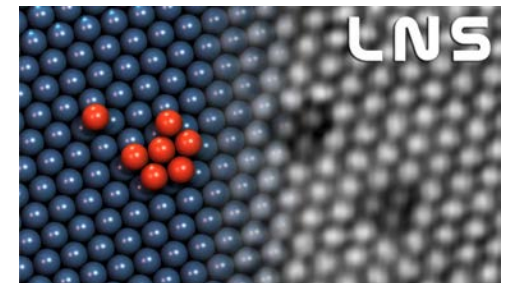


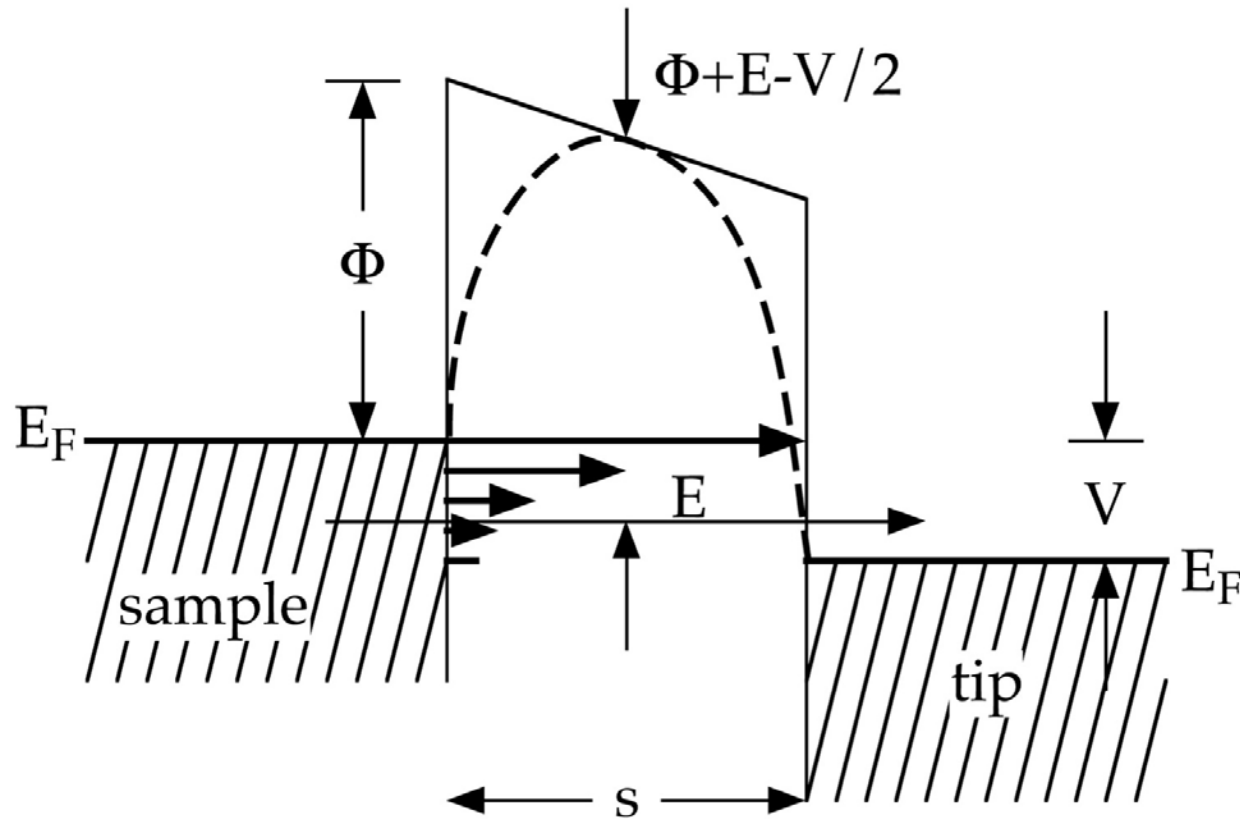
Scanning Tunneling Microscopy

1. Principles
2. History
3. Experimental Realization
4. Tips
5. Atomic Resolution
6. Scanning Tunneling Spectroscopy
7. Surface States
8. Inelastic Electron Tunneling Spectroscopy
9. Electron Spin Resonance with the STM

EPFL



Vacuum Tunneling



Tunnel Current in transfer Hamiltonian:

$$I = \frac{2\pi e}{\hbar} \sum_{\mu, \nu} f(E_{\mu}) (1 - f(E_{\nu} + eV)) |M_{\mu\nu}|^2 \delta(E_{\mu} - E_{\nu})$$

$$M_{\mu\nu} = \frac{\hbar^2}{2m} \int (\psi_{\mu}^* \nabla \psi_{\nu} - \psi_{\nu} \nabla \psi_{\mu}^*) dS$$

J. Bardeen, Phys. Rev. Lett. 6, 57 (1961).

Calculating the Tunnel Current

Application of Transfer Hamiltonian to STM geometry :

$$I = \rho(\mathbf{r}_0, E_F) e^{-2ks} \quad s \text{ tip-sample distance}$$

With decay length $k = \sqrt{2m / \hbar^2 (\Phi + E - eV / 2)}$ Φ workfunction

where $\sqrt{2m / \hbar^2} = 0.51 \text{\AA}^{-1} \sqrt{eV}^{-1}$

$$\Phi = 4eV \Rightarrow 2k = 2 / \text{\AA}$$

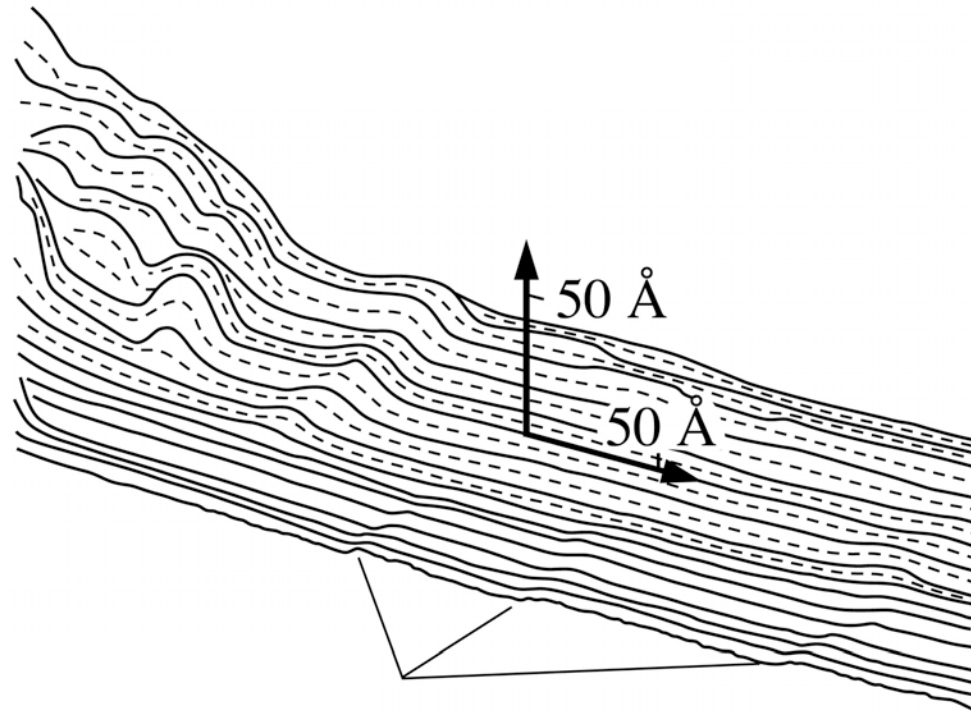
Tunnel current decays by 1 order of magnitude per \AA change in tip-sample distance

First STM by Binnig & Rohrer

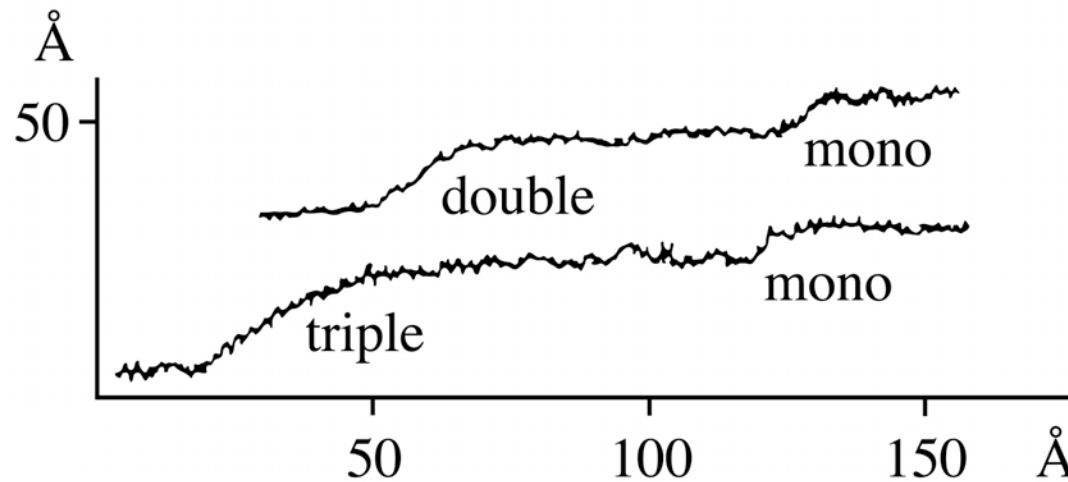


First Results on $\text{CaIrSn}_4(110)$

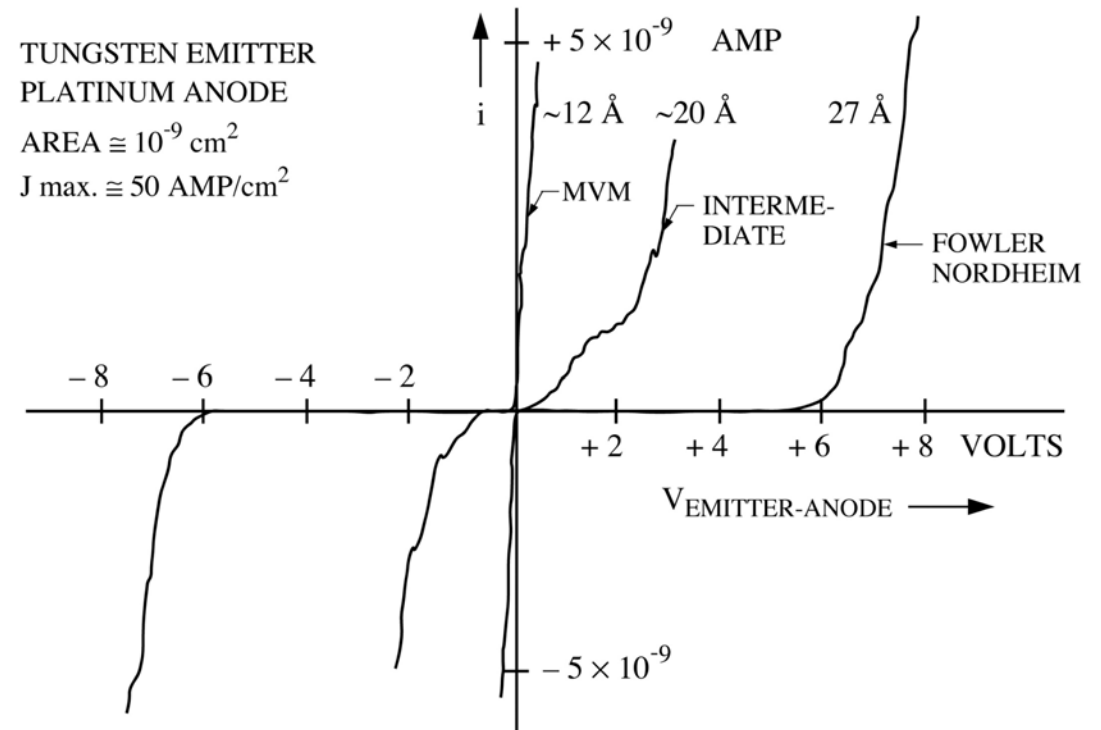
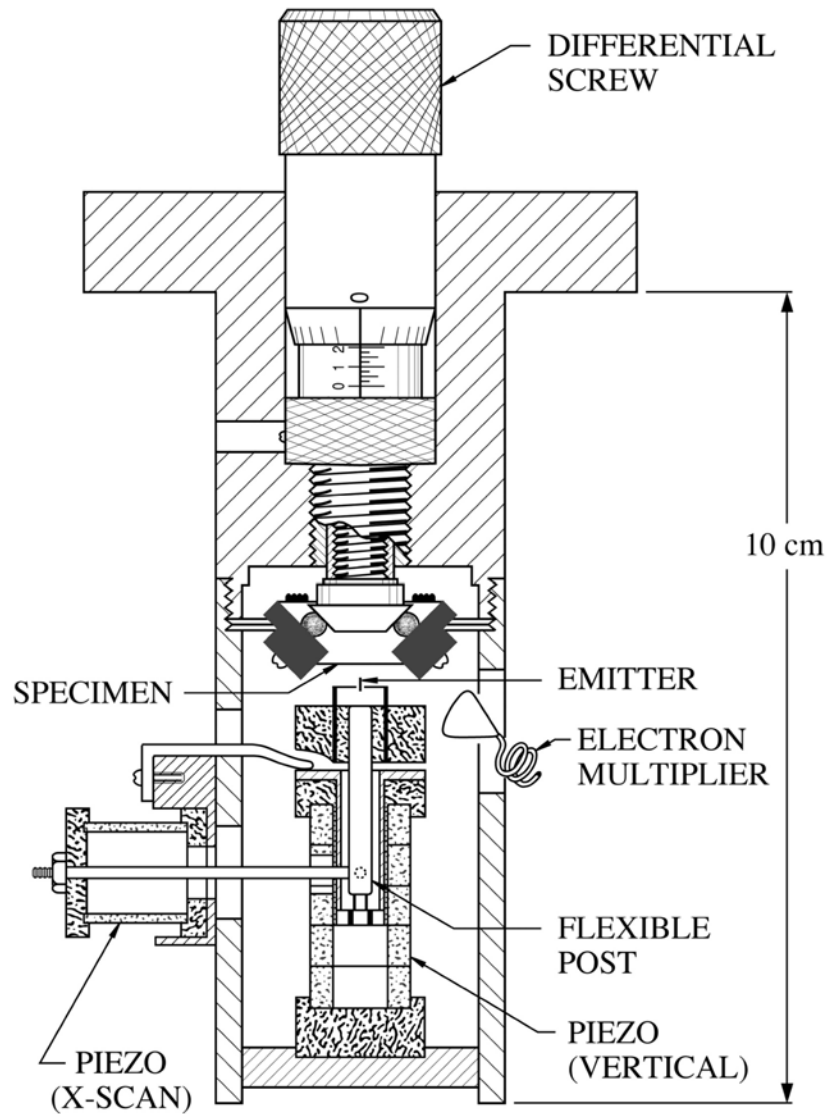
Growth Spiral



Atomic Steps

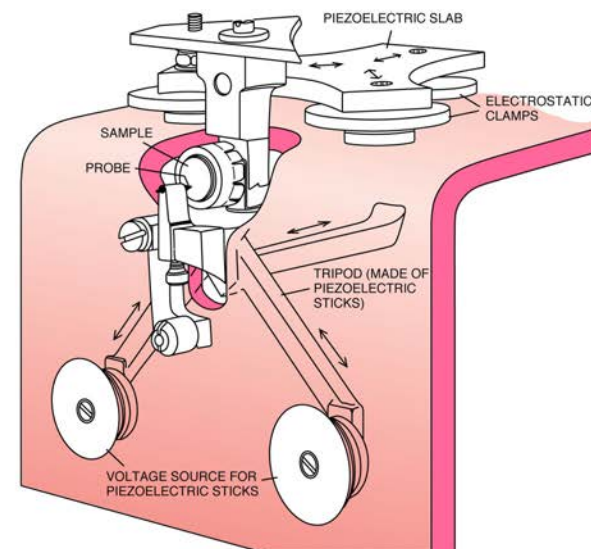
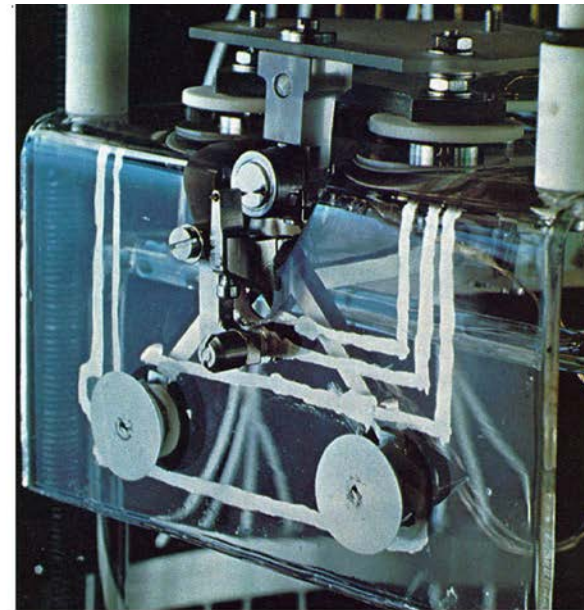
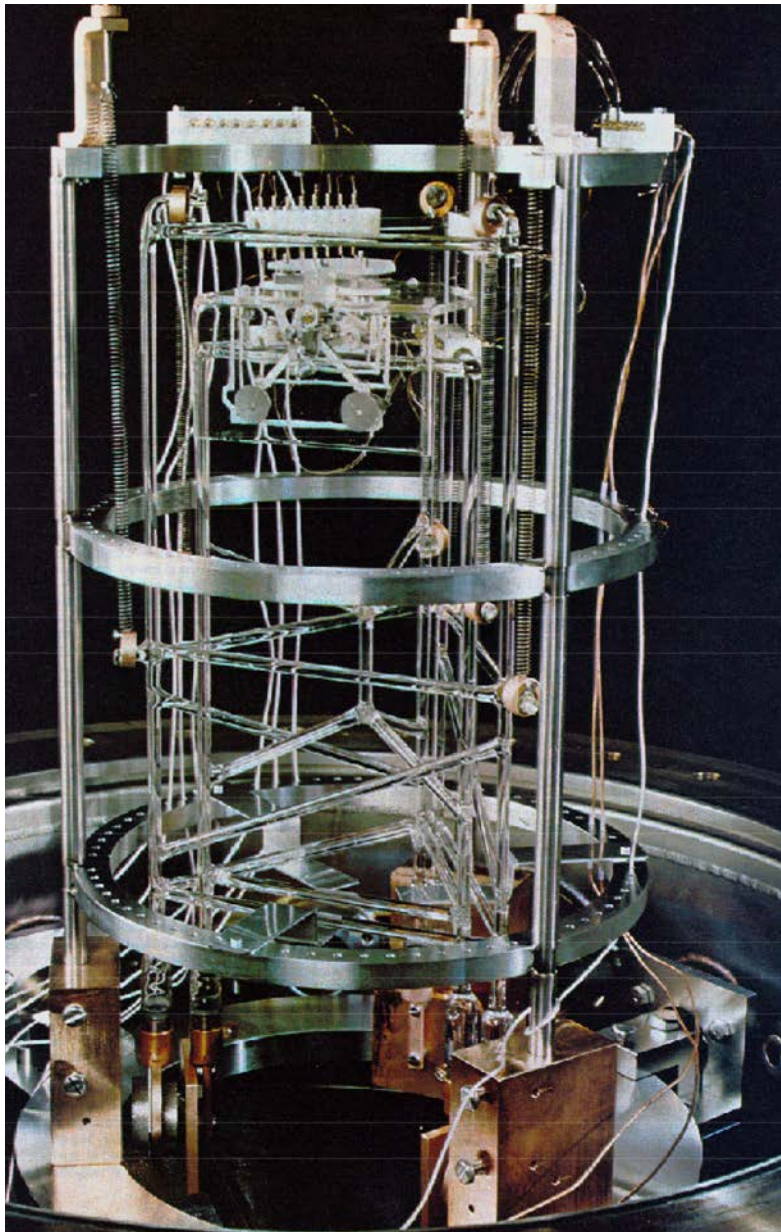


Topografiner – the Predecessor of the STM



R. Young *et al.*, Rev. Sci. Instrum. **43**, 999 (1972);
See also: I. Amato, Science **276**, 1982 (1997).

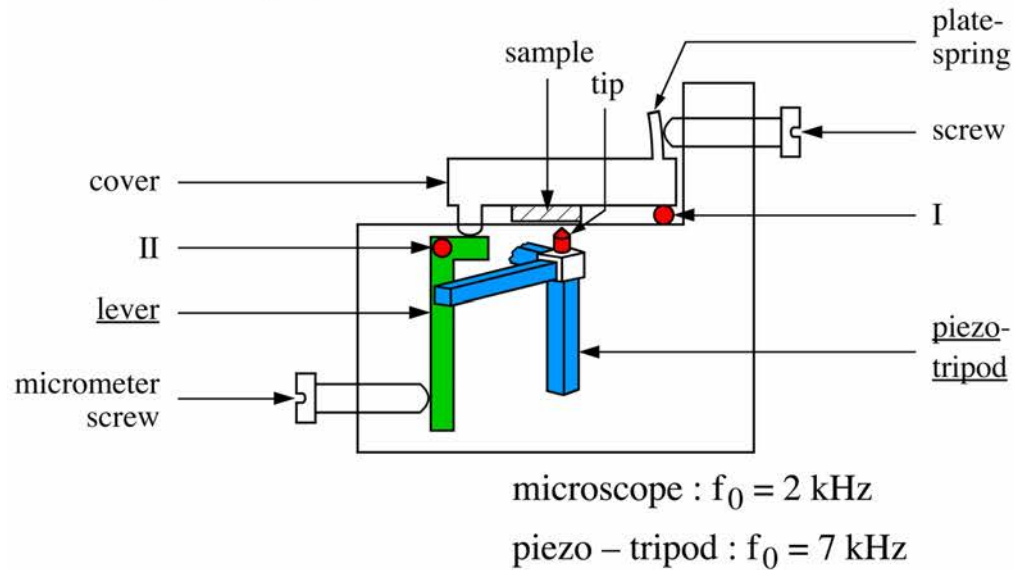
Realization of Coarse Approach and Vibration Damping



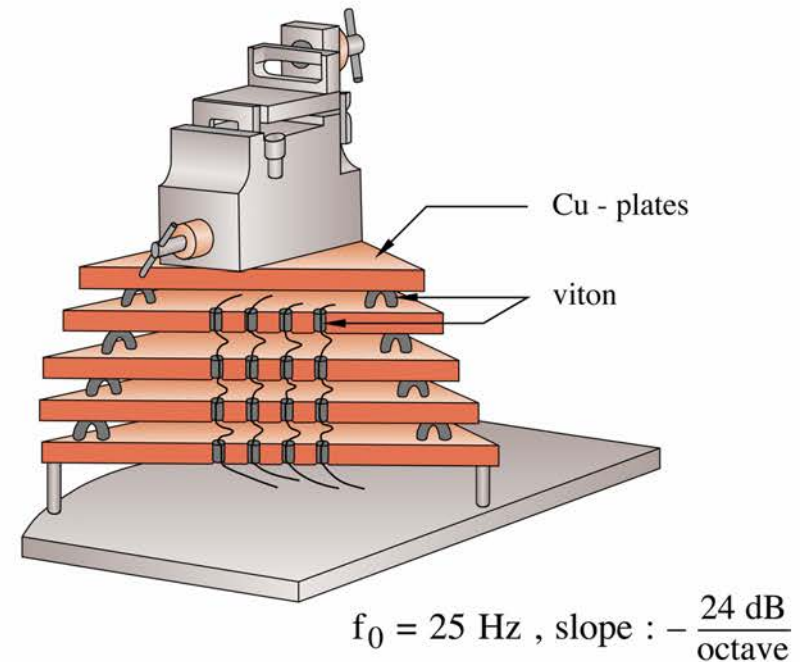
Pocket-size STM and viton stack for vibration damping

Mechanical properties

- sample – tip approach:

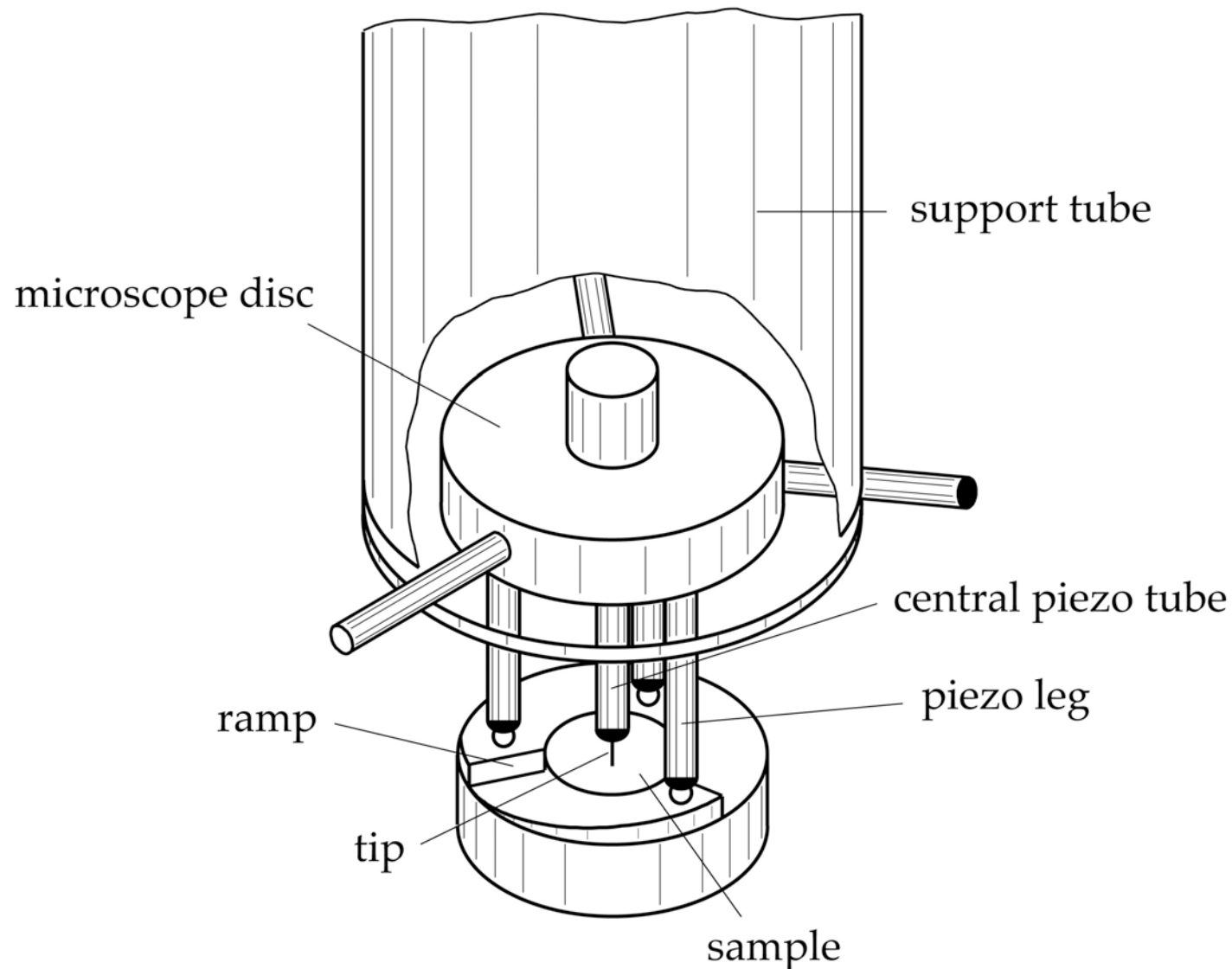


- viton – damped stack:

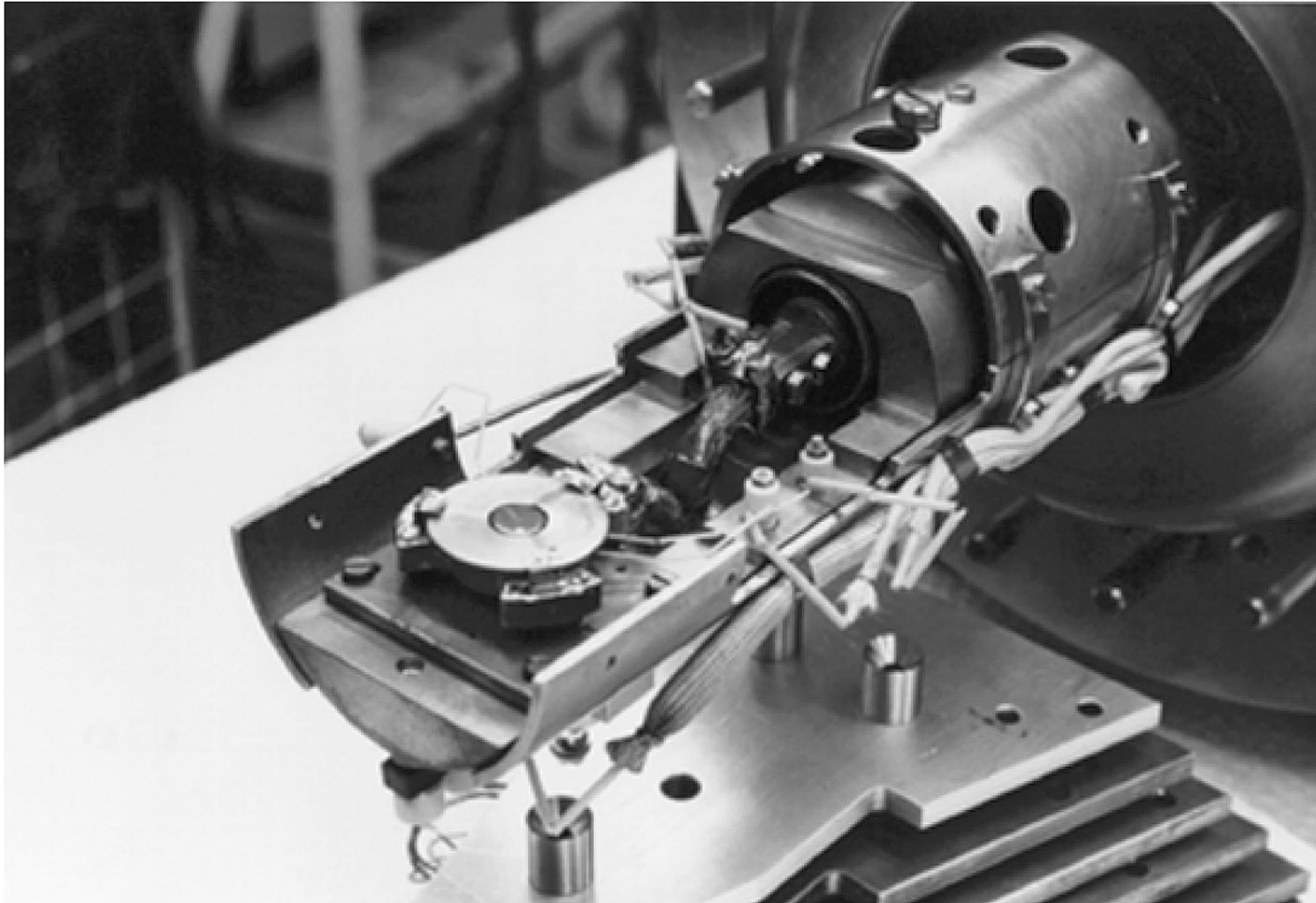


Beetle Type STM Compensating Thermal Drifts

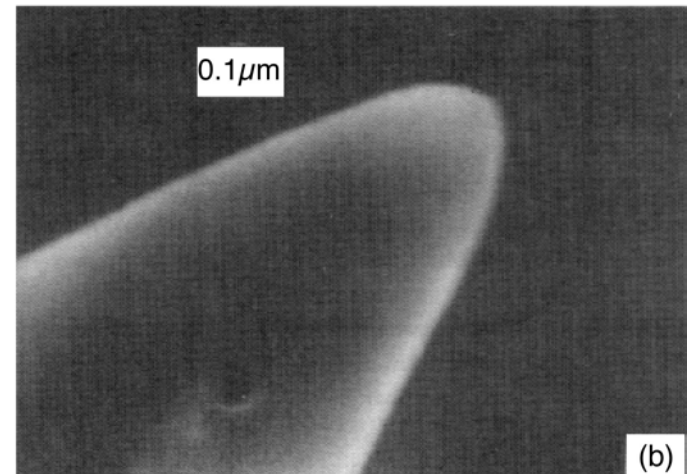
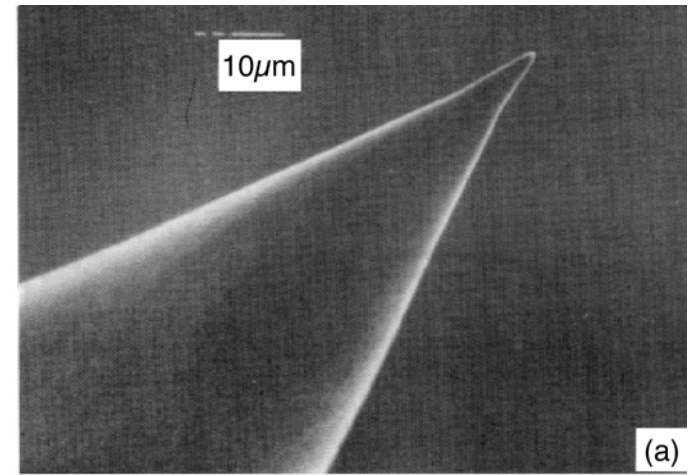
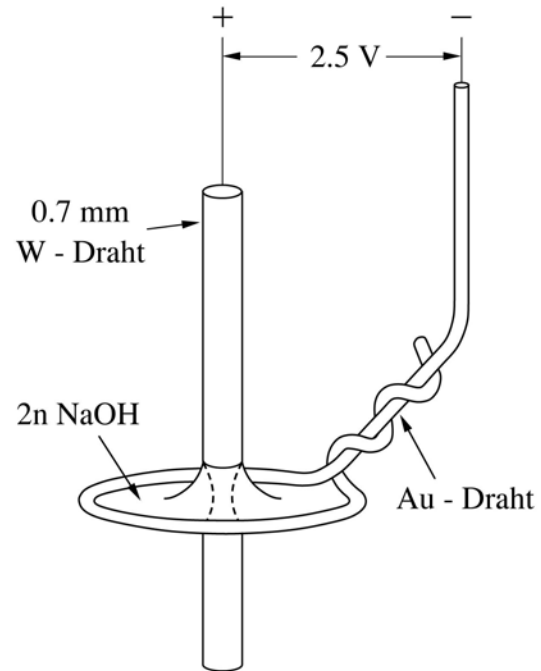
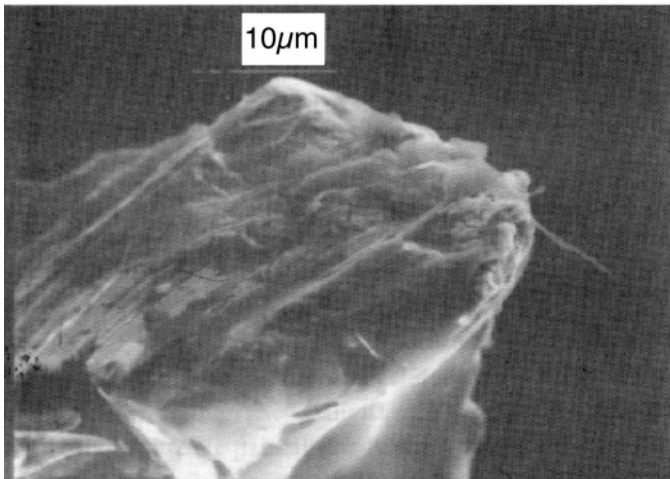
Beetle-STM Principle



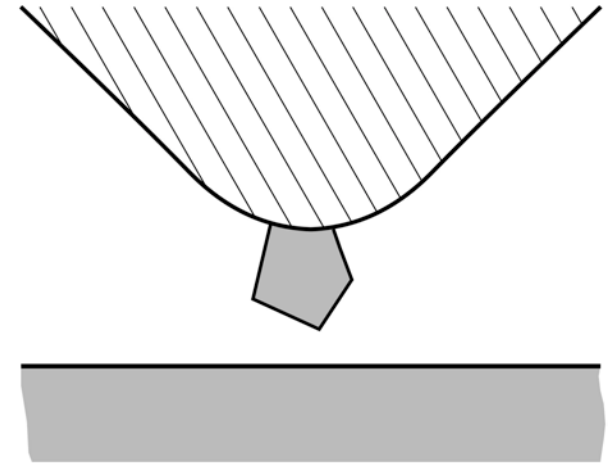
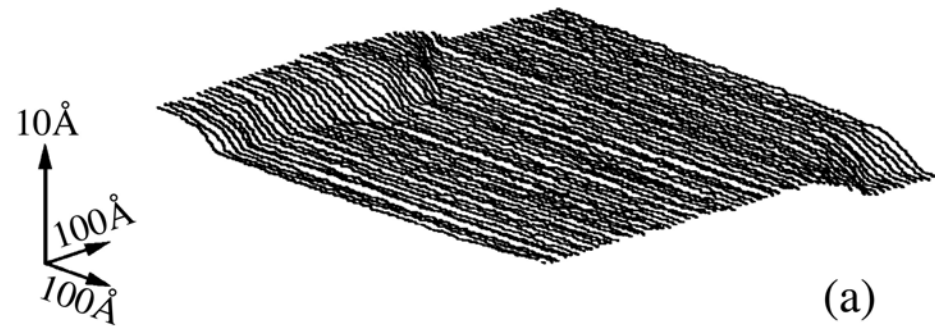
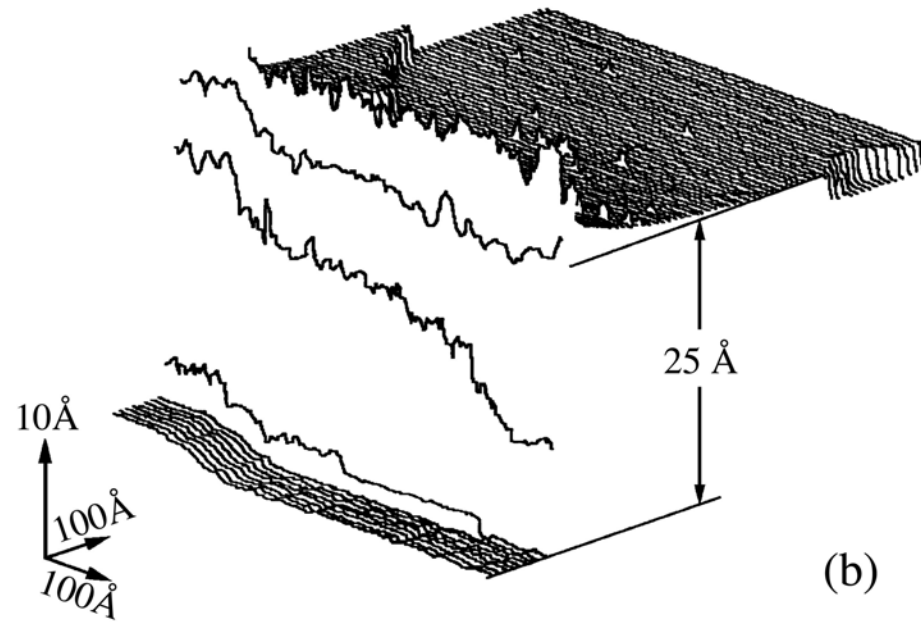
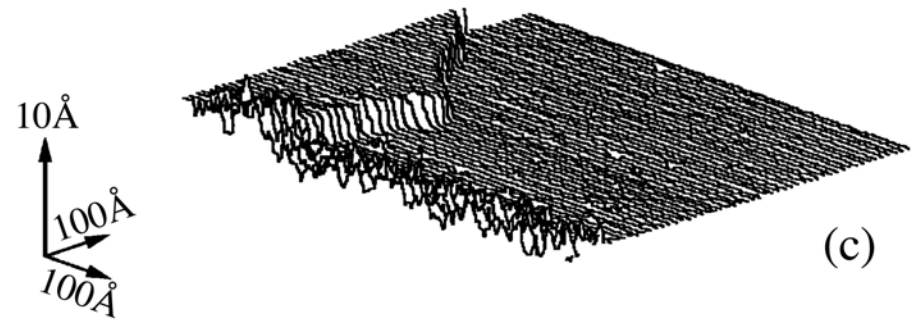
Sample Holder for Variable-Temperature STM 30 - 600 K



Electrochemical Etching of W-tips

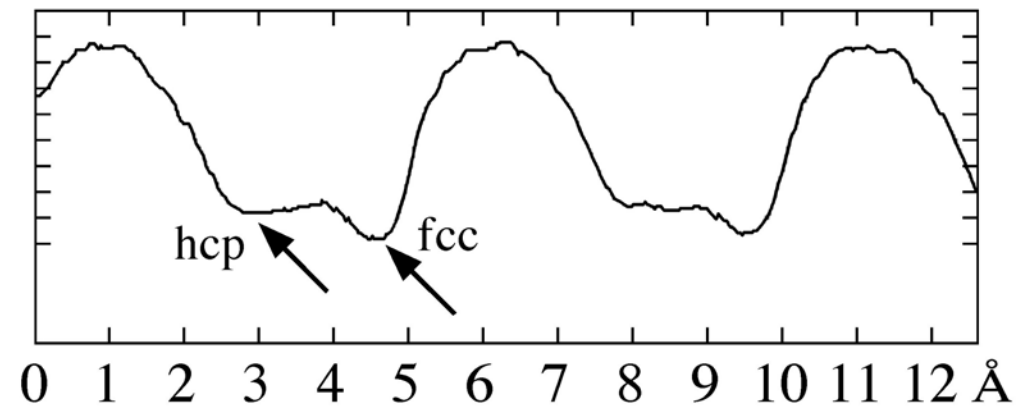
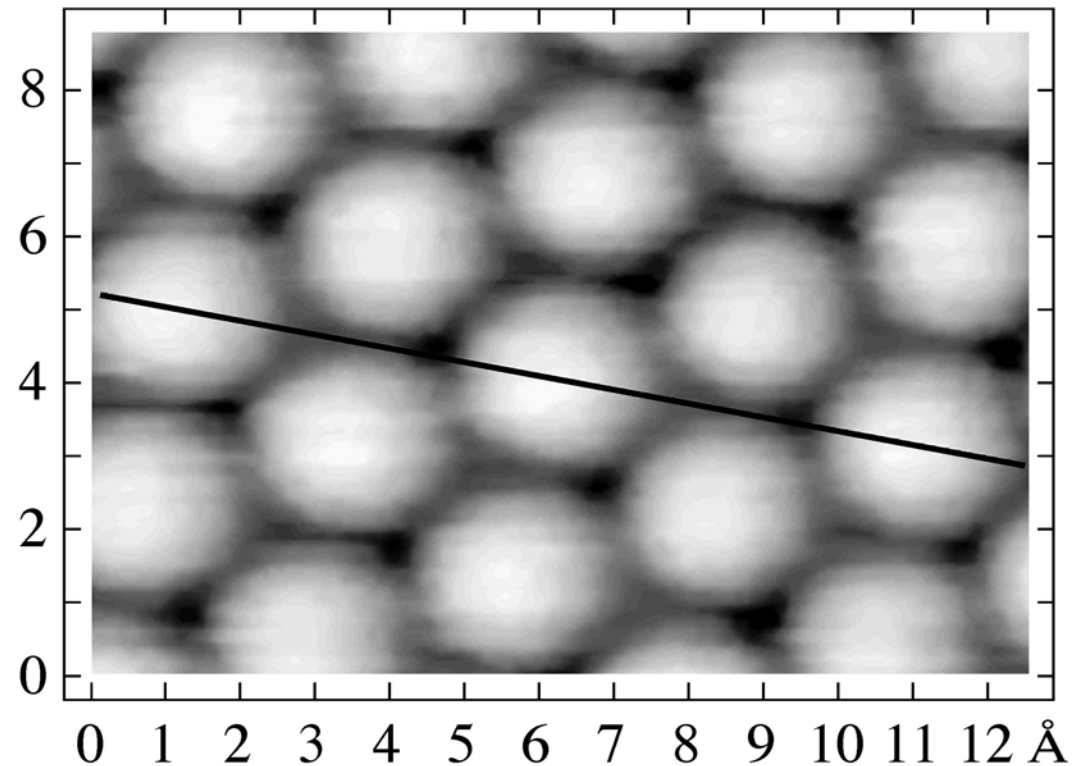
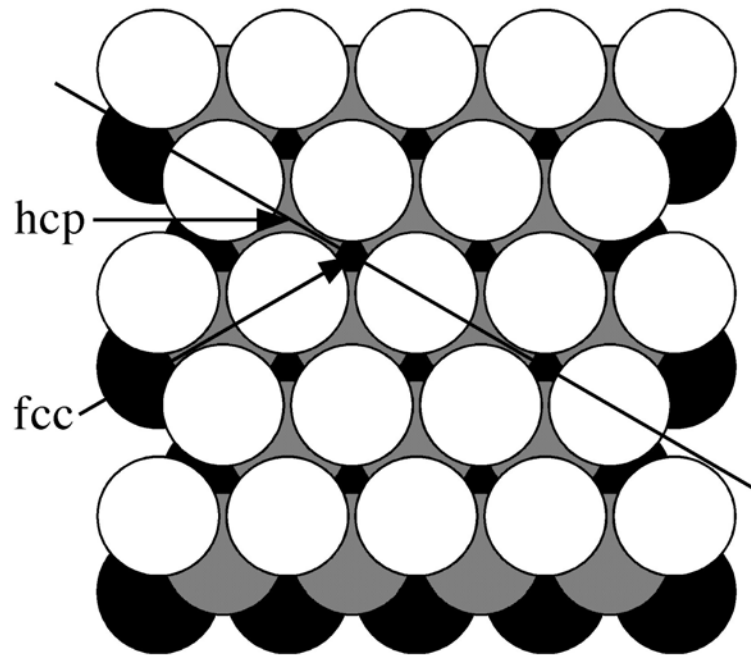


Tip preparation by Voltage Pulses during STM Operation

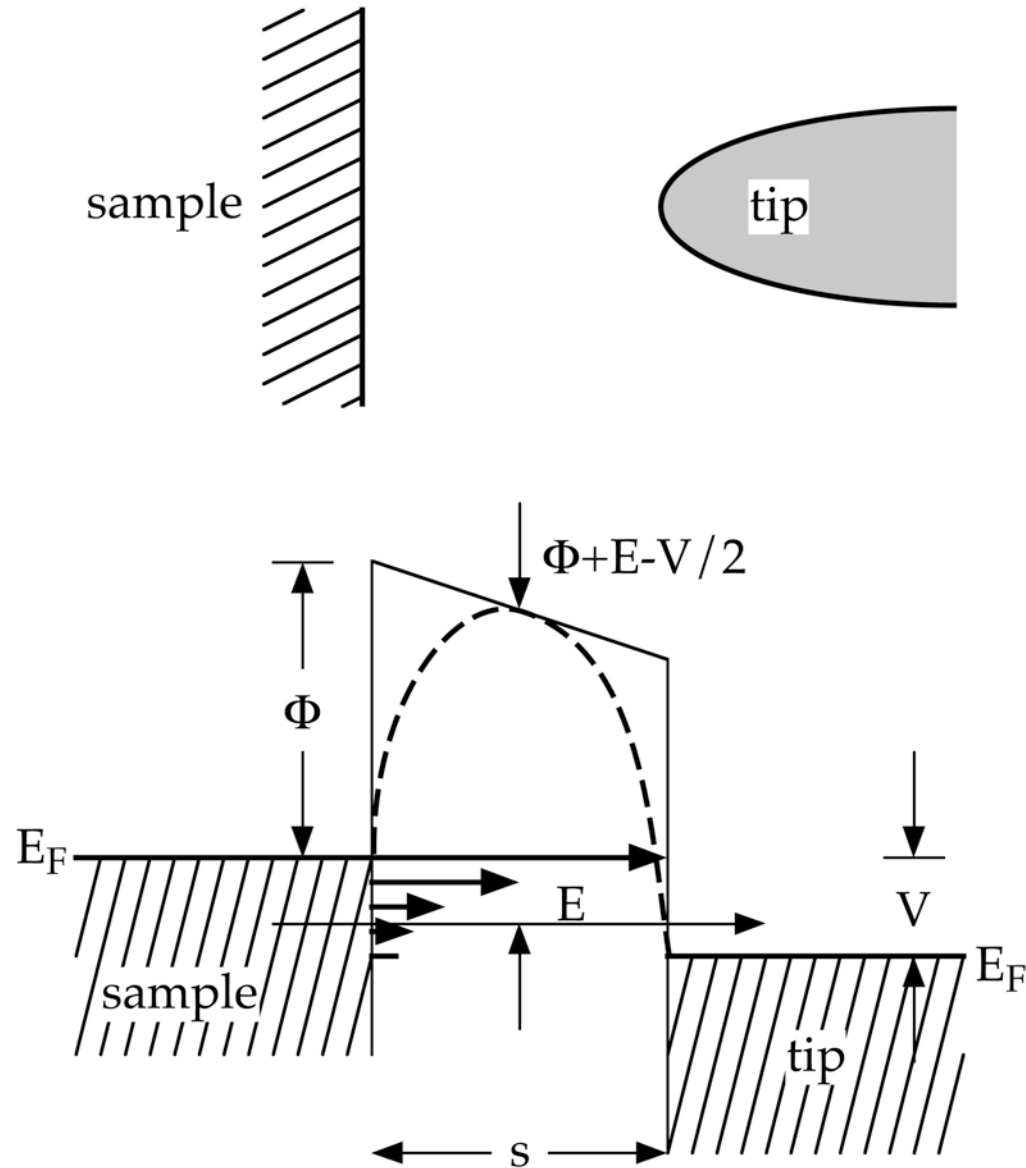


What 'sees' the STM

Al(111) – seeing atoms and below – fcc vs hcp hollows



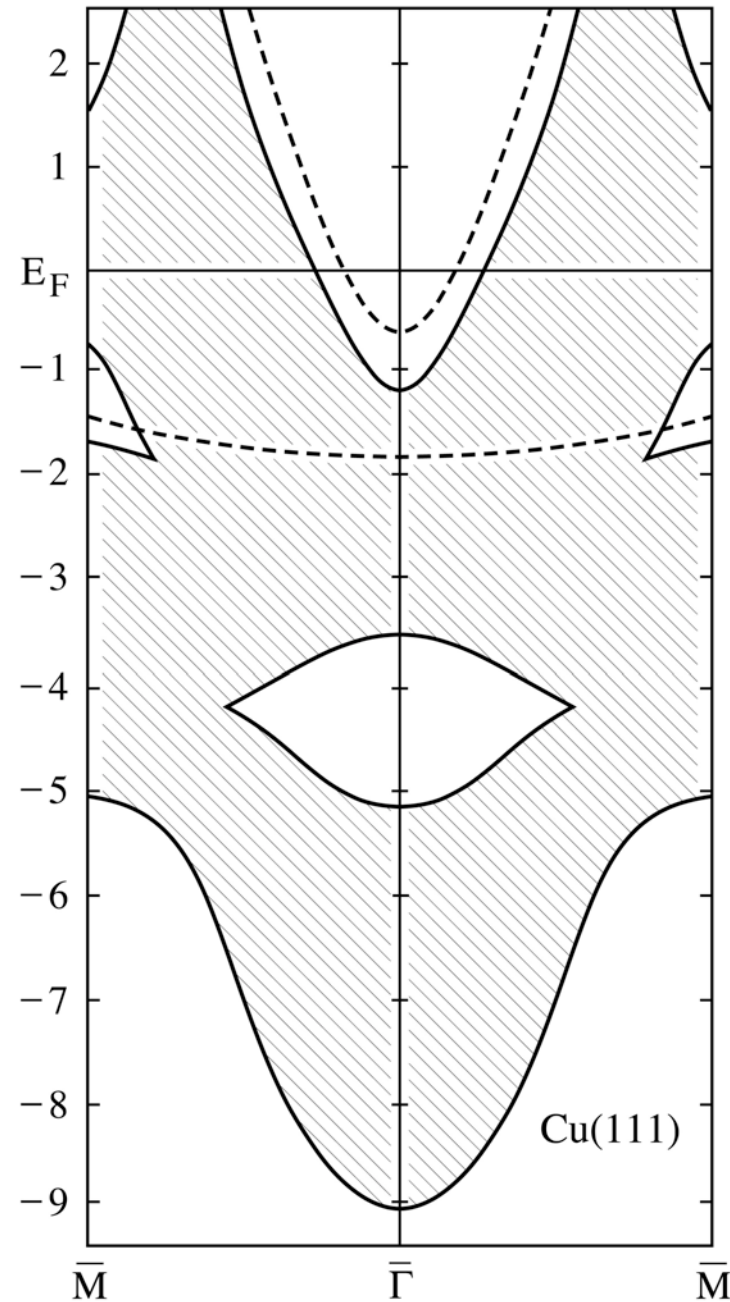
Scanning Tunneling Spectroscopy - STS



$$I \propto \int_0^{eV} dE \rho_{\text{sample}}(E, x, y) \rho_{\text{tip}}(E - eV) \longrightarrow dI / dV(V, x, y) \approx \rho_{\text{sample}}(eV, x, y)$$

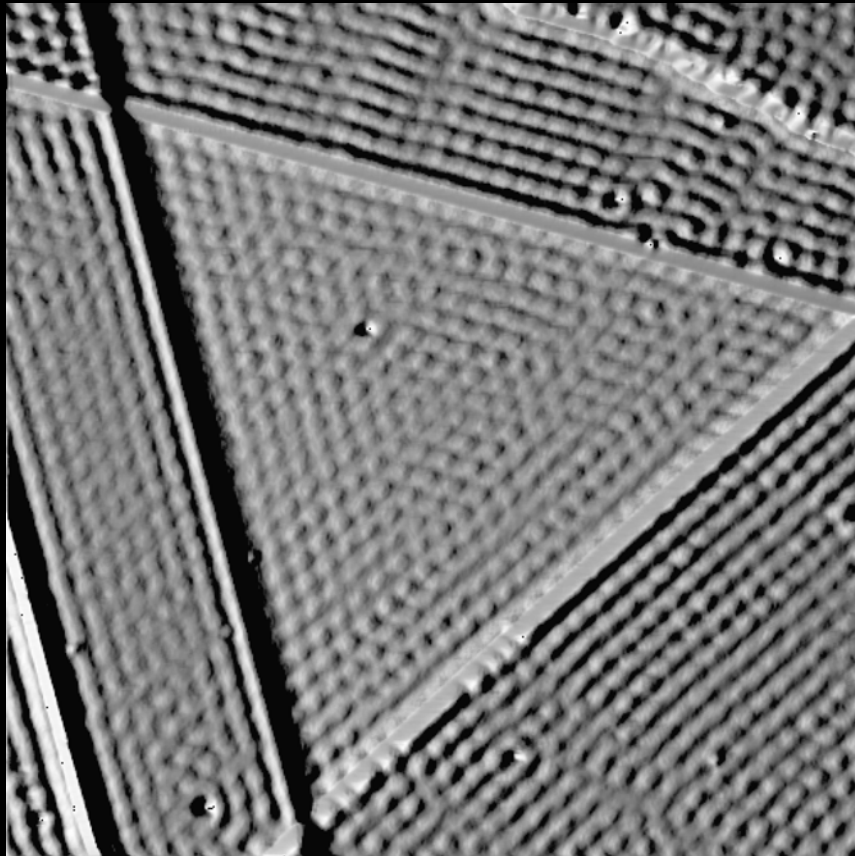
Surface States - Cu(111)

*(111)-projected bulk
bandstructure of Cu*



Electron scattering at atomic steps

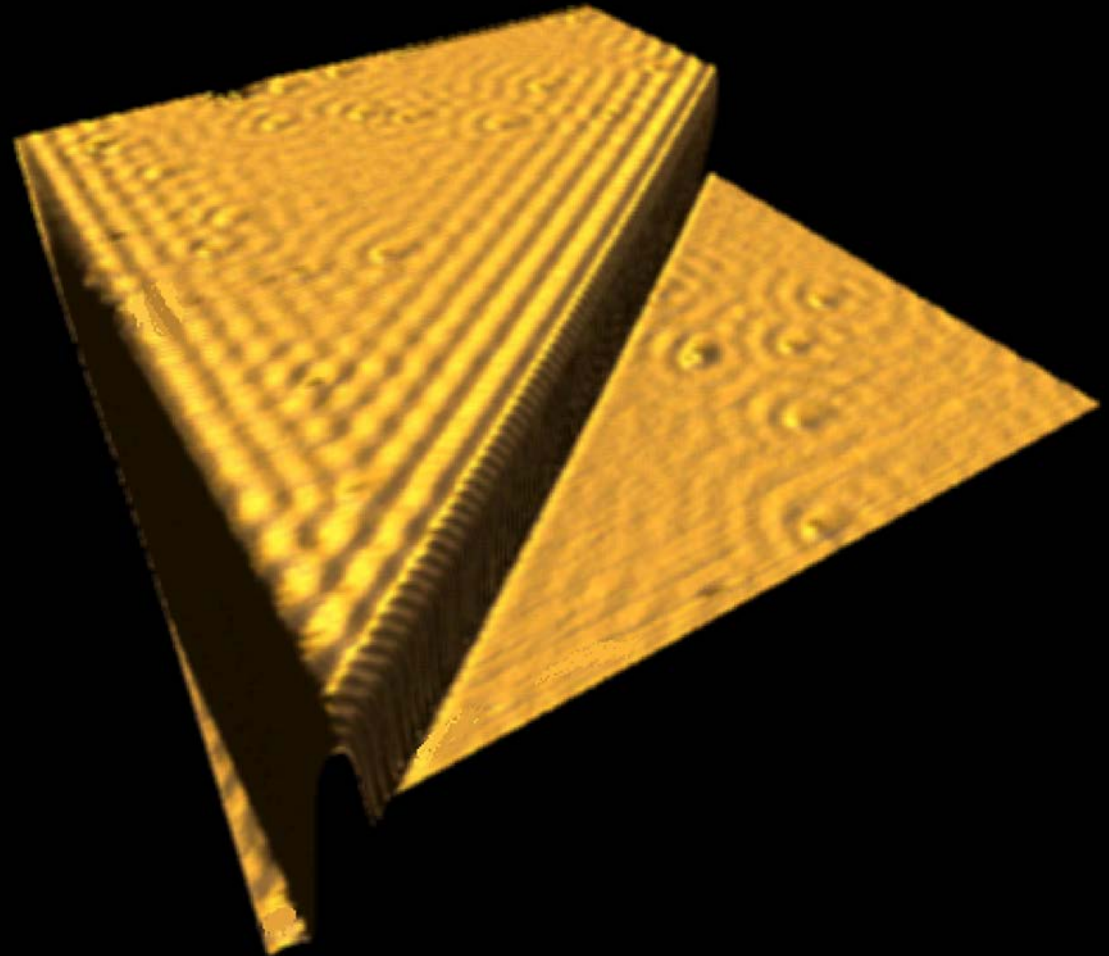
Cu(111)



100 Å

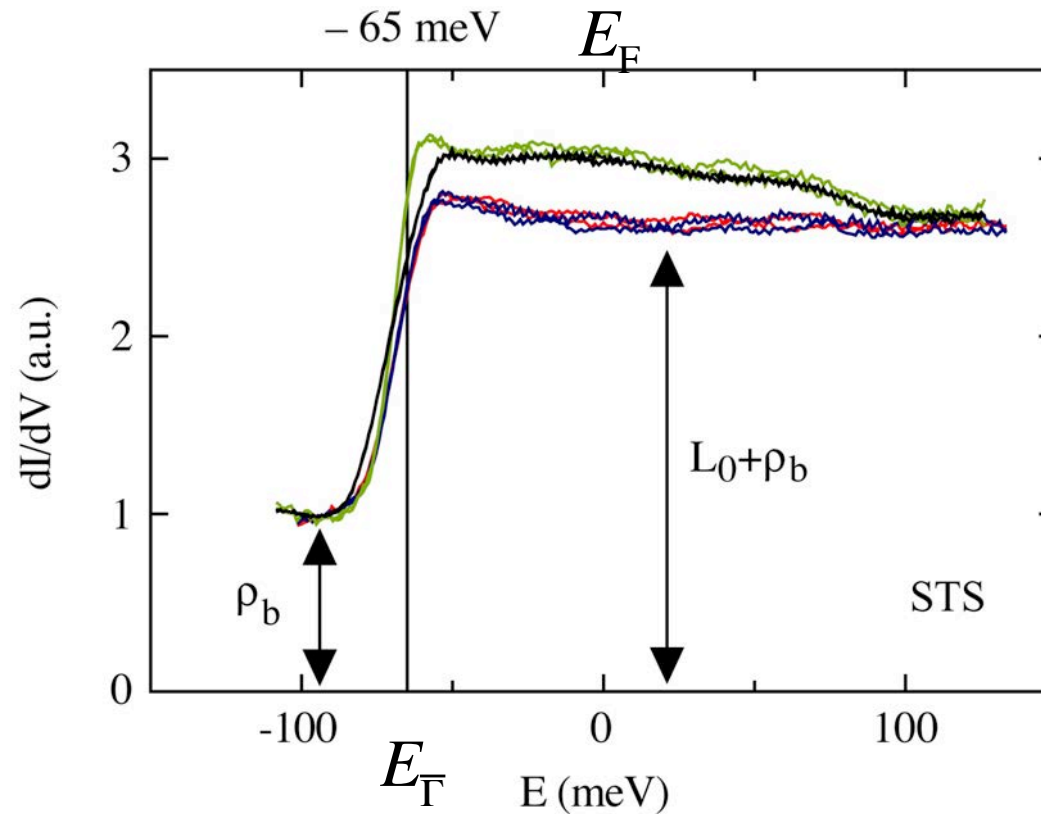
5 K, $V_t = 1.0$ mV, $I_t = 1.1$ nA

Ag(111)



5 K, $V_t = 13$ mV, $I_t = 0.32$ nA, 1000 Å x 1000 Å

Local Density of States (LDOS) of Ag(111)



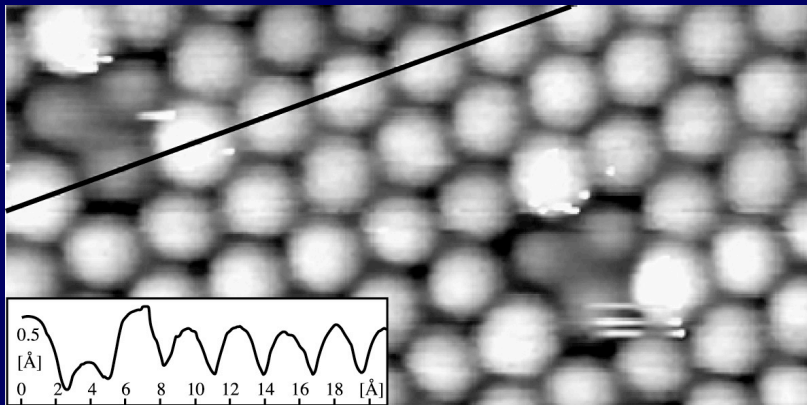
2D LDOS: $\rho_{2D}(E) = L_0 \Theta(E - E_{\bar{\Gamma}}) = \frac{m^*}{\pi \hbar^2} \Theta(E - E_{\bar{\Gamma}})$

2D e^- density: $n_{2D} = \frac{m^*}{\pi \hbar^2} |E_{\bar{\Gamma}}| \approx 10^{13} \text{ cm}^{-2}$

2DEG at semiconductor heterojunctions: $n_{2D} \approx 5 \cdot 10^{11} \text{ cm}^{-2}$

Friedel Oscillations

Bulk
C/Al(111)

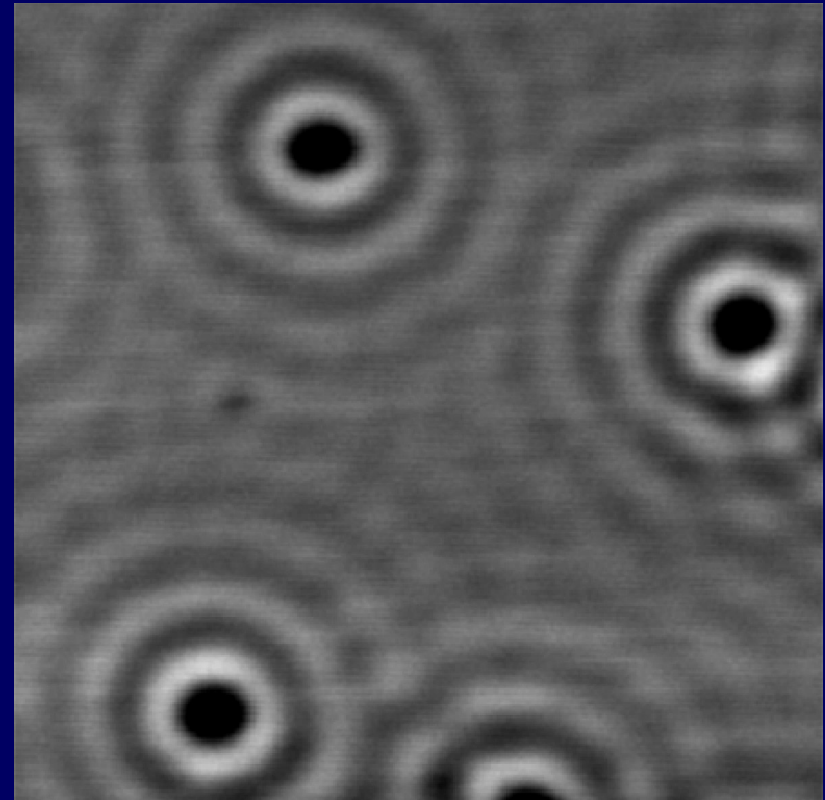


10 Å

$$\lambda_F = 3 \text{ Å}$$

$$\text{LDOS} \approx \cos(2k_F r)/r^5$$

Surface State
substitutional defects on Ag(111)

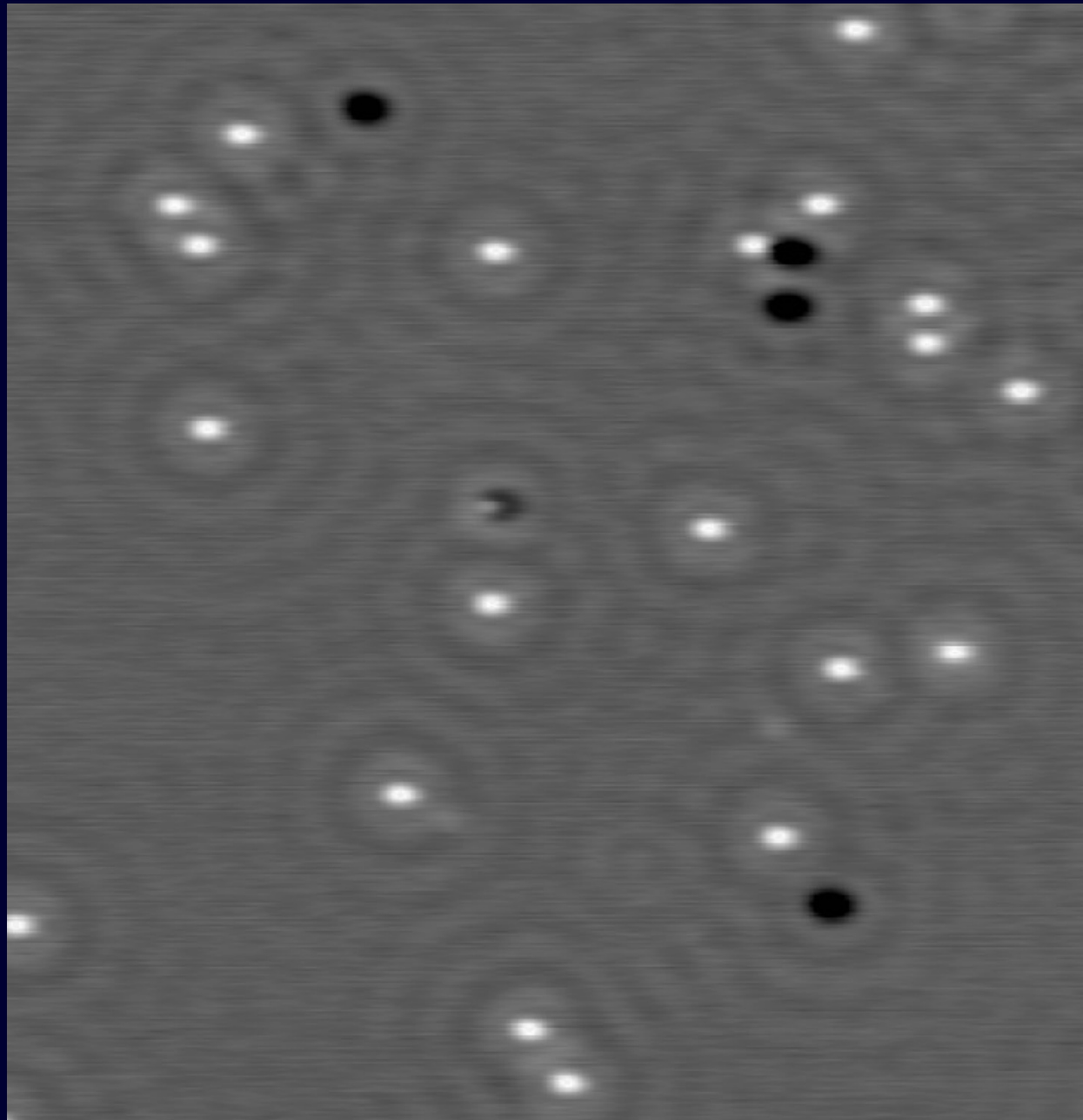


100 Å

$$\lambda_F = 75 \text{ Å}$$

$$\text{LDOS} \approx \cos(2k_F r)/r^2$$

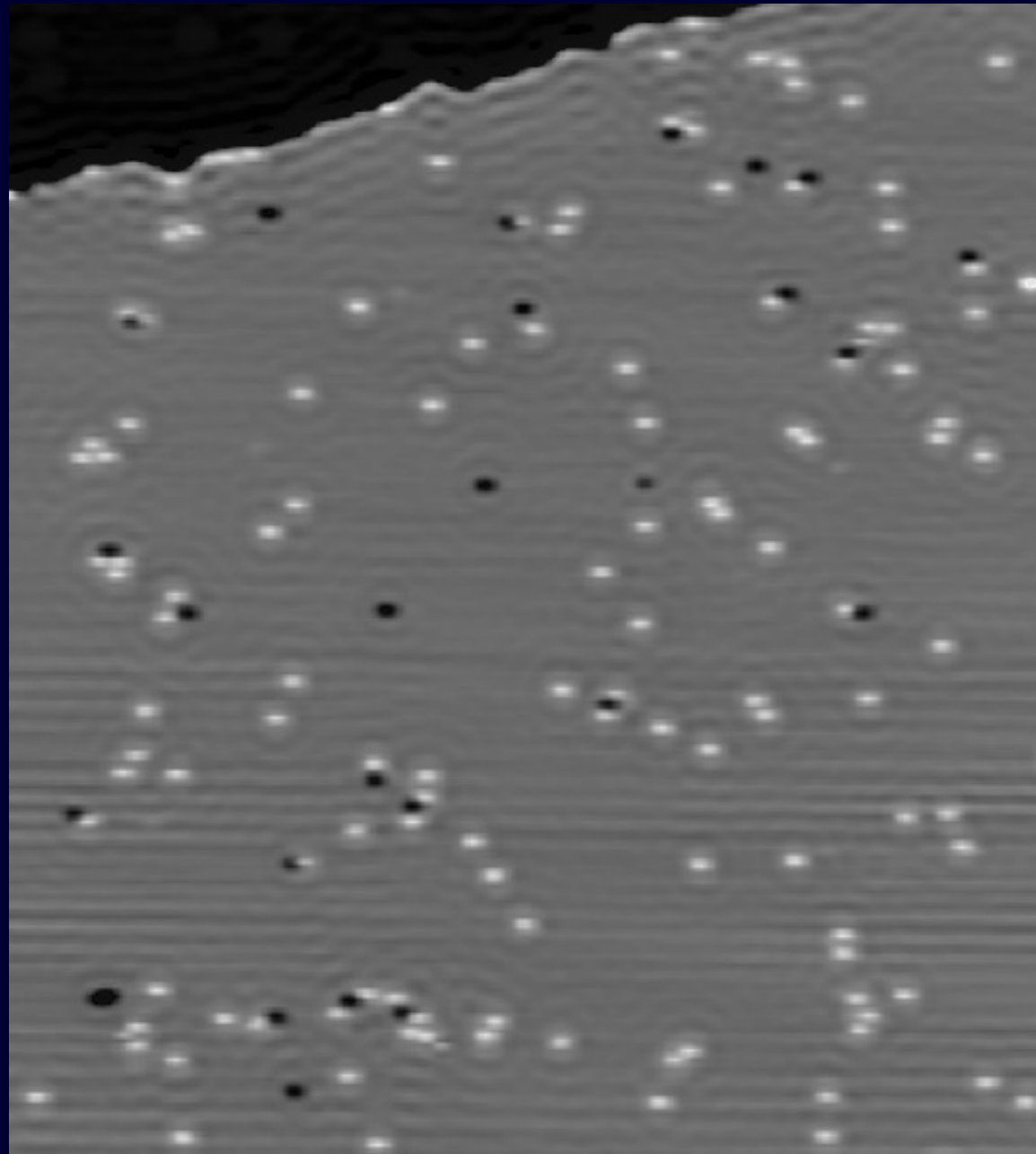
Watching tracer diffusion: Cu/Cu(111)



100 Å

$T = 13.5 \text{ K}$, $\Theta = 1.4 \times 10^{-3} \text{ ML}$

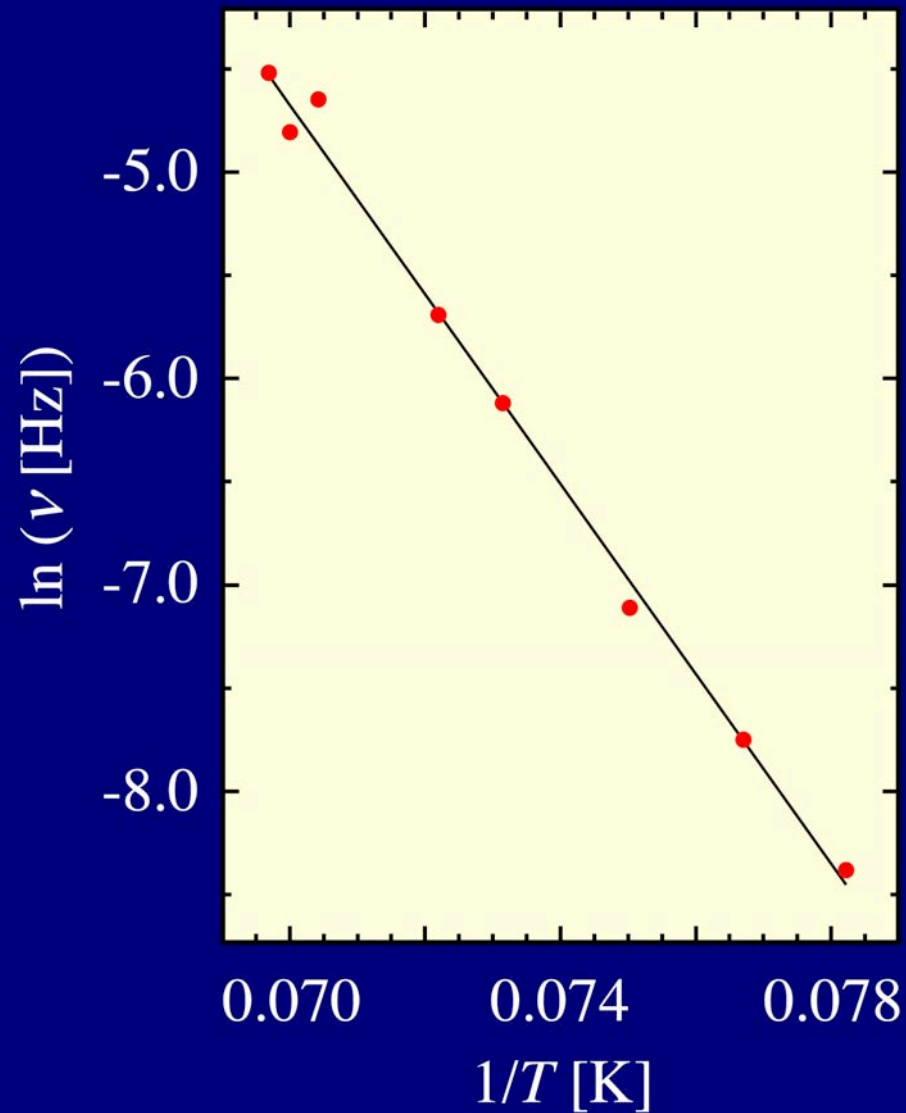
Watching tracer diffusion: Cu/Cu(111)



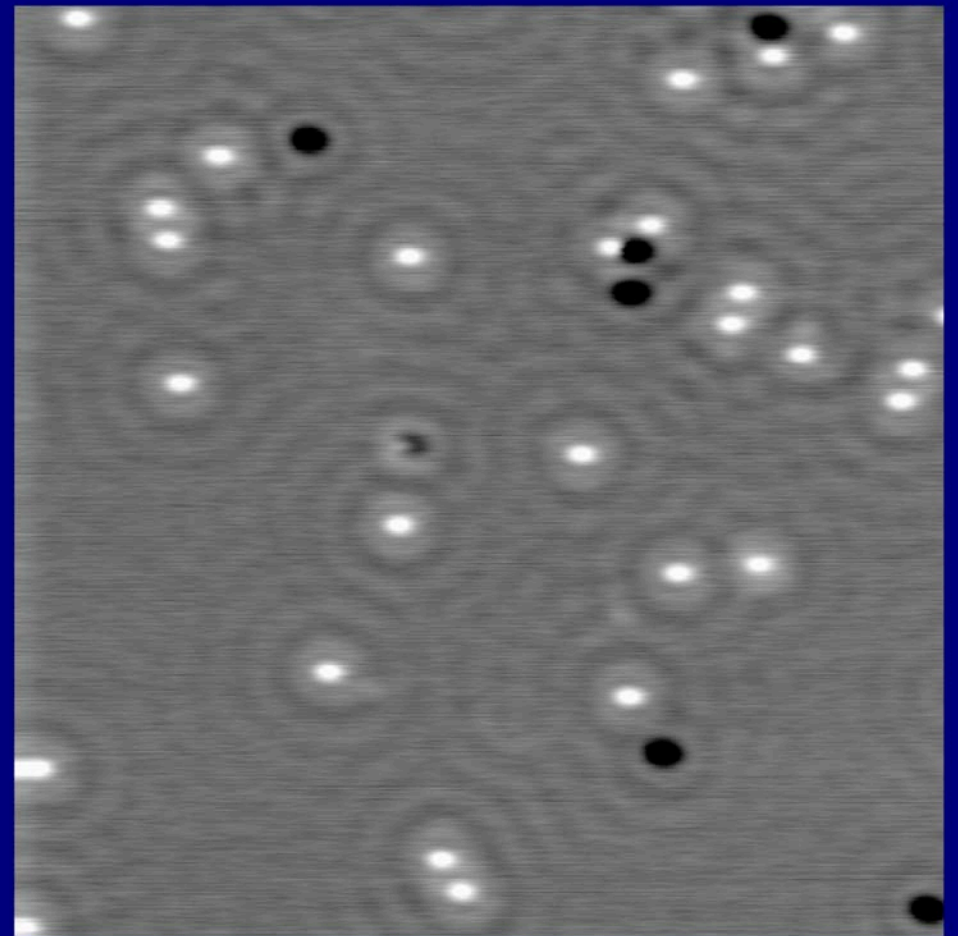
100 Å

$T = 15.6 \text{ K}$, $\Theta = 1.4 \times 10^{-3} \text{ ML}$

Tracing Cu monomer diffusion Cu(111)



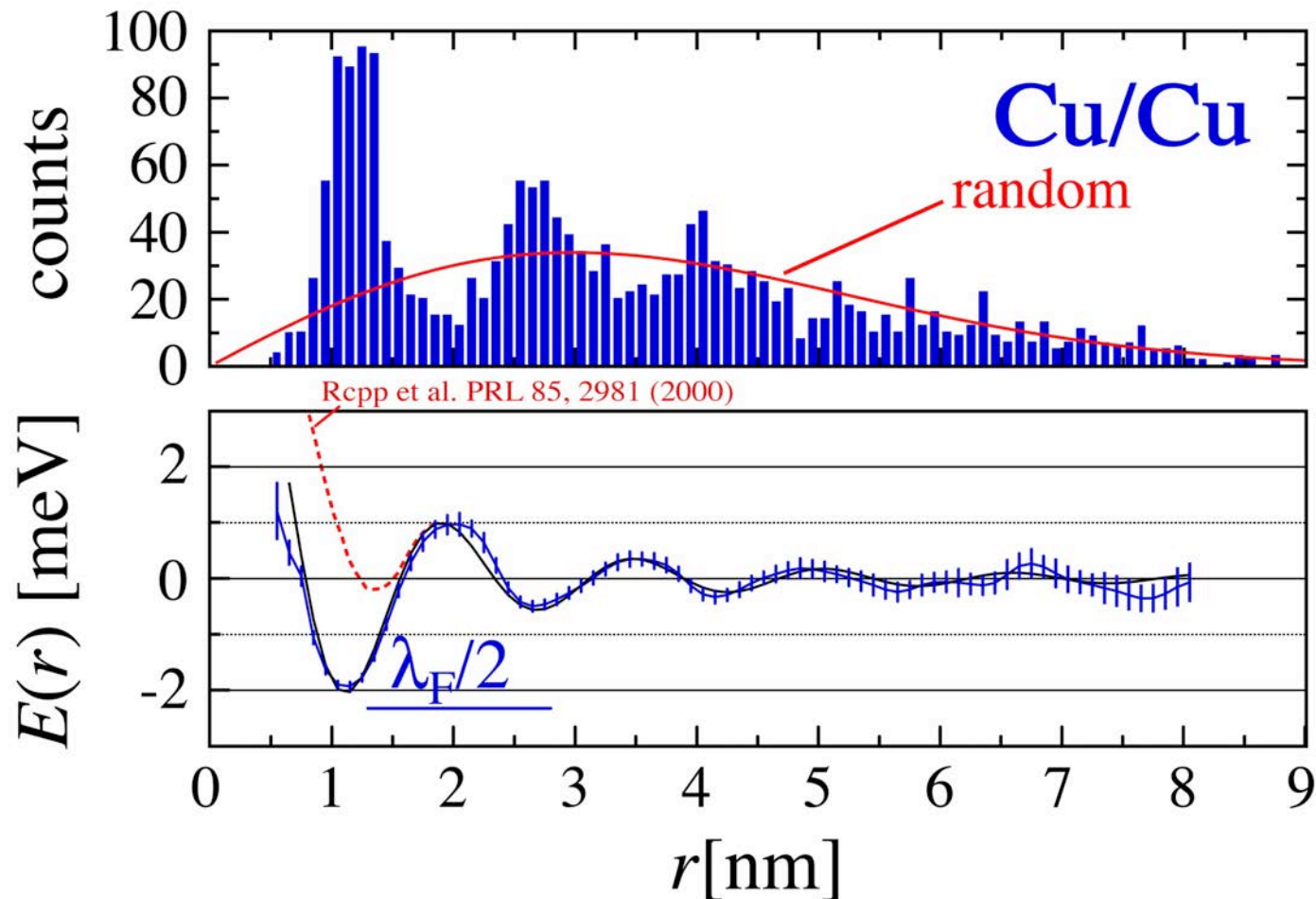
$$E_m = 40 \pm 1 \text{ meV} \quad \nu_0 = 1 \times 10^{12.0 \pm 0.5} \text{ s}^{-1}$$



$$T = 13.5 \text{ K}, \Theta = 1.4 \times 10^{-3} \text{ ML}$$

$$V_t = 0.1 \text{ V}, I_t = 0.1 \text{ nA}$$

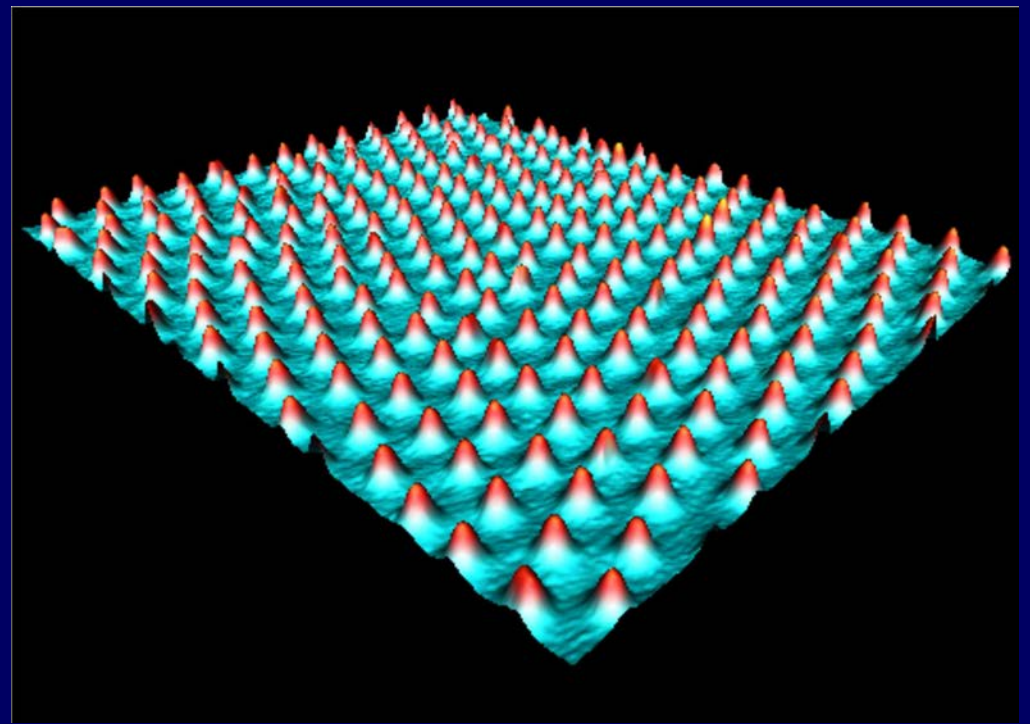
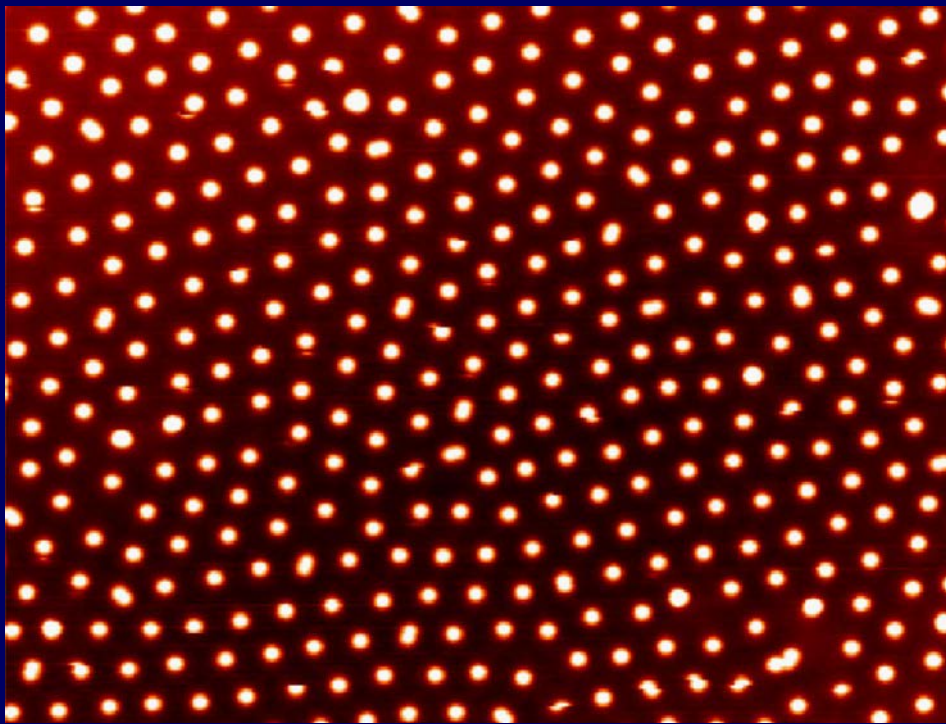
Long range interactions show up in pair-distribution



$\Phi = (0.50 \pm 0.07) \pi$, $q = (0.20 \pm 0.01) \text{ \AA}^{-1}$, $k_{F, \text{Cu}(111)} = 0.21 \text{ \AA}^{-1}$
 prediction: Lau & Kohn (1978), model: Hyldgaard & Persson, JPCM (2000)

Short-range repulsion of 14 meV !

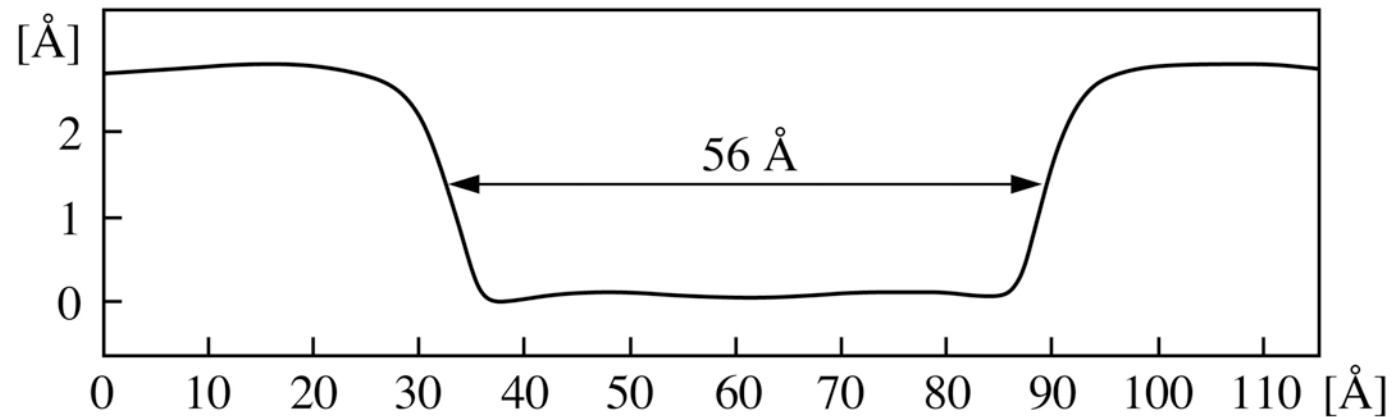
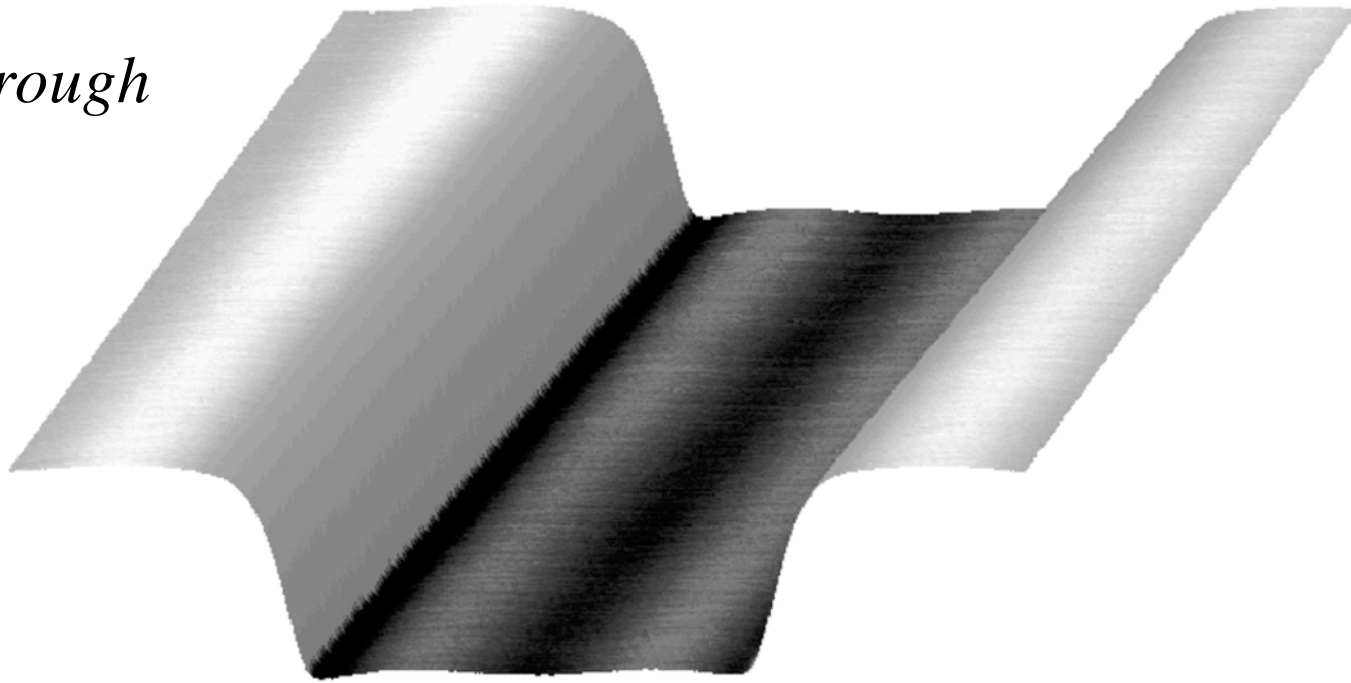
$Ce/Ag(111)$



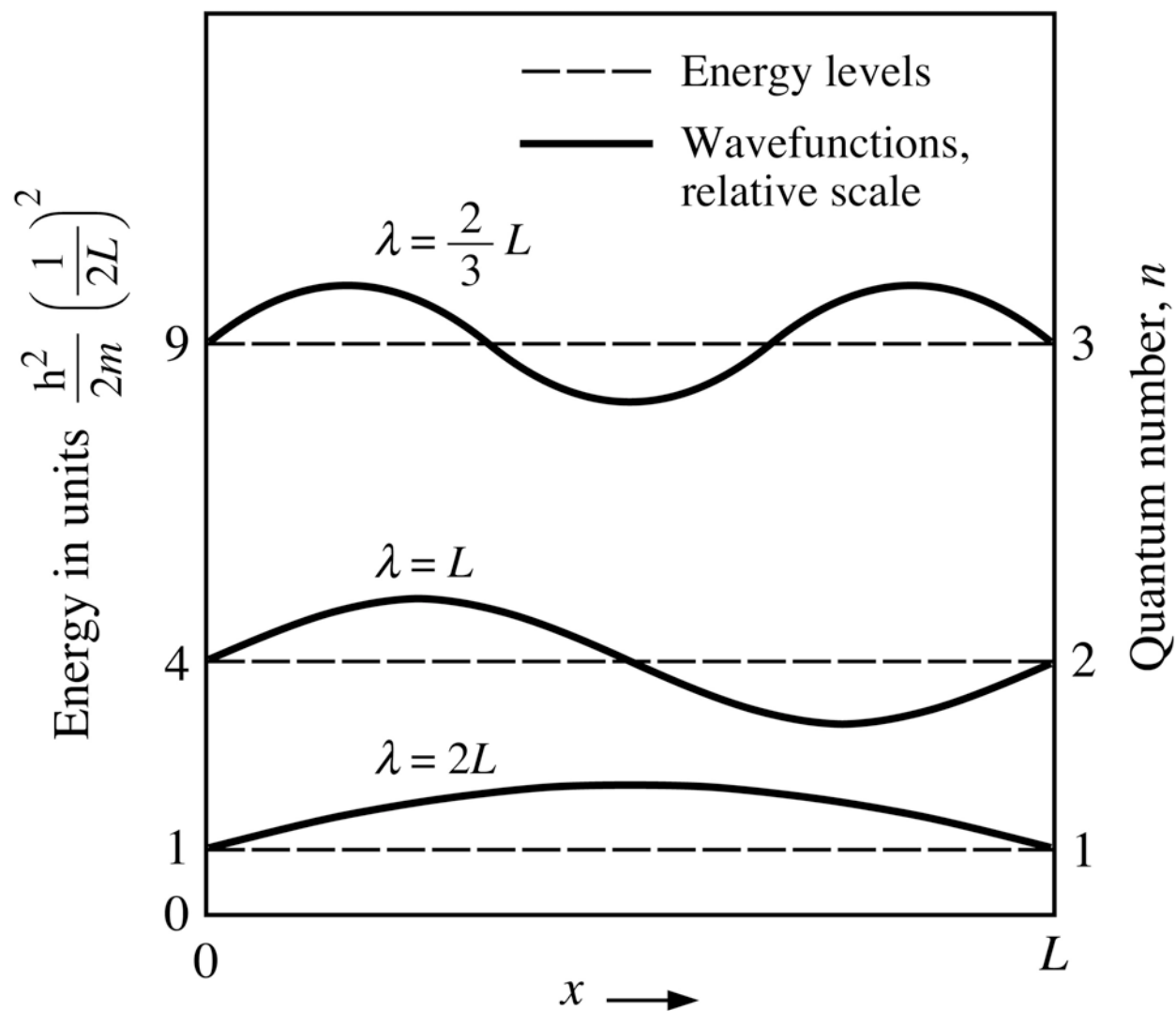
10 \AA

Quantum Confinement

*Quantum trough
on Ag(111)*

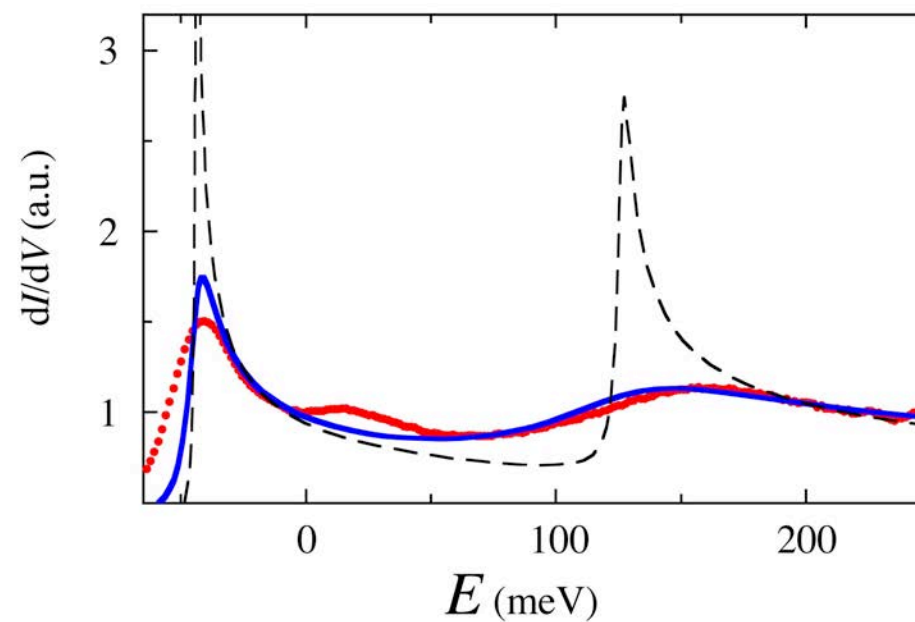
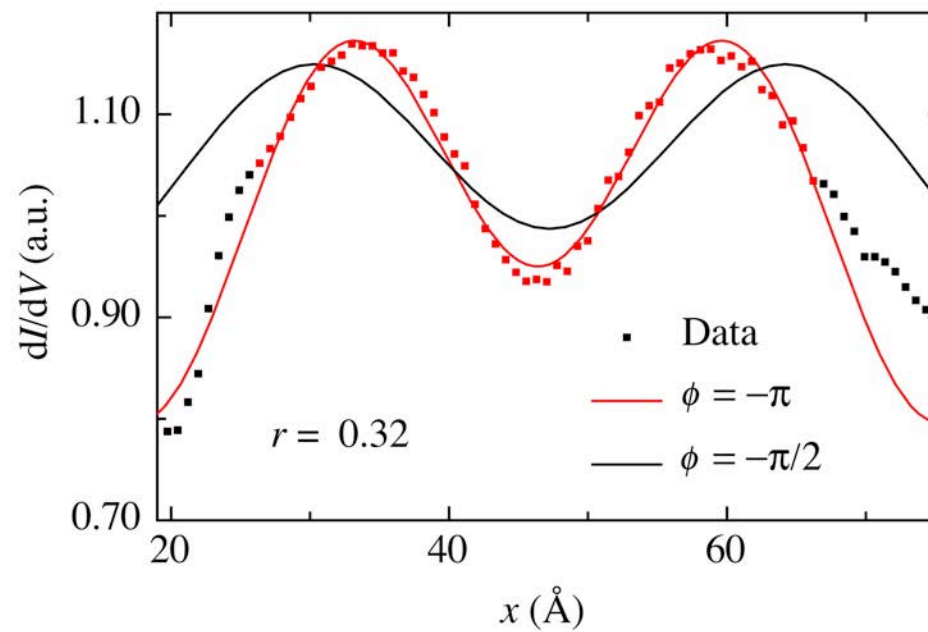
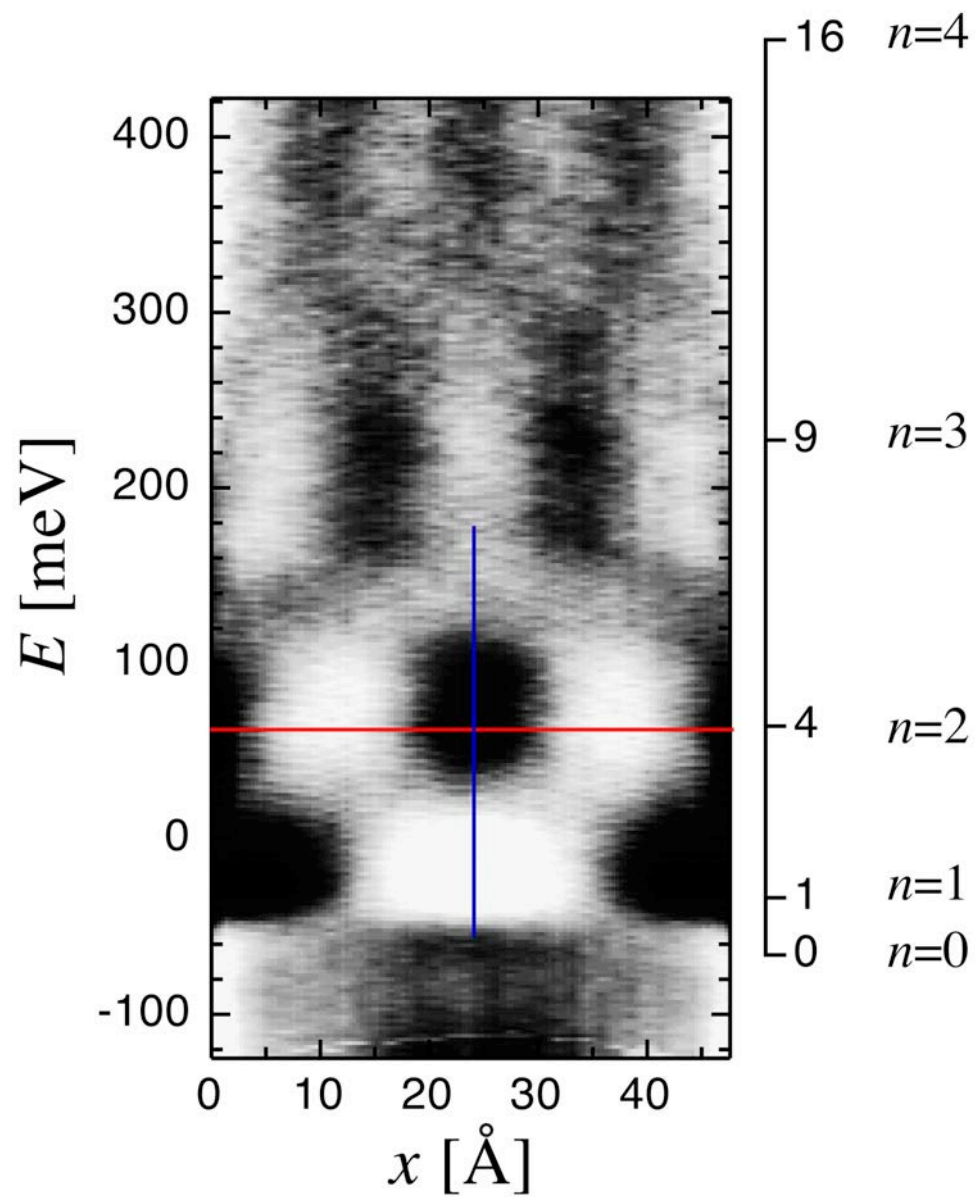


Particle in box of width L

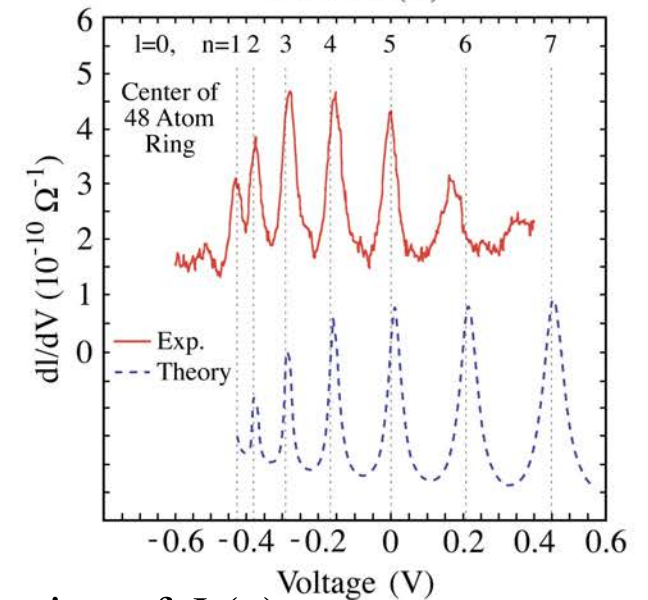
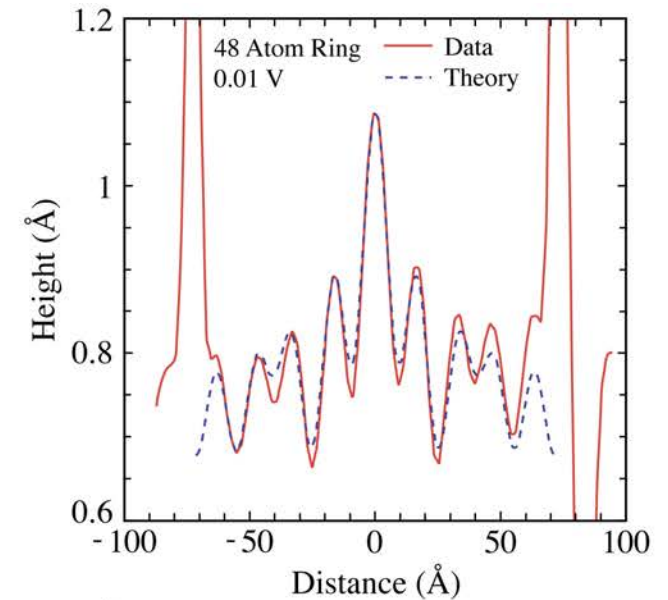
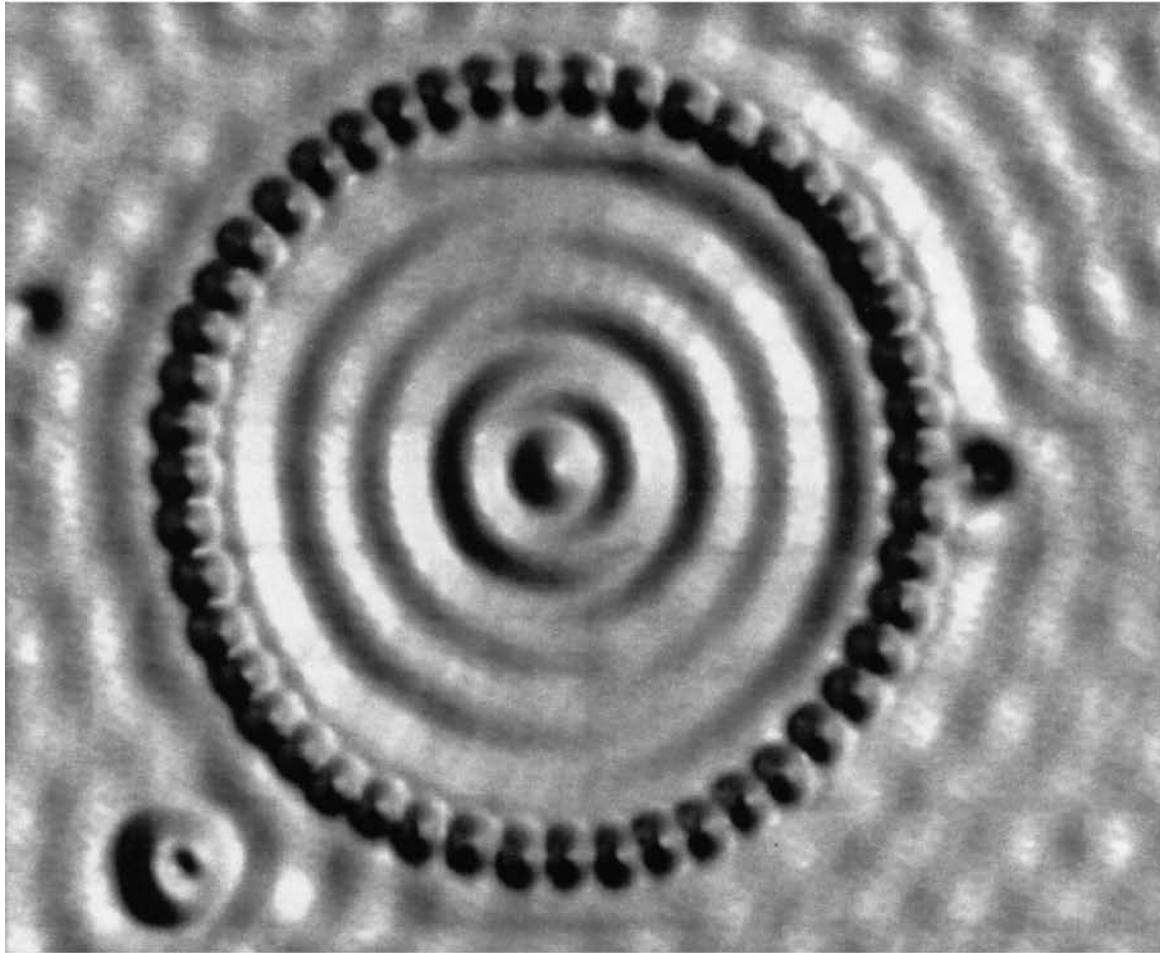


$$E_n = \frac{h^2}{2m} k_n^2 = \frac{h^2}{2m} \left(\frac{2\pi}{\lambda_n} \right)^2 = \frac{h^2}{2m} \left(\frac{n}{2L} \right)^2$$

LDOS in Quantum trough



Electrons in Quantum Corral: Fe/Cu(111)

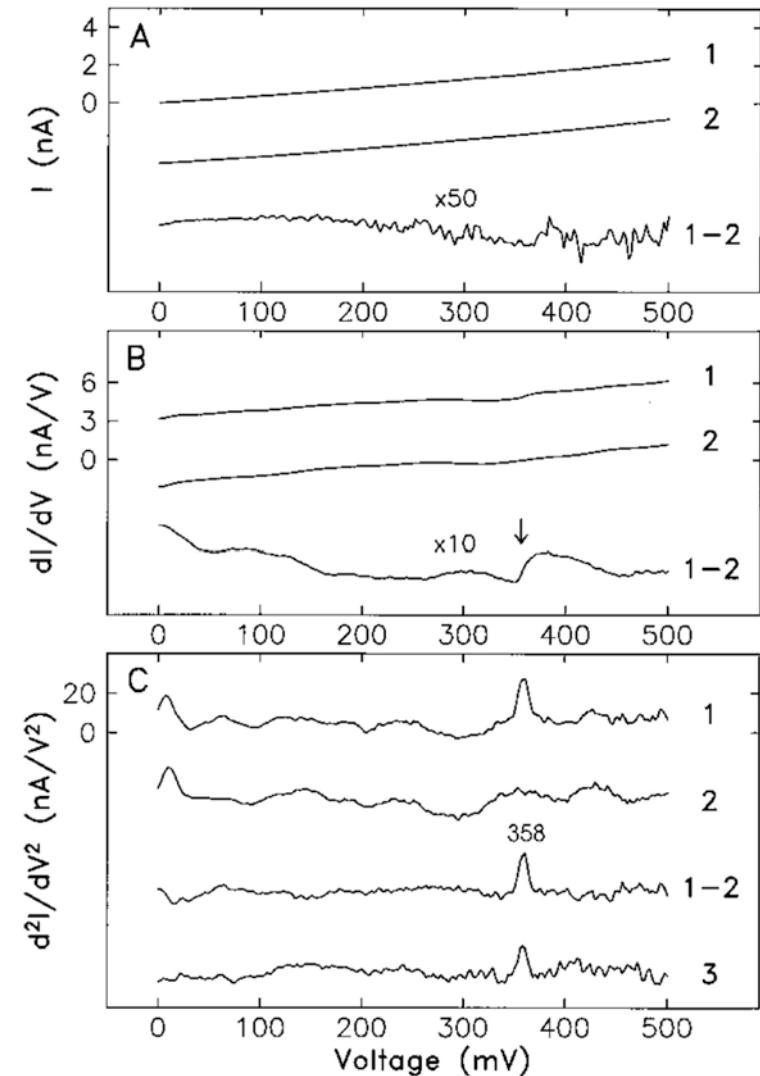
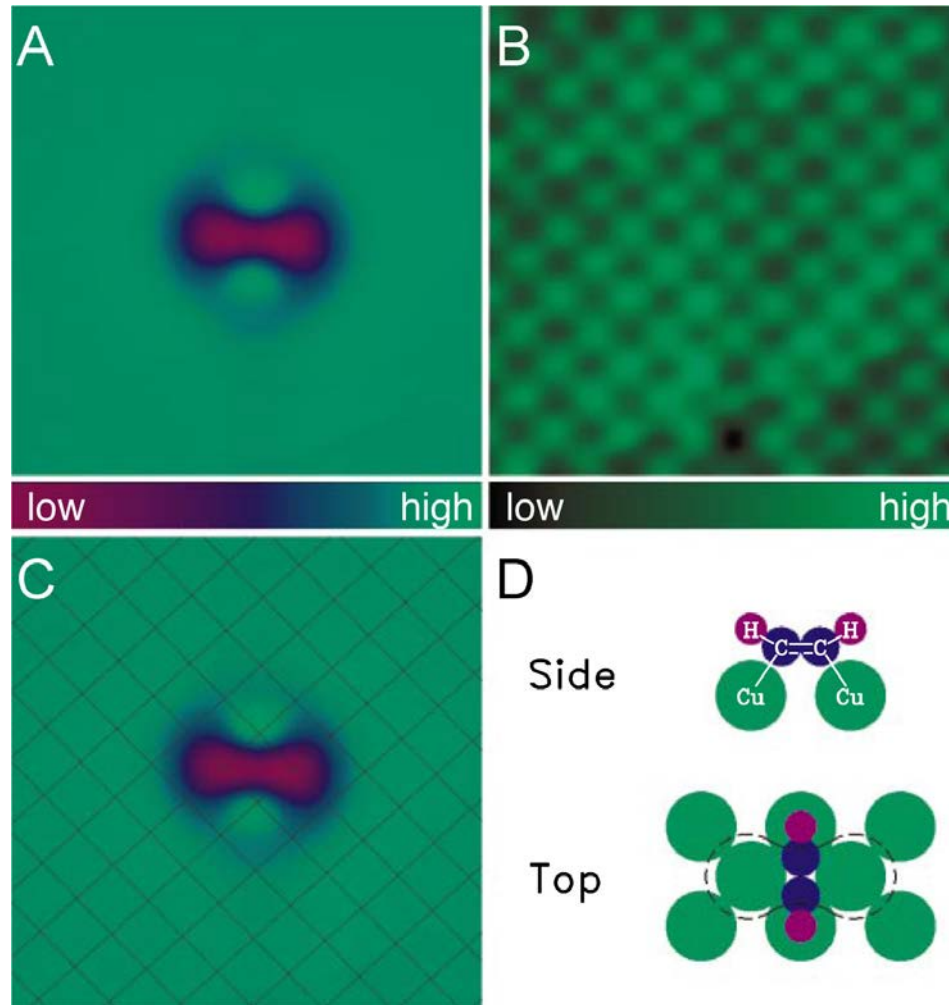


$$\Delta LDOS(x) = \frac{1}{kx} \left(\cos^2(kx - \frac{\pi}{4} + \delta_0) - \cos^2(kx - \frac{\pi}{4}) \right), k = \sqrt{\frac{2m^*E}{\hbar^2}}$$

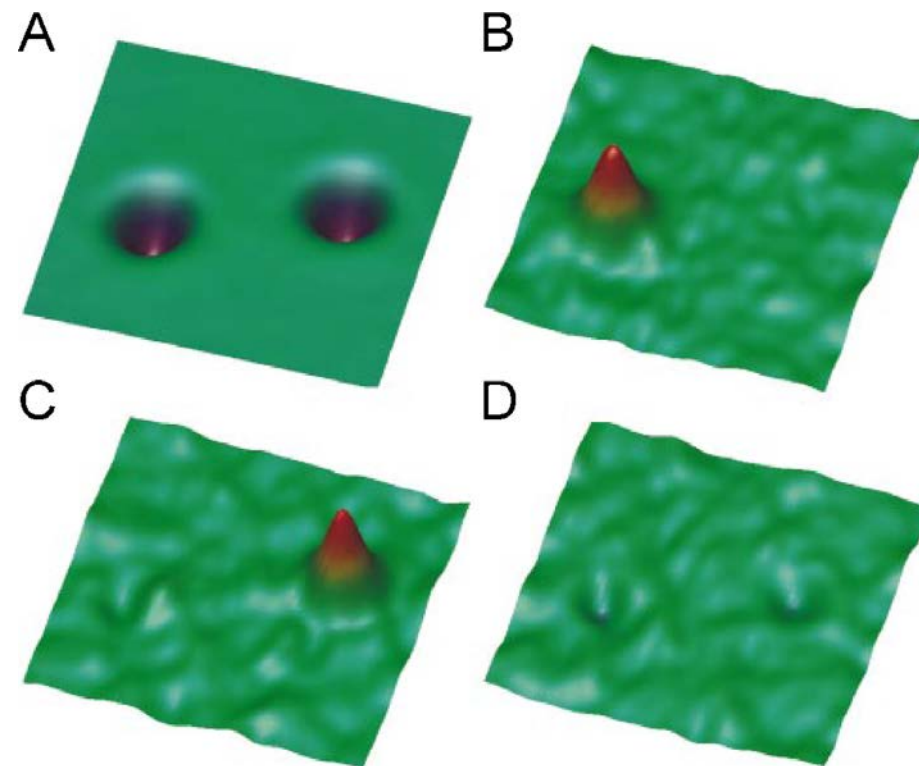
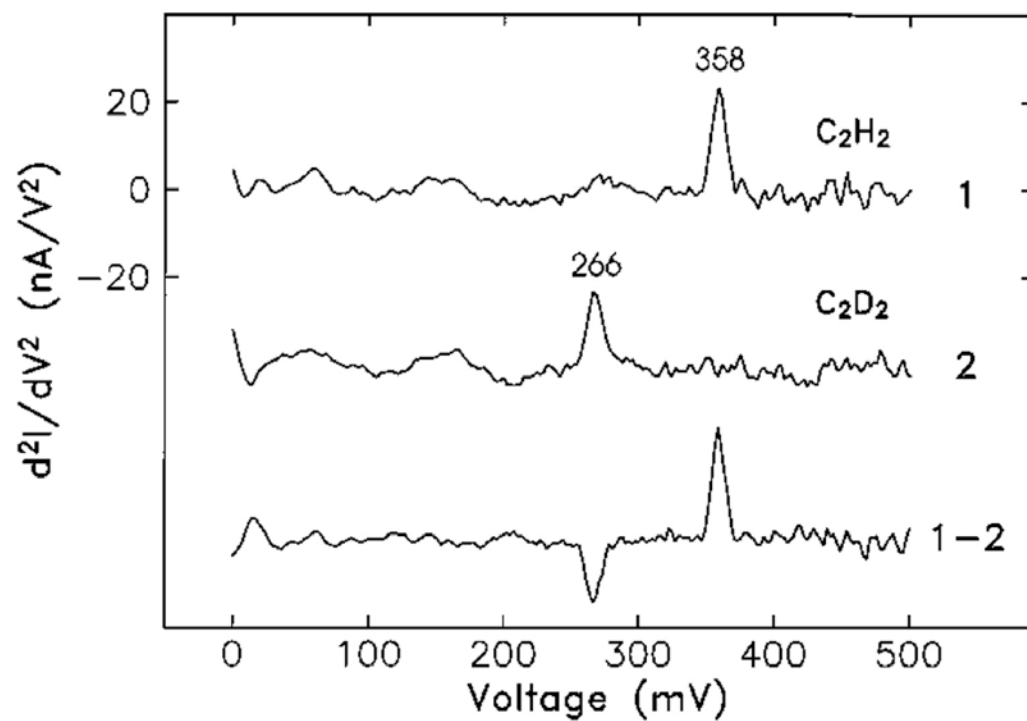
$$\Psi_{n,l}(x, \Phi) = \text{const.} \cdot J_l(k_{n,l}x) e^{il\Phi}, \text{ with } k_{n,l} = \frac{z_{n,l}}{r}, z_{n,l} \text{ n'th zero-crossing of } J_l(z)$$

Inelastic Electron Tunneling Spectroscopy (IETS)

Detecting vibrational quantum levels for $C_2H_2/Cu(100)$

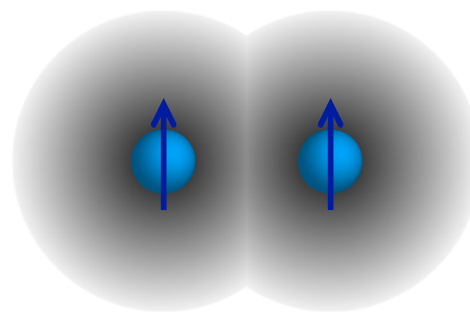


Isotope Effect – C_2H_2 vs. $C_2D_2/Cu(100)$





Para and Ortho Species in Homonuclear Diatomics



$$\Psi_{\text{tot}} = \Psi_{\text{el}} \Psi_{\text{vib}} \Psi_{\text{nuc}} \Psi_{\text{rot}}$$

W. Heisenberg, Z. Phys. **41**, 239 (1927).

The first preparation of pure para H₂ enabled the confirmation by emission spectra and heat conductivity measurements in the gas phase

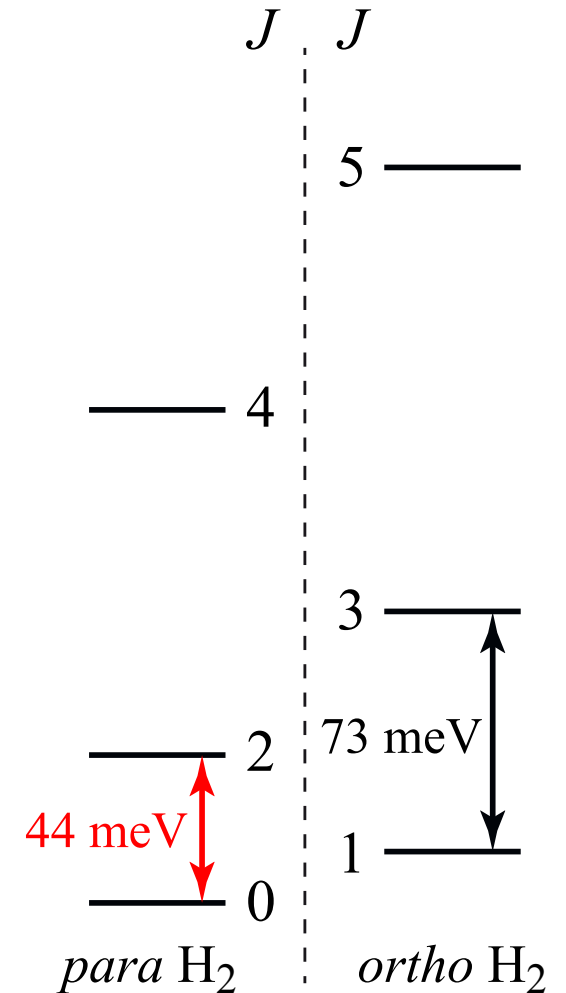
K. F. Bonhoeffer and P. Harteck, Z. Phys. Chem. B **4**, 113 (1929).

Example: Hydrogen and Deuterium

$I_N = 1/2$ Fermions

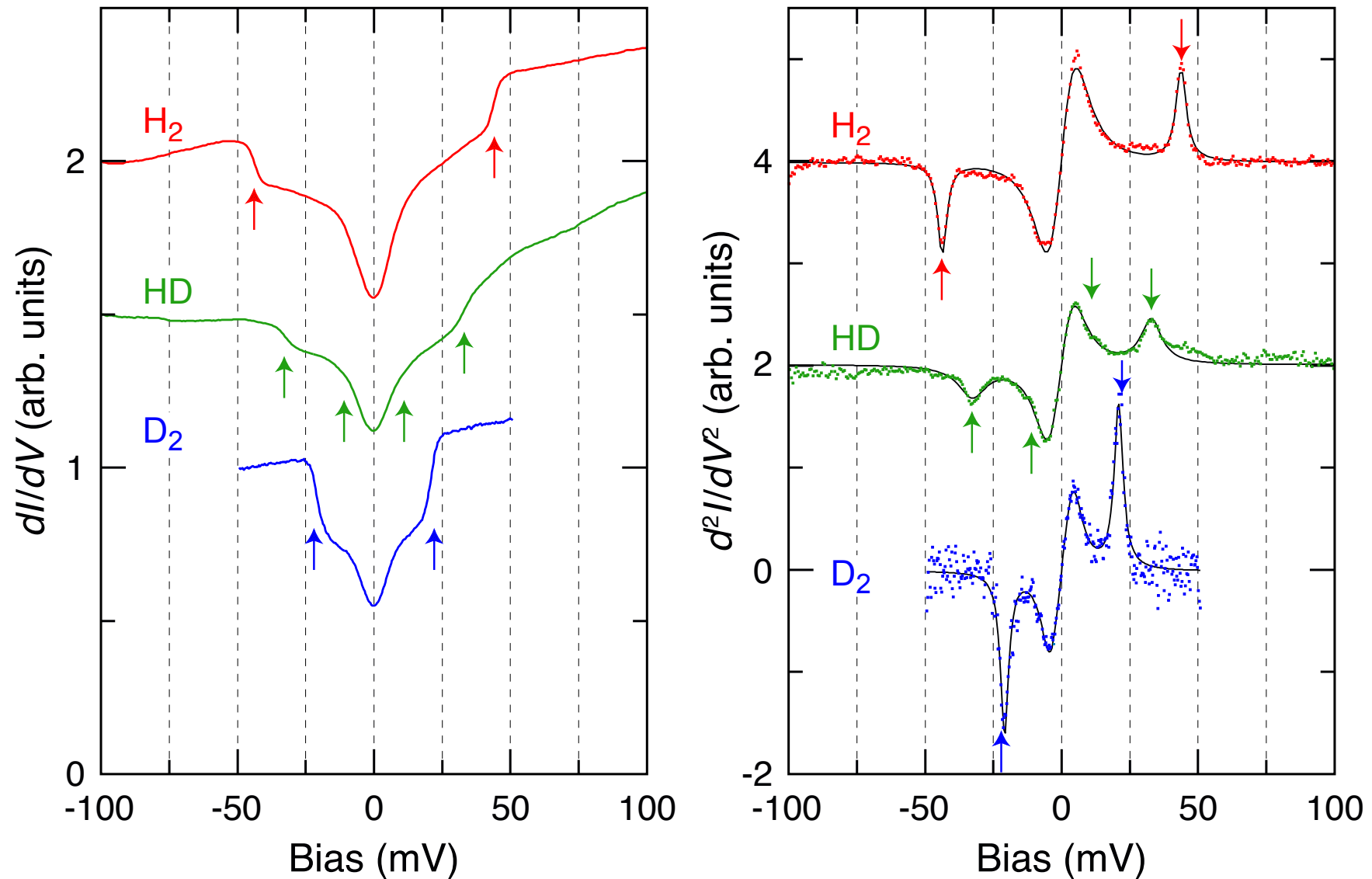
Molecule	Ψ_{tot}	Ψ_{nuc}	Ψ_{rot}
<i>para</i> -H ₂	AS	AS	S (even J)
<i>ortho</i> -H ₂	AS	S	AS (odd J)
<i>ortho</i> -D ₂	S	S	S (even J)
<i>para</i> -D ₂	S	AS	AS (odd J)

$I_N = 1$ Bosons



Detection of rotational quantum levels

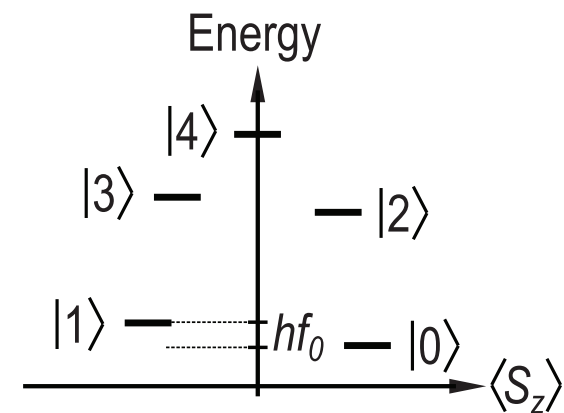
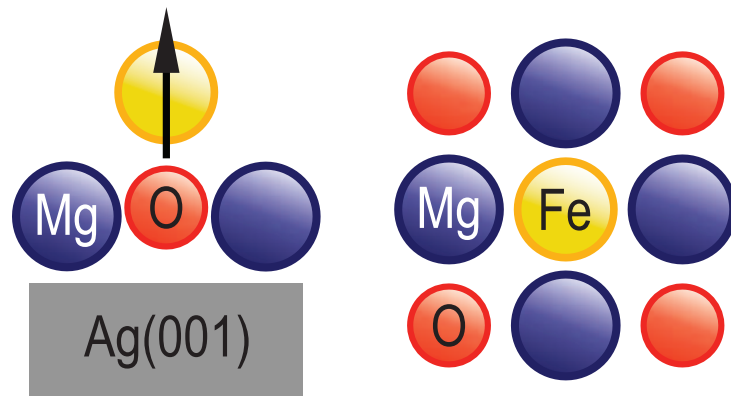
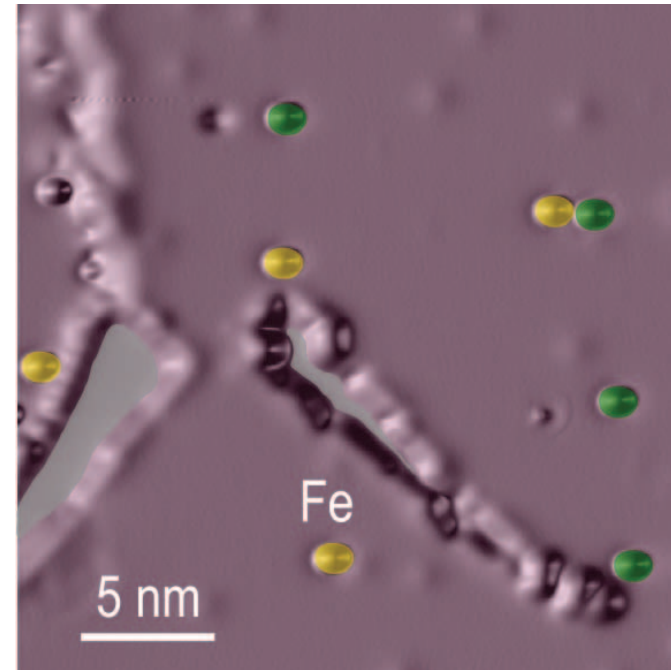
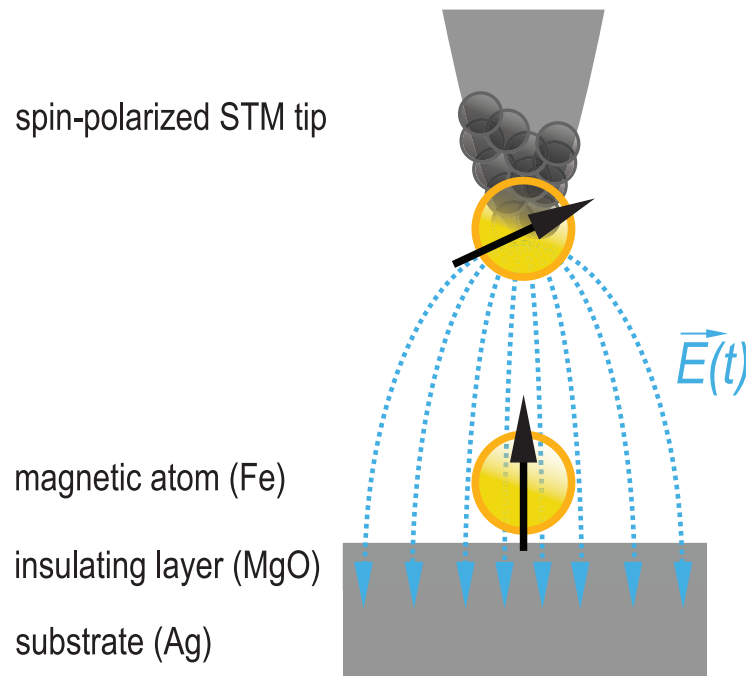
STM-IETS on H_2 , D_2 , and HD / $h\text{-BN}$ / $\text{Ni}(111)$



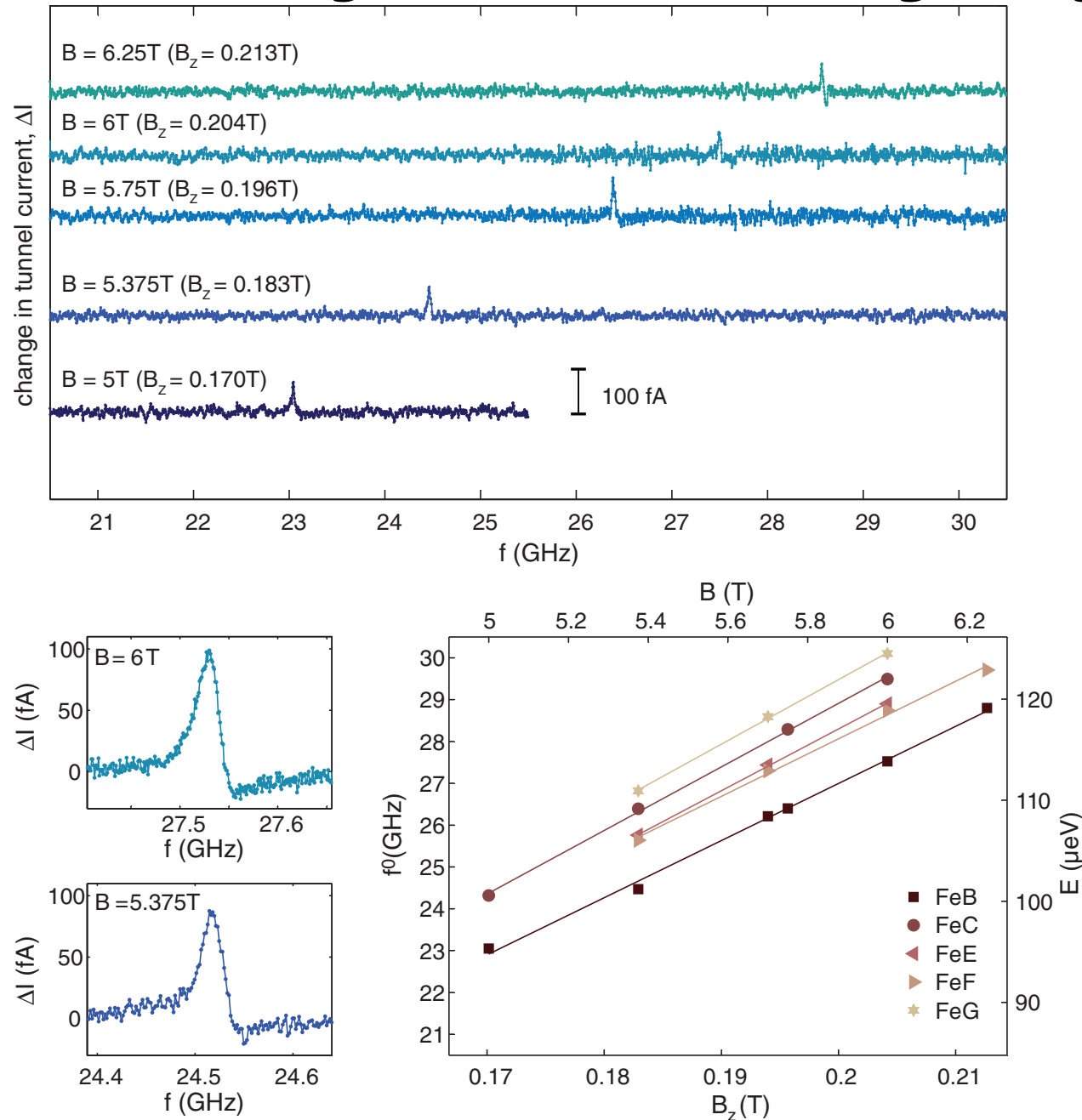
$R_g = 10^9 \Omega$, $T = 4.2 \text{ K}$

F. D. Natterer *et al.* PRL **111**, 175303 (2013).

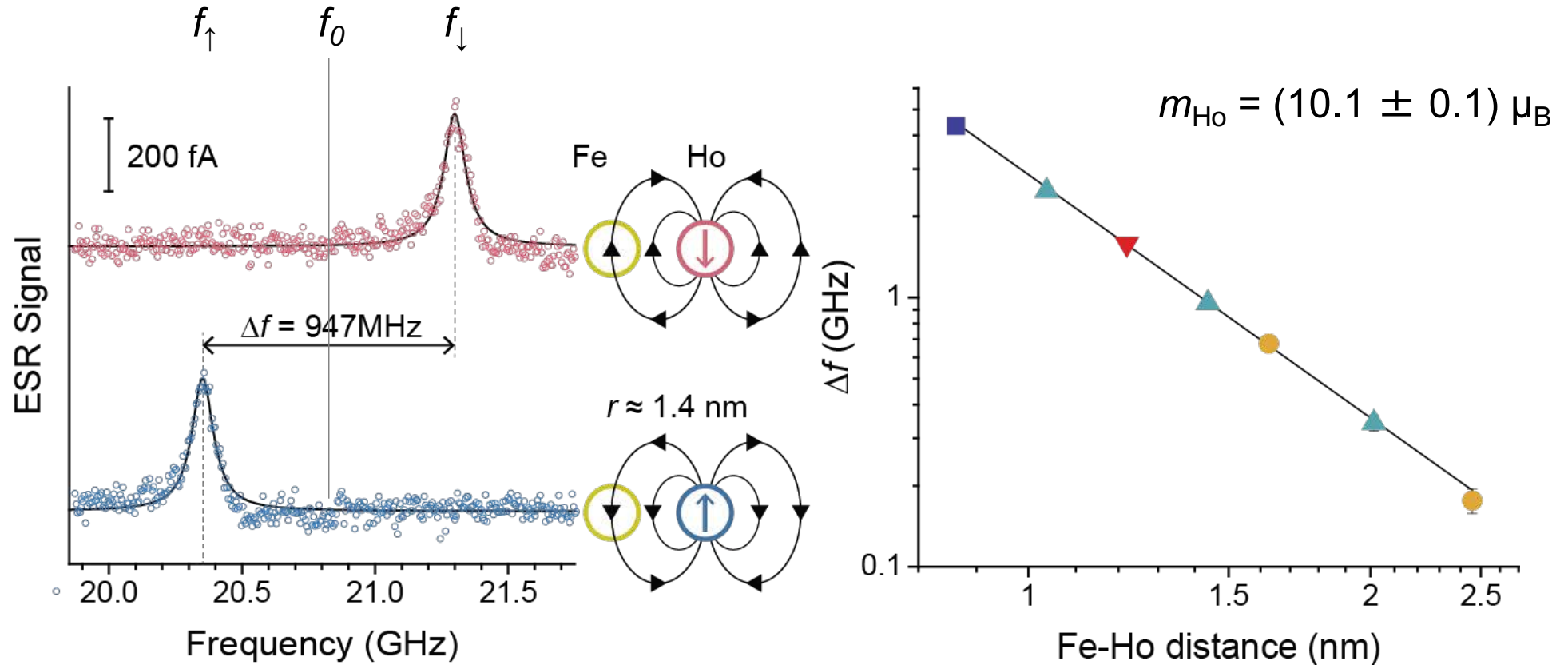
Electron Spin Resonance (ESR) with the STM



ESR-STM on single Fe atoms on MgO/Ag(100)

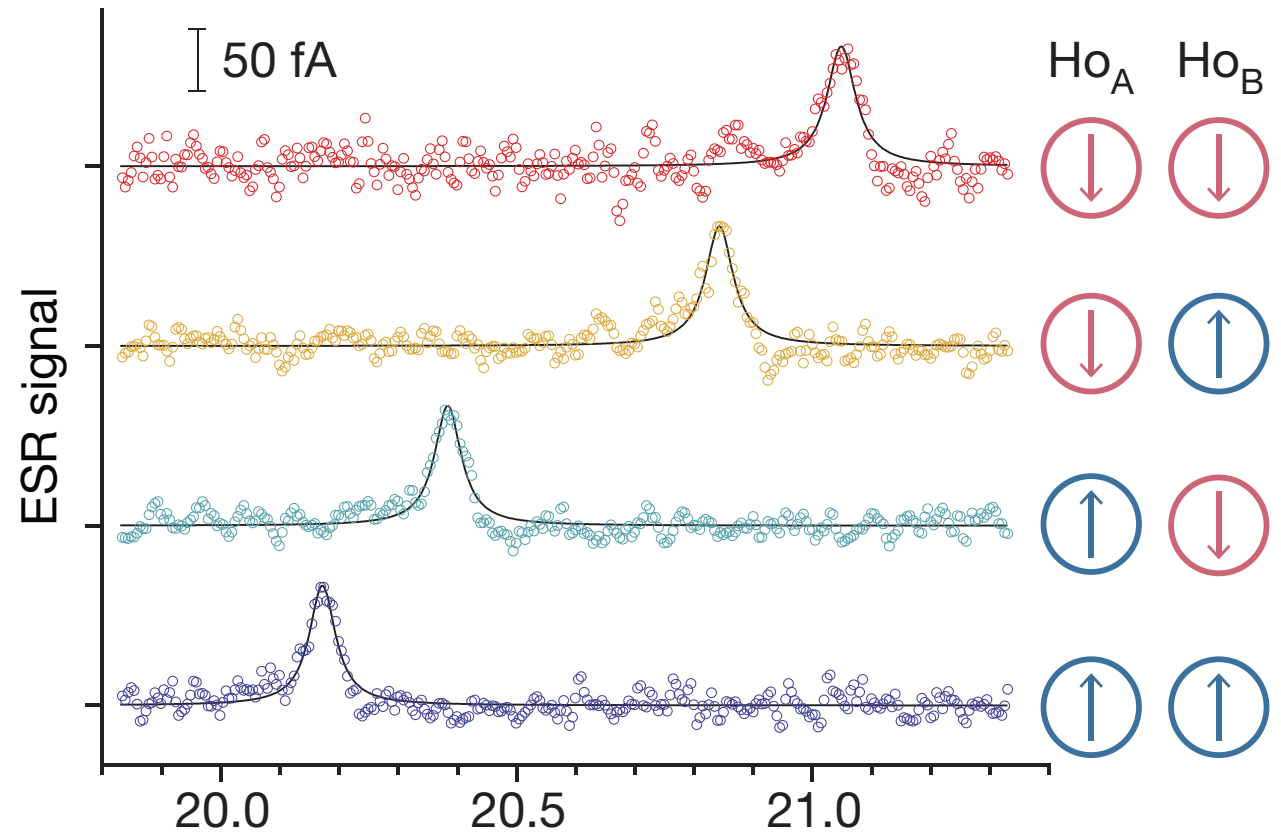
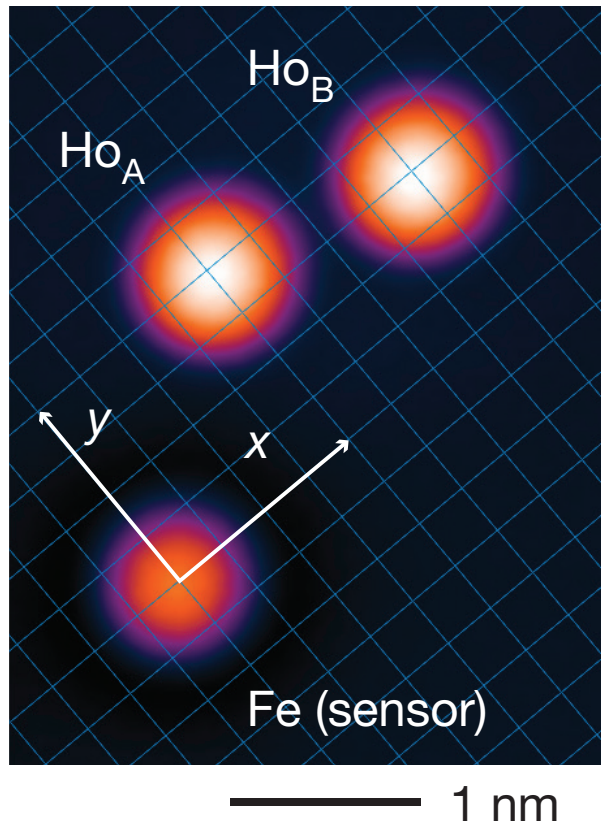


Coupling Ho to an Fe sensor – read with ESR-STM



Ho/MgO/Ag(100) first single atom magnet: F. Donati *et al.* Science **352**, 318 (2016);
Fe to read stray-field of Ho on MgO/Ag(100): F. D. Natterer *et al.* Nature **543**, 226 (2017).

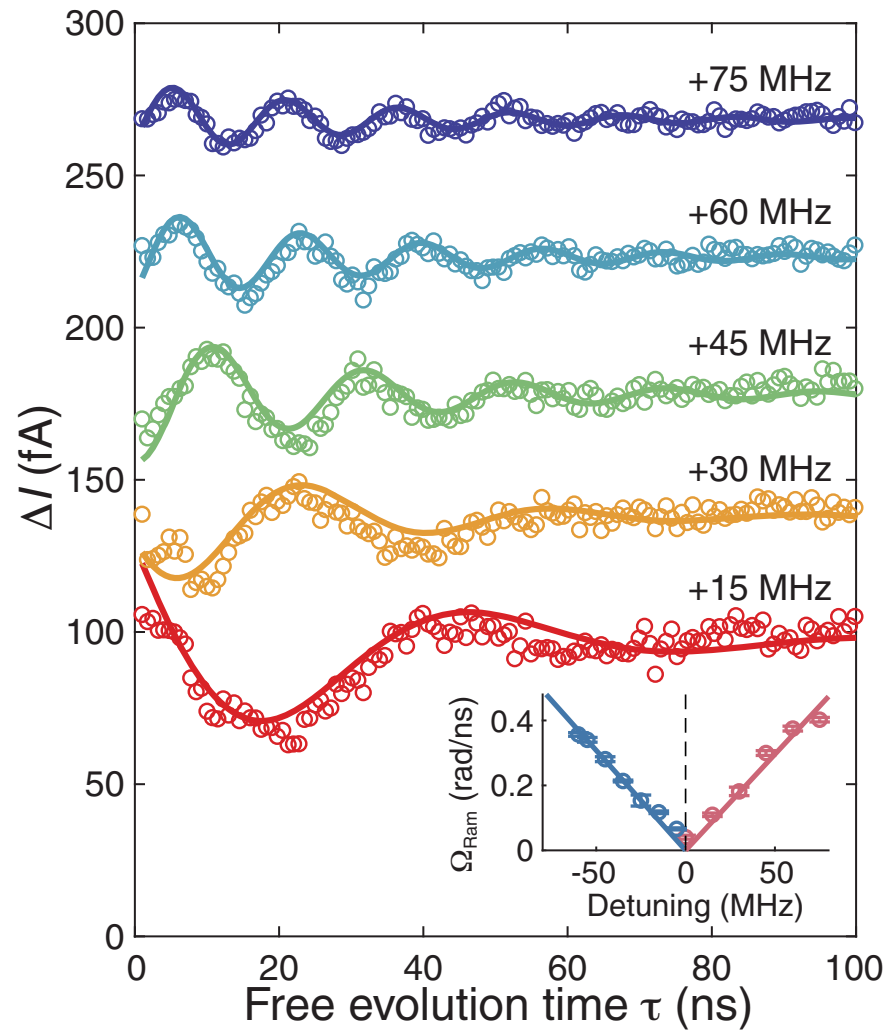
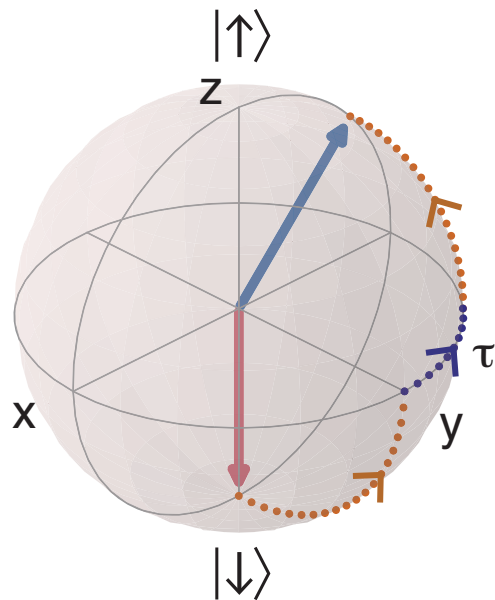
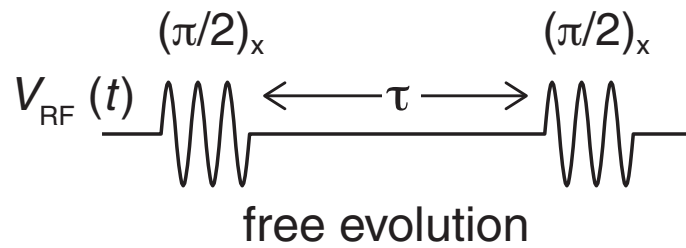
2 bit memory – ESR read-out on Fe sensor atom



no switching at 1.2 K for 5 h

F. D. Natterer *et al.* Nature **543**, 226 (2017).

TiH/MgO/Ag(100): coherent spin manipulation



$$T_{2, \text{Rabi}} = 40 \text{ ns} \quad T_2 = 189 \pm 23 \text{ ns}$$