

MICRO 372 - Advanced Mechanisms for Extreme Environments

Chapter 8

(Ultra-) High precision

200 nm



Florent Cosandier

(Ultra-) High precision

- Calibration
- Flexure's tolerance effect
 - Manufacturing
 - Assembly
- Kinematic couplings

Calibration of robot or mechanisms

- **Kinematics:**

Calibration of the robot's kinematics involves adjusting parameters related to its **joint angles**, **link lengths**, and **coordinate systems**. This ensures that the robot moves accurately according to its intended trajectory.

- **Accuracy and repeatability:**

Robots often undergo calibration procedures to **improve their accuracy and repeatability**.

- **Sensor calibration:**

If the robot is equipped with sensors such as **cameras**, **force/torque sensors**, or **proximity sensors**, these sensors may need calibration to ensure accurate data acquisition and integration into the robot's control system.

- **Environmental factors:**

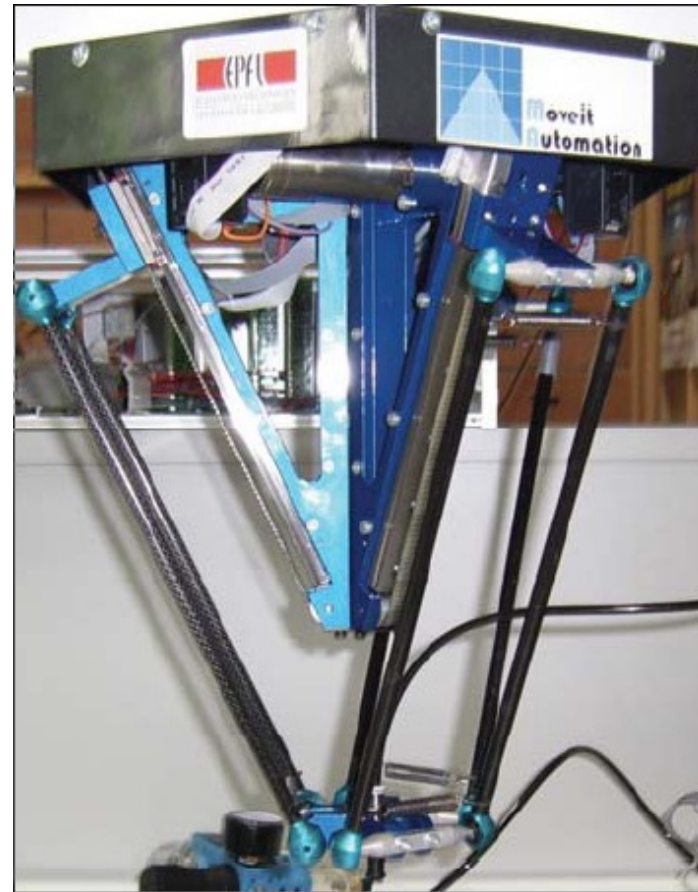
Calibration may also account for environmental factors such as **temperature variations**, **humidity levels**, and **gravitational effects**

- **Load and payload calibration**

calibration may involve adjusting parameters related to **varying loads** or payloads.

Calibration example: Kheops robot

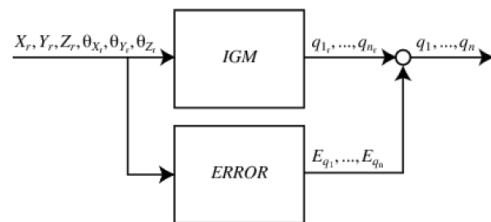
- **Calibrate the robot** makes possible to bring the actual **output** (position of the tool) **as close as possible** to the **desired theoretical position**.
- The purpose to calibrate a robot is to **correct its positioning errors due to differences between theoretical values and actual values**.
- These errors can be due to an **inaccuracy of the geometric model**, like imprecision of the lengths of the robot arms.
- **Other types of error** that can be calibrated: **sensor drift, nonlinearity, hysteresis, noise, interference**.
- Or to an influence of the **robot's environment**: **temperature, humidity, pressure**.



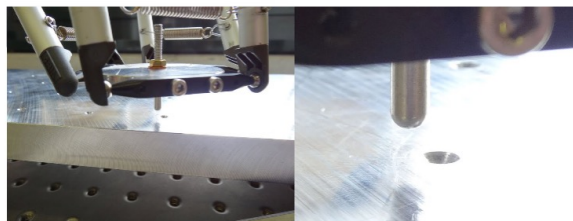
Calibration example: Kheops robot

Calibration procedure:

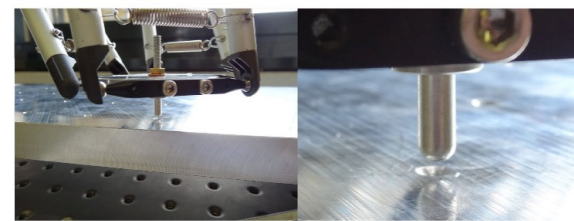
- Calculate the IGM
- Manual positioning the robot on precise points (motors off)
- Measurement of the motor coordinates at these points
- Determination of a polynomial fit of measured errors
- Addition to the IGM
- Validation of the correction by comparing the motor theoretical values and measured values on control points (motors still off)



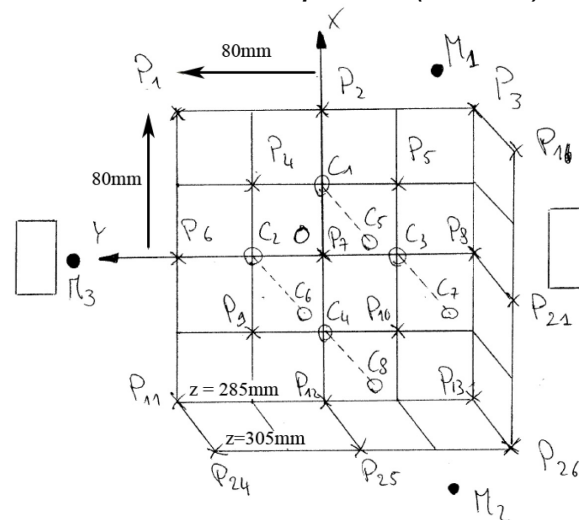
before calibration



after calibration



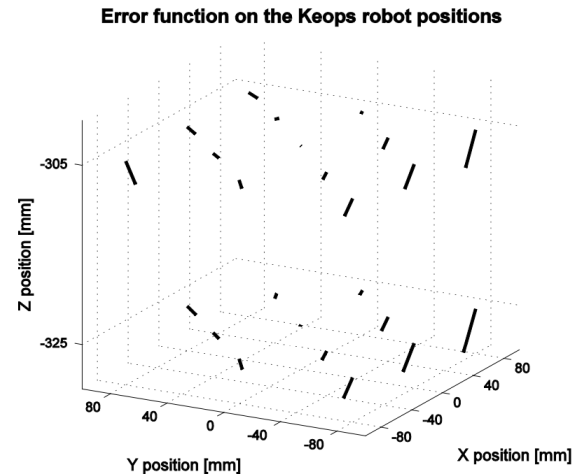
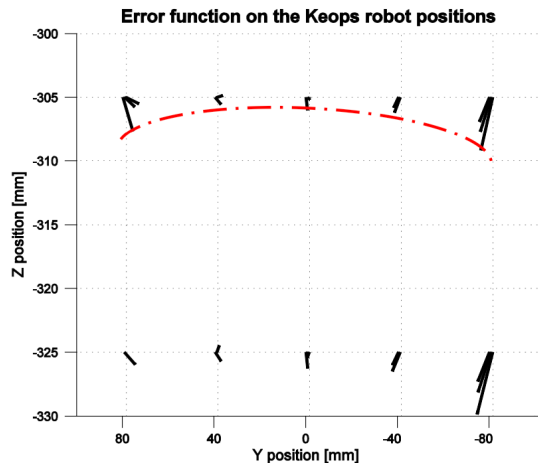
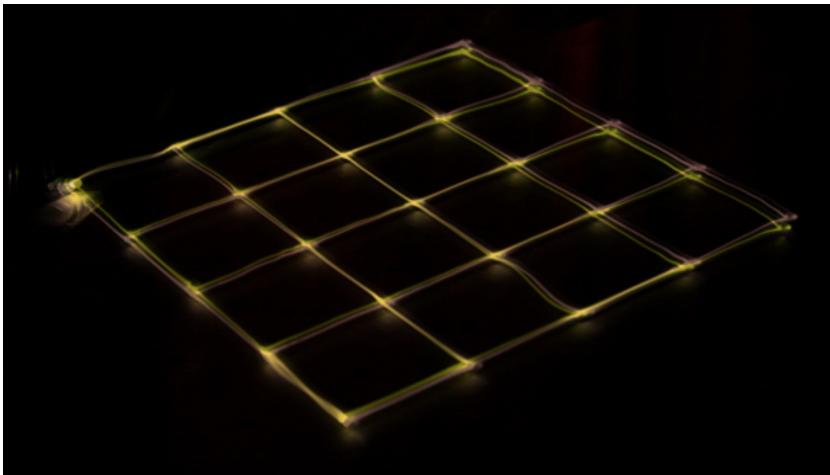
Calibration points (P1-P26)
and control points (C1-C8)



Calibration example: Kheops robot

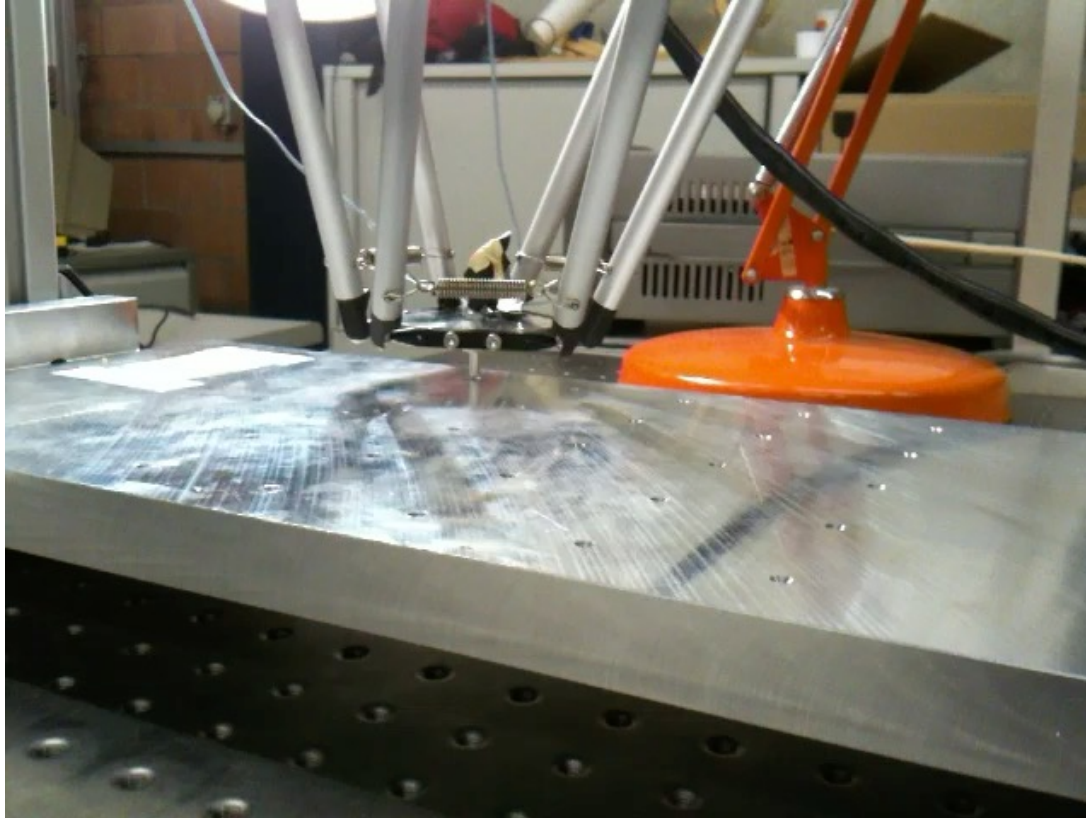
Results:

- Prior to calibration, the **workspace of the robot is distorted**, mainly due to bad length identification of the robot arms.
- **Twisting, tilting and scaling effects** are removed from the workspace of the robot
- Resulting **absolute accuracy** over the workspace $< 20 \text{ } \mu\text{m}$



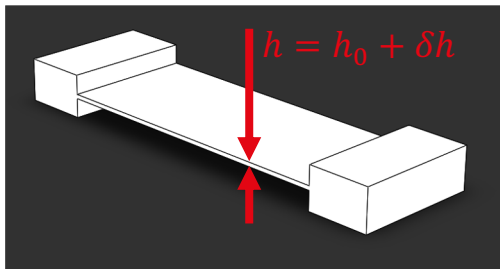
Calibration example: Kheops robot



Kheops robot's tool stays at 0.2 mm of the surface



Flexure's manufacturing tolerance calculation

δh depends mainly on the manufacturing technology



SPRINGS			STIFFNESS K: N/m K_a : Nm/rad	ADMISSIBLE STROKE x: m α : rad
BENDING	PURE		$K = \frac{E \cdot b \cdot h^3}{12 \cdot l}$	$\alpha = \frac{2 \cdot \sigma \cdot l}{E \cdot h}$
	SIMPLE		$K = \frac{E \cdot b \cdot h^3}{4 \cdot l^3}$	$x = \frac{2 \cdot \sigma \cdot l^2}{3 \cdot E \cdot h}$

STIFFNESS

$$K = K_0 \cdot \left(\frac{h_0 + \delta h}{h_0} \right)^3 = K_0 \cdot \left(1 + 3 \frac{\delta h}{h_0} + 3 \frac{\delta h^2}{h_0^2} + \frac{\delta h^3}{h_0^3} \right) \cong K_0 \cdot \left(1 + 3 \frac{\delta h}{h_0} \right)$$

$\frac{\delta h}{h_0} \ll 1$

$$\Delta K \cong 3 \frac{\delta h}{h_0}$$

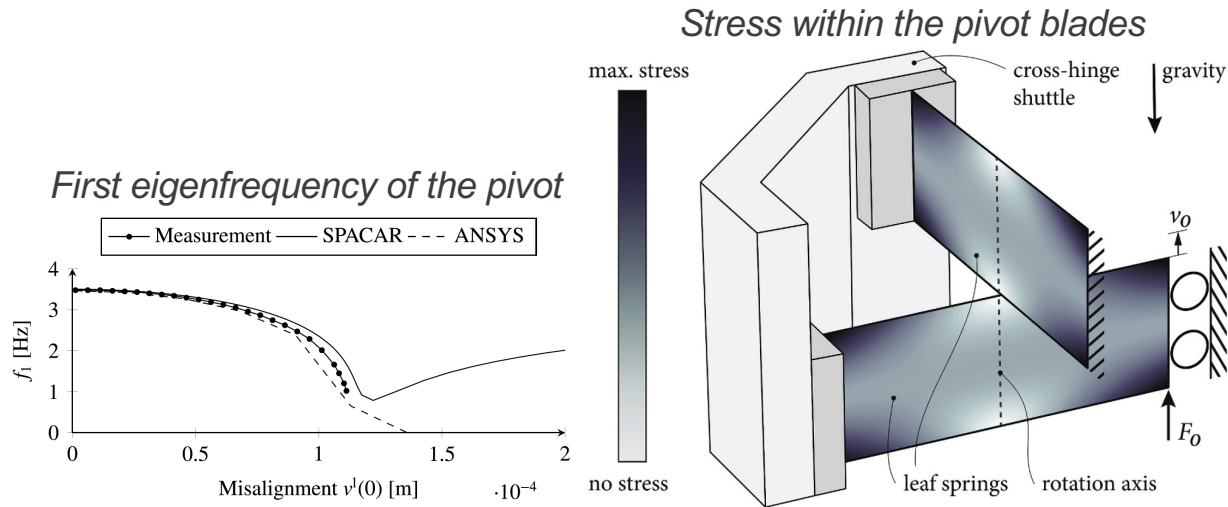
STRESS

$$\sigma \sim h$$

$$\Delta \sigma \cong \frac{\delta h}{h_0}$$

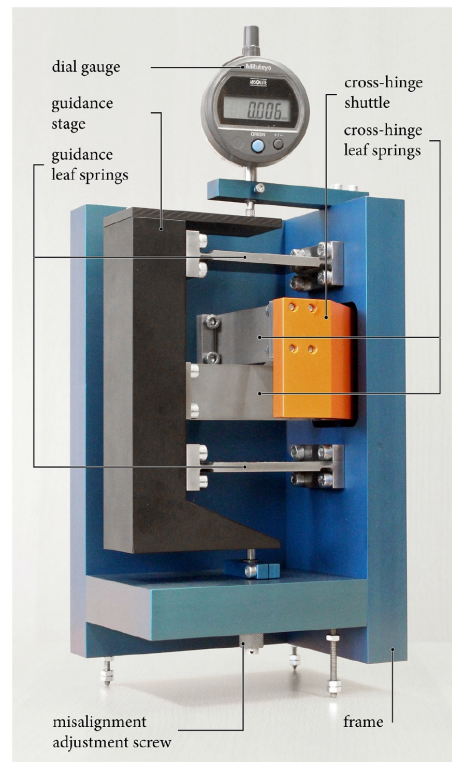
Flexure's assembly tolerance calculation

- The effect of assembly tolerances is assessed
- Analytical and FEM values are compared with measurements



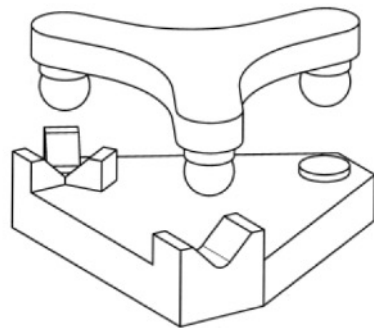
Overconstrained cross-hinge design consisting of two leaf springs. Gray scales in the leaf springs represent the von Mises stress distribution caused by misalignment v_0 due to a force F_0 .

Experimental setup

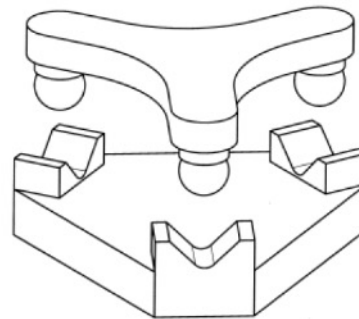


Kinematic coupling: Kelvin and Maxwell Clamps

- Kinematic couplings are **exact constraint design couplings** because they use six known contact points to locate one component with respect to another.
- They have long been known to provide an **economical and dependable method** for attaining high repeatability in fixtures.
- **Kinematic couplings are deterministic** because they only make contact at a number of points equal to the number of degrees of freedom that are to be restrained.



Kelvin clamp



Maxwell clamp

Kinematic coupling: Hertzian contact

- Heinrich Hertz is a mathematician famous for his work in the frequency domain
- He also created the first analytical solution for determining the stress between two bodies in point contact
- Exact constraint design often creates contact at single points

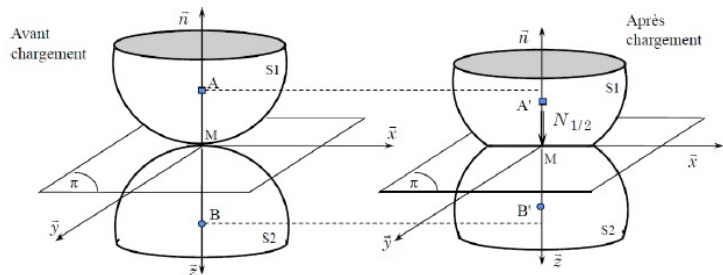


FIGURE 3 – Modélisation des déformations

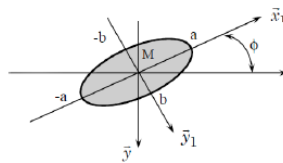


FIGURE 4 – Zone de contact

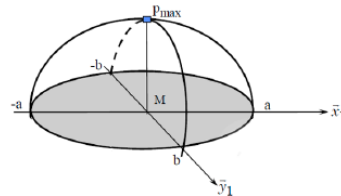
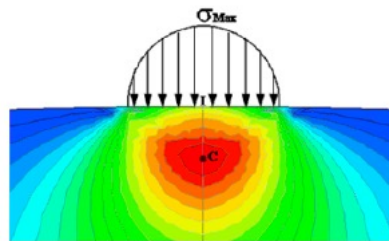
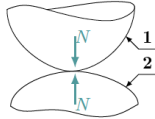
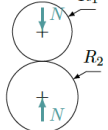
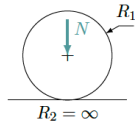
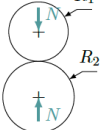
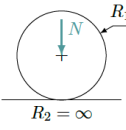
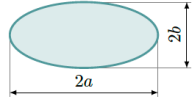

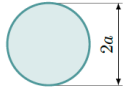

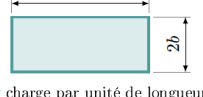


FIGURE 5 – Répartition de pression (ellipsoïde)

On détermine alors : $p_{moy} = \frac{N_{1 \rightarrow 2}}{\pi ab}$ et $p_{max} = \frac{3}{2} p_{moy} \Rightarrow p_{max} = \frac{3 N_{1 \rightarrow 2}}{2 \pi ab}$



Kinematic coupling: Hertzian contact

		Contact ponctuel			Contact linéique	
Types de contacts		Solides quelconques 	Sphère/sphère 	Sphère/plan 	Cylindre/cylindre 	Cylindre/plan 
Surface de contact	Forme	Ellipse (a, b) 	Cercle (a) 	Cercle (a) 	Rectangle (infinity, b) 	Rectangle (infinity, b) 
	Dimensions	$a = m \sqrt{\frac{3\pi}{2} \frac{k_1 + k_2}{C_1 + C_1' + C_2 + C_2'} N}$ $b = \frac{n}{m} a$	$a = \sqrt[3]{\frac{3\pi}{4} (k_1 + k_2) \frac{R_1 R_2}{R_1 + R_2} N}$	$a = \sqrt[3]{\frac{3\pi}{4} (k_1 + k_2) R N}$	$b = 2 \sqrt{(k_1 + k_2) \frac{R_1 R_2}{R_1 + R_2} q}$	$b = 2 \sqrt{(k_1 + k_2) q R}$
Rapprochement δ		$\delta = r \frac{3\pi}{4a} (k_1 + k_2) N$	$\delta = \sqrt[3]{\frac{9\pi^2}{16} (k_1 + k_2)^2 \frac{R_1 + R_2}{R_1 R_2} N^2}$	$\delta = \sqrt[3]{\frac{9\pi^2}{16} \frac{(k_1 + k_2)^2}{R} N^2}$	$\delta = 3,84 \cdot 10^{-5} \frac{N^{0,9}}{L^{0,8}}$ (acier)	
Pression max p_{\max}		$p_{\max} = \frac{3 N}{2 \pi a b}$	$p_{\max} = \frac{3 N}{2 \pi a^2}$	$p_{\max} = \frac{3 N}{2 \pi a^2}$	$p_{\max} = 0,59 \sqrt{\frac{E_1 E_2}{E_1 + E_2} \frac{R_1 + R_2}{R_1 R_2} q}$ Si $\nu = 0,3$: $p_{\max} = \frac{2N}{\pi L b} = \frac{2q}{\pi b}$ $p_{\max} = \frac{1}{\pi} \sqrt{\frac{1}{k_1 + k_2} \frac{R_1 + R_2}{R_1 R_2} q}$	$p_{\max} = 0,59 \sqrt{\frac{E_1 E_2}{E_1 + E_2} \frac{1}{R} q}$ Si $\nu = 0,3$: $p_{\max} = \frac{2N}{\pi L b} = \frac{2q}{\pi b}$ $p_{\max} = \frac{1}{\pi} \sqrt{\frac{1}{k_1 + k_2} \frac{1}{R} q}$
Profondeur pour τ_{\max} (pour $\nu = 0,3$)		Fonction de l'excentration de l'ellipse	$h = 0,5a$	$h = 0,5a$	$h = \frac{\pi}{4} b$	$h \approx 0,78b$

* avec : $k_i = \frac{1 - \nu_i^2}{\pi E_i}$

Kinematic coupling parameters

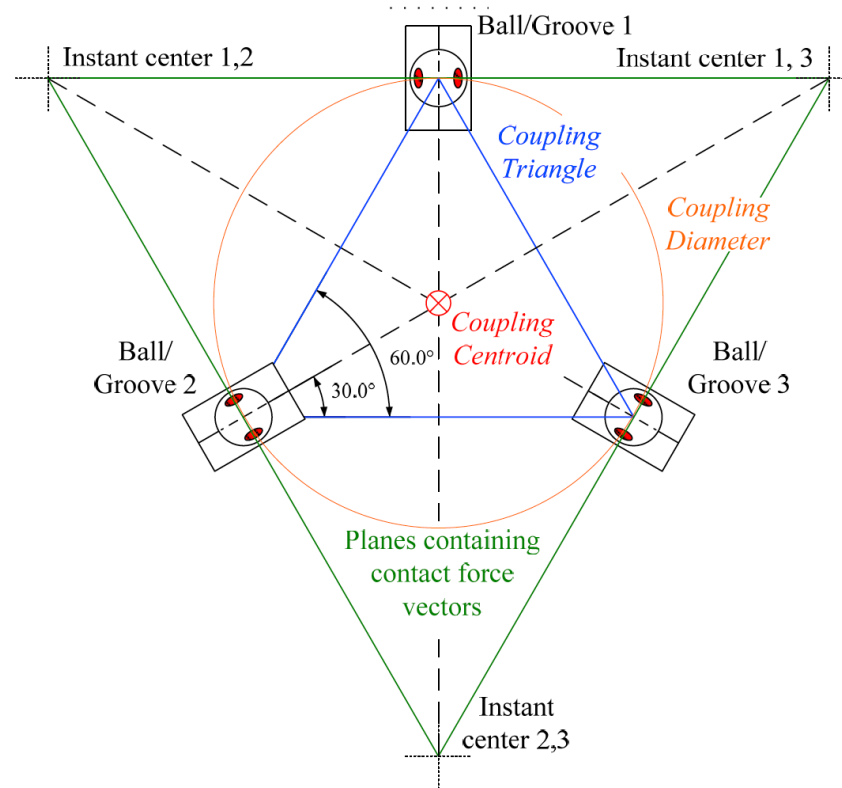
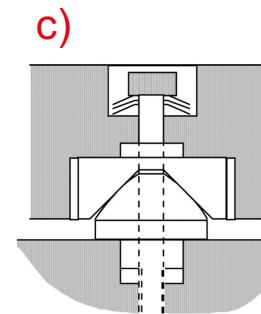
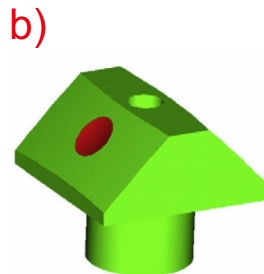
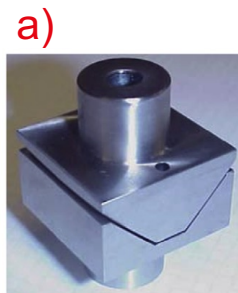


Figure 5 Geometric parameters for a three groove kinematic coupling.

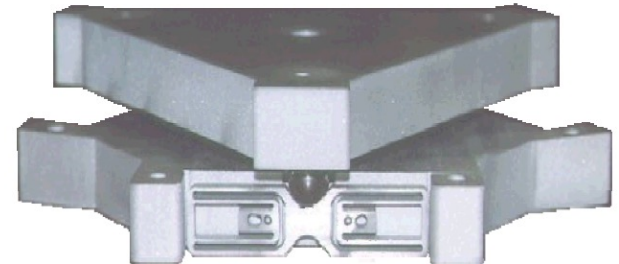
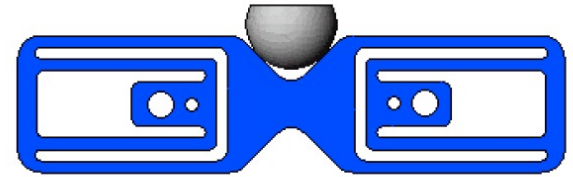
Kinematic coupling: Canoe ball

- Acts like a **ball 1 meter in diameter**
 - Has **100 times the stiffness** and **load capacity** of a normal **1" ball**
 - The **large shallow Hertzian zone** is very repeatable
- a) Modular “Canoe ball” and vee
- b) Solid model showing Hertz contact zone used in the kinematic coupling.
- c) Preloading a kinematic coupling through the coupling elements to avoid deforming the rest of the structure.



Flexural Kinematic coupling

- Combines the **repeatable location** of traditional kinematic couplings with the **stiffness characteristics** of many other coupling methods
- After the kinematic members (3 "balls" and 3 "grooves") are mated, **force is applied to bring the two components together.**
- Parts of the kinematic coupling (flexures attached to one of the major components) displace and allow the components to mate, thereby creating a **classical surface-to-surface, high load capacity joint.**
- When properly designed, this can be accomplished **without compromising the kinematic nature of the coupling.**

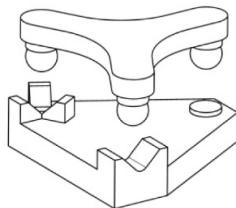


Kinematic coupling: repeatability calculation

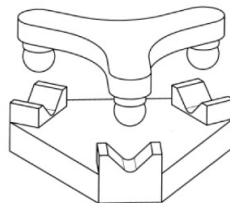
Nonrepeatability (ρ) due to friction decreases linearly with decreasing coefficient of friction between the balls and grooves, following the general relation between the friction coefficient (μ), ball radius (R), the applied load (P) and the elastic modulus (E):

$$\rho = \mu \left(\frac{2}{3R} \right)^{\frac{1}{3}} \left(\frac{P}{E} \right)^{\frac{2}{3}}$$

Kelvin clamp



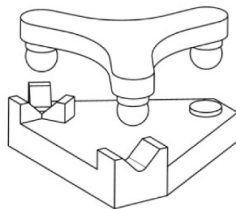
Maxwell clamp



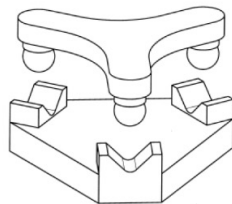
Kinematic coupling: conclusions

- Offers **very high positioning accuracy**
- **Repeatability** of the positioning is in the **sub-micron range**, generally in the order of the **surface roughness**
- **Stability zone** is limited
- Requires a **repeatable preload**
- Stiffness is limited by **hertzian contacts** and by the **rigid bodies' rigidity**
- **More stiffness** when the **contact radius is increased**

Kelvin clamp



Maxwell clamp



Common coupling methods



Pinned Joints

No Unique Position



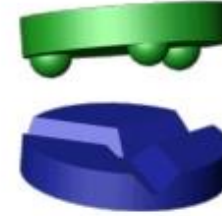
Flexural Kin. Couplings

Kinematic Constraint



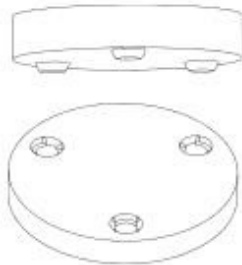
Elastic Averaging

Non-Deterministic



Kinematic Couplings

Kinematic Constraint

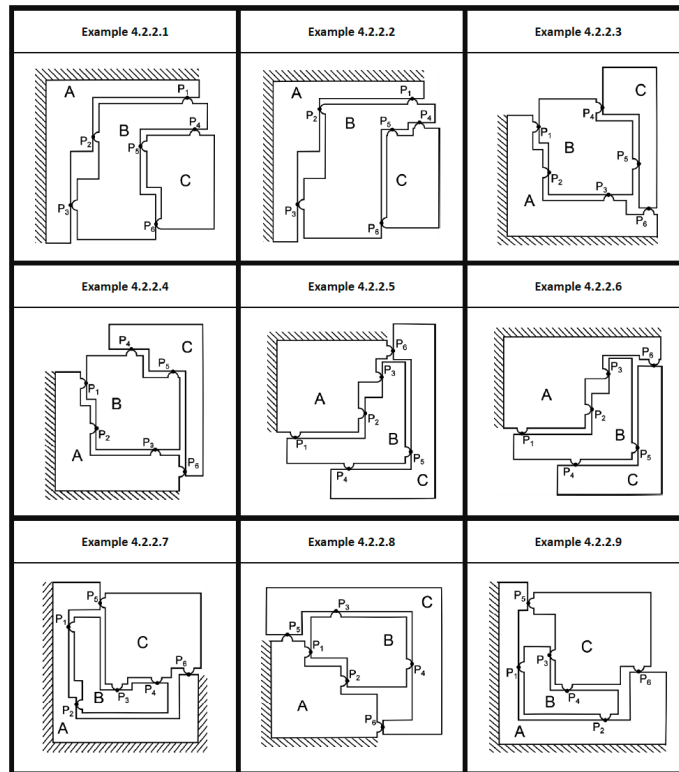


Quasi-Kinematic Couplings

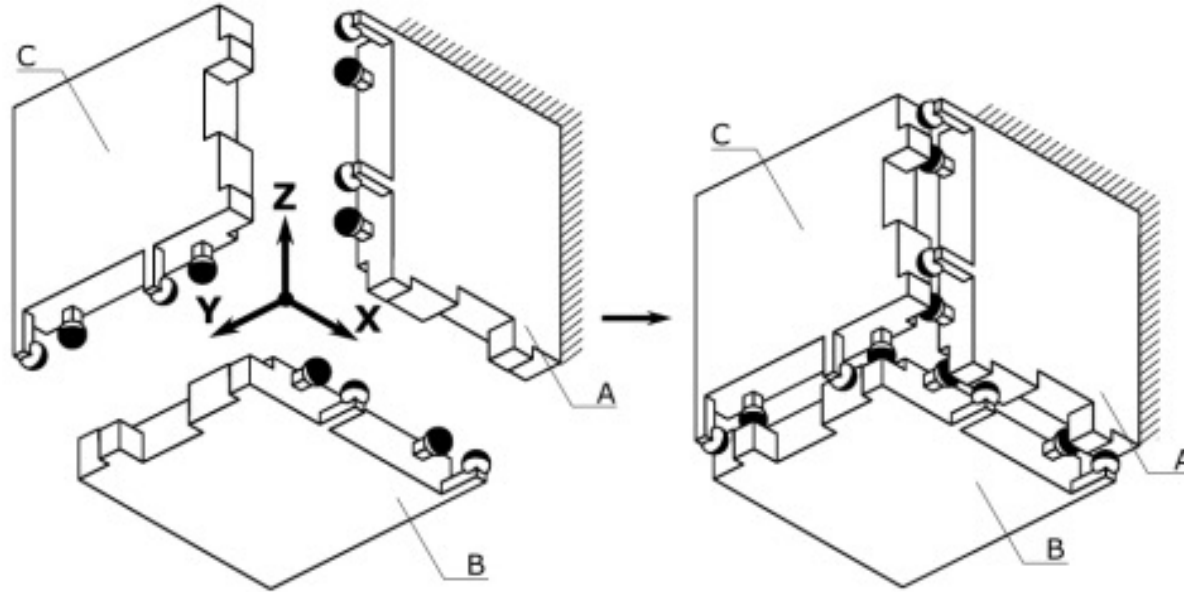
Near Kinematic Constraint

	$0.01 \mu\text{m}$	$0.10 \mu\text{m}$	$1.0 \mu\text{m}$	$10 \mu\text{m}$	$100 \mu\text{m}$
Pinned Joints					
Flexural Kinematic Couplings					
Elastic Averaging					
Quasi-Kinematic Couplings					
Kinematic Couplings					

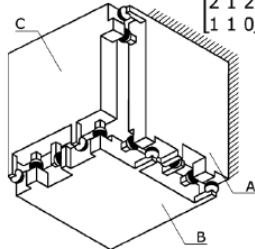
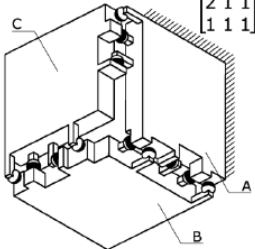
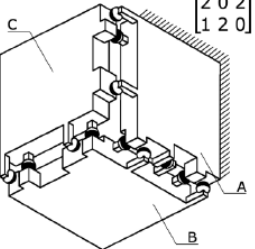
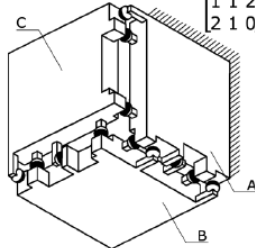
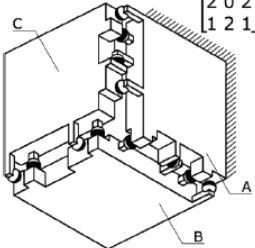
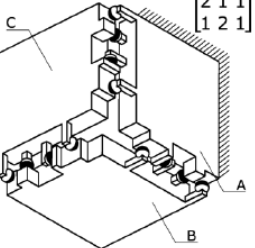
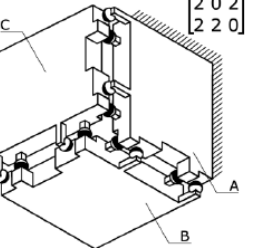
Kinematic coupling (3 bodies – 2D)



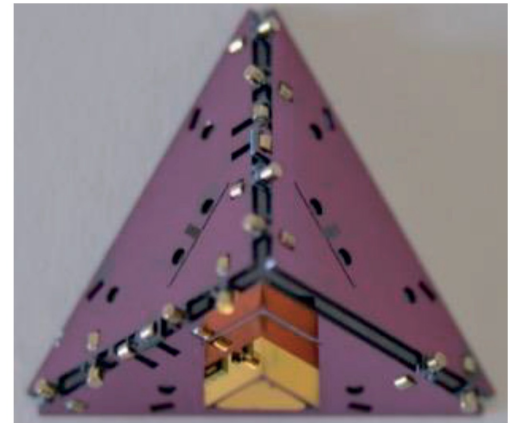
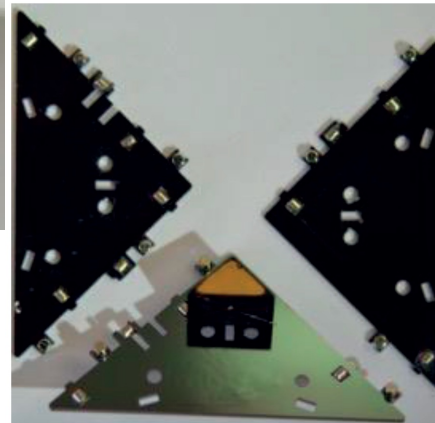
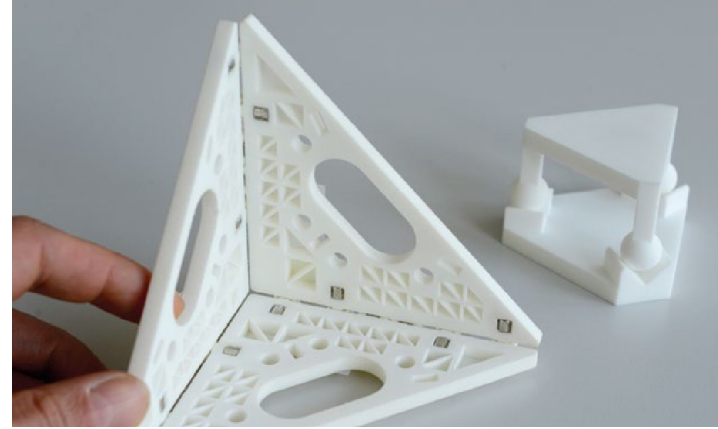
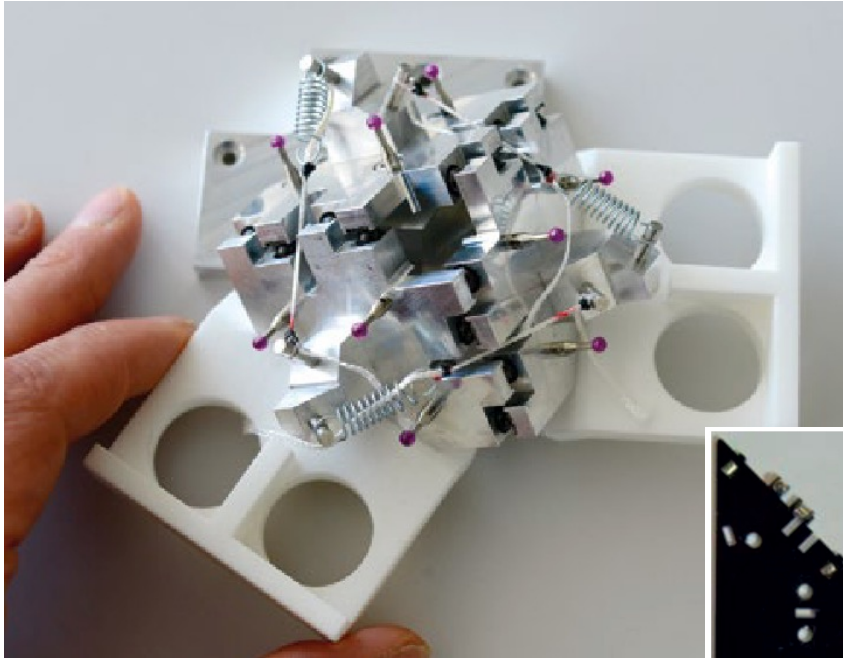
Kinematic coupling (3 bodies – 3D)



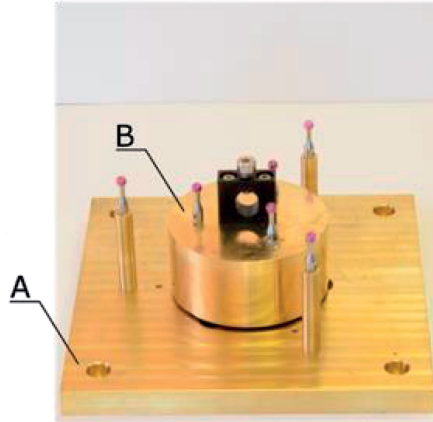
Kinematic coupling (3 bodies - 3D)

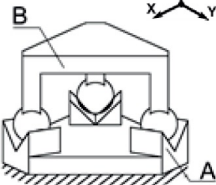
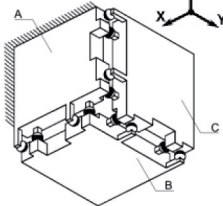
Example 7.4.2.1	Example 7.4.2.2	Example 7.4.2.3	
 $\begin{bmatrix} 1 & 2 & 2 \\ 2 & 1 & 2 \\ 1 & 1 & 0 \end{bmatrix}$	 $\begin{bmatrix} 1 & 2 & 2 \\ 2 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}$	 $\begin{bmatrix} 1 & 2 & 2 \\ 2 & 0 & 2 \\ 1 & 2 & 0 \end{bmatrix}$	
Figure 7.4.2.1	Figure 7.4.2.2	Figure 7.4.2.3	
Example 7.4.2.4	Example 7.4.2.5	Example 7.4.2.6	Example 7.4.2.7
 $\begin{bmatrix} 1 & 2 & 2 \\ 1 & 1 & 2 \\ 2 & 1 & 0 \end{bmatrix}$	 $\begin{bmatrix} 1 & 2 & 1 \\ 2 & 0 & 2 \\ 1 & 2 & 1 \end{bmatrix}$	 $\begin{bmatrix} 1 & 1 & 2 \\ 2 & 1 & 1 \\ 1 & 2 & 1 \end{bmatrix}$	 $\begin{bmatrix} 0 & 2 & 2 \\ 2 & 0 & 2 \\ 2 & 2 & 0 \end{bmatrix}$
Figure 7.4.2.4	Figure 7.4.2.5	Figure 7.4.2.6	Figure 7.4.2.7

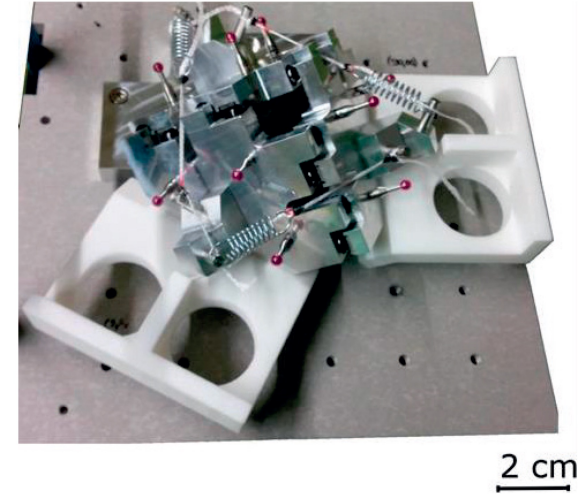
Kinematic coupling (3 bodies – 3D)



Kinematic coupling (3 bodies - 3D)



		Average		
		Three-Vee	Example 7.3.2.7	
				
			Body	
			B	C
Degree of Freedom (DOF)	D	0.178 μm	0.902 μm	0.712 μm
	α	5 μrad	42 μrad	31 μrad
Number of measurements		10	3	



Week 10 exercises and homework

Exercise on MOODLE:

- EXO10_Balancing_II.pdf

Homework:

- No homework