

## Problem set 10

### Problem 1

- Determine the value of  $\Lambda_{\text{QCD}}$  for three fermions ( $N_f = 3$ ), knowing that the strong coupling constant has been measured at the  $Z^0$  mass:  $\alpha_s(M_Z) = 0.12$ .
- Compute the strong potential energy (binding energy) for the mesons  $\phi$  ( $s\bar{s}$ ),  $J/\Psi$  ( $c\bar{c}$ ) and  $\Upsilon(1S)$  ( $b\bar{b}$ ), for which  $m_\phi = 1020 \text{ MeV}$ ,  $m_{J/\Psi} = 3100 \text{ MeV}$ , and  $m_\Upsilon = 9500 \text{ MeV}$ . Assume the typical radius of the meson to be of order 1 fm.

### Problem 2

Show that the number of degrees of freedom for

- all the quarks and gluons is 79.
- all the particles of the standard model (quarks, leptons, gauge bosons, Higgs boson) is 106.75.