

# Parallel robotics

## EPFL – Dr M. Bouri, 2021

### The course

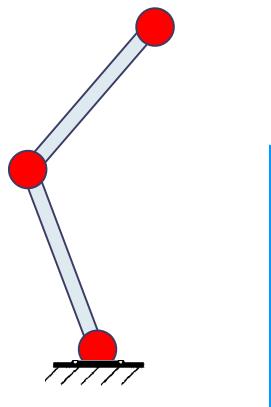
- What is parallel robotics and why ?
- The example of the robot Delta.
- Calculation of mobility.
- The family of Delta robots.
- More DOFs.
- The Hexapods.

## Parallel vs Serial robots

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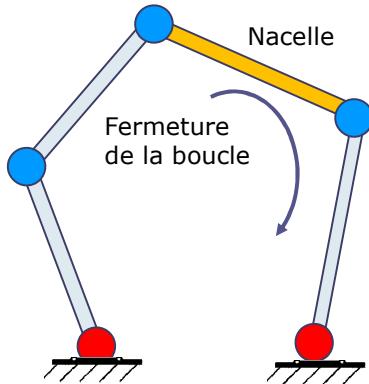
### Serial robots

With **actuated segments in series**



### Parallel robots

- ✓ Robots with closed kinematic chains
- ✓ All the motors are on the basis



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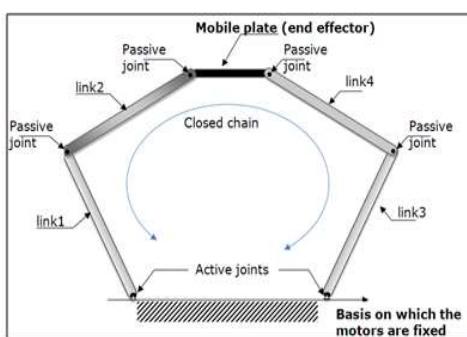
## Leightweight, fast and stiff

4

1. All the kinematic **chains** from the basis to the mobile parts are **closed** to the basis.
2. All the **motors are on the basis** and no one is on the structure. The **intermediate joints** in the structure are all **passive**.



Mitsubishi RP 1AH



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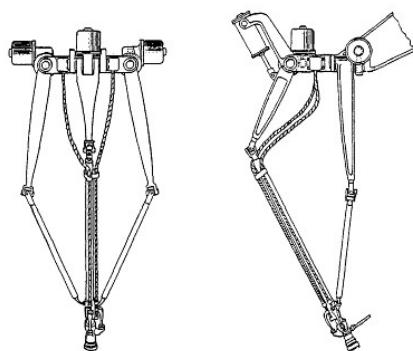
*Close the chain and let us talk about parallel kinematics !*



## Parallel Robots

### Since When?

The oldest «known» is  
Pollard robot (Pollard 1938) invented by  
Mr Pollard



Parallel link to remote an actuator and make the link stiffer

7



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Parallel kinematics....

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**The Most known**

[The flight simulator](#)

[The Gough Stewart platform](#)



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## The robot "Delta"

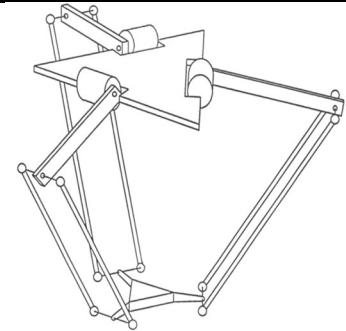
## 7 years : from the idea to the customer!

9



1985: Patented by R. Clavel (EPFL)

Principle



1988 – The patent is Sold to the Swiss company Demaurex SA (currently Bosch Packaging Technology Unit, Romanel).

1992 – The first customer was Nestlé.

> Has been the **precursor** for the market of parallel robotics.

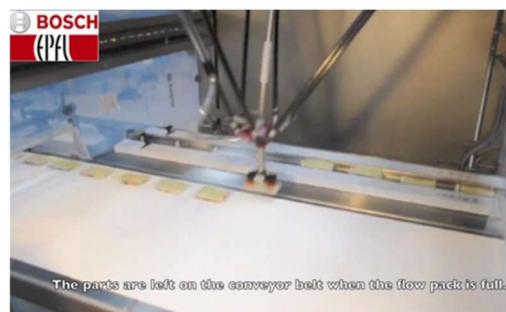


More than **200 companies** have adopted this kinematics since **2007** when the patent was in the [public domain](#)

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## Direct Drive Actuated Delta realized for BOSCH Packaging Technology

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August 2019  
0,4mm RMS\_error @30 Ge  
acceleration pick\_and\_place

[Patent 2015] Device For Moving And Positioning An Object In Space, Huser M., Tschudi M., Keiffer D., Teklits A., Bouri M., Clavel R., Demaurex MO., Device For Moving And Positioning An Object In Space, reference WO2012152559

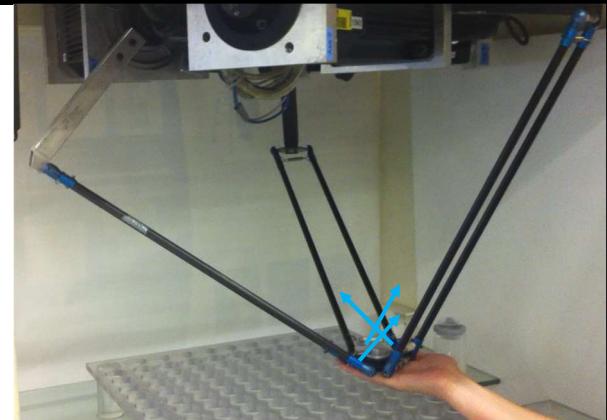
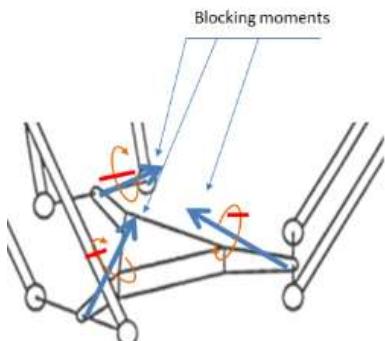


Invented for life

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## The robot "Delta"

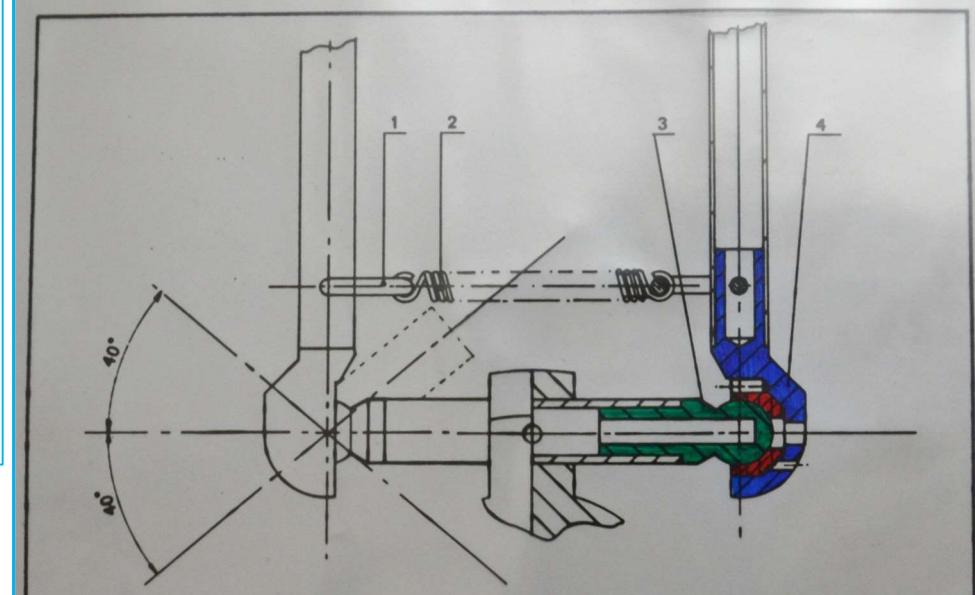
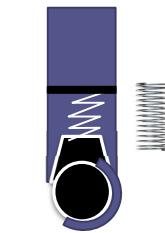
11



- The sum of the blocking moments is not null, **which explains that the orientations of the mobile plate are all blocked**.
- When the sum of the blocking moments is null, the robot is in **a singular position**.

## The spherical joints – The easiest way !

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## Mobility of parallel robots

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In a parallel robot,

- There are active joints (actuators) and passive joints (pivots, universal joints, spherical joints, and others)
- kinematic chains are closed.
- The number DOF of the mobile plate does not suffice to illustrate some constrained internal mobilities and to illustrate free internal mobilities.

The number “**Mobility**” illustrates the resulting mobility of the robot, by considering all the joints and the segments of the robot.



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## Mobility of parallel robots

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The mobility is **the balance of the overall mobilities** of all the links that constitute the robot, by considering of course the existing kinematic constraints.

**In the case of a serial robot, the mobility is equal to the number of actuated joints.**

[!] It is also the **dimension of the joint space**.

**For parallel robots (kinematics),** two formulas allows to calculate the number (mobility)

- **Formula of Grübler.**
- **Formula of kinematic loops.**



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### Formule of Grübler

By considering a kinematic structure composed by **n solid elements**, the degrees of freedom (called DOF or Mobility MO) of this set of elements before any assembly is obviously equal to  **$MO = 6 \cdot n$**  (each element has 6 spatial DOF). Each link between 2 elements reduces the total mobility by a value corresponding to the number of the generalized forces (NGF) in the considered link. With **k joints**, the mobility is computed as follows:

$$MO = 6n - \sum_{i=1}^k NGF_i$$

The number of the generalized forces (NGFi) involved in a considered joint is a complementary to 6 of the number of the degrees of freedom (MOi). We then obtain:

$$NGF_i = 6 - MO_i$$

$$\text{And hence: } MO = 6n - 6k + \sum_{i=1}^k MO_i$$

$$\text{That gives: } MO = 6(n - k) + \sum_{i=1}^k MO_i$$

Since one element of the structure is fixed on the frame, its 6 DOF must be differentiated from the total mobility number MO. We obtain:

$$MO = 6(n - k - 1) + \sum_{i=1}^k MO_i$$

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### Formula of kinematic loops

$$MO = \sum_{i=1}^k MO_i - 6bo$$

**bo (boucles in French)** is the number of disjointed kinematic loops in the structure.



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## Mobility of parallel robots

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### Reminder: Representations of kinematic links

#### Pivot

Pivot (fr)

Pivot joint / Rotary joint (en)



#### Cardan

Cardan (fr)

Universal joint / cardan joint (en)



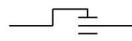
#### Spherical joint

Rotule (fr)

Spherical joint (en)



#### Prismatic joint

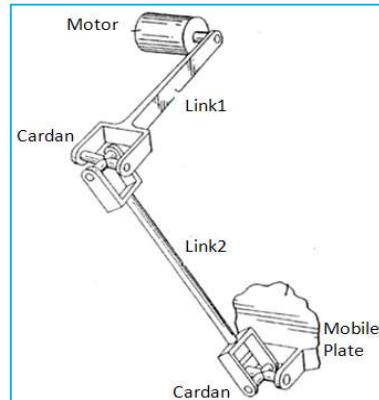


### Example 1: Delta with cardans / universal joints): Exercise ☺

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#### Example 1,

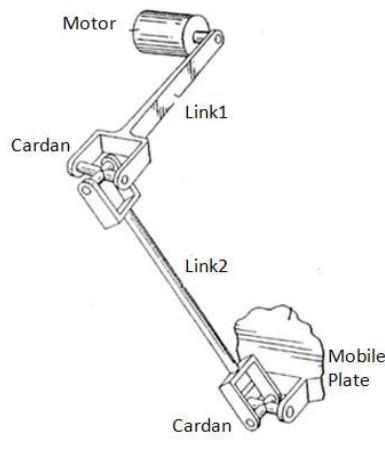
- Illustrate the Kinematic representation of a Delta with gimbals.
- Calculate its mobility.
- Conclude...



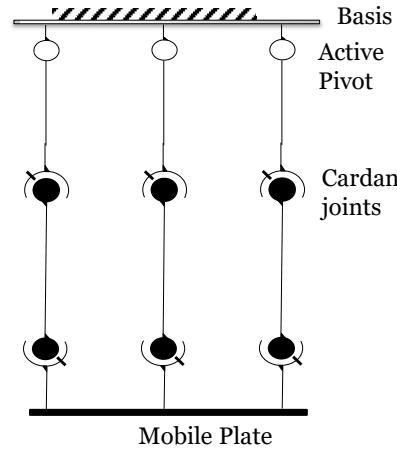
Representation of one kinematic chain of the cardan based Delta

**Example 1: The simplest variant: with cardans at the passive joints**

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Representation of one kinematic chain

**Delta with cardans: Calculation of the Mobility ☺**

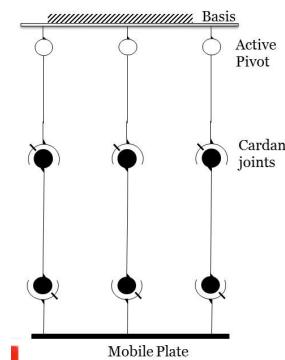
20

By applying the Grubler formula, we have:

- The number of elements of the structure is  **$n = 8$**  (1+1+3.2) {1 basis + 1 mobile plate + 3 arms + 3 forearms}.
- The number of joints  **$k = 9$**  {(1 pivot + 2 cardans) X 3 identical links}.
- The mobility of the pivot is equal to **1**. The mobility of each cardan is equal to **2**. The total mobility of this Delta is then computed as follows:

$$MO = 6 \cdot (8 - 9 - 1) + \{1 + 2 + 2\} \cdot 3 = -12 + 15 = 3$$

$$MO = 6(n - k - 1) + \sum_{i=1}^k MO_i$$



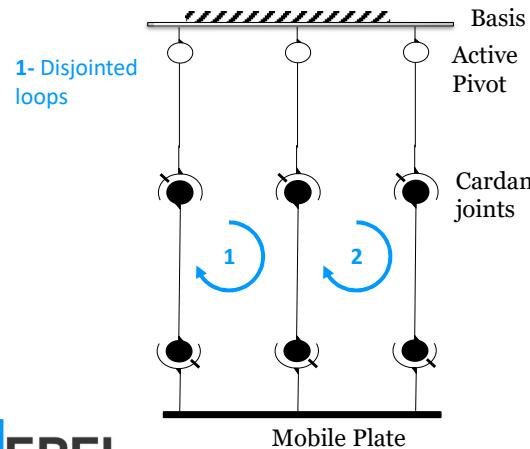
## Delta with cardans: Calculation of the Mobility using the the loop formula ☺

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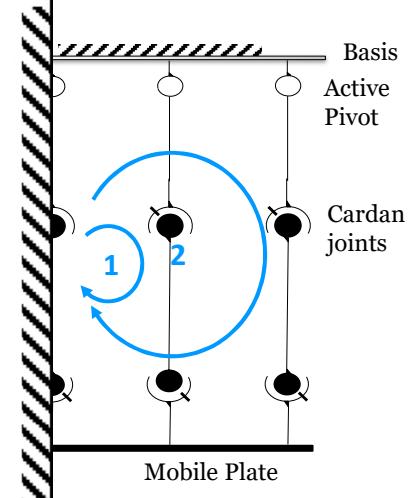
## Formula of kinematic loops

$$MO = \sum_{i=1}^k MO_i - 6bo$$

How to count the loops ?



2- Closed loops with same reference

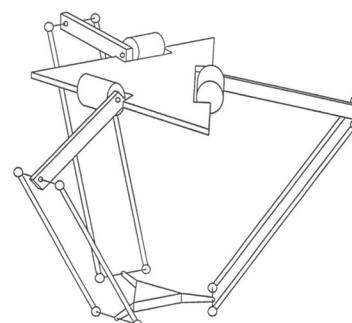
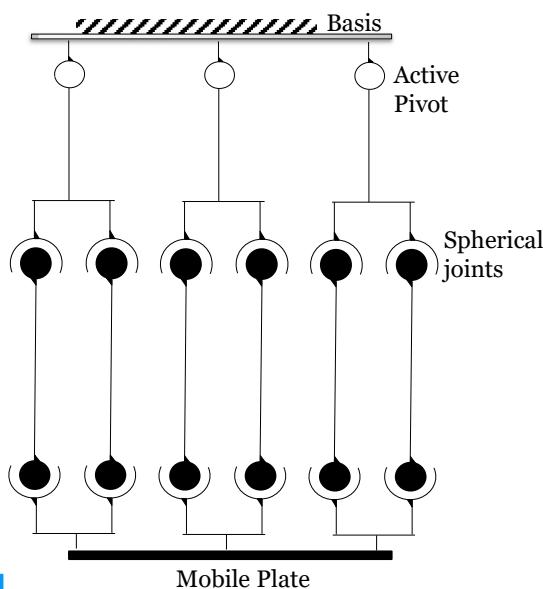


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Example 2: The most common realization, Delta with parallel bars and spherical joints

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- n = 11 (1+1+3.3) {1 basis + 1 mobile plate + 3 arms + 6 bars}.
- k = 15 {(1 pivot + 4 spherical joints) X 3 identical links}.

$$\begin{aligned}
 MO &= 6 \cdot (11 - 15 - 1) + \{1 + 4 \cdot 3\} \cdot 3 \\
 &= -30 + 39 = 9
 \end{aligned}$$

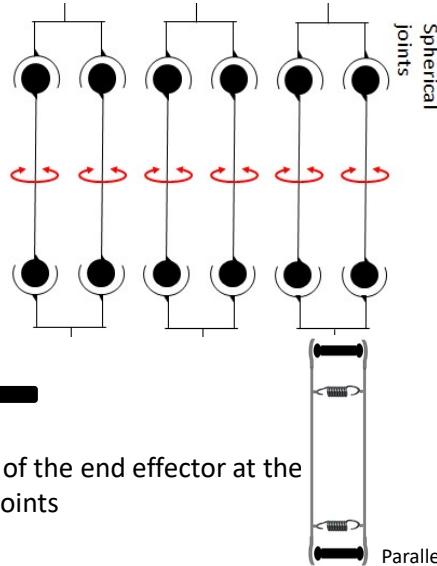
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## Observation

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- The Delta robot as designed with the parallel bars and spherical joints has **6 supplementary mobilities**.
- These mobilities concern **internal mobilities** not affecting **the pure translation of the mobile plate**.
- They are actually related to the **rotation of each bar around its principal axis**.



- Springs limit the internal mobility at the cost of friction
- The internal mobility does not affect the final precision of the end effector at the condition of an ideal spherical contact of the spherical joints



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## Delta with cardans ☺

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### Using cardans instead of a parallel bars and spherical joints



#### Never do it....

- The structure is not enough stiff
- Not easy to find cardans with reduced play.
- The play will reduce the proper mechanical frequency



Never say never ....



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## More DOFs

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- The family of Delta robots
- More DOFs
- The Hexapods



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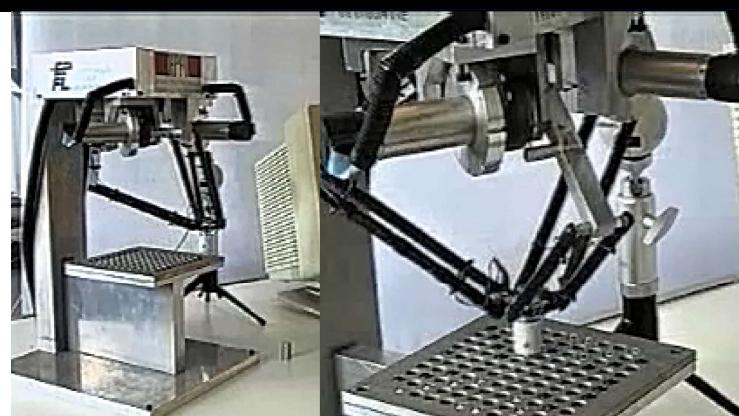
## Simplicity of the Delta

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The diagram illustrates the kinematic structure of a Delta robot. It shows a triangular frame with three parallel bars connecting the vertices. A horizontal bar at the bottom, labeled 'Parallel bars', supports the frame. The photograph shows a real-world implementation of this design, featuring a vertical column with a motor and gear box at the top, two arms extending downwards, and a mobile plate at the bottom where the arms converge. The mobile plate is shown in a horizontal position, indicating the robot's ability to move in multiple degrees of freedom.



Parallel bars





Motor + Gear Box + Arm + Fore arms



Motor + Gear Box + Arm + Fore arms



Motor + Gear Box + Arm + Fore arms



+



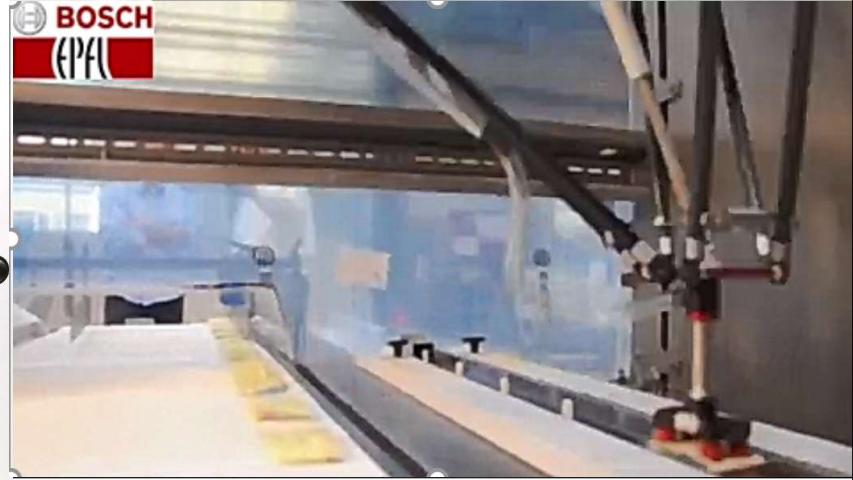
Mobile plate

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## Even simpler without gearboxes : the trend

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Direct Drive Actuated Delta realized for **BOSCH Packaging Technology**



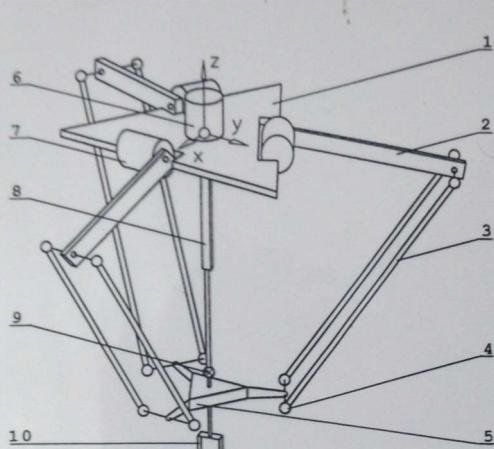
[Patent 2012] Device For Moving And Positioning An Object In Space, Huser M., Tschudi M., Keiffer D., Teklits A., **Bouri M.**, Clavel R., Demaurex MO., Device For Moving And Positioning An Object In Space, reference WO2012152559



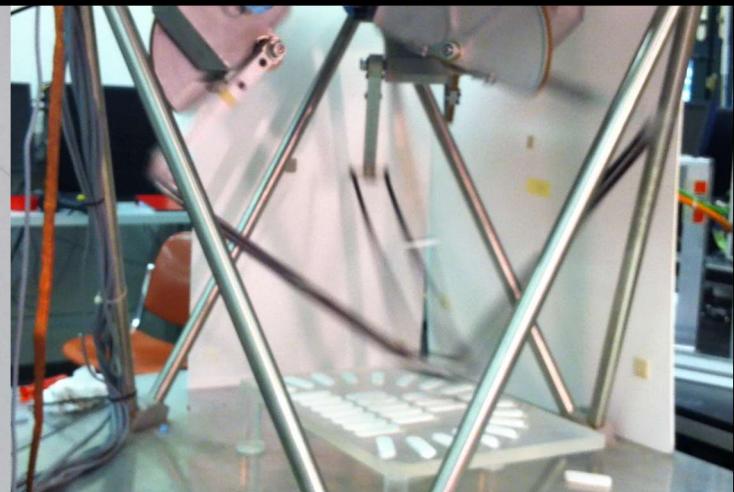
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## The Delta 4, with 4 DOFs

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Angular Delta with **4 DOFs**



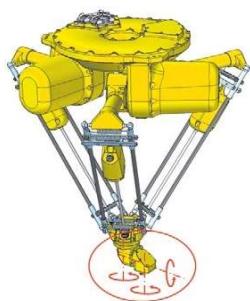
Additional DOF : **Serial or Parallel?**



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## Other companies are proposing parallel robots in their catalog:

1. **Mitsubishi** that proposes the double Scara robot.
2. **ABB** (Delta FlexPicker).
3. **Demaurex** at Ecublens, VD/ CH
4. **Adept** that is proposing the Quattro robot
5. **Fanuc** that proposes different variants of the Delta robot.



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Fanuc



ABB

Demaurex (the first manufacturer of the Delta) 21

## Other companies are proposing parallel robots in their catalog:

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Fanuc Delta robots



Omron robots



6 axes



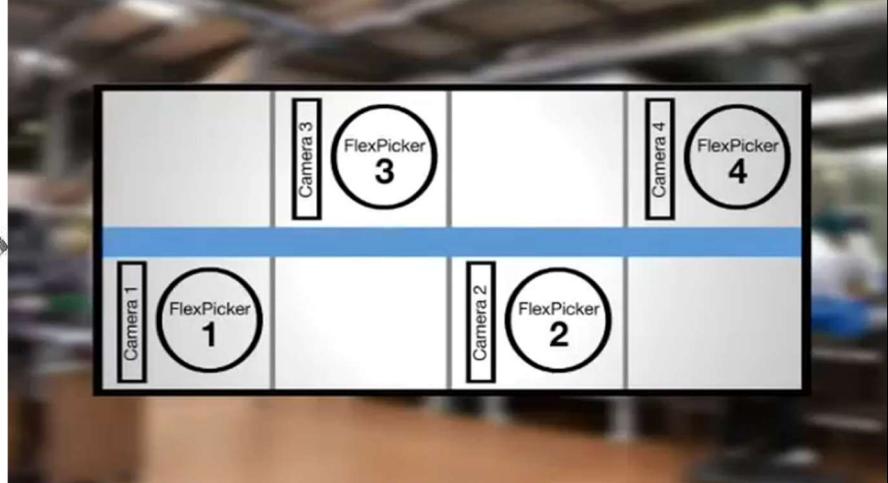
IP67

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## ABB - example

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4 axes – Delta robot



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## Delta Omega: Parallel robotics for haptic feedback

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How to reduce friction ?      Bearings in series instead of spherical joints

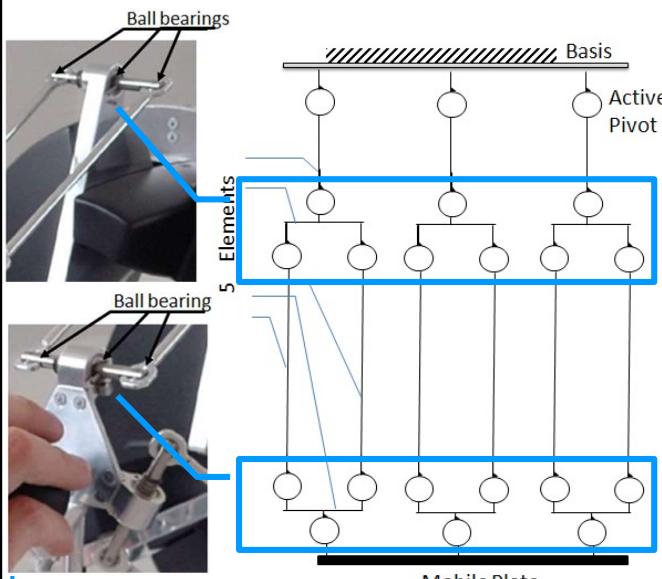


How to reduce friction while keeping big torques ?      Cable transmission instead of gears

Robot Omega from Force Dimension (Nyon) for haptic feedback and tele-manipulation



## What is about the mobility of the Delta Omega ?



- $n = 17$  (1+1+5 X 3)  
{1 basis + 1 mobile plate + 5 elements X 3}.
- $k = 21$  {(1 pivot + 6 pivot joints) X 3 identical links}.

$$MO = 6 \cdot (17 - 21 - 1) + \{21\} = -9$$

Over-constraint of order 12

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## The Quattro – 4 DOFs from Omron (prev. Adept)

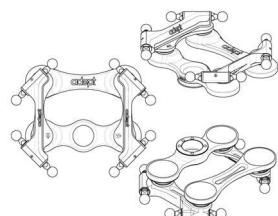
34

### Parallel Robot (Delta Robot): Adept Quattro s650H

The Adept Quattro™ s650H parallel robot is specifically designed for high-speed applications in packaging, manufacturing, assembly, and material handling. The Adept Quattro robot is the only parallel robot (or "delta robot") in the world that features a patented four-arm design, advanced control algorithms, and large work envelope make the Adept Quattro the ideal overhead-mount robot for smooth motion, high-throughput applications. The Adept Quattro is powered by ultra-compact controls and embedded amplifiers, which reduces the cycle time and improves footprint efficiency.



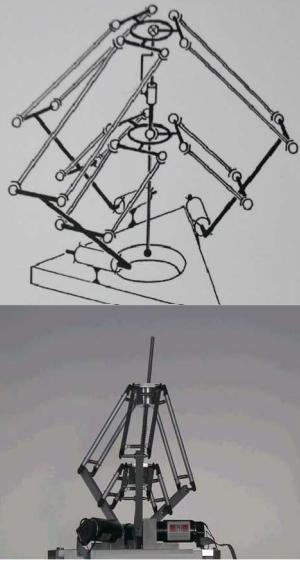
Figure 1-1. Adept Quattro s650H Robot



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## Thales ... idea found an application !

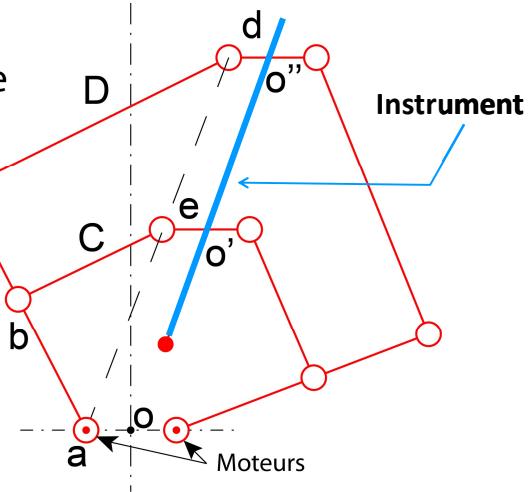
35



Initial kinematics



● = pivot  
○ = rotule

**A spherical robot.....**

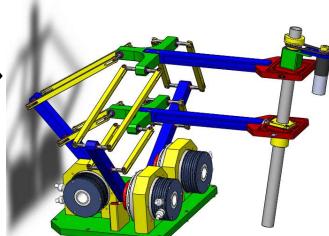
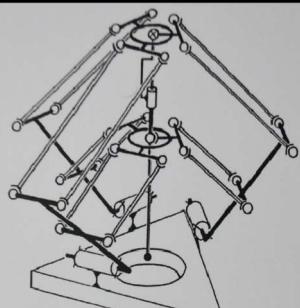
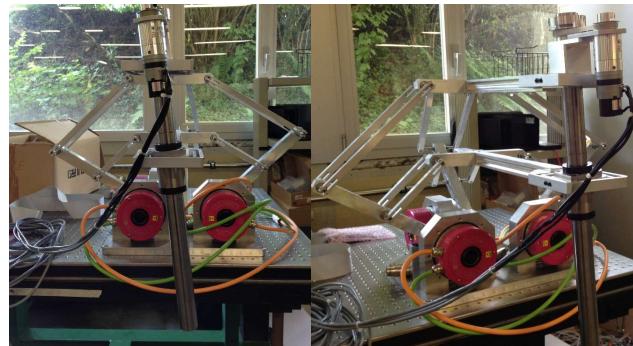
1 translation (insertion) of the instrument

2 tilts (orientations) of the instrument

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## Thales ... idea found an application for surgery!

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.....for laparoscopic surgery with an **ex-centered** tool

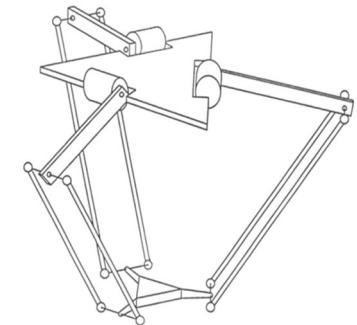
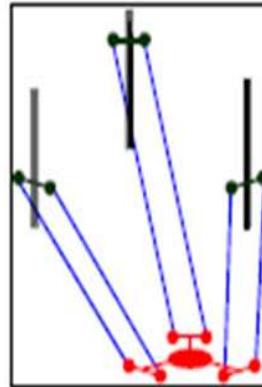
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## Linear Variants

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Variants with linear movements

- for applications requiring stiffness.
- For applications requiring precision



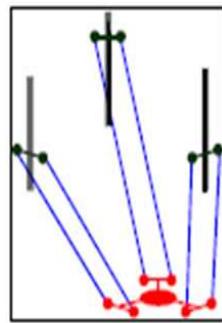
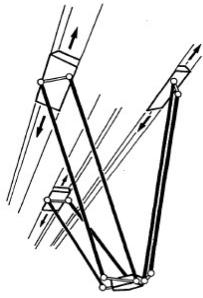
## Linear **versus** Angular

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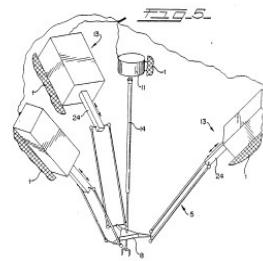
- **The speed** of the linear variants is **only limited by the actuators**
- **The stiffness** of the rotational variants is only limited by the stiffness of the arm.
- **Increasing the resolution** of the rotational variants is only limited by the sensor quality.

## Types of the linear Delta

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U.S. Patent Dec. 11, 1990



- Horizontal linear structure,
- Vertical structures,
- Orthogonal,
- Inclined guided



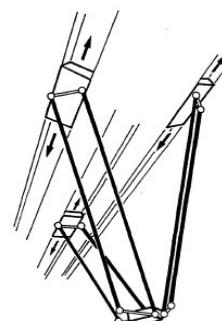
Bouri, M, and Clavel, R, "The linear delta: Developments and applications." ISR 2010

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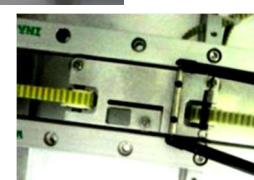
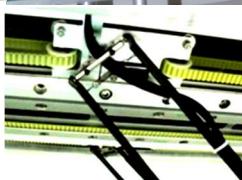
## Developments and applications

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## The Horizontal family



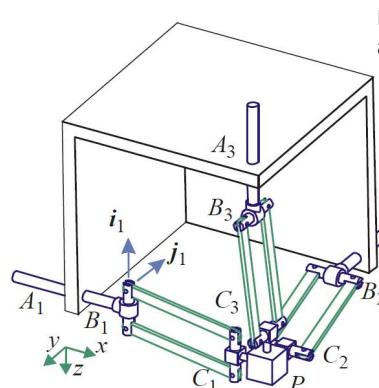
Double hoist system as a translational transmission  
(FR, double palan)



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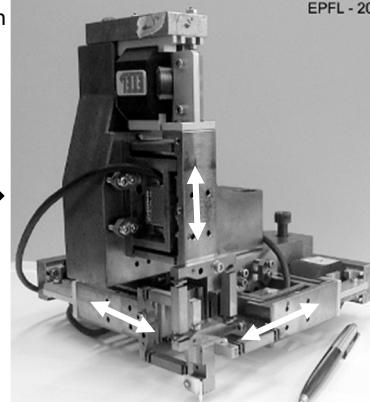
## The orthogonal family

41

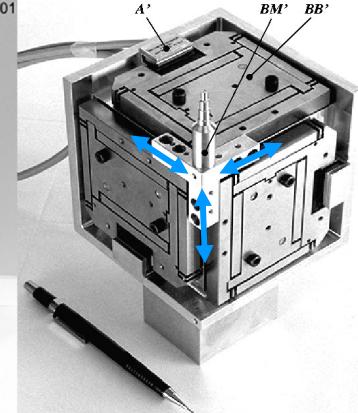


The orthoglide from IRCCyN

**[!] Problem of the orthogonality  
of the three plans**

High precision  
applications

MX3000 from MECARTEX SA  
<http://www.mecatex.ch/>



Delta Cube I  
 Thesis, Simon Henein, EPFL

**The orthogonality of the three plans is solved through a monolithic  
machining**



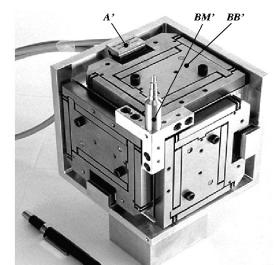
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## The orthogonal family

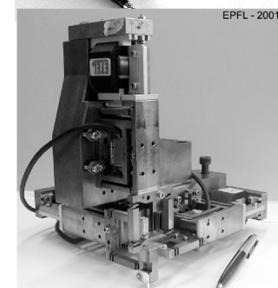
42

### More details

This Delta structures called “**Delta Cube**” reach a repeatability of **+/-10nm**.



“**Delta Cube I**” that has a travel of +/- 1mm in each direction.



“**Delta Cube II**” has a travel of +/- 4 mm in each direction with a proper frequency of 350Hz.



M. Bouri, R. Clavel [ISR 2010]

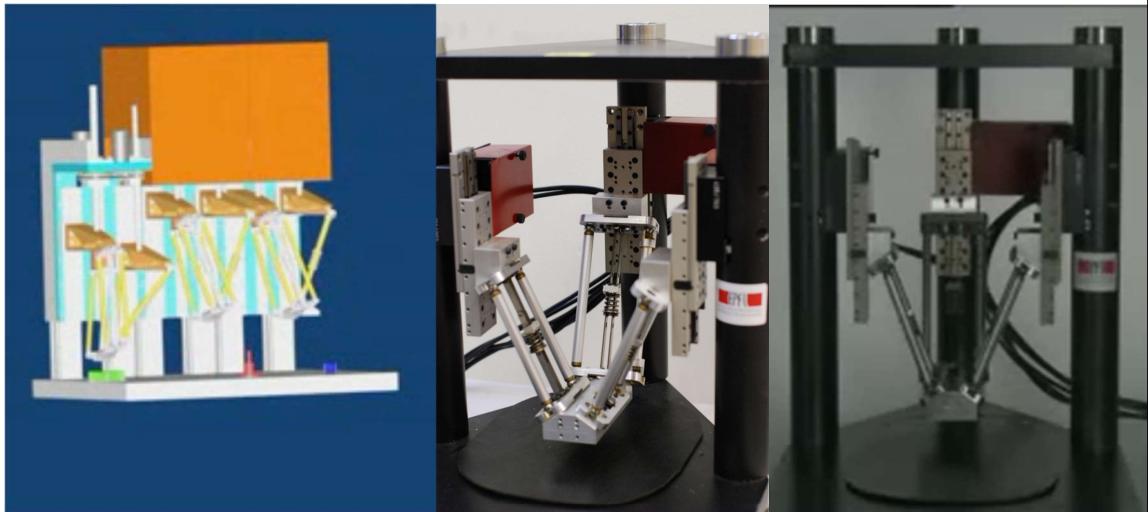
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## Developments and applications

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The Vertical family

### 1. Assembly for microEngineering



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## Developments and applications

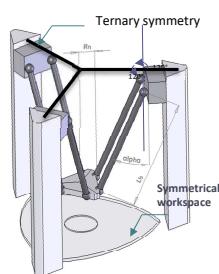
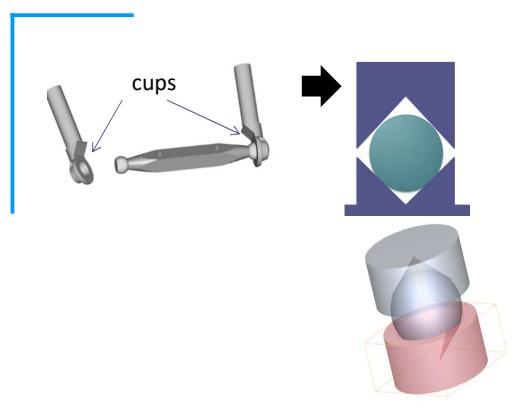
44

The Vertical family

### 2. Towards PIN insertion for watch industry

- Stiffness
- Speed
- Simplicity

Modify the spherical joints  
Adapt the parallel bars  
Use ball screw to increase  
insertion forces up to 300N



EPFL

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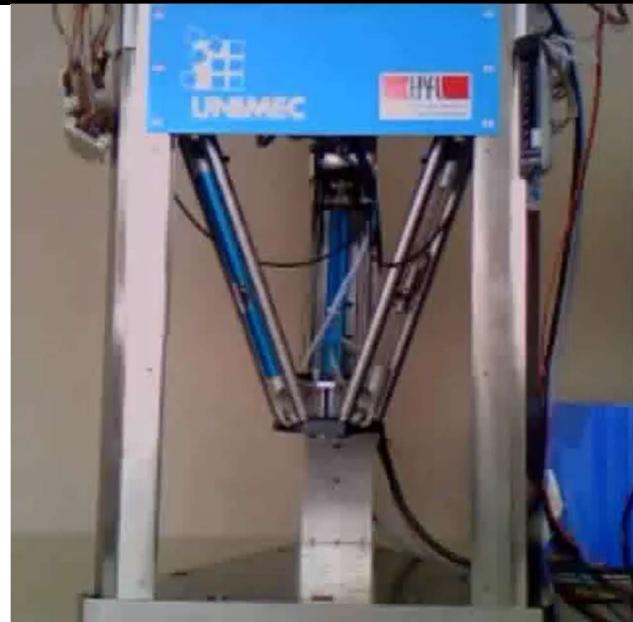
## Developments and applications

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The Vertical family

### 2. Towards Pin insertion for Watch Industry

Length of parallel bars:	<b>300 mm</b>
Space resolution:	<b>0.1-0.25 <math>\mu\text{m}</math></b>
Vertical resolution (center):	<b>0.1 <math>\mu\text{m}</math></b>
Velocity:	<b>0.4 m/s</b>
Acceleration:	<b>50 <math>\text{m/s}^2</math></b>
Vertical force:	<b><math>\leq 350\text{N}</math></b>
Stiffness:	<b><math>50\text{N/mm}</math> (<math>5.10^7\text{N/m}</math>)</b>
Working space:	$\phi = 240 - 280 \text{ mm}$ $H = 80 \text{ mm}$



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## Developments and applications

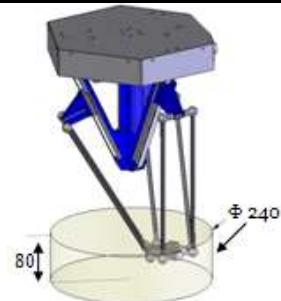
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The Vertical family

The Inclined Keops- Advantage 1

[Workspace .vs. robot size](#)

Resolution on the linear axis is **7.5  $\mu\text{m}$** ;  
the worst resolution in the workspace is  
better than **20  $\mu\text{m}$** ;  
the velocity can easily reach **3.5m/s** at  
the acceleration value of **3.5g**.



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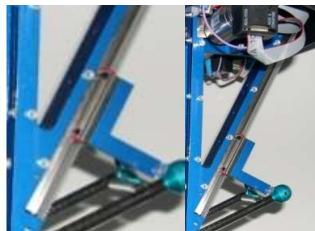
## Developments and applications

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The Vertical family

The Inclined Keops- Advantage 2

Simplicity



The Inclined Keops- Advantage 3

Stiffness at the extremity of the volume



What else...

1µm - sensors integrated to Schneeberger guideways.



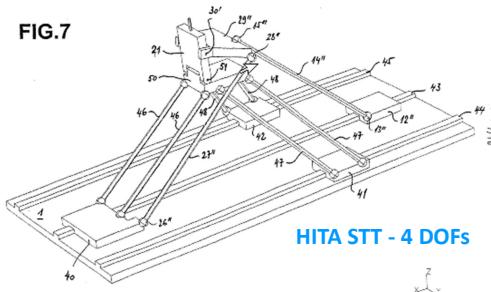
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## Developments and applications

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The Horizontal family - Tool Machining

FIG.7



**Extension** of the linear horizontal Delta to have one additional degree of freedom.

STT: Stiffness Tracking Technology.



HITA STT, EPFL, 4 DOFs / XYZ and one tilt  
[ref Willemin Macodel]

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Plenty of  $\Delta$  -structures.....

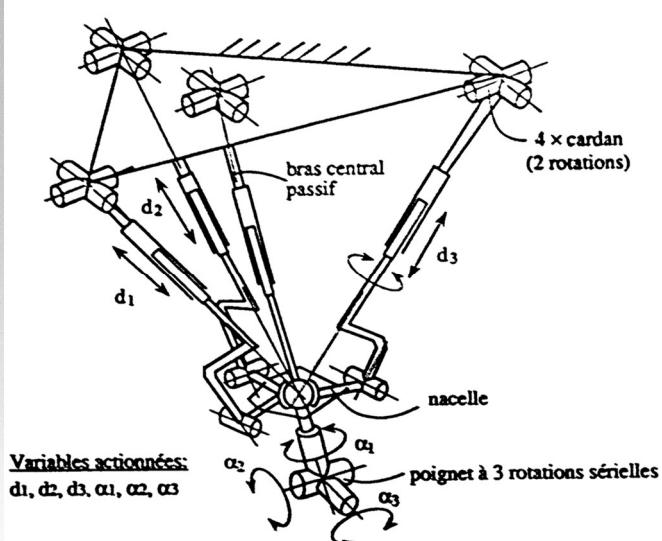
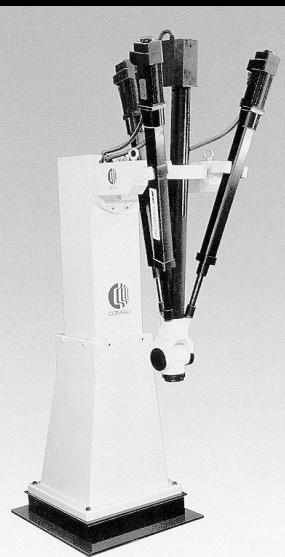
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## The Tricept (Tetrabot)

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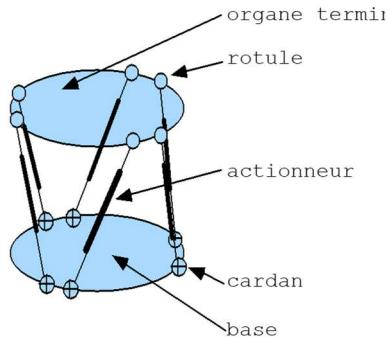


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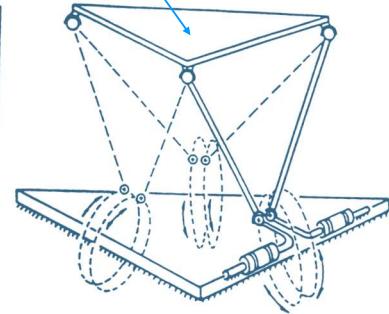
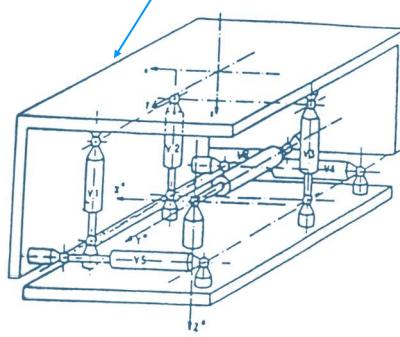
## Platforms 6 DOFs

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## GOUGH-STEWART (1962)



## ARTIGUE (1984) and HUNT (1983)



- Decoupled for small motions

- Actuators fixed to base



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## Gough-Stewart vs Hunt vs Artigue

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Artigue 3x2x1



Artigue 2x2x2



Gough-Stewart Hexapod [ref. Symetrie]



Hunt Rotational Stewart

- «Artigue» has more **decoupled movements** than «Gough-Stewart» and «Hunt»
- «Artigue 2x2x2» is **even more decoupled** than «Artigue 3x2x1»
- All the **linear variants** are stiffer than the Rotational «Hunt»
- «Hunt» is **more dynamic**, has a **bigger workspace** than «Gough-Stewart»

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**Platform 6 DOFs inspired from the Delta**

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