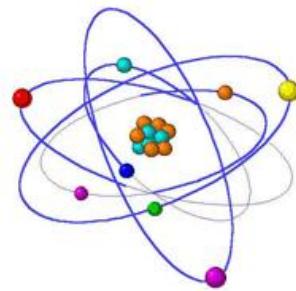


# Introduction to Nuclear Engineering

## ME 464

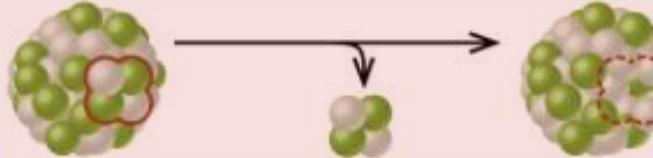
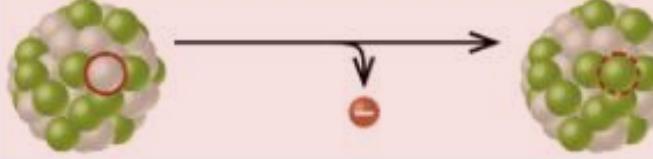
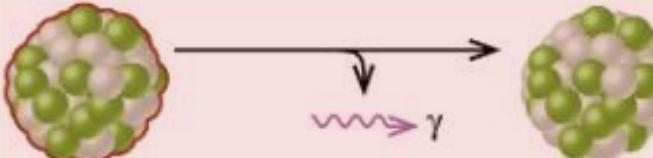
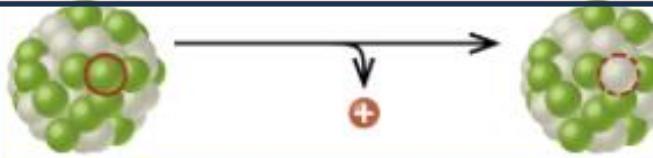
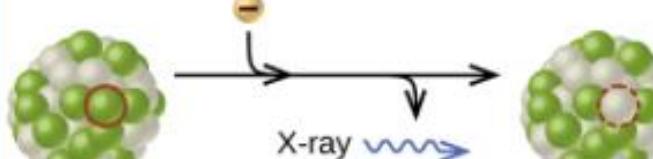


### Radiation protection

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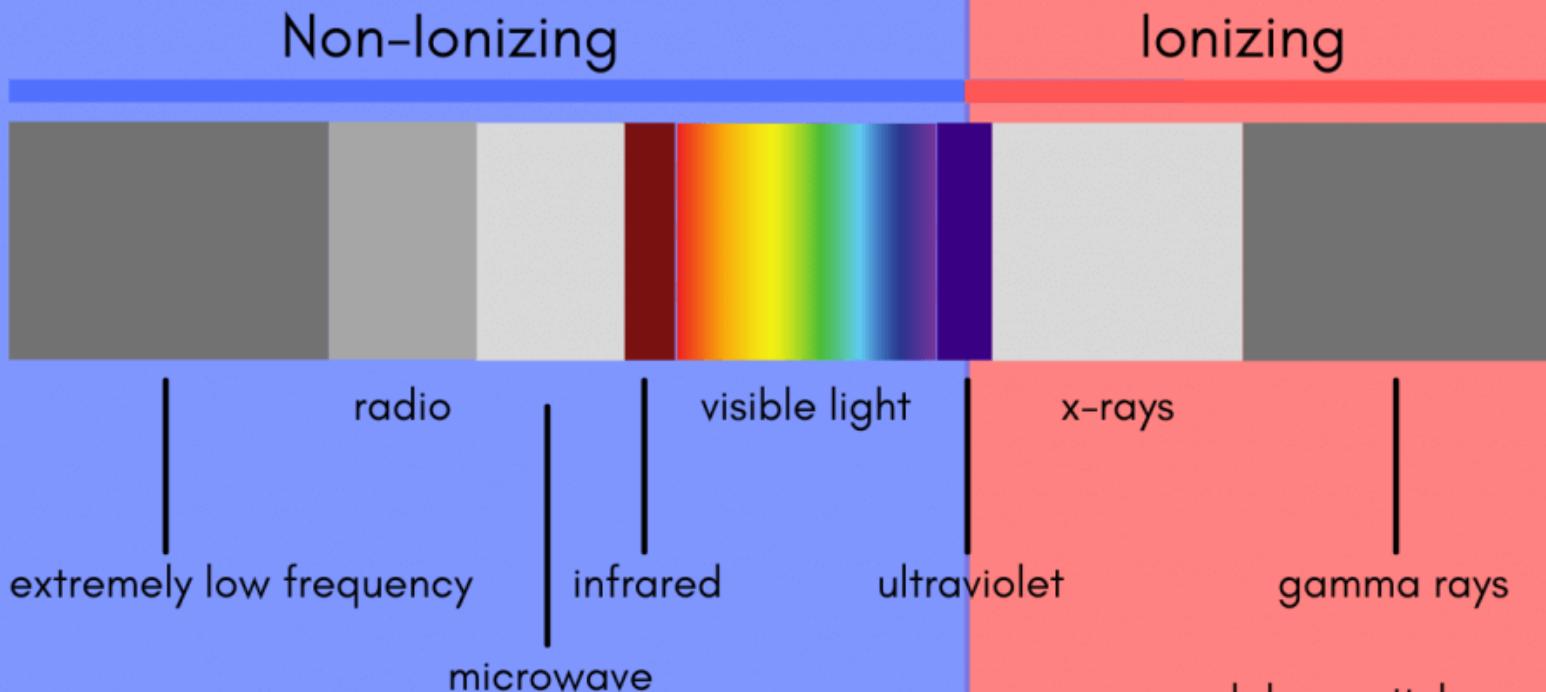
- Interaction of radiation with matter
- Concept of Dose, absorbed, equivalent and effective
- Origin of an average annual effective dose
  - Radionuclides in the environment
- Interaction of radiations with biological systems
  - Effect of radiations on DNA
- Radiation Shielding and Protection

## Main Types of Radiation

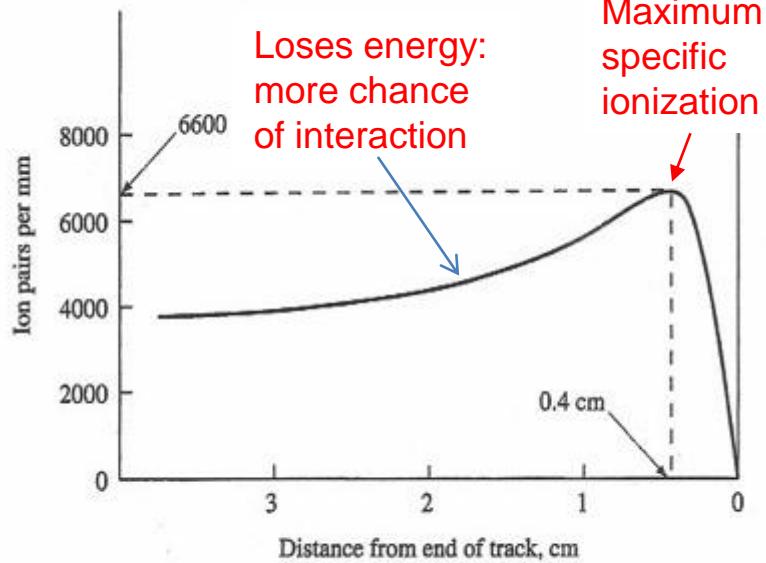
Type	Nuclear equation	Representation	Change in mass/atomic numbers
Alpha decay	${}_{Z}^{A}X \rightarrow {}_{2}^{4}\text{He} + {}_{Z-2}^{A-4}Y$		A: decrease by 4 Z: decrease by 2
Beta decay	${}_{Z}^{A}X \rightarrow {}_{-1}^{0}\text{e} + {}_{Z+1}^{A}Y$		A: unchanged Z: increase by 1
Gamma decay	${}_{Z}^{A}X \rightarrow {}_{0}^{0}\gamma + {}_{Z}^{A}Y$	 Excited nuclear state	A: unchanged Z: unchanged
Positron emission	${}_{Z}^{A}X \rightarrow {}_{+1}^{0}\text{e} + {}_{Z-1}^{A}Y$		A: unchanged Z: decrease by 1
Electron capture	${}_{Z}^{A}X + {}_{-1}^{0}\text{e} \rightarrow {}_{Z-1}^{A}Y + \text{X-ray}$		A: unchanged Z: decrease by 1

- There are four general types of radiation generated in **nuclear** and **atomic** processes:
  - **Charged particles:**
    - Fast electrons: *beta*<sup>+</sup> and *beta*<sup>-</sup> from nuclear decay.
    - Heavy charged particles: all energetic ions with  $A \geq 1$  (*p*<sup>+</sup>, *alpha*<sup>2+</sup>, fission products, nuclear reaction products)
  - **Uncharged particles:**
    - Electromagnetic radiation: photons, X-rays (from electron transitions between atomic shells), gamma-rays (from nuclear transitions)
    - Neutrons: slow and fast (generated in nuclear reactions.)

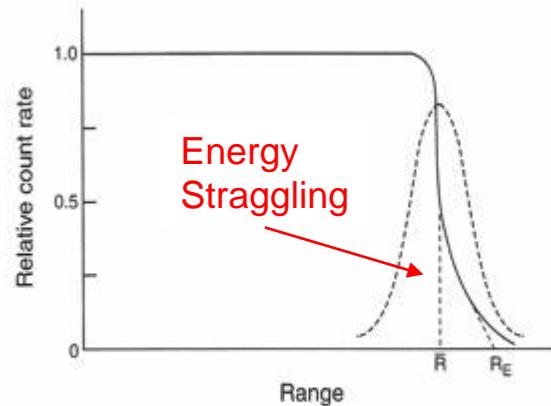
## Non-Ionizing and Ionizing Radiation



- ❑ Alphas lose energy primarily by **ionizing** the atoms in the medium (i.e. energy is transferred to electrons).
- ❑ The specific ionization (number of ion-electron pairs created per cm) of alpha particles follows a **Bragg curve**.
- ❑ The range  $R$  is well defined and relatively abrupt, as the alpha particle continues to penetrate (with gradually lower energy) until it is finally stopped
- ❑ Range of few cm in standard air

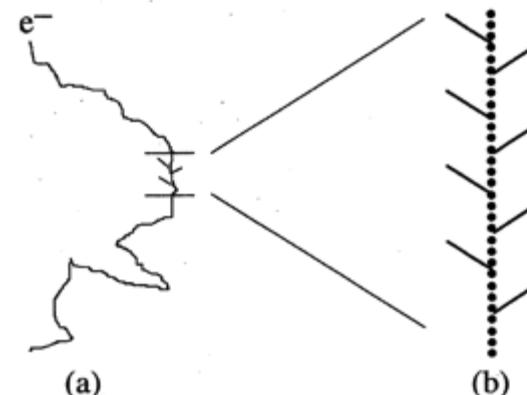


Specific ionization of an  $\alpha$ -particle in air.

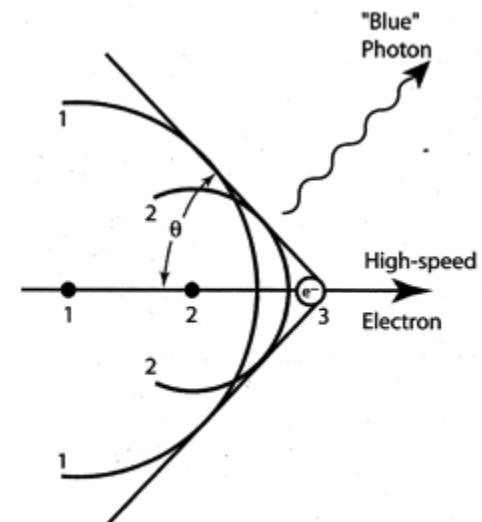


Range in air of a collimated monoenergetic source of alpha particles showing straggling that is normally distributed about the mean range at  $\bar{R}$ . An extrapolated range,  $R_E$ , can be obtained by extending the straight-line portion of the curve to the  $x$ -axis.

- Beta particles lose energy mostly by **ionization**
  - Direct ionization (main mechanism)
  - “Delta” rays from electrons ejected by ionization.
  - Beta particle paths are tortuous:
  
- At higher energies other mechanism become relevant:
  - **Bremsstrahlung** - occurs when beta particles are decelerated or deflected by the electric fields of nuclei in the medium, resulting in the emission of X-rays
  - **Cherenkov radiation** caused by high-speed beta particles in media if  $(v/c) > (1/n)$ ,  $n$ =refractive index of the medium.



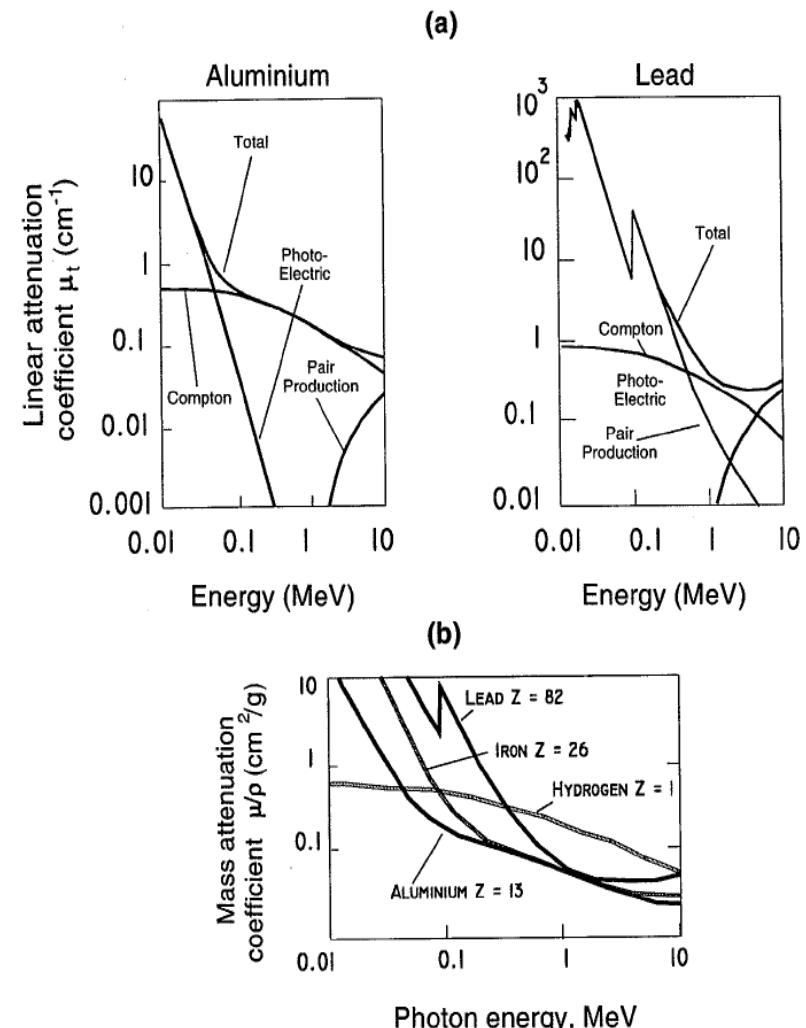
(a) Range and ionization path of a beta particle in an absorbing medium; (b) amplified segment of ionization track showing delta ray tracks produced by ejected electrons.



Wavefronts produced by a particle with velocity  $\geq c/n$  constructively interfere to produce blue photons of light, or Cherenkov radiation.

- Photons lose energy interacting with matter **mainly** by:
  - Photoelectric effect ( $E < 0.5$  MeV)**  
 $\sigma_{pe} \sim Z^n/E^3$  ( $n=4-5$ )
  - Compton Scattering ( $E$  0.5 - 1.0 MeV)**  $\sigma_c \sim Z/E$
  - Pair Production ( $E > 1.022$  MeV)**  
 $\sigma_{pp} \sim Z^2 \cdot 1/(E)$
- Attenuation follows exponential law with attenuation coefficient:  $\mu_{tot} = \mu_{pe} + \mu_c + \mu_{pp}$

$$I(x) = I_0 e^{-\mu x}$$



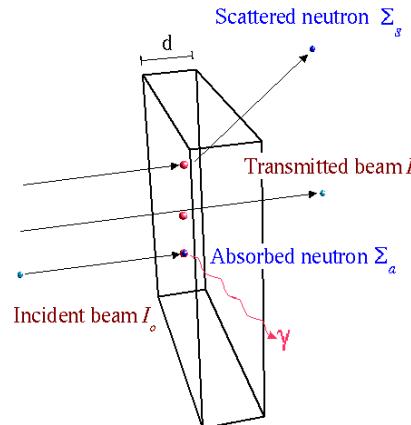
Total linear and mass attenuation coefficients ( $\mu_t$  cm<sup>-1</sup> and  $\mu_m$  cm<sup>2</sup>/g) for  $\gamma$  rays. (a)  $\mu_t$  values for aluminium ( $Z=13$ ,  $\rho=2.70$  g/cm<sup>3</sup>) and lead ( $Z=82$ ,  $\rho=11.3$  g/cm<sup>3</sup>), showing the three mutually independent components. (b) The mass attenuation coefficient  $\mu_m$  for the elements H, Al, Fe and Pb. Note the different function for hydrogen.

□ Neutrons ( $n$ ) interact with matter (nuclei) in many ways:

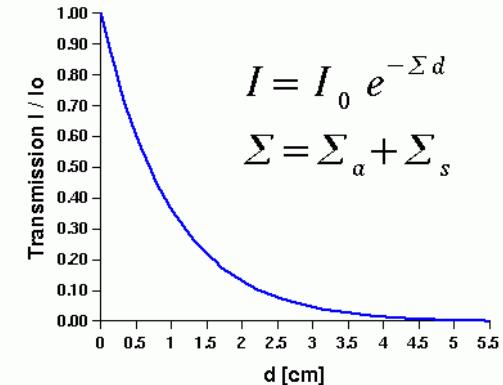
- Elastic scattering:  ${}^A Z(n,n){}^A Z$  ; energy loss of  $n$  is highest for light nuclei
- Inelastic scattering:  ${}^A Z(n,n'){}^A Z^*$
- Radiative capture:  ${}^A Z(n,g){}^{A+1} Z$
- Nuclear reactions:  ${}^A Z(n,p)$ ,  ${}^A Z(n,a)$ ,  ${}^A Z(n,2n)$ , ...
- Fission of heavy nuclei:  ${}^A Z(n,f)$

### Narrow Beam Attenuation

$$I = I_0 e^{-\Sigma d}$$



### Exponential Attenuation Law



### Macroscopic Cross Section $\Sigma$

$$\Sigma = N \sigma \quad [cm^{-1}]$$

$$N = \frac{\rho}{A} N_A \quad [cm^{-3}]$$

$N$  := number density [ $cm^{-3}$ ]

$\rho$  := material density [ $g cm^{-3}$ ]

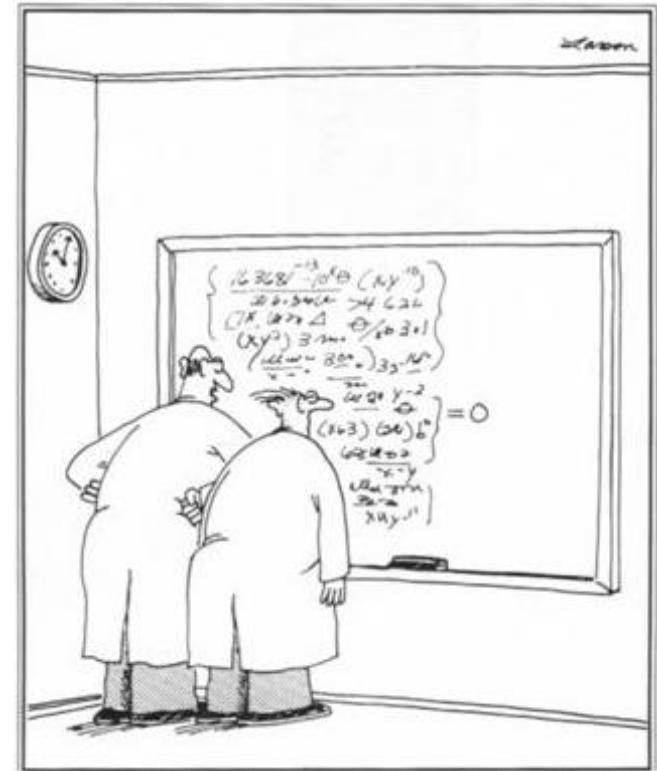
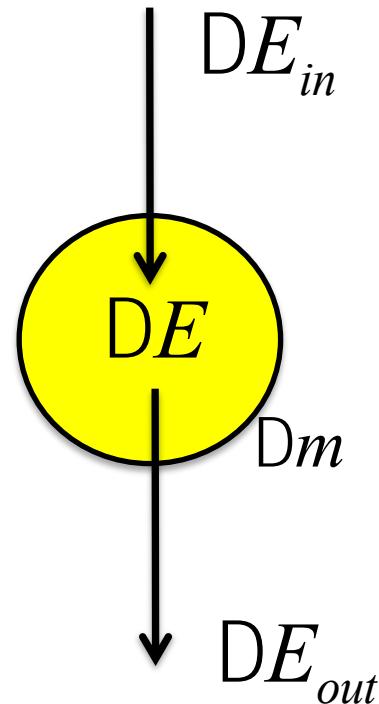
$A$  := atomic weight [ $g mol^{-1}$ ]

$N_A$  := Avogadro number  $6.022 \cdot 10^{23} [mol^{-1}]$

Absorbed dose:

- Basic **physical quantity**
- Energy deposited per unit mass
- Unit: gray (1 Gy = 1 J/kg)

$$D = \lim_{Dm \rightarrow 0} \frac{DE}{Dm}$$

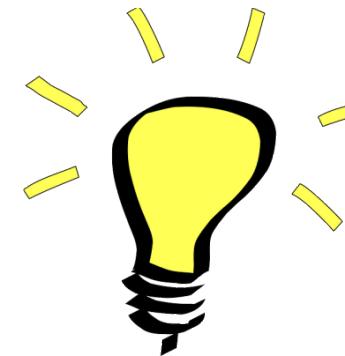


What is the increase of temperature when 3.2 liters of water receive an absorbed dose of 1 Gy?

- a) c. 10 K
- b) c. 1 K
- c) c. 0.1 K
- d) c. 20 mK
- e) c. 0.1 mK



- What is the increase of temperature when 3.2 liters of water receive an absorbed dose of 1 Gy?

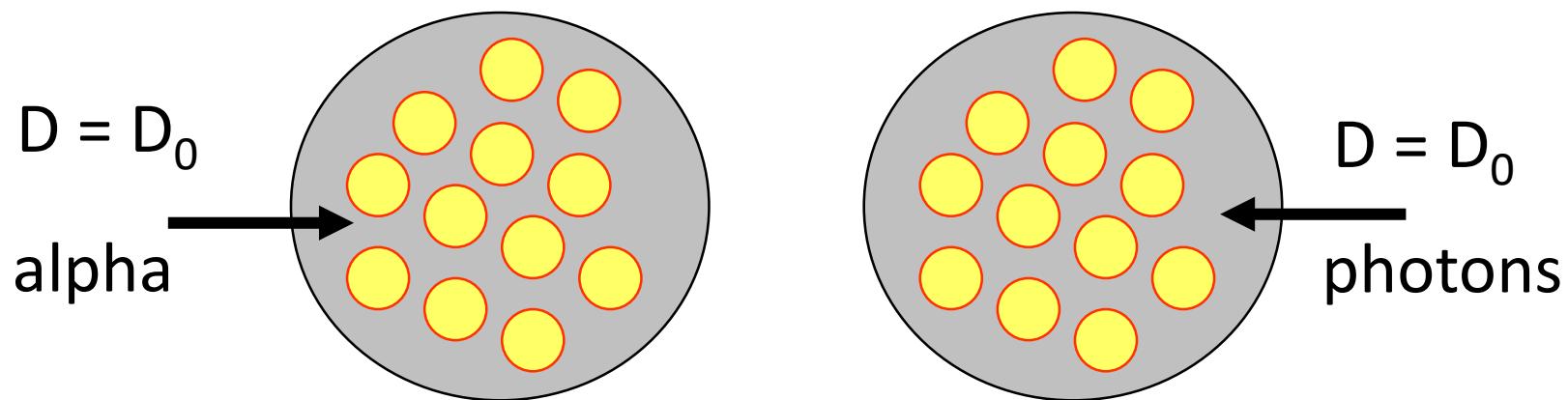


$$\Delta E = Dm = 1 \text{ Gy} \times 3.2 \text{ kg} = 3.2 \text{ J}$$

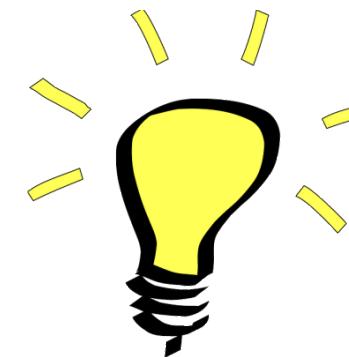
$$\Delta T = \frac{\Delta E}{m c_p} = \frac{3.2 \text{ J}}{3.2 \text{ kg} \times 4181 \frac{\text{J}}{\text{kg K}}} = 0.24 \text{ mK}$$

OR:  $\Delta T = \frac{D}{c_p} = \frac{1 \frac{\text{J}}{\text{kg}}}{4181 \frac{\text{J}}{\text{kg K}}}$

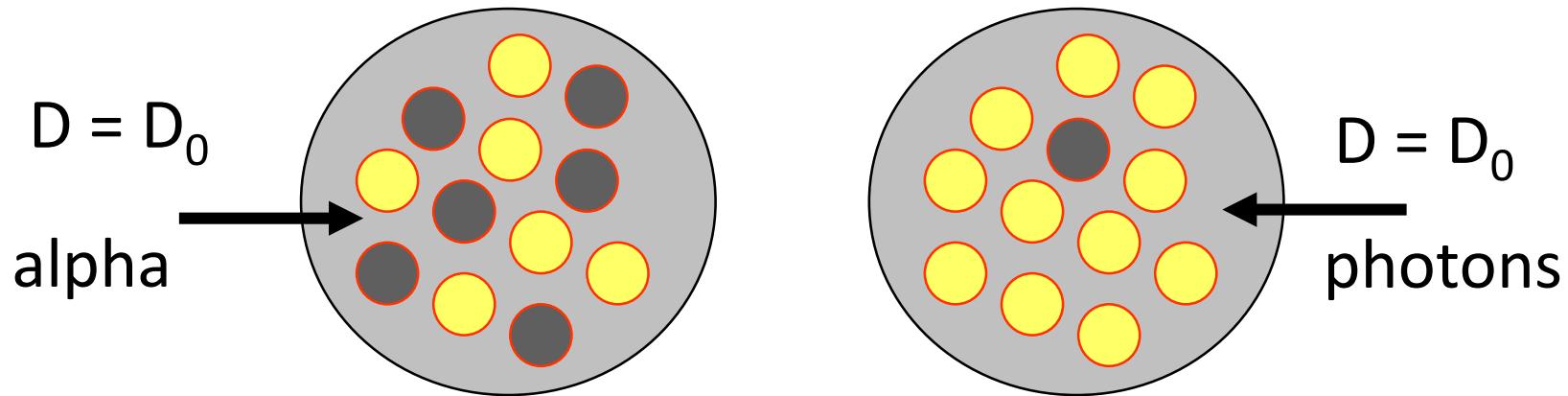
- For a given absorbed dose, what kind of radiation is the most damaging?



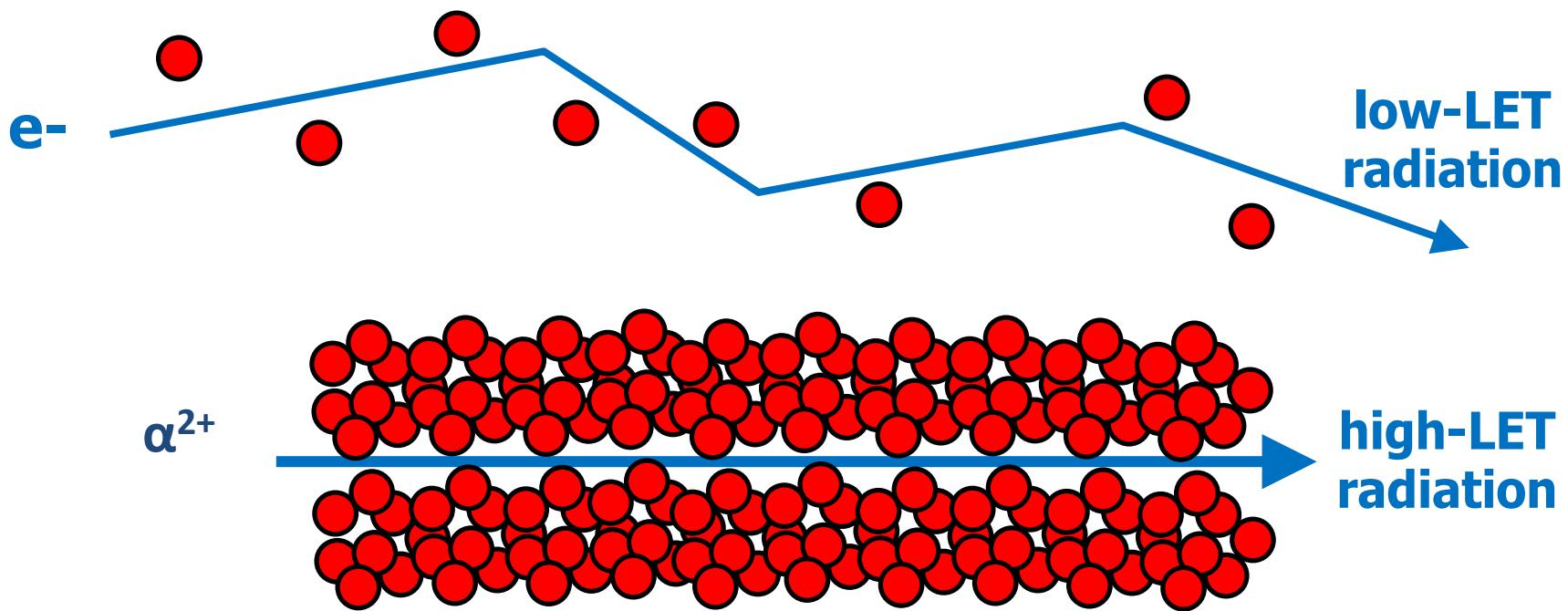
❑ For a given absorbed dose, what kind of radiation is the most damaging?



- For a given absorbed dose **alpha particles** are **more damaging** than **photons** → The absorbed dose is not always linked to the biological risk

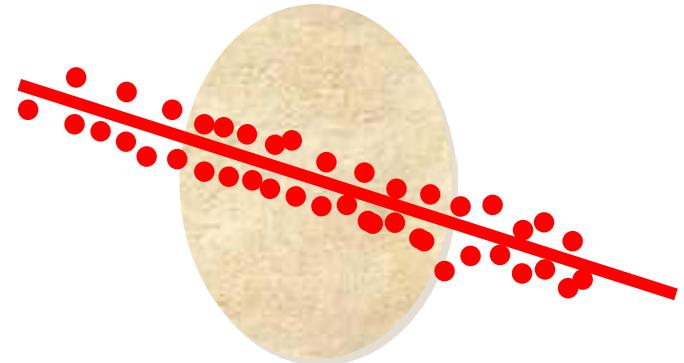
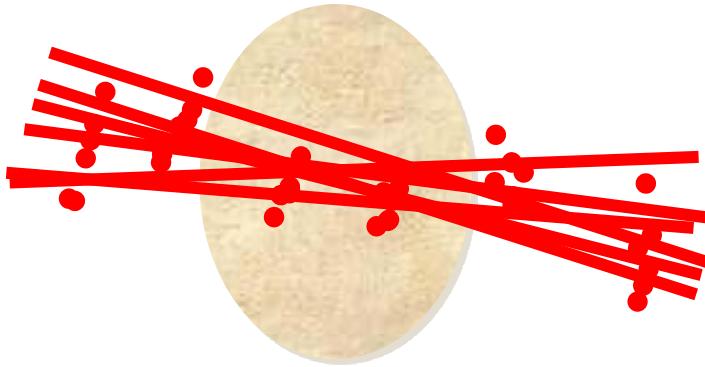


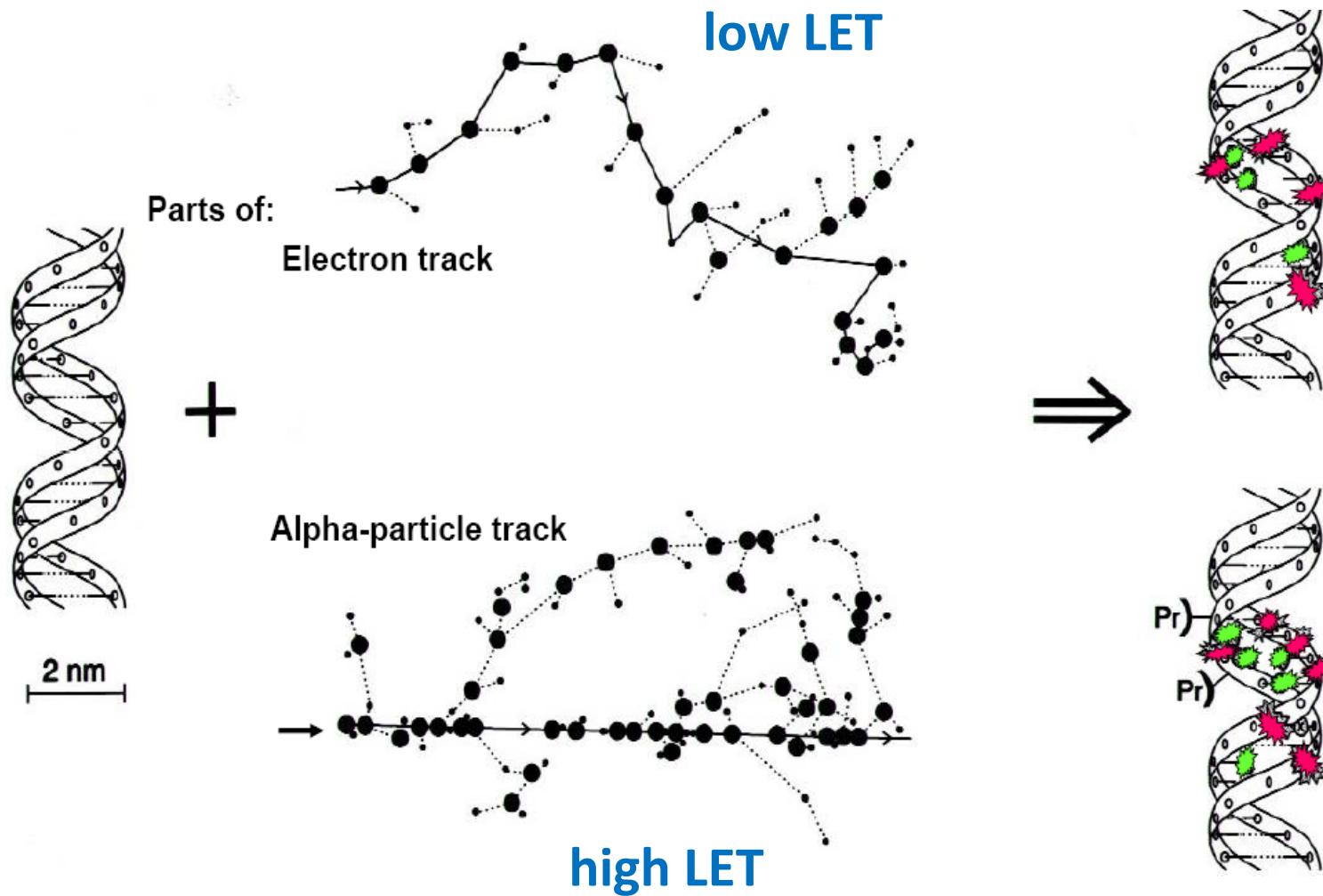
- ☐ LET explains the difference of biological efficiency



- ☐ LET: linear energy transfer ( $\approx dE_{\text{coll}}/dx$ )
  - Energy transferred through collision to the electrons of matter

- Low LET radiation
  - Many cells lightly wounded
  - Recovery probable
- High LET radiation
  - Few cells highly injured
  - Lower probability to recover





- Radiation weighting ( $w_R$ ) of the absorbed dose

- Unit: **sievert** [Sv]

equivalent dose  
to organ T

$$H_T = \sum_R w_R D_{R,T}$$

absorbed dose to the  
**organ T** delivered by  
the radiation of  
**quality R**

radiation weighting factor

Radiation	$w_R$
Photons (all energies)	1
Electrons	1
Neutrons < 1MeV	$2.5 + 18.2 \exp(-\ln(E)^2/6)$
Neutrons > 1MeV, <50 MeV	$5.0 + 17.0 \exp(-\ln(2E)^2/6)$
Neutrons >50 MeV	$2.5 + 3.25 \exp(-\ln(0.04E)^2/6)$
Protons	2
Charged particles	20

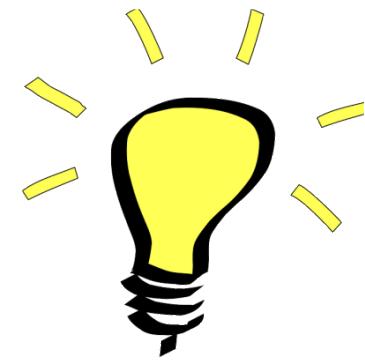
- A 2 MeV proton beam of intensity  $I=10^{10}$  proton/s/cm<sup>2</sup> and a section  $S$  of 5 cm<sup>2</sup> is used in a radiotherapy facility. A technician of mass  $m$  80 kg accidentally walk in front of the beam and stands there for 30s ( $t_{exp}$ ).
- What are the doses (absorbed/equivalent) received by the technician?



- ❑ A 2 MeV proton beam of intensity  $I=10^{10}$  proton/s/cm<sup>2</sup> and a section  $S$  of 5 cm<sup>2</sup> is used in a radiotherapy facility. A technician of mass  $m$  80 kg accidentally walk in front of the beam and stands there for 30s ( $t_{exp}$ ).
- ❑ What are the doses (absorbed/equivalent) received by the technician?

$$D = E_P \cdot I \cdot S \cdot t_{exp} \text{ 1eV/m} \quad D = 6 \cdot 10^{-3} \text{ Gy}$$

$$H_T = w_T D \quad H_T = 12 \text{ mSv}$$



- Radiation weighting ( $w_T$ ) of the absorbed dose to achieve full body dose estimate
- Unit: Sievert [Sv]

$$E = \sum_T w_T H_T$$

equivalent dose  
 to organ T

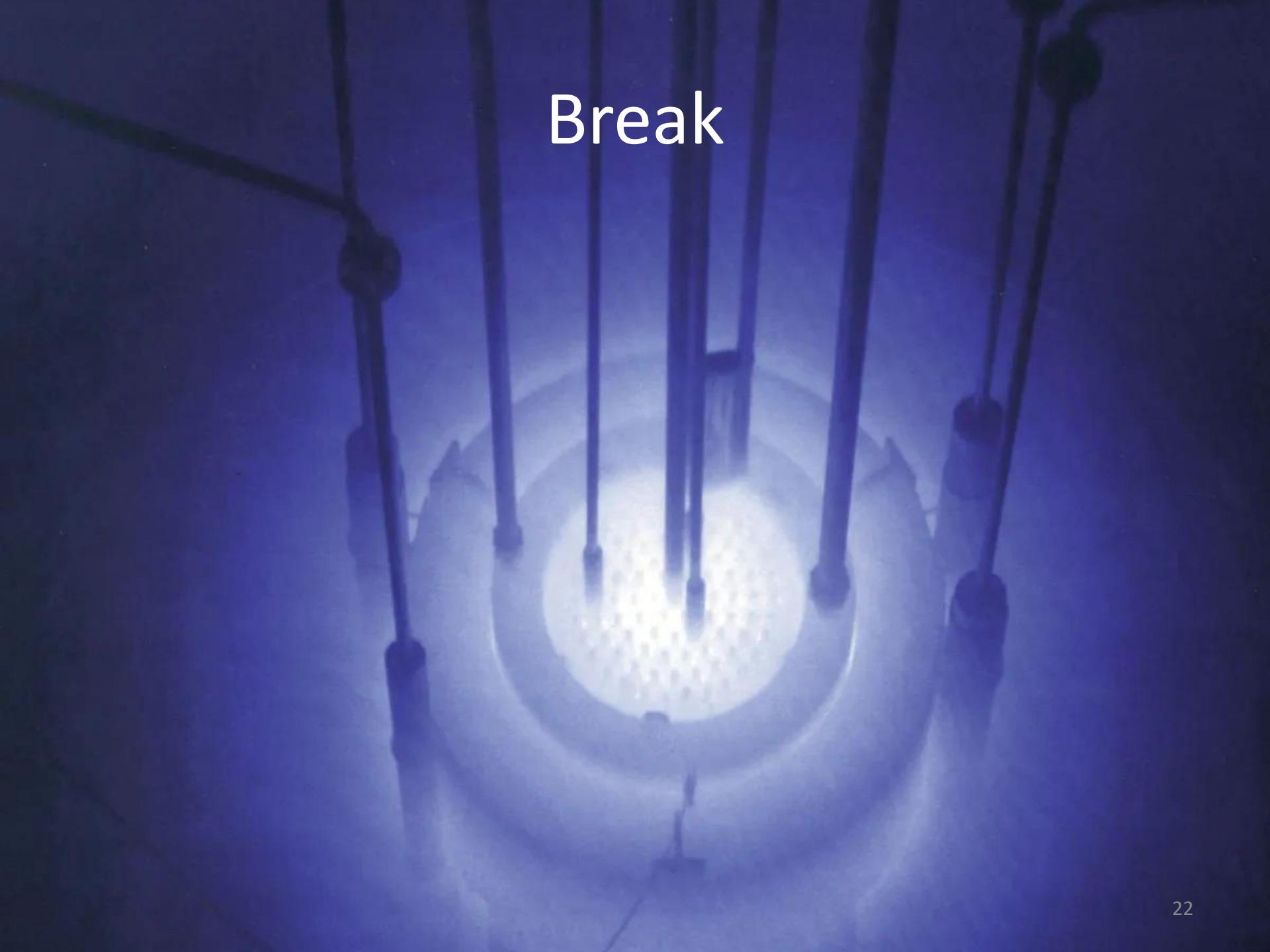
weighting factor  
 of organ T

**sex and age averaged**

**Table 3.** Recommended tissue weighting factors.

Tissue	Tissue weighting factor, $w_T$	Sum of $w_T$ values
Bone-marrow (red), colon, lung, stomach, breast, remainder tissues <sup>a</sup>	0.12	0.72
Gonads	0.08	0.08
Bladder, oesophagus, liver, thyroid	0.04	0.16
Bone surface, brain, salivary glands, skin	0.01	0.04
Total		1.00

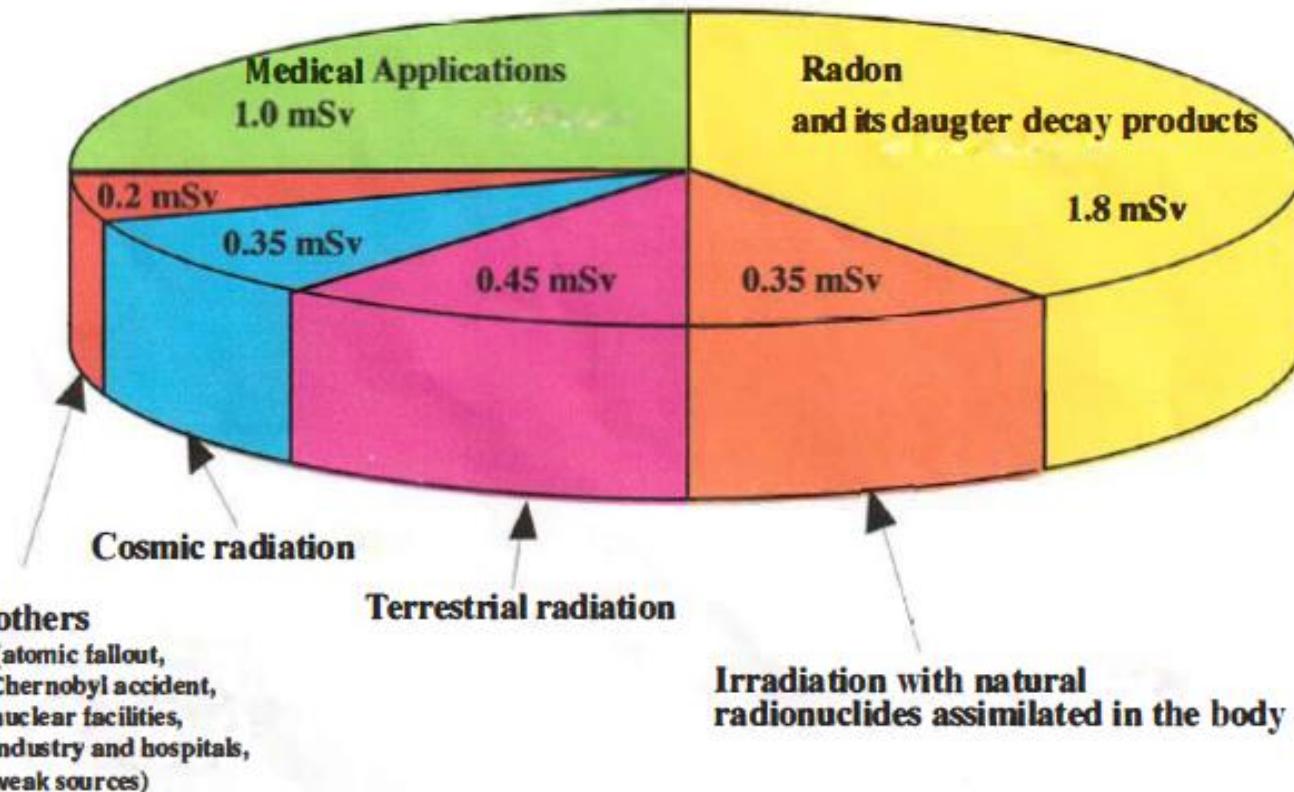
<sup>a</sup> Remainder tissues: Adrenals, extrathoracic (ET) region, gall bladder, heart, kidneys, lymphatic nodes, muscle, oral mucosa, pancreas, prostate (♂), small intestine, spleen, thymus, uterus/cervix (♀).

A dark, atmospheric image of a city skyline at night. The city is silhouetted against a bright, circular light source, likely a moon or a large street lamp, which creates a strong lens flare effect. The city lights are visible as small points of light through the haze. The overall color palette is dominated by deep blues and blacks.

# Break

## Average annual effective dose of the Swiss population in milli-Sievert

Total : 4 mSv/an ( including 3 mSv / year of natural origin )



Ref. : *Radioactivité de l'environnement et doses de rayonnements en Suisse 2003* , Office fédéral de la santé publique, Division radioprotection, Section de surveillance de la radioactivité, ISBN 3-905235-44-7

## Cosmic rays and cosmogenic radionuclides

- Cosmic radiation includes high-energy protons and atomic nuclei (originate from the **Sun**, from **outside of the solar system** and from **distant galaxies**)
  
- Interaction of cosmic rays with atmosphere can produce radionuclides e.g.
  - $^3\text{H}$  from  $^{14}\text{N}(\text{n}, \text{t}) ^{12}\text{C}$
  - $^{14}\text{C}$  from  $^{14}\text{N}(\text{n}, \text{p}) ^{14}\text{C}$
  - $^{10}\text{Be}$  from interaction of p and n with  $^{14}\text{N}$  and  $^{16}\text{O}$
  - $^{32}\text{Si}$  or  $^{36}\text{Cl}$  from interaction of cosmic rays with  $^{40}\text{Ar}$



## Terrestrial radionuclides

- Circa 70 naturally occurring radionuclides on Earth (most of them are heavy radioactive elements from the natural decay chains)

Decay series	Decay mode of the mother nuclide	Half-life of the mother nuclide [y]
$^{238}\text{U} \dots ^{226}\text{Ra} \dots ^{206}\text{Pb}$	$\alpha$	$4.468 \cdot 10^9$
$^{235}\text{U} \dots ^{207}\text{Pb}$	$\alpha$ (sf: $3.7 \cdot 10^{-7}\%$ )	$7.038 \cdot 10^8$
$^{232}\text{Th} \dots ^{208}\text{Pb}$	$\alpha$	$1.405 \cdot 10^{10}$

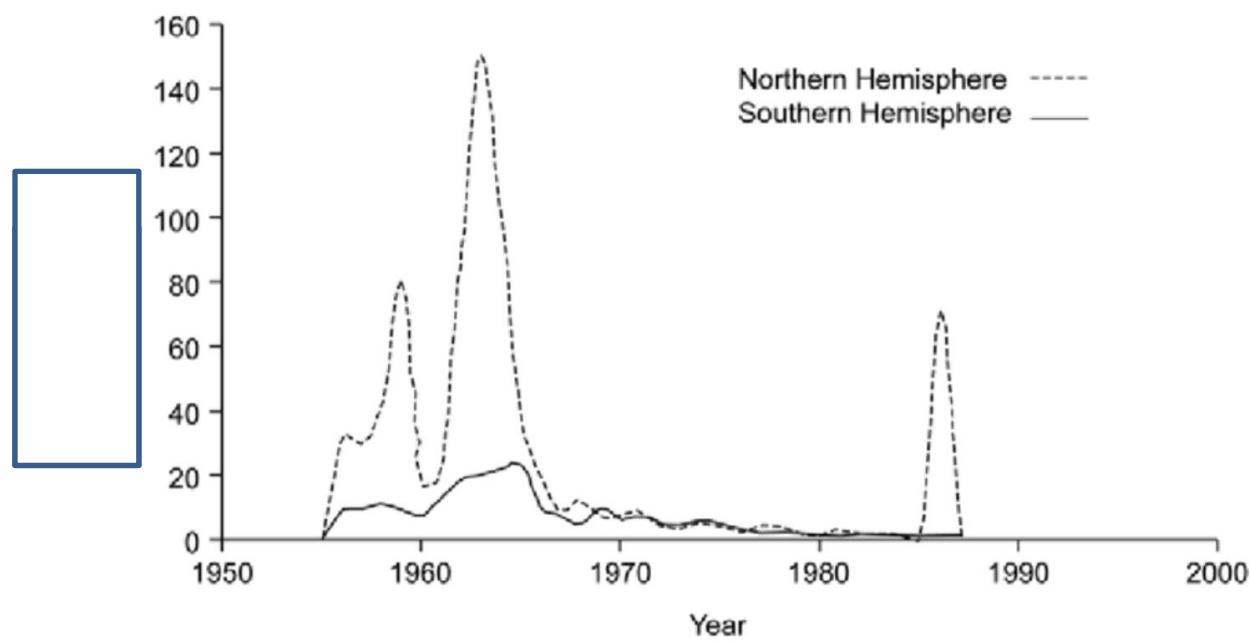
- Several important light elements, such as **H-3, C-14, K-40, etc.**

These radioactive species are ubiquitous, occurring in plants, animals, the air we breathe, the water we drink, the soil, etc. **For example**, in a 70 kg man one finds:

~ 4.4 kBq of K-40

&

~ 3.6 kBq of C-14.



## Radionuclides in food

- All foods contain natural radionuclides. The natural radioactivity in foods contributing to the radiation exposure to humans is mainly caused by the **K-40** and the long-lived radionuclides of the uranium-radium decay chain and the thorium decay chain.

...

U-238,

U-234,

Ra-226,

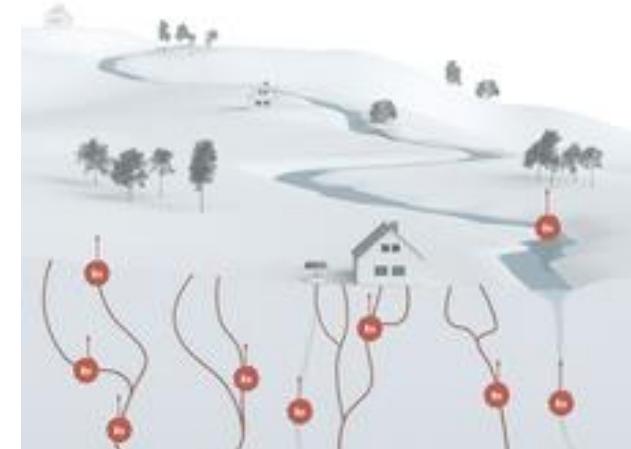
Ra-228,

Pb-210,

Po-210

Th-230, Th-232 & Th-228

...

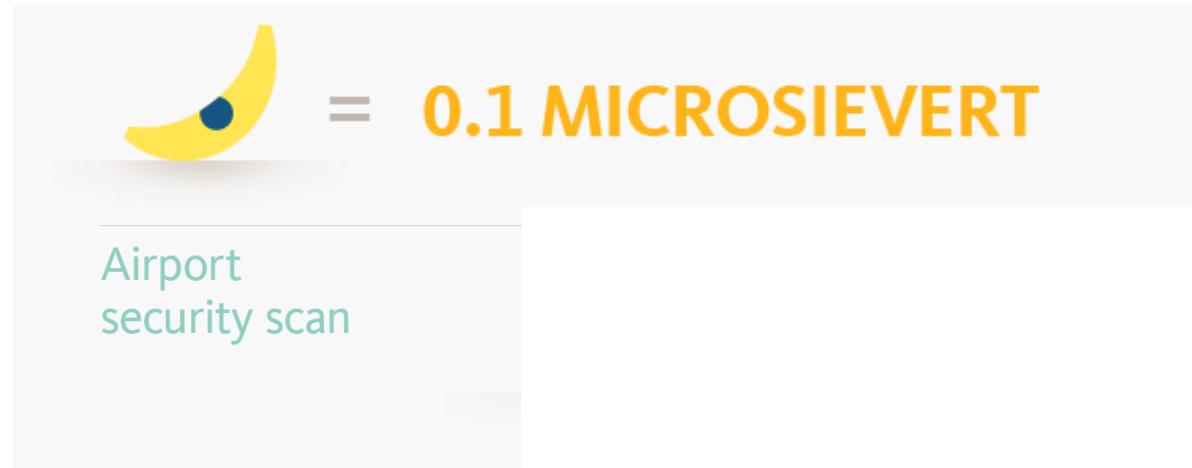


Radon decay products can deposit on leaf surfaces and be taken up in the leaves

- Among artificial radionuclides, **Cs-137** plays an important role as to food from forests, i.e. edible wild mushrooms and game, in particular wild boars.

- **Legacy of the Chernobyl accident and the atmospheric nuclear weapons tests**





[https://www.universityofcalifornia.edu/sites/default/files/uc\\_climatechange\\_illustrations\\_banana-radiation.png](https://www.universityofcalifornia.edu/sites/default/files/uc_climatechange_illustrations_banana-radiation.png)

## Flight from NY to LA

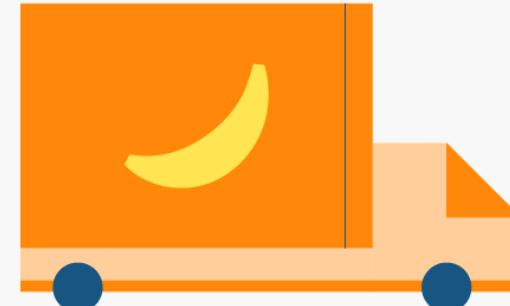
Long flights expose you to more radiation than airport security.



## Living in a concrete stone, or brick building for a year



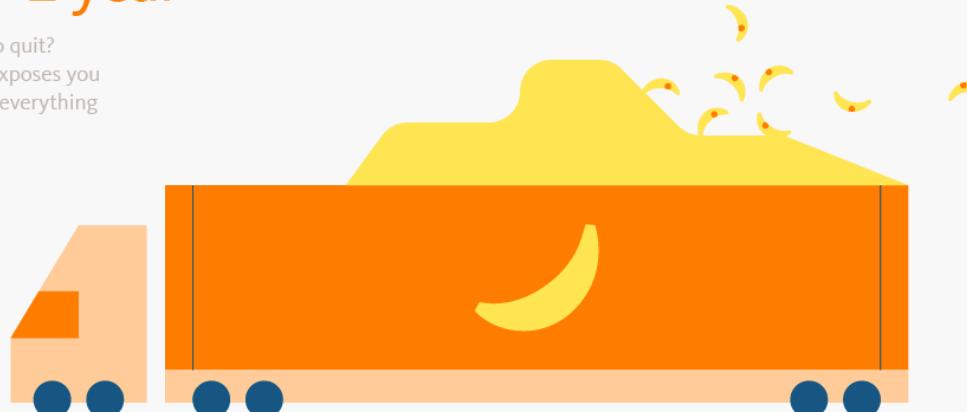
## CT Scan



100,000 BANANAS  
10,000  $\mu$ Sv

## Smoking a pack of cigarettes a day for 1 year

Need another reason to quit?  
Smoking a pack a day exposes you  
to more radiation than everything  
above put together.



240,000 BANANAS  
24,000  $\mu$ Sv

# Dose at which an increased risk of death from cancer is evident

Now it's starting to get a little bananas.  
There's no precise line at which radiation becomes dangerous, but cancer risk starts to increase to measurable levels around here.



1 MILLION BANANAS  
100,000 µSv

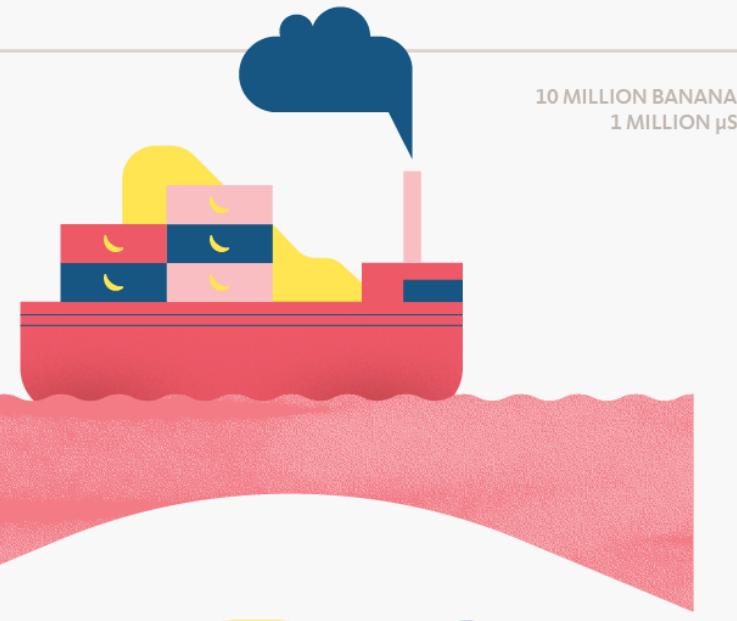


## Average dose of Chernobyl residents evacuated after 1986 accident

3.5 MILLION BANANAS  
350,000 µSv

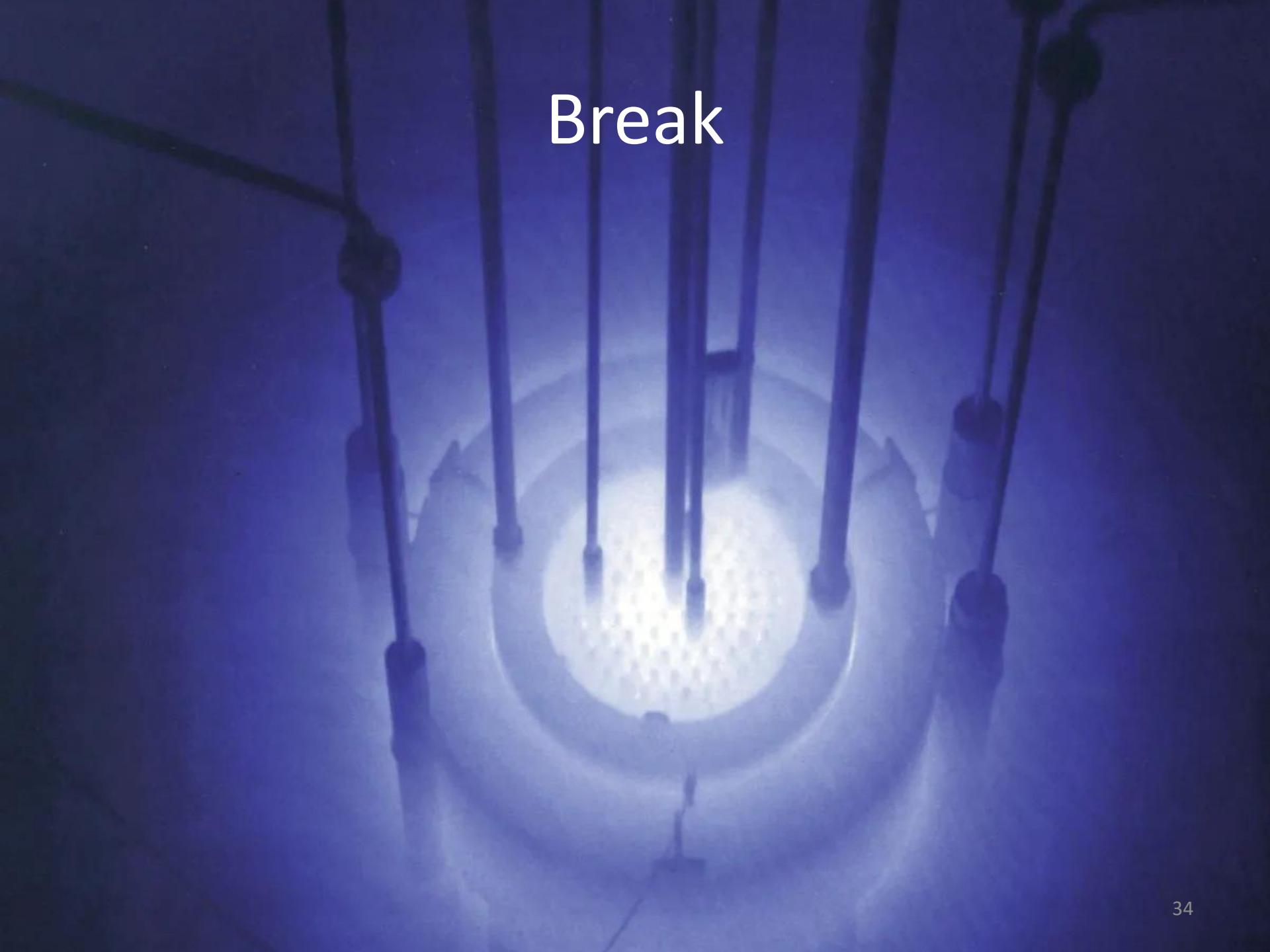


Temporary radiation sickness, not fatal



Fatal dose,  
death within  
2 weeks





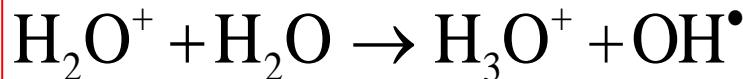
Break

- **Biological effects** are usually thought of **as effects on cells**.
- Ionizing radiation interacts with atoms by ionization.
- **The biological effects of radiation result mainly from damage to the DNA, which is the most critical target within the cell.**
- **Direct Action Damage:**
  - The radiation interacts **directly** with the critical target in the cell.
  - The interactions lead to the chain of physico-chemical events that will produce the biological damage.
  - This is the dominant process for high LET radiation.
- **Indirect Action Damage:**
  - The radiation interacts **indirectly** with other molecules: 80% water.
  - **Production of free radicals.**
  - The free radicals produce chemical damage in the critical target molecule.
  - This is the dominant process for low LET radiation (2/3 of damage).

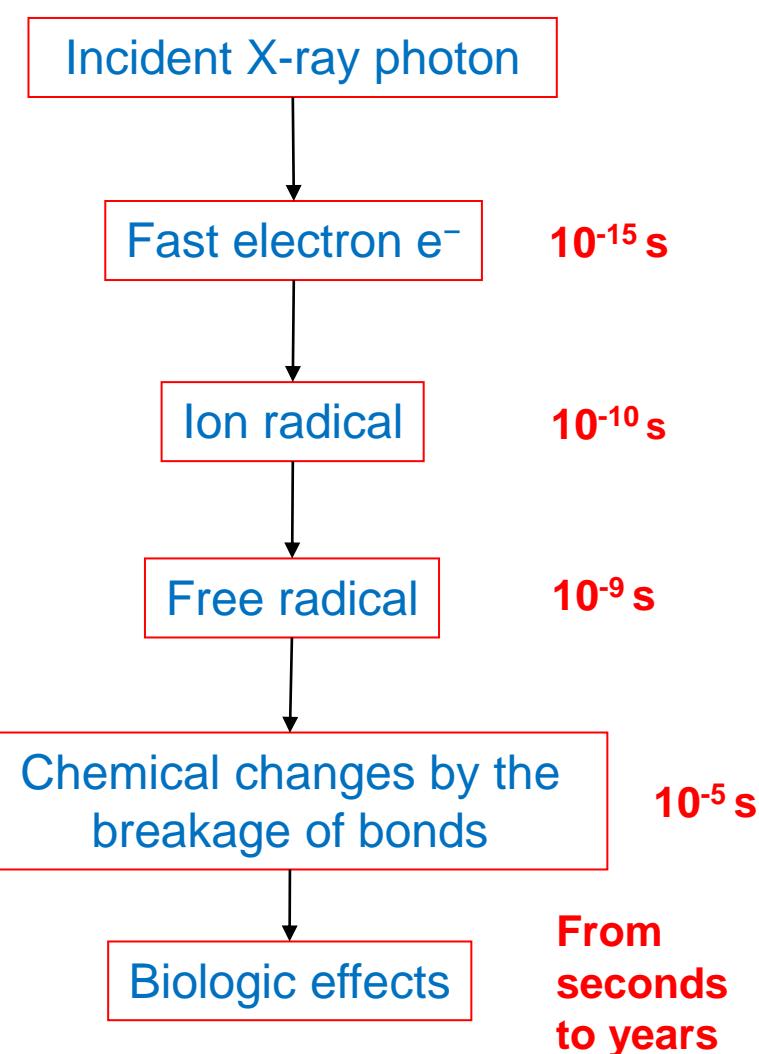
- Radiation interacts with a water molecule (80% cell is water).
- Ionization of the water molecule:



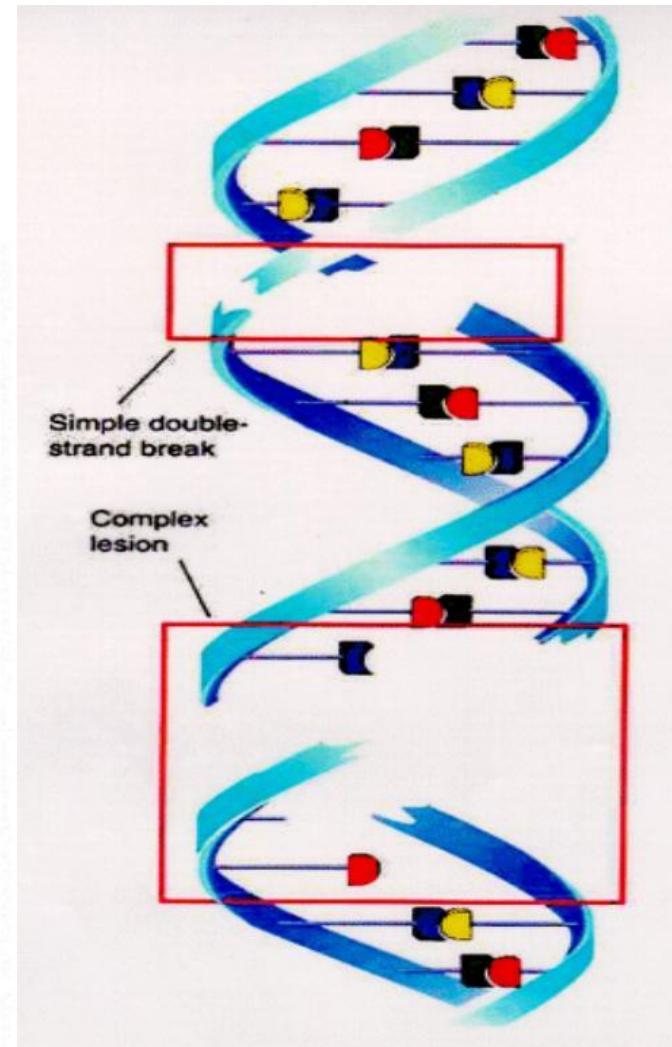
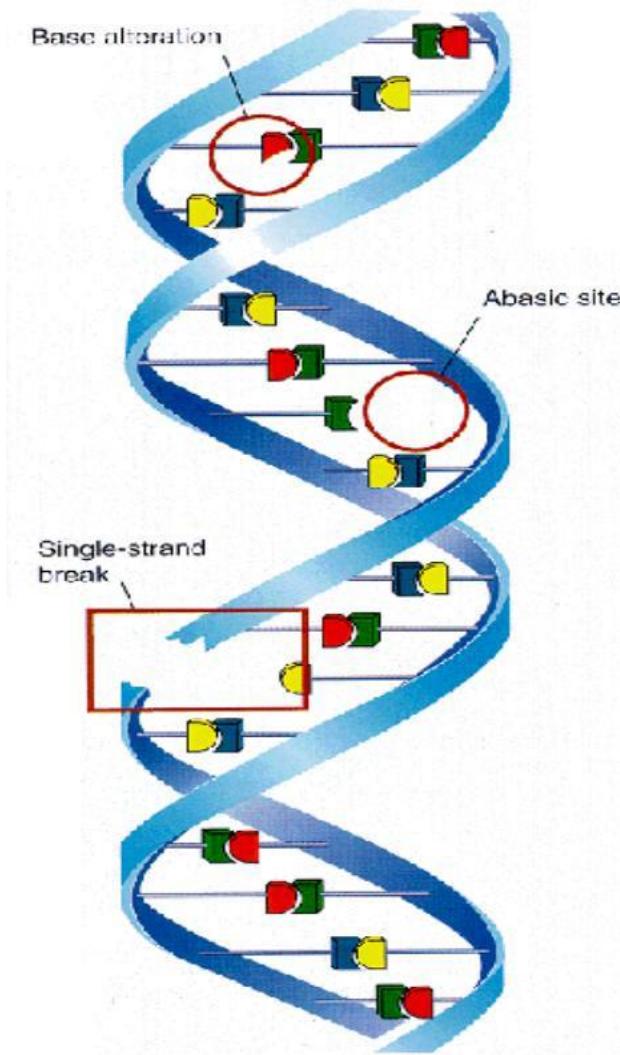
- Ion radical forms free radical:



- Hydroxyl radical  $\text{OH}^\bullet$  diffuses and attacks the DNA molecule.



- Base pair deletion
- Cross-linking injuries
- Single strand break
- Double strand break
- Multiple (complex) lesions



- No effect.**
- Division delay.**
- Apoptosis**: cell death before it can divide.
- Reproductive failure**: cell death when attempting **mitosis**.
- Genomic instability**: delayed reproductive failure.
- Mutation**: cells survives, but contains mutation in genome.
- Transformation**: mutation leads to carcinogenesis.
- Bystander effects**: damaged cell induces damage in surrounding ones.
- Adaptive response**: increased resistance to radiation.

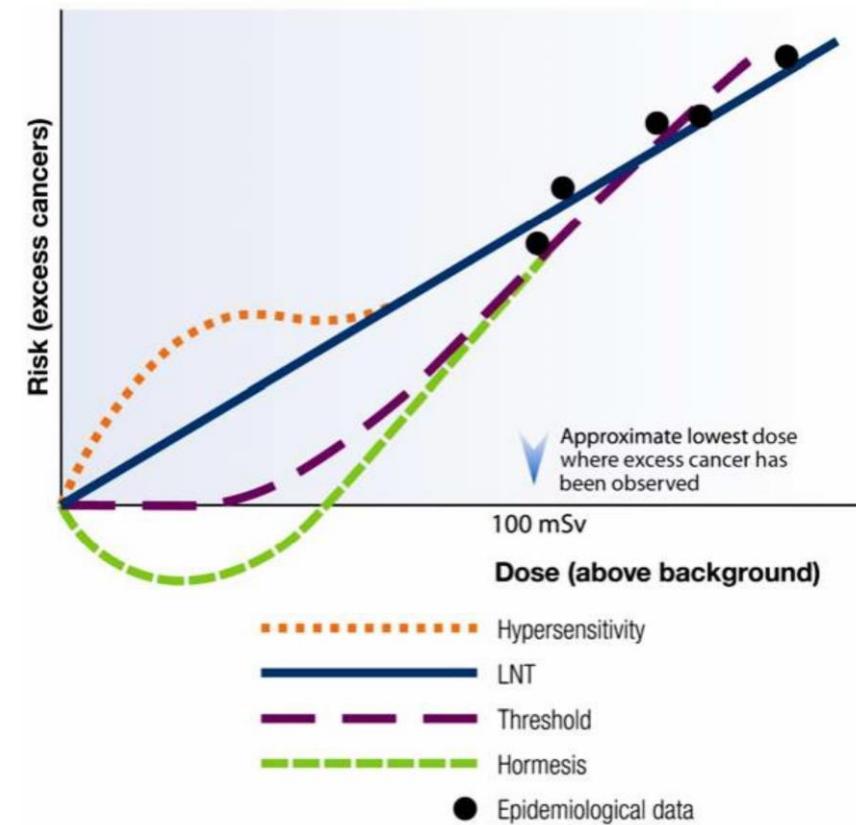
- The harmful effects of radiation may be classified into:
  - **Stochastic**: the probability of the effect increases with dose. There is no threshold, but it may be assumed that there is always a small probability the event occurring even at small doses.
  - **Deterministic**: there is a threshold for the effect, above which the severity increases with dose.
  
- Related to the response of an organ or tissue to radiation:
  - **Acute** (after high doses): cells are killed in large quantities. Tissues and organs are damaged. Rapid body response.
  - **Late** (after low doses): cells are damaged or changed. Slow body response.

Cancer Induction

- The **most important stochastic effect** for radiation safety considerations
- Reliable evidence through Hiroshima & Nagasaki (H&N) dataset
- Linear pattern of risk with respect to dose
- Controversy with respect to extrapolation to very low dose (airline pilots; inhabitants of area of high radiation background)
- Decline of radiosensitivity with age
- Complicated process (multi-stage, large amount of parameters)

 Hereditary Defects

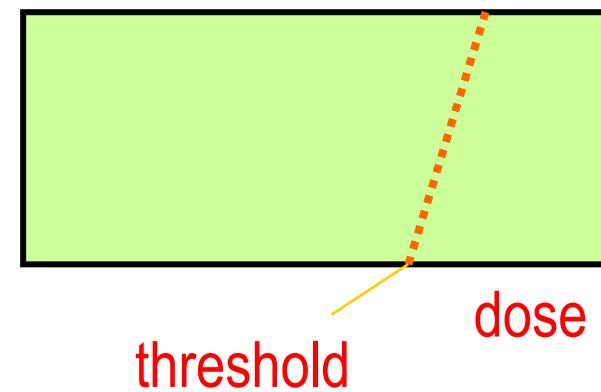
- Demonstrated during animal experiments
- No increase of defects in patients exposed to radiations in Japan (H&N) and Chernobyl



- ❑ Due to cell killing.
- ❑ Only above dose threshold.
- ❑ Specific to tissues.
- ❑ Severity of harm is dose dependent.
- ❑ Examples:
  - Skin breakdown
  - Cataract of the lens of the eye
  - Sterility
  - Kidney failure
  - Acute radiation syndrome (whole body)

- ❑ Thresholds for deterministic effects:
  - Cataracts of eye lens: 2-10 Gy
  - Permanent sterility
    - males 3.5-6 Gy
    - females 2.5-6 Gy
  - Temporary sterility
    - males 0.15 Gy
    - females 0.6 Gy

severity



# Radiation effects: Dose Ranges

3 hours flight in 10 km altitude

0.01 mSv

Effective dose limit for the exposure of the population by effluents from NPPs via air and water paths

0.3 mSv/a

Average exposure due to medical applications in Germany (effective dose)

2 mSv/a

Average natural radiation exposure in Germany (effective dose)

2.1 mSv/a

Additional natural radiation exposure in concrete or granite buildings

3 mSv/a

ca. 7,000 mSv

4,000 mSv

1,000 mSv

250 mSv

200 mSv/a

20 mSv/a

Lethal radiation dose after single full body exposure without medical treatment

Severe acute radiation disease after single full body exposure, 50 % lethality without medical treatment

Temporary acute radiation disease after single full body exposure

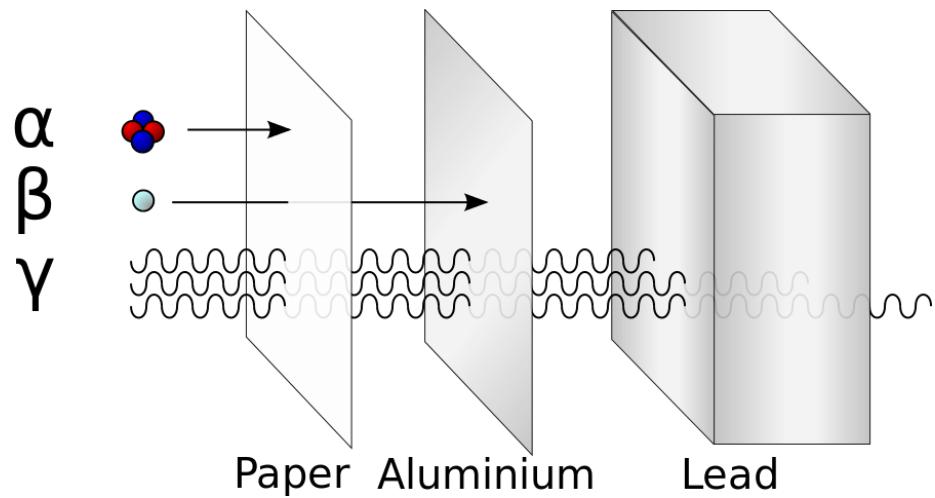
Threshold dose of first clinical symptoms of a single full body exposure

Maximum natural exposure in Brazilian monazite districts

Effective dose limit for the radiation exposure of nuclear workers in Germany

- Not all cells are equally sensitive to radiation.
- Those cells actively reproducing are more sensitive:
  - DNA is exposed to damage when the cell is dividing.
  - Non reproducing cells are more resistant to radiation.
- Classify cells according to their rate of reproduction:
  - Constantly reproducing: e.g. Lymphocytes.
  - Moderate regeneration: e.g. Gastrointestinal lining cells.
  - Slowest to regenerate: e.g. Muscle and Nerve cells.
- Fast reproducing cells well oxygenated are the most susceptible:
  - Tumour at the periphery. Irradiation causes rapid shrinkage -> Fractional irradiation.
  - Foetus: the sensitivity of the developing embryo is very large.

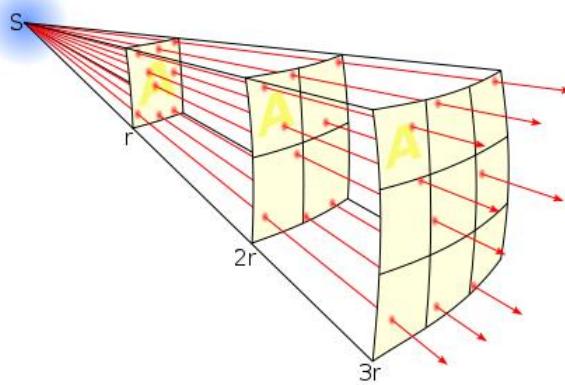
# Radiation protection principles and shielding



- ◆ “As Low As Reasonable Achievable”: A principle of keeping radiation doses and releases of radioactive materials to the environment as low as can be achieved, based on technologic and economic considerations

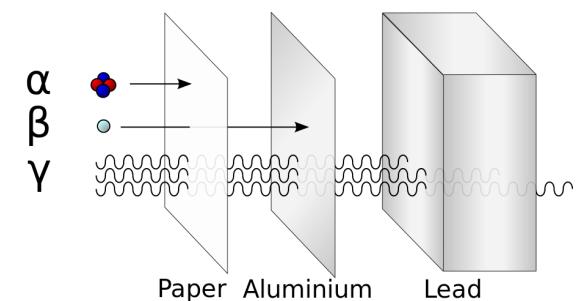
- ◆ Factors to consider to reduce exposure

- ① **Time:** Reducing the time of an exposure reduces the effective dose proportionally.
- ② **Distance:** Increasing distance reduces dose due to the inverse square law.
- ③ **Shielding:** A mass of absorbing material placed around a radioactive source, to reduce radiation levels

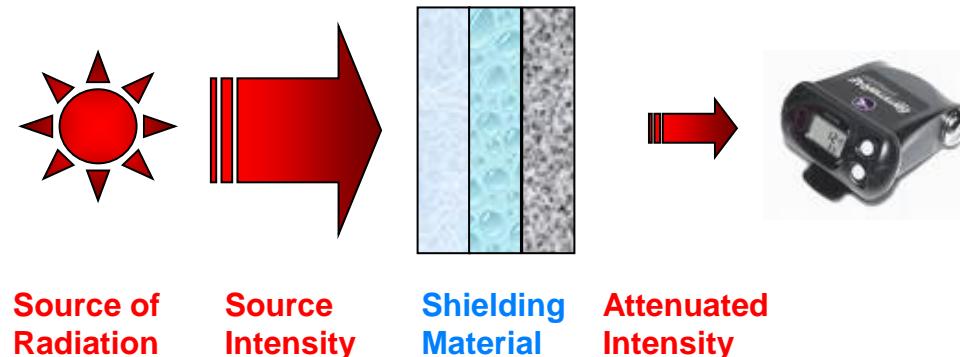


$$\frac{\text{Intensity}_1}{\text{Intensity}_2} = \frac{\text{distance}_2^2}{\text{distance}_1^2}$$

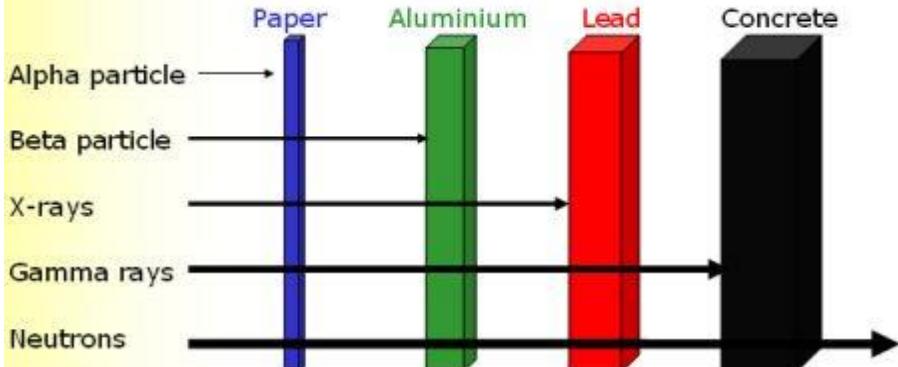
$$\text{Intensity} \propto \frac{1}{\text{distance}^2}$$



- Purpose of radiation shielding:
  - Reduce the radiation exposure to persons and equipment.
  - Can be used to control radiation and thus is an important aspect of Radiation Protection.
- Radiation shielding is **based upon the mechanisms by which different radiations interact** in an absorbing medium.
- **Radiation shielding is** a very **complex discipline**:
  - There are many radiation sources.
  - There is a wealth of materials and geometric configurations.



### Typical radiation shielding materials



Interaction properties of radiation.

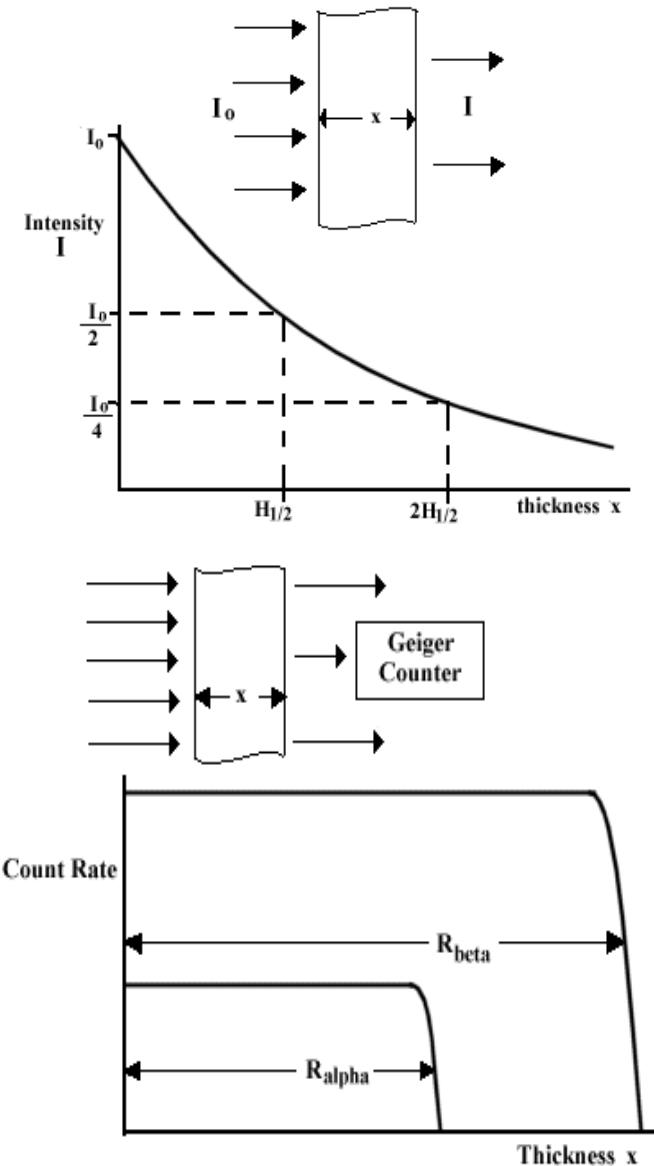
Radiation	Charge	Energy	Range in air	Range in H <sub>2</sub> O
$\alpha$ particles	+2	3–10 MeV	2–10 cm	20–125 $\mu$ m
$\beta^+$ , $\beta^-$ particles	$\pm 1$	0–3 MeV	0–10 m	<1 cm
Neutrons	0	0–10 MeV	0–100 m	0–1 m
X-rays	0	0.1–100 keV	m–10 m	mm–cm
Gamma rays	0	0.01–10 MeV	cm–100 m	mm–10s of cm

## □ Attenuation:

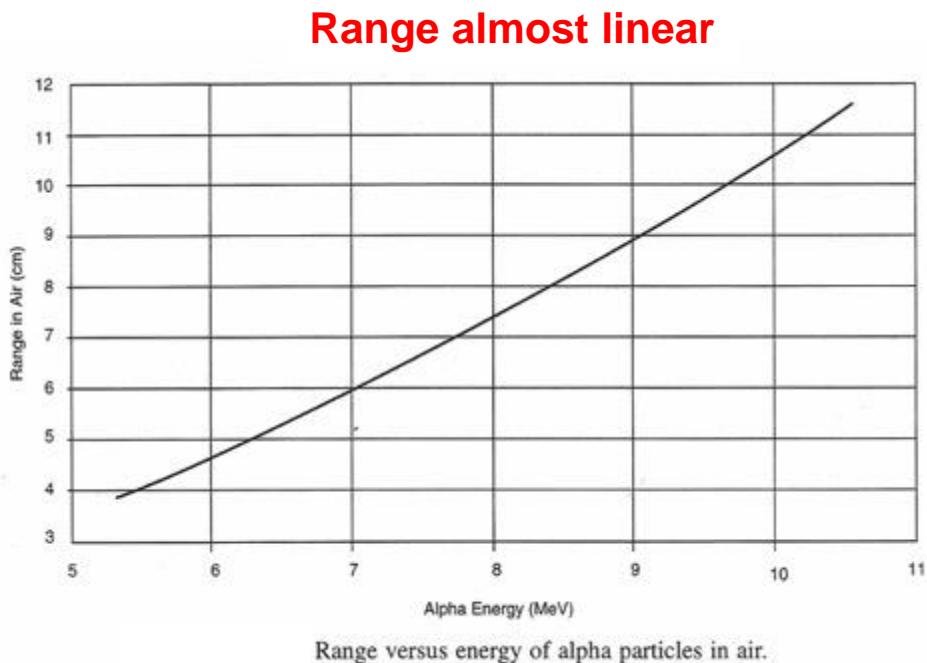
- A **reduction in intensity** of radiation with respect to distance traveled through a medium.

## □ Range $R_{\text{particle}}$ :

- In passing through matter, charged particles ionize and thus lose energy in many steps, **until their energy is (almost) zero**. The distance to this point is called the range of the particle.
- The range depends on:
  1. The type of particle,
  2. its initial energy and
  3. the material which it passes through.



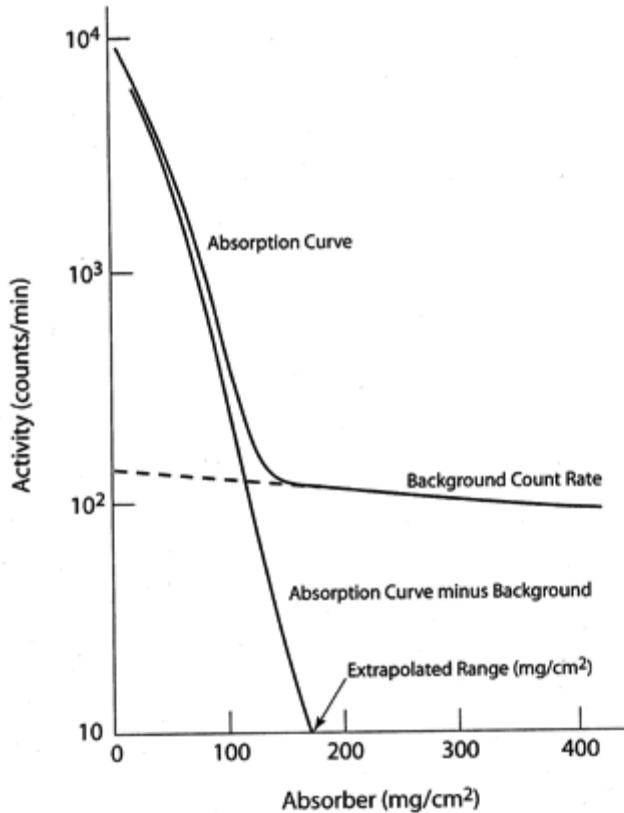
- Alpha particles are easy to shield due to their short and well predictable range.
- External radiation:
  - Absorbed by very **thin** layers of dense materials (range generally less than 1mm).
  - Stopped by dead skin layer.
- Internal Radiation:
  - Considerable damage to biological tissue: **Large ionization**.
  - High LET radiation.
- Shielding avoids spread and contact by using fixatives on surfaces.**
- Very short range makes detection difficult:
  - Detector windows must be thin.
  - Highly contaminated areas may be missed by failing to get close enough.



# Attenuation and Range of Beta Particles

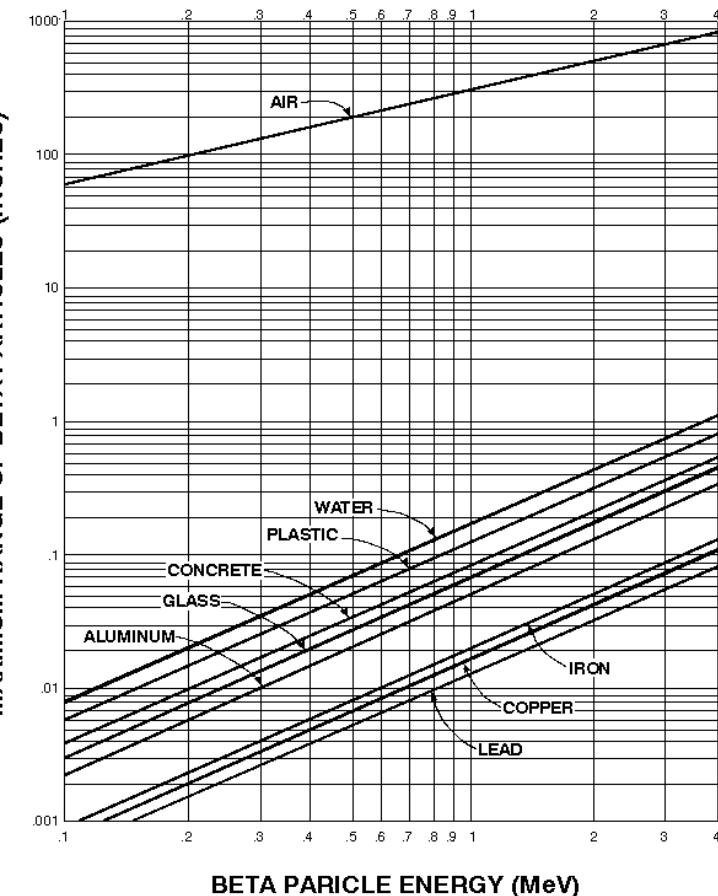
- The attenuation of beta particles in a medium is exponential:
- The range of beta particles is short (few meters in air, tenths of mm in dense materials) and depends on their **kinetic energy** and **Z** of the material.

$$I(x) = I_0 e^{-\mu_{\beta,i} (\rho x)}$$

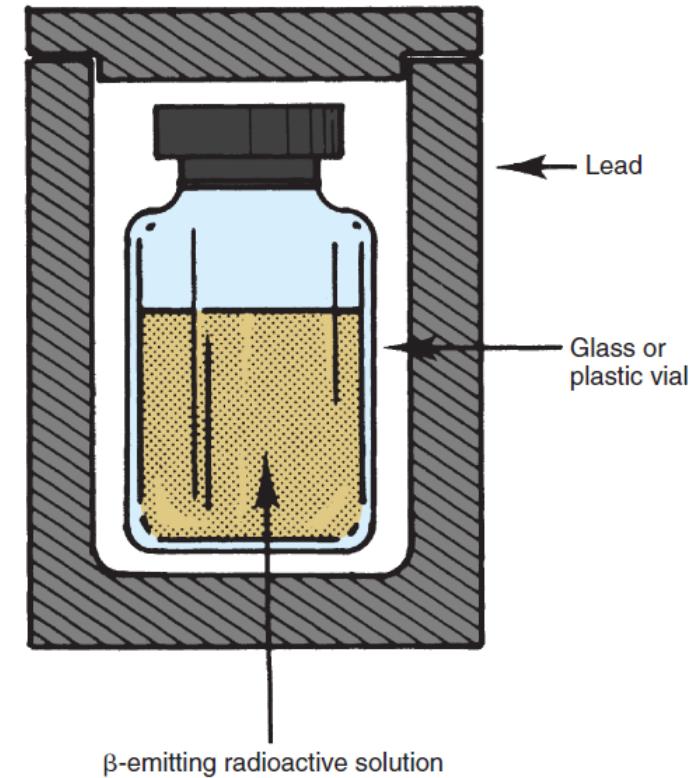
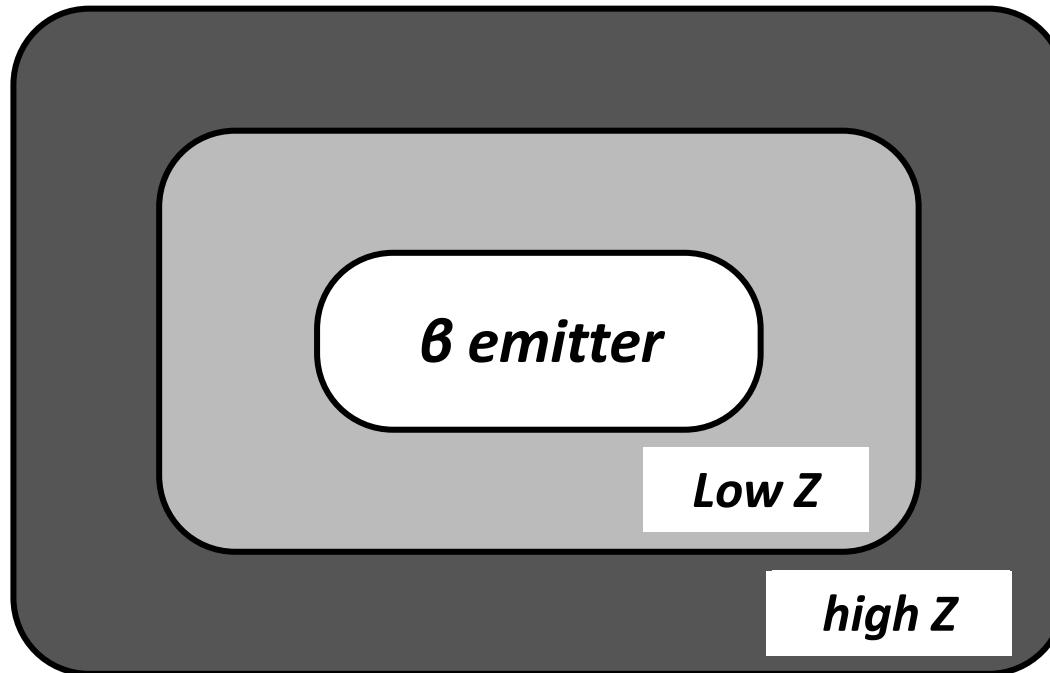
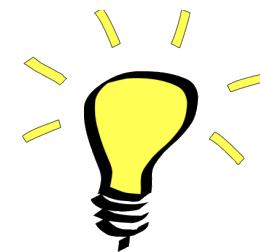


Decrease in measured activity of a beta particle source versus  $\text{mg}/\text{cm}^2$  of absorber thickness that trails off into the background of the detector system. Subtraction of the background portion from the total curve yields a curve that can be extrapolated to estimate the maximum range (in  $\text{mg}/\text{cm}^2$ ) of the beta source.

**MAXIMUM RANGE OF BETA PARTICLES**  
as a Function of Energy in Various Materials



- Bremsstrahlung is important for high Z materials (Pb).
- Shield design must account for the fraction of total energy transformed into photons by Bremsstrahlung.



**FIGURE 6-3** Preferred arrangement for shielding energetic  $\beta$ -emitting radioactive solution. Glass or plastic walls of a vial stop the  $\beta$  particles with minimum bremsstrahlung production, and a lead container absorbs the few bremsstrahlung photons produced.

- The attenuation obeys an exponential law:
- The attenuation coefficient  $\mu$  ( $\text{cm}^{-1}$ ) is the sum for **all interactions**:
  - Depends on photon energy and  $Z$  of the absorber medium:
    - $\Rightarrow$  Pb is often used as shield for X-rays.
    - $\text{BaSO}_4$  is incorporated into concrete.
  - $\mu$  grows with  $Z$  because of rising importance of photoelectric effect and pair production.

### Attenuation of Photons

$$I(x) = I_0 e^{-\mu x}$$

### Half-Value Layer (HVL)

$$\frac{I(x_{1/2})}{I_0} = \frac{1}{2} = e^{-\mu x_{1/2}}$$

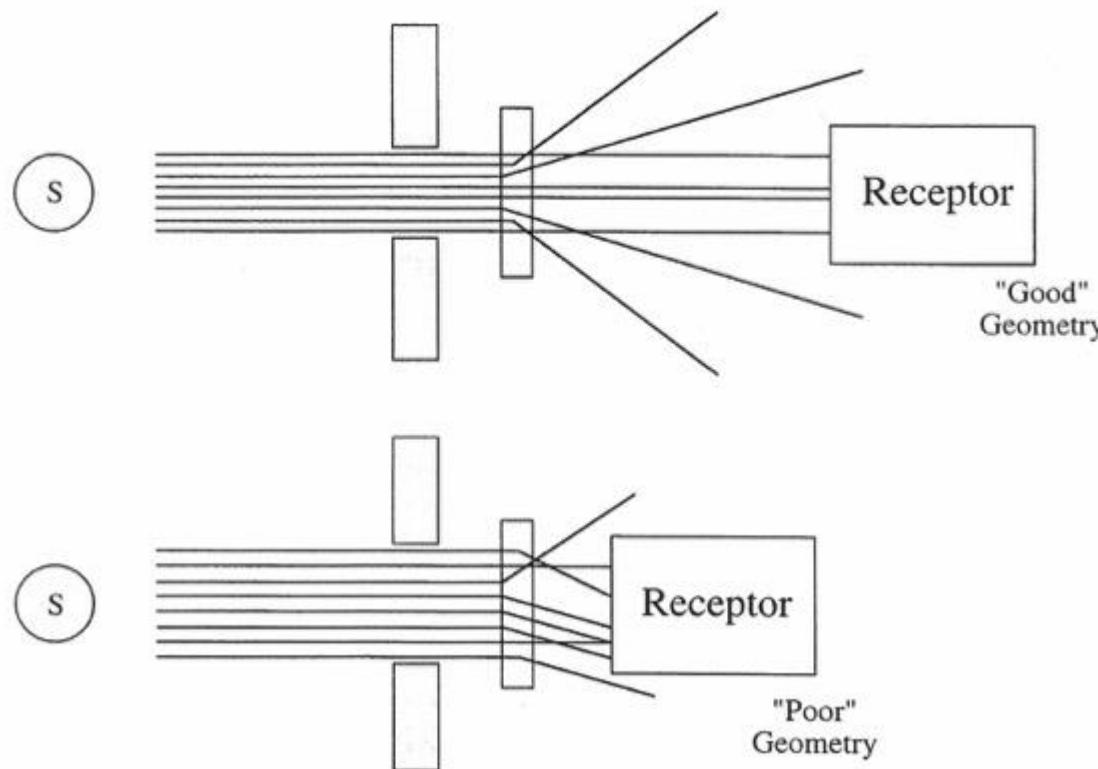
$$x_{1/2} = \text{HVL} = \frac{\ln 2}{\mu}$$

### Tenth-Value Layer (TVL)

$$x_{1/10} = \text{TVL} = \frac{\ln 10}{\mu}$$

“Good” and “Bad” geometry:

- **“Good” geometry (narrow-beam):** Only non-scattered (primary) photons (that have the same energy as the original beam) reach the receptor.
- **“Bad” (broad-beam) geometry:** Also scattered (secondary) photons of lower energy can reach the receptor and lead to a complex energy spectrum.
- Shield design must tend to “good” geometry.



- The basis is to use materials that enhance the interactions that deplete neutrons:
  - Fast neutrons:
    - **First** moderation: elastic and inelastic scattering ( $\gamma$ -rays).
    - **Then** absorption of thermal neutrons.
  - Thermal neutrons:
    - Absorption:  $(n,\gamma)$ -reactions, but not  $(n,2n)$ ,  $(n,3n)$ ,  $(n,f)$ , ...
- Best moderating materials are those with:
  - Low Z: higher energy loss per collision, e.g., H<sub>2</sub> (1/2E loss per interaction).
  - High elastic scattering X-sections.
- Best absorbing materials are those with large absorption cross sections for thermal neutrons: e.g., <sup>10</sup>B, Cd, H, Li, Gd, ...
- **Neutron attenuation under “good” geometry conditions:**
$$I(x) = I(0) \cdot \exp(-\Sigma_t \cdot x), \quad \Sigma_t = N \cdot \sigma_t = N \cdot (\sigma_e + \sigma_i + \sigma_\gamma + \sigma_r + \dots)$$
- **Otherwise**, when the scattering of neutrons “back into the beam” plays a role, it must be taken into account (as for photons), by **buildup factors**, e.g., B~5.0 for 20 cm or more water or paraffin.

## □ Hydrogenous materials (moderators)

- **Water**: (corrosion, leakage, contamination, etc.).
- **Paraffin**: (flammable). Shielding needed for the 2.225 MeV  $\gamma$ -photon from H neutron capture.
- **Polyethylene**: larger H/volume than water.
- **LiH**: no  $\gamma$  from neutron capture, but Tritium formation from  $^6\text{Li}$ .

## □ Elements used as shielding materials in NPP

- **Pb, Fe**: Capture  $\gamma$ -rays,  $^{59}\text{Fe}$  activation.
- **W**: Better than Pb. Secondary  $\gamma$ -radiation from neutron capture.
- **U (depleted)**: best attenuator for  $\gamma$ -rays, low neutron capture  $\gamma$ , but high  $\gamma$  flux from fast fission reactions.
- **B**: incorporated in Boron based shields. High thermal absorption cross section.
- **Concrete and earth**: high H content; added B.
- **Cd**: large absorption X-section; high capture  $\gamma$ -photons (9.05 MeV).