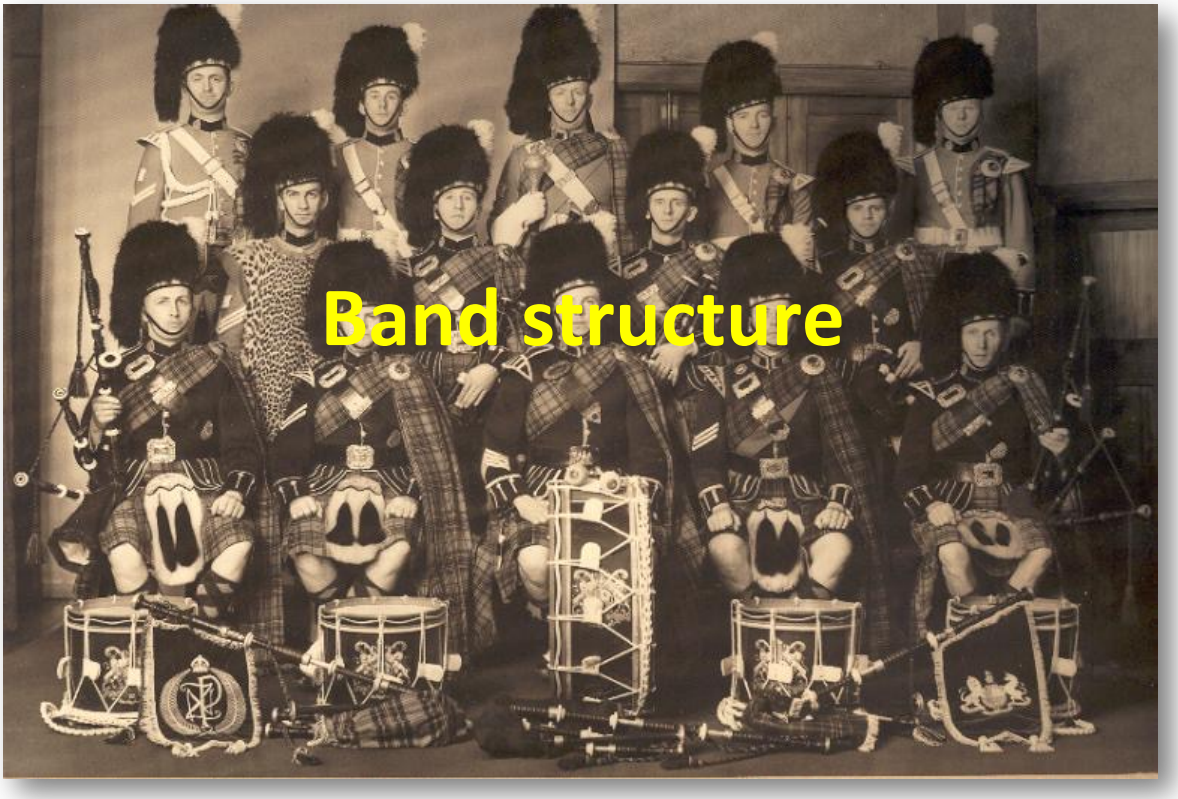
MSE 423 Fall 2024 – Week 10

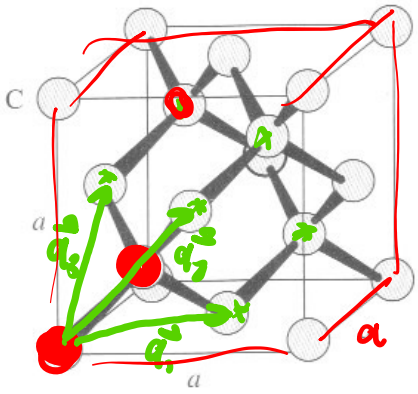


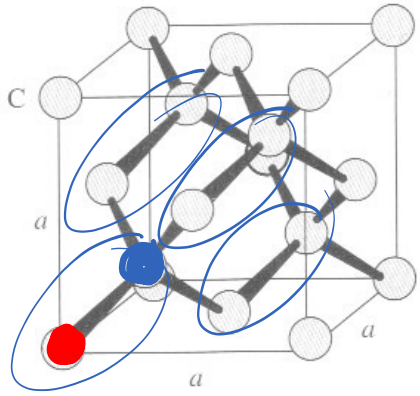
Last week

- Reciprocal lattice, and Brillouin zones
- Hamiltonian in a periodic potential, and graphical representation
- Bloch theorem, in two forms
- From k in extended space to 1st BZ + band index

Diamond and Zincblend

C - Si - Ge





DIAMOND: FCC LATTICE WITH A BASIS OF 2 ATOMS

ZINCBLEND: FCC LATTICE WITH A BASIS OF 2 DIFF. ATOM (Ga & As)

Brillouin Zone (fcc)

$\vec{b}_1 = 2\pi \frac{(\vec{a}_2 \times \vec{a}_3)}{\vec{a}_1 \cdot (\vec{a}_2 \times \vec{a}_3)}$

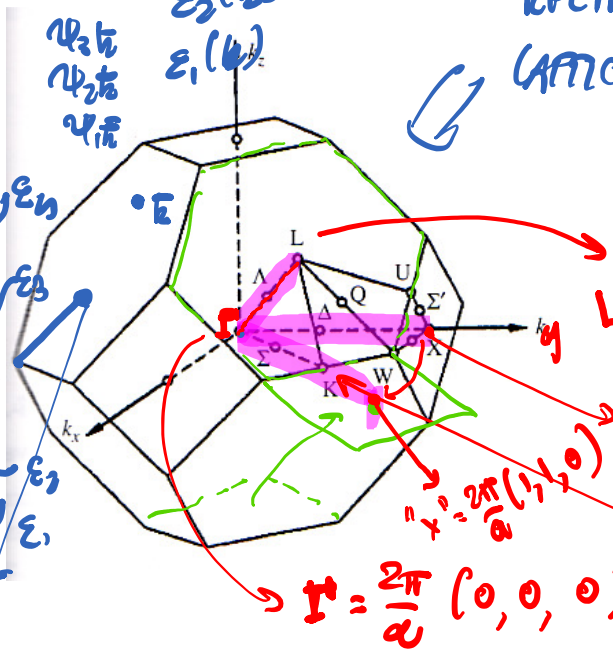
1st N. | 2nd N.

(1 1 1) | (1 0 0)
(1 1 $\bar{1}$) | (0 1 0)
(1 $\bar{1}$ 1) | (0 0 1)
($\bar{1}$ 1 1) | ($\bar{1}$ 0 0)
($\bar{1}$ $\bar{1}$ 1) | (0 $\bar{1}$ 0)
($\bar{1}$ 1 $\bar{1}$) | (0 0 $\bar{1}$)
(1 $\bar{1}$ $\bar{1}$)
($\bar{1}$ $\bar{1}$ $\bar{1}$)

$\varepsilon_3(k)$
$\varepsilon_2(k)$
$\varepsilon_1(k)$

$\psi_{2\pi}$
$\psi_{2\pi}$
$\psi_{1\pi}$

RECIPROCAL LATTICE IS BCC



$L = \frac{2\pi}{a}\left(\frac{1}{2}, \frac{1}{2}, \frac{1}{2}\right)$

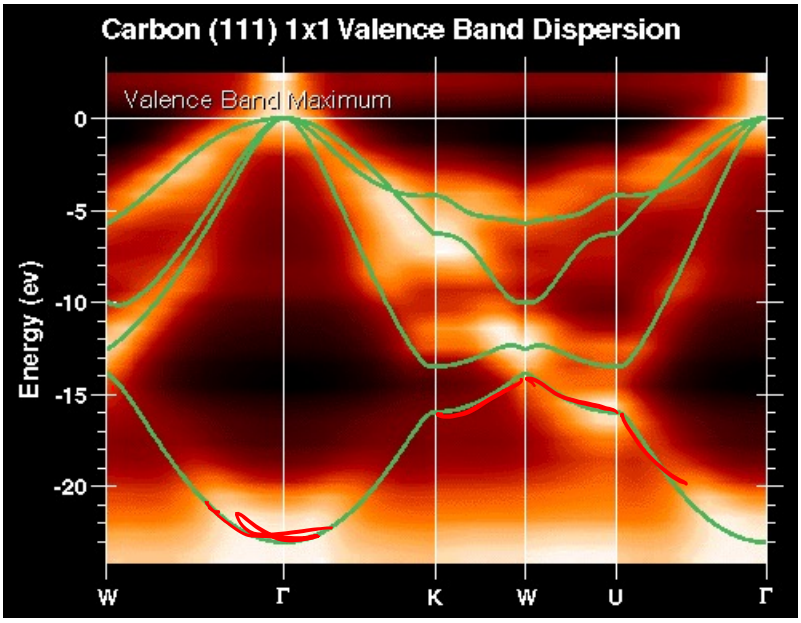
$X = \frac{2\pi}{a}(0, 1, 0)$

$"X" = \frac{2\pi}{a}(1, 1, 0)$

$K = \frac{2\pi}{a}\left(\frac{3}{4}, \frac{3}{4}, 0\right)$

$\Gamma = \frac{2\pi}{a}(0, 0, 0)$

Band Structure of Diamond



https://osscar-quantum-mechanics.materialscloud.io/voila/render/index.ipynb

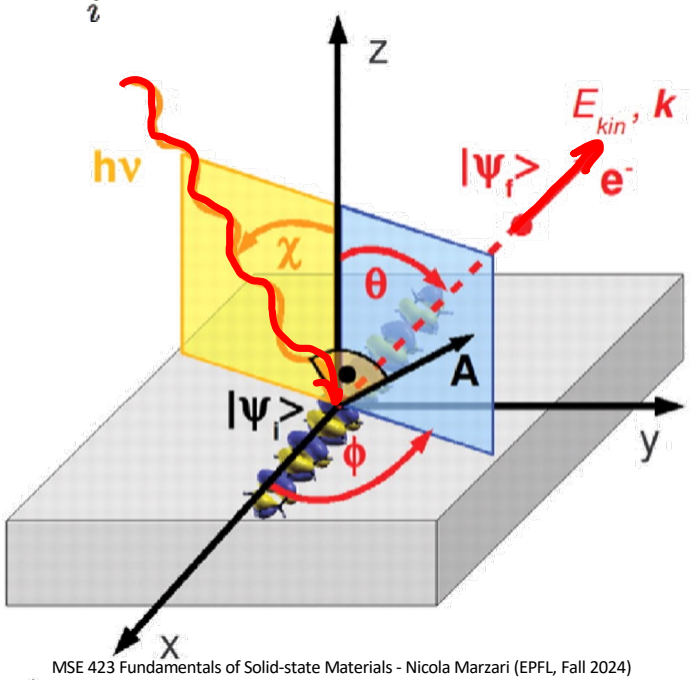
Section 2: **Band Theory of Crystals**

1. Fourier Transforms and Plane-Wave Expansions
2. Brillouin Zone
3. Free-Electron Bandstructure
4. Density of States
5. Norm-conserving Pseudopotentials

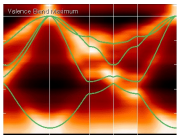
OSSCAR.ORG

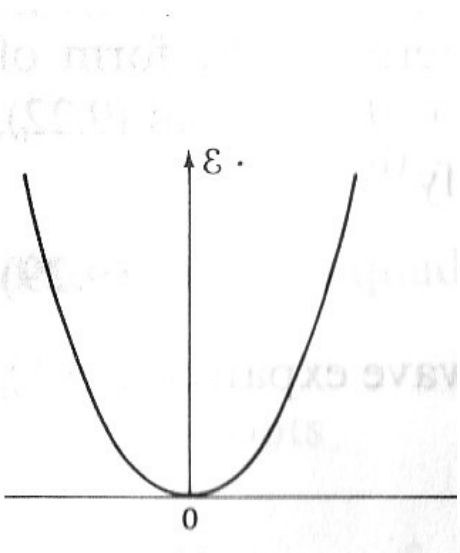
ARPES: Angle resolved photoemission spectroscopy

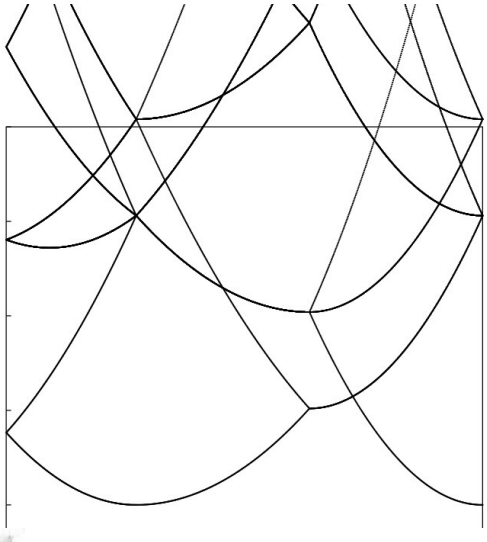
$$I(\omega) = \sum_i |\langle \varphi_f | \hat{H}_{\text{int}} | \varphi_i \rangle|^2 \delta(\epsilon_f - \epsilon_i - \hbar\omega)$$



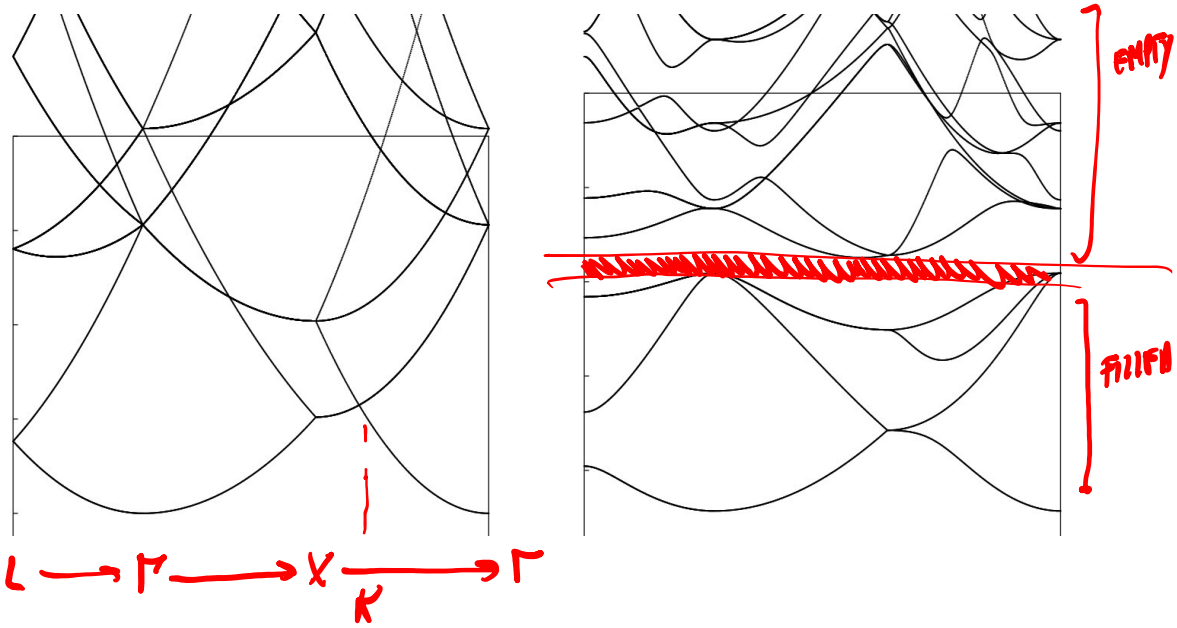
Why does it look like this?



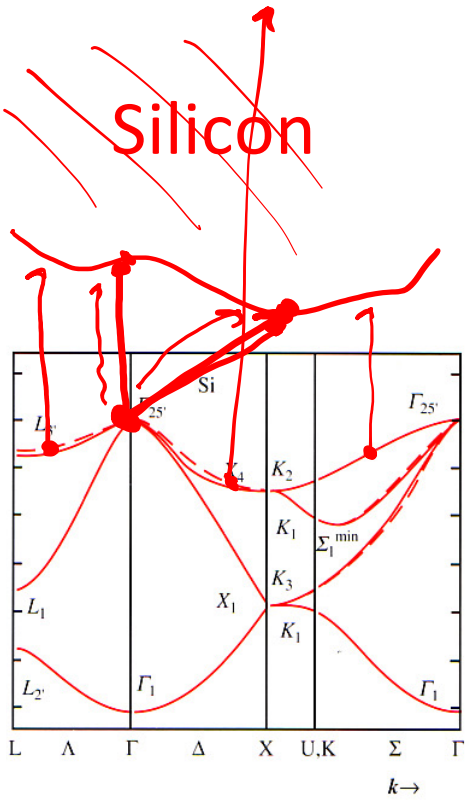




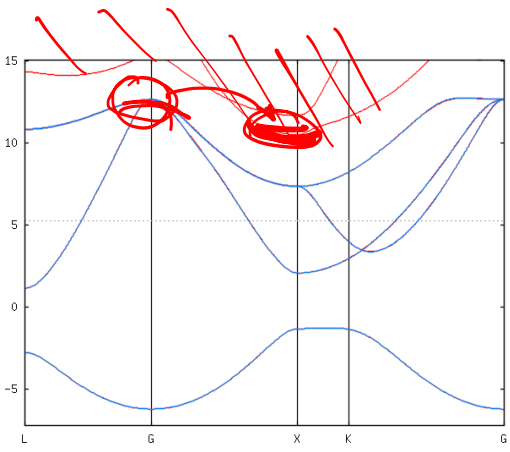
Band Structures: Free Electron Gas, Silicon



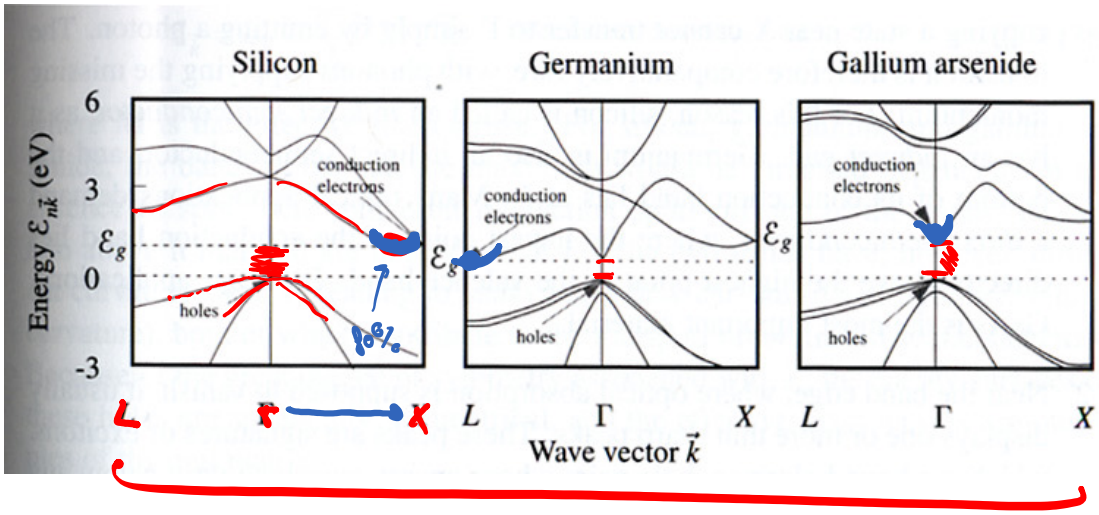
Silicon



Lead



Band structure of Si, Ge, GaAs



Conduction band minima (in 3d)

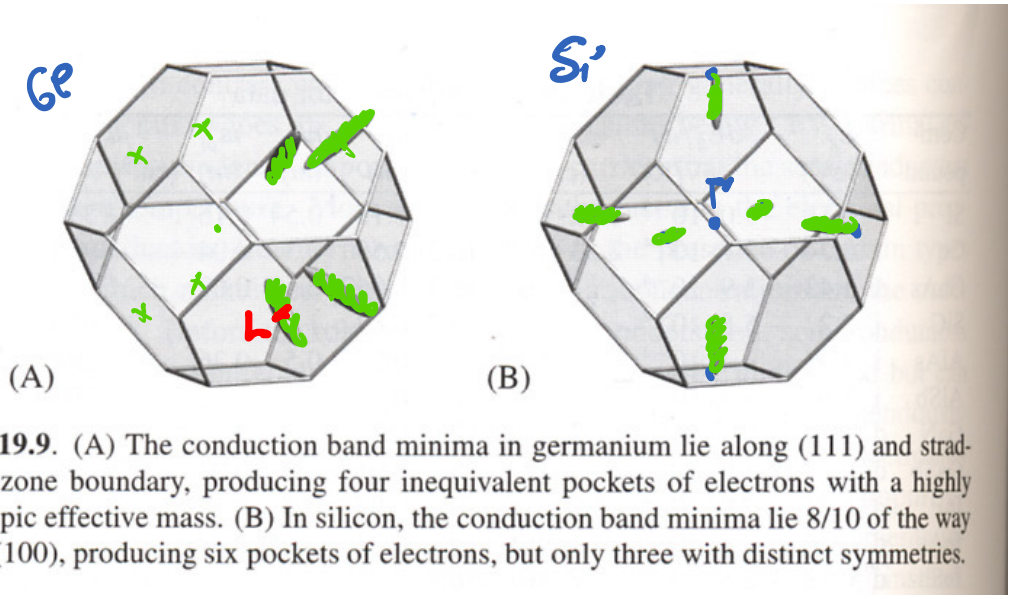


Figure 19.9. (A) The conduction band minima in germanium lie along (111) and straddle the zone boundary, producing four inequivalent pockets of electrons with a highly anisotropic effective mass. (B) In silicon, the conduction band minima lie 8/10 of the way toward (100), producing six pockets of electrons, but only three with distinct symmetries.

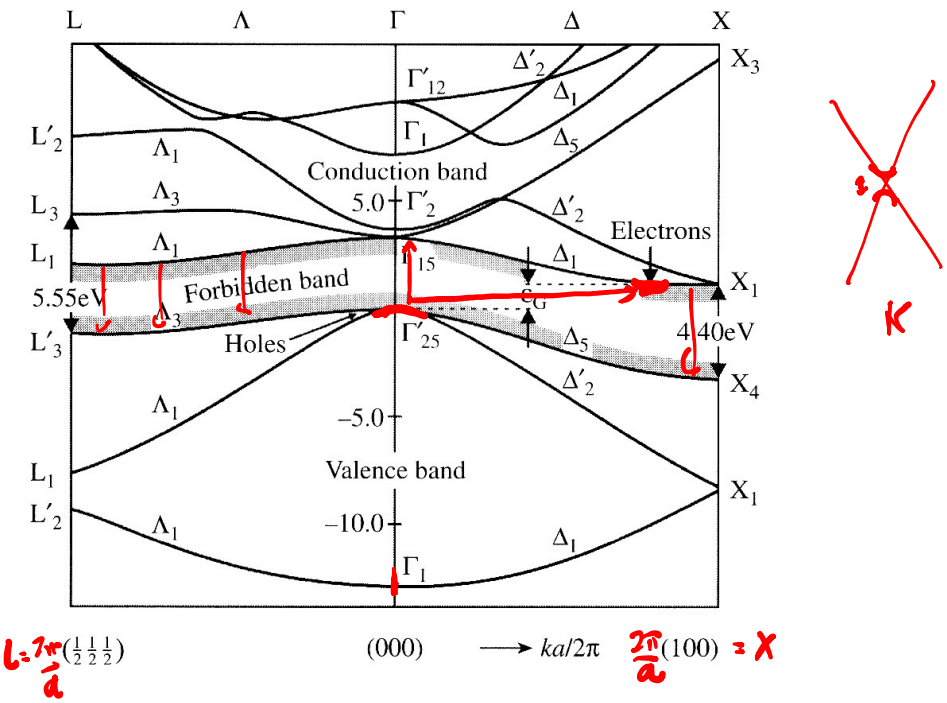
Impress your examiners (orals)

Table 19.1. Semiconductor data

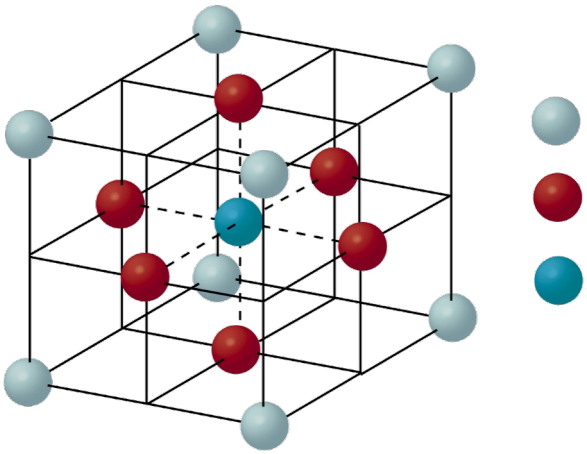
Compound		$\mathcal{E}_g$ (eV)	$d\mathcal{E}_g/dT$ (eV/K)	n_i (cm^{-3})	ϵ^0	$m_n^\star$ (m)	$m_{ph}^\star$ (m)	$m_{pl}^\star$ (m)	μ_n ($cm^2/V\,s$)	μ_p ($cm^2/V\,s$)
Si	i	1.11	$-9.0\cdot10^{-5}$	$1.02\cdot10^{10}$	11.9	1.18	0.54	0.15	1350	480
Ge	i	0.74	$-3.7\cdot10^{-4}$	$2.33\cdot10^{13}$	16.5	0.55	0.3	0.04	3900	1800
GaAs	d	1.43	$-3.9\cdot10^{-4}$	$2\cdot10^{6}$	12.5	0.067	0.50	0.07	7900	450
SiC	i	2.2	$-5.8\cdot10^{-4}$		9.7	0.82	1		900	50
AlAs	i	2.14	$-4\cdot10^{-4}$	$2\cdot10^{17}$	10.0	0.5	0.5	0.26	294	
AlSb	i	1.63	$-4\cdot10^{-4}$		12.0	0.3	1	0.5	200	400
GaN	d	3.44	$-6.7\cdot10^{-4}$	$2\cdot10^{17}$	12.0	0.3	1		440	
GaSb	d	0.7	$-3.7\cdot10^{-4}$	10^{14}	15.7	0.05	0.3	0.04	7700	1600
InP	d	1.34	$-2.9\cdot10^{-4}$	$1.2\cdot10^{8}$	15.2	0.073	0.6	0.12	5400	150
InAs	d	0.36	$-3.5\cdot10^{-4}$	$1.3\cdot10^{15}$	15.2	0.027	0.4	0.03	30 000	450
InSb	d	0.18	$-2.8\cdot10^{-4}$	$2.0\cdot10^{16}$	16.8	0.013	0.4	0.02	77 000	850

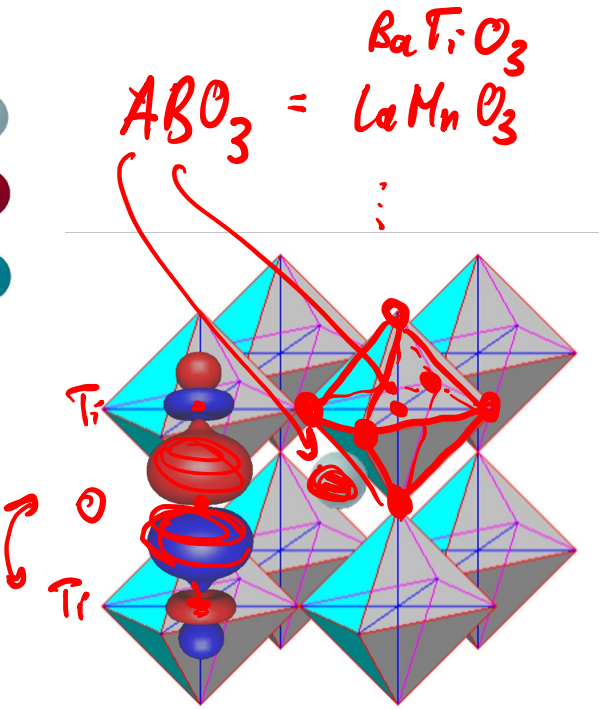
Data on whether a compound has a direct (d) or indirect (i) gap, energy gap, static dielectric constant, effective masses, and mobilities, for some semiconductors. The electron effective mass $m_n^\star$ is the density of states effective mass defined in Eq. (19.23). The data refer to room temperature, and to samples with donor and acceptor impurities at densities of 10^{15} cm^{-3} or less. Source: Landolt and Börnstein (New Series) vol. 17 and Pierret (1996).

Valence+conduction bands in Si

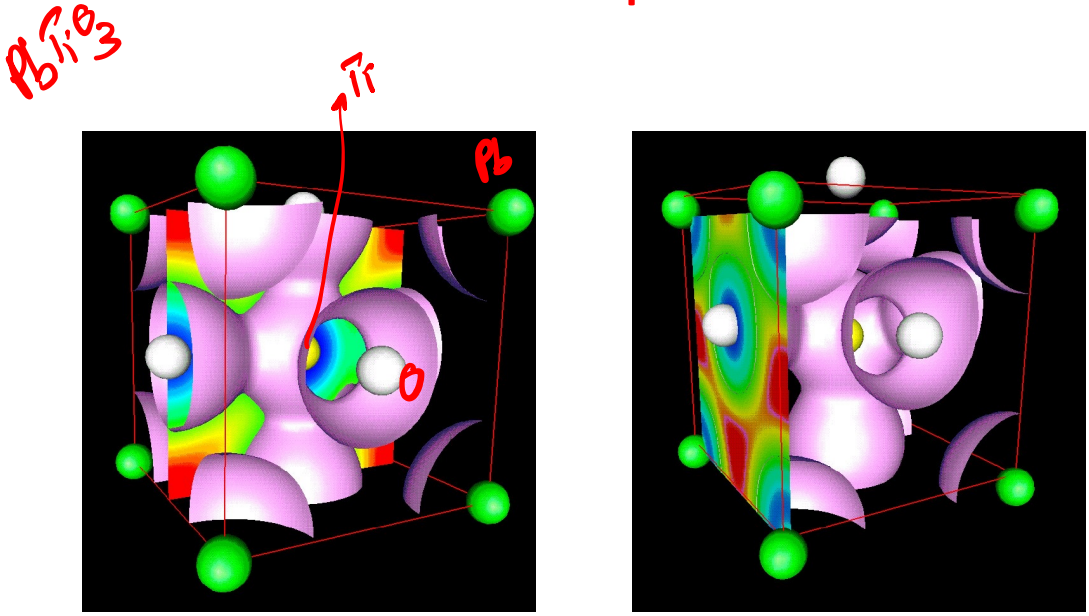


Perovskites





Ferroelectric perovskites



Ferroelectric perovskites

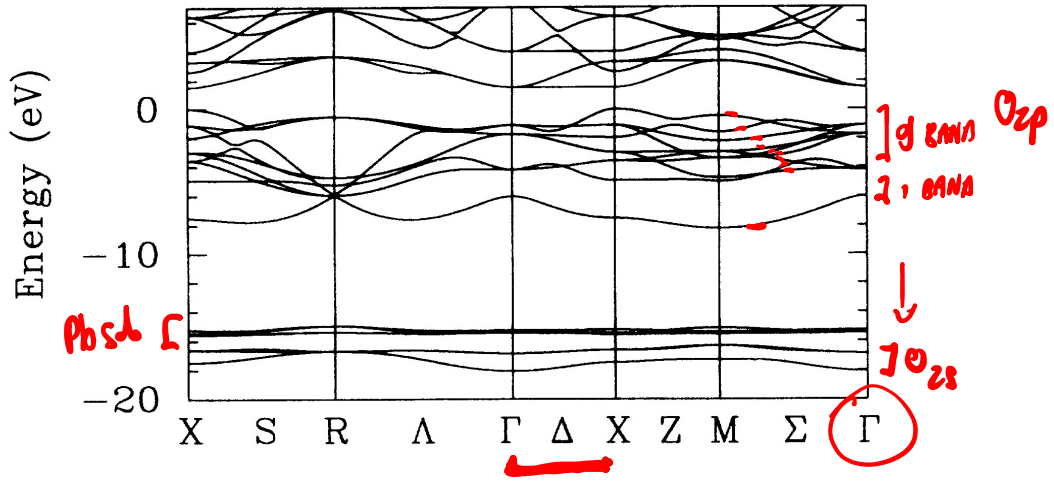
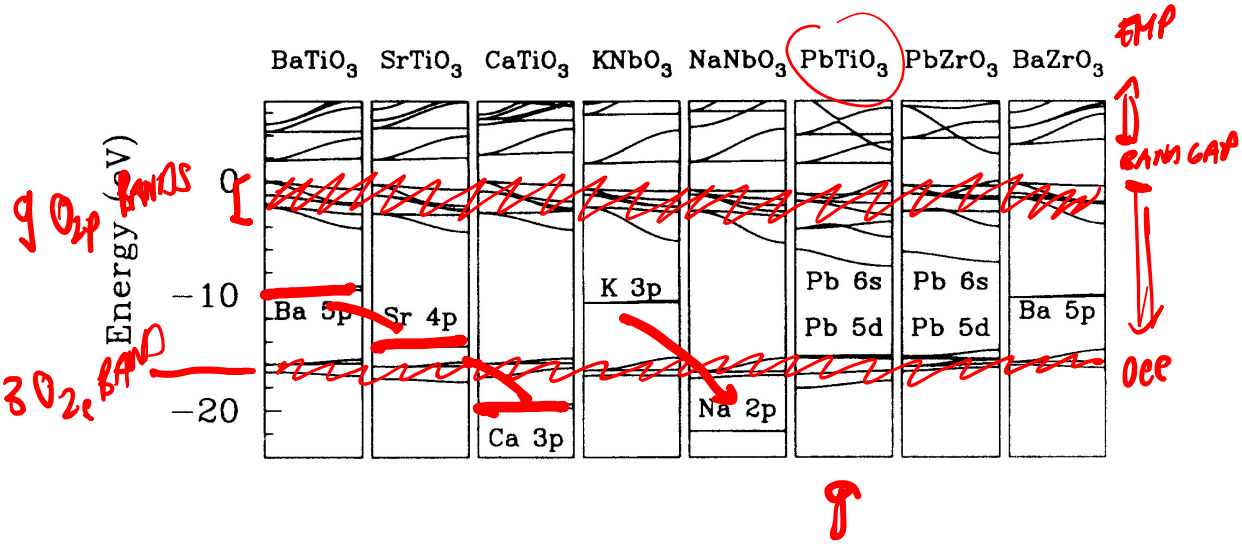
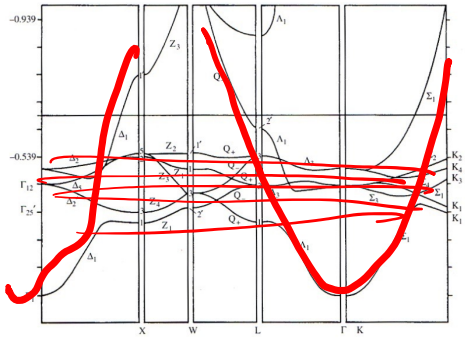


FIG. 3. Band structure of cubic $PbTiO_3$ for selected high-symmetry directions.

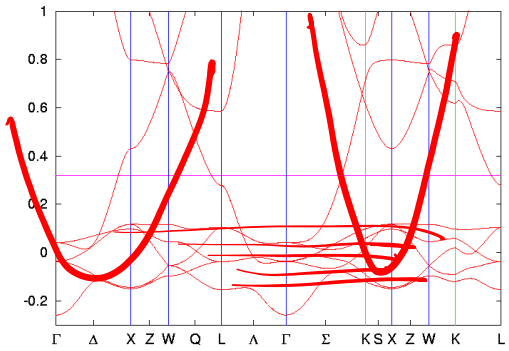
Ferroelectric perovskites



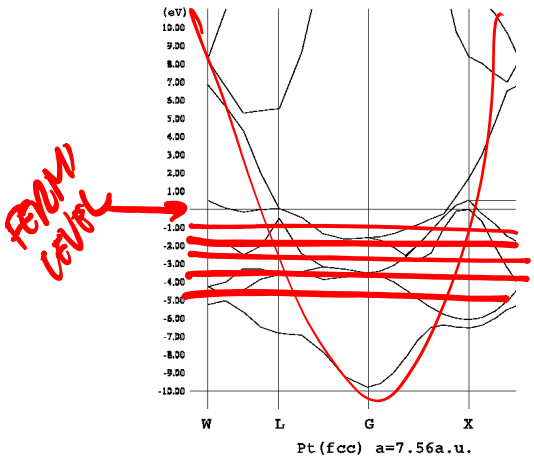
Copper



Silver



Platinum



Gold