

Phys-301

Biophysics: Physics of the Cell

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exercises (problems)



journal articles

Overall course goals

- Understand the **organization of the cell** and its components
- Examine **universal** features/processes of cells
- Model features/processes using **physical concepts**

Note: This course is taken by students from PH, SV, GM ...

Biophysics overview

Key physical concepts behind most biophysical models:

1. Simple numerical estimates
2. Elasticity theory (1D, 2D, 3D)
3. Statistical mechanics models
4. Diffusion and random walks
5. Circuit/network theory
6. Fluid mechanics (Newtonian, Navier-Stokes) (BA5, Ramirez-San Juan)
7. Information theory, dynamical systems (MA1/3, PHYS-302, Rahi)
8. Biopolymers (MA2, PHYS-441, De Los Rios)
9. Charges in solution (Poisson-Boltzmann)
10. Rate equation models of chemical kinetics

Course content

Topics (lectures):

1. **Introduction to the cell** (1-3)
2. **Biological membranes** (4-5)
3. **Proteins** (6-7)
4. **Dynamics** (8-9)
5. **Genomes** (10-13)

Course components:

1. **Introduction to systems and concepts**
2. **Description of observations and measurements**
3. **Estimates of relevant numbers / development of quantitative models**
4. **Analysis of research articles**

Why is the course designed this way?

Introduce fundamental topics in cellular biophysics

Develop skills in model building

Practice reading to find information, provide context

Consider uncertainties of unsolved problems

Course structure

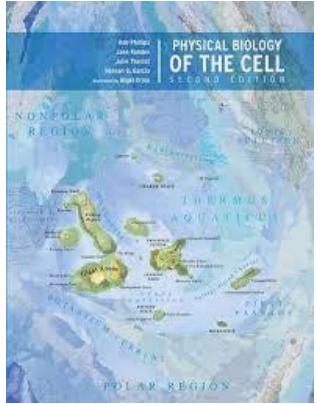
- One lecture and one exercise session per week.
(C) Mon, 13:15-15:00 (SM).
(E) Mon, 15:15-16:00 (SR or NM)
- Your role:
Read weekly before the course from PBOC (~1-2 hours)
Attempt the exercises/article before the exercises (~1-2 hours)
- Lectures will introduce and develop topics
- Exercises: problem solving or analyzing journal articles
- Written final exam

Resources:

- Moodle
- Lecture slides (TAKE NOTES)
- Bionumbers website <https://bionumbers.hms.harvard.edu/search.aspx>
- Physical Biology of the Cell by Rob Phillips, Jane Kondev and Julie Theriot.
- Selected journal articles

Your roles

1. Before class: read PBoC, glossary, attempt weekly assignment



Exercise set 1

1. A feeling for the numbers: molecular

a) Estimate the mass of a typical α -helix, explaining how many of each type of their key amino acids: glycine, proline, arginine

b) On the basis of your result for part (a), mass of a protein (reported in kDa) based thumb to myosin II and G-actin and compare these properties with the following table: <http://www.ncbi.nlm.nih.gov/entrez/query.fcgi?db=Protein>

c) Estimate the size of the same proteins: proteins $R_d = 0.395 \pi N^2 / 7.257$ [1], where radius of gyration in Angstrom (the root in from the square of the center of mass). Relate between mass and R_d .

[1] Narang et al. Phys. Chem. Chem. Phys.

2. Areas, volumes and diffusion in orga

a) Estimate the area of the ER (endoplasmic ER) form. Use a model for its structure of 1a, and estimated values for α and d base (scale bar = 1 μ m).



A quantitative model for low-energy intermediates

Peter J. Kasten*, Joshua Zimmerberg*, Yael A. Chinnaiyan

Princeton Institute of Molecular Medicine, Princeton, NJ 08543, Department of Molecular Biology, Princeton University, Princeton, NJ 08544, Department of Chemistry, Princeton University, Princeton, NJ 08544, Department of Molecular Biology, Princeton University, Princeton, NJ 08544

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2. During lecture: take notes, do in-class exercises

Biophysics: MEMBRANES

① Self-Assembly & Hydrophobic effect

Spontaneous organization

We say that "Living things tend to be complex and highly organized" (def. life). However, this is also true for some non-living systems! For instance, **BIOLOGICAL MEMBRANES** self-assemble with a little bit of energy.

- made of small (< 1 kDa) amphiphilic molecules called lipids
- self-assemble into vesicles

Spontaneous Organization

cell mass = $1 \text{ pg} = 10^{-12} \text{ g}$

protein mass $\approx 1.5 \times 10^{-12} \text{ g}$

in cytoplasm $\approx 10^{-13} \text{ g}$

in membrane $\approx 5 \times 10^{-19} \text{ g}$

mean protein size = 300 amino acids

mean amino acid mass = 100 Da

$1 \text{ Da} = 1.6 \times 10^{-24} \text{ g}$

Number of proteins in cell?

$$\frac{\text{mass of protein}}{\text{mass of one protein}} = \frac{1.5 \times 10^{-12} \text{ g}}{300 \text{ amino acids}} = \frac{1.5 \times 10^{-13} \text{ g}}{300 \times 100 \text{ Da}} = \frac{1.6 \times 10^{-24} \text{ g}}{300 \times 100 \text{ Da}} = 5 \times 10^{-20} \text{ proteins}$$
$$\approx 3 \times 10^6 \text{ proteins}$$

3. After lecture: participate in exercise session, complete weekly assignment, compare with posted solutions (Wednesday each week)

Lecture 1 outline

Today's goal: Introductions

- Physical biology of the cell
- The stuff of life
- Model building in biology
- Quantitative models and the power of idealization

atoms / molecules
electrical / mechanical

philosophy / approach
components : biomolecules
physical models for different examples
components

PBOC Chapter 1

Physical biology of the cell

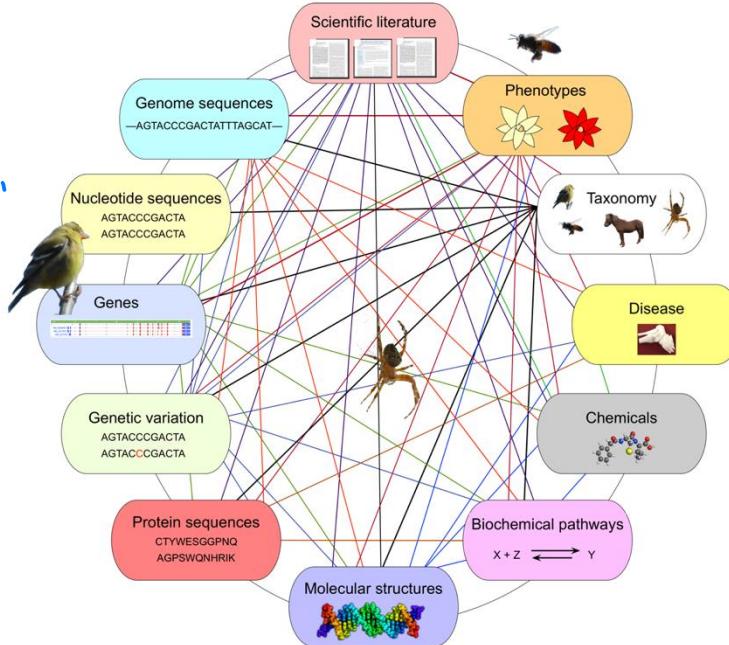
... all observation must be for or against some view if it is to be of any service!

Darwin

lots of data!

lists of constituents: "ome"

- genome (genetic sequences)
- proteome (proteins)
- biome (organisms)



Good models overlook some of the details, while keeping enough to make useful predictions.

The stuff of life

What is life?



- grow
- move
- reproduce
- consume energy
- die
- respond to stimuli

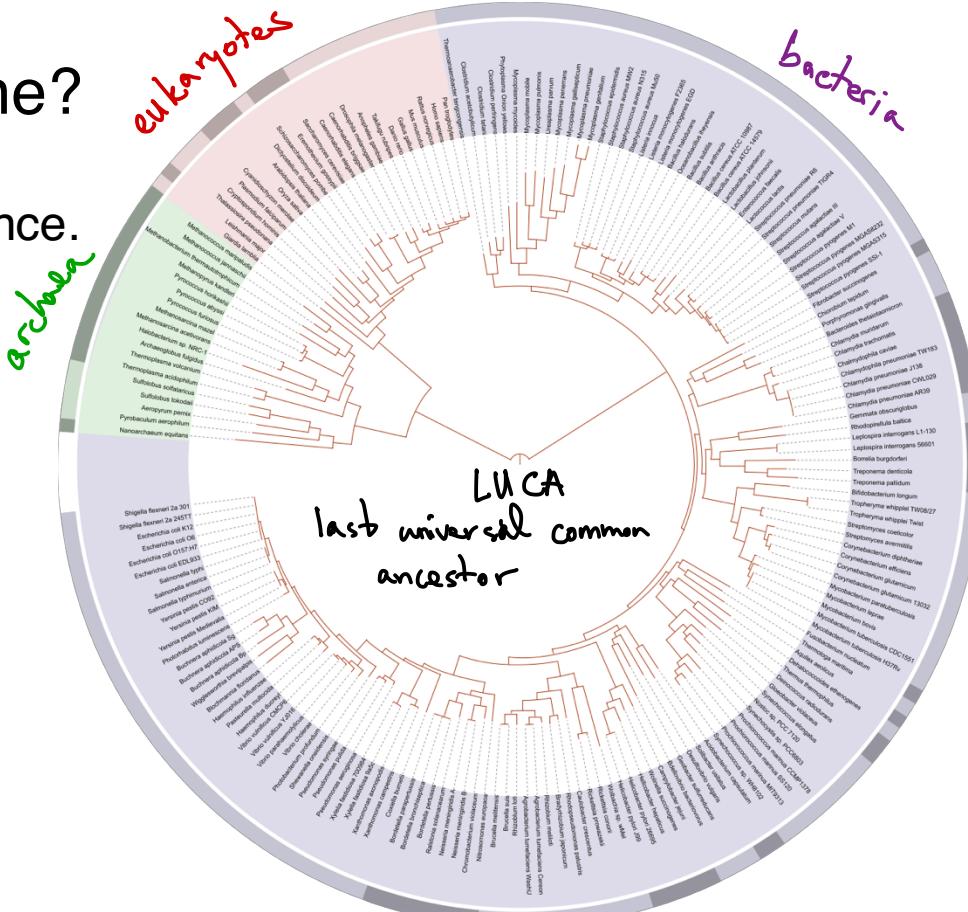
The stuff of life

Why is it so difficult to define?

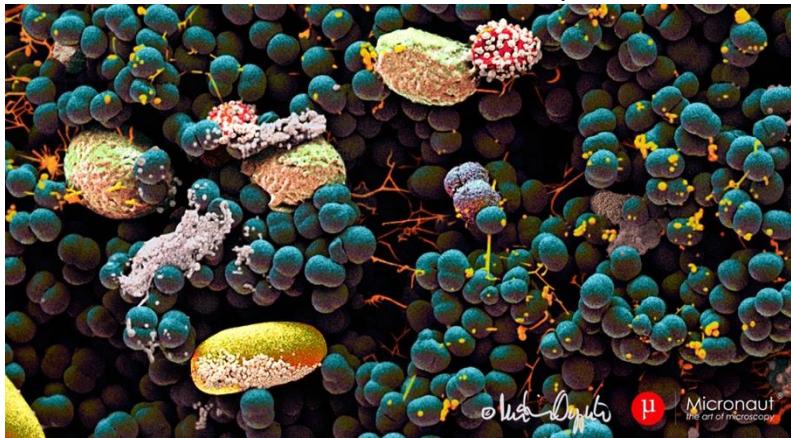
Life is a process, not a pure substance.
A great diversity of life exists.

phylogenetic classification: evolutionary
history, encoded in genes

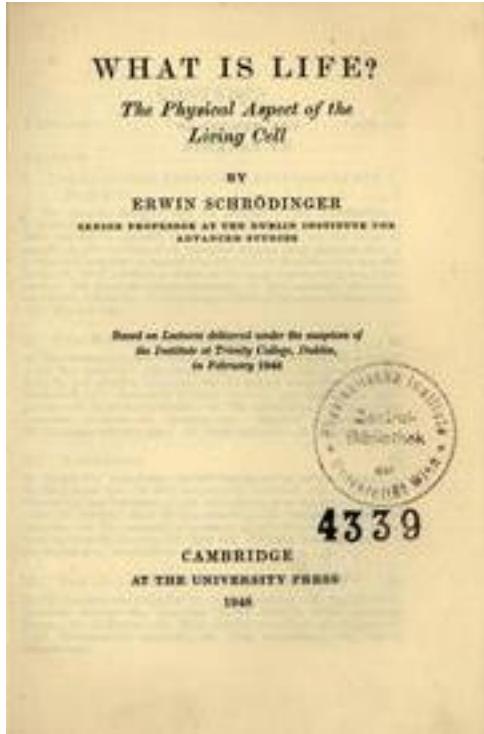
NASA: life is a self-sustaining
chemical system capable of
Darwinian evolution



LIFE ADAPTS/EVOLVES TO ENVIRONMENTAL NICHE



The stuff of life



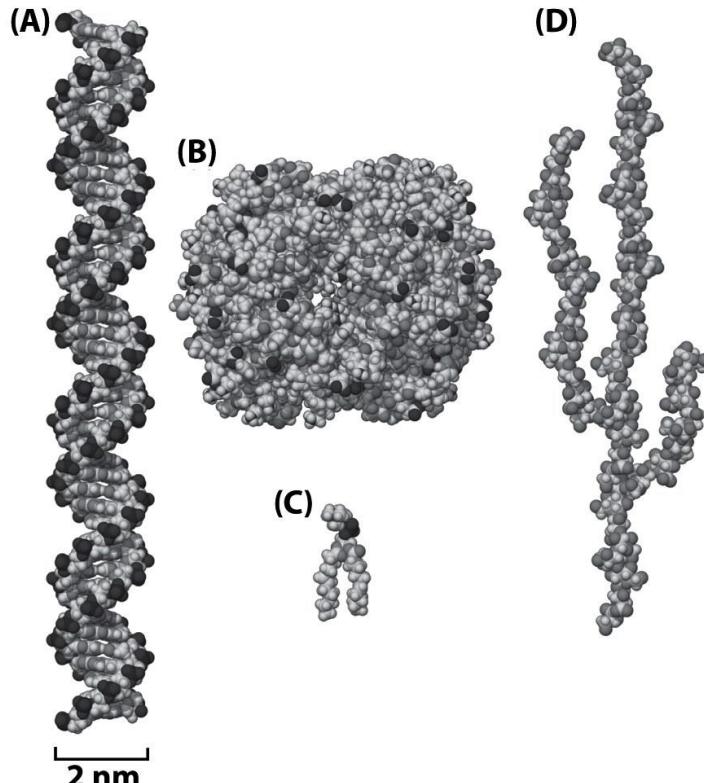
When is a piece of matter said to be alive? When it goes on "**doing something**," ... for a much longer period than we would expect an inanimate piece of matter to "keep going" under similar circumstances. When a system that is not alive is isolated or placed in a uniform environment, all motion usually comes to a standstill very soon as a result of various kinds of friction; differences of electric or chemical potential are equalized, substances which tend to form a chemical compound do so, temperature becomes uniform by heat conduction. After that the whole system fades away into a dead, inert lump of matter. A permanent state is reached, in which no observable events occur. *The physicist calls this the state of thermodynamical equilibrium, or of "maximum entropy."*

"What is life", 1944, Schrödinger

The stuff of life

What macromolecules are cells made of?

Four main
bio-macromolecules



Name the molecule
What are its parts?
What are its units?
What is it used for?

The stuff of life

What macromolecules are cells made of?

Name the molecule

lipid (phospholipid)

What are its parts?

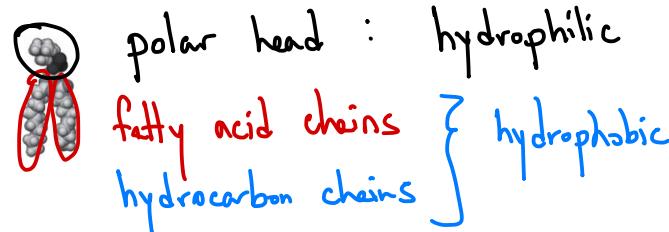
hydrophilic / hydrophobic

What are its units?

chain length, saturation of bonds in chains

What is it used for?

cell membrane, compartmentalize (cell, organelles)



The stuff of life

What macromolecules are cells made of?

(we aren't going to study this one)

Name the molecule

carbohydrate

What are its parts?

carbon, hydrogen, oxygen

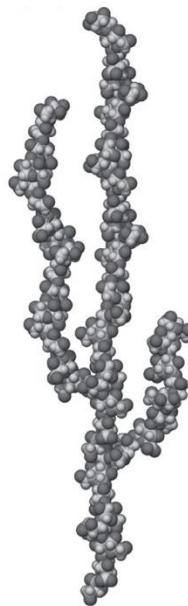
What are its units?

$(C_mH_{2m}O)_n$ chain length n

What is it used for?

energy storage, cell surface

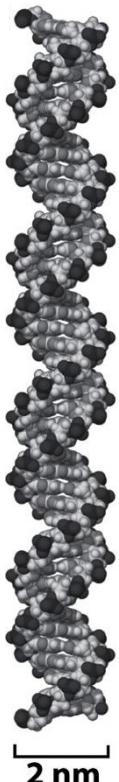
selectivity, cell walls



The stuff of life

What macromolecules are cells made of?

Name the molecule
What are its parts?
What are its units?
What is it used for?

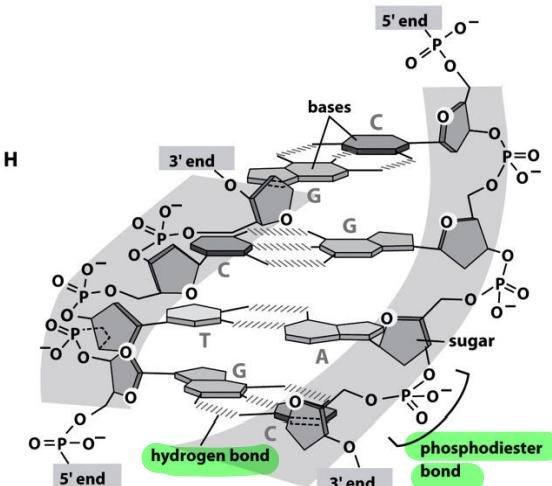
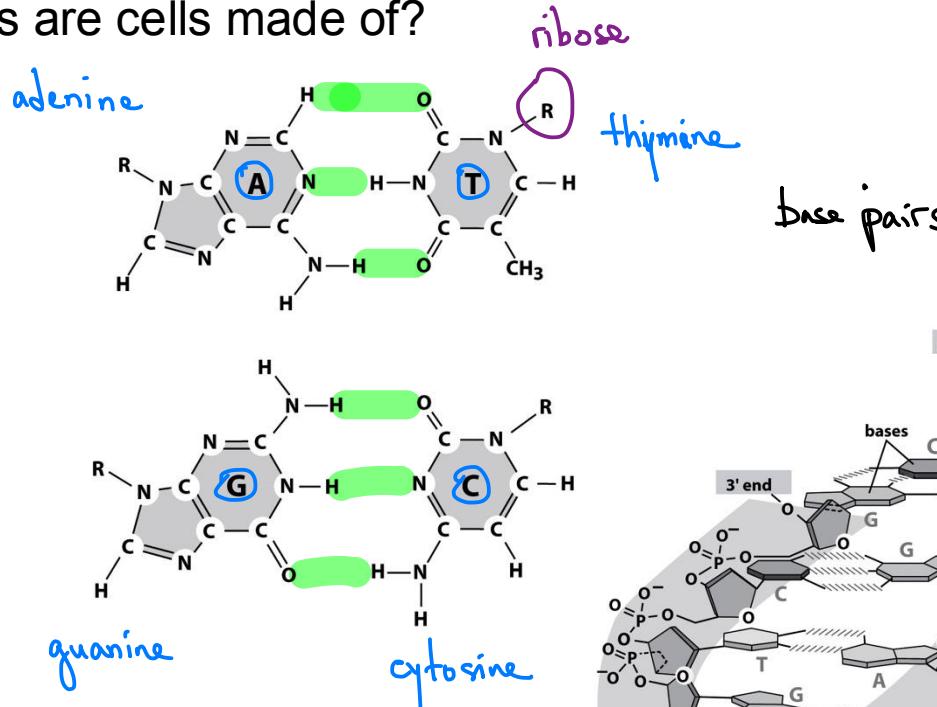
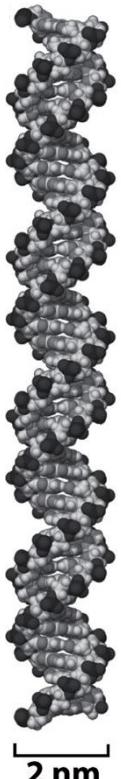


DNA
bases / nucleotides (A, T, G, C)
base pairs
encoding genetic information

The stuff of life

What macromolecules are cells made of?

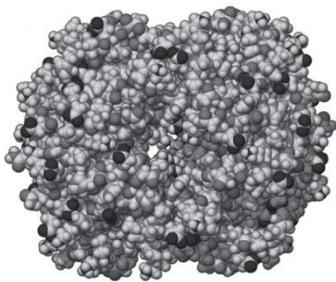
Name the molecule
What are its parts?
What are its units?
What is it used for?



The stuff of life

What macromolecules are cells made of?

Name the molecule
What are its parts?
What are its units?
What is it used for?



protein (hemoglobin)
amino acids
Daltons (unified atomic mass unit)
 $\frac{1}{12}$ mass of C_{12} atom
enzymes (catalyze processes) or
structural (mechanical properties)
bind ligands/ions (sensors, carriers)

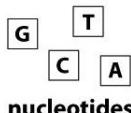
structural motifs: alpha helices, beta sheets

The stuff of life

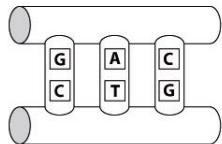
Nucleic acids and proteins are polymer languages

NUCLEIC ACIDS

four natural



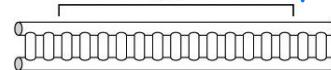
codon (3 bp)



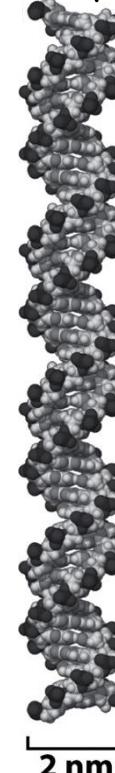
DNA is read as codons

string of codons, may encode a protein gene

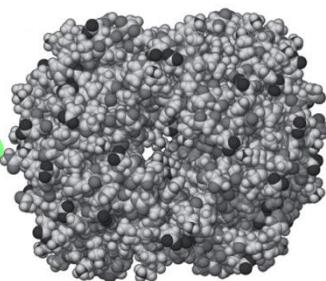
SENTENCES



DNA



protein



protein

ribosome
translation

DNA → mRNA

RNA polymerase
transcription

How many?

$$4^3 = 64$$

ALPHABET

structured
motifs

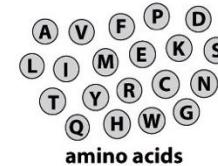
WORDS

folded
protein

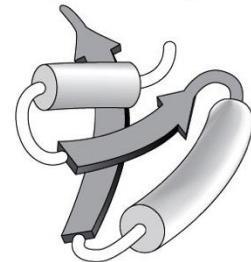
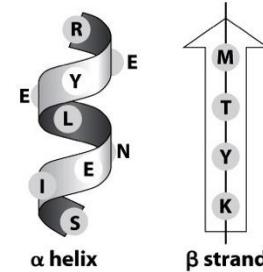
SENTENCES

codon → amino acid

PROTEINS



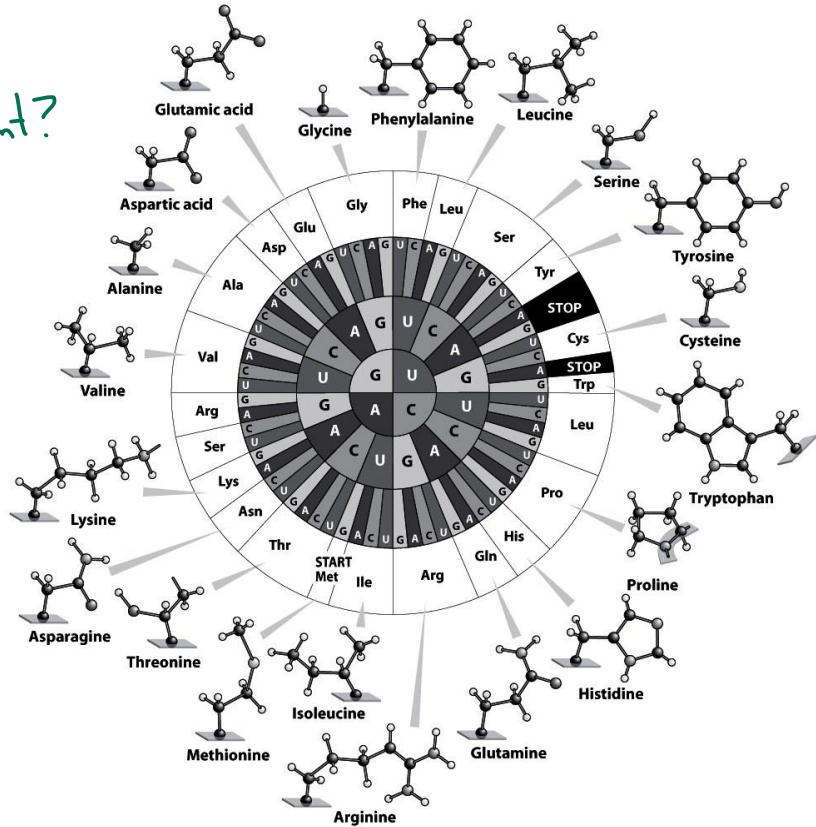
20 natural
amino acids



The stuff of life

What macromolecules are cells made of?

Why redundant?
Robustness

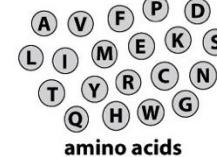


ALPHABET

WORDS

SENTENCES

PROTEINS

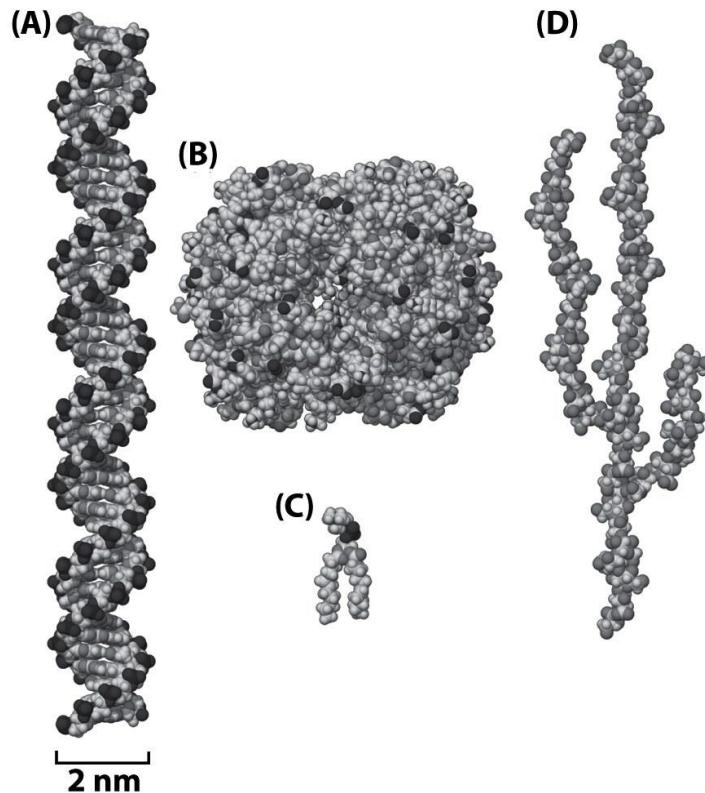


amino acids

The diagram illustrates the structure of a protein segment. On the left, an α helix is shown as a spiral ribbon with amino acid side chains (R, Y, L, E, S, I) protruding from the right side. On the right, a β strand is shown as a vertical line with side chains (M, T, Y, K) attached to it.

The stuff of life

What macromolecules are cells made of?



Advantages:

- Each class can be assembled by the cell from a small set of simpler subunits
- Combinatorial assembly gives rise to diversity
- Limited repertoire of chemical reactions needed
- Facilitates existence of food chain

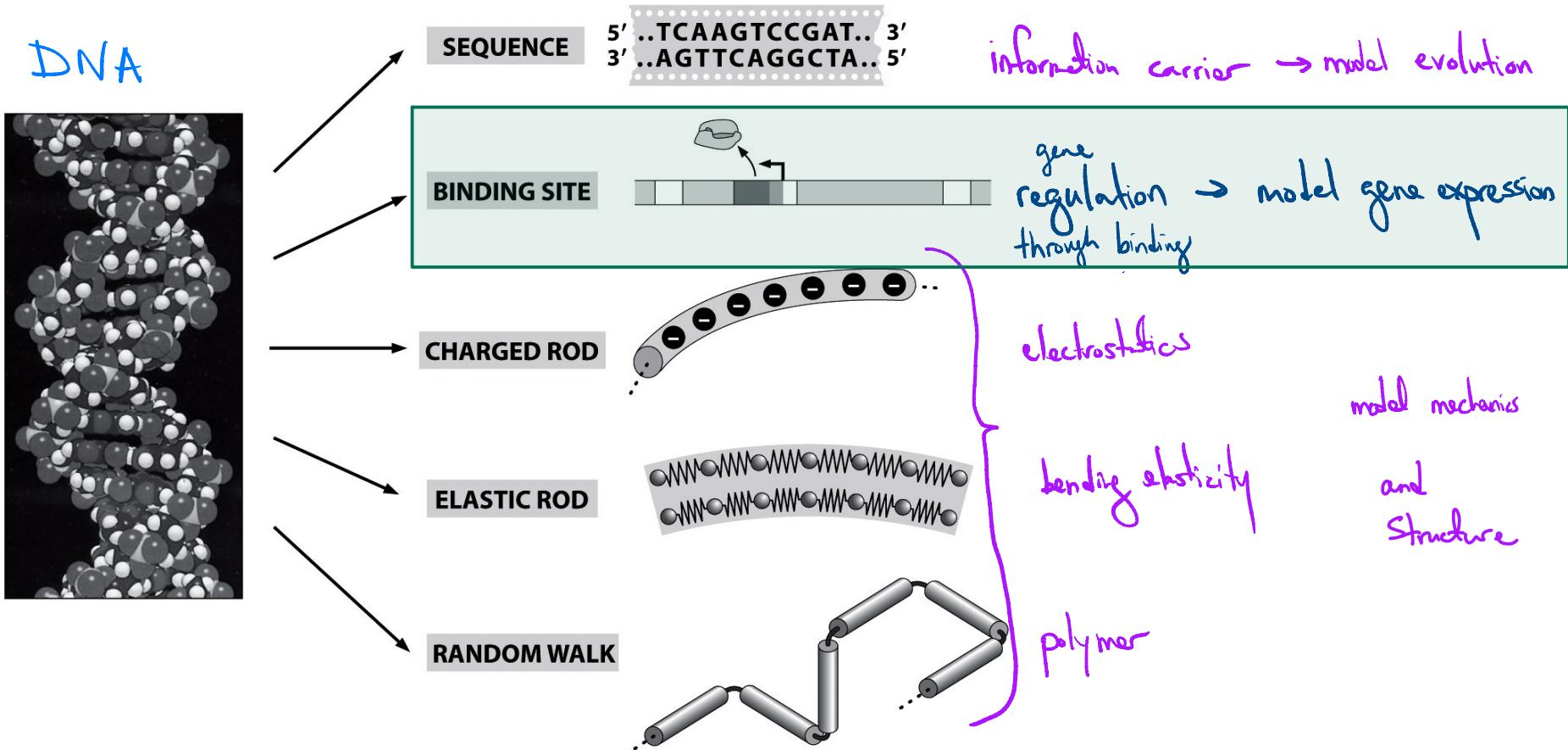
Model building

What is a model?

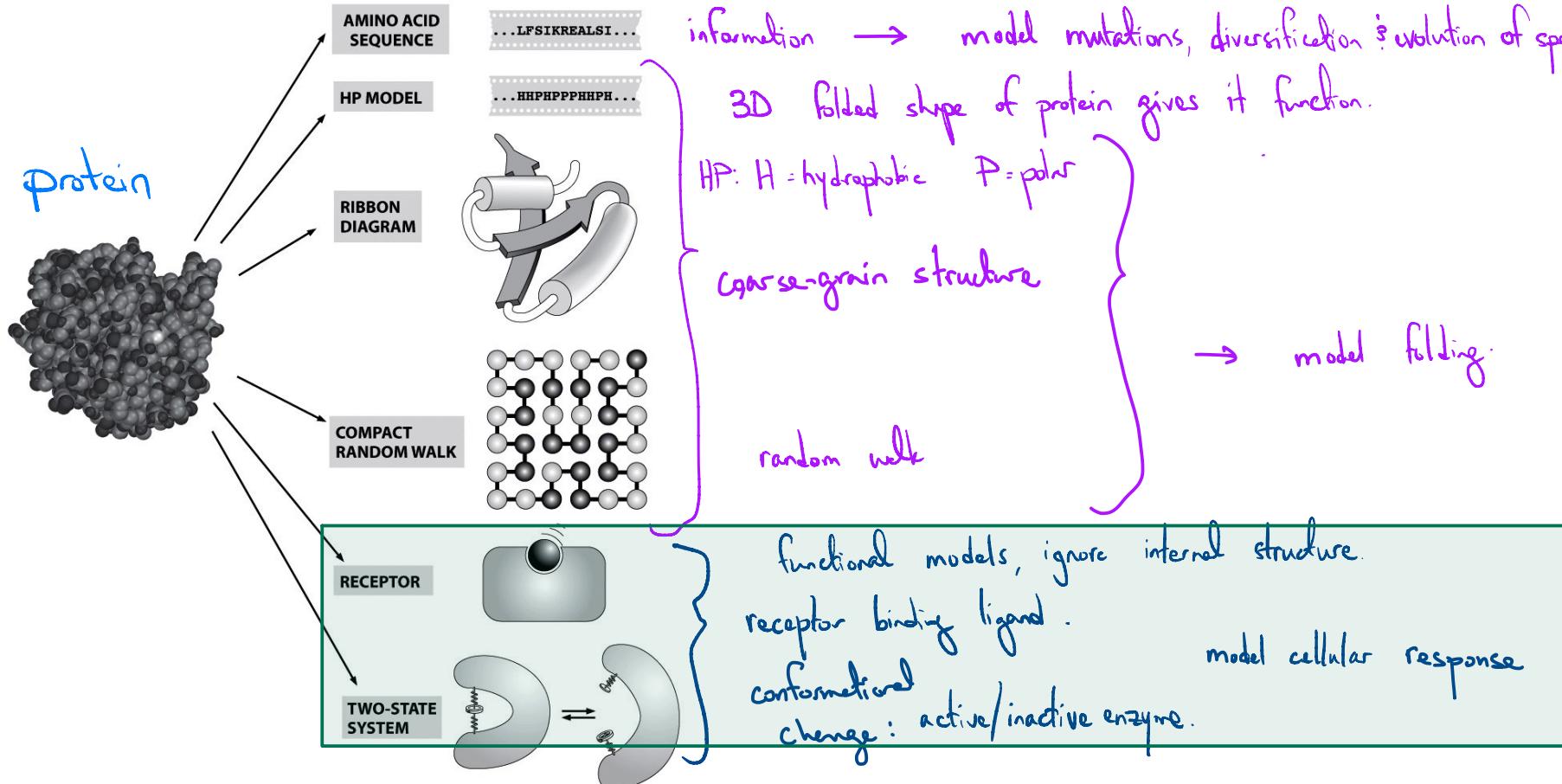
- Overlook / coarse grain some details, keep enough to make prediction
- Explain / capture existing phenomena → extrapolable to predict

Main challenge: what to simplify, what to keep complex

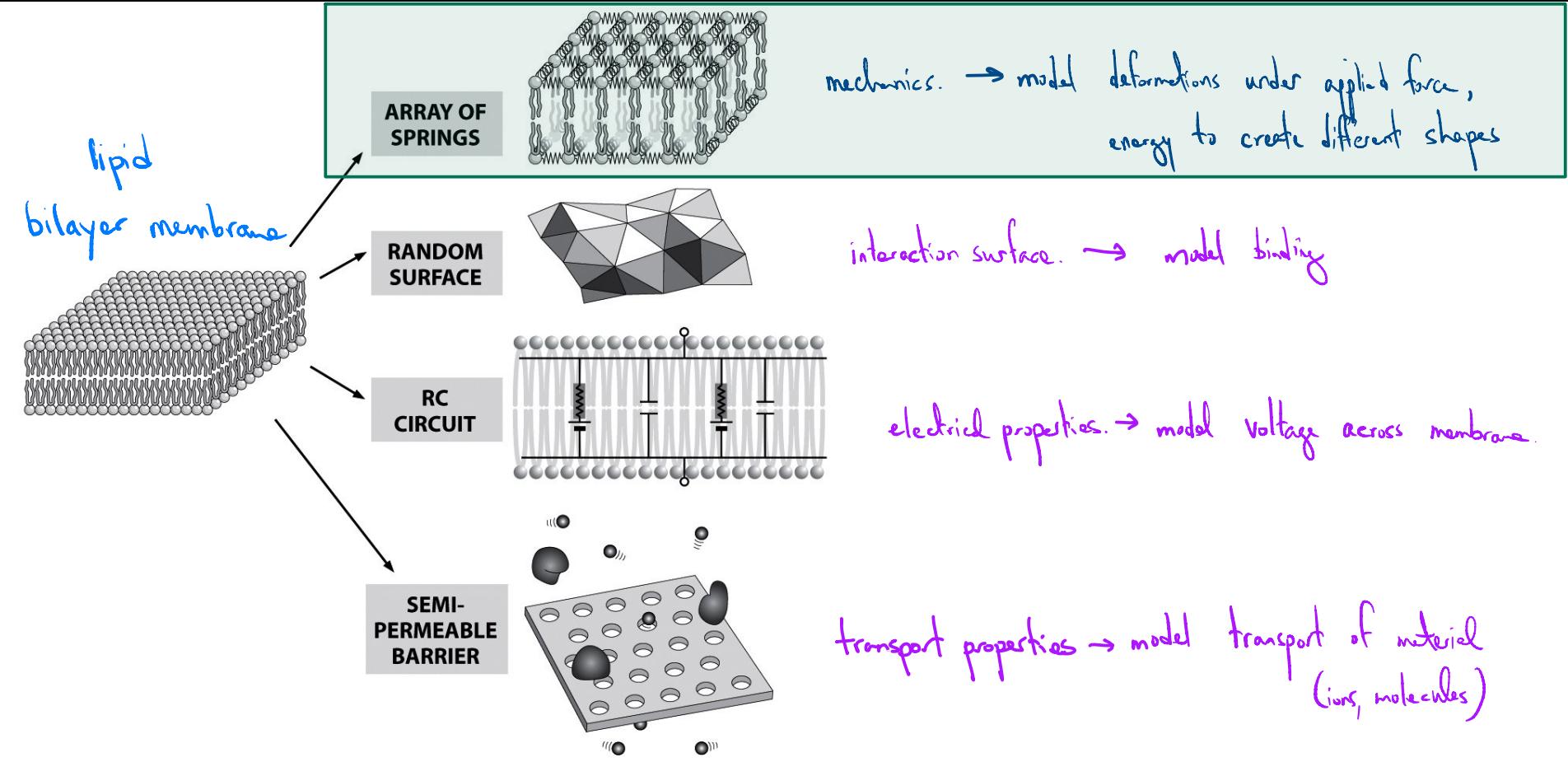
Model building



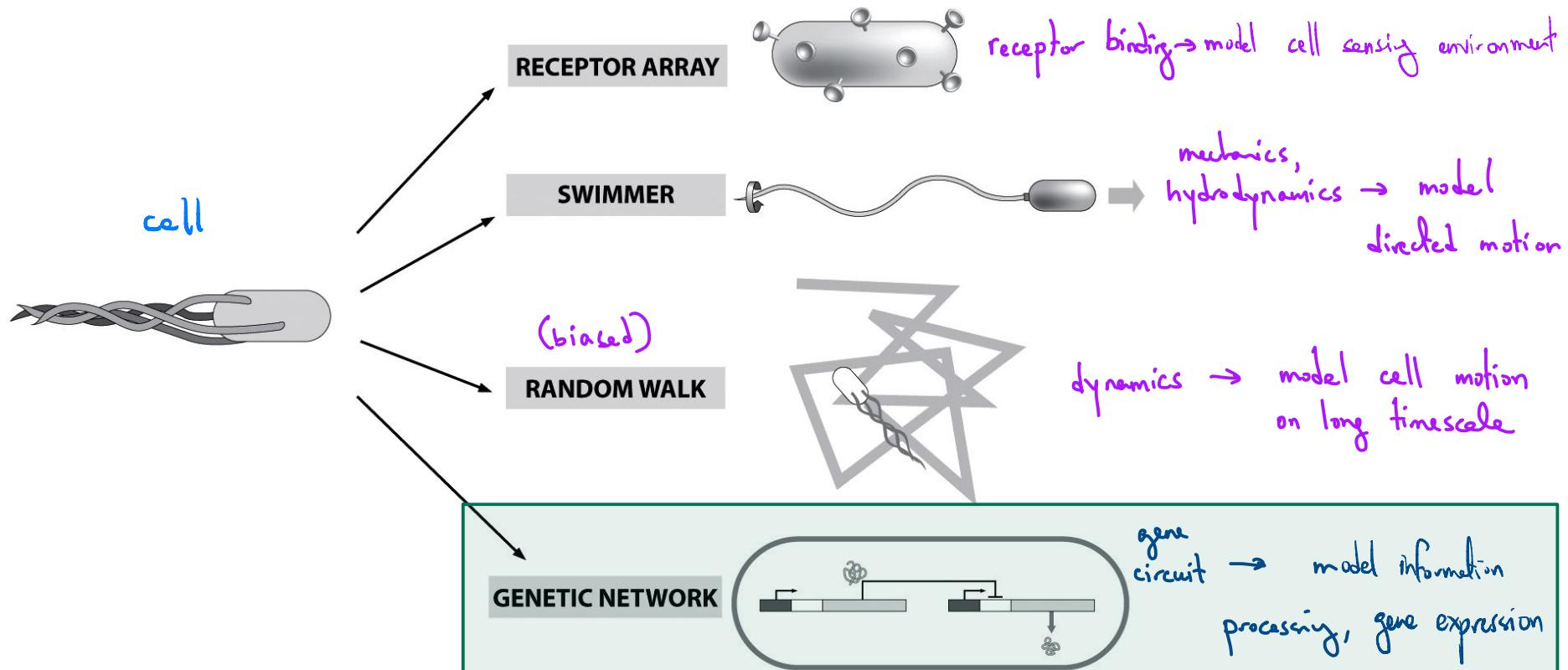
Model building



Model building



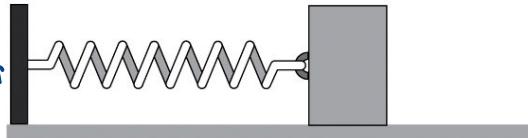
Model building



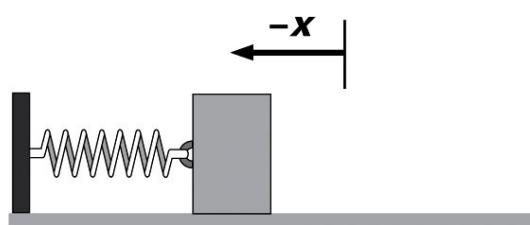
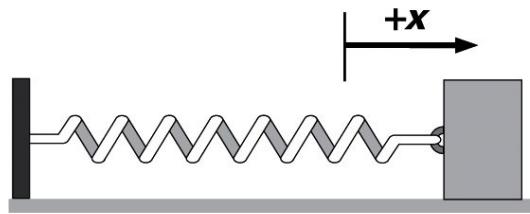
Quantitative models and the power of idealization

Simple spring model

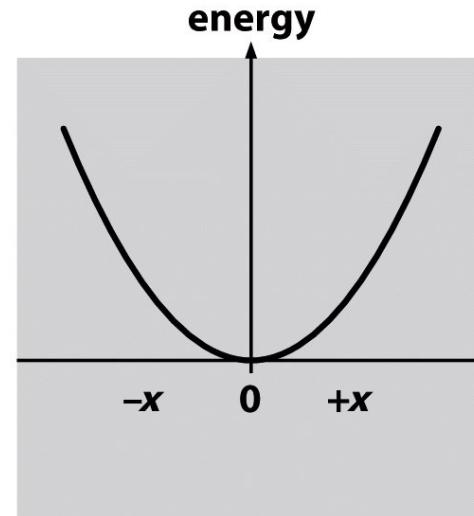
linear
force-displacement



$$F = -kx$$



Example: Potential energy landscape



potential energy
 $U = \frac{1}{2} kx^2$

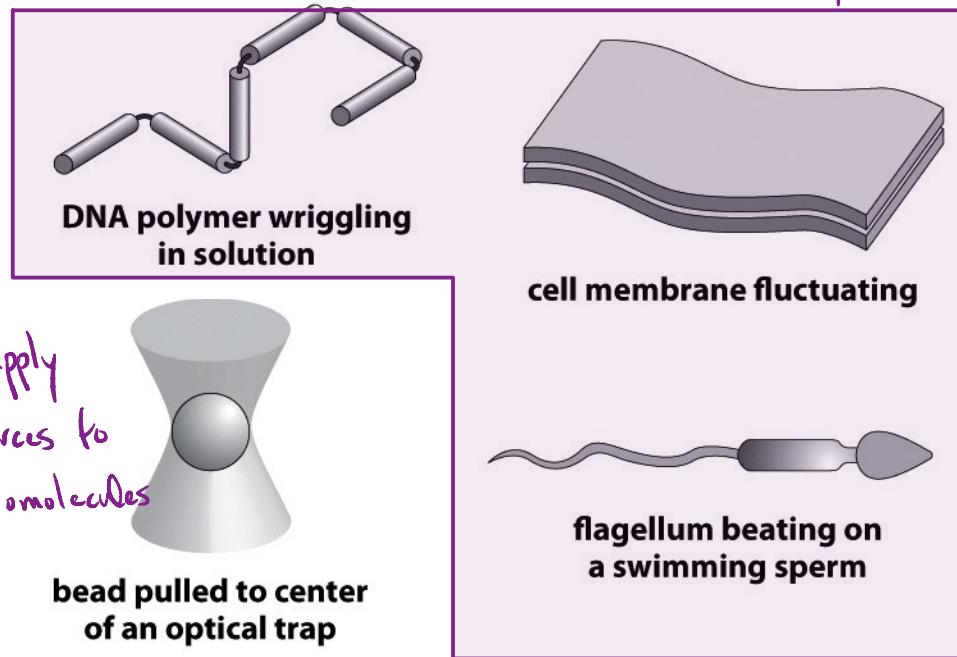
free energy minimization
position

oscillation when energy
is added

Quantitative models and the power of idealization

Analogs in biophysics

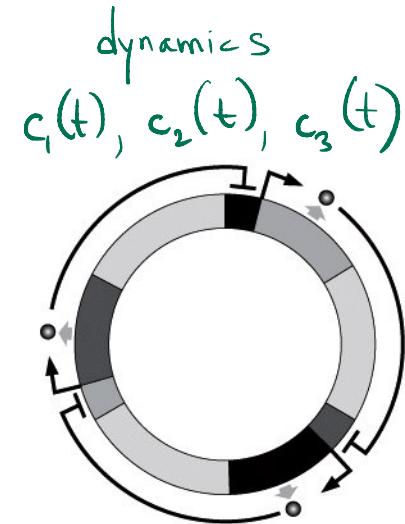
measure mechanics of biological systems



Example: Potential energy landscape

probability $p(E)$

molecules in an energy landscape



oscillatory solutions
to differential eqns

Quantitative models and the power of idealization

Numerical estimates

Phillips Numbers SnapShot
BioNumbers website

Quantity of interest		Symbol	Rule of thumb				
<i>E. coli</i>	Cell volume	$V_{E. coli}$	$\approx 1 \mu\text{m}^3$	DNA	Length per base pair	l_{bp}	$\approx 1/3 \text{ nm}$
	Cell mass	$m_{E. coli}$	$\approx 1 \text{ pg}$		Volume per base pair	V_{bp}	$\approx 1 \text{ nm}^3$
	Cell cycle time	$t_{E. coli}$	$\approx 3000 \text{ s}$		Charge density	λ_{DNA}	$2 \text{ e}/0.34 \text{ nm}$
	Cell surface area	$A_{E. coli}$	$\approx 6 \mu\text{m}^2$		Persistence length	ξ_p	50 nm
	Genome length	$N_{bp}^{E. coli}$	$\approx 5 \times 10^6 \text{ bp}$				
	Swimming speed	$v_{E. coli}$	$\approx 20 \mu\text{m/s}$				
Yeast	Volume of cell	V_{yeast}	$\approx 60 \mu\text{m}^3$	Amino acids and proteins	Radius of "average" protein	$r_{protein}$	$\approx 2 \text{ nm}$
	Mass of cell	m_{yeast}	$\approx 60 \text{ pg}$		Volume of "average" protein	$V_{protein}$	$\approx 25 \text{ nm}^3$
	Diameter of cell	d_{yeast}	$\approx 5 \mu\text{m}$		Mass of "average" amino acid	M_{aa}	$\approx 100 \text{ Da}$
	Cell cycle time	t_{yeast}	$\approx 200 \text{ min}$		Mass of "average" protein	$M_{protein}$	$\approx 30,000 \text{ Da}$
	Genome length	N_{bp}^{yeast}	$\approx 10^7 \text{ bp}$		Protein concentration in cytoplasm	$c_{protein}$	$\approx 300 \text{ mg/mL}$
Organelles	Diameter of nucleus	$d_{nucleus}$	$\approx 5 \mu\text{m}$		Characteristic force of protein motor	F_{motor}	$\approx 5 \text{ pN}$
	Length of mitochondrion	l_{mito}	$\approx 2 \mu\text{m}$		Characteristic speed of protein motor	v_{motor}	$\approx 200 \text{ nm/s}$
	Diameter of transport vesicles	$d_{vesicle}$	$\approx 50 \text{ nm}$		Diffusion constant of "average" protein	$D_{protein}$	$\approx 100 \mu\text{m}^2/\text{s}$
Water	Volume of molecule	V_{H_2O}	$\approx 10^{-2} \text{ nm}^3$	Lipid bilayers	Thickness of lipid bilayer	d	$\approx 5 \text{ nm}$
	Density of water	ρ	1 g/cm^3		Area per molecule	A_{lipid}	$\approx \frac{1}{2} \text{ nm}^2$
	Viscosity of water	η	$\approx 1 \text{ centipoise}$ $(10^{-2} \text{ g}/(\text{cm s}))$		Mass of lipid molecule	m_{lipid}	$\approx 800 \text{ Da}$
	Hydrophobic embedding energy	$\approx E_{hydr}$	$25 \text{ cal}/(\text{mol } \text{\AA}^2)$				

Lecture 2 outline

Goal: Size and contents of cells

- An ode to E. coli
- Cells and the structures within them

PBOC Chapter 2.1, 2.2