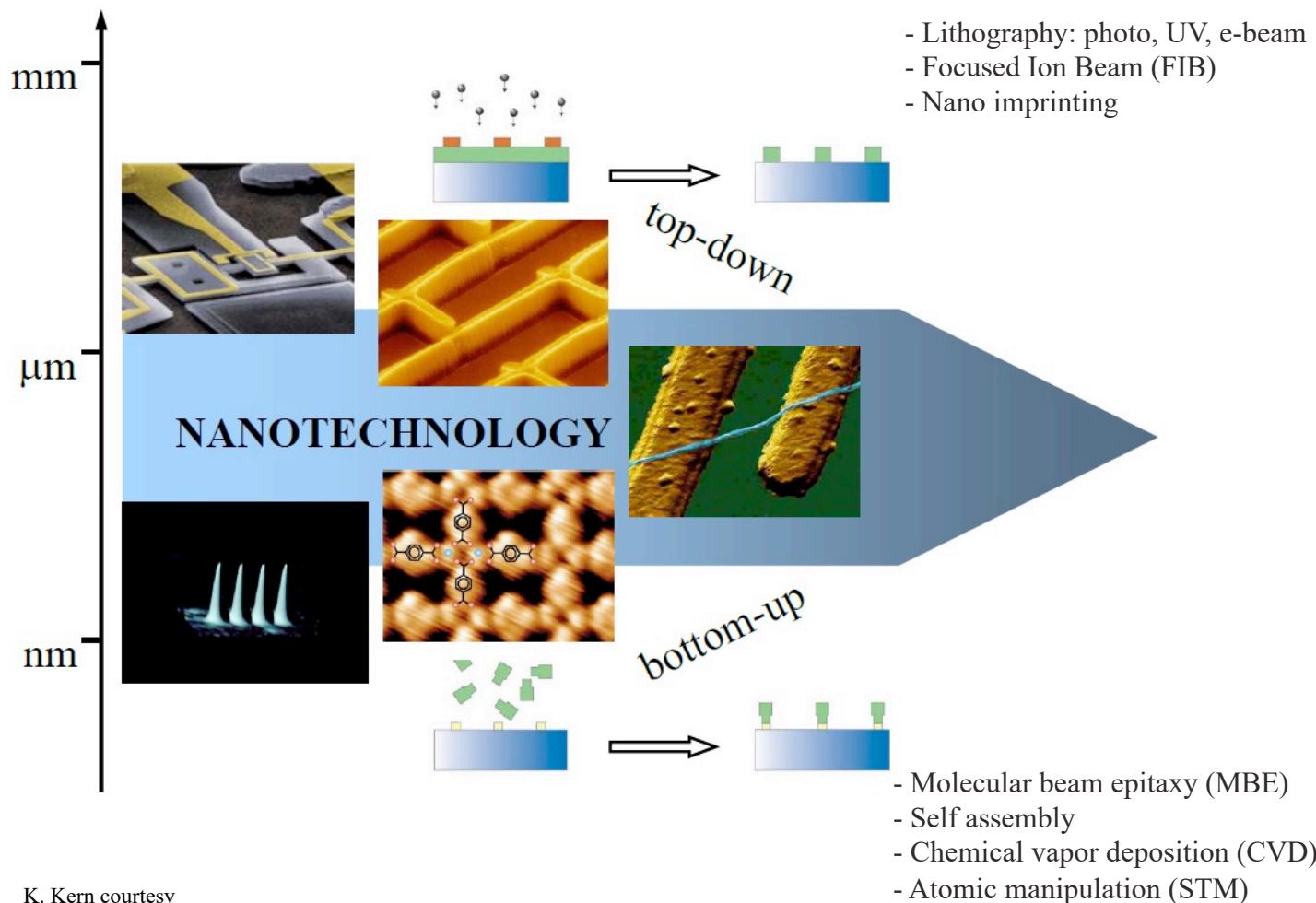
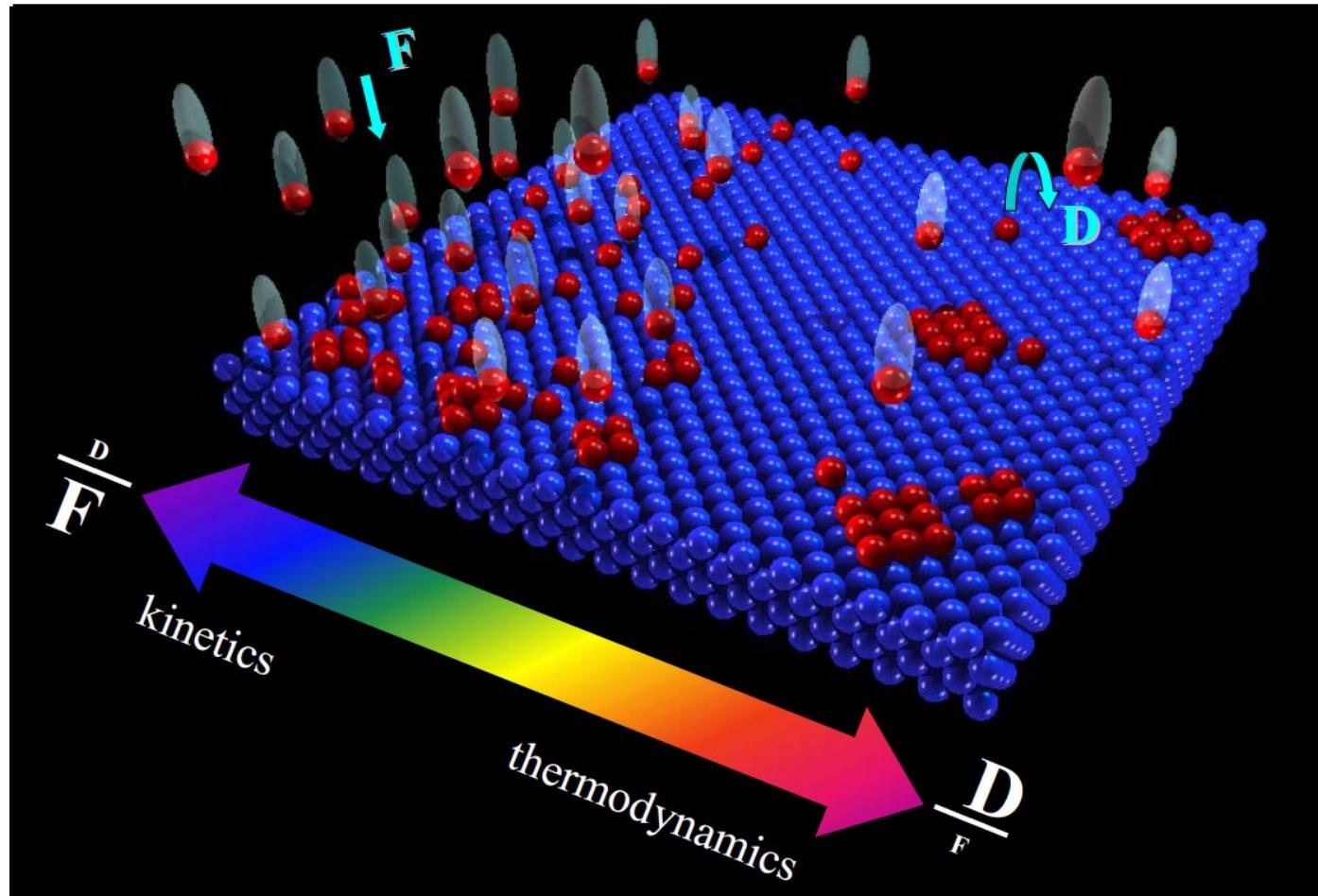


# How to make the nanostructures: two approaches



# Thin film growth / Nanostructure growth



## Surface tension, surface energy and equilibrium surfaces

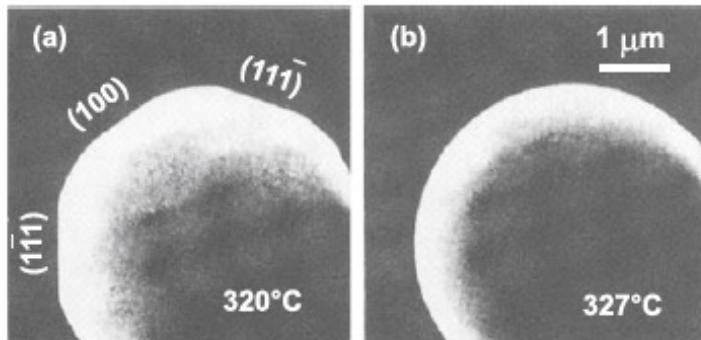
from bulk, creation of a surface (atoms that are not fully coordinated, i.e. broken bonds) → additional energy term  $\gamma$ : surface energy per unit surface (surface tension)

$\gamma > 0$  and energy =  $\gamma A$ , with  $A$  the area of the additional surface, at constant volume

shape of a solid at equilibrium minimizes the surface energy

in liquids  $\gamma$  is isotropic → spherical shape (smallest surface area)

in solids  $\gamma$  is different for the different surface orientations of a crystal:  $\gamma(\vec{n})$



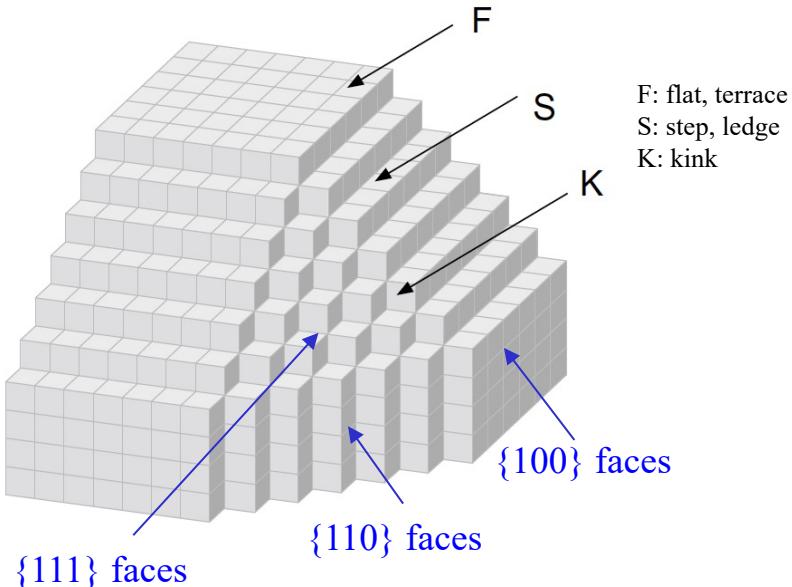
SEM photographs of the equilibrium shape of Pb crystals in the [011] azimuth; in b) Pb is liquid  
J.J. Métois & J.C. Heyraud, **31**, 73 (1989)

# Kossel crystal – TLK model

different crystal orientation → different surface energy

simplest model: Kossel crystal (simple cubic - sc)

evaluate the number of broken bonds per unit surface depending on the surface orientation



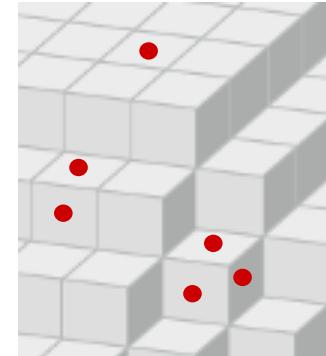
considering only the nearest neighbors (NN)

bulk: 6 NN → 6 bonds per atom

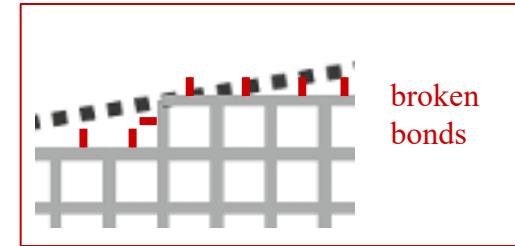
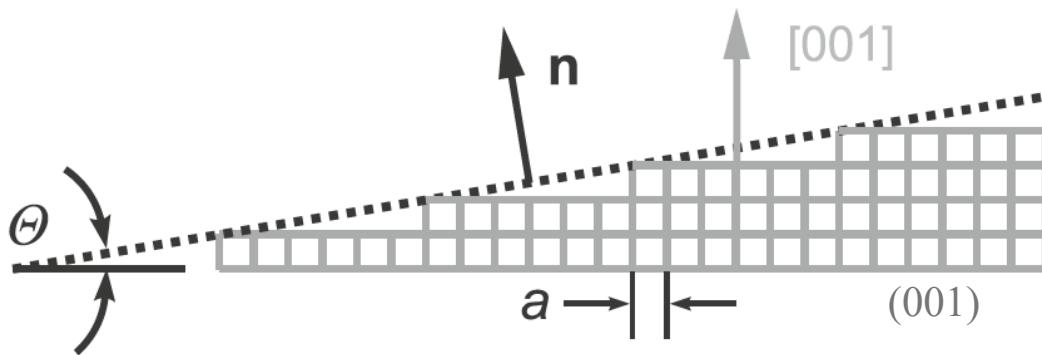
terrace: 5 NN → 5 bonds per atom, 1 broken bond

step: 4 NN → 4 bonds per atom, 2 broken bonds

kink: 3 NN → 3 bonds per atom, 3 broken bonds  
(half-crystal site)



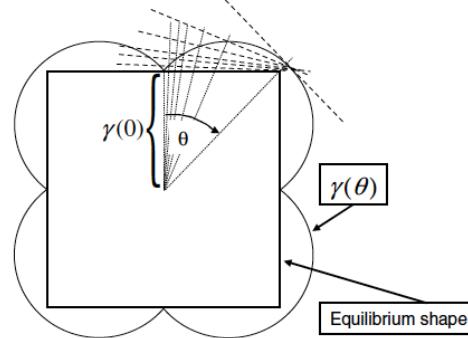
# Vicinal surfaces (stepped)



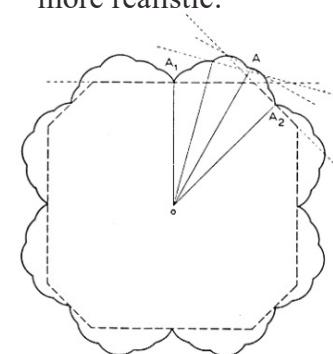
Wulff construction /  $\gamma$  plot

- The surface energy of a vicinal surface always exceeds that of the corresponding singular surface
- From  $\gamma(\theta) \rightarrow$  equilibrium crystal shape
- Experimentally: from crystal shape  $\rightarrow$  surface energy

simplest example:



more realistic:



## Surface tension for cubic crystals

considering the number of broken bonds per unit surface, for singular (low-Miller index) surfaces:

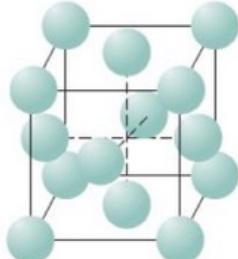
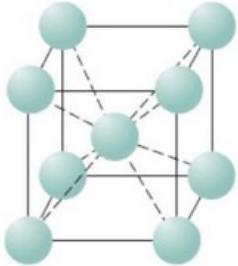
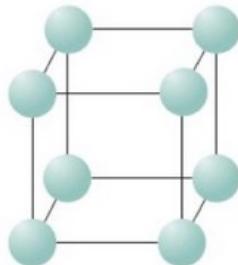
sc:  $\gamma_{100} < \gamma_{110} < \gamma_{111}$

bcc:  $\gamma_{110} < \gamma_{100} < \gamma_{111}$

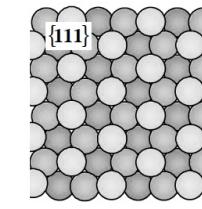
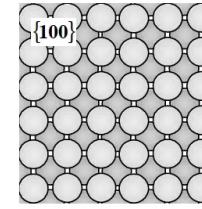
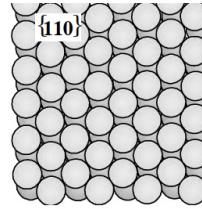
fcc:  $\gamma_{111} < \gamma_{100} < \gamma_{110}$

in general, the more compact the surface, the lower the energy

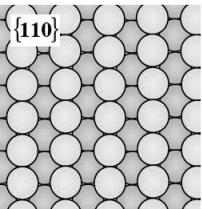
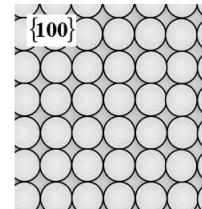
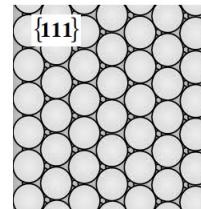
conventional unit cell



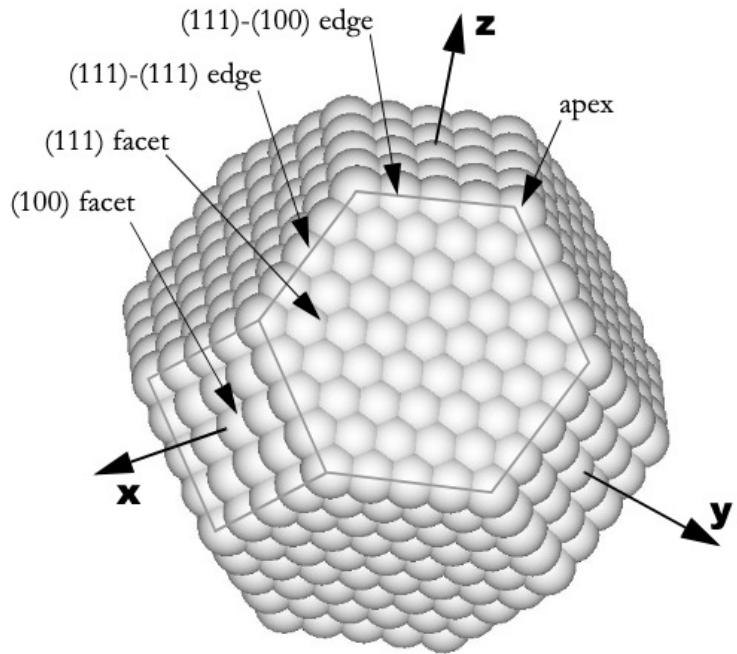
bcc



fcc



# Equilibrium crystal shape



1289 atoms, truncated octahedron  
surface:volume ratio = 482:807

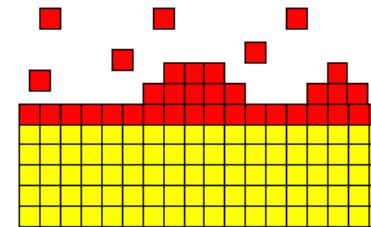
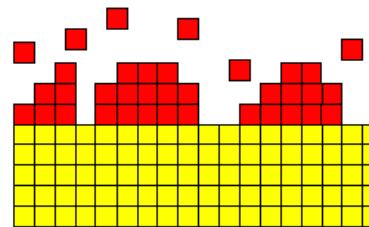
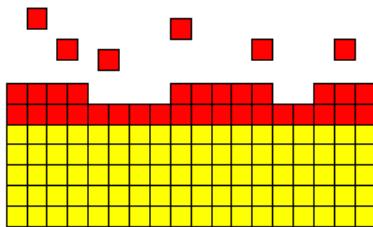
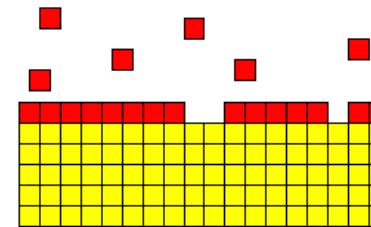
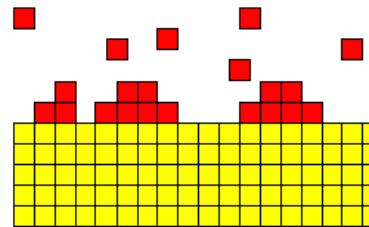
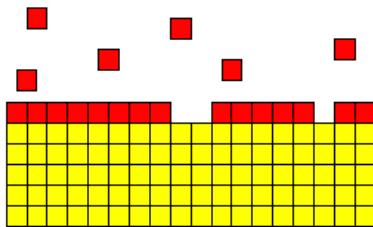
## Facts and Figures:

- 482 surface atoms
- 8 (111)-facets
- 6 (100)-facets
- 24 apex positions
- 54 atoms on a (100)-surface  
(excluding edges)
- 296 atoms on a (111)-surface  
(excluding edges)
- 36 atoms form a (111)-(111)  
edge
- 72 atoms form a (100)-(111)  
edge

Warning: the broken bond model for surface energy neglects the relaxation in positions of the atoms near the surface of a crystal (discussed later)

# Growth modes (at thermodynamic equilibrium)

Growth of B on A



layer - by - layer growth  
(Frank - van der Merve)

surface energy

island growth  
(Volmer - Weber)

layer - by - layer  
+ island growth  
(Stranski - Krastanov)  
surface energy & strain

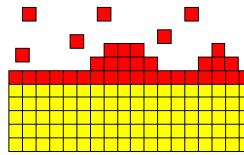
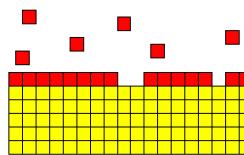
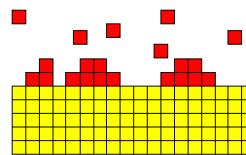
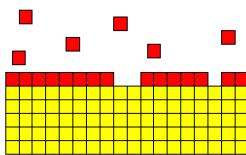
# Growth modes (at thermodynamic equilibrium)

## Growth of B on A

$\gamma_A$ : surface energy of A  
(interface with vacuum)

$\gamma_B$ : surface energy of B  
(interface with vacuum)

$\gamma_{AB}$ :  
A-B interface energy  
(hybridization,  
lattice mismatch,...)



layer - by - layer growth  
(Frank - van der Merve)

island growth  
(Volmer - Weber)

layer - by - layer  
+ island growth  
(Stranski - Krastanov)

$$\gamma_B + \gamma_{AB} \leq \gamma_A$$

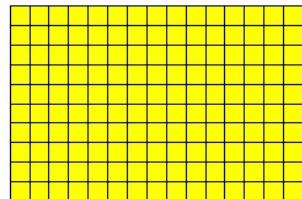
$$\gamma_A < \gamma_B + \gamma_{AB}$$

$\gamma_B + \gamma_{AB} < \gamma_A$  at the beginning, but  $\gamma_{AB}$  increases with coverage (typically due to strain) → change from 2D to 3D

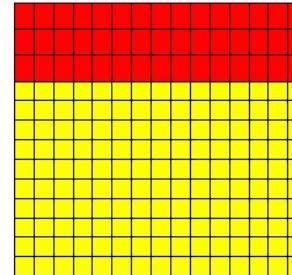
# Stranki-Krastanov growth of semiconductor quantum dots

lattice parameters  
don't match

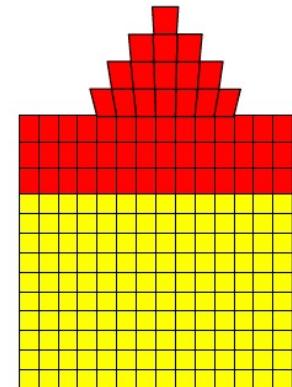
$$a_B > a_A$$



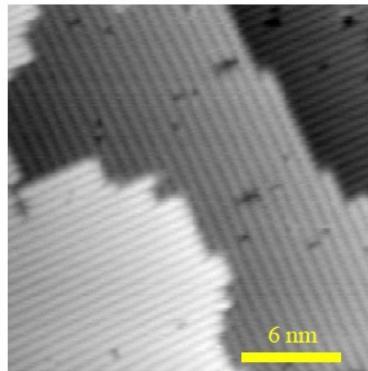
substrate



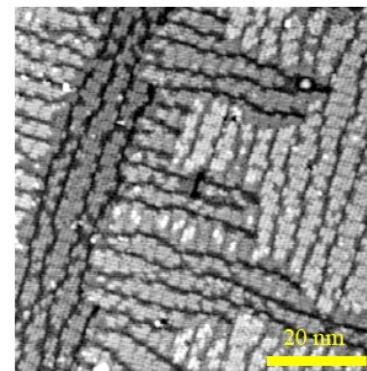
wetting layer



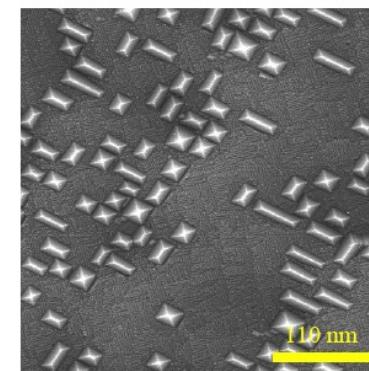
islands



Si(001)



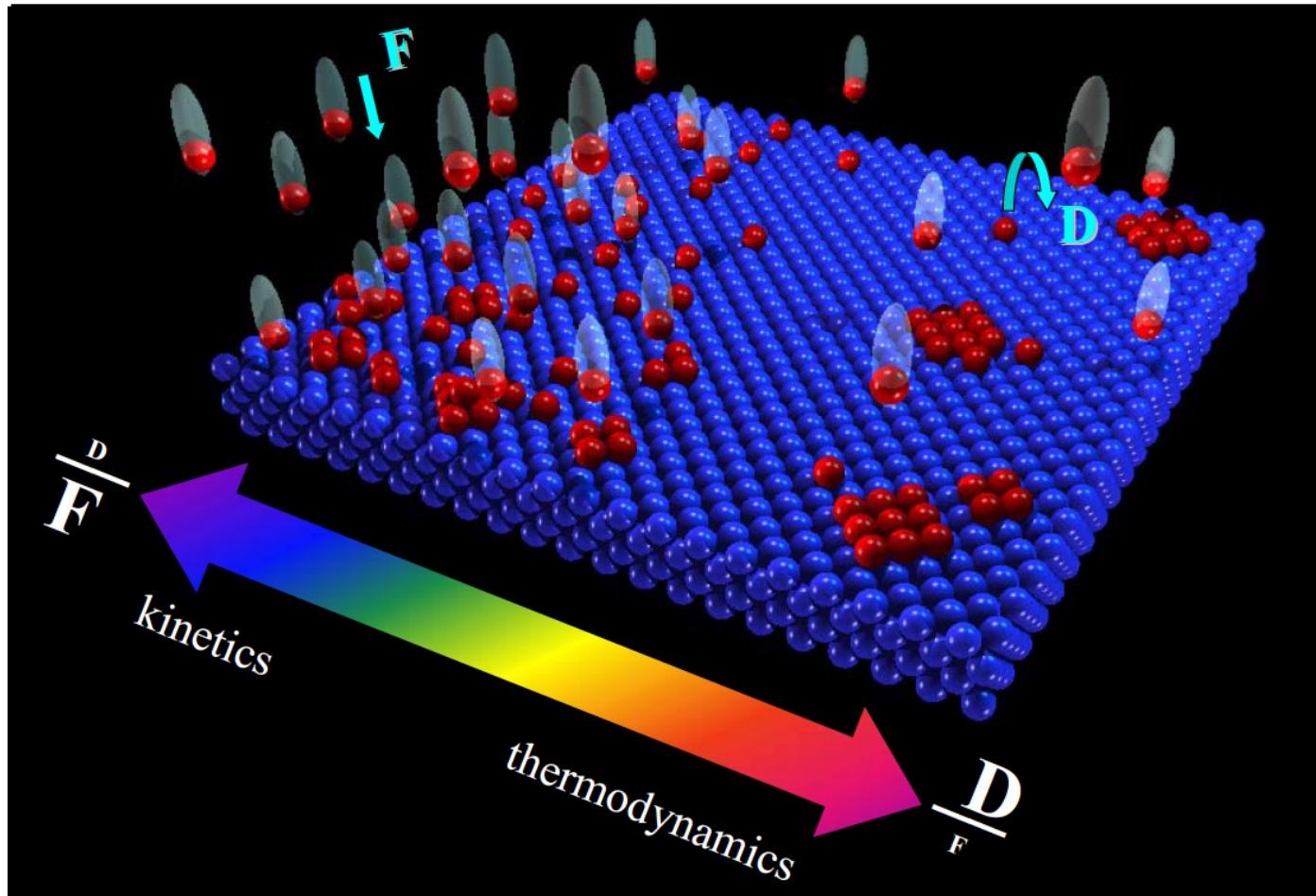
3ML Ge on Si(001)



6ML Ge on Si(001)

exact shape:  
balance between  
surface energy,  
strain energy, and  
volume

## Thin film growth / Nanostructure growth

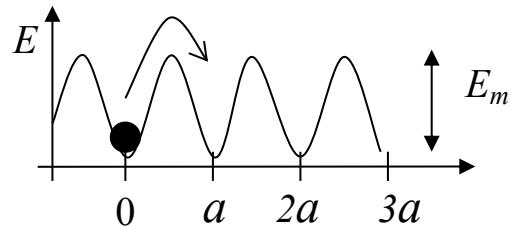


# Growth as a non-equilibrium process: kinetics

single crystal surfaces: a 2D laboratory

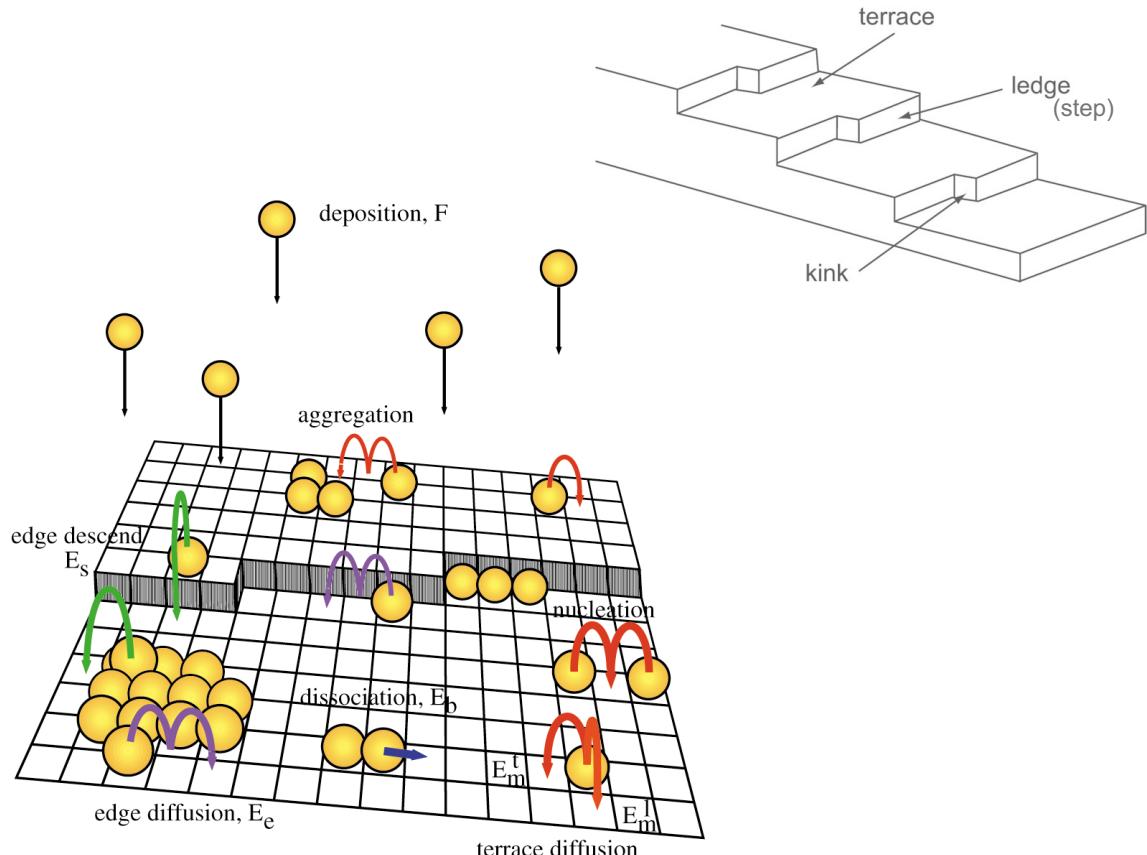
each process  $i$  has  
an energy barrier  $E_i$  and a rate  $v$

$$\nu = \nu_0 \exp(-E_i/k_B T)$$



diffusion process, random walk  
a lattice constant,  $t$  time  
number of jumps =  $\nu t$   
mean squared displacement:

$$\langle \Delta r^2 \rangle = \nu a^2 t$$



# Growth as a non equilibrium process

Aim: controlling

- mean size (size distribution)
- density
- shape
- composition

Control parameters:

- substrate temperature  $T$
- deposition flux  $F$
- surface coverage  $\Theta$
- substrate/overlayer material (strain, mixing, etc.)
- substrate symmetry or patterning

# Statistical growth: $T \rightarrow 0$ K

- thermally-activated diffusion is frozen

$$\nu = \nu_0 \exp(-E_1/k_B T) \rightarrow 0$$

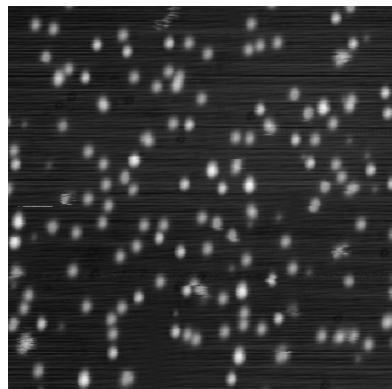
- coverage determines mean island size  $n$

- broad size distribution

Co/Pt(111)

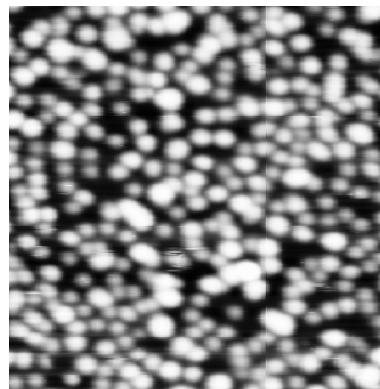
0.03 ML,  $T = 50$  K:

$$n = 1.2$$



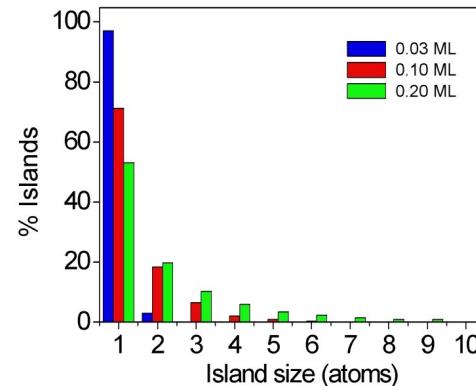
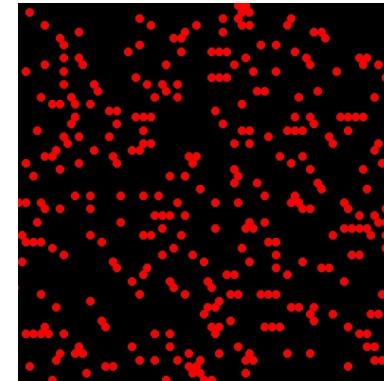
0.10 ML,  $T = 50$  K:

$$n = 2.9$$



$n$  = mean island size = coverage/island density

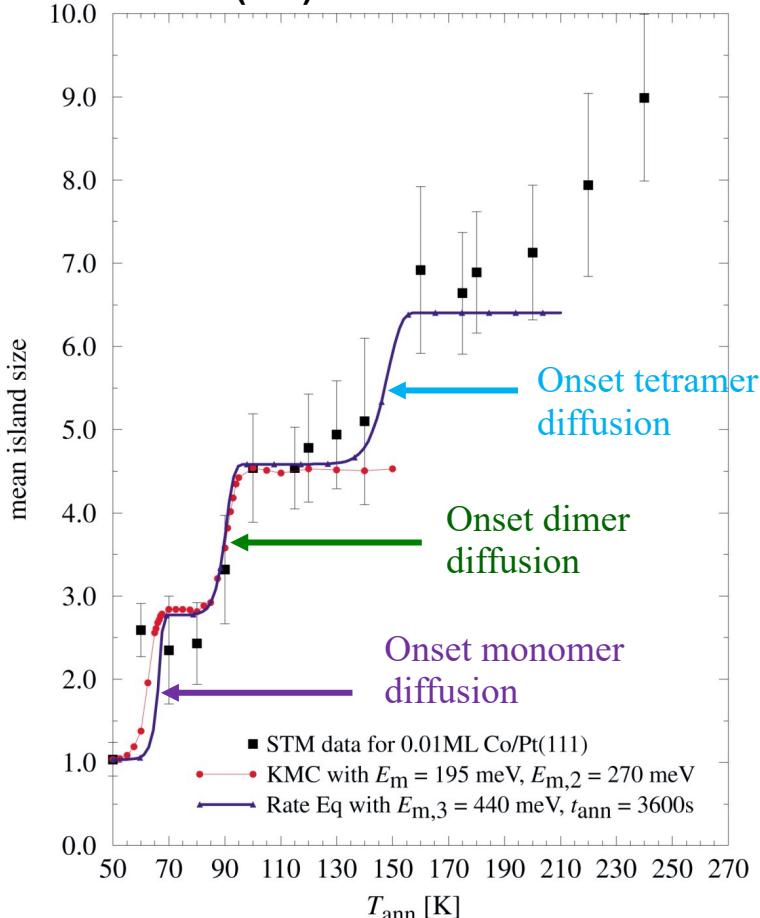
Kinetic Monte Carlo simulation



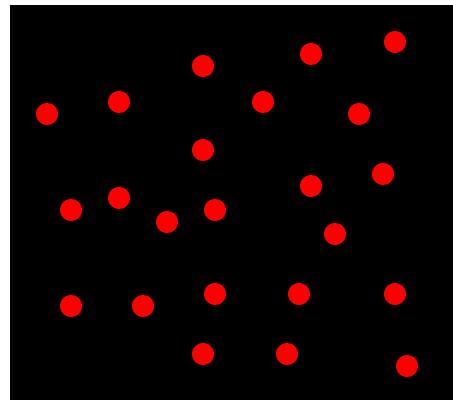
# Adatom and cluster diffusion

Ex:

Co/Pt(111)



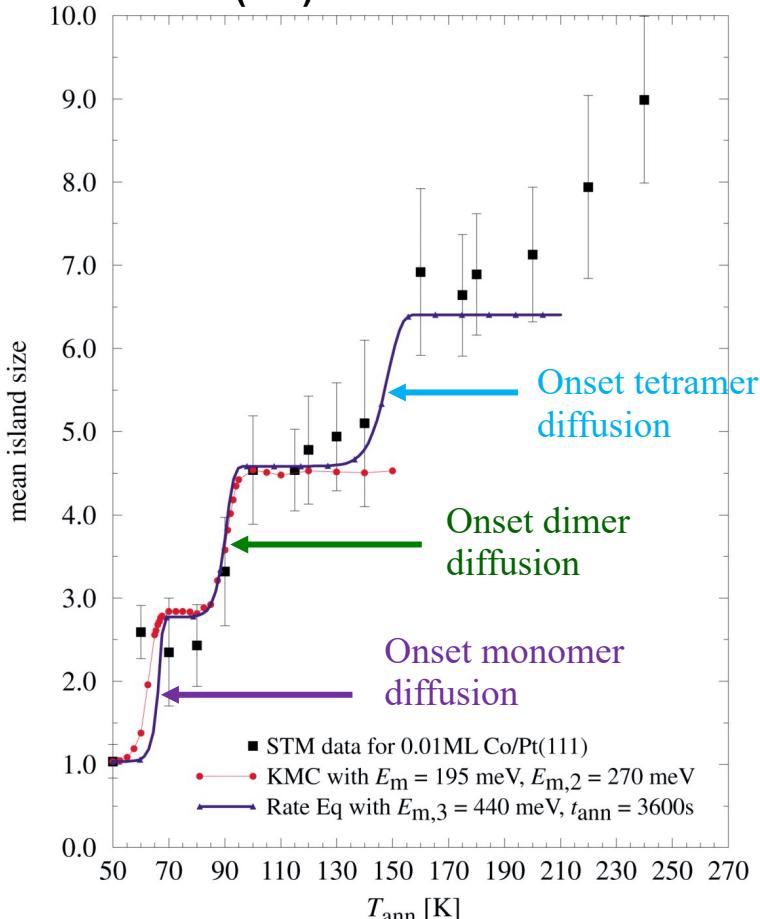
$T < 60$  K: monomers



# Adatom and cluster diffusion

Ex:

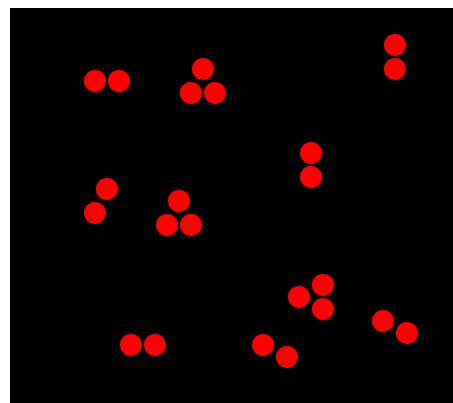
Co/Pt(111)



By increasing T, sequential activation of cluster diffusion results in size selection:

$T < 60$  K: monomers

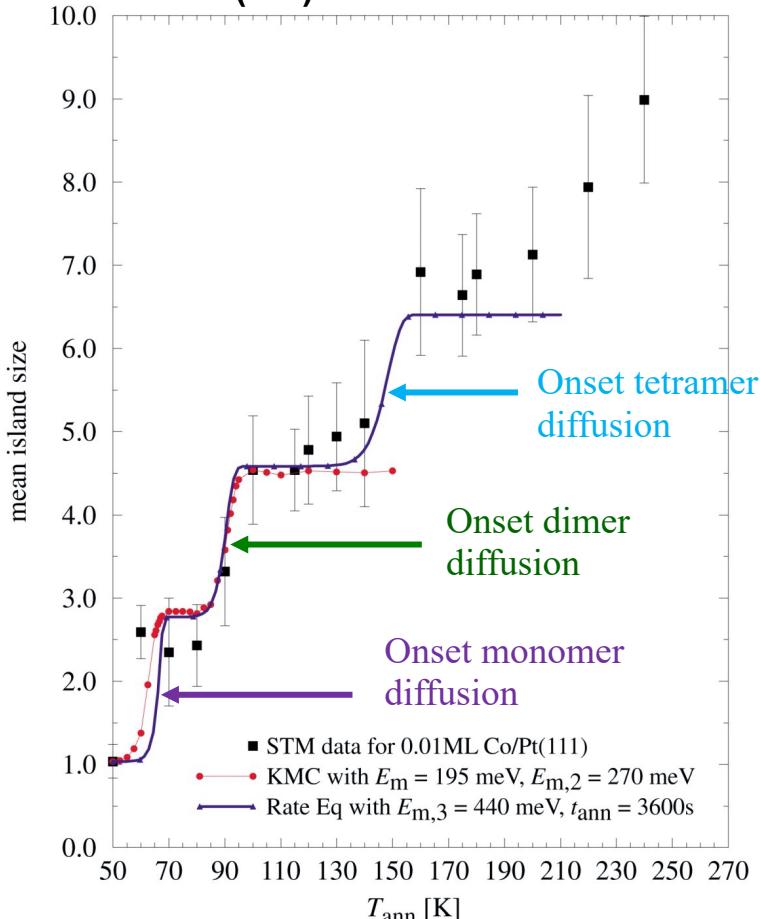
$60$  K  $< T < 90$  K: dimers and trimers



# Adatom and cluster diffusion

Ex:

Co/Pt(111)

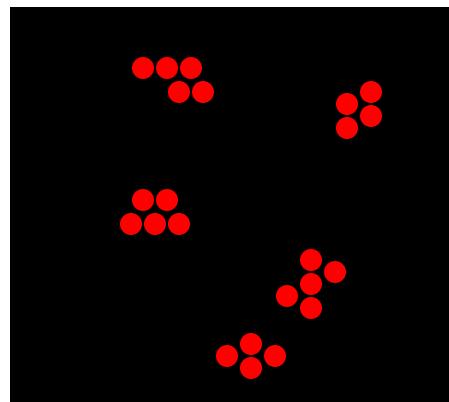


By increasing T, sequential activation of cluster diffusion results in size selection:

$T < 60$  K: monomers

$60 \text{ K} < T < 90$  K: dimers and trimers

$100 \text{ K} < T < 130$  K: tetramers and pentamers



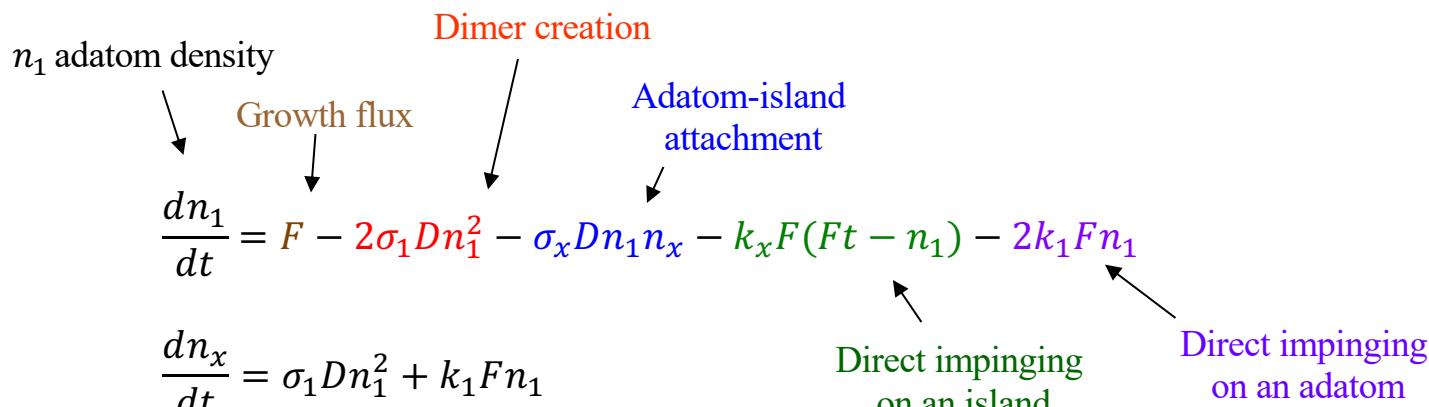
## Rate equations: simple case of $i = 1$

Assumption: adatom can diffuse with a rate  $D$   
but

dimer is stable, i.e. when two atoms meet, they cannot detach

Critical size  $i=1$

Time evolution of average values of  $n_1$  and  $n_x$



$$D = D_0 \exp(-E_1/k_B T)$$

$\sigma_1$  and  $\sigma_x$  capture rates

$E_1$  is the diffusion energy barrier of a monomer ( $i=1$ )

Rate equations give the formation rate for adatoms and stable islands

## Island density

$$n_x = \eta(\theta, i) \left(\frac{D}{F}\right)^{-\chi} \exp\left(\frac{E_i^c}{(i+2)k_B T}\right)$$

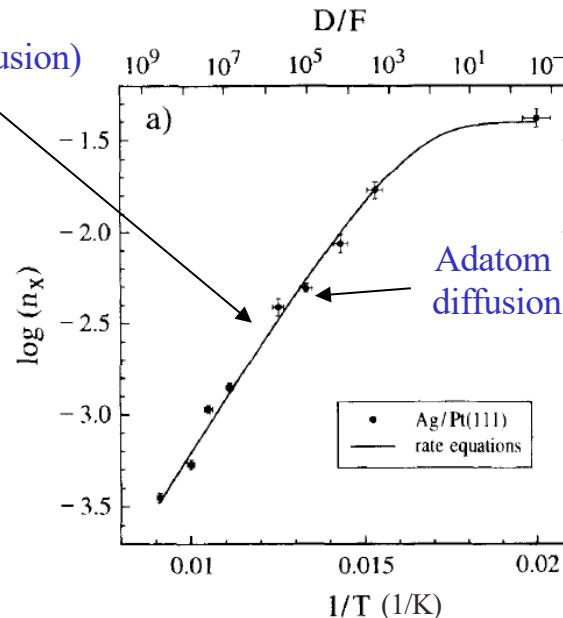
$$D = D_0 \exp\left(-\frac{E_1}{k_B T}\right) \quad \chi = \frac{i}{i+2}$$

$E_i^c$  is the dissociation energy of the island with critical size =  $i$

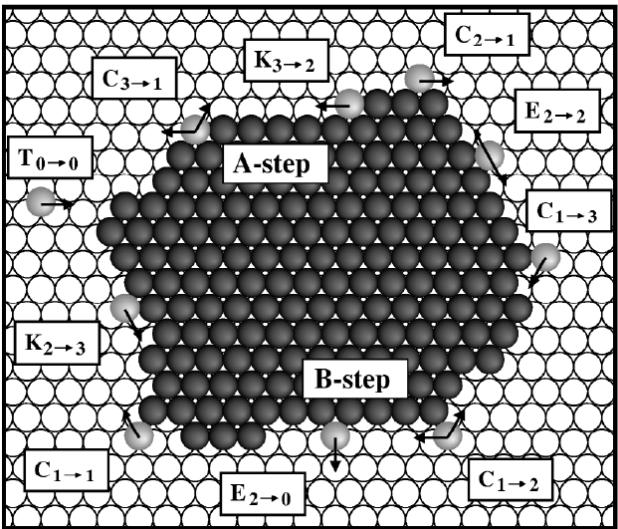
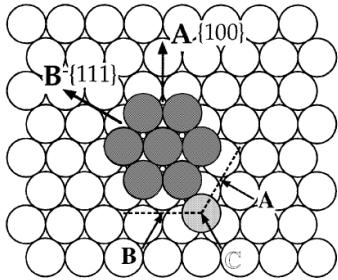
$$i = 1 \rightarrow E_i^c = 0 \rightarrow n_x = \eta(\theta, 1) \left(\frac{D}{F}\right)^{-1/3} = \eta(\theta, 1) \left(\frac{D_0}{F}\right)^{-1/3} \exp\left(\frac{E_1}{3k_B T}\right)$$

The slope gives  $E_1$   
(energy barrier for adatom (monomer) diffusion)

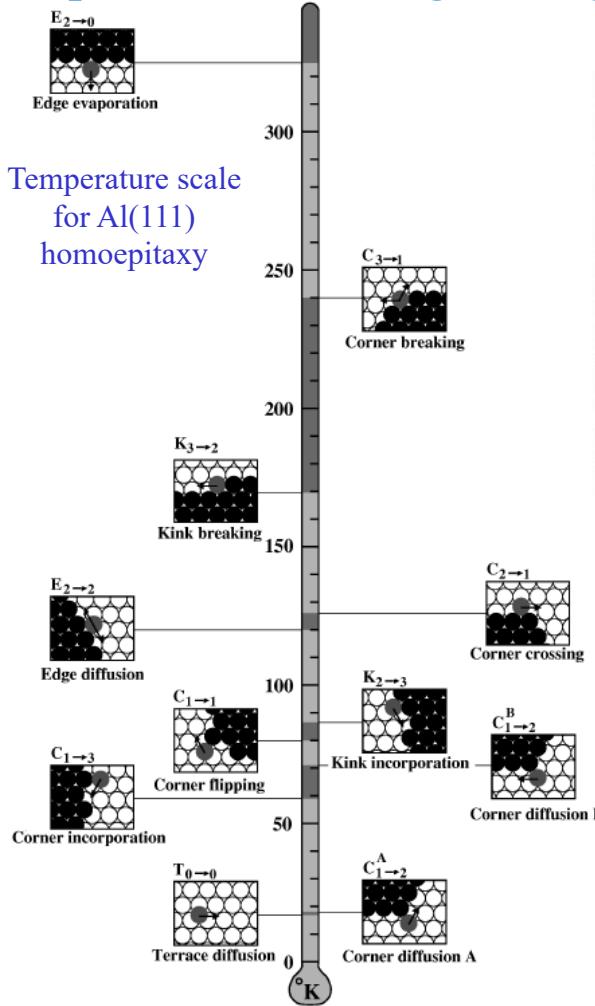
Arrhenius plot of saturation island densities (cov. = 0.2 ML) for the regime where dimers are stable nuclei.



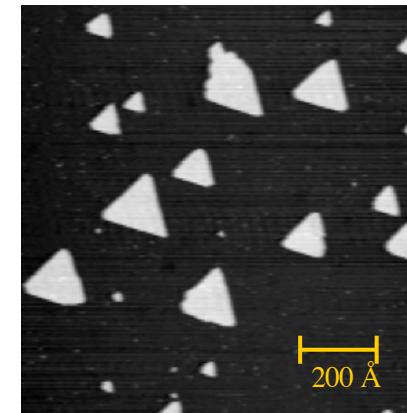
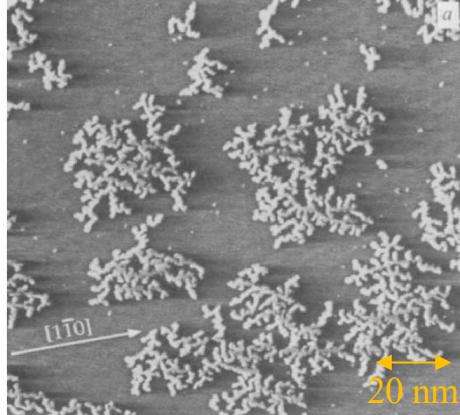
# Island shape: diffusion along the edges



H. Brune *et al.* *Nature* **369**, 469 (1994);  
 S. Ovesson *et al.* *Phys. Rev. Lett.* **83**, 2608 (1999);  
 A. Bogicevic *et al.* *81*, 637 (1998)



Ag/Pt(111) T=110K:  
 Adatom stick at the island edge and stop



Co/Pt(111) T=270K:  
 Activated adatom edge diffusion

20

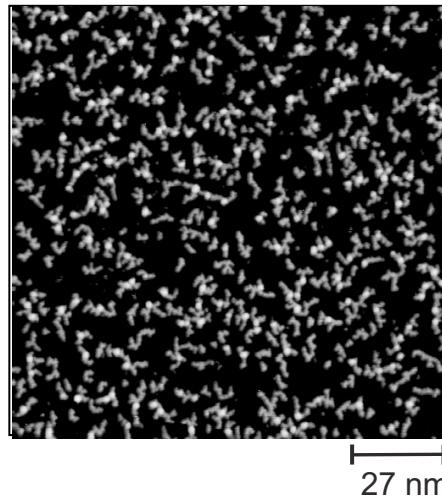
## Diffusion rate

Diffusion rate depends on the supporting substrate and on the deposited species

Fe



$$\nu = \nu_0 \exp(-E_{Fe}/k_B T)$$

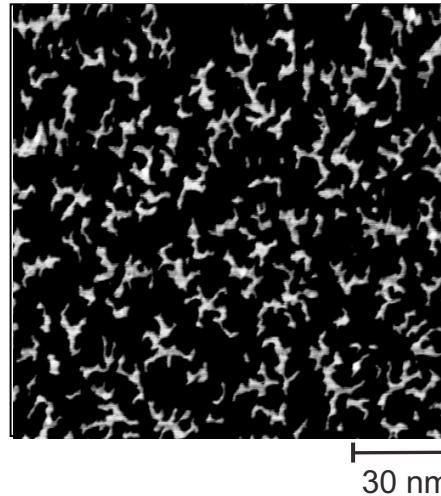


Island size = 90 atoms/isl

Co



$$\nu = \nu_0 \exp(-E_{Co}/k_B T)$$



Island size = 390 atoms/isl

$$T_{dep} = 140 \text{ K}$$
$$\Theta = 0.25 \text{ ML}$$

Substrate: Pt(111)

$$E_{Fe} > E_{Co}$$

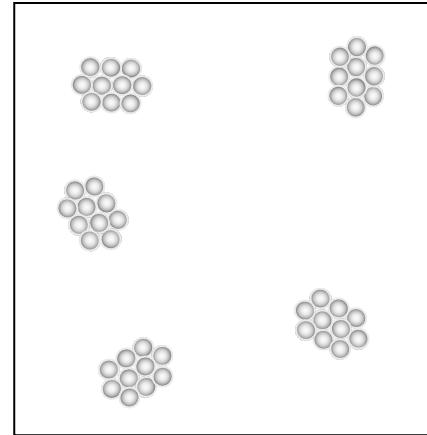
How to form alloy clusters?  
How to form lattices?



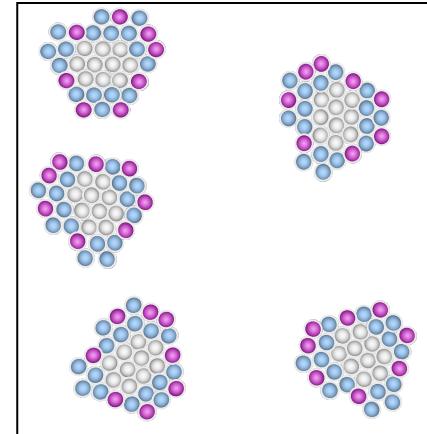
Patterned substrate

# Epitaxial growth of two-dimensional alloys

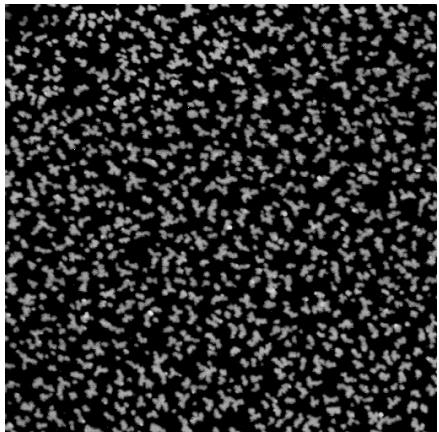
Pre-defined nucleation sites  
(seeds) to define the island  
density: template



Growth of the alloyed nanostructures  
on the template substrate



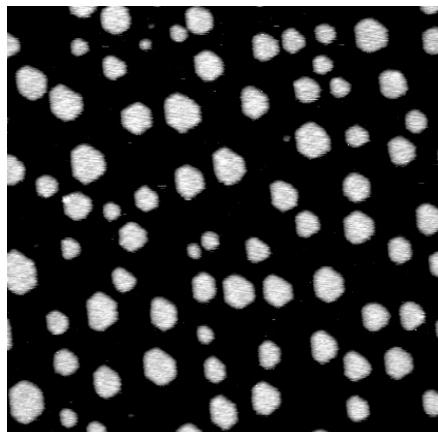
# Epitaxial growth of two-dimensional alloys



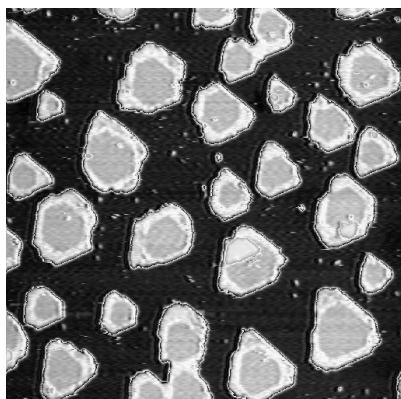
Pt  
 $T_{dep} = 200\text{K}$   
 $\Theta = 0.2 \text{ ML}$



Annealing  
to 800 K



10 nm

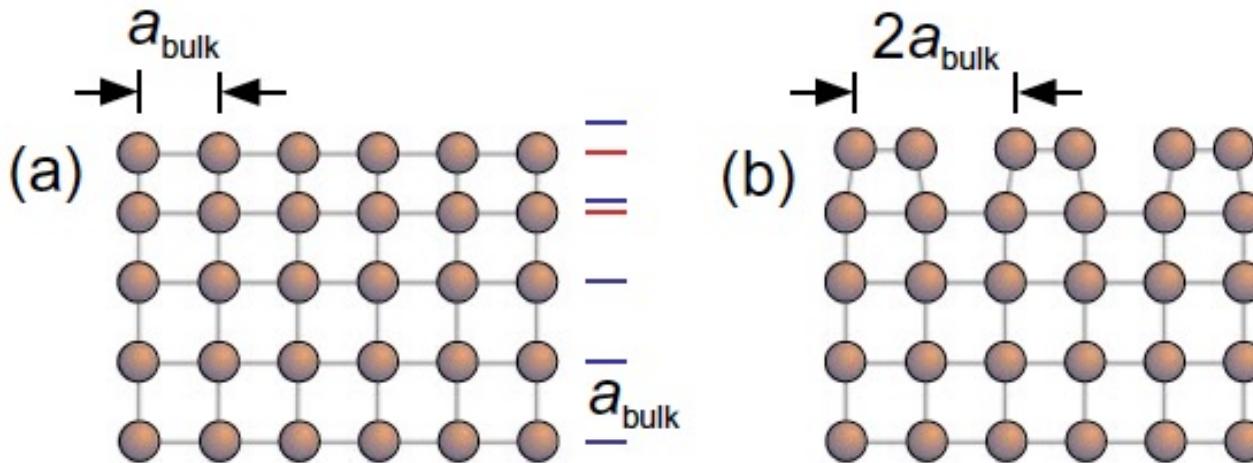


30 nm

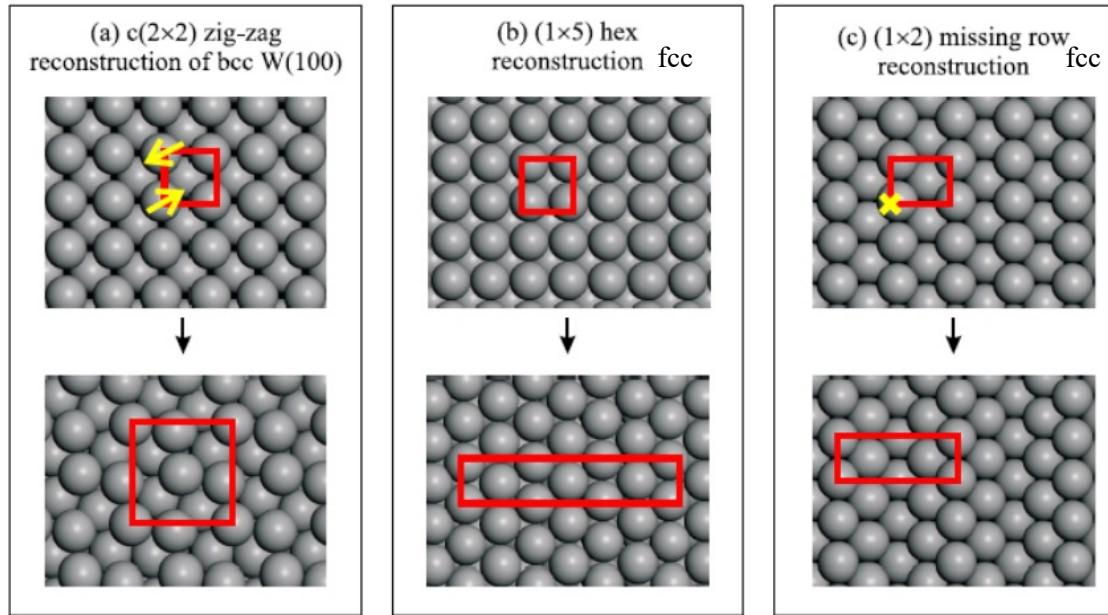
$\text{Co}_x\text{Fe}_{1-x}$  decoration  
 $T_{dep} = 250\text{K}$   
 $\Theta = 0.2 \text{ ML}$



## Surface relaxation and surface reconstruction



# Surface reconstructions



**Figure 5.5.** - Illustration of three bulk truncated surfaces and typical types of reconstruction that they undergo. (a) depicts the  $(1 \times 1)$  to  $c(2 \times 2)$  reconstruction of bcc W(100). The arrows indicate the direction in which the top layer W atoms move upon reconstruction. (b) displays an example of the “hex” reconstruction that the late 5d (fcc) transition metals undergo. The specific example is the  $(1 \times 1)$  to  $(1 \times 5)$  reconstruction of fcc Ir(100). (c) displays the  $(1 \times 1)$  to  $(1 \times 2)$  “missing row” reconstruction that occurs on the  $(110)$  surfaces of the late 5d (fcc) transition metals. The rows of atoms removed by the reconstruction are indicated by the  $\times$  at the edge of the unit cell.

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PhD Thesis 2015,  
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# Au(111): herringbone reconstruction

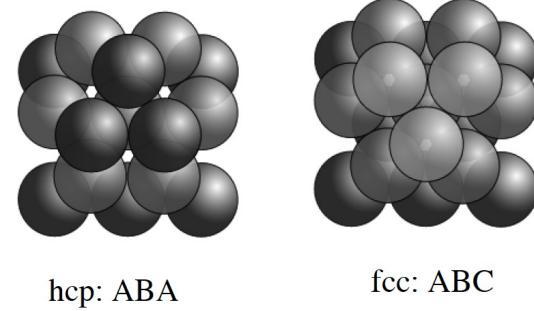
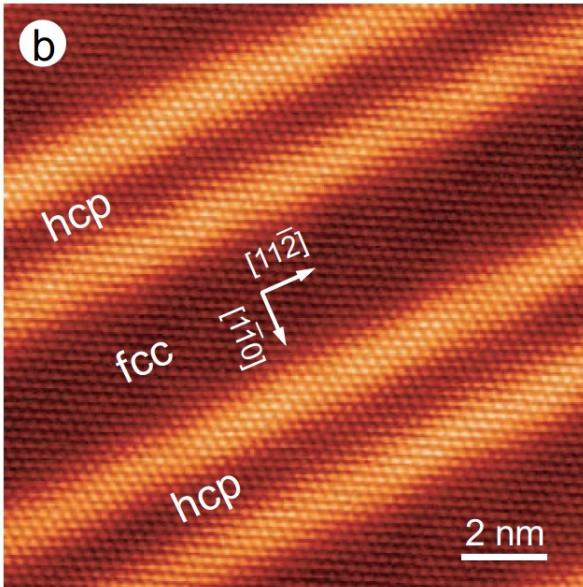
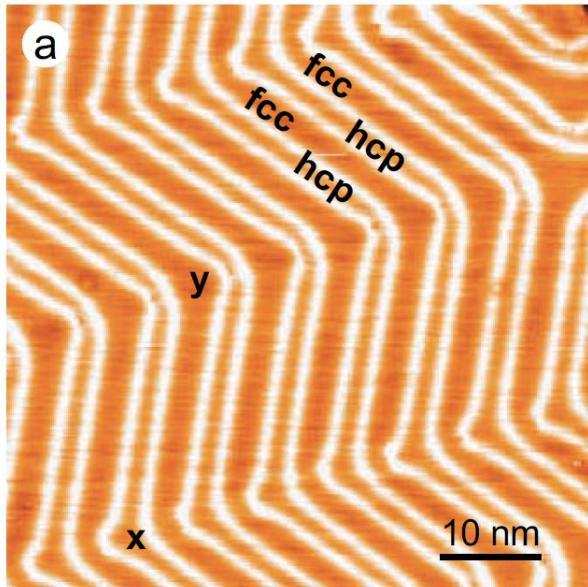
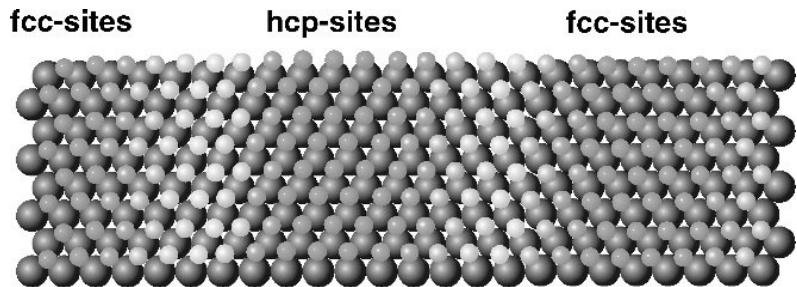
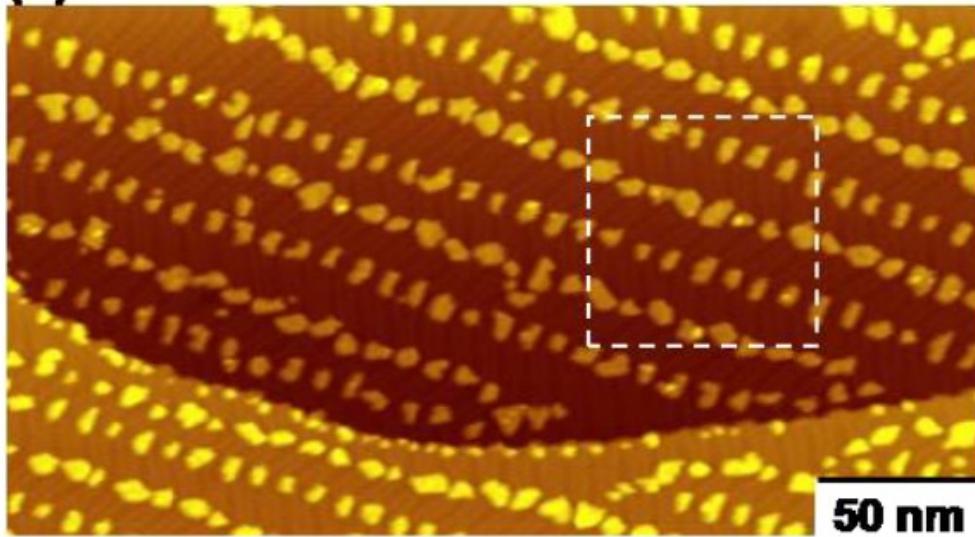


Figure 3.1: STM image showing the herringbone reconstructed Au(111) surface. a) Alternating fcc and hcp stacking domains, as well as x- and y-type elbows are visible. b) Atomically resolved STM image, revealing the slightly distorted hexagonal arrangement of the surface atoms together with the domain walls separating fcc and hcp stacking. The interatomic distances along  $[11\bar{2}]$  and  $[1\bar{1}0]$  are 2.88 Å and  $\approx 2.75$  Å, respectively. (Tunneling parameters: a)  $V = -0.7$  V,  $I = 0.2$  nA; b)  $V = -0.02$  V,  $I = 1.3$  nA)



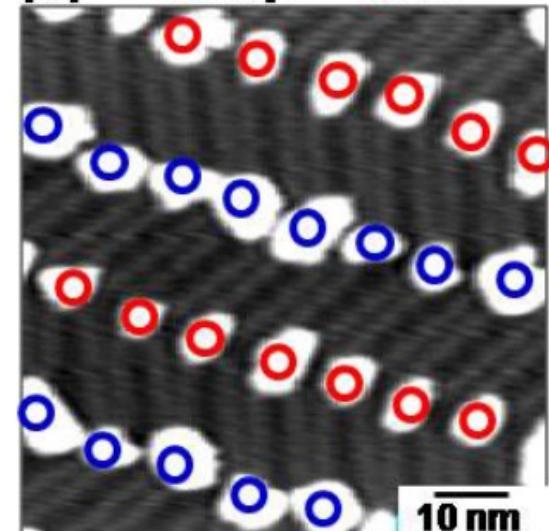
# Au(111) herringbone reconstruction - Nucleation

**(a) 250 K - 0.18 ML**

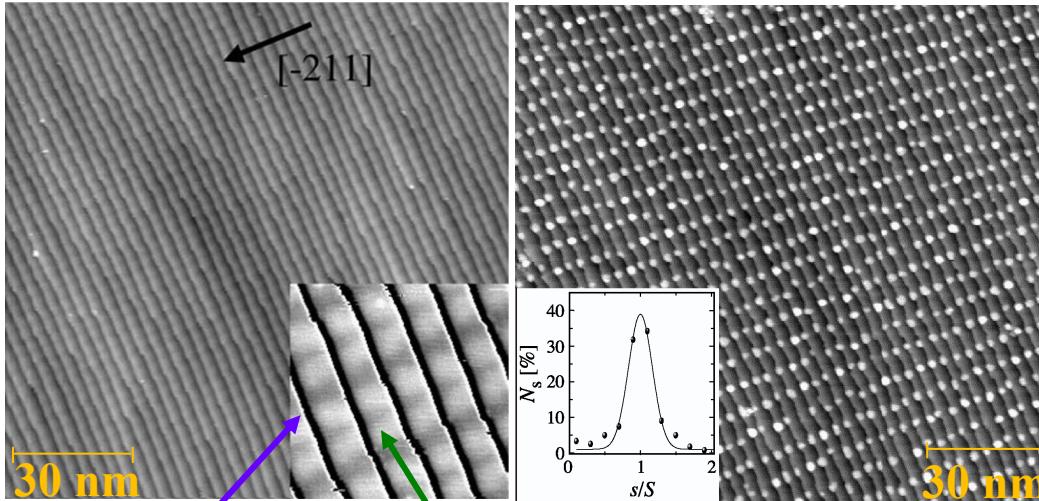


0.18 ML Fe grown at 250 K  
islands nucleate at elbows

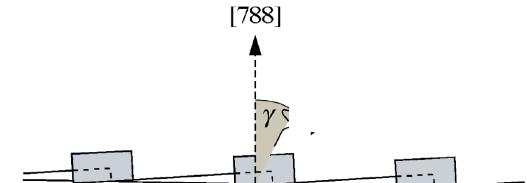
**(b)** ○ hcp ○ fcc



# Vicinal Au surfaces: Au(7,8,8)

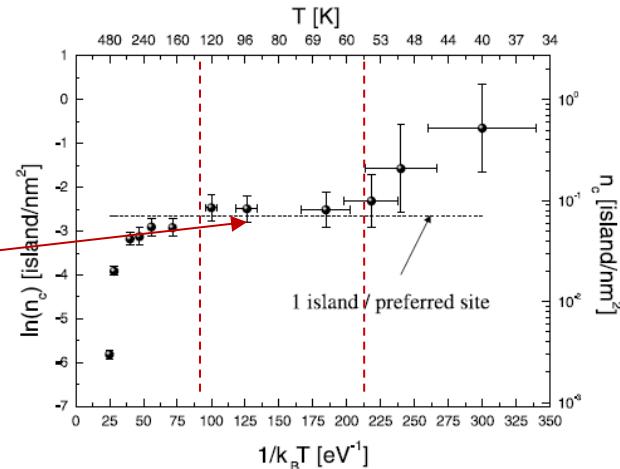


0.2 ML Co  
 $T_{\text{dep}} = 130 \text{ K}$   
 $T_{\text{ann}} = 400 \text{ K}$



the step edges and the terrace reconstruction lines  
 confine the Co adatoms

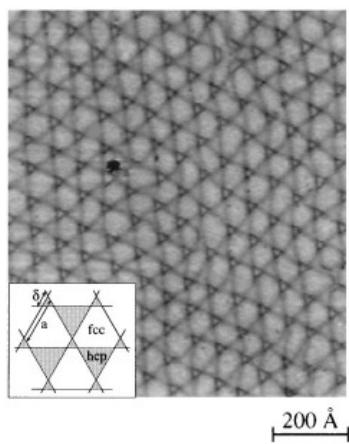
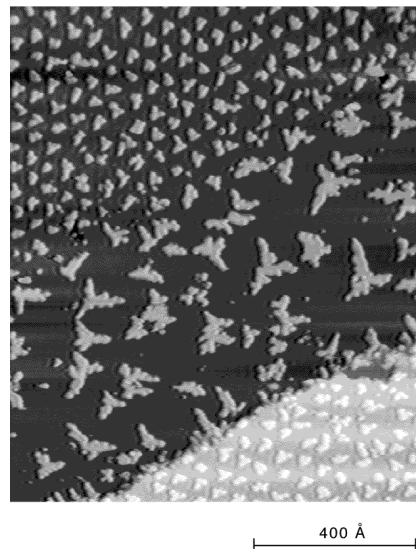
range of T where the island density ( $n_x$ ) does not change



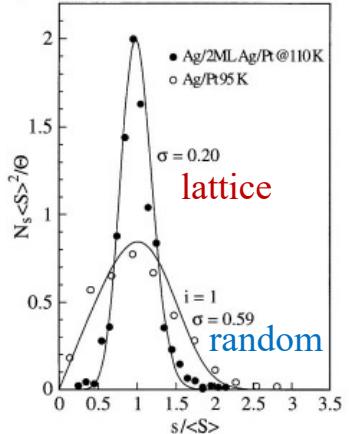
S. Rohart *et al.* Surf. Sci. **559**, 47 (2004);  
 N. Weiss *et al.* Phys. Rev. Lett. **95**, 157204 (2005)

# Self assembled nanostructure arrays on patterned substrate

Nucleation of an Ag island superlattice ( $T_{\text{dep}} = 110 \text{ K}$ ) on the dislocation network formed by 2 ML of Ag on Pt(111)



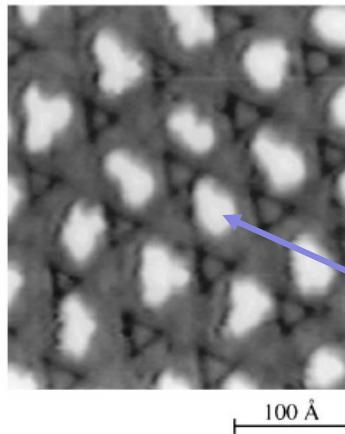
## c) Size distribution



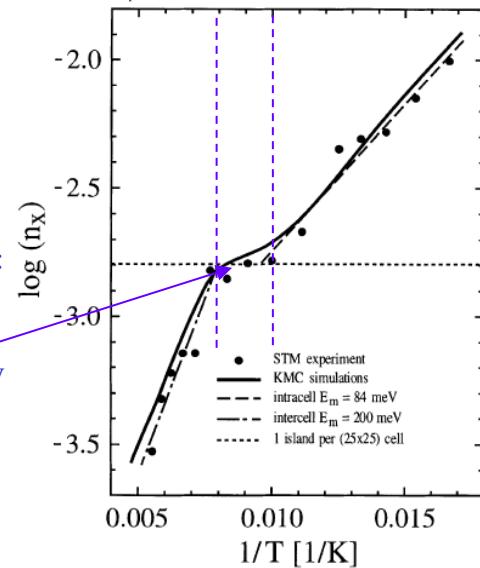
Almost monodispersed size distribution thanks to the template effect of the dislocation network



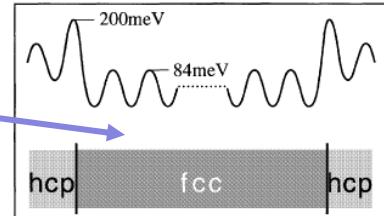
d)



Confinement: range of T where the island density ( $n_x$ ) does not change



c)

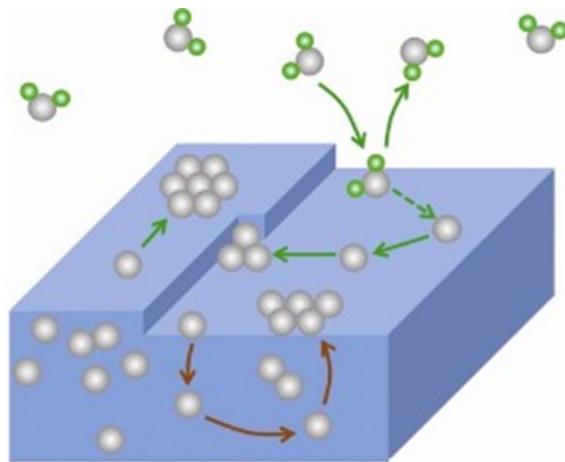


Atoms are confined in the fcc stacking areas

# Self assembled nanostructures on graphene

## Graphene growth by CVD (chemical vapor deposition)

hydrocarbon flux



- Hydrogen
- Carbon

Hydrocarbon molecules dissociate on the hot surface: H atoms leave the surface while C atoms organize in the honeycomb network of graphene

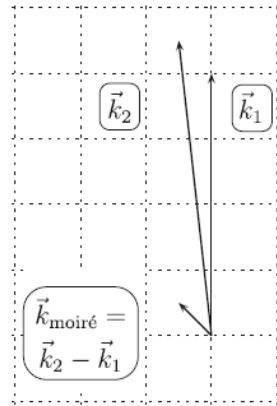
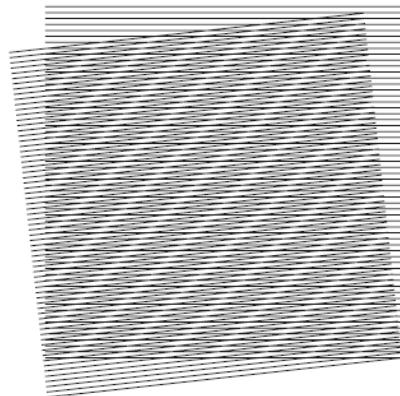
Ex of hydrocarbons:

$\text{CH}_2$  → Methylene  
 $\text{C}_2\text{H}_4$  → Ethylene

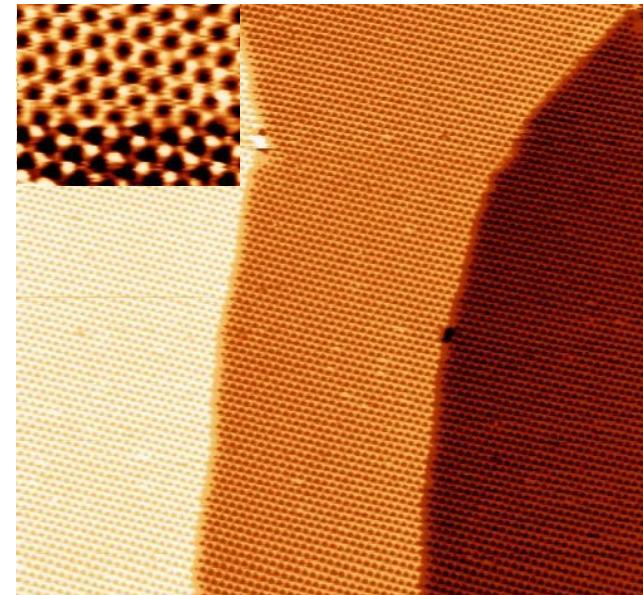
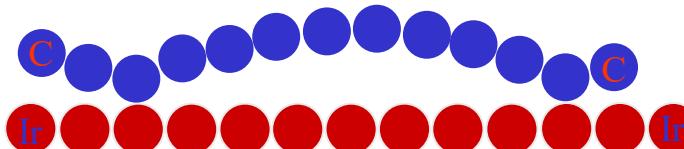
Note: C atoms dissolved in the bulk segregate to the sample surface and also contribute to form graphene

# Moiré pattern due to graphene-Ir(111) lattice mismatch

A moiré is a superposition of two lattices generating a third one.



$$a_{\text{Ir}} = 0.27 \text{ nm}$$
$$a_c = 0.245 \text{ nm}$$

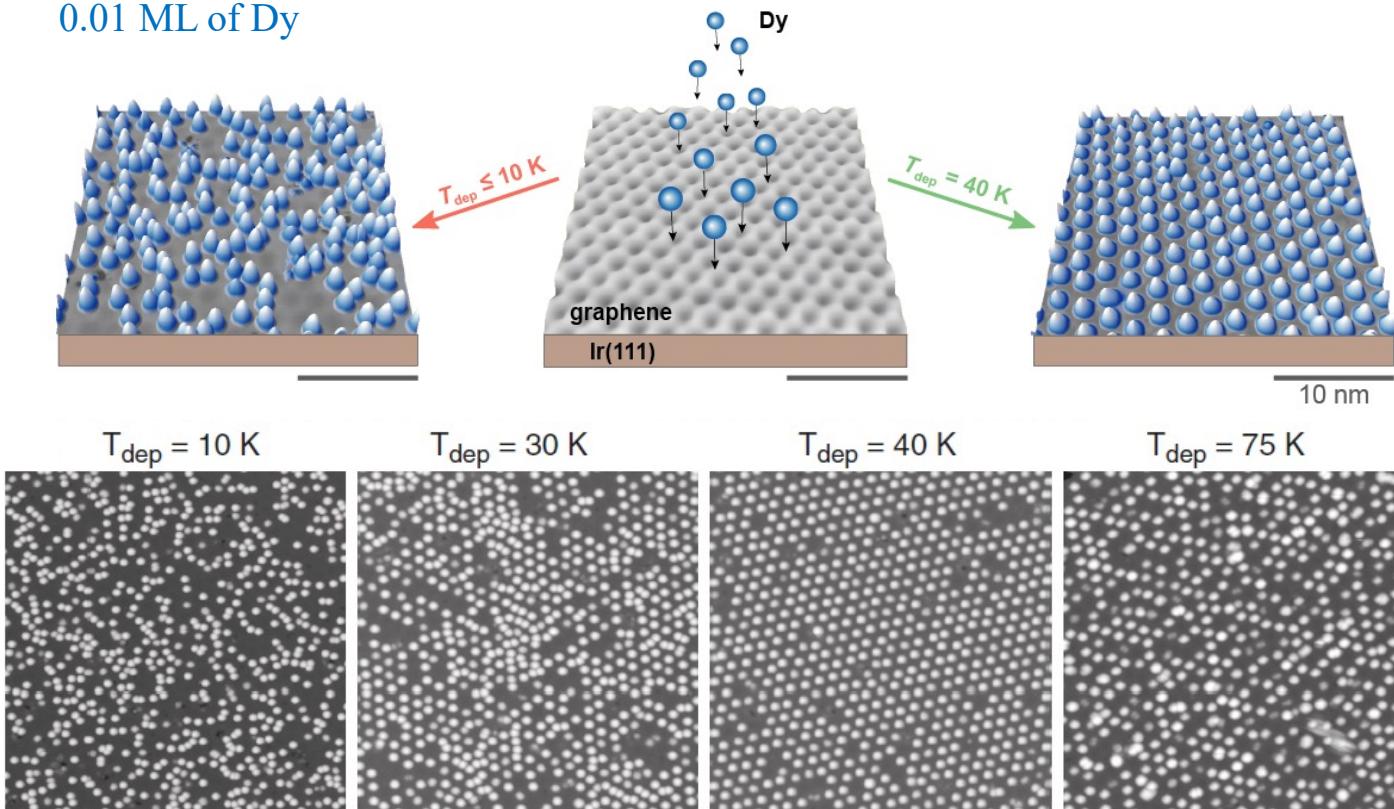


180 x 200 nm<sup>2</sup>

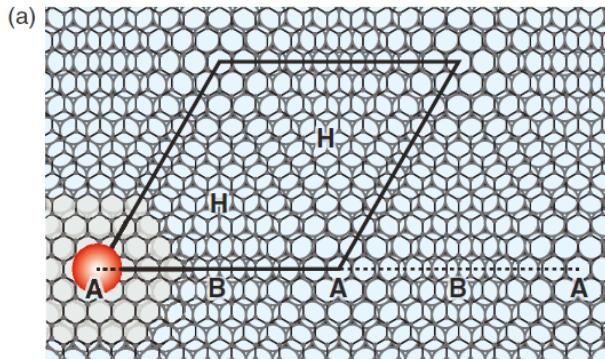
# Superlattice of single atom magnets on graphene

Dy atoms on graphene/Ir(111)

0.01 ML of Dy



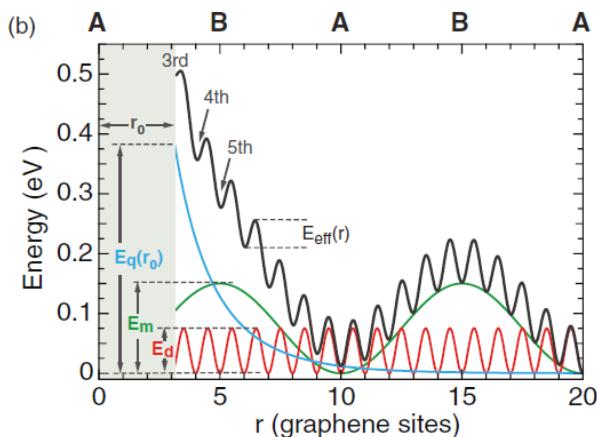
# Diffusion energy landscape



Moiré with  $(10 \times 10)$  graphene unit cells on  $(9 \times 9)$  Ir(111) atoms.

Stacking areas: (A) atop, (B) bridge, and (H) hollow.

Rare-earth atom (red) together with its direct impingement area (gray).



1D diffusion energy profile for a second rare-earth atom resulting from the superposition of:

- 1) atomic corrugation  $E_d$
- 2) moiré corrugation  $E_m$  of graphene
- 3) Coulomb repulsion  $E_q$

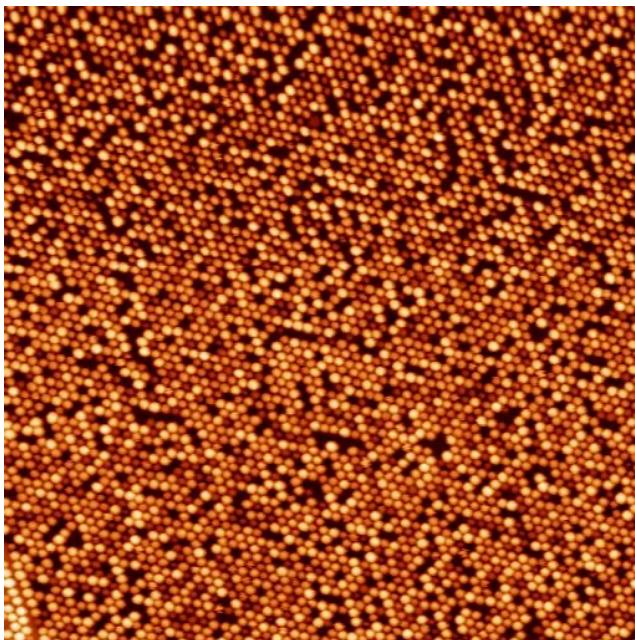
$$E_q(r) = \frac{1}{4\pi\epsilon_0} \frac{q^2}{r} \exp\left(-\frac{r}{r_0}\right)$$

$q$  is the charge transferred from the rare-earth to graphene

# Self assembled core-shell nanostructure arrays on graphene/Ir(111)

**Ir island**

Ir deposition: T=375 K



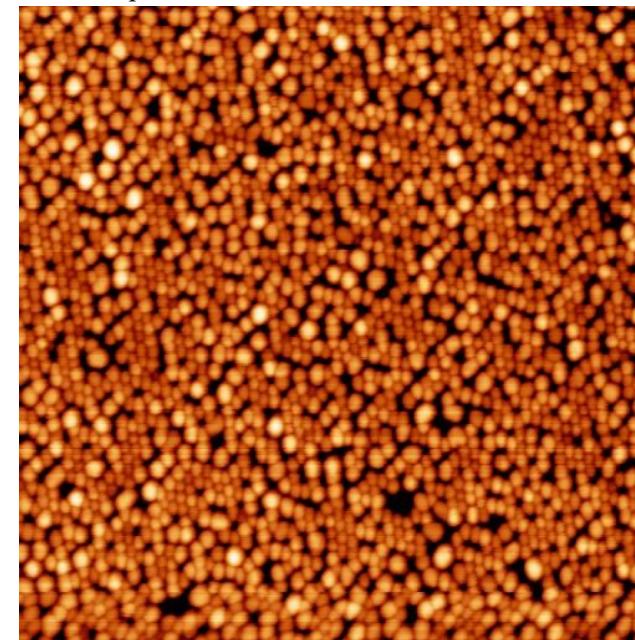
graphene



**Ir-core Co-shell islands**

Ir deposition: T=375 K

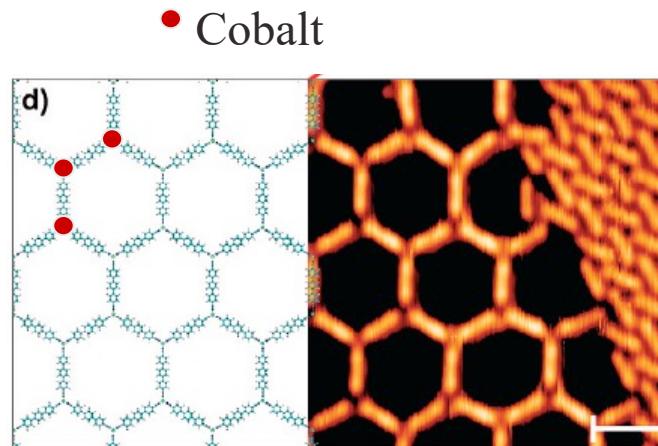
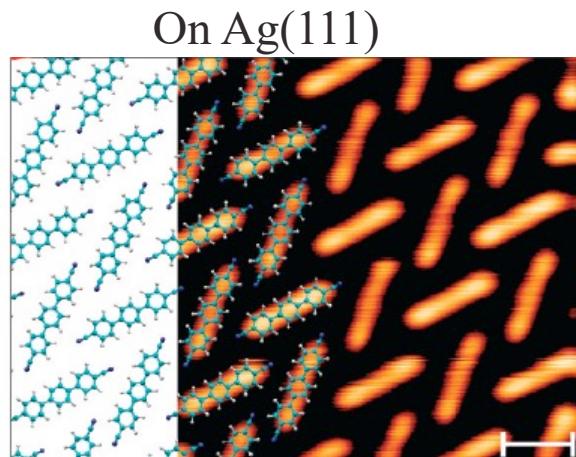
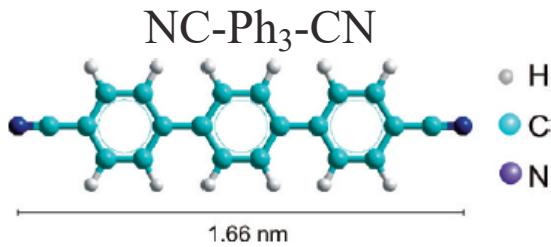
Co deposition: 1 ML, T=300 K



**Ir-core  
Co-shell**



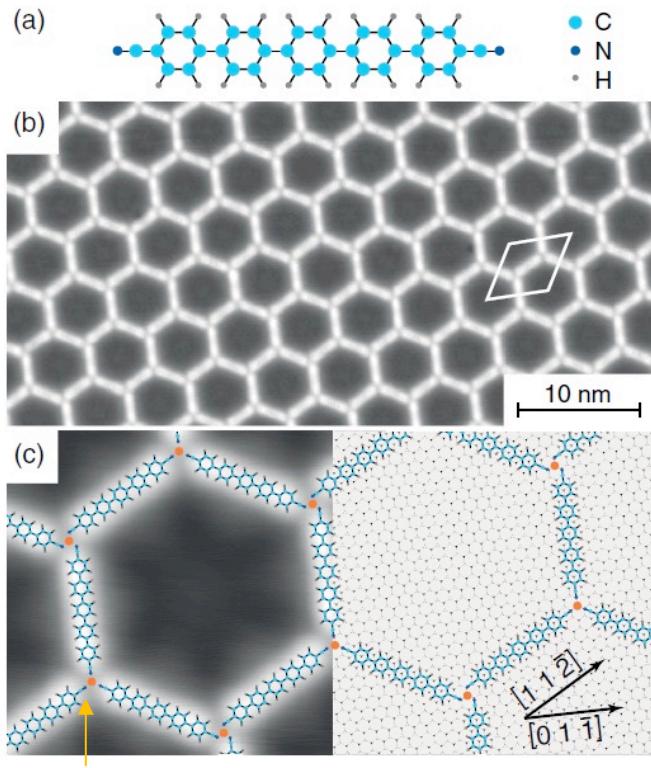
# Molecular and metal-organic networks



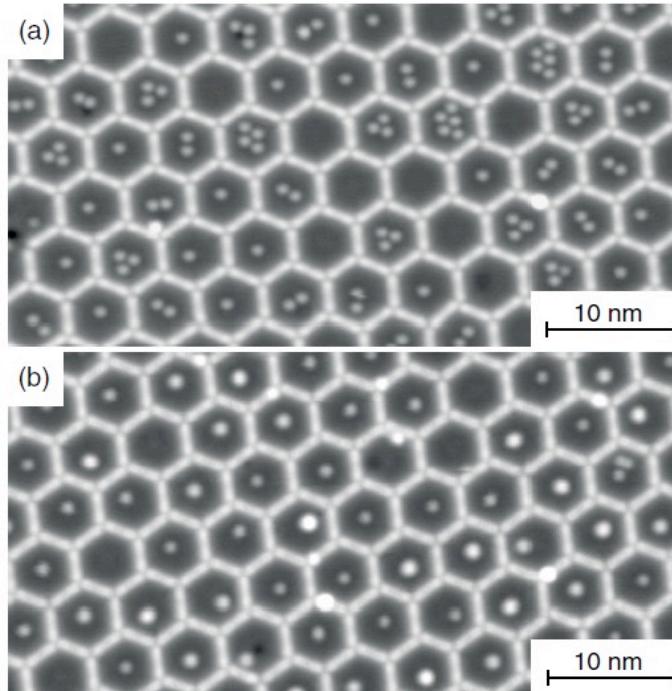
Co atoms added at room temperature coordinate the molecules in a 3-fold coordinated motif

# Cluster superlattice in a metal-organic quantum box network

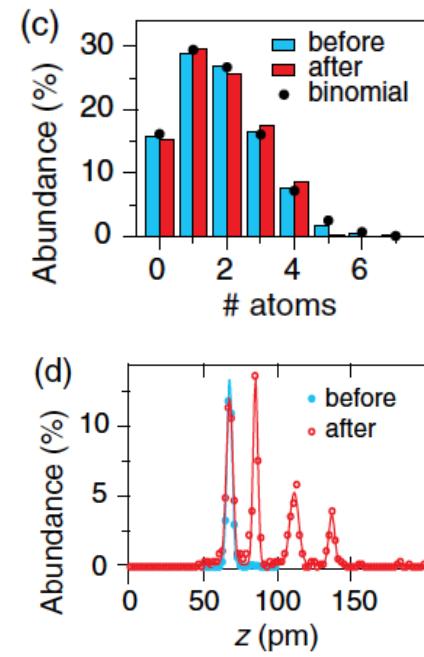
Metal organic quantum box network on Cu(111)



a) Fe deposition at  $T = 10\text{K}$



b) cluster formation after annealing to  $T_{\text{ann}} = 18\text{K}$



## Superlattices: density vs blocking T

System	density	$T_b$
Co/Au(11,12,12)	$15 \text{ T}_{\text{dot}}/\text{in}^2$	75 K
Fe/Co/Au(11,12,12)	$15 \text{ T}_{\text{dot}}/\text{in}^2$	105 K
Co/Au(788)	$26 \text{ T}_{\text{dot}}/\text{in}^2$	50 K
Co/GdAu <sub>2</sub> /Au(111)	$52 \text{ T}_{\text{dot}}/\text{in}^2$	< 90 K
Fe/NC-Ph <sub>3</sub> -CN/Cu(111)	$90 \text{ T}_{\text{dot}}/\text{in}^2$	?
Fe/Al <sub>2</sub> O <sub>3</sub> /Ni <sub>3</sub> Al(111)	$92 \text{ T}_{\text{dot}}/\text{in}^2$	?
Co/Ir/graphene/Ir(111)	$116 \text{ T}_{\text{dot}}/\text{in}^2$	< 50 K