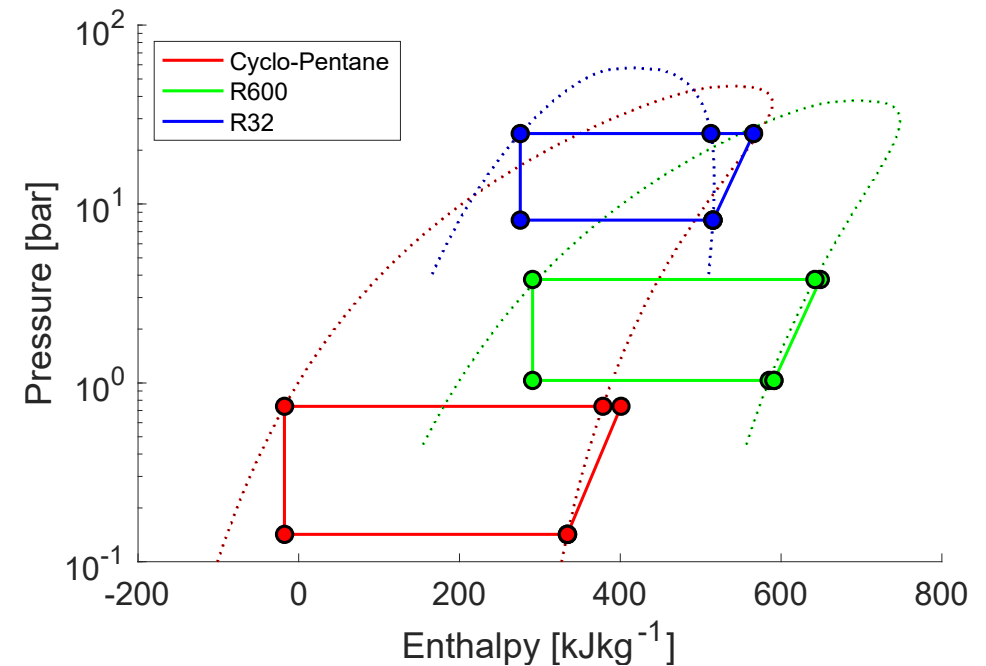


Heat Pump Systems

Summary W7

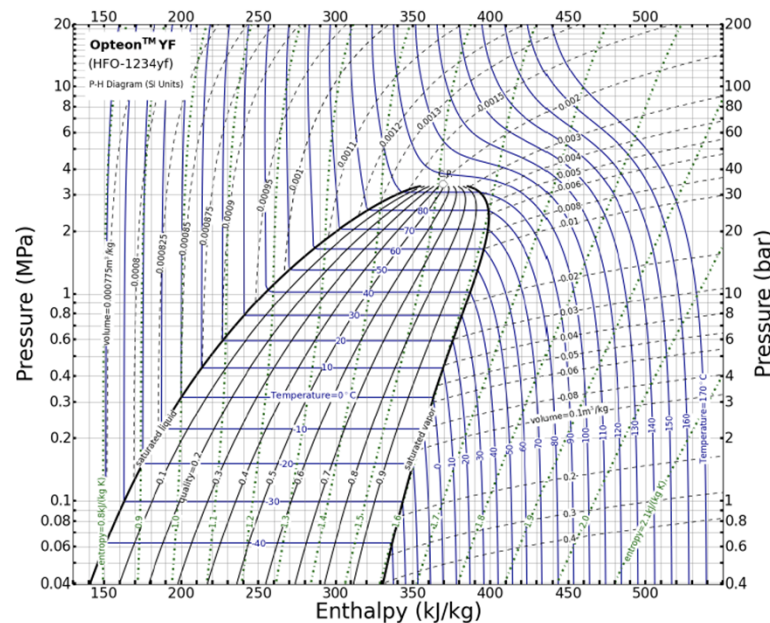
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- Working fluid selection has important effect of cycle design
 - Design pressure ratio
 - Slope of saturation line
 - Slope of isentropic lines
 - Thermophysical properties
 - ODP & GWP
 - Compatibility with oil
 - Chemical stability
 - Toxicity
 - Flammability
 - Cost ...



Working Fluid Modeling

- Cycle modeling requires accurate thermophysical properties
- Equation of state constructed on P_{Vap} , ρ_{Liq} , c_{p0} , P_{Crit} , T_{crit}
- Basis is cubic EOS \rightarrow Refprop & CoolProp

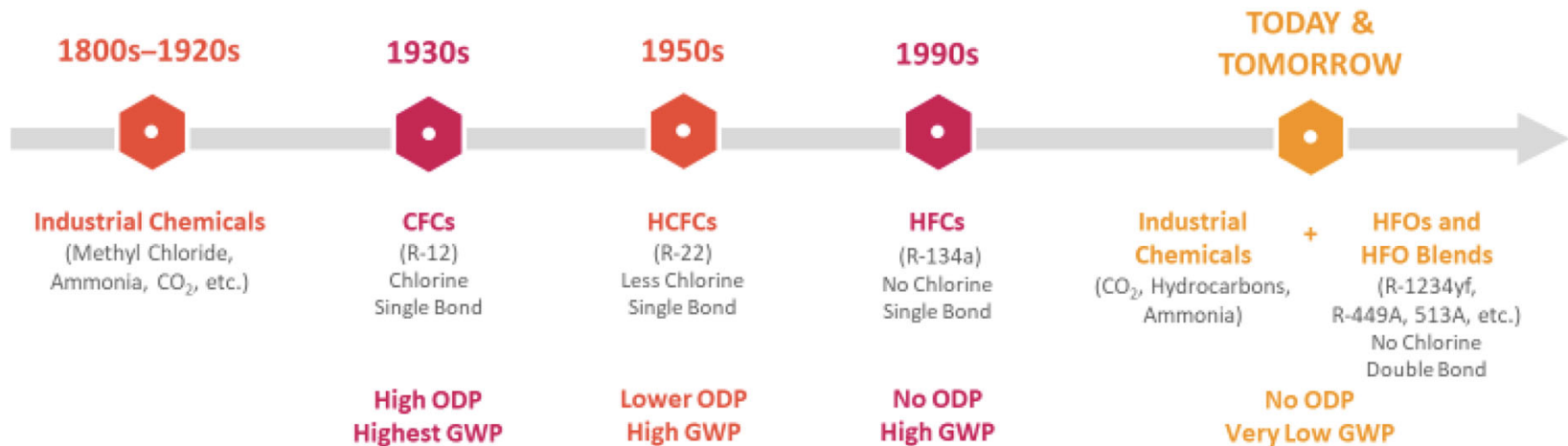


$$P = \frac{rT}{(v - b)} - \frac{a\alpha}{(v^2 + uvb + wb^2)}$$

EOS	u	w
Van der Waals (1873)	0	0
Redlich-Kwong (1949)	1	0
Soave-Redlich-Kwong (1972)	1	0
Peng-Robinson (1976)	2	-1

Evolution of Working Fluids

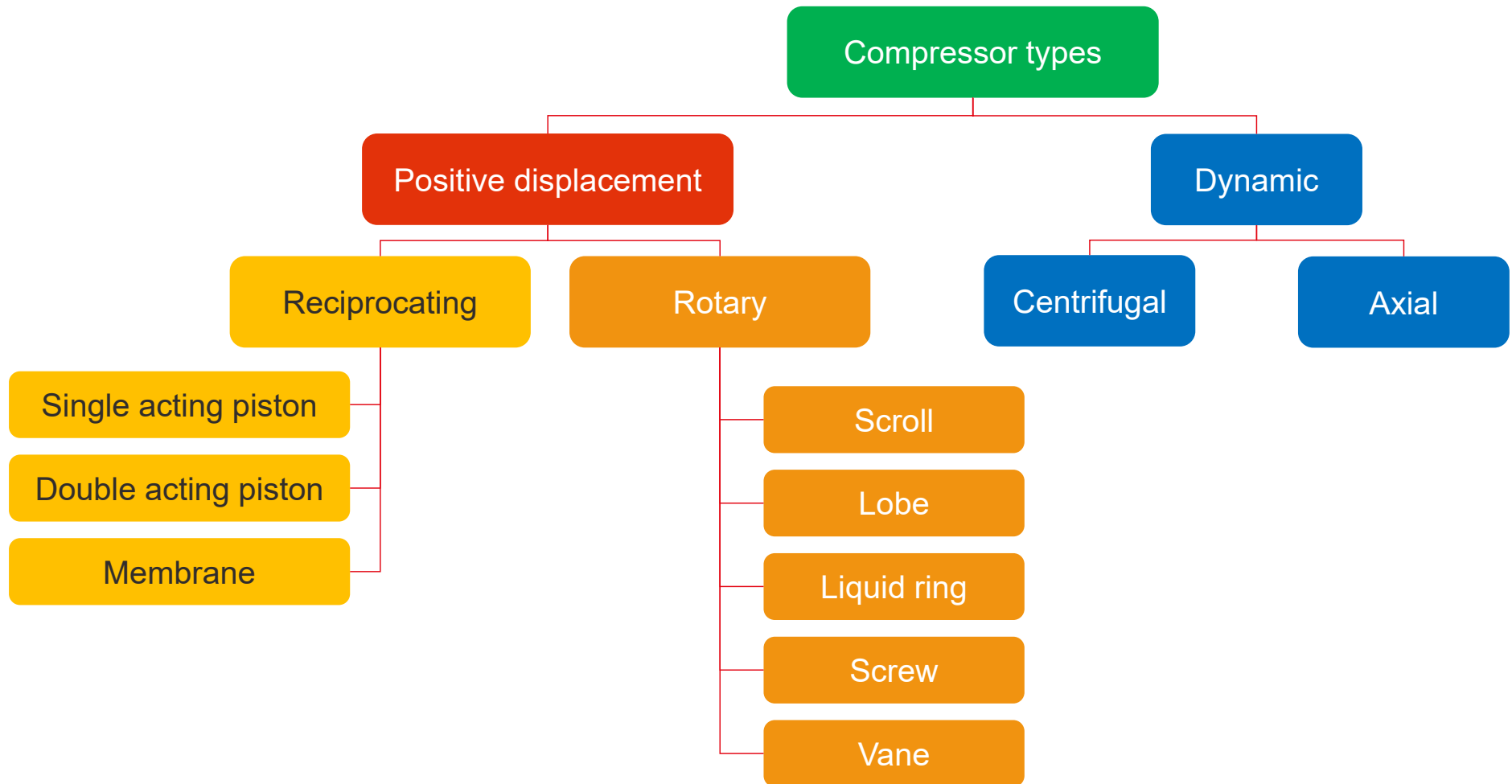
- Companies interested in selling synthetic fluids
- Natural working fluids pick up again
 - Carbon dioxide, water, ammonia, butane, propane



Role of Compressors

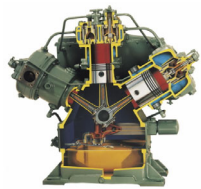
- Compressors play key role in driving heat pump cycles
- Compressor efficiency has direct impact on cycle performance
- Significant efforts are invested to improve compressor performance while increasing range, robustness
- Heat pump designers usually have a wide spectrum of machines to select from

Compressor Classification



Compressor Operational Areas

- Positive displacement machines preferred for small capacity, dynamic compressors traditionally for high capacities



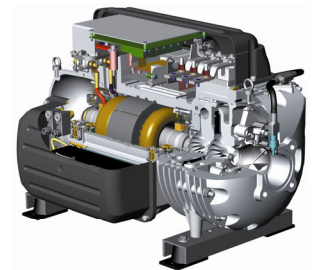
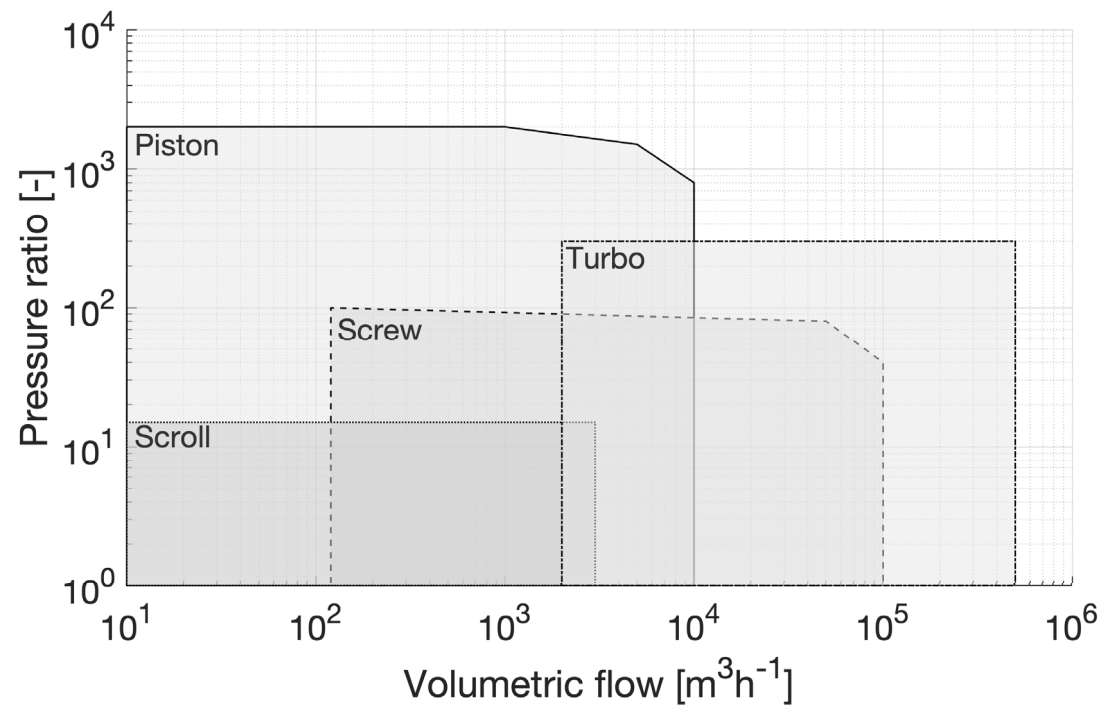
weiku.com



bitzer.de



atlascopco.ch



turbocor.com



Heat Pump Systems

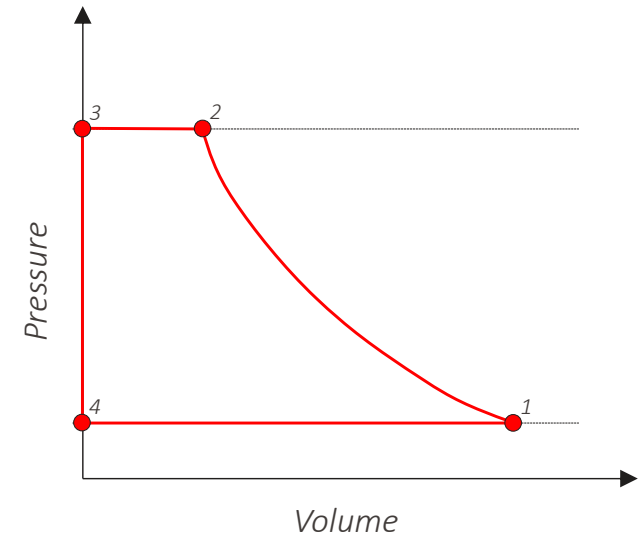
Compressor
Performance

Prof. J. Schiffmann

Ideal Compression

- Ideal compression process:

- Isobaric suction ($4 \rightarrow 1$)
- Compression ($1 \rightarrow 2$)
- Isobaric discharge ($2 \rightarrow 3$)
- Expansion ($3 \rightarrow 4$)



- Invested work for compression cycle

$$e^+ = - \oint P dv$$

$$e^+ = - \int_4^1 P dv - \int_1^2 P dv - \int_2^3 P dv - \int_3^4 P dv$$

Ideal Compression

- Isobaric suction ($4 \rightarrow 1$)

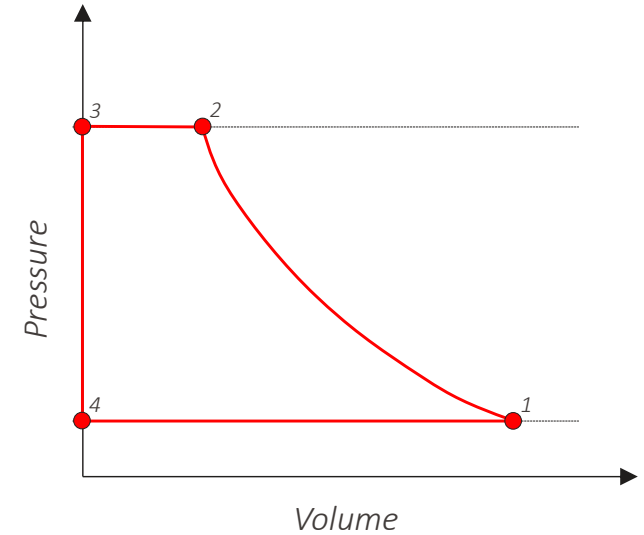
$$e_{4 \rightarrow 1}^+ = - \int_4^1 P dv = - (v_1 - v_4) P_1$$

- Isobaric discharge ($2 \rightarrow 3$)

$$e_{2 \rightarrow 3}^+ = - \int_2^3 P dv = - (v_3 - v_2) P_2$$

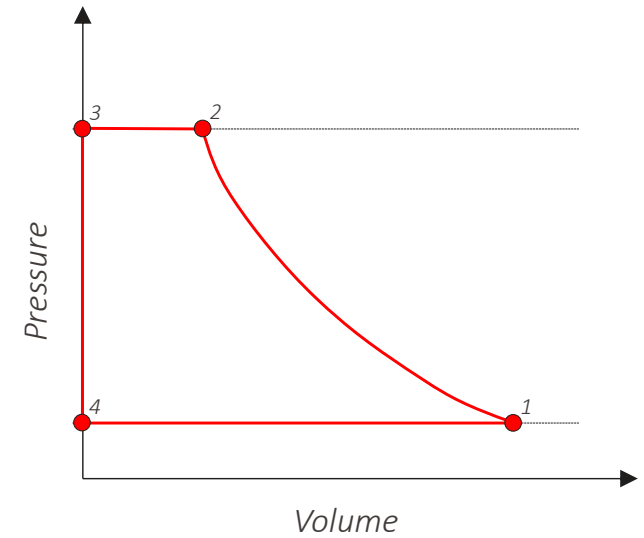
- Expansion ($3 \rightarrow 4$)

$$e_{3 \rightarrow 4}^+ = - \int_3^4 P dv = 0$$



Ideal Compression

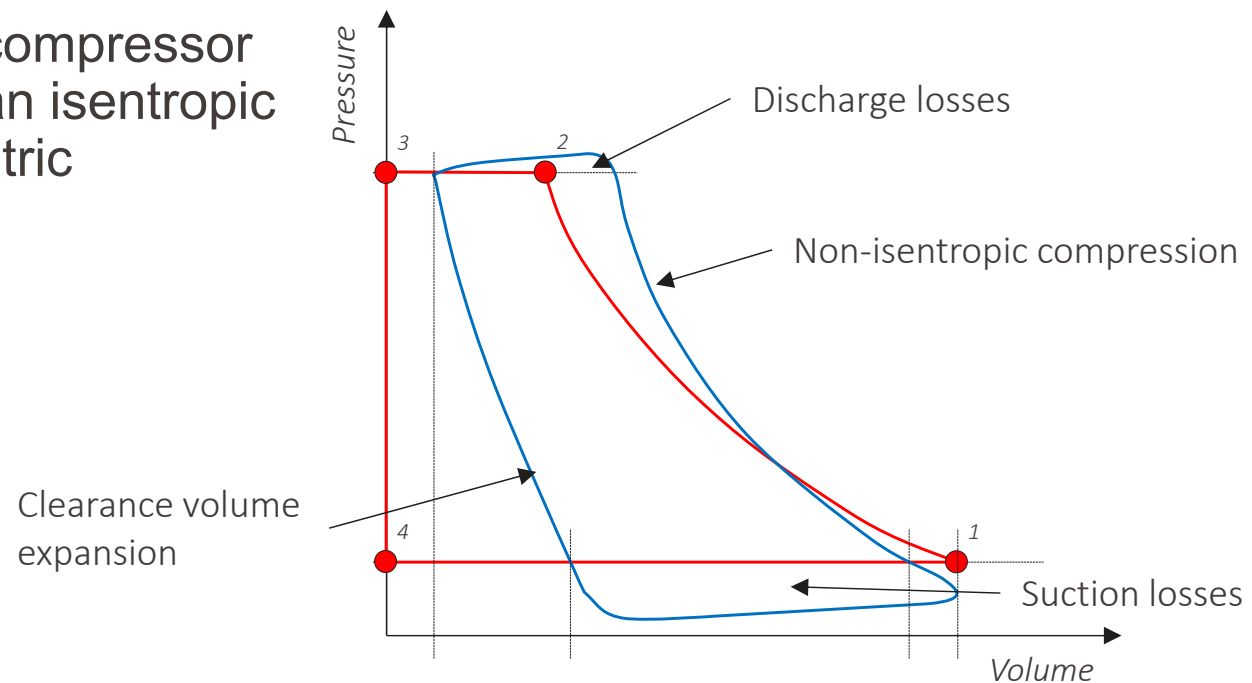
- Compression ($1 \rightarrow 2$)



Real Compression Process

- Real compression deviates from ideal process

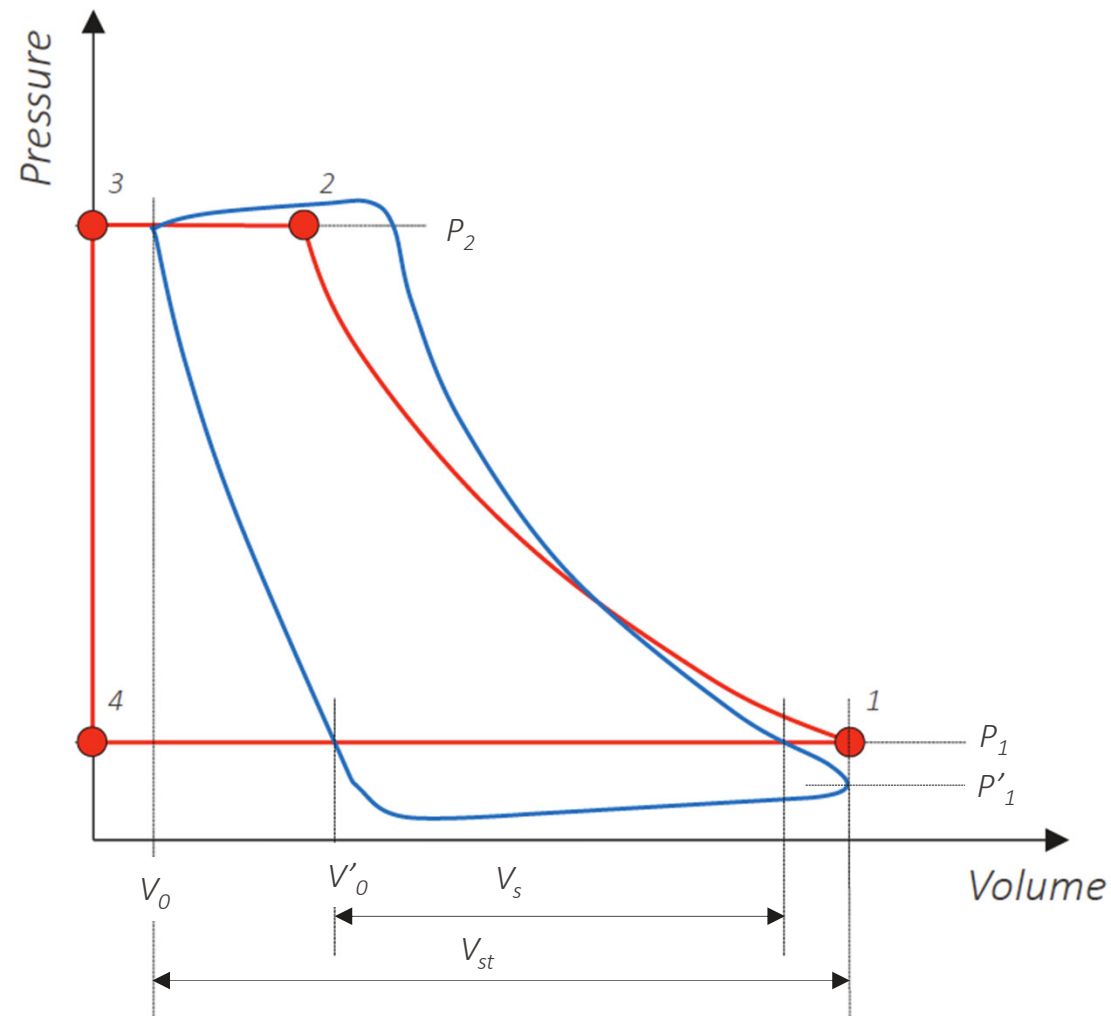
- Positive displacement compressor characterized through an isentropic efficiency and a volumetric performance metric



Volumetric Losses

- Clearance volume expands from discharge to suction & reduces suction volume
 - Assume isentropic expansion from P_2 to P_1
- Suction pressure drop leads to suction volume reduction
 - Assume isothermal compr. from P_1' to P_1
- Clearance volume ratio

$$\epsilon = V_0/V_{st}$$



Volumetric Efficiency

- Secondary effects related to mechanical design result in reduced suction volume
- Volumetric efficiency definition

$$\eta_v = \frac{V_s}{V_{st}} \approx \eta_{v1} \eta_{v2} \eta_{v3}$$

The diagram shows the equation $\eta_v = \frac{V_s}{V_{st}} \approx \eta_{v1} \eta_{v2} \eta_{v3}$. Three blue arrows point from text labels to the efficiency terms: 'Suction losses' points to η_{v1} , 'Leakage' points to η_{v2} , and 'Clearance volume expansion' points to η_{v3} .

$$\dot{V}_{st} = V_{st} f_c$$

The diagram shows the equation $\dot{V}_{st} = V_{st} f_c$. Two red arrows point from text labels to the variables: 'Compressor drive frequency' points to f_c , and 'Stroke volume' points to V_{st} .

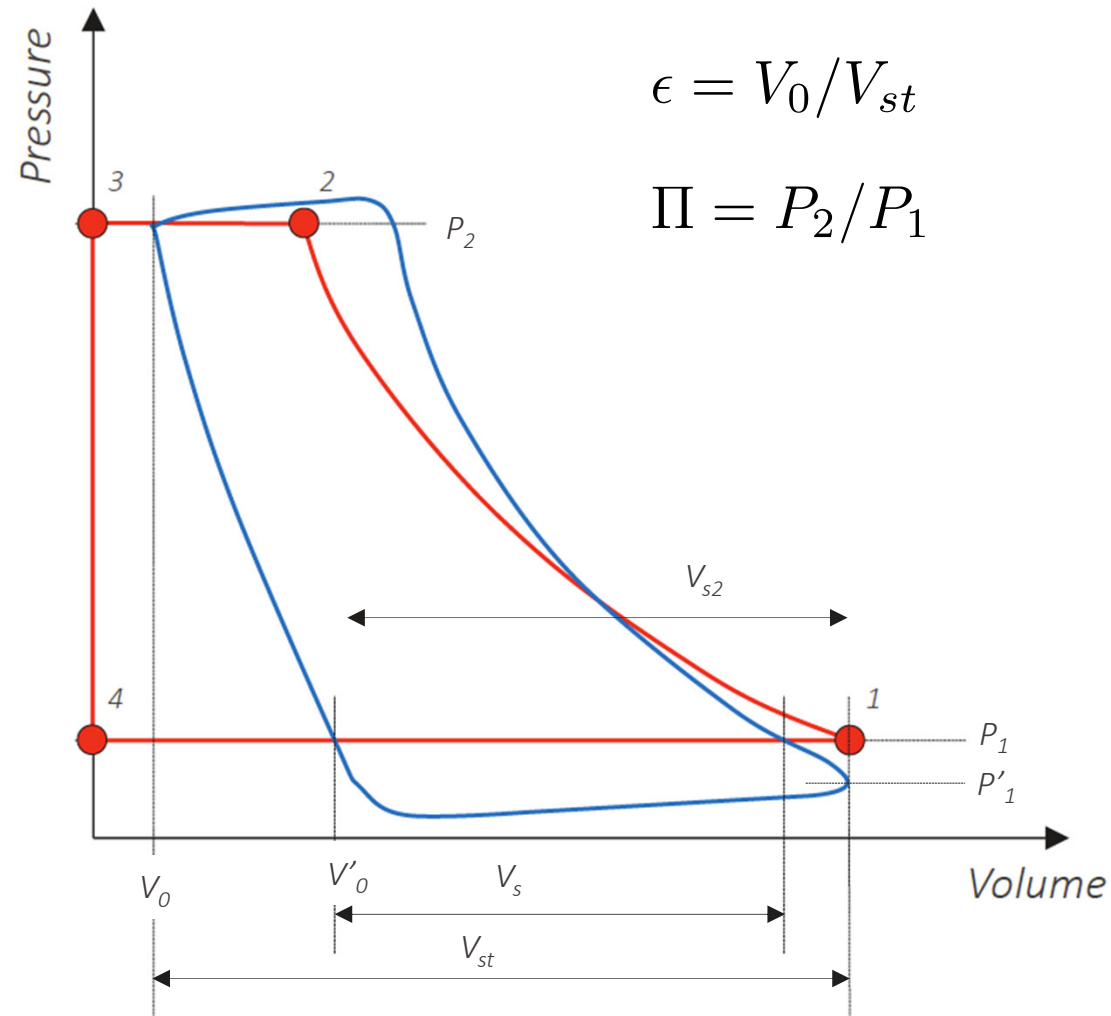
Volumetric Efficiency

$$P_1' (V_{st} + V_0) = P_1 (V_s + V_0')$$

$$V_s = \frac{P_1'}{P_1} (V_{st} + V_0) - V_0'$$

$$V_s = \frac{P_1'}{P_1} V_{st} (1 + \epsilon) - V_{st} \epsilon \Pi^{1/\kappa}$$

$$\eta_v = \frac{V_s}{V_{st}} = \frac{P_1'}{P_1} (1 + \epsilon) - \epsilon \Pi^{1/\kappa}$$



Effect of Clearance Volume Expansion

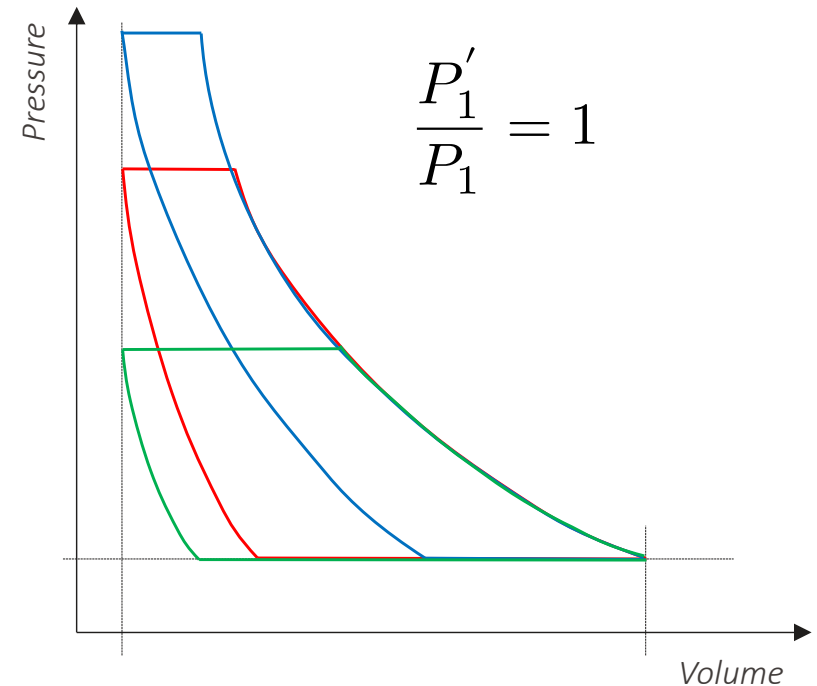
Isolated Losses on Clearance Volume

- Clearance volume expanding from discharge to suction decreases suction volume with increasing pressure ratio

$$\eta_{v2} = 1 - \frac{V_0}{V_{st}} \left[\left(\frac{P_2}{P_1} \right)^{\frac{1}{\kappa}} - 1 \right]$$

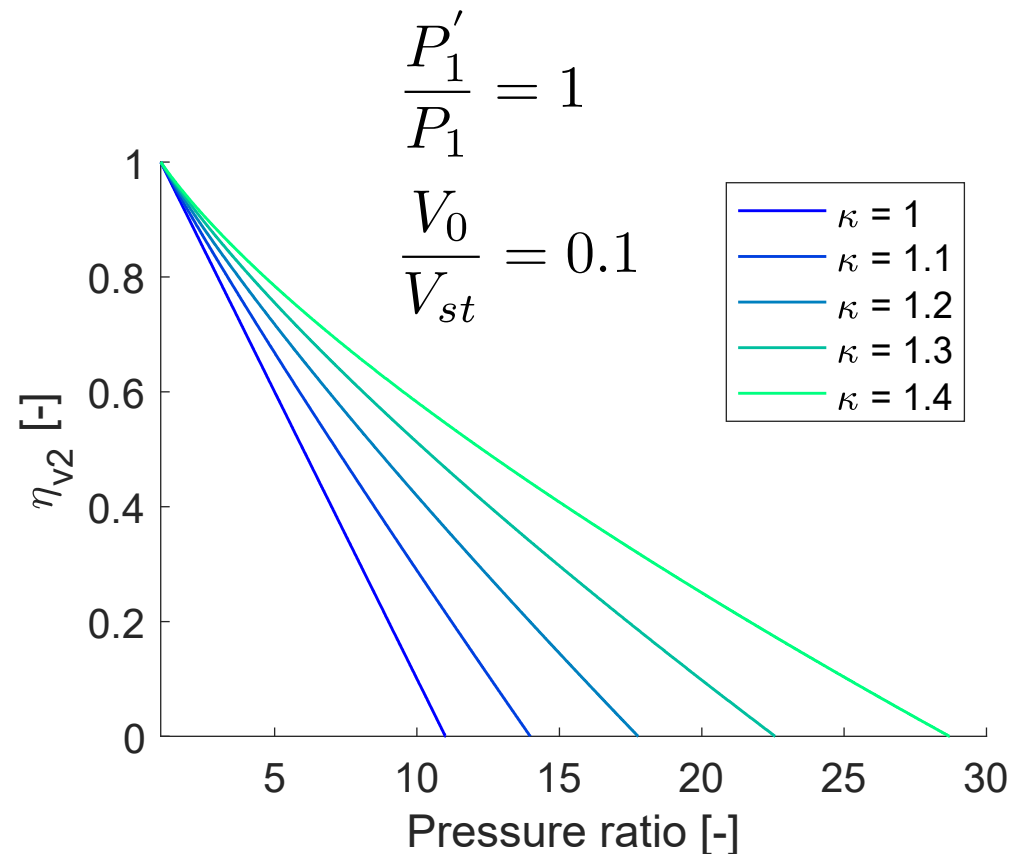
- Critical pressure ratio above which no mass-flow is delivered $\rightarrow \eta_{v2} = 0$

$$\left. \frac{P_2}{P_1} \right|_{Crit} = \left[\frac{V_{st}}{V_0} + 1 \right]^{\kappa}$$



Effect of Clearance Volume Expansion

- Volumetric efficiency drops with increasing pressure ratio and with decreasing kappa
- Critical pressure ratio drops with decreasing kappa
- Volumetric efficiency needs to be considered when selecting compressor stroke volume for given application

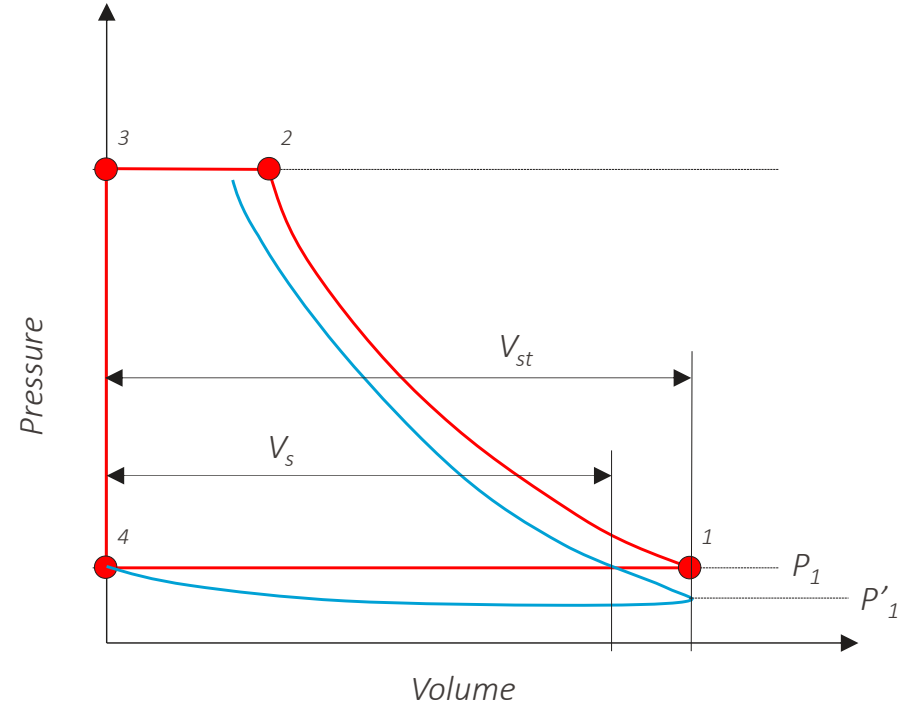


Volumetric Efficiency

Isolated Losses on Suction Volume

- Suction pressure drop can be linked to suction volume reduction

$$\left. \frac{P'_1}{P_1} \right|_{T=cst} = \frac{V_s}{V_{st}} = \eta_{v1}$$



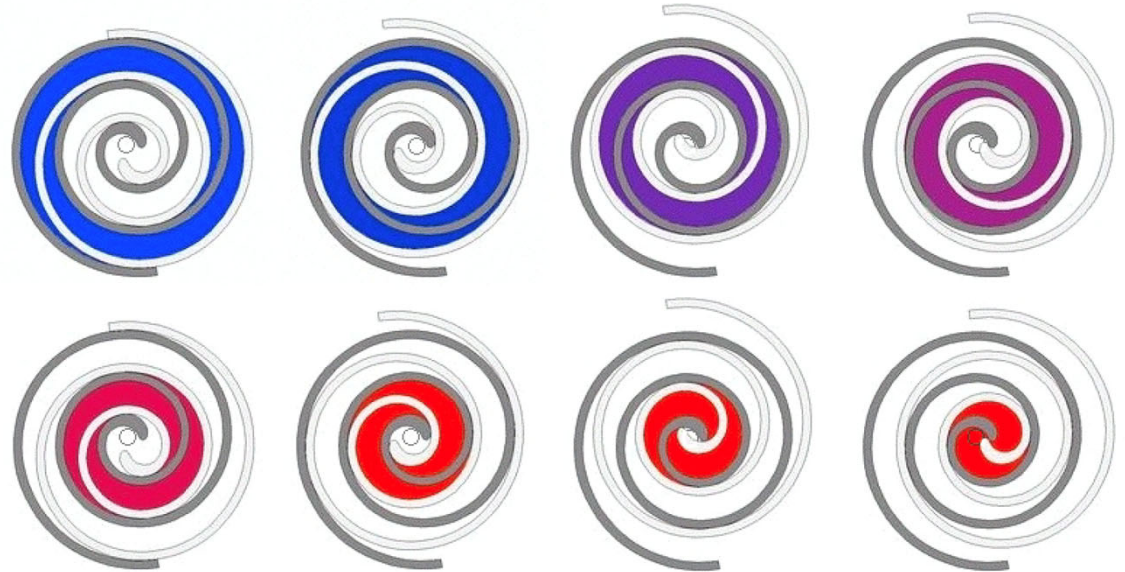
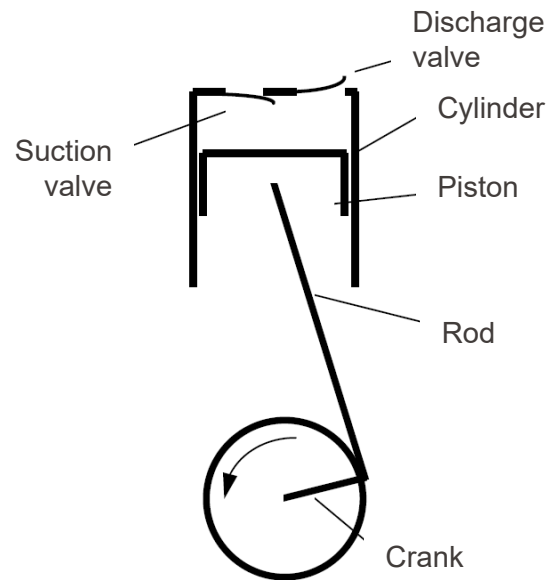
Volumetric Efficiency

- Overall volumetric efficiency

$$\eta_v = \frac{V_s}{V_{st}} = \frac{P'_1}{P_1} (1 + \epsilon) - \epsilon \Pi^{1/\kappa} = \eta_{v1} (1 + \epsilon) - \epsilon \Pi^{1/\kappa}$$

$$\eta_v = \eta_{v1} \left[1 - \epsilon \left(\frac{\Pi^{1/\kappa}}{\eta_{v1}} - 1 \right) \right] \approx \eta_{v1} \eta_{v2}$$

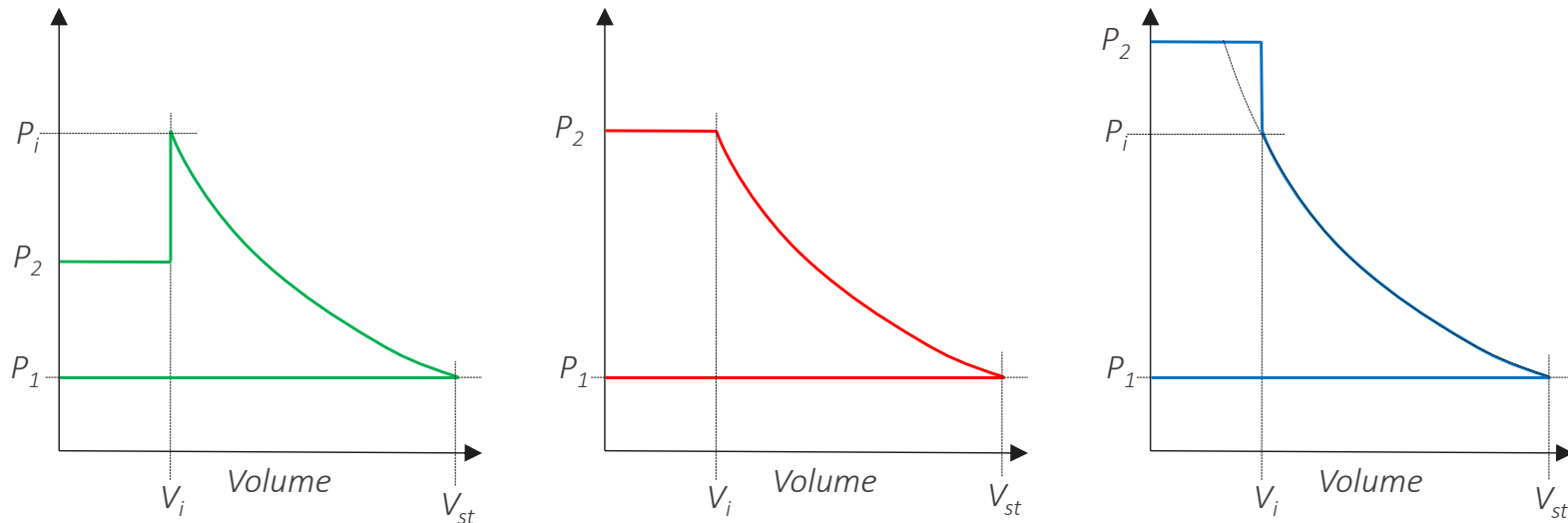
Piston vs. Fixed Volume Ratio Compressors



- In piston compressors discharge valve opens only when discharge pressure is achieved in working chamber
- In fixed volume ratio compressor over- & under-compression may occur

Over- & Under-Compression

- Occurs in built-in fixed volume ratio compressors → work surplus



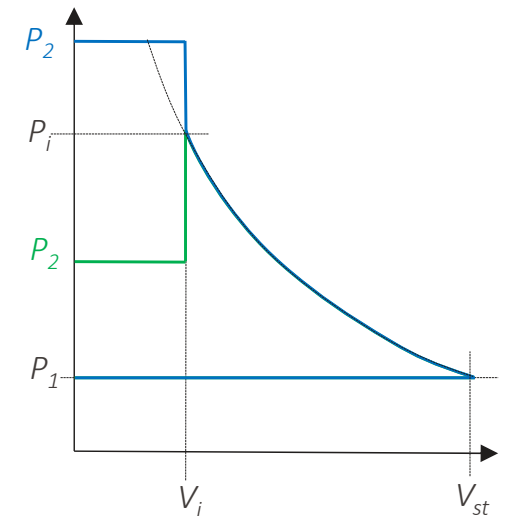
$$V_R = \frac{V_{st}}{V_i} \quad \Pi = \frac{P_2}{P_1} \quad \Pi_i = V_R^\kappa$$

Over- & Under-Compression

- Expression for theoretical compressor efficiency (perfect gas)

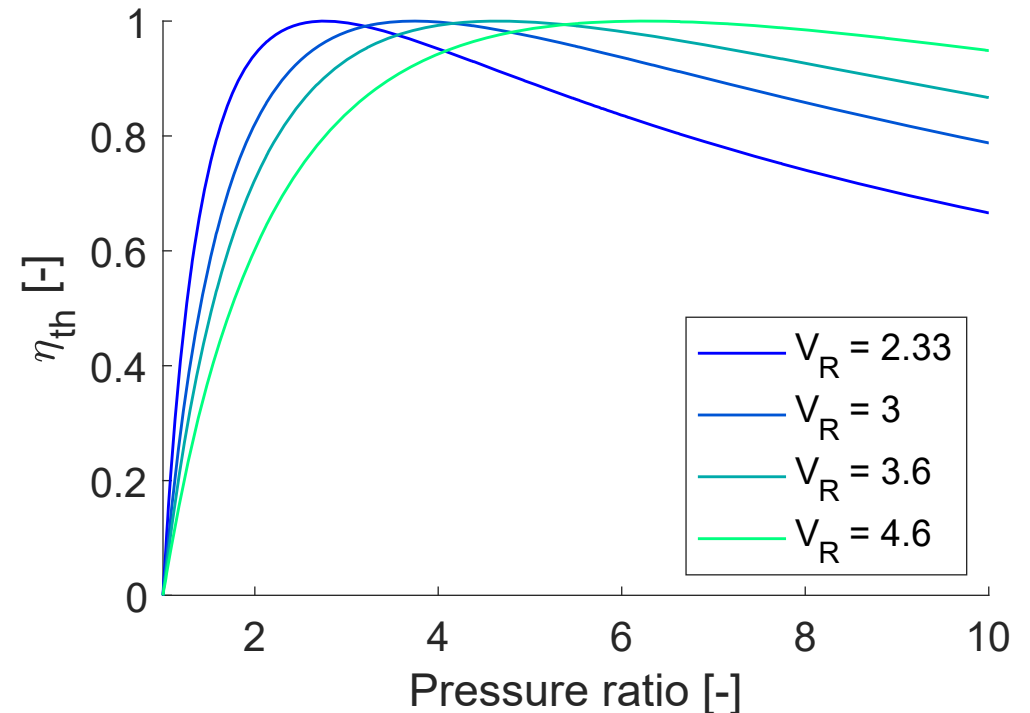
$$\eta_{th} = \frac{\frac{\kappa}{\kappa-1} RT_1 \left[\Pi^{\frac{\kappa-1}{\kappa}} - 1 \right]}{\frac{\kappa}{\kappa-1} RT_1 \left[\Pi_i^{\frac{\kappa-1}{\kappa}} - 1 \right] + (P_2 - P_i) V_i} = \frac{\kappa \left[\Pi^{\frac{\kappa-1}{\kappa}} - 1 \right]}{V_R^{\kappa-1} - \kappa + (\kappa - 1) \frac{\Pi}{V_R}}$$

$$V_R = \frac{V_{st}}{V_i} \quad \Pi = \frac{P_2}{P_1} \quad \Pi_i = V_R^\kappa$$



Theoretical Efficiency (Over- & Under-Compression)

- Efficiency drops rapidly in over-compression mode
- Built-in pressure ratio depends on built-in volume ratio and fluid
- Ideal compressor built-in volume ratio depends on operating envelope of heat pump cycle and on working fluid



Isentropic Efficiency

- Electrical efficiency

$$\eta_{el} = \frac{e_m^+}{e_{el}^+}$$

- Mechanical efficiency

$$\eta_m = \frac{e_f^+}{e_m^+}$$

- Internal isentropic efficiency

$$\eta_{is-int} = \frac{e_{is}^+}{e_f^+}$$

- Isentropic efficiency

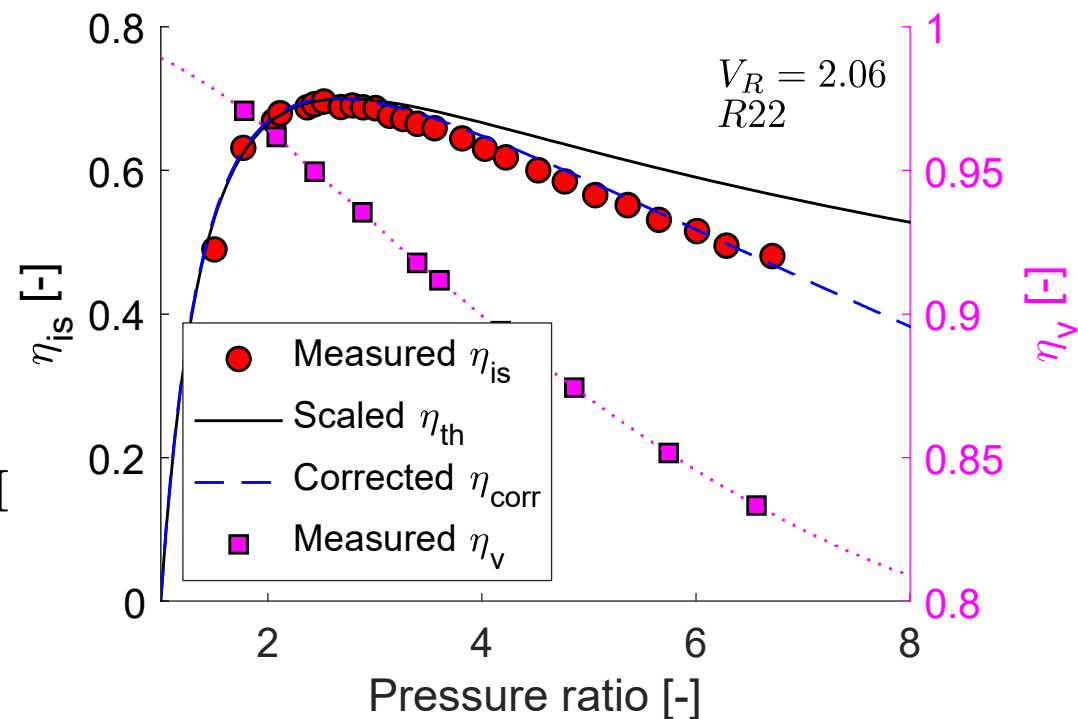
$$\eta_{is} = \eta_{el}\eta_m\eta_{is-int} \approx \eta_{is-max}\eta_{th}$$

Comparison to Measured Data

- Experimental scroll compressor data with $\eta_{is-max} = 0.71$
- Scaled theoretical efficiency overpredicted at high Π
- Correction to account for effect of leakage on isentropic efficiency

$$\eta_{is} = \eta_{is-max} \eta_{th} - c(1 - \eta_v) \Pi$$

$$c = 0.07$$



- Positive displacement compressors are characterized by a volumetric and an isentropic efficiency
- Volumetric efficiency is decreased by underfilling at suction, expansion of the clearance volume after discharge and by internal leakage
- Compressors with built-in volume ratio may suffer from over- and under-compression, which scaled with the maximum measured isentropic efficiency offers a good predictive model

Heat Pump Systems

Screw & Scroll
Compressors

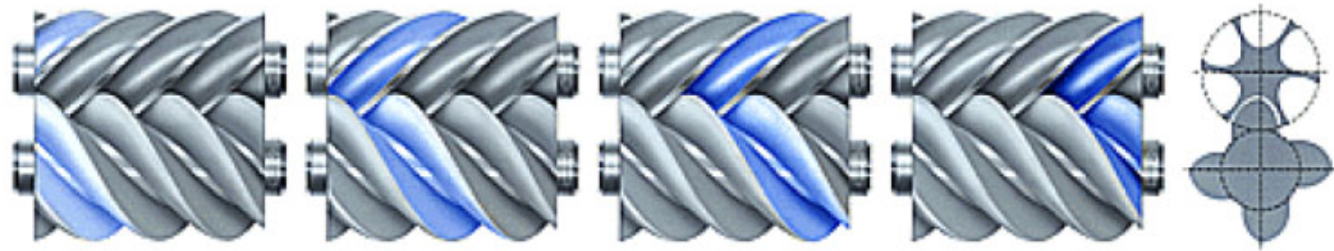
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Varying Compressor Operating Conditions

- Heat pumps need to be able to operate under varying conditions
- Changing temperature levels in evaporator and condenser imply varying pressure ratios across compressor
- Changing heating and cooling power at constant temperature levels implies changing mass-flow / volumetric flow delivered by compressor
- Ideal positive displacement compressor should be able to change installed volume ratio and volume flow

Variable Screw Compressor Geometry

- In fixed geometry screw compressors volume ratio and suction volume are defined by geometry of screw rotors and on axial discharge port



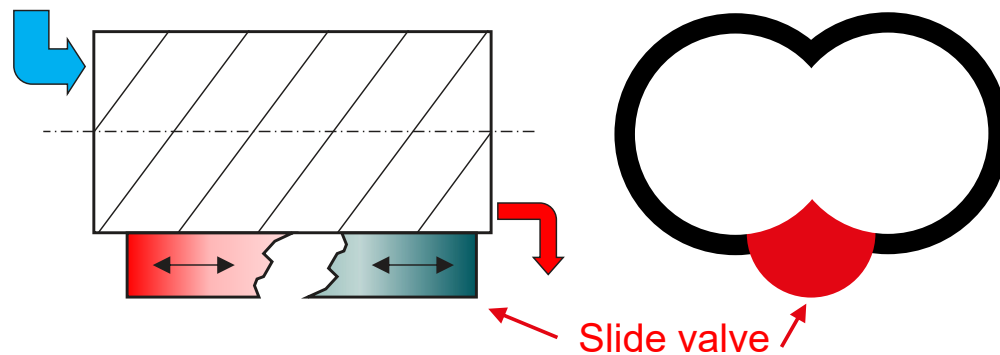
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Variable Screw Compressor Geometry

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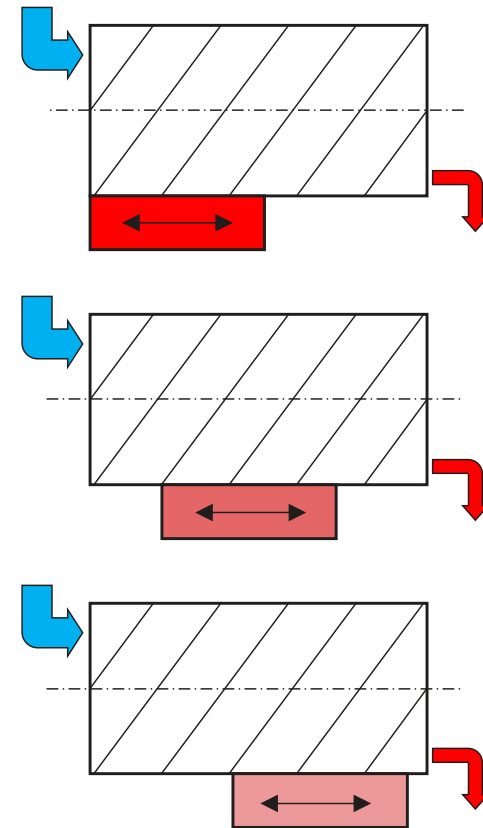
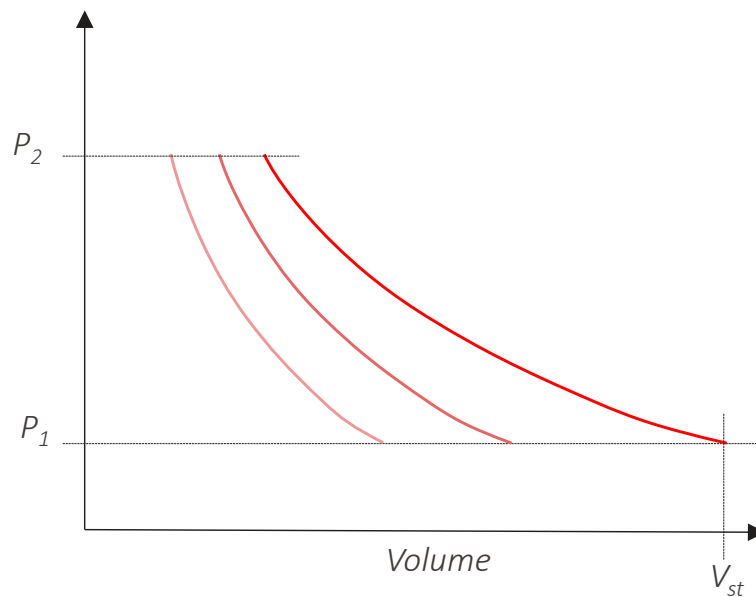


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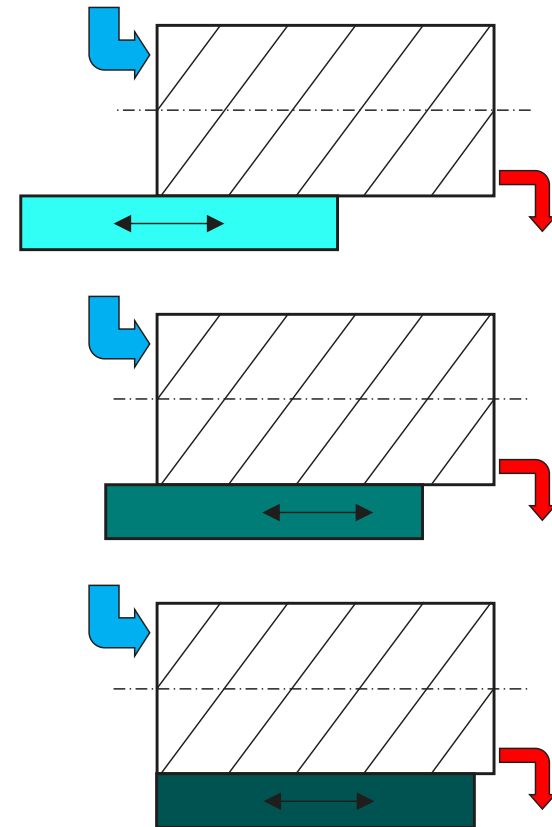
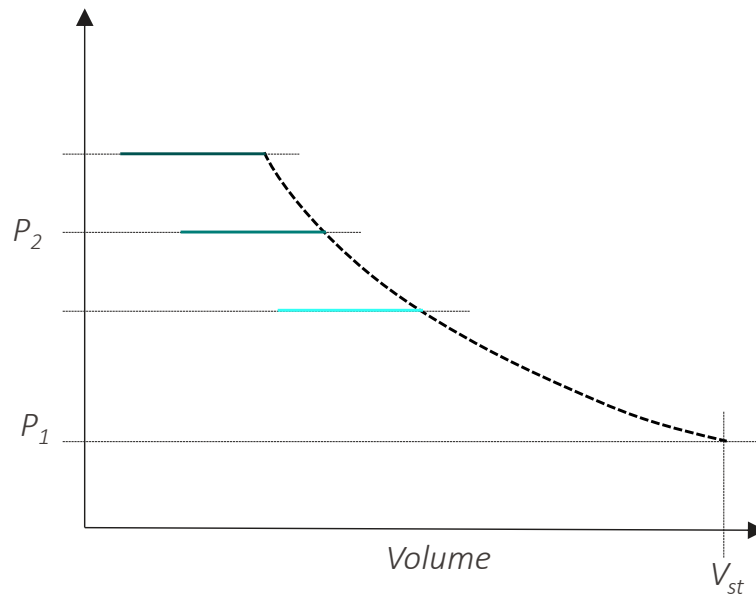
Suction Volume Modulation at Constant V_r

- Slide vane covering constant width yields constant volume ratio while modulating suction volume (\rightarrow power modulation)



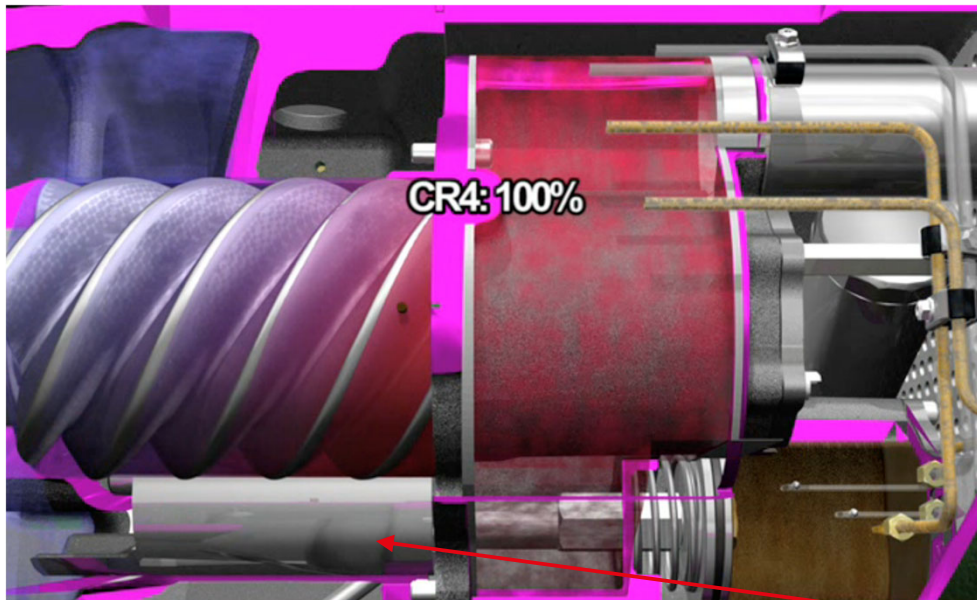
Volume Ratio Modulation at Constant Suction

- Long slide valve to modify volume ratio while keeping suction volume constant

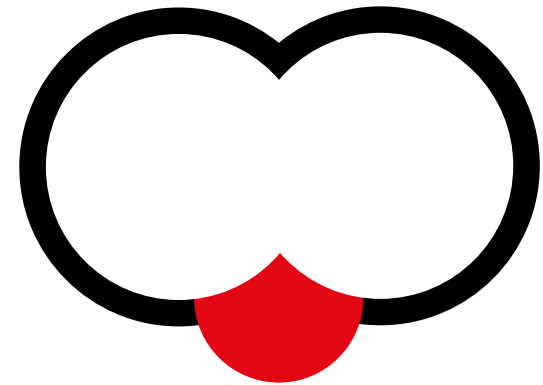


Volume Ratio and Suction Volume Modulation

- Long sliding vane with moving edge on the suction side only



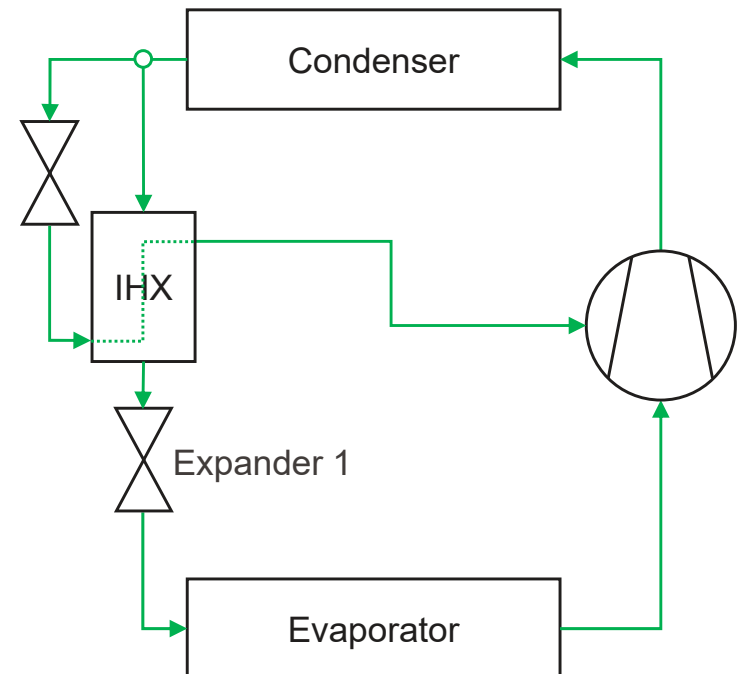
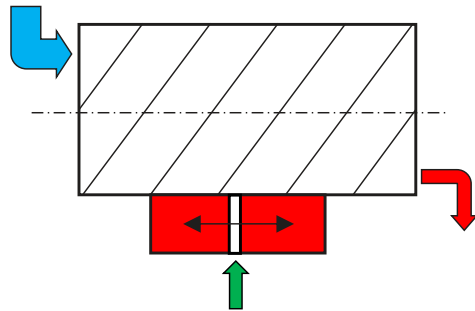
Courtesy of Bitzer



Slide valve

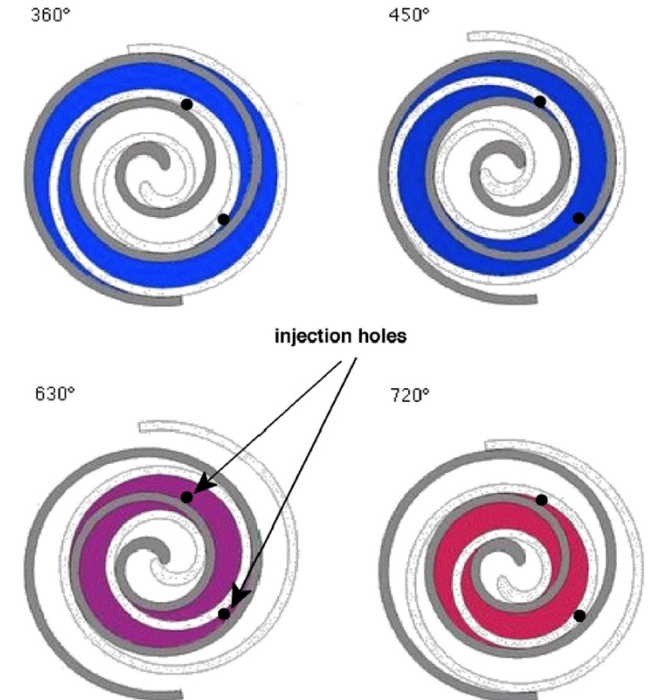
Injected Screw Compressor

- Use single stage compressor with intermediate injection port to avoid investment of two compressors
- In screw compressors intermediate injection can be implemented on sliding valve → economizer port



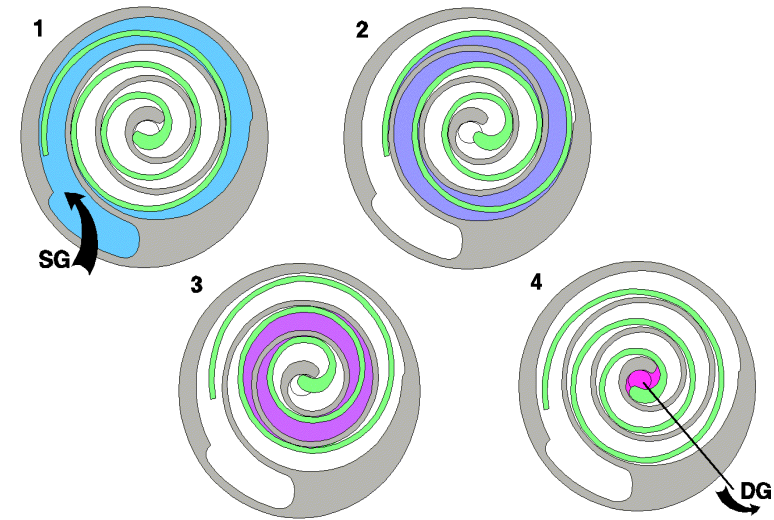
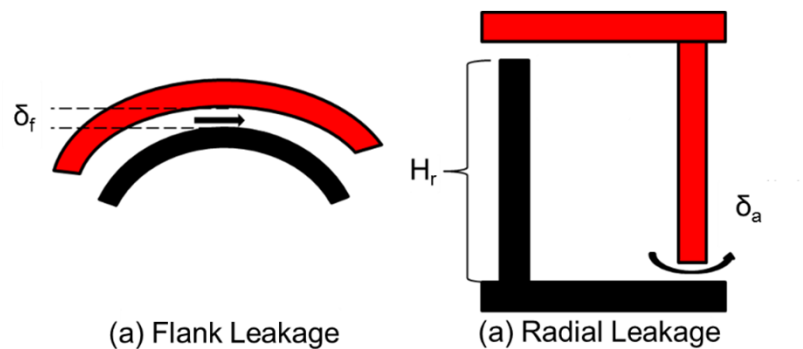
Injected Scroll Compressor

- Scroll compressors can also be designed with economizer ports
- Injection ports located in fixed scroll
- Injection occurs into closed compression chambers after compression initiated



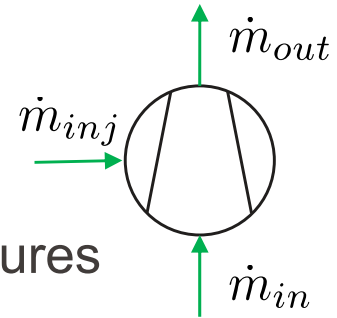
Scroll Compressor Features

- Scroll compressor design prevents direct leakage from discharge to suction pressure → limited losses through internal leakage
- Feature small clearance volume compared to alternative designs

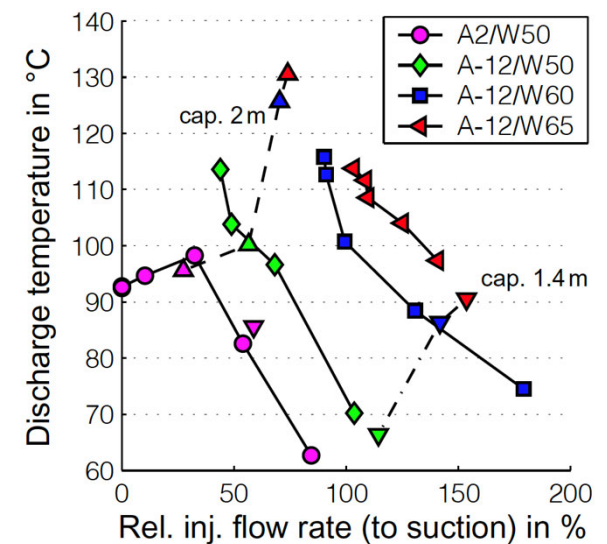
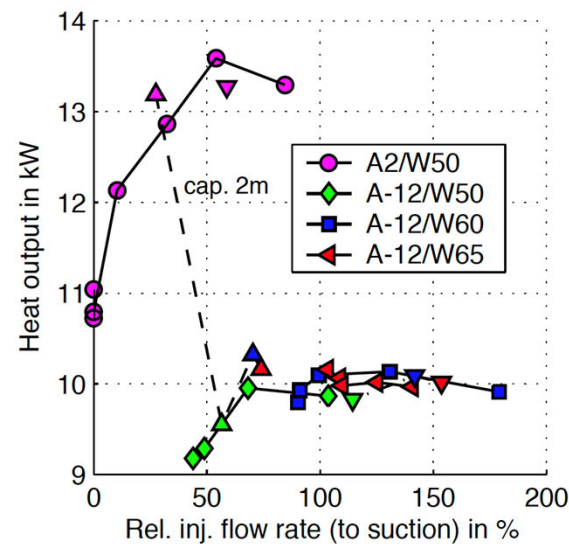
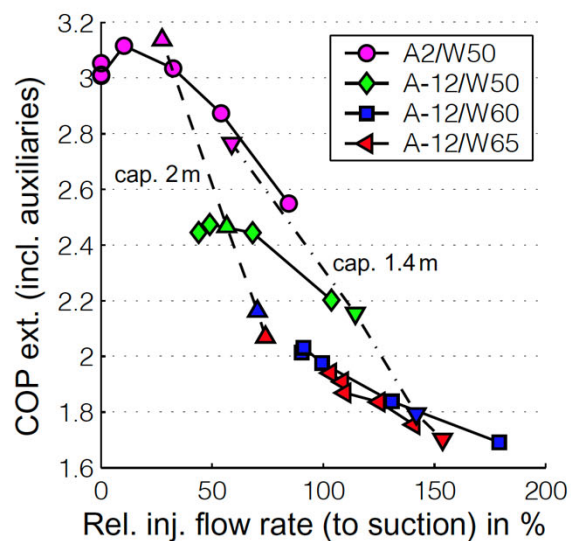


Courtesy of Bitzer

Test Results with Injected Scroll Compressor



- Lifts of 77K achieved with low compressor discharge temperatures
- COP drops with injection rate \rightarrow injection losses
- Injection means to increase output power



Summary

- Screw compressors with sliding vane offer added flexibility (variable volume ratio, variable suction volume, intermediate injection)
- Screw compressors preferred at large scale, scrolls for domestic scale
- Scrolls yield fixed volume ratio, mass-flow modulation is achieved with speed control
- For high temperature lifts scroll compressors can be equipped with intermediate economizer injection ports

Exercises W8

- Comprehension questions
- Compressor selection