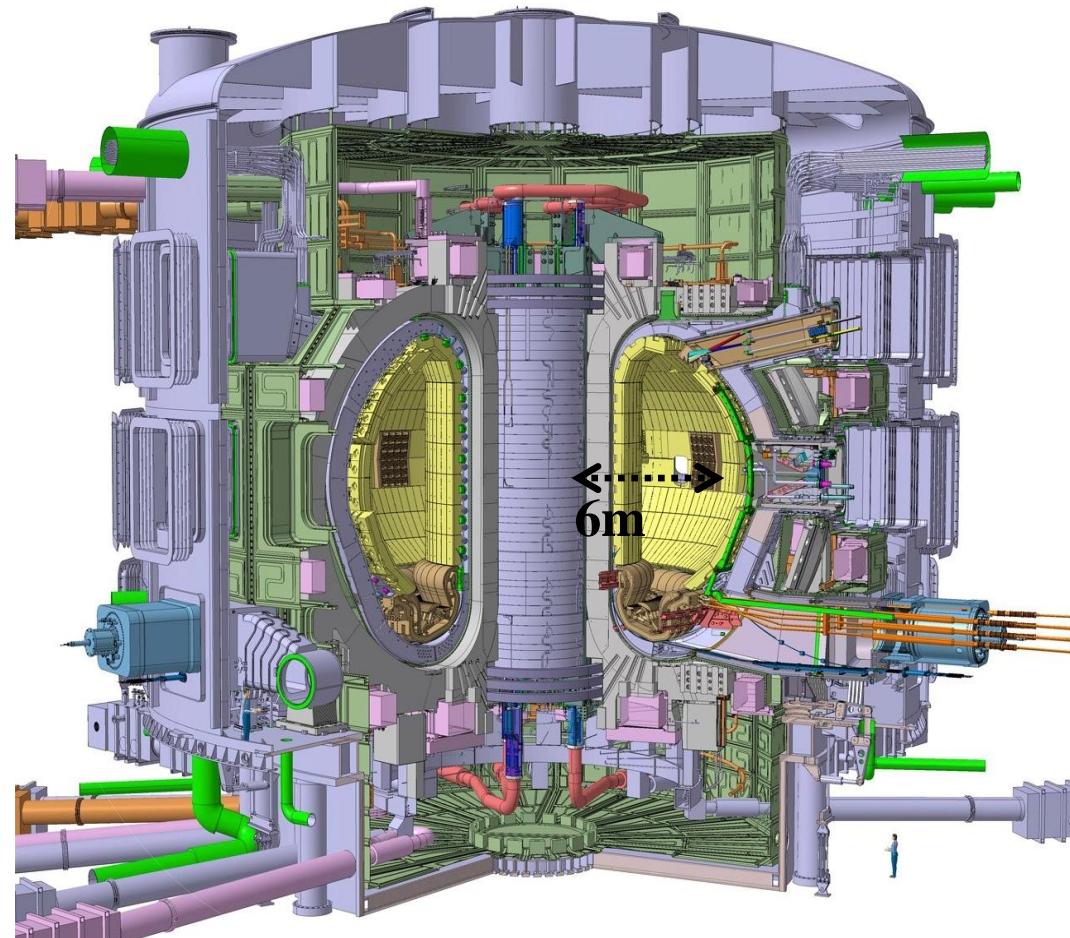
Need to fill in ‘gap’ between ohmic heating region and  $\alpha$ -heating, where losses dominate

# Progress in magnetic fusion



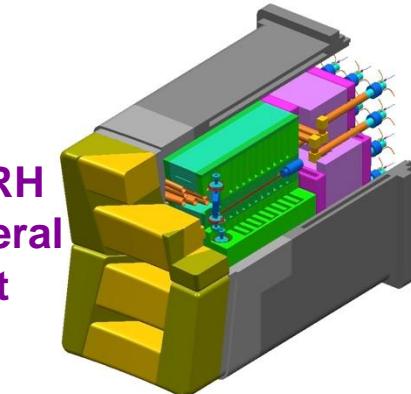
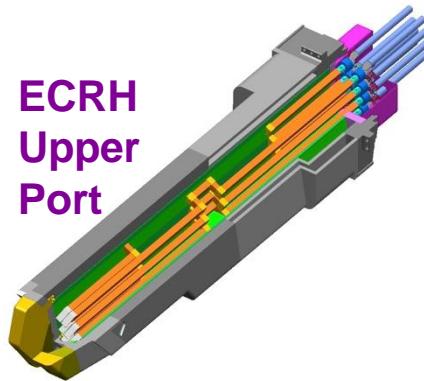
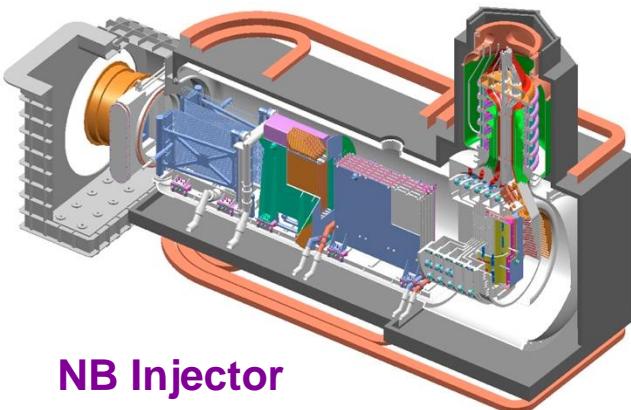
*Demonstration of the scientific and technological feasibility of fusion energy for peaceful purposes*

Burning plasma  
 $Q \geq 10$   
 $P_{\text{fusion}} \geq 500\text{MW}$   
for  $\sim 500\text{s}$

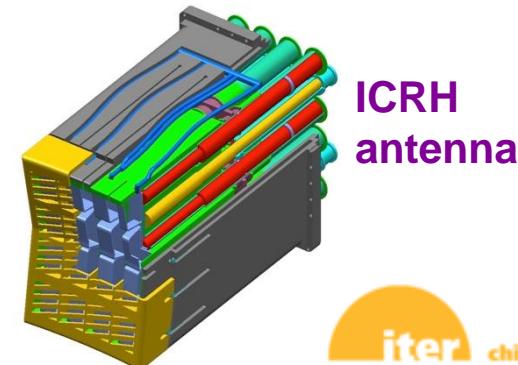


$R \sim 6\text{m}$ ;  $B \sim 5\text{T}$ ;  $I_{\text{plasma}} \sim 15\text{MA}$

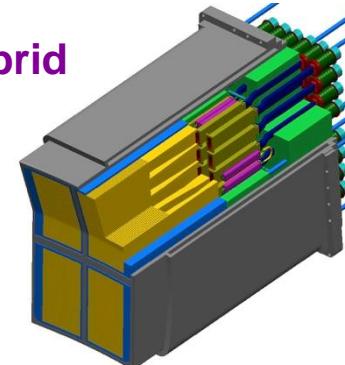
## ITER Heating systems



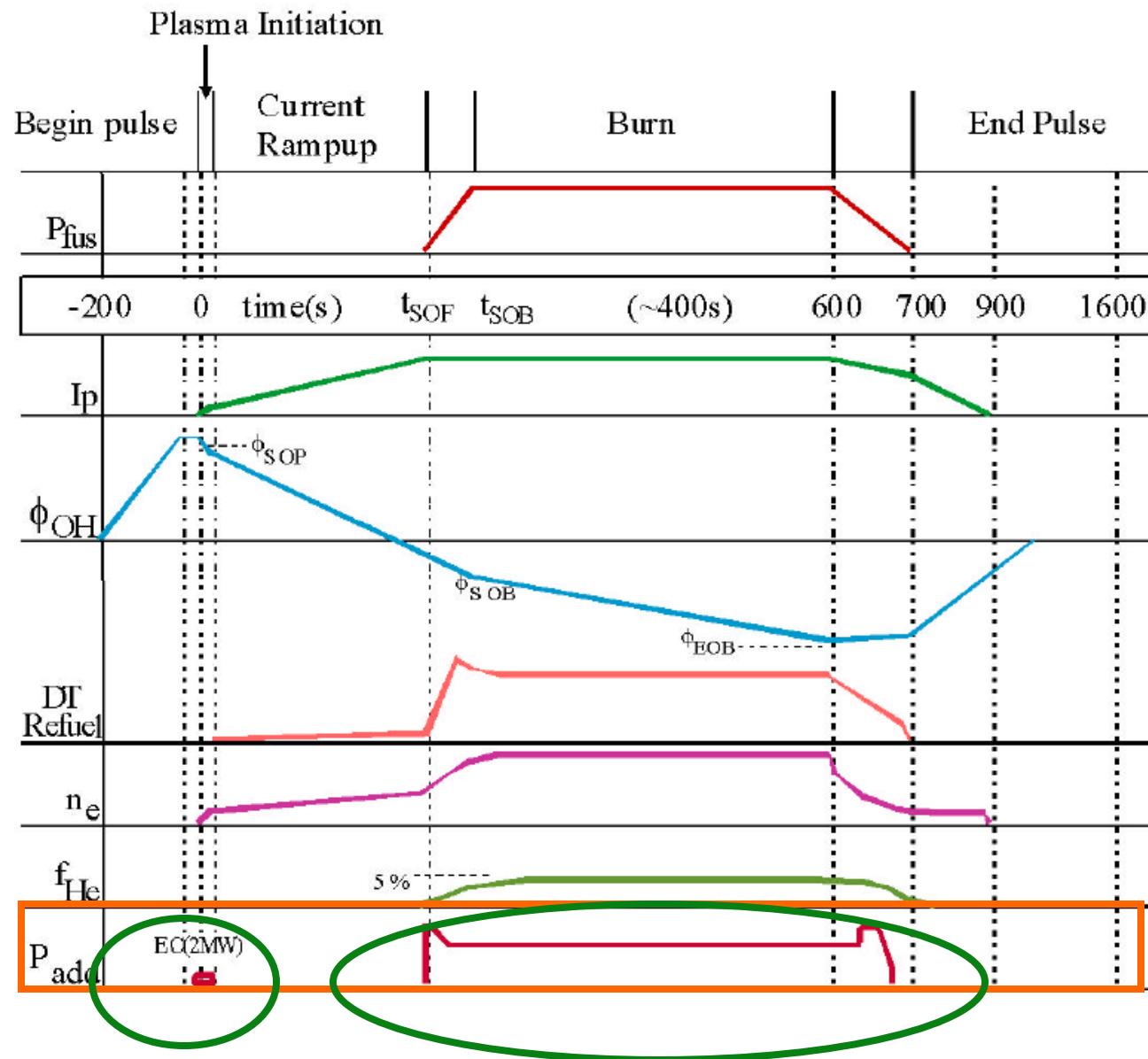
System	Power [MW]	Frequency
NBI	33 MW	N/A
ICRH	20 MW	40-55 MHz
LH	20 MW ( <i>second stage</i> )	5 GHz
ECRH	67 MW	170 GHz



Lower Hybrid  
Launcher

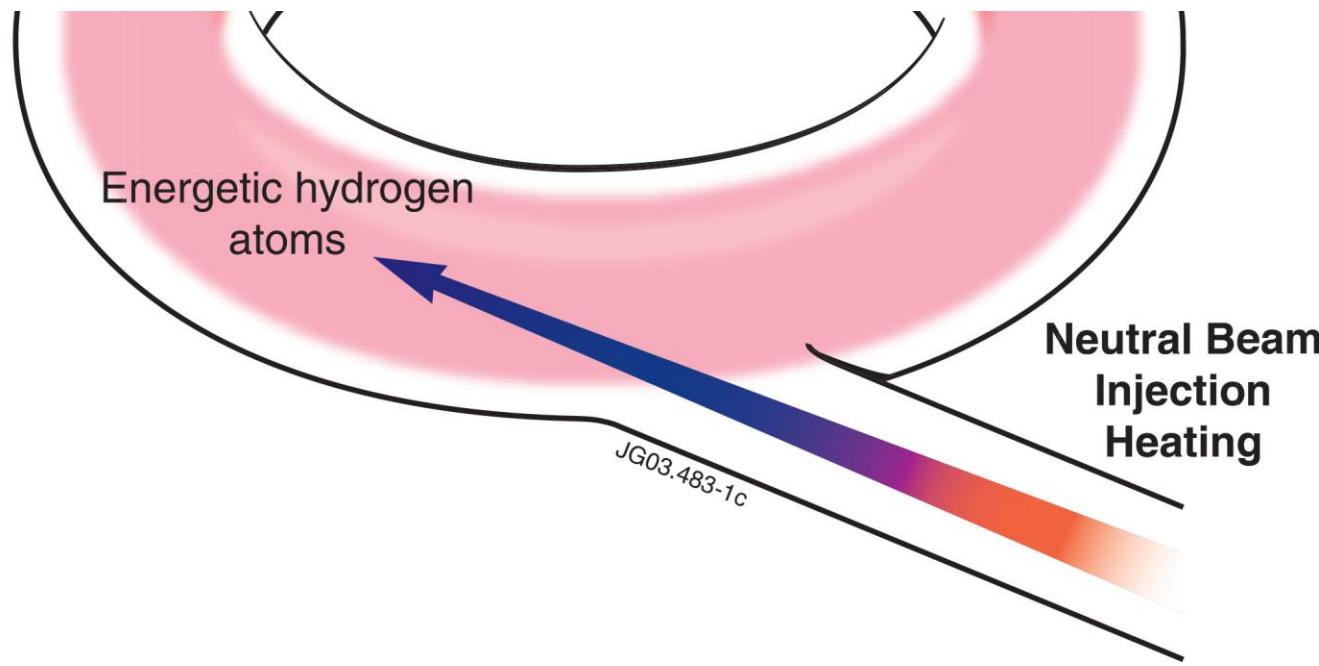


## ITER plasma sequence



# Heating by neutral beam injection

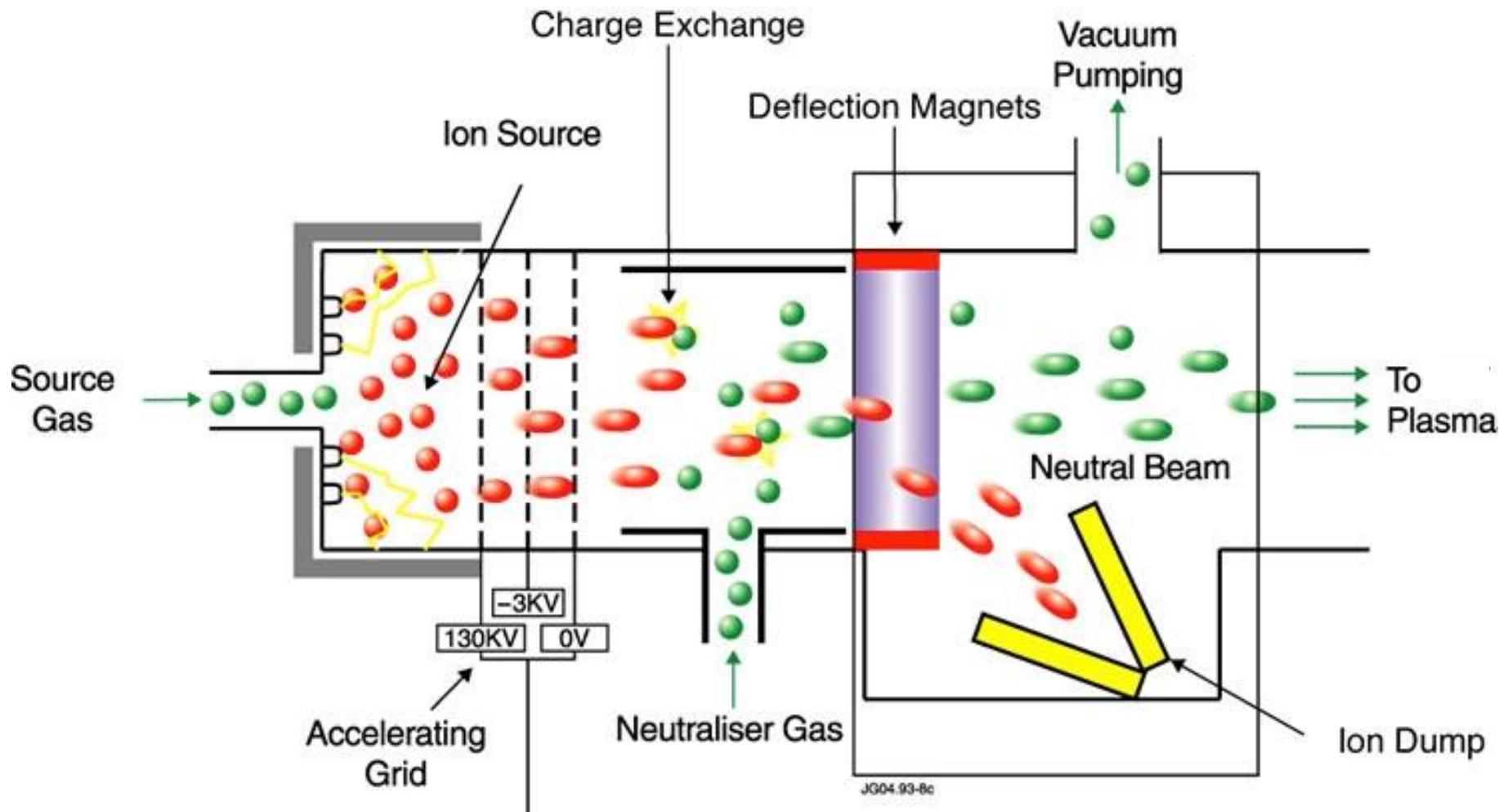
# Basic idea of Neutral Beam Heating



Energetic ions could be injected into plasma, to give energy to *colder* plasma particles, but B-field would prevent energetic ions penetration

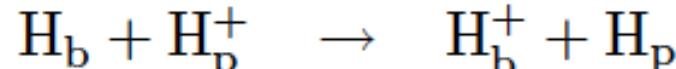
Idea: use neutral particles at high energy to get into the plasma, then let them be ionized by the plasma itself, so that they become a beam of energetic ions

# Neutral Beam Injector



# Physical processes occurring during beam penetration in plasma, leading to ionization

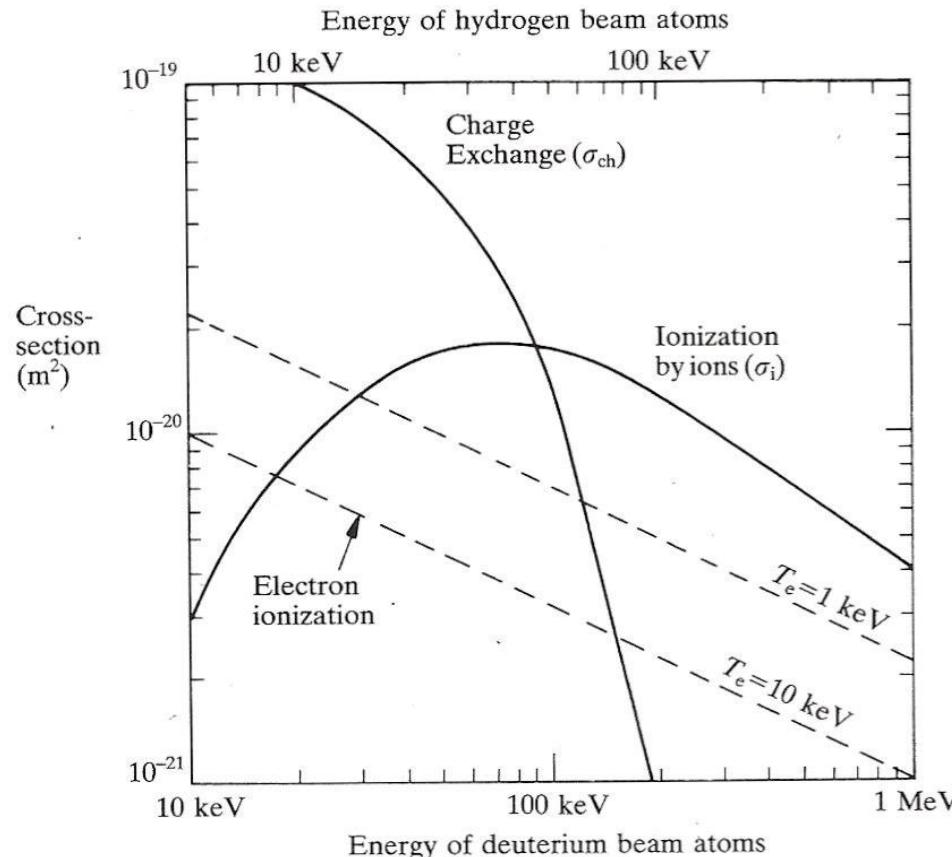
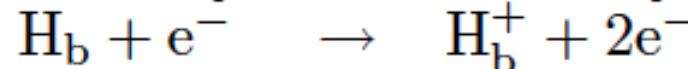
Charge exchange:



Ionization by ions:

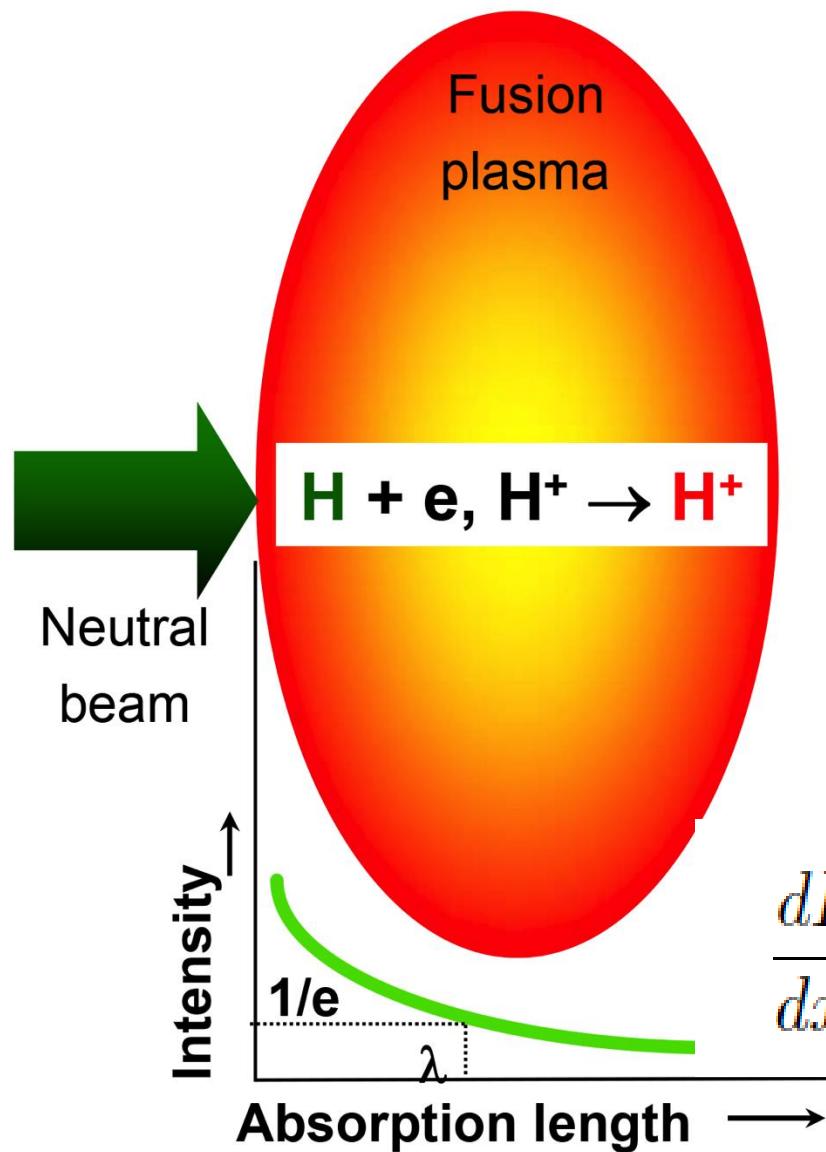


Ionization by electrons:



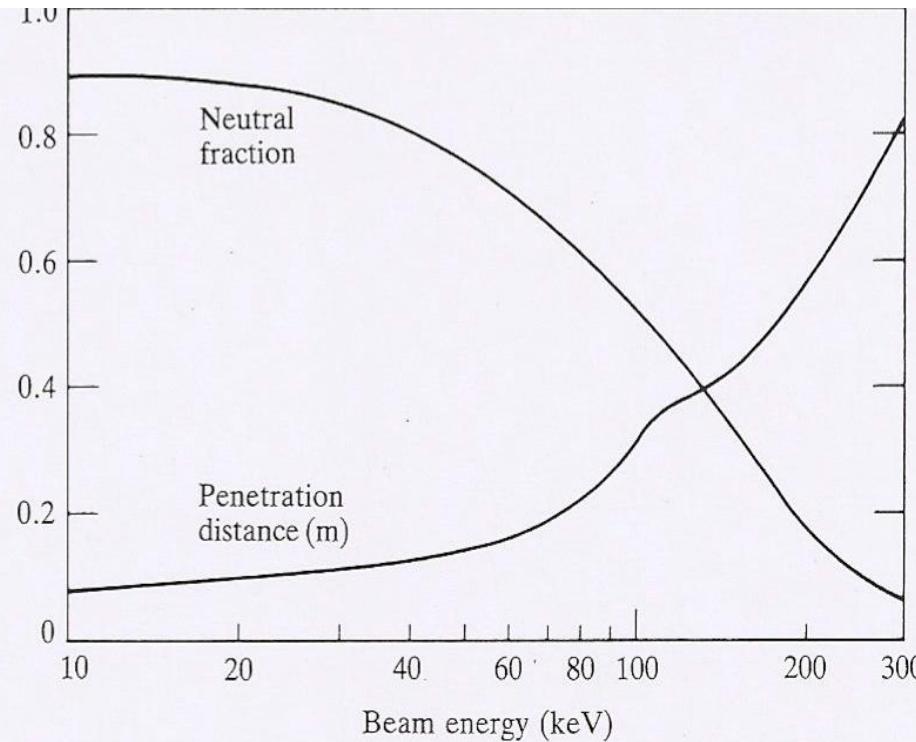
**Fig. 5.3.1** Cross-sections for charge exchange and ionization by plasma ions (protons, deuterons, or tritons) and the effective cross-section  $\langle \sigma_e v_e \rangle / v_b$  for ionization by electrons, as functions of the neutral beam energy. The cross-sections for a hydrogen beam are the same as those for a deuterium beam having twice the energy.

## Evolution of beam intensity



$$\frac{dI}{dx} = - n_p \left( \sigma_{ch} + \sigma_i + \frac{\langle \sigma_e v_e \rangle}{v_b} \right) I$$

$\lambda$  = penetration distance

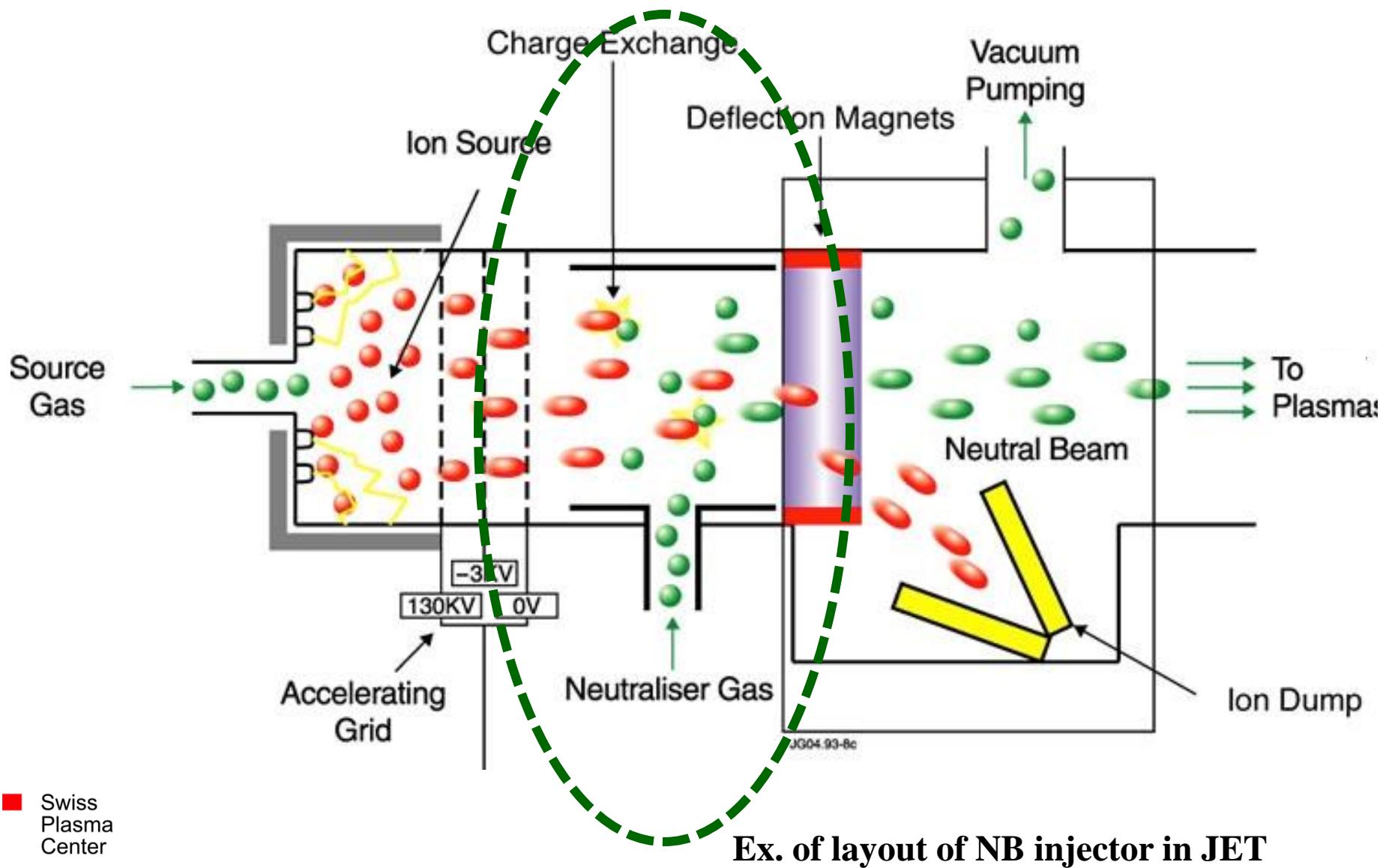


**Fig. 5.5.3** Graphs showing the energy dependence of (i) the equilibrium neutral fraction in a deuterium beam and (ii) the penetration distance of the neutrals in a plasma of density  $n = 10^{20} \text{ m}^{-3}$ . The change of behaviour of the penetration distance at around 100 keV indicates the transition from charge exchange dominance to ionization dominance.

For large plasma ( $>1\text{m}$ ) we need high beam energies ( $>300\text{keV}$ )

# Neutral Beam Injector

## Neutralisation



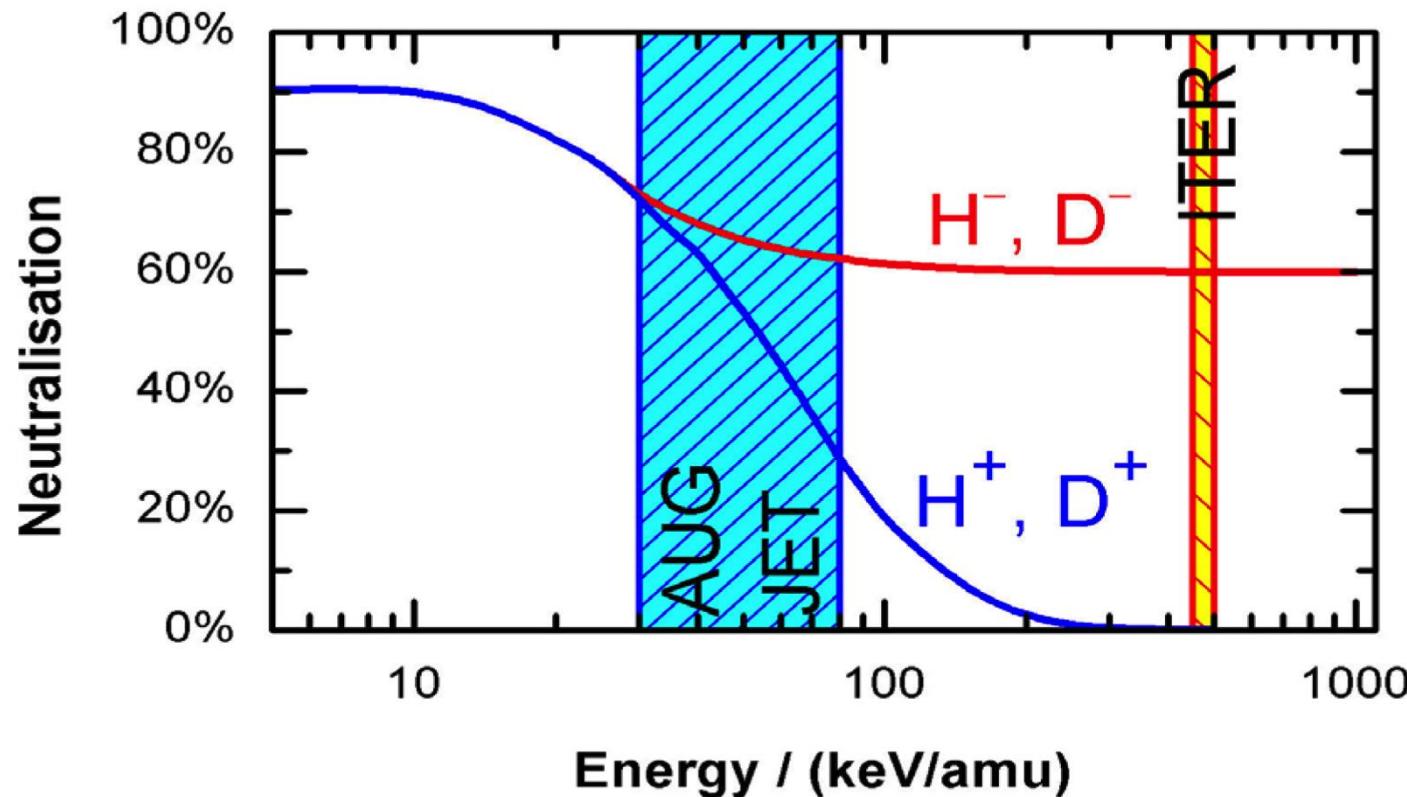
# NBI: neutralisation efficiency

Efficiency for positive ions goes down for high energies

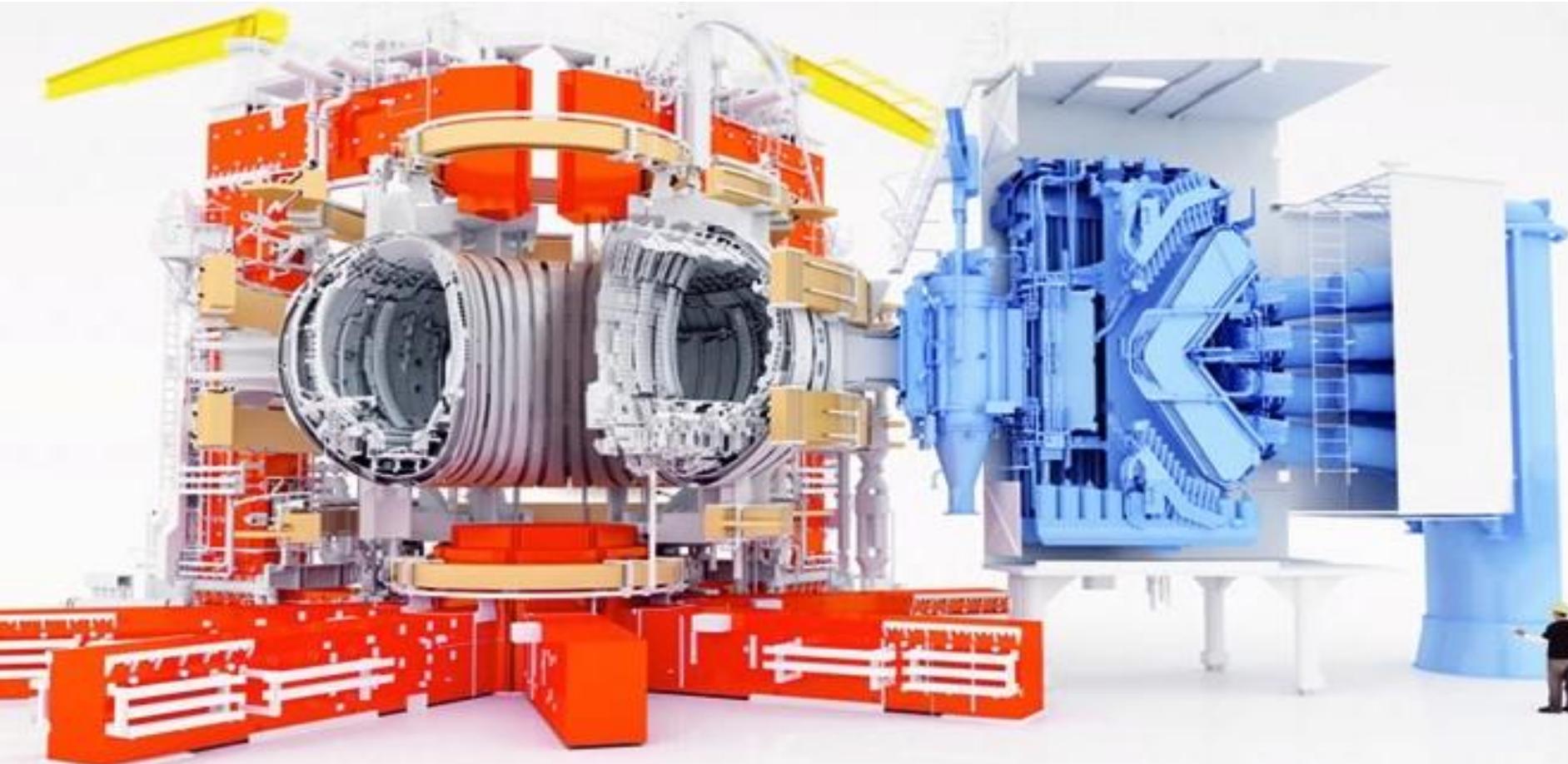
Negative ion neutralisation easier due to low affinity

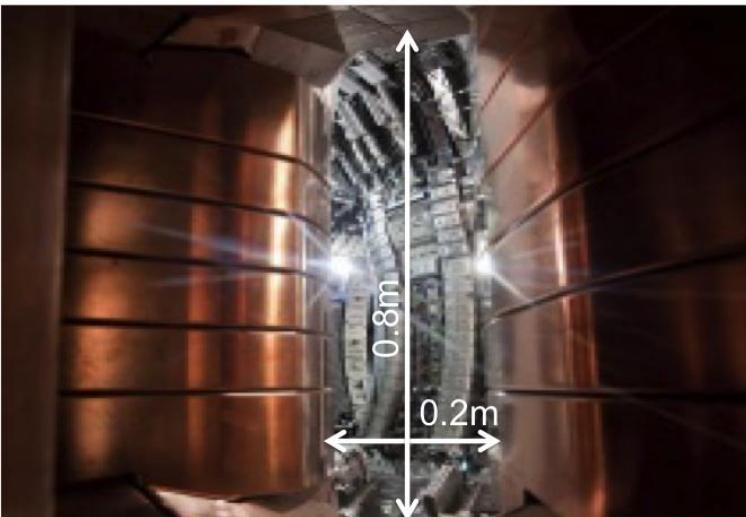
(0.75eV) of additional electron:  $H^- + H_2 = H + H_2 + e^-$

For large, dense plasmas we need negative ion beams

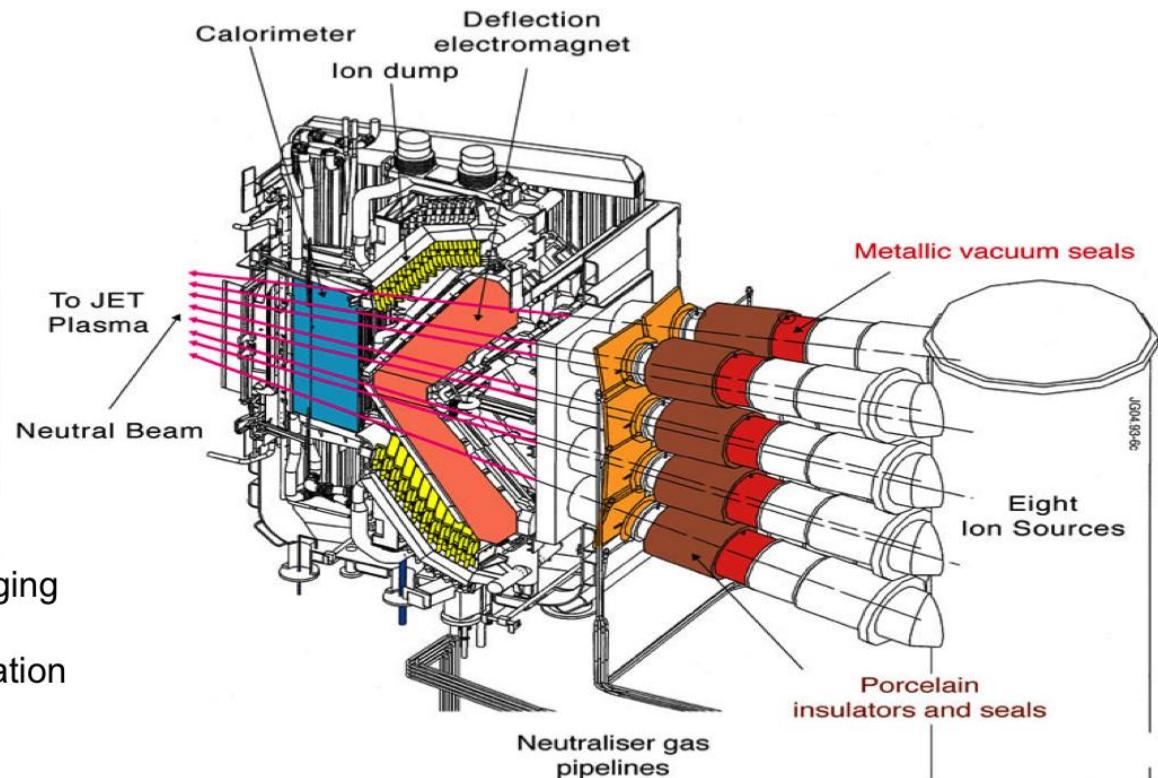


Radial and tangential injection; 2x8 injectors 80keV (H<sup>+</sup>), 130keV (D<sup>+</sup>) – up to 34MW





Beam divergence must be low to avoid damaging beam duct and outgassing from beam-wall interactions, which would block beam propagation



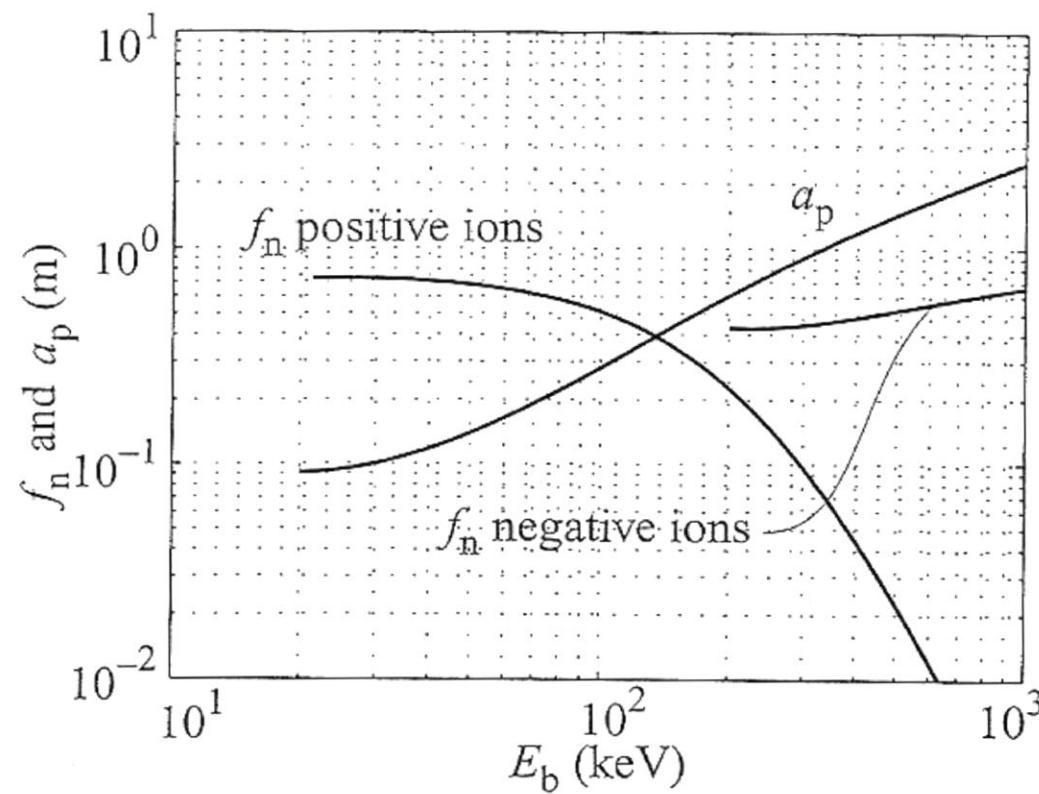


Figure 15.5 Neutralization fraction vs. beam energy for positive and negative ion beams. Also plotted is the penetration depth for  $n_{20} = 1.5$ . (Wesson, J. (2004). *Tokamaks*, third edition. Oxford: Clarendon Press).

# Which species will be heated by the beam?

**Collisional Theory:** the energy transfer from fast ions (originating from a beam) to the plasma particles (electrons and ions) results in plasma heating. This process is governed by collisional interactions.

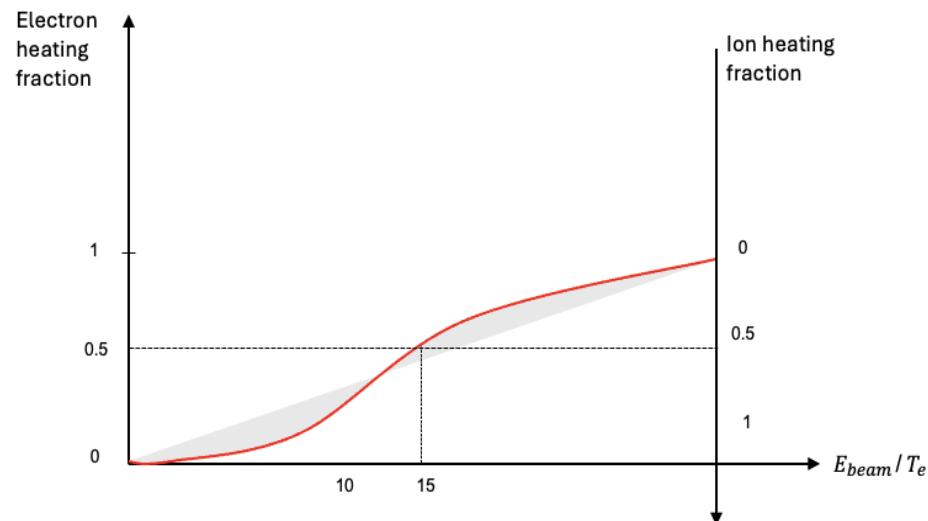
Where:

$$P = -\frac{2 E_{\text{beam}}}{\tau_{\text{SD}}} \left[ 1 + \left( \frac{E_{\text{crit}}}{E_{\text{beam}}} \right)^{3/2} \right]$$

- $P$ : Power transferred to the plasma.
- $I$ : Current of the ion beam.
- $E_{\text{beam}}$ : Energy of the fast ions in the beam.
- $\tau_{\text{SD}}$ : Slowing down time, the time it takes for the fast ions to lose energy through collisions.
- $E_{\text{crit}}$ : Critical energy at which the heating of electrons and ions is balanced.

The **critical energy**  $E_{\text{crit}} \approx 15 T_e \left[ \frac{M_{\text{beam}}}{m_e} \sum \frac{n \cdot Z_i^2}{n_e} \right] \approx 15 T_e$  is the energy at which the heating of the electrons is equivalent to that of the ions.

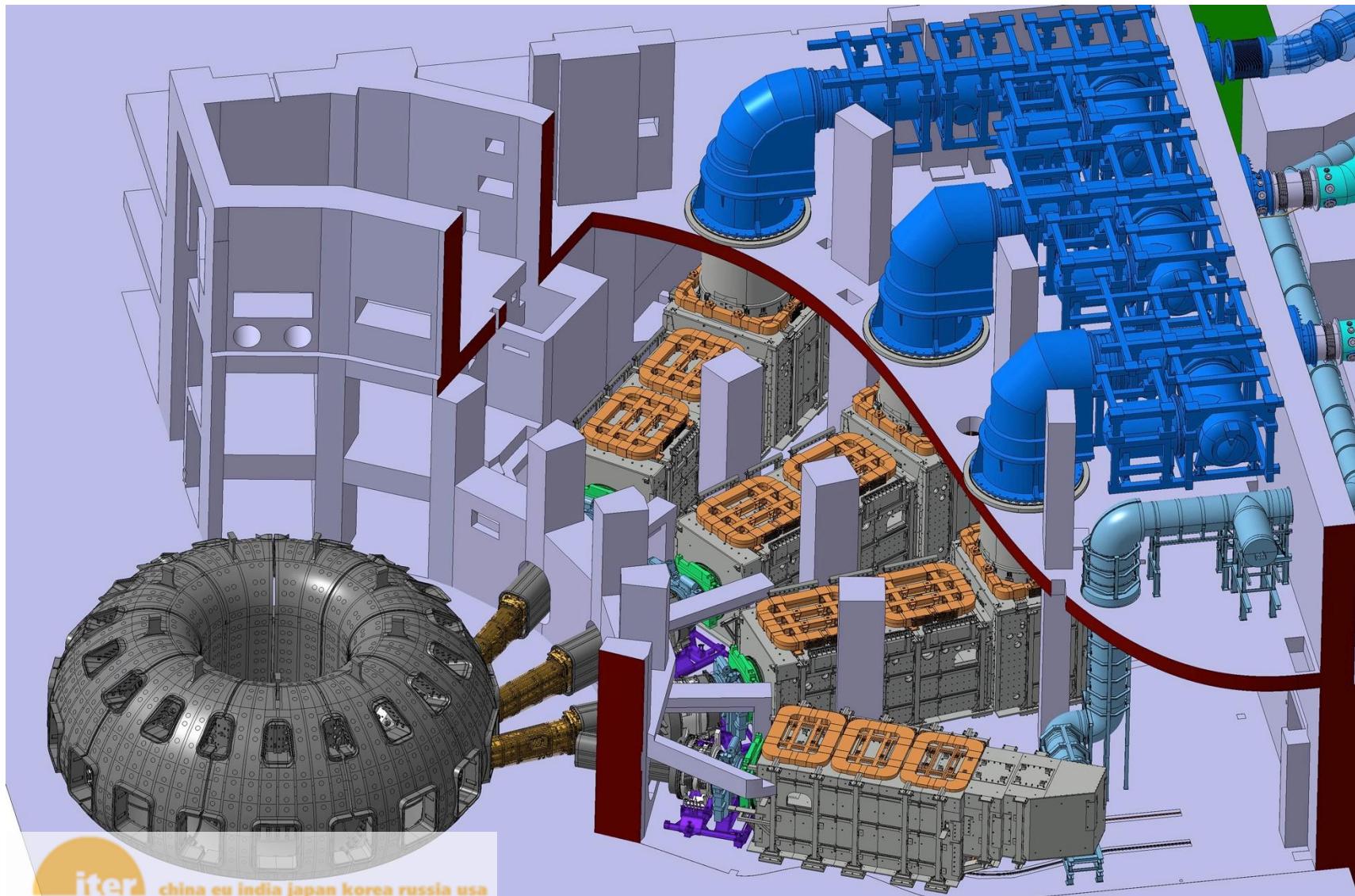
- When  $E_{\text{beam}} \gg E_{\text{crit}}$  : heating mainly of the **electrons** (often encountered in large devices)
- When  $E_{\text{beam}} \ll E_{\text{crit}}$  : heating mainly of the **ions** (current plasma devices)



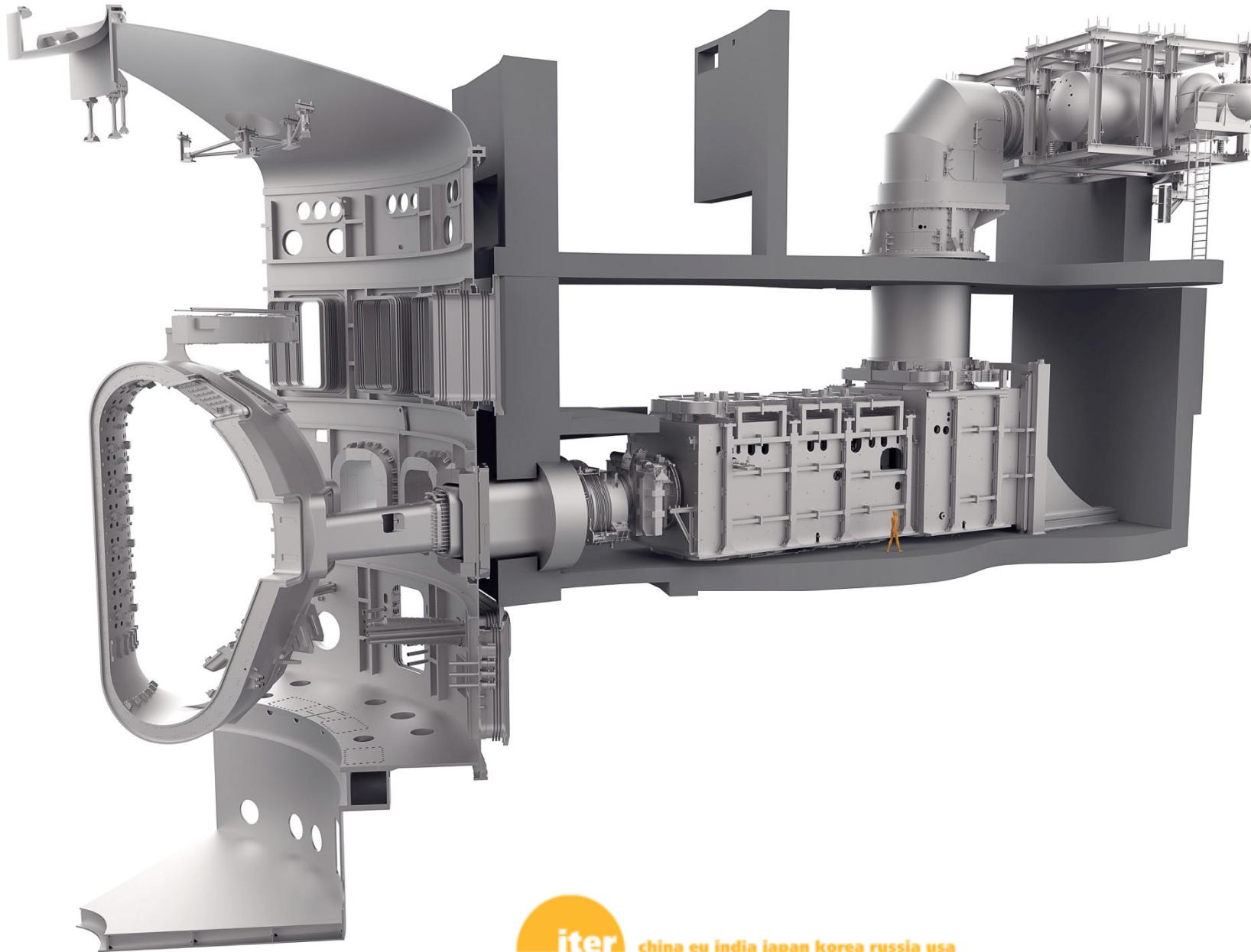
# EPFL ITER neutral beams for H&CD, diagnostic

Heating and current drive: 2 tangential D<sup>-</sup> (1MeV, 33MW,3600s)

Charge exchange diagnostic: 1 radial H<sup>-</sup> (100keV, 3MW, 400s)



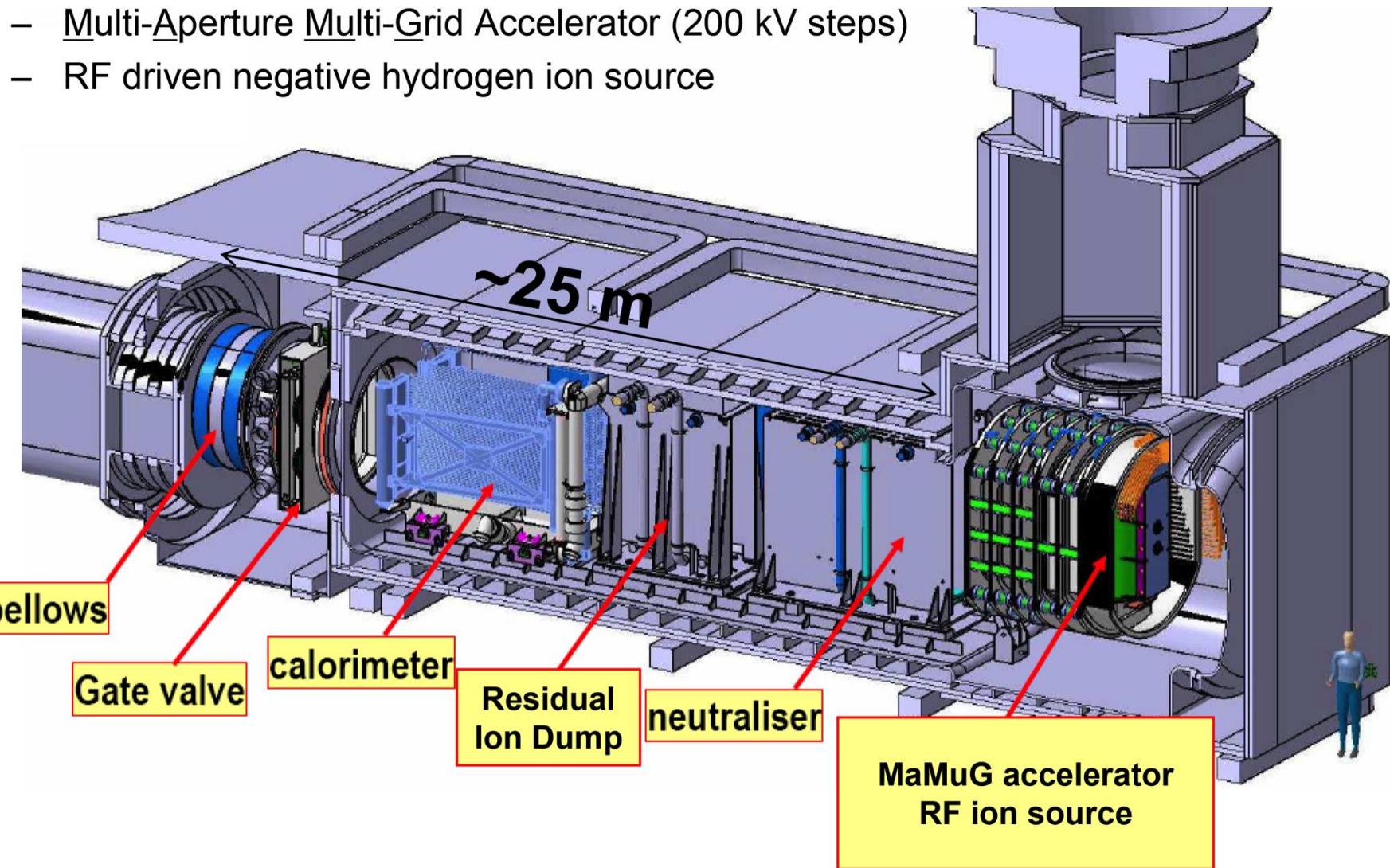
# EPFL ITER neutral beams for H&CD, diagnostic



china eu india japan korea russia usa

# EPFL ITER neutral beams for H&CD, diagnostic

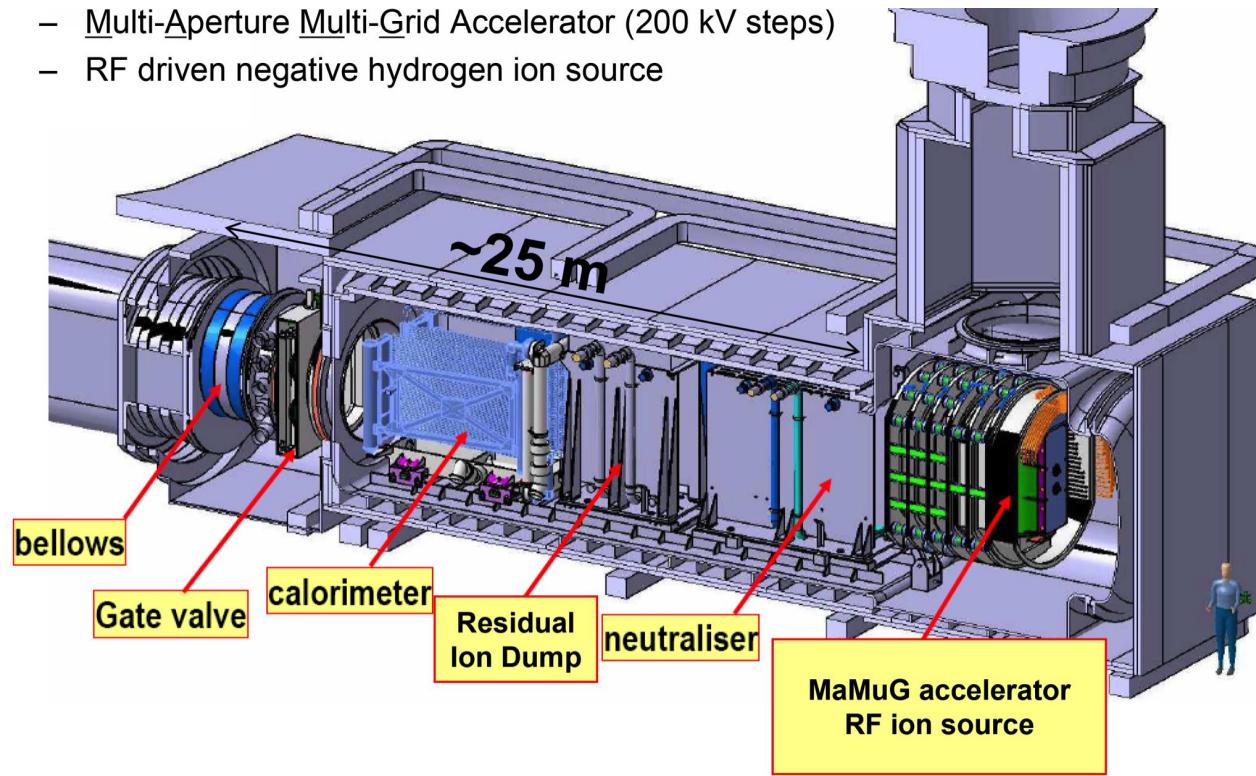
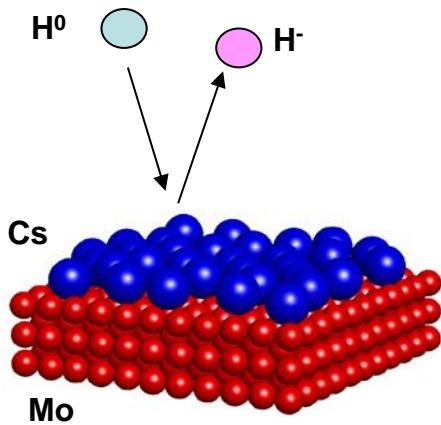
- Multi-Aperture Multi-Grid Accelerator (200 kV steps)
- RF driven negative hydrogen ion source



Large current density ( $\sim 300\text{A/m}^2$ ), high uniformity ( $\pm 10\%$ ) over  $\sim 2\text{m}^2$

# EPFL ITER neutral beams for H&CD, diagnostic

- Multi-Aperture Multi-Grid Accelerator (200 kV steps)
- RF driven negative hydrogen ion source



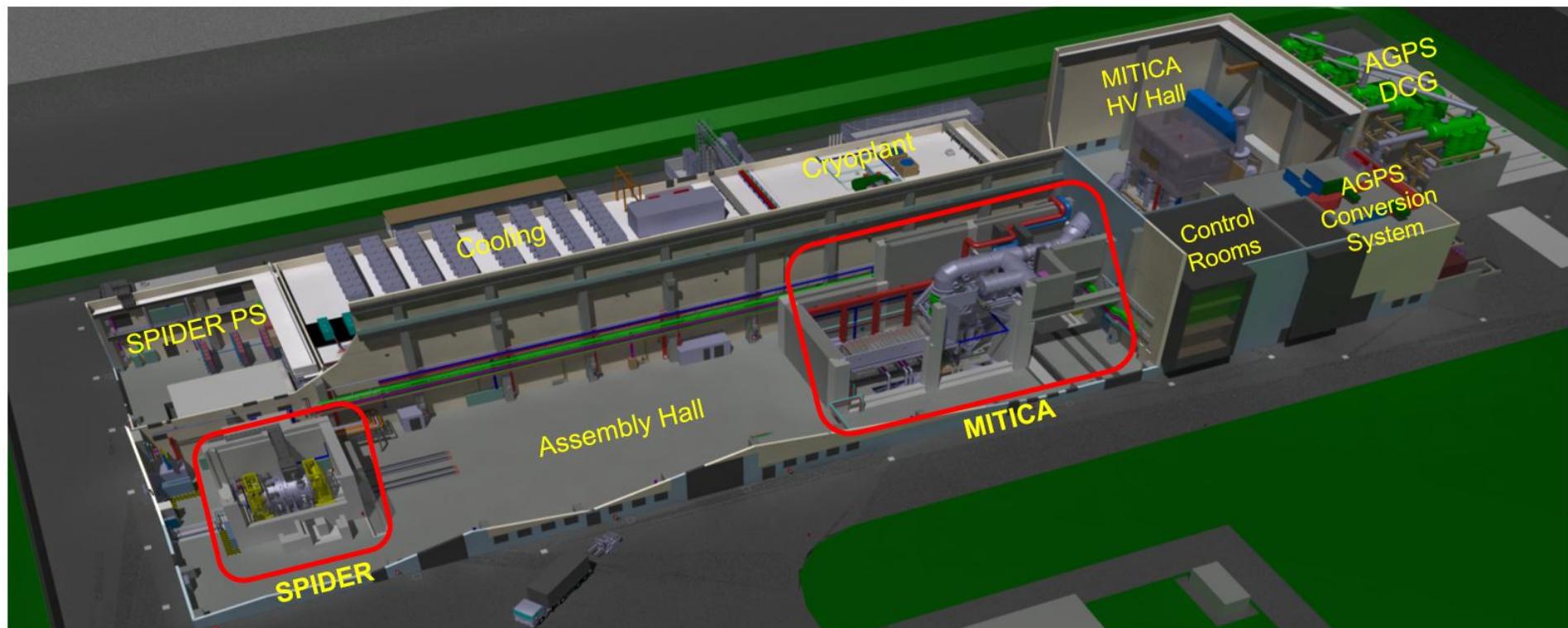
Negative ions are produced on Cs-adsorbed surfaces with low work function  
Atoms and ions interact with a surface, capturing electrons to form  $H^-$

# EPFL ITER neutral beams for H&CD, diagnostic

The Neutral Beam Test Facility at Padua

**SPIDER** – full size ITER beam source

**MITICA** – prototype ITER beamline



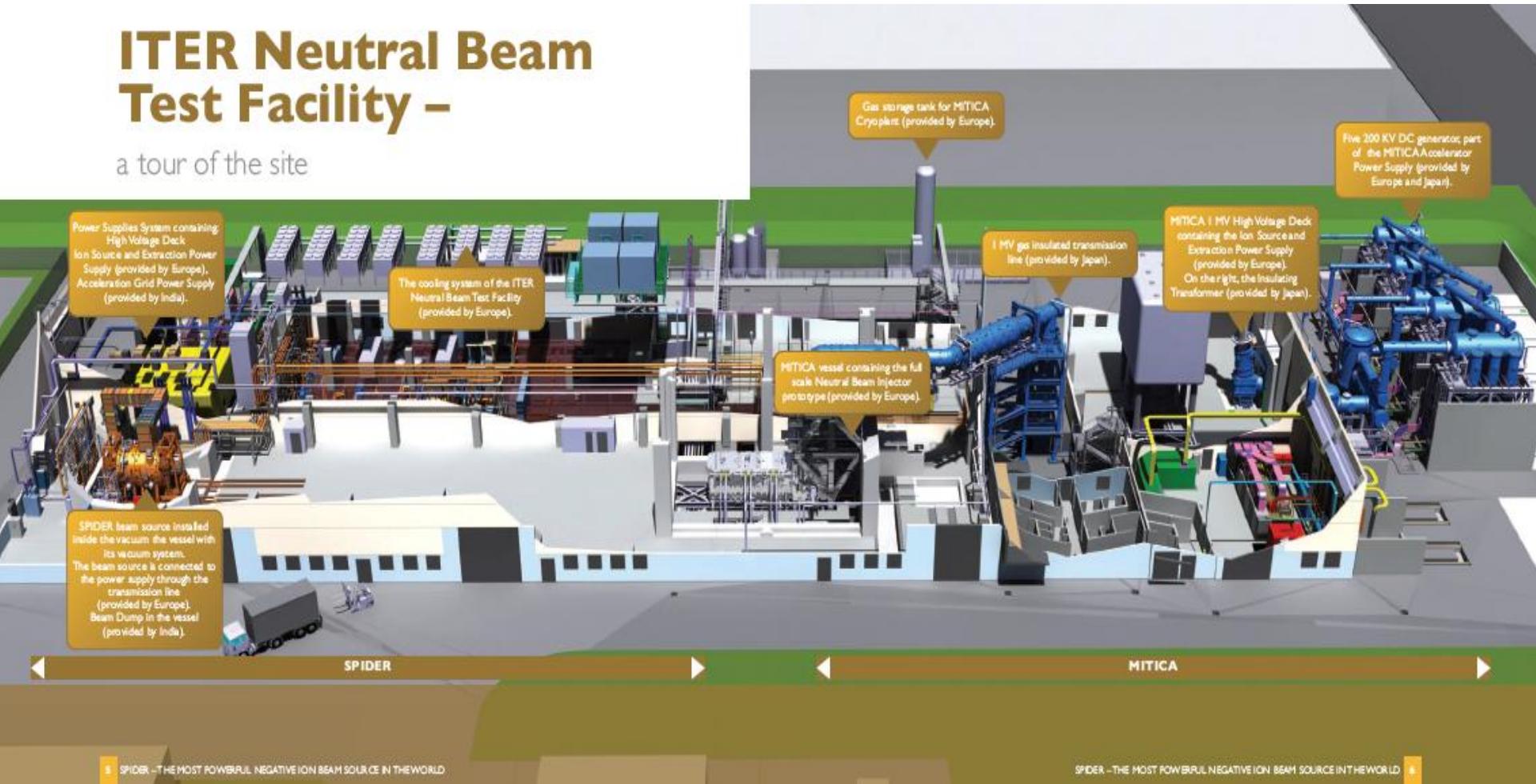
■ Swiss  
Plasma  
Center



# EPFL ITER neutral beams for H&CD, diagnostic

## ITER Neutral Beam Test Facility –

a tour of the site

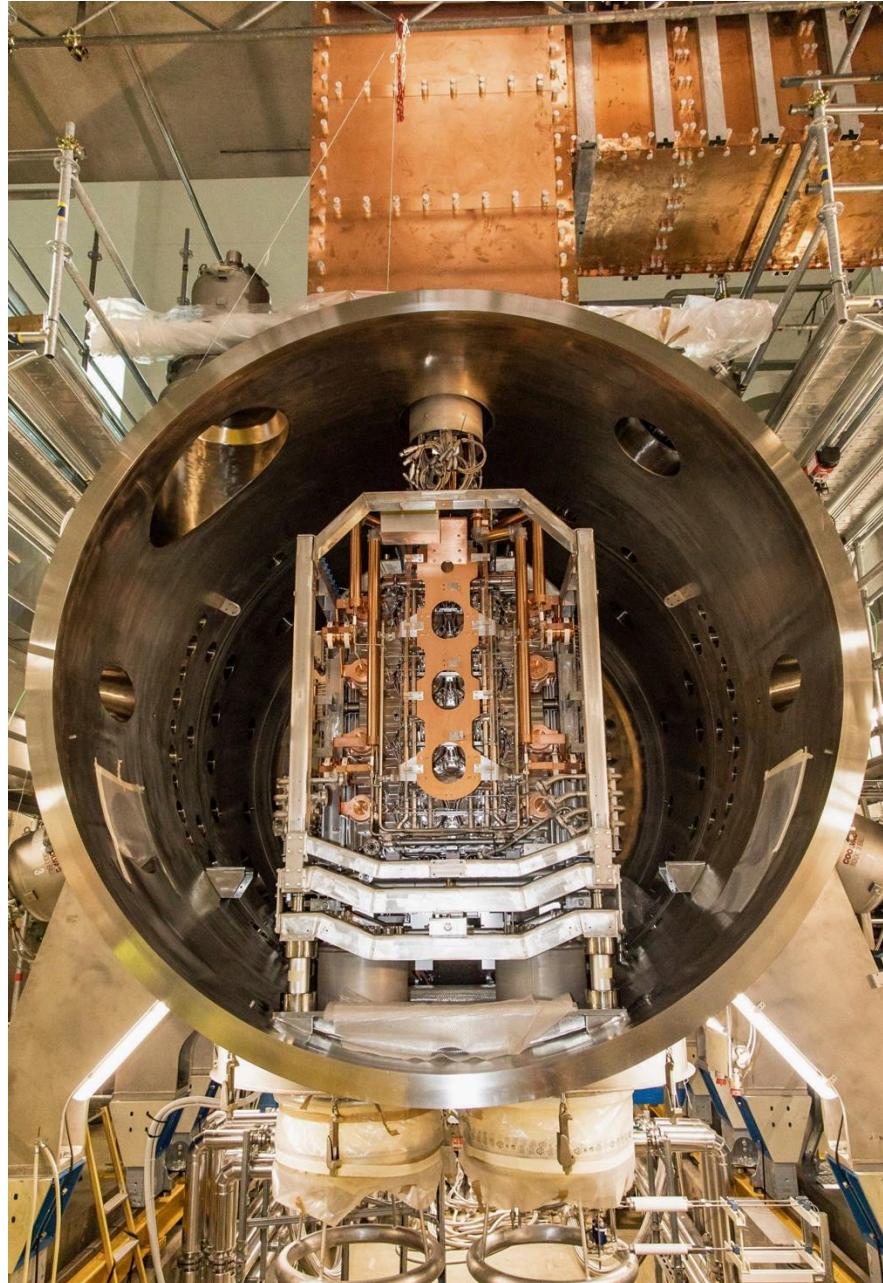
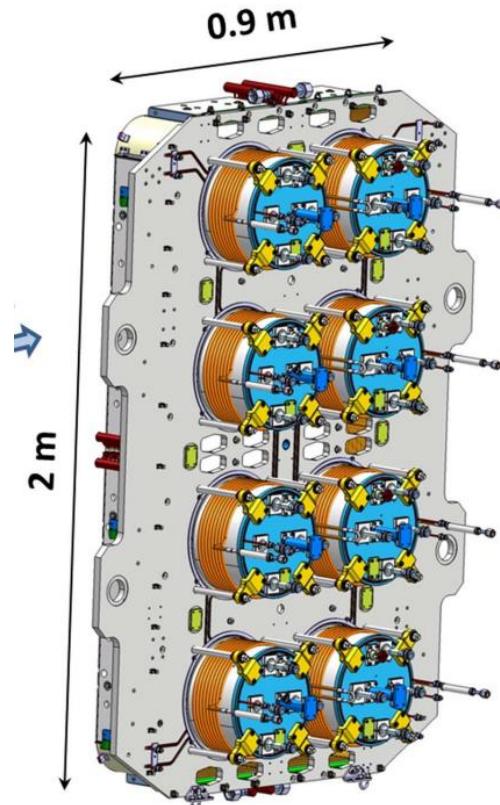


■ Swiss  
Plasma  
Center



# EPFL ITER neutral beams for H&CD, diagnostic

## SPIDER H- beam RF-source

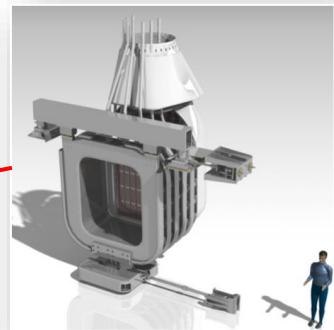
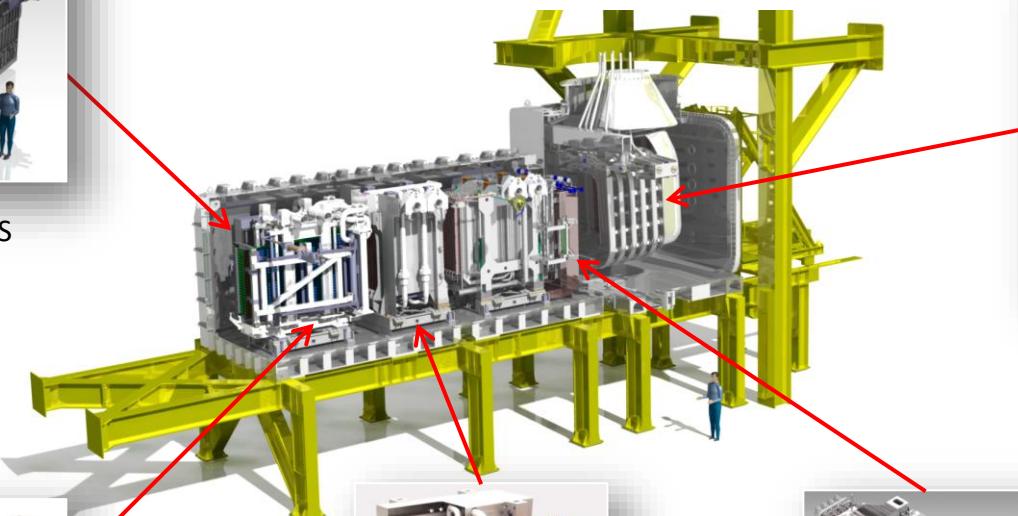


# EPFL ITER neutral beams for H&CD, diagnostic

## MITICA



CRYOGENIC PUMPS



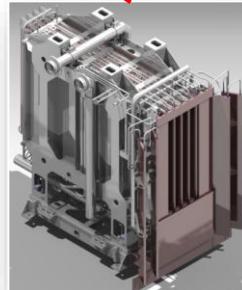
BEAM SOURCE



CALORIMETER



RESIDUAL ION DUMP



NEUTRALIZER

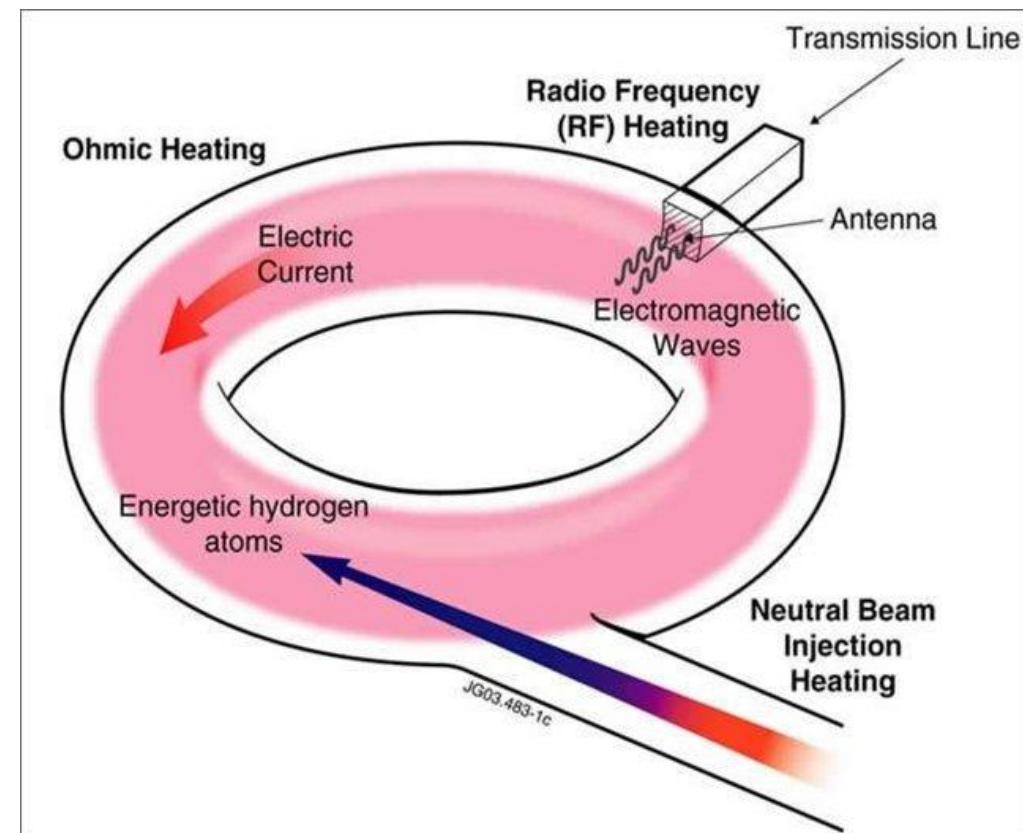
Burning plasma regime is reached using external heating and current drive

*Electron cyclotron heating*

*Ion cyclotron heating*

*Neutral beam heating*

Based on creation of  $\sim$ MeV ions, then thermalised by collisions

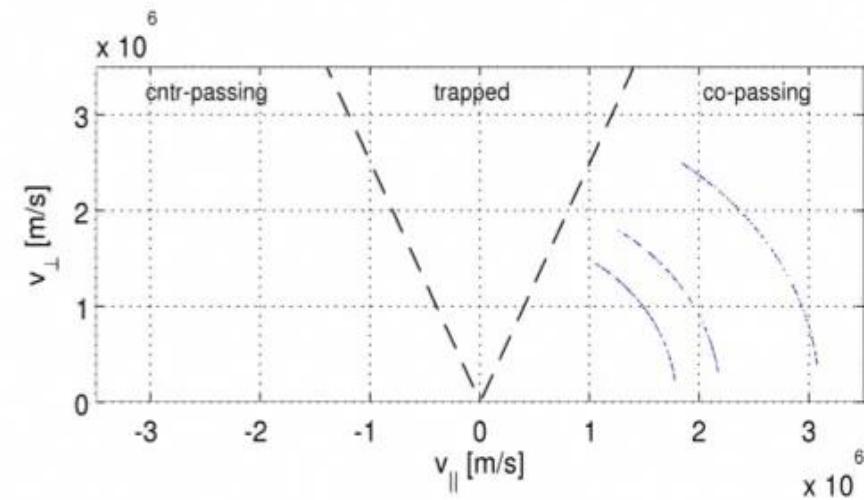
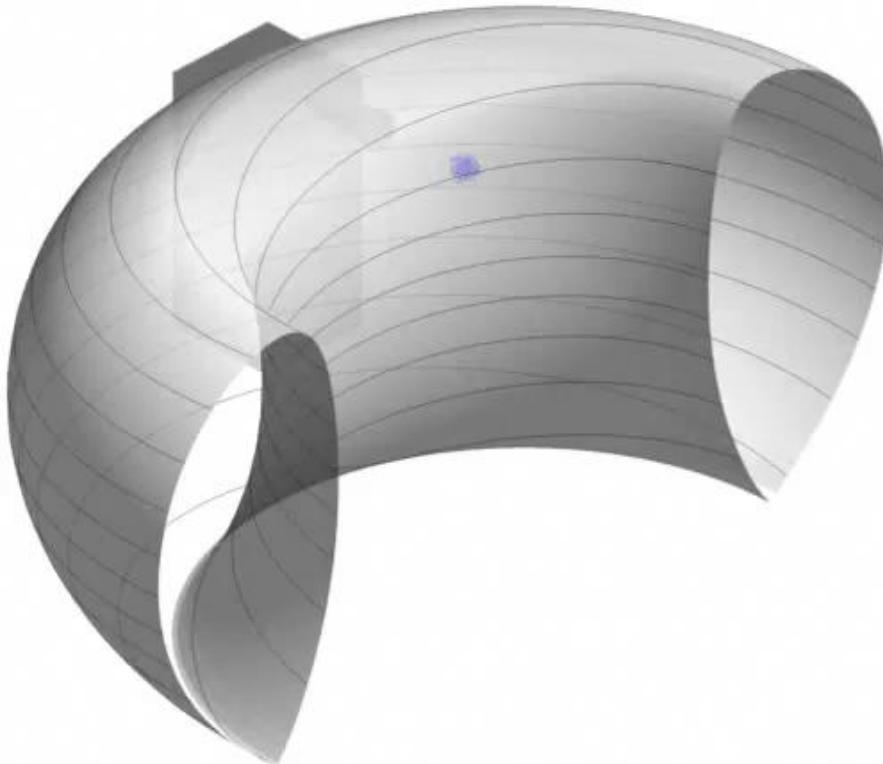


# EPFL Energetic ions from Neutral Beam Injection

Ions at  $\sim 100\text{keV}$  in present devices,  $\sim 1\text{MeV}$  in ITER

Injection geometry determines initial orbits

If tangential, mostly passing orbits, collisions scatter into trapped



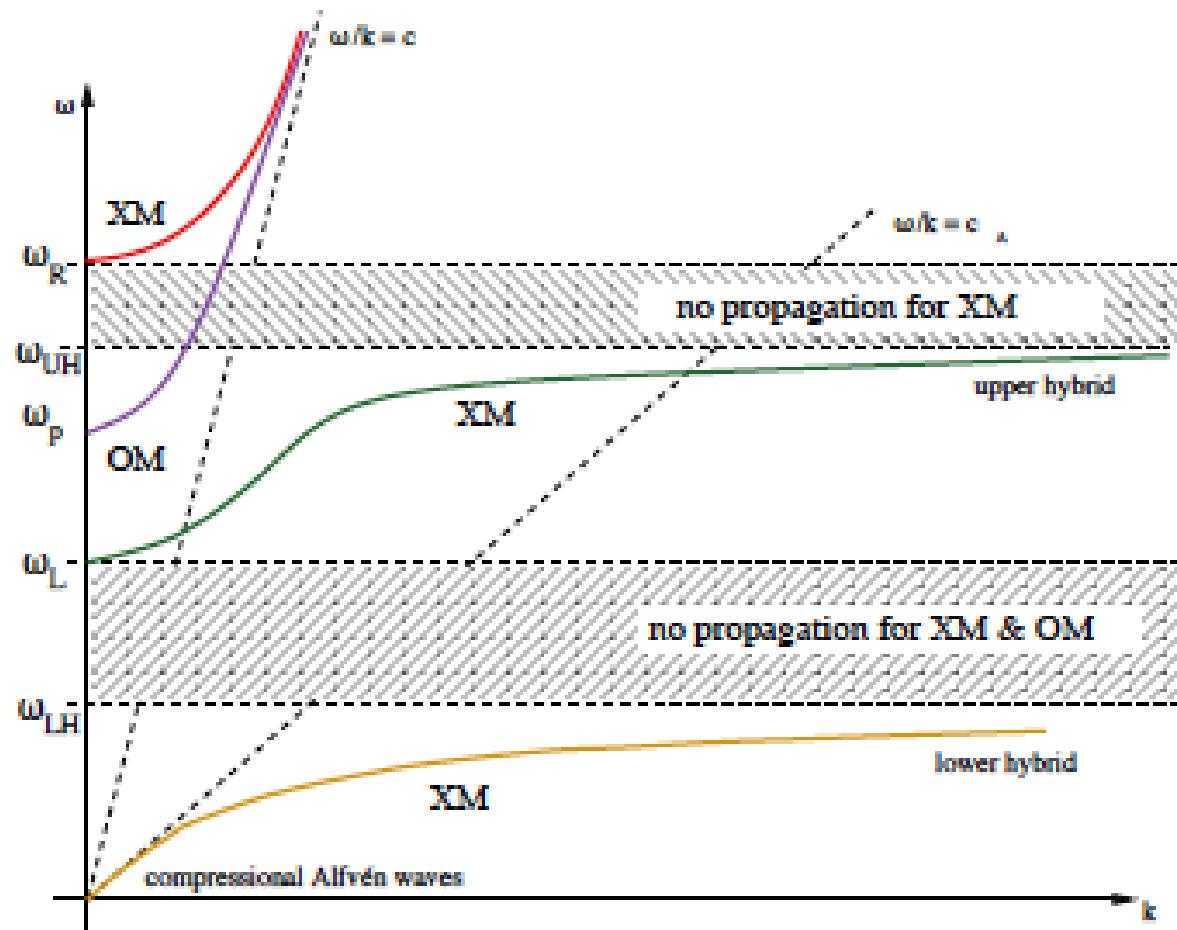
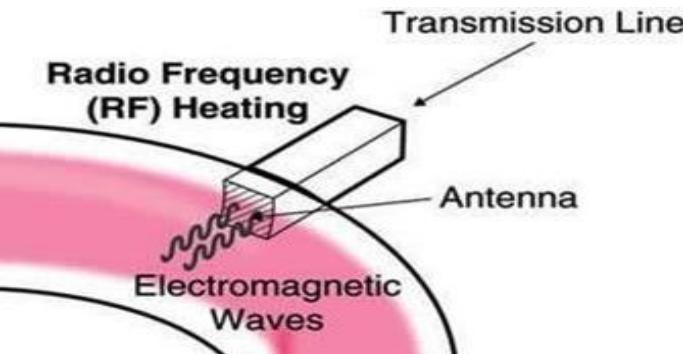
Mattia Albergante

# Heating by waves

# Heating by waves

Reminder of waves dispersion relation ( $T \sim 0$ )

Perpendicular to  $\mathbf{B}_0$



# Heating by waves

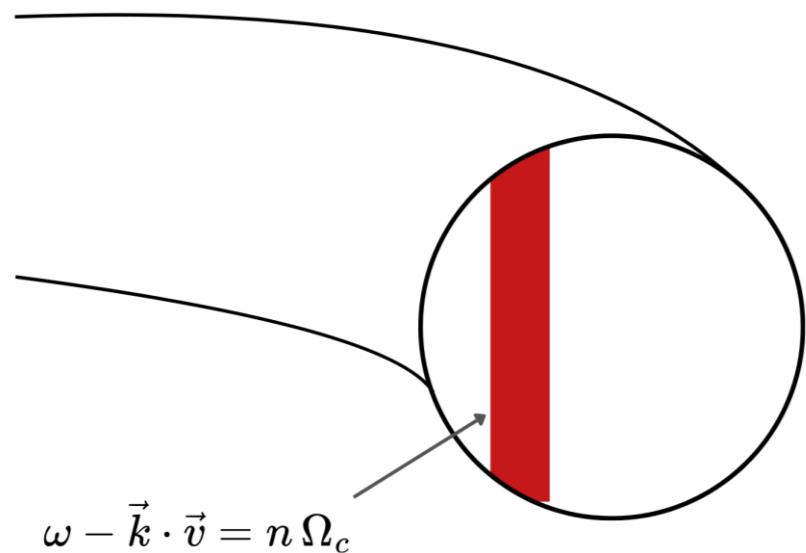
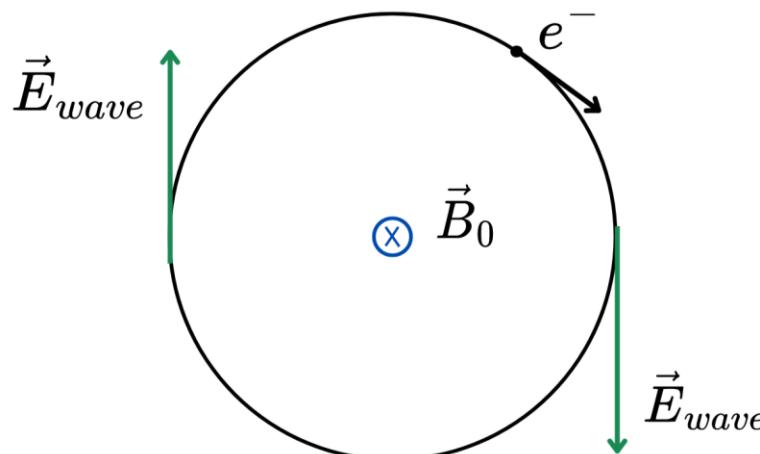
If  $T \gg 0$  (hot plasma - kinetic model needed)

Wave-particle resonances occur at  $\omega - \vec{k} \cdot \vec{v} = n\Omega_c$  ( $n = 0, 1, 2, \dots$ )

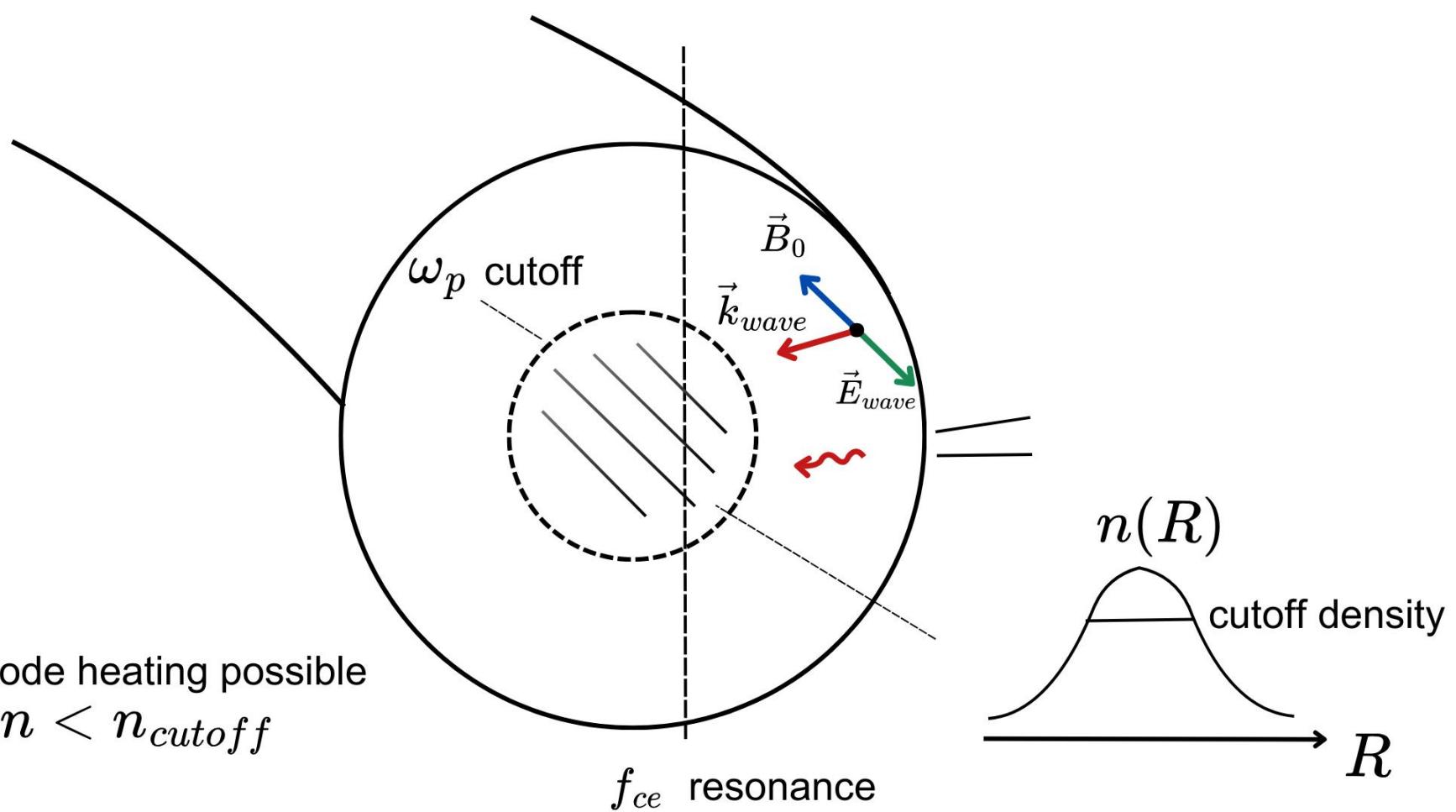
Ions or electrons feel in their reference frame a constant force when the E-field is in phase with their motion

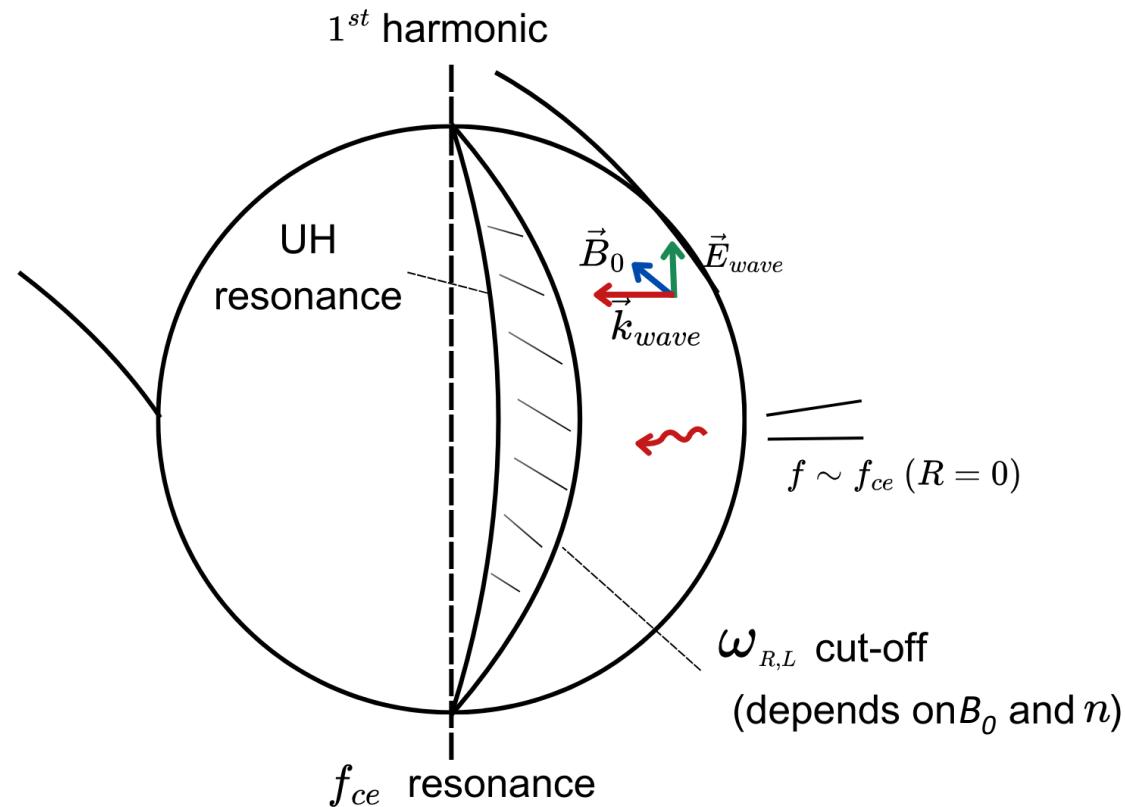
Cyclotron resonances also for waves that do not propagate along  $\vec{B}_0$

Finite  $k_{\parallel}$  and relativistic effects, for electrons,  $\Omega_{ce} = eB_0/m(v)$ , make the resonance velocity dependent, i.e. of finite width, effective for the energy exchange between particles and waves

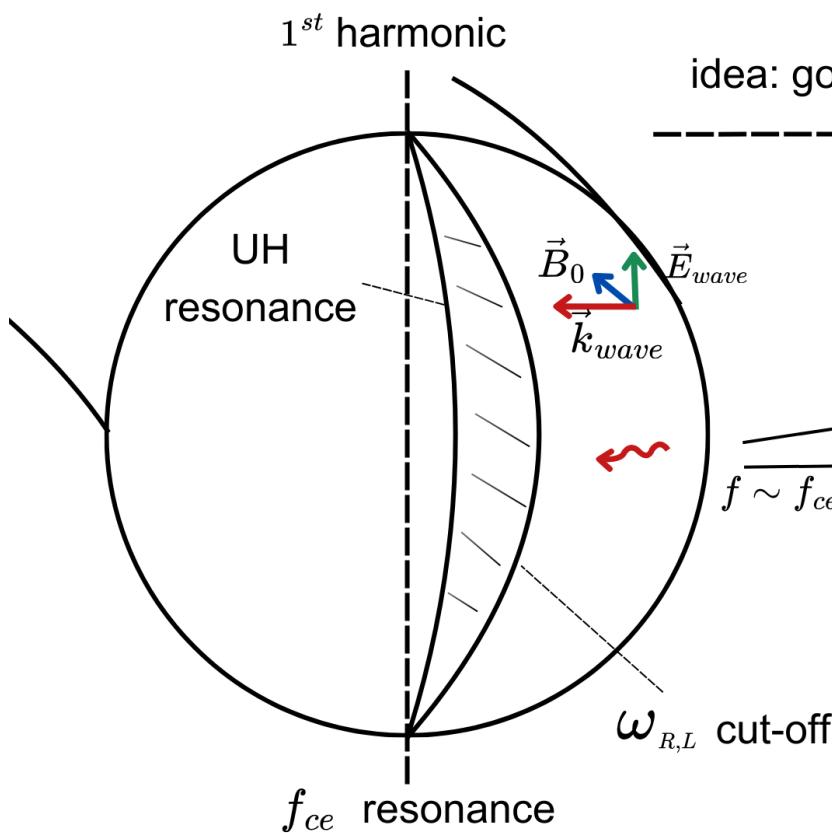


# Electron Cyclotron Resonance Heating ECRH



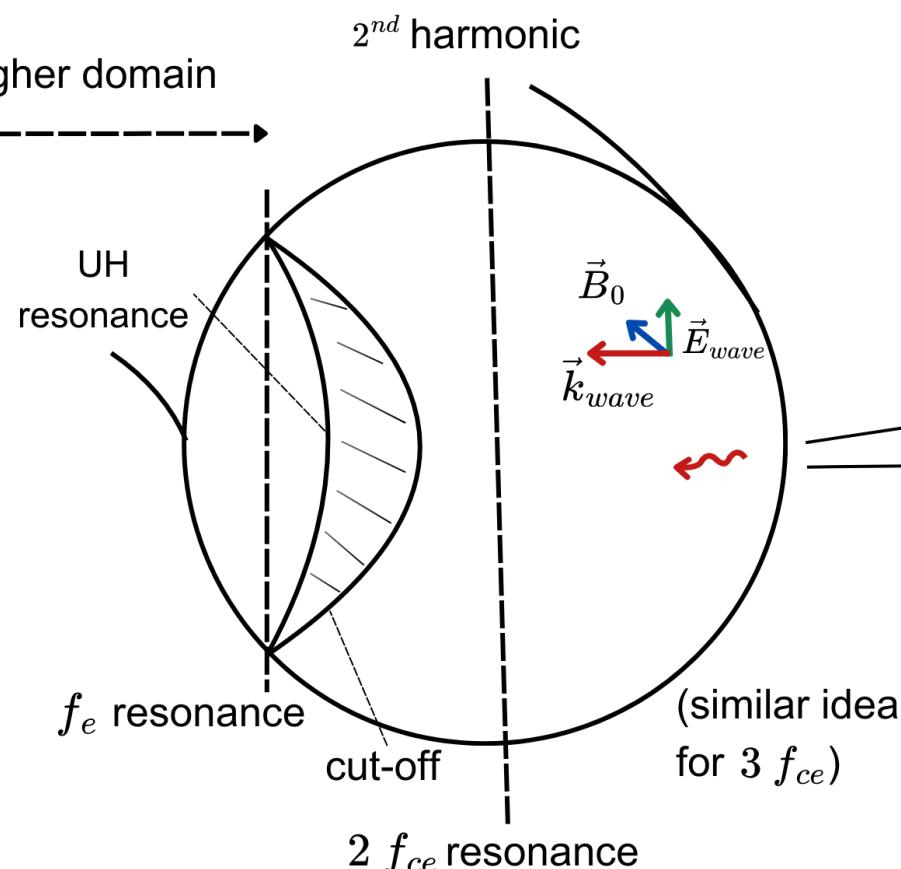


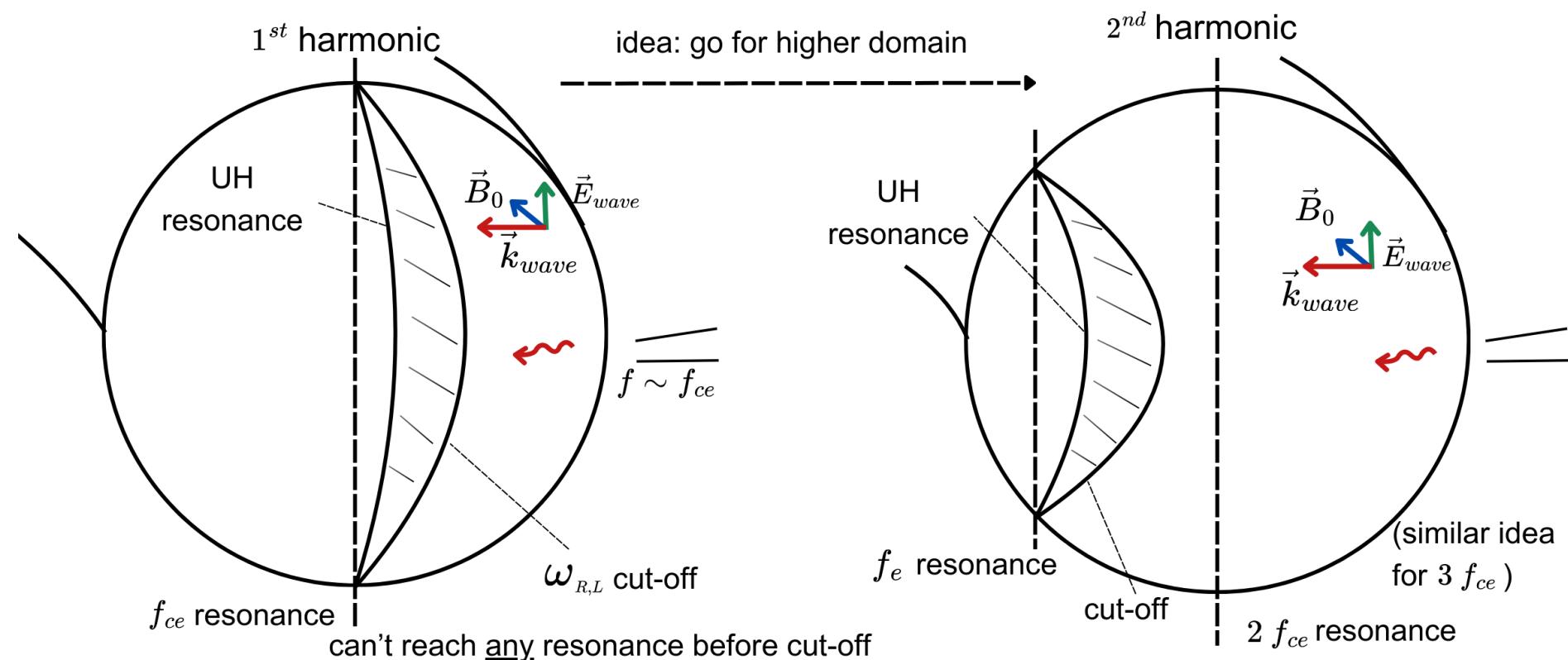
can't reach any resonance before cut-off



can't reach any resonance before cut-off

idea: go for higher domain





**Note:** Pb with going to higher frequency and higher harmonics

reduced absorption

availability of high power sources

## ECRH – Accessibility

$$X = \frac{\omega_p^2}{\omega^2} (\propto n) \quad Y = \frac{\Omega_e^2}{\omega^2} (\propto B_0^2)$$

Cut-offs:

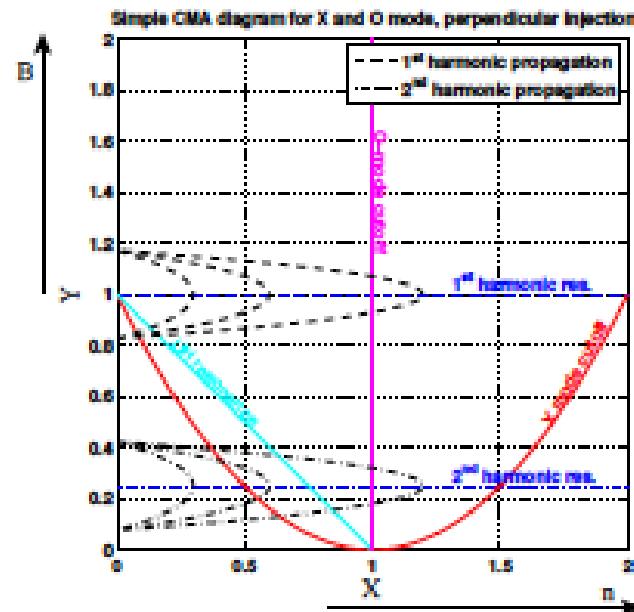
$$O - \text{mode: } X = 1$$

$$X - \text{mode: } Y = (1 - X)^2$$

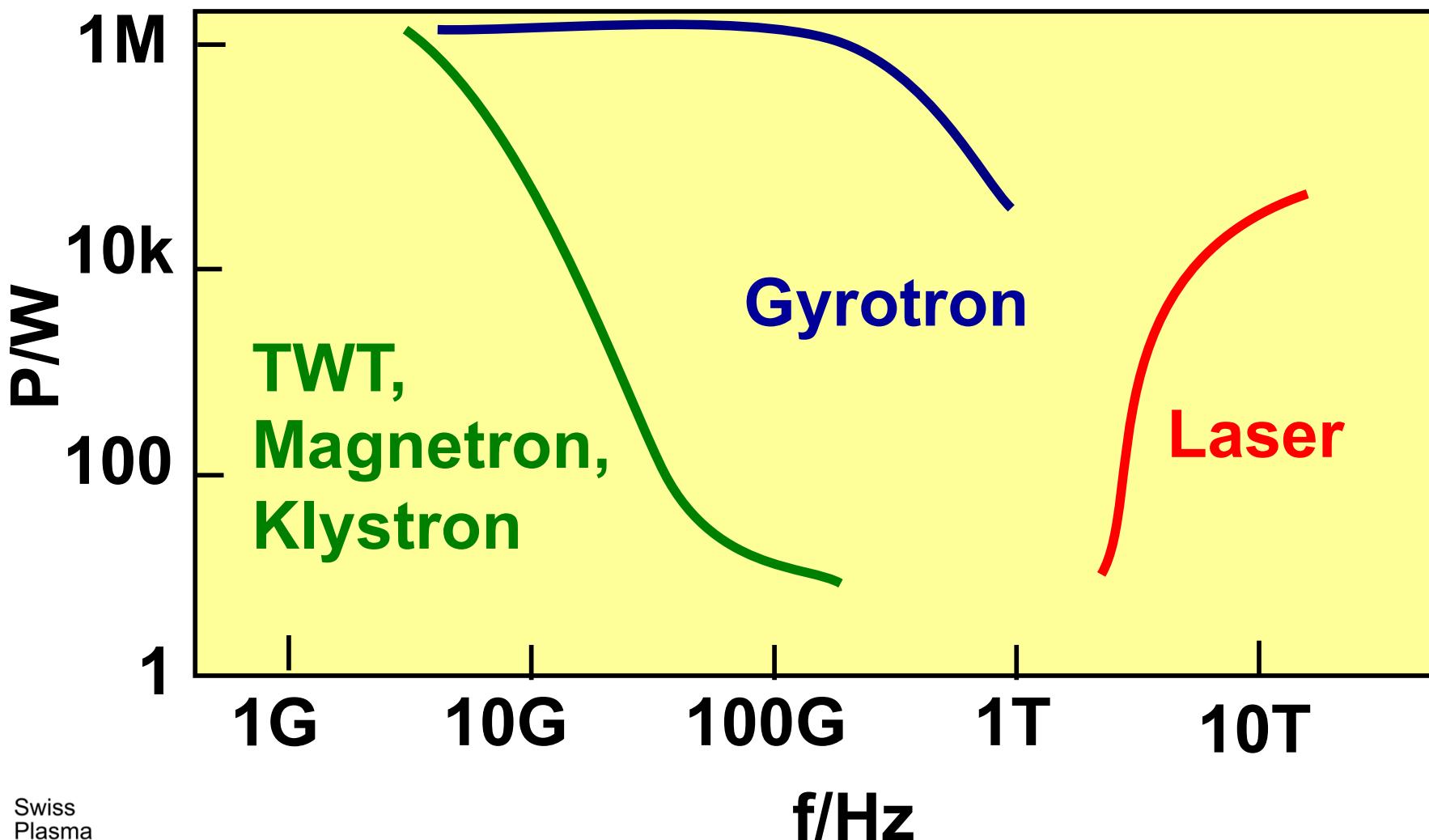
Resonances:

$$\omega = \omega_{UH} \quad Y = 1 - X$$

$$\omega = l\Omega_e \quad Y = \frac{1}{l^2}(1, 0.25, \dots)$$



**Figure 9.3:** Clemmow-Mullaly-Allis diagram for X and O mode. Wave trajectories are shown for 1<sup>st</sup> and 2<sup>nd</sup> harmonic injection and for different core plasma densities. Note that for low field side X1 injection the wave first encounters a cutoff. X2 may encounter a cutoff or resonance, depending on the density. O mode has a higher density limit but will eventually be cut off at the plasma frequency.



## ECRH – Accessibility

$$X = \frac{\omega_p^2}{\omega^2} (\propto n) \quad Y = \frac{\Omega_e^2}{\omega^2} (\propto B_0^2)$$

Cut-offs:

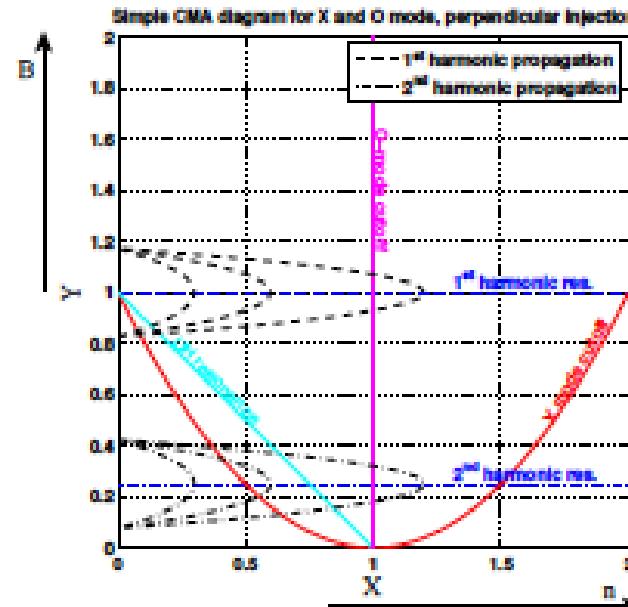
$$O\text{-mode: } X = 1$$

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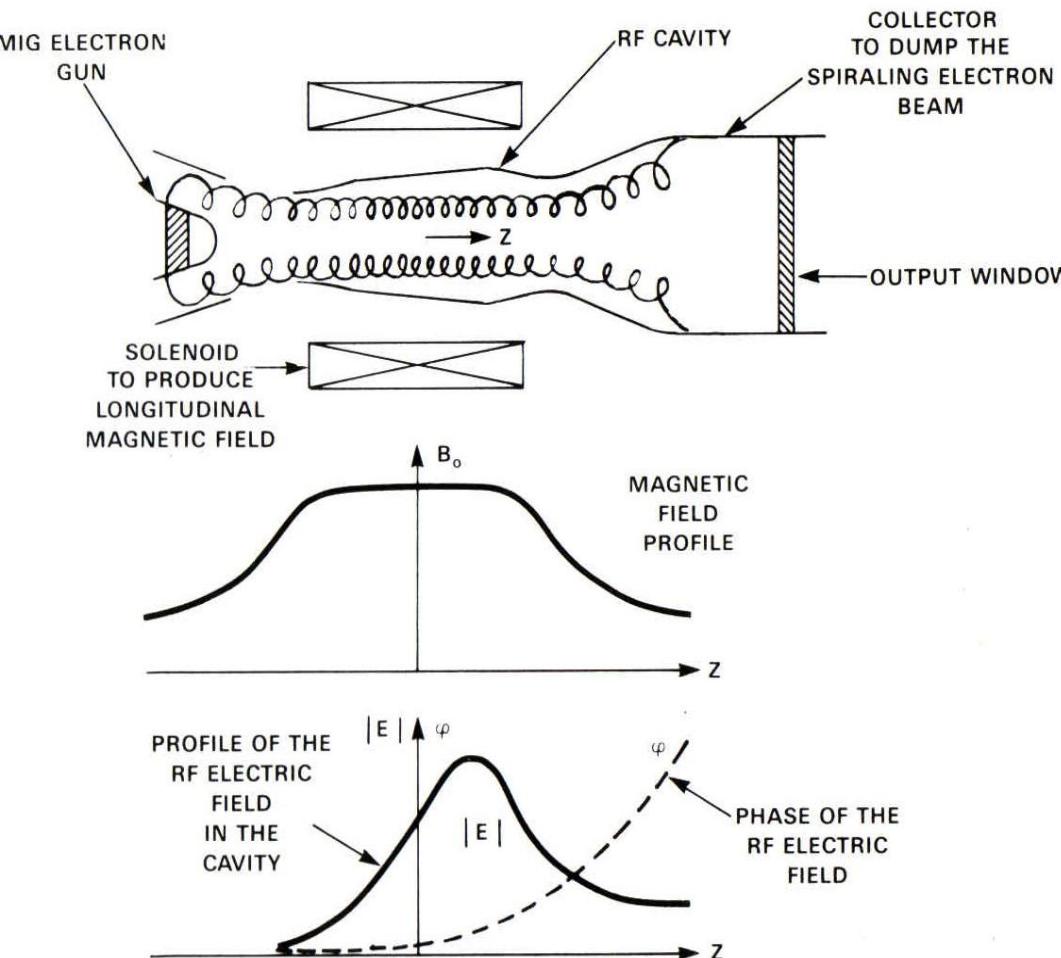


TCV ( $f_{ce}=41\text{GHz}$ )  
can use  $n=2$  or  $n=3$   
X2 (83GHz) or X3 (118GHz)

**ITER ( $f_{ce}=170\text{GHz}$ )**  
**must use  $n=1$**   
**O1 (170 GHz)**

Figure 9.3: Clemmow-Mullaly-Allis diagram for X and O mode. Wave trajectories are shown for 1<sup>st</sup> and 2<sup>nd</sup> harmonic injection and for different core plasma densities. Note that for low field side X1 injection the wave first encounters a cutoff. X2 may encounter a cutoff or resonance, depending on the density. O mode has a higher density limit but will eventually be cut off at the plasma frequency.

# Principle based on Cyclotron Resonance Maser instability



**Three “ingredients”:**

**Magnetic field**

Guides the  $e^-$

Determines the frequency

$$\omega \approx \frac{\Omega_0}{\gamma}$$

$\omega$	Oscillation frequency
$\Omega_0$	Cyclotron frequency
$\gamma$	Relativistic factor

**Annular electron beam**

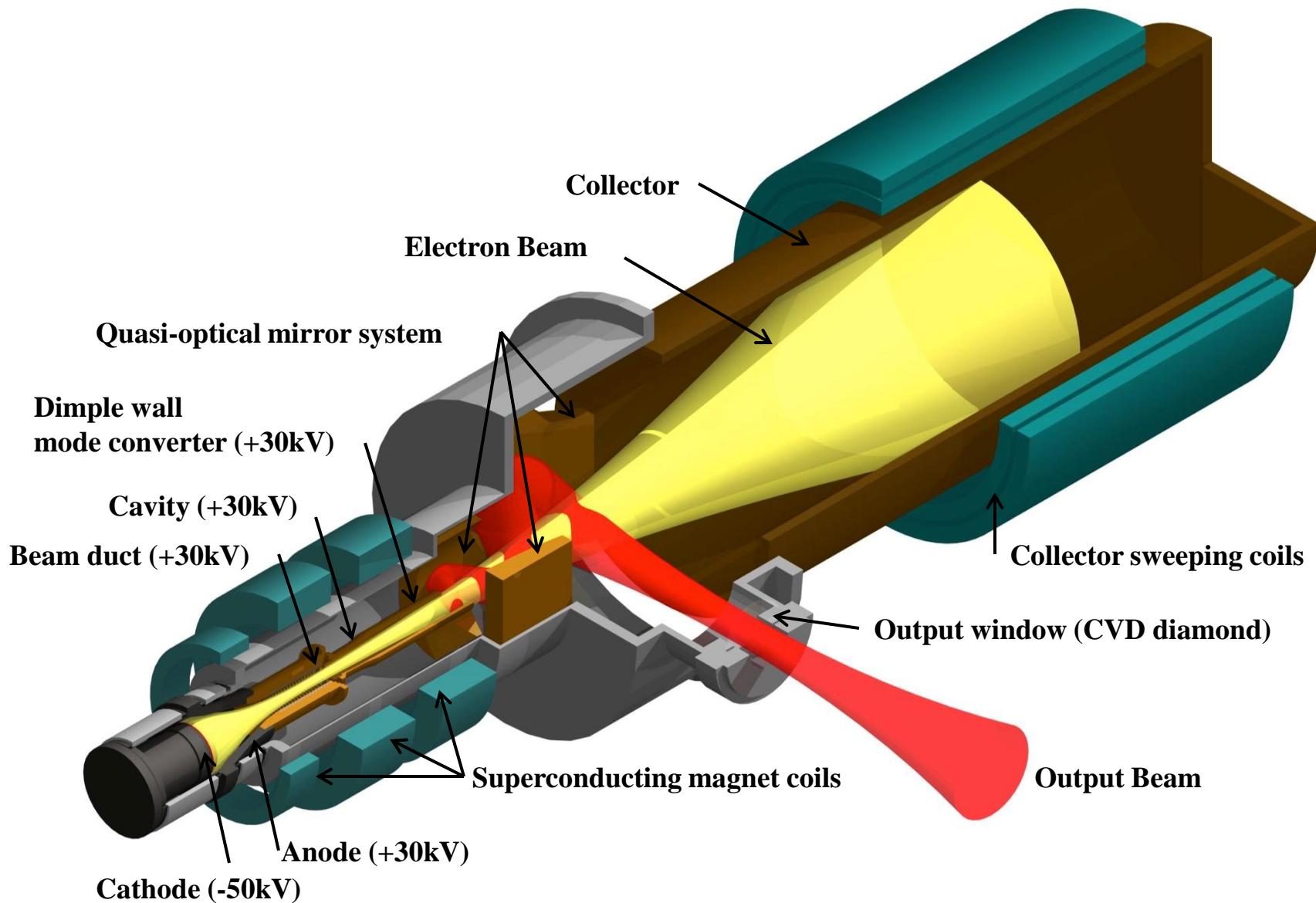
Source of free energy

**Resonant cavity**

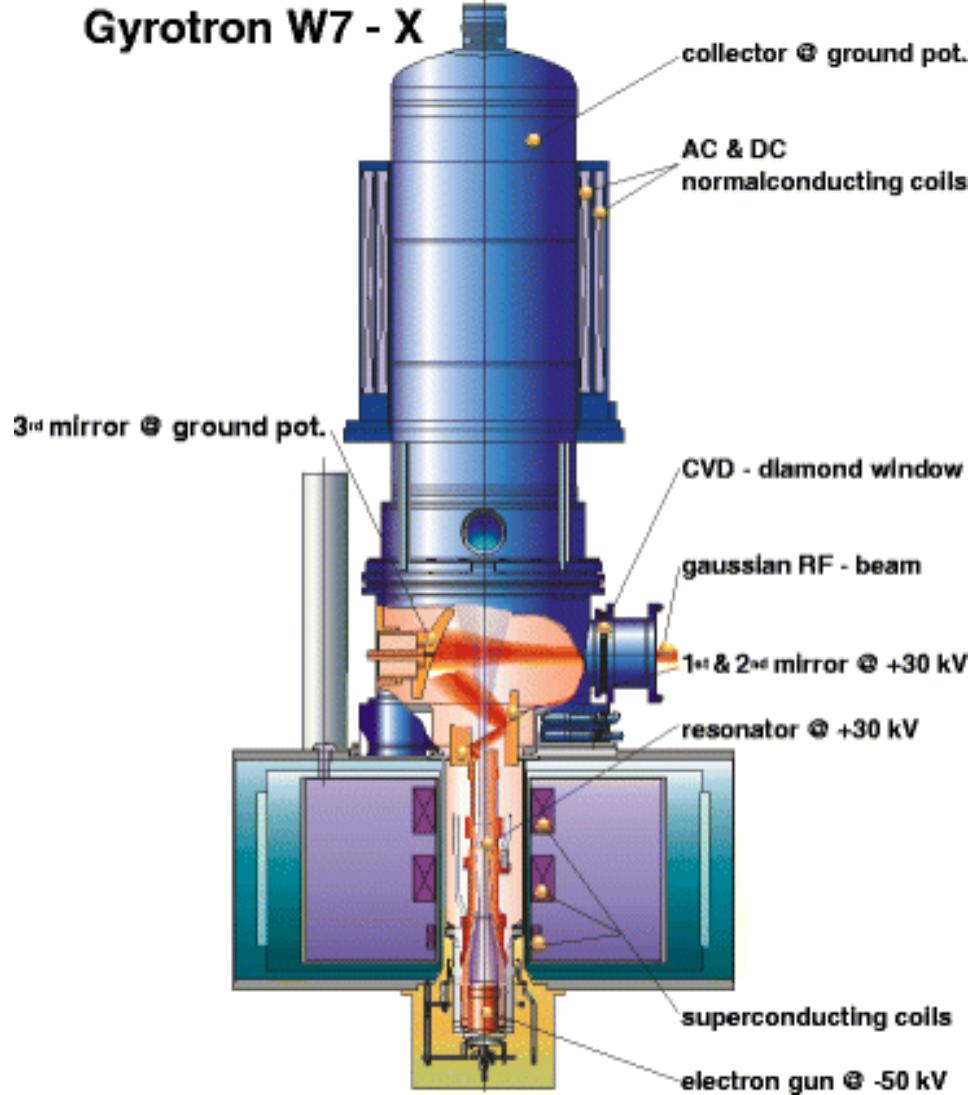
Cylinder with a smoothly varying cross-section

Resonant interaction between electrons and cavity mode ( $TE_{m,n}$ )

# The gyrotron

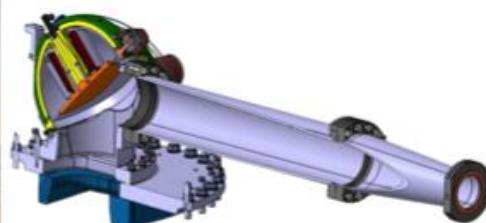


# The gyrotron

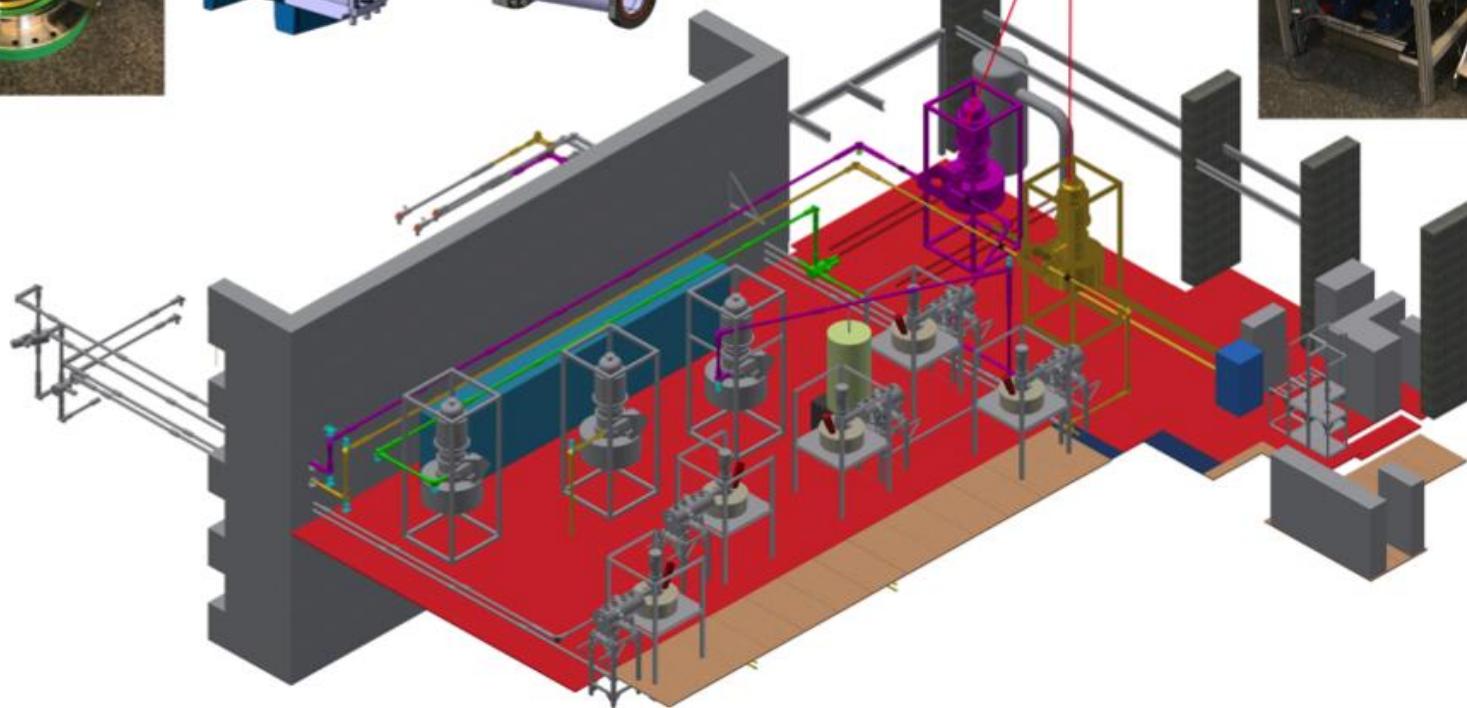
**Gyrotron W7 - X**

# A modern ECRH system: TCV

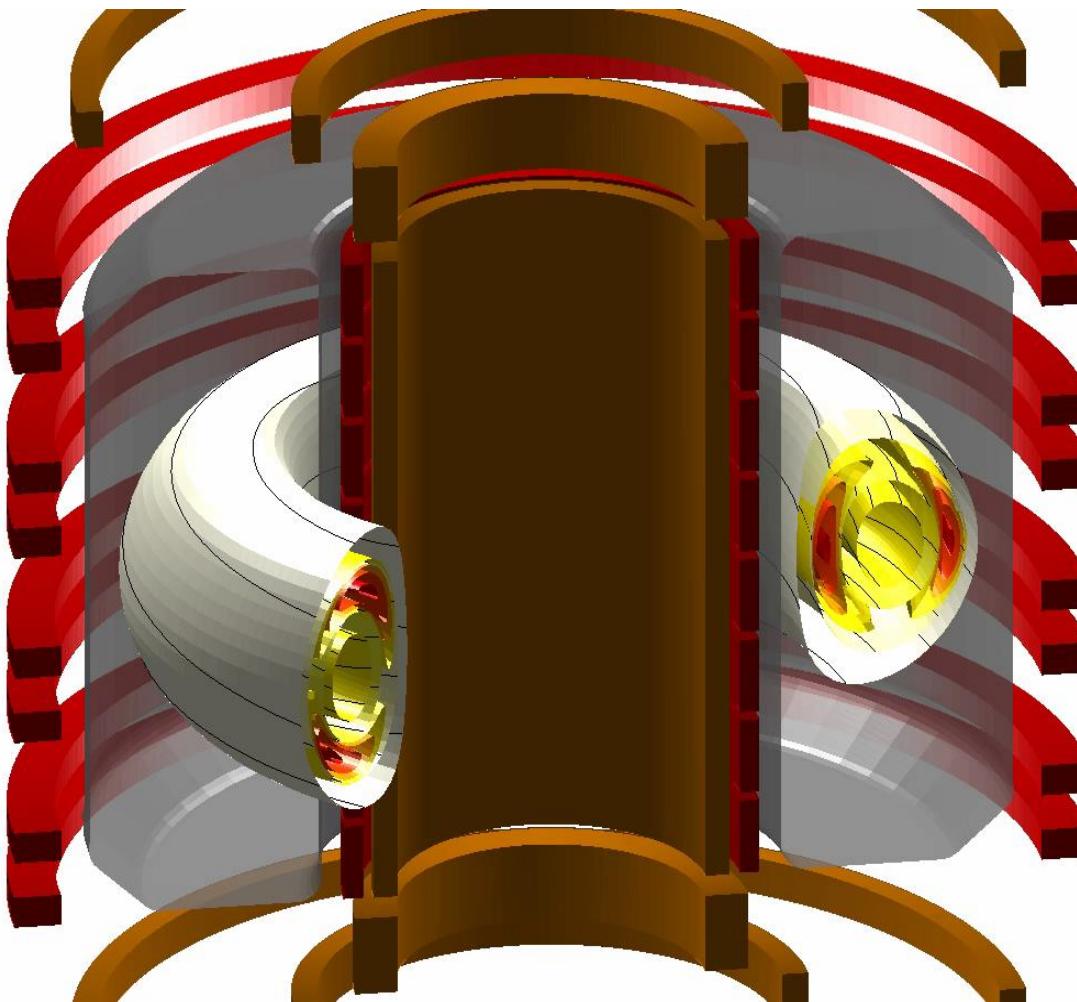
New X3 Top Launcher



Dual-frequency gyrotrons



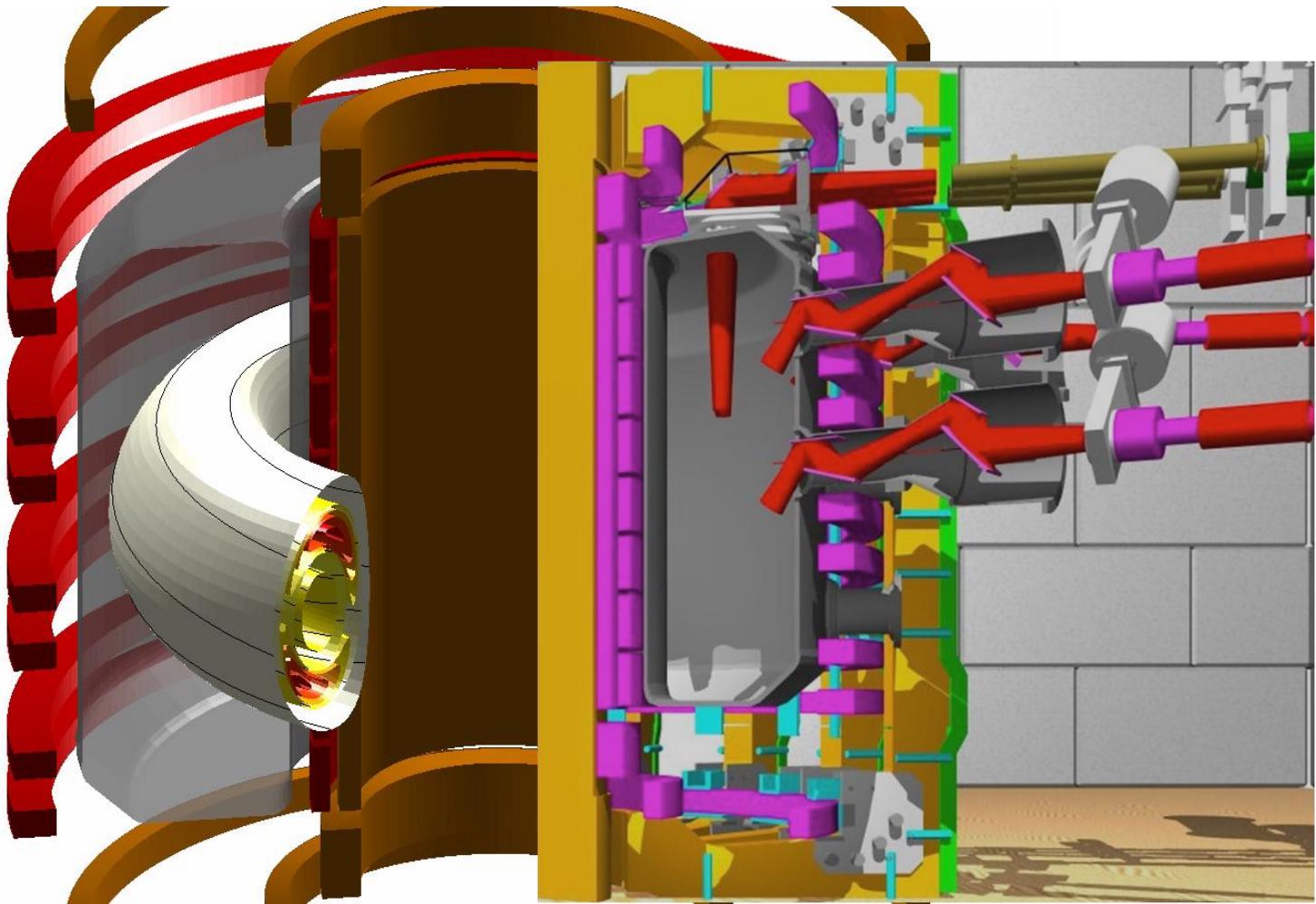
# ECRH for instability control



TCV

# ECRH for instability control

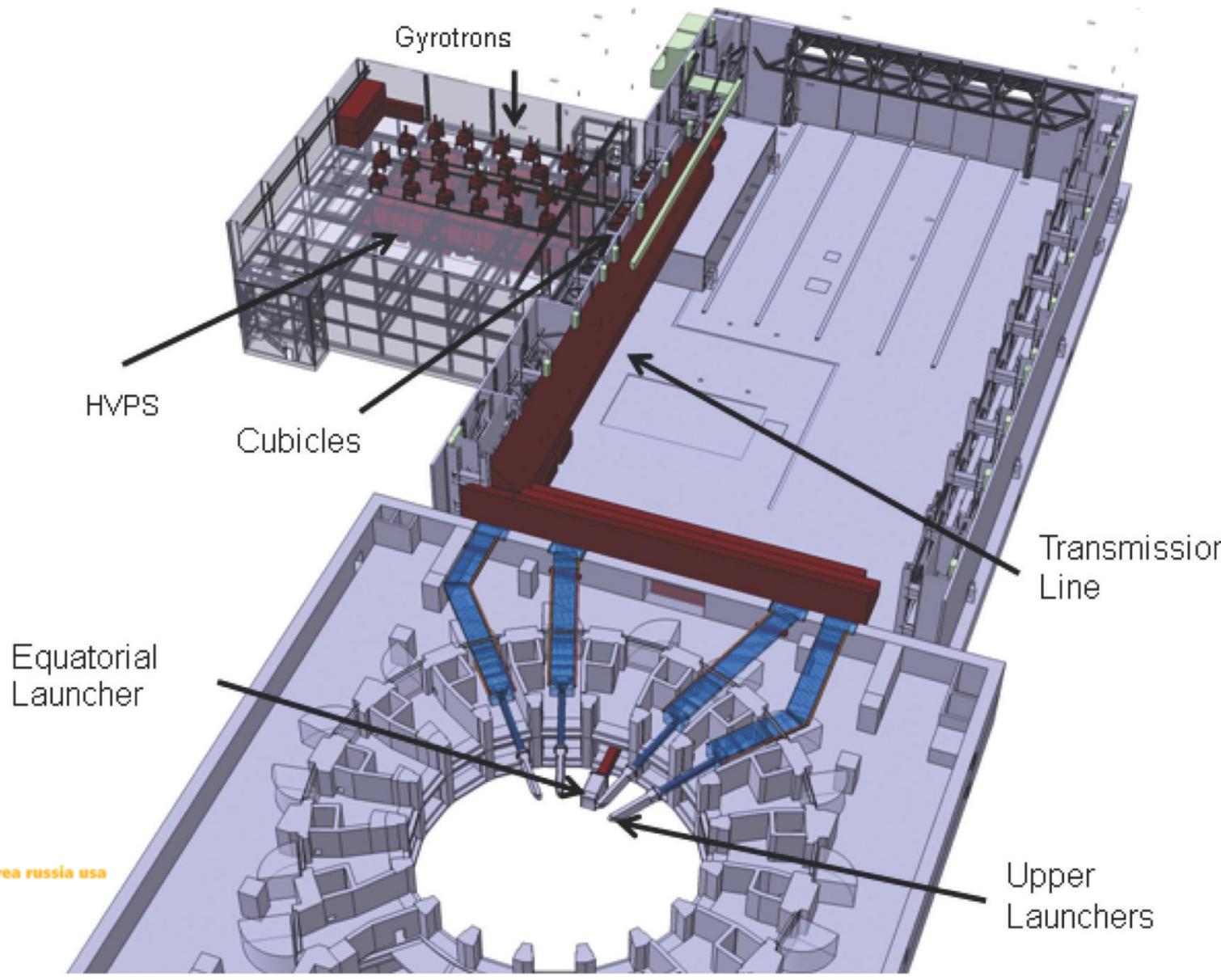
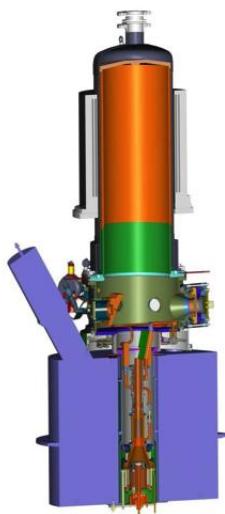
## *Proof of principle on TCV*



**TCV**

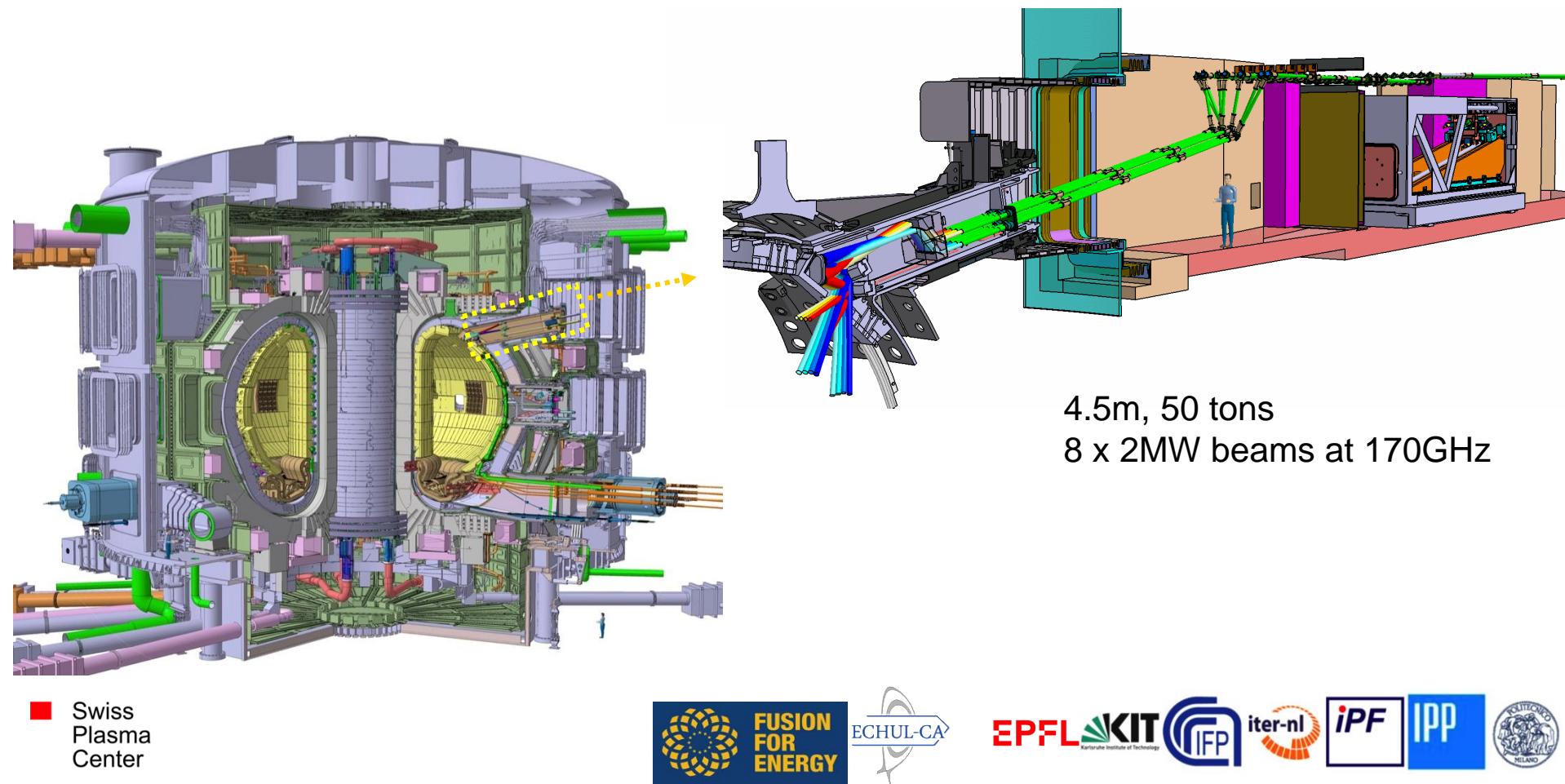
## ECRH system on ITER

80 gyrotrons  
1MW each  
170GHz



Front steering launcher of 170 GHz microwaves

Goal: heat locally and stabilize plasma instabilities



108 gyrotrons (216MW), 7200s

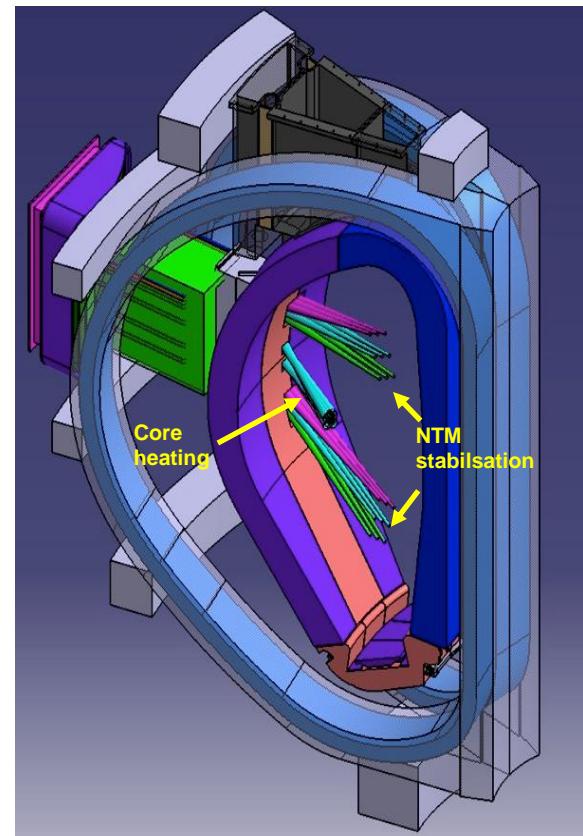
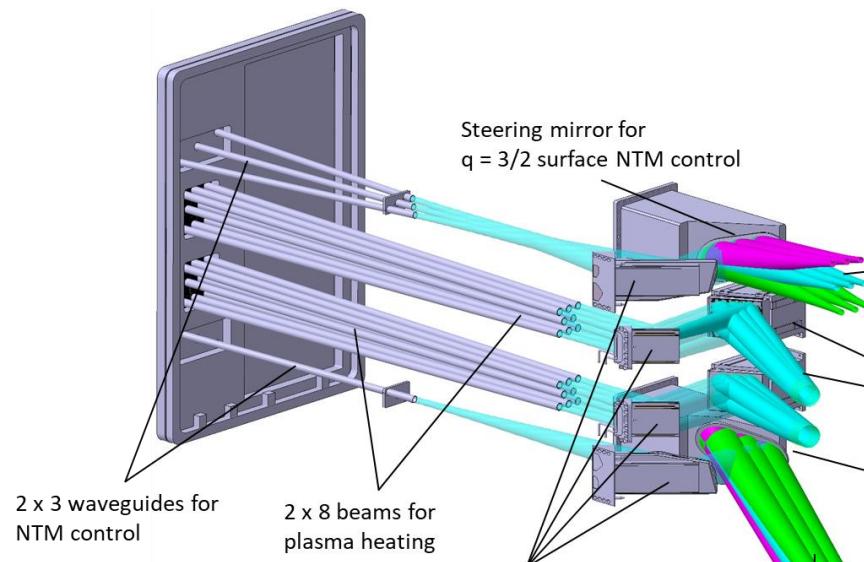
Break down and plasma ramp-up

Bulk heating and NTM control (core)

Radiative instability control (edge)

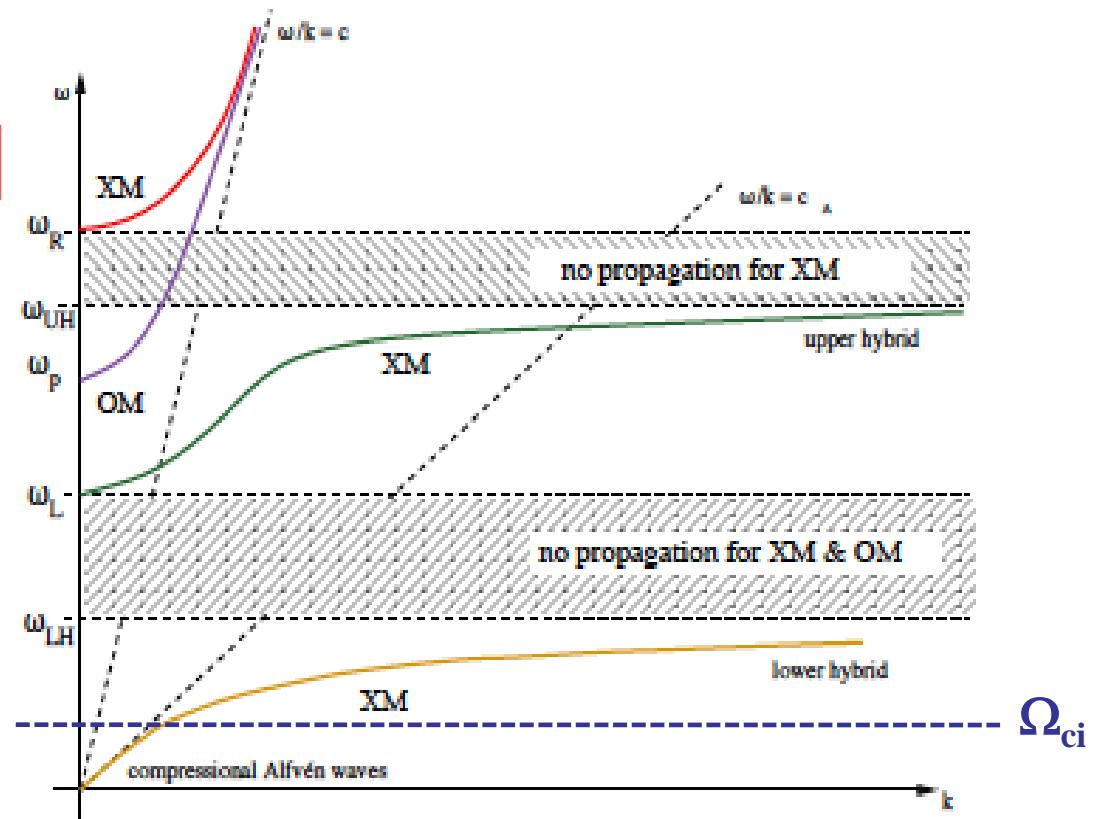
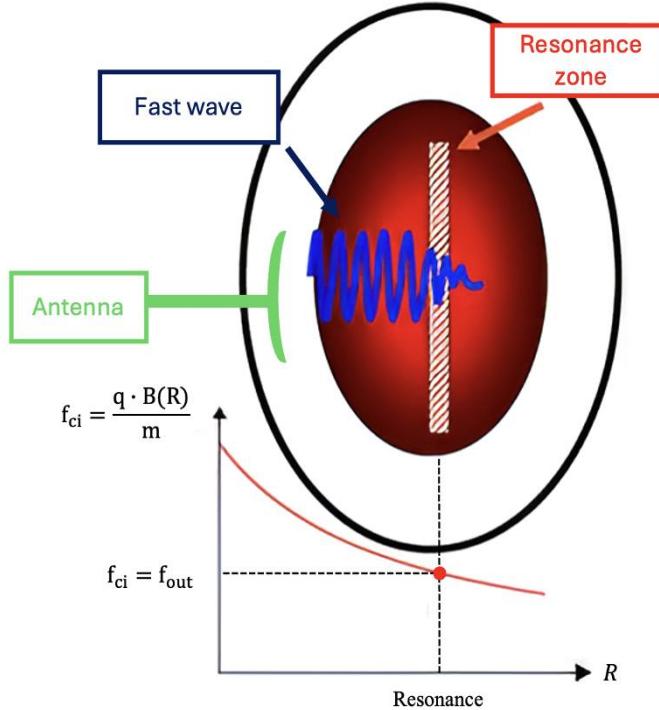
Plasma ramp-down

SPC contribution - launcher



# Ion Cyclotron Resonance Heating ICRH

# Perpendicular wave dispersion relation

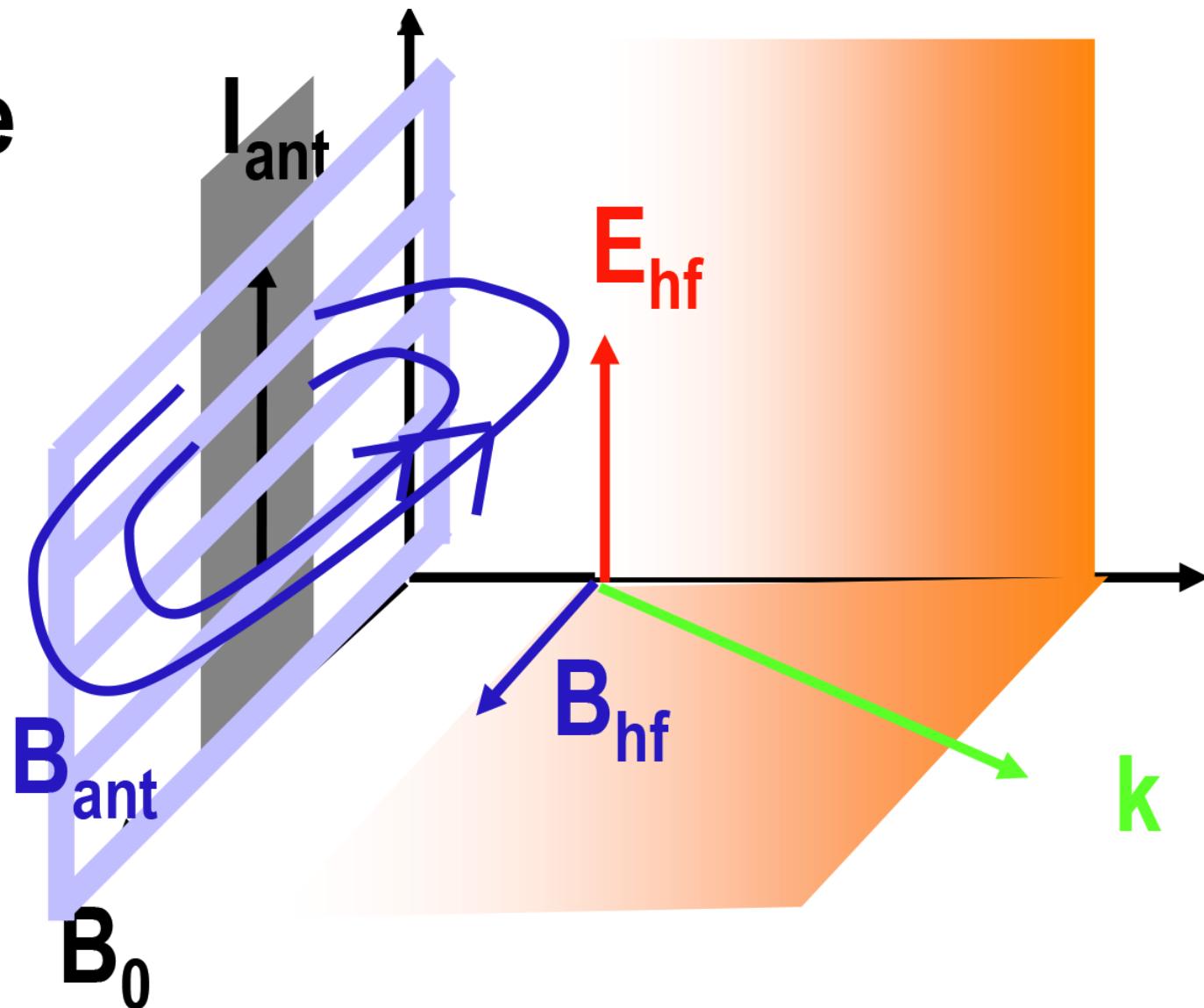


We rely on the *fast wave*, i.e. compressional Alfvén (fast magnetosonic) wave, to bring energy to antenna to plasma

Fast wave

Strap  
antenna

Faraday  
screen



# ICRH - Main principles

Tokamak plasmas contain more than one ion species: dispersion relation is more complicated and allows different schemes for wave absorption

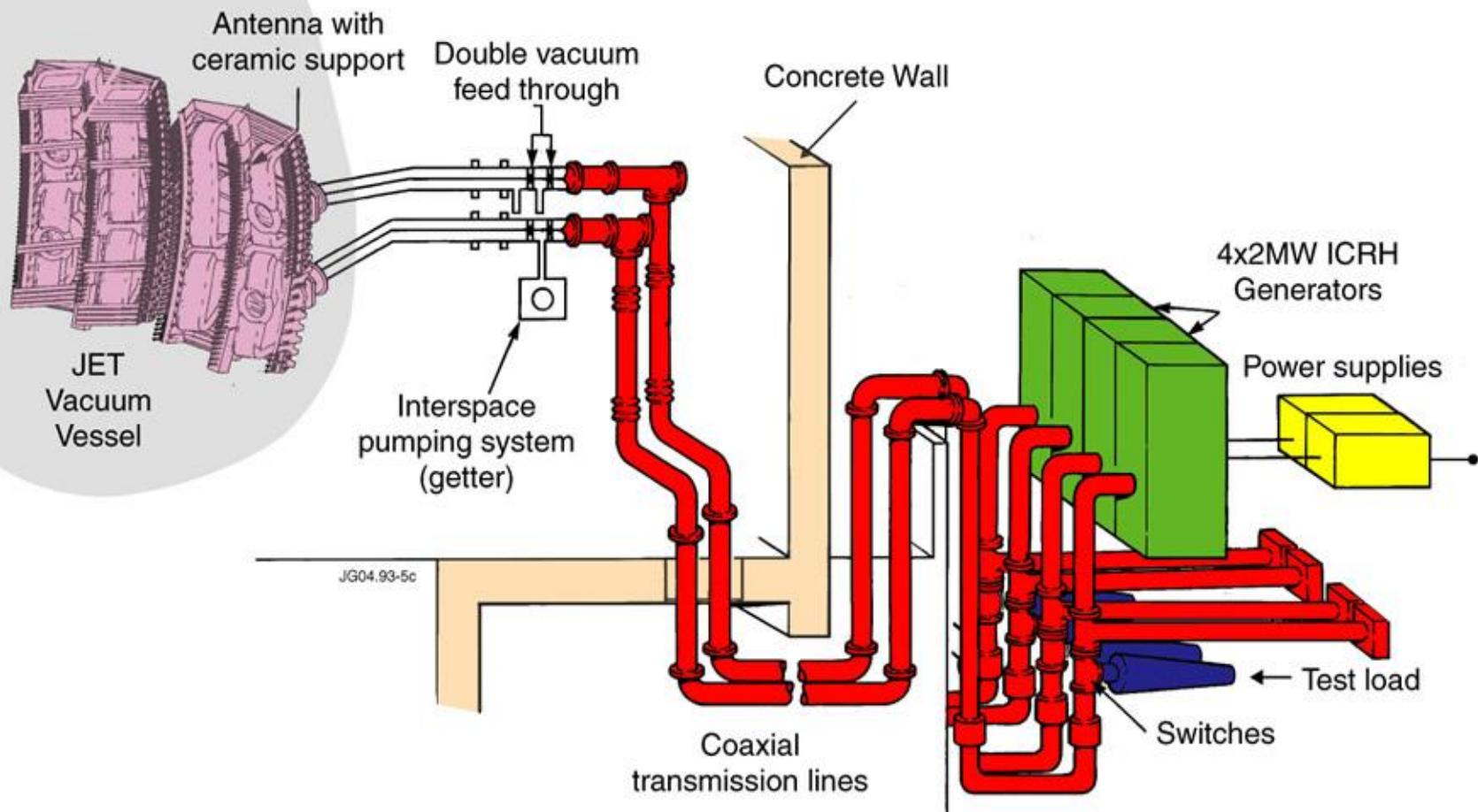
1<sup>st</sup> harmonic of a minority ion (e.g.  $\omega = \Omega_{cH}$  or  $\omega = \Omega_{cHe3}$ )

2<sup>nd</sup> harmonic of main ion species (e.g. in 50:50 DT plasmas  $\omega = 2\Omega_{cT}$ )

Ion-ion hybrid resonance (e.g. in 50:50 DT plasmas  $\Omega_{cT} < \omega < \Omega_{cD}$ )

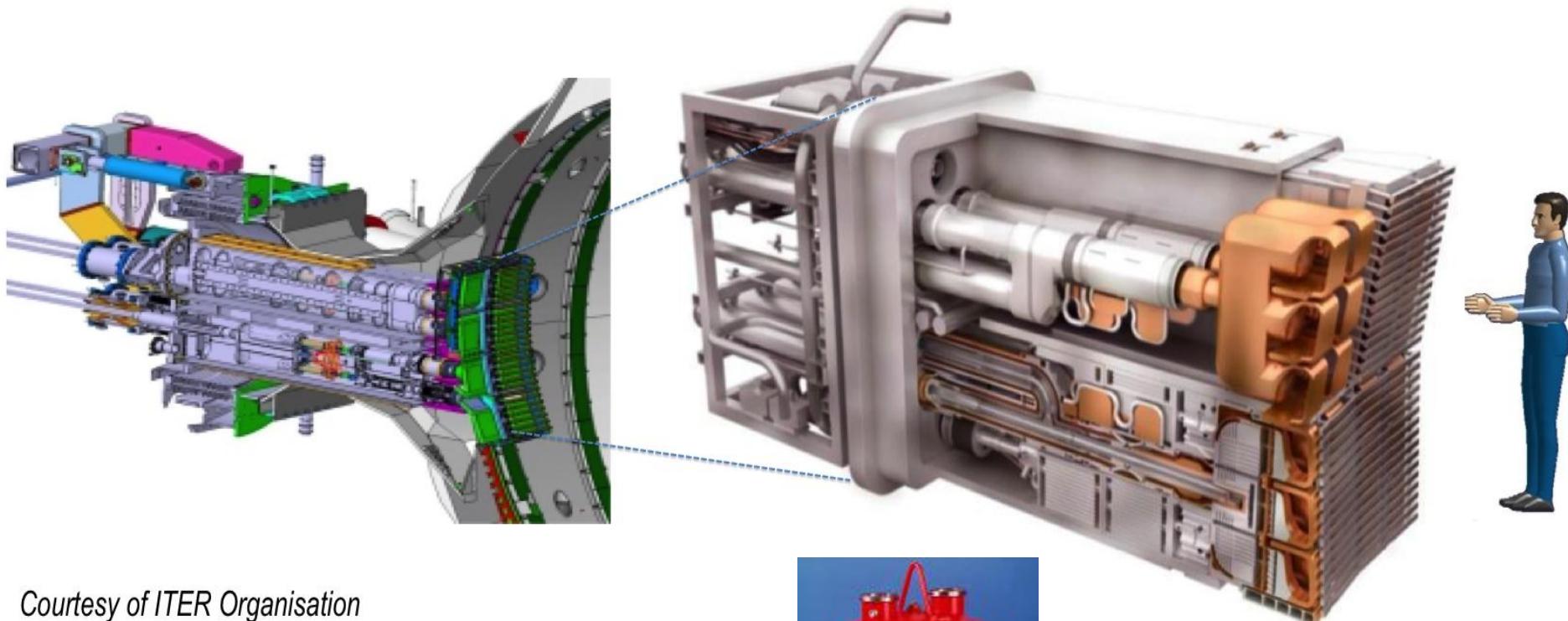
....

## ICRH – JET system



# ICRH – ITER antenna

40 – 55MHz, 20MW, 3600s, 8 coaxial lines, antenna on port-plug



Courtesy of ITER Organisation

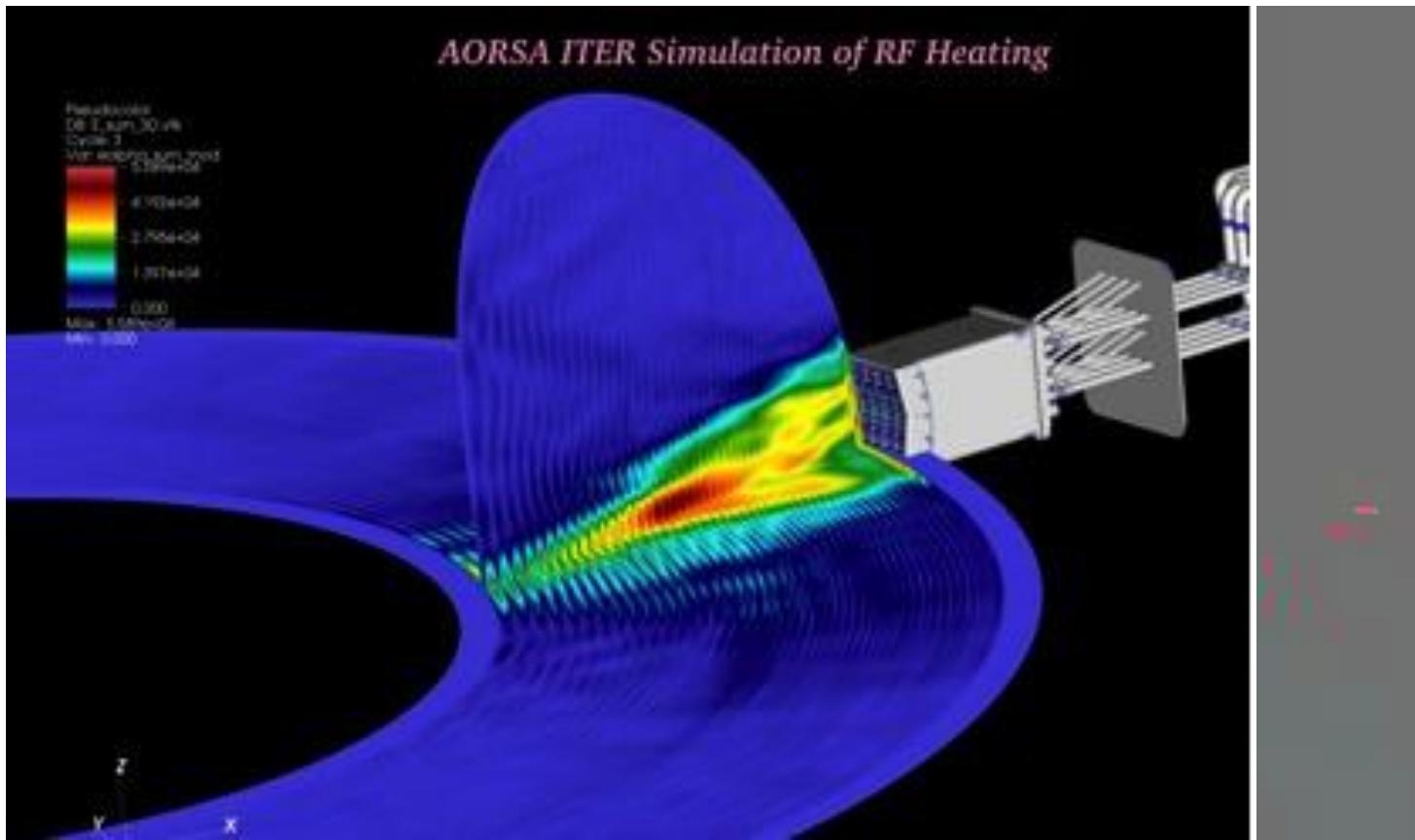


# ICRH modeling

Fast wave has large vacuum  $\lambda$  – cannot be described in simple Fourier formalism

Ex. of wave field from full wave calculation of 2<sup>nd</sup> harmonic T ICRH in ITER (53MHz, 20MW)

*Courtesy of P.Bonoli, E.F.Jaeger et al., PoP 15, 072513 (2008)*



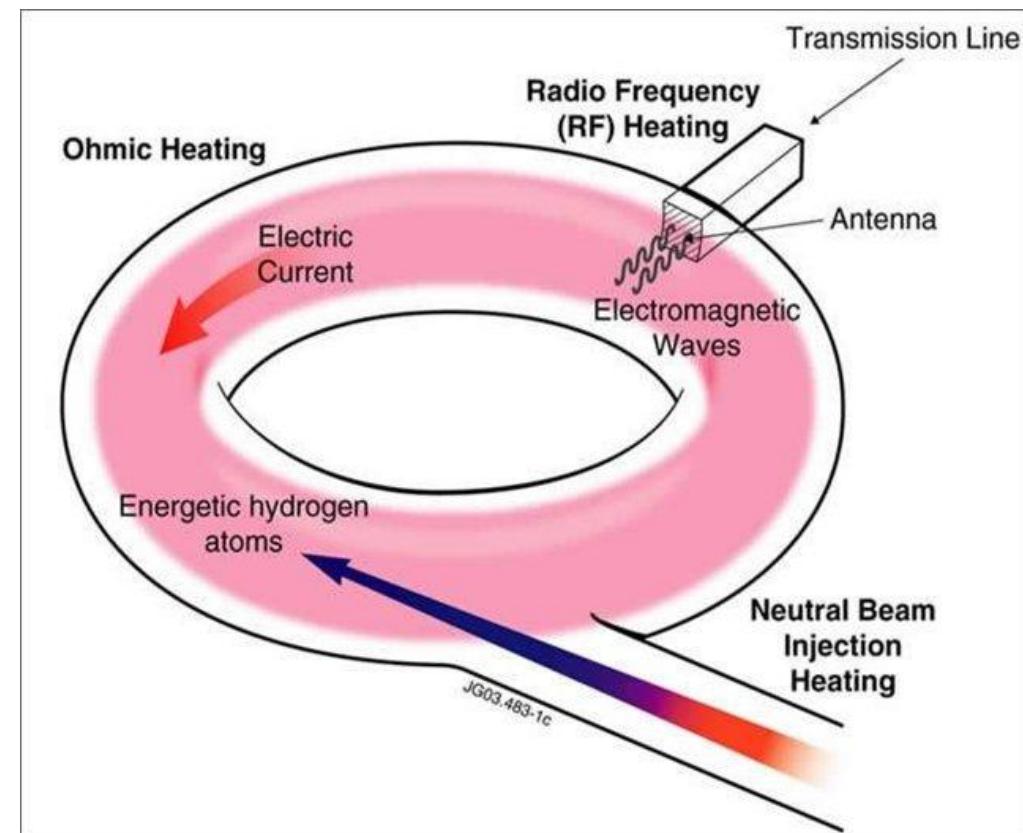
Burning plasma regime is reached using external heating and current drive

*Electron cyclotron heating*

*Ion cyclotron heating*

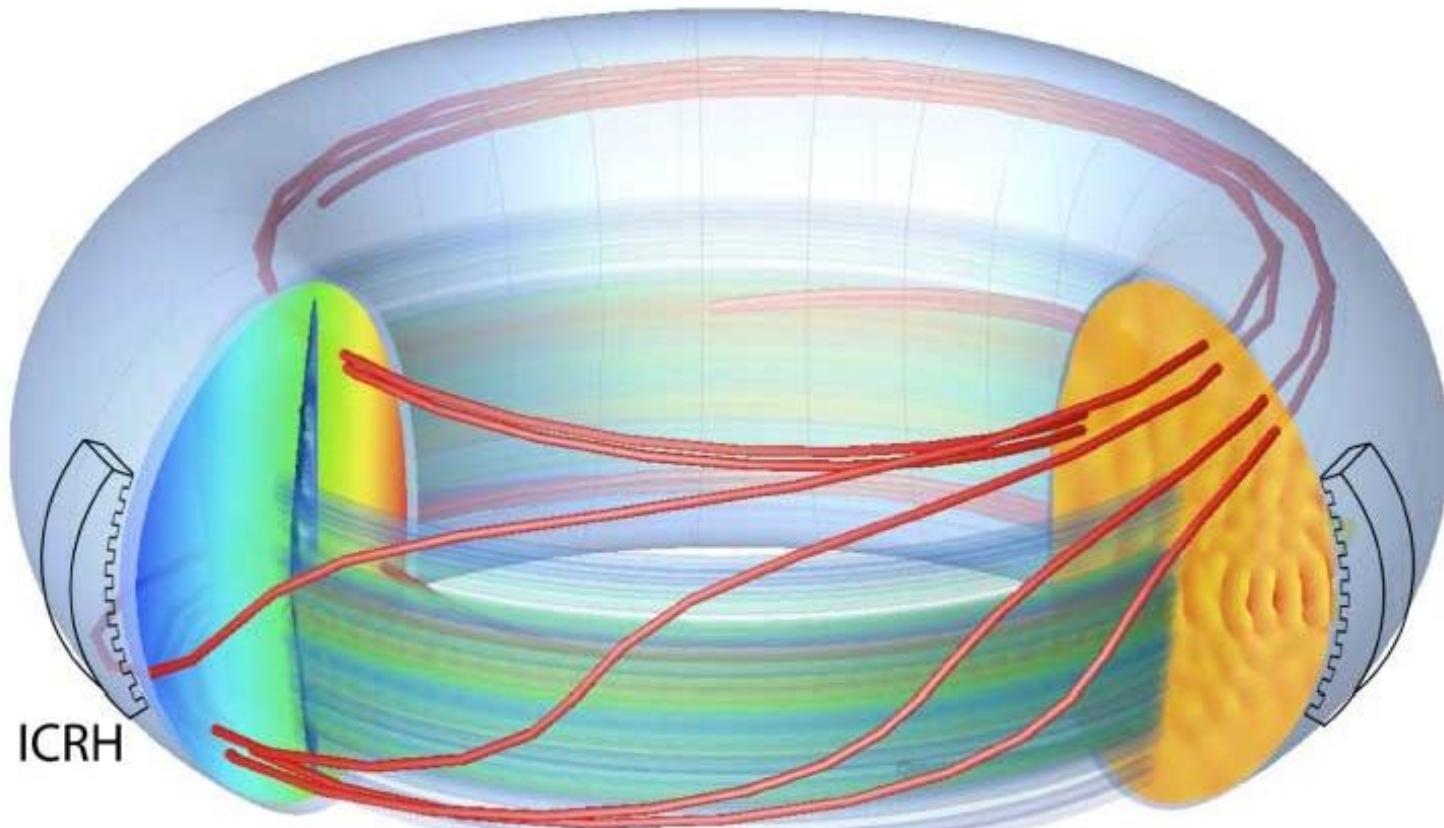
*Neutral beam heating*

Based on creation of  $\sim$ MeV ions, then thermalised by collisions



Wave fields at  $\omega \sim \Omega_{ci}$  give energy to perpendicular motion of minority ions

Strongly anisotropic distribution function: mostly trapped orbits



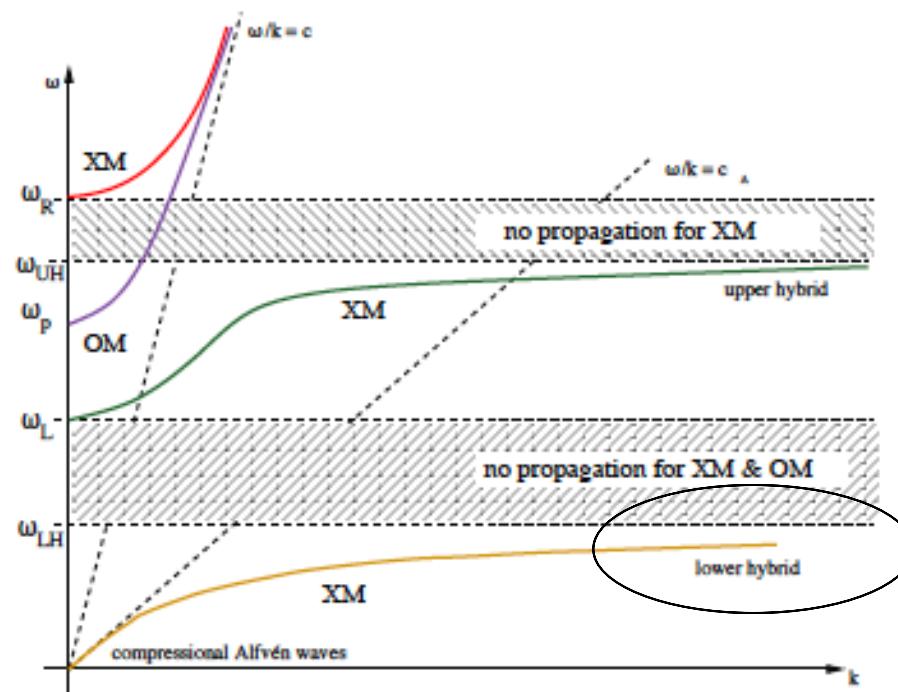
Wave-particle  
resonance

$$f_{LH} = k \cdot v / 2\pi$$

$$\sim 1.3 T_e^{1/2} [\text{keV}] / \lambda_{||} [\text{cm}]$$

$$[\text{GHz}]$$

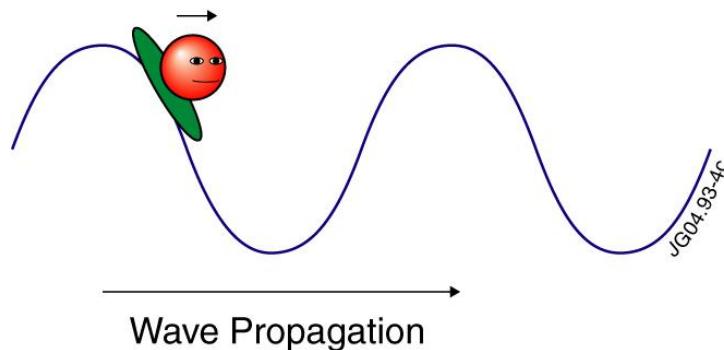
Electrostatic waves  
( $\delta B \sim 0$ )



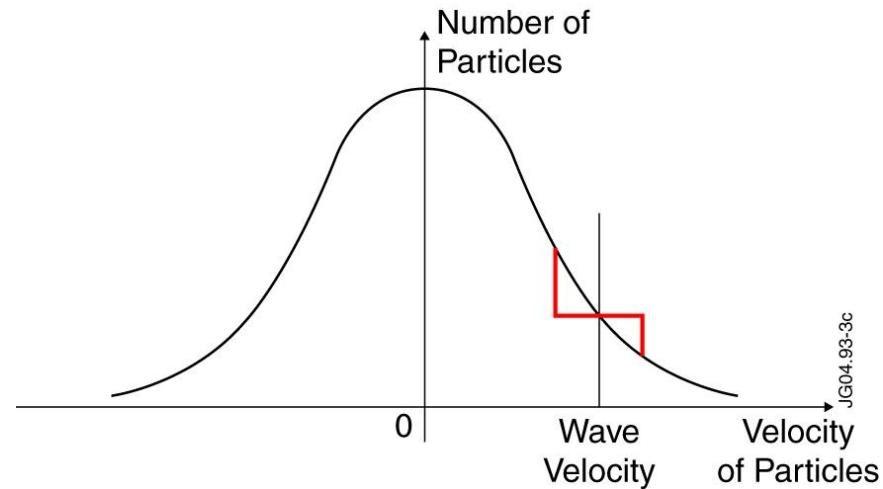
JET  
 $f_{LH} \sim 2.45 \text{ GHz}$

ITER  
 $f_{LH} \sim 5 \text{ GHz}$

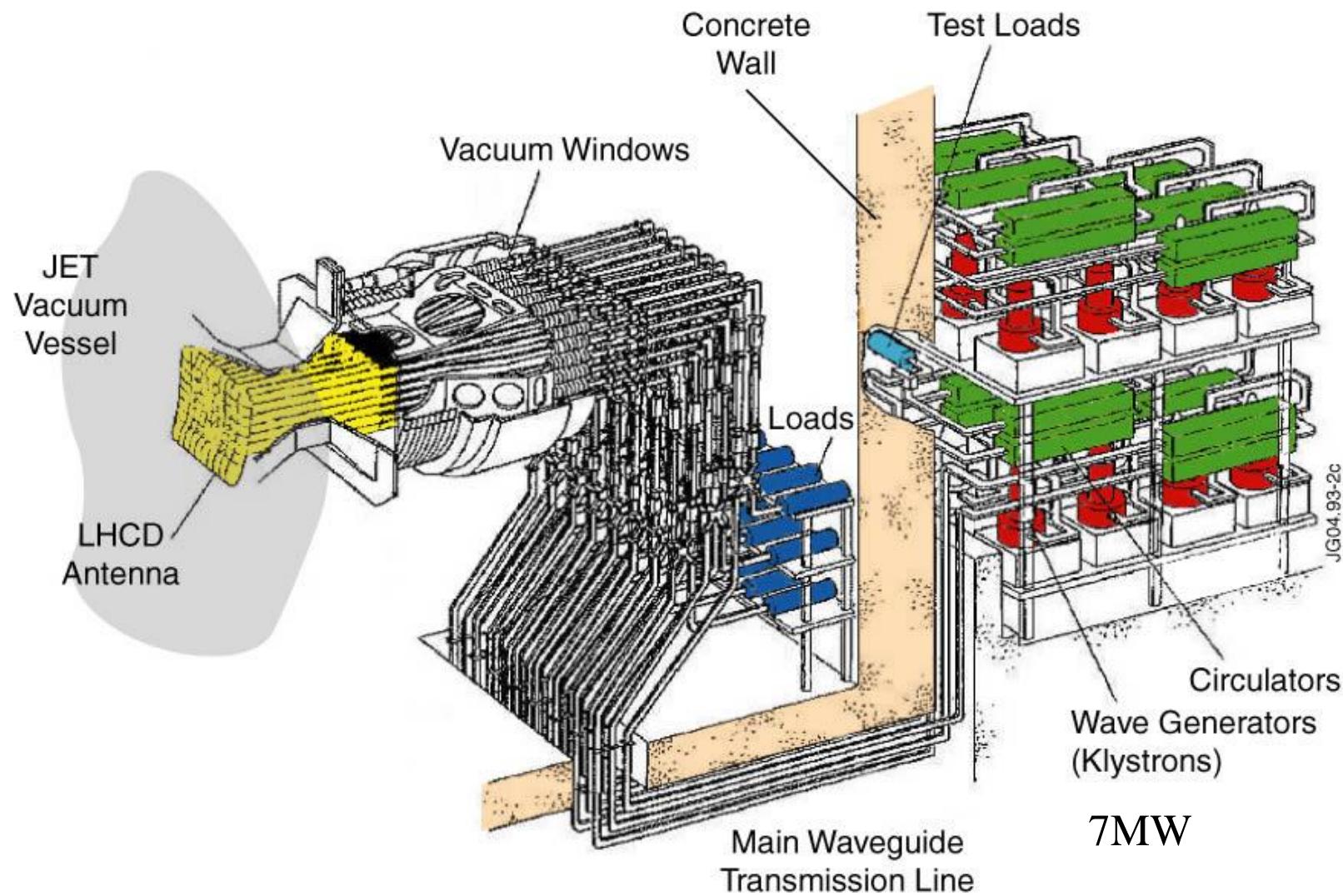
Particle Acceleration



Number of  
Particles

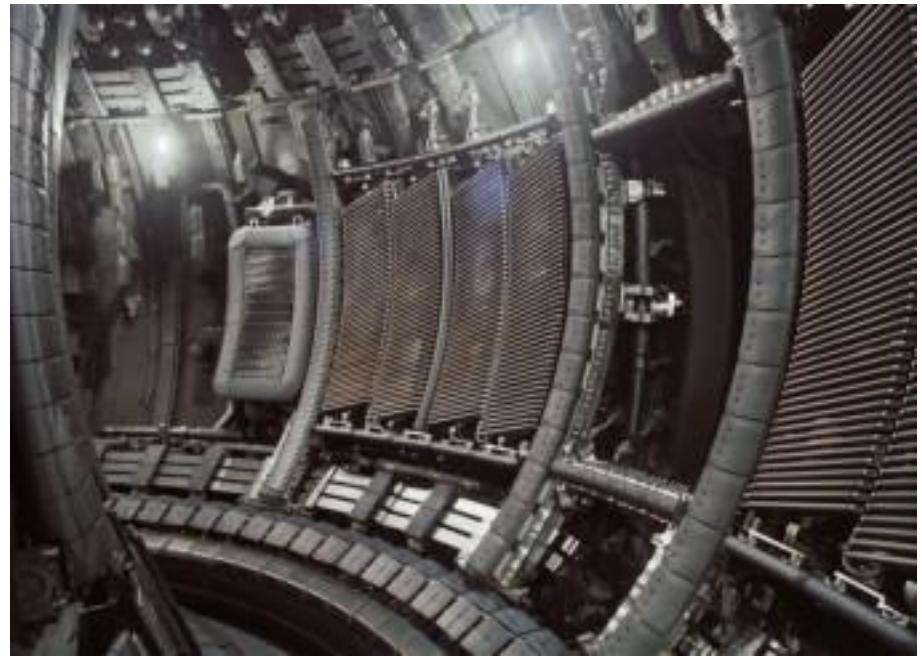


# The Lower Hybrid system in JET



LH waves are electrostatic: need antenna in the plasma

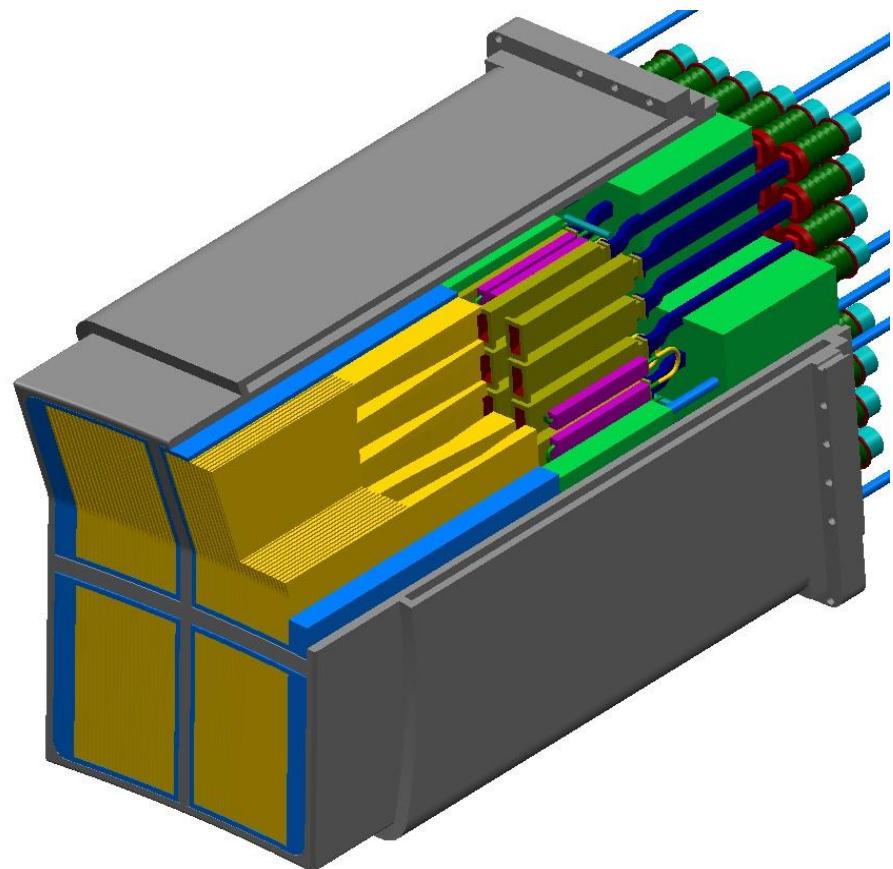
# The Lower Hybrid antenna in JET



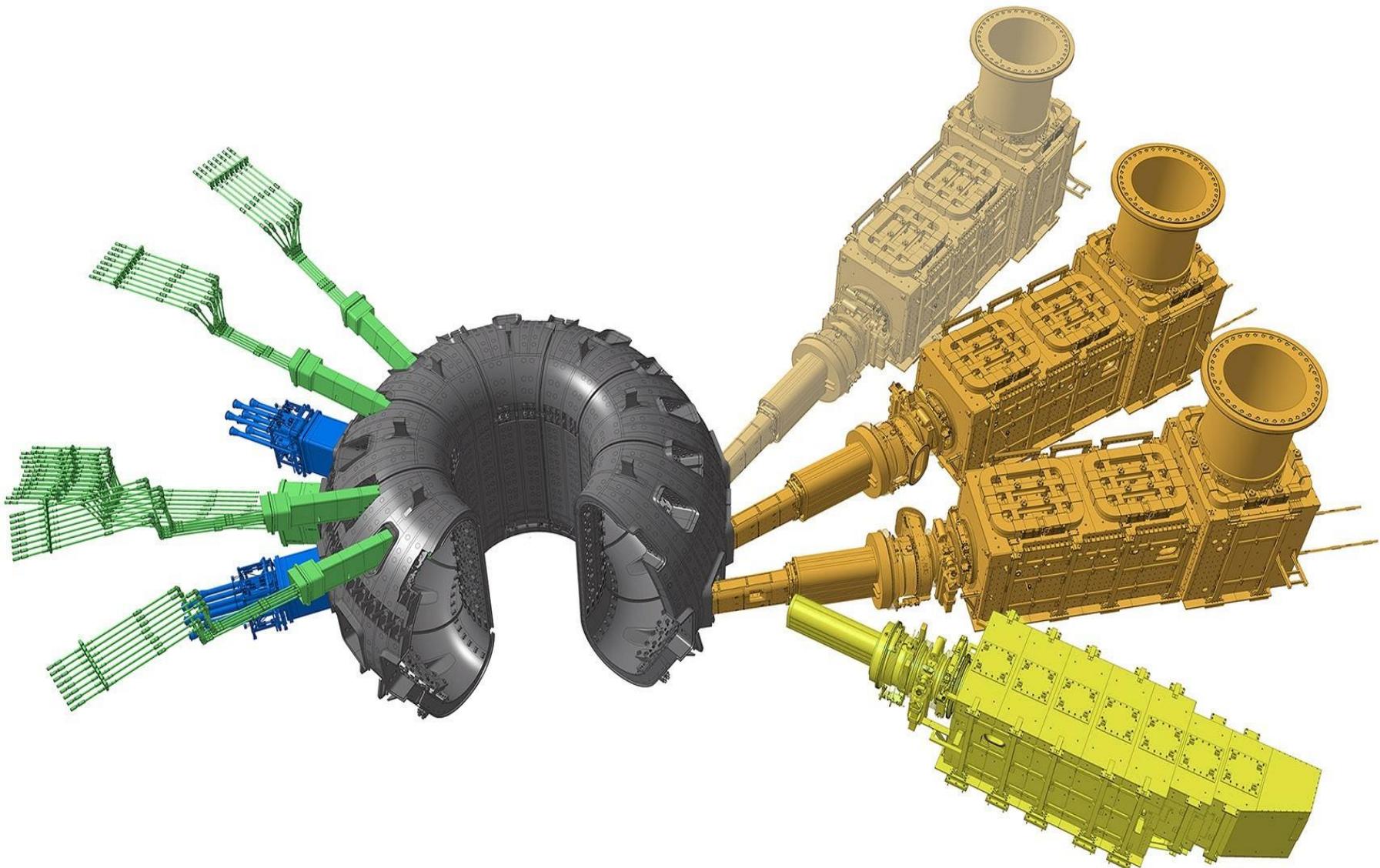
To launch propagating wave for CD, needs well defined spectrum → phasing of many waveguides (‘grill’)  
To couple to plasma needs proximity  
Interaction between antenna and plasma  
Wave must reach core where CD is of interest

# The LH system for ITER

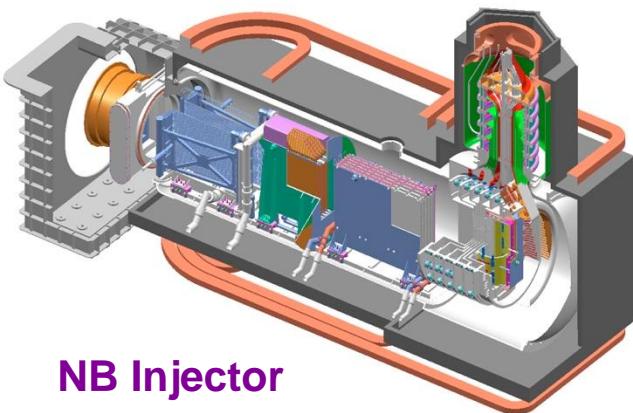
Frequency 5GHz, 20MW will be installed for second stage of heating upgrades  
Mostly for off-axis current drive



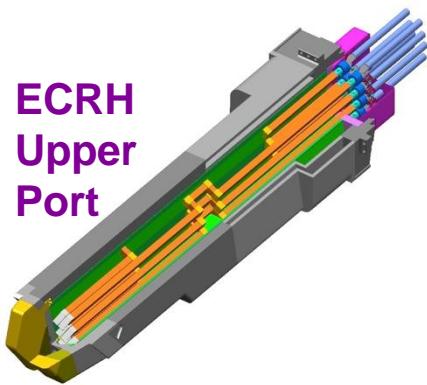
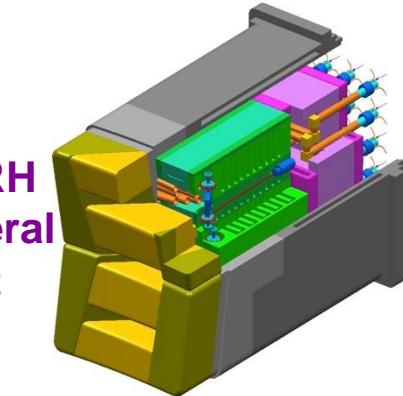
# ITER Heating systems



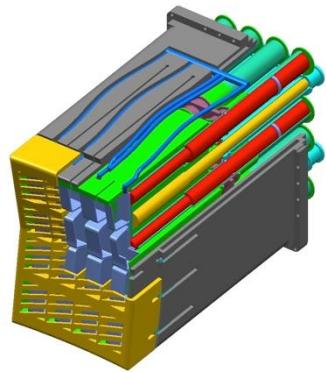
## ITER Heating systems



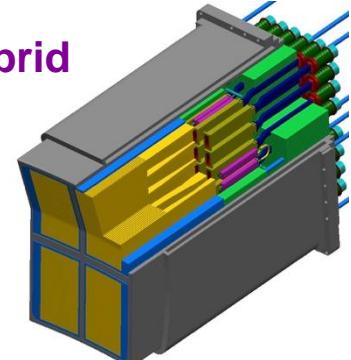
NB Injector

ECRH  
Upper  
PortECRH  
Lateral  
Port

System	Power [MW]	Frequency
NBI	33 MW	N/A
ICRH	20 MW	40-55 MHz
LH	20 MW (second stage)	5 GHz
ECRH	67 MW	170 GHz

ICRH  
antenna

*Discussion: pros and cons of different methods ?*

Lower Hybrid  
Launcher

china eu india japan korea russia usa