

# Plasma II - Exercises

Dr. H. Reimerdes, Dr. E. Tonello - SPC/EPFL

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## 1 Multi-choice questions

### 1.1 If the electron flux to an electrode is not equal to the ion flux, this means that:

- ☐ the electrode is electrically floating.
- ☐ there will soon be no gas left between the electrodes.
- ☐ the ions are much heavier than the electrons.
- ☐ there is an electric current flowing.

### 1.2 The sheath is a dark layer principally because:

- ☐ the Force is not with it.
- ☐  $T_e$  is lower than in the plasma bulk, which reduces the gas excitation rate.
- ☐ the electrode surface absorbs the light in the vicinity of the sheath.
- ☐  $n_e$  is lower than in the plasma bulk, which reduces the gas excitation rate.

### 1.3 The Boltzmann relation can be used to calculate the electron density in the sheath because:

- ☐ the electron drift velocity is much smaller than the electron thermal velocity.
- ☐ the ion drift velocity is much smaller than the ion thermal velocity.
- ☐ the ion drift velocity is much larger than the electron thermal velocity.
- ☐ the electron drift velocity is much smaller than the ion thermal velocity.

### 1.4 Negative ions in a plasma can have almost the same mass and temperature as positive ions. Therefore:

- ( ) They cross the sheath in a similar way to positive ions.
- ( ) They cross the sheath in a similar way to electrons.
- ( ) They cross the sheath in a similar way to neutrals.
- ( ) They cannot cross the sheath and are trapped in the plasma.

## Exercise 1 - Electron motion and ohmic power in radio-frequency fields

Consider a uniform plasma in a background gas with a time-varying electric field  $\vec{E}(t)$ . The first moment of the Boltzmann equation gives the intuitively-reasonable momentum balance for the electrons:

$$m \frac{\partial \vec{u}}{\partial t} = -e \vec{E}(t) - m \nu_{e/n} \vec{u}$$

where  $\vec{u}$  is the electron velocity and  $\nu_{e/n}$  is the electron-neutral collision frequency.

- a) Writing  $\vec{E} = \vec{E}_0 \exp(i\omega t)$ , find an expression for the electron RF current  $\vec{j} = -ne\vec{u}$  and hence find the time-averaged ohmic power  $P_{\text{ohm}}$  per unit volume.  
Hint: the time-averaged power  $\langle \vec{j} \cdot \vec{E} \rangle = \frac{1}{2} \Re(\vec{j} \cdot \vec{E}^*)$ .  
(Note: the power transfer is zero in absence of collisions.)
- b) Show that the ohmic power transfer to the plasma, for a given RF frequency, reaches a maximum when the angular RF frequency  $\omega = \nu_{e/n}$  as the pressure is varied.

## Exercise 2 - Practise the derivation of Bohm's criterion, ion flux, and ion energy to a floating wall

(See Lecture Notes, slides 21-29)

## Exercise 3 - Ion energy in RF plasmas

An engineer needs to bombard a substrate with a constant flux 100 eV ions for an etching process. Explain why you recommend to use an RF power generator at 13.56 MHz frequency with a peak-to-peak output voltage of 400 V. Note that at the chosen gas pressure the RF heats electrons to approximately 2 eV.