

Heat Pump Systems

Summary W10

Prof. J. Schiffmann

Radial Compressor Geometry

■ Typical geometric features

- Impeller tip width ratio

$$0.02 < b_4/r_4 < 0.2$$
- Relative impeller tip clearance

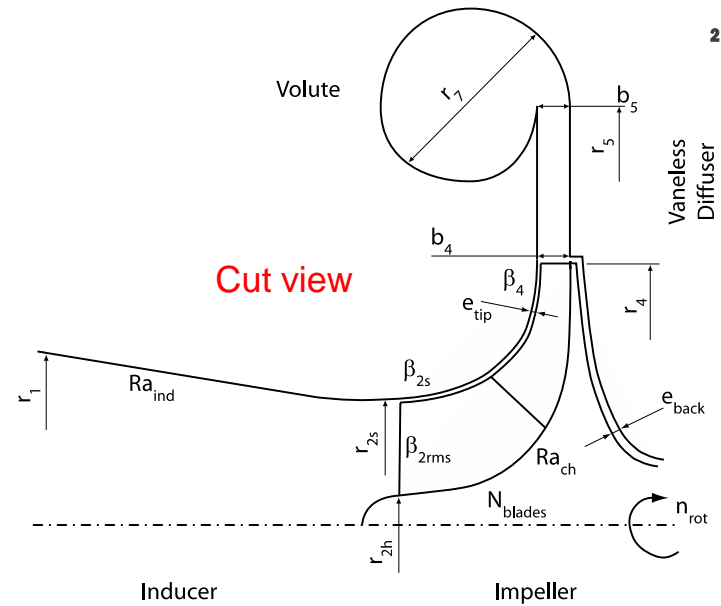
$$e_{tip}/b_4 < 0.05$$
- Number of blades

$$12 < N_{blades} < 32$$
- Axial length

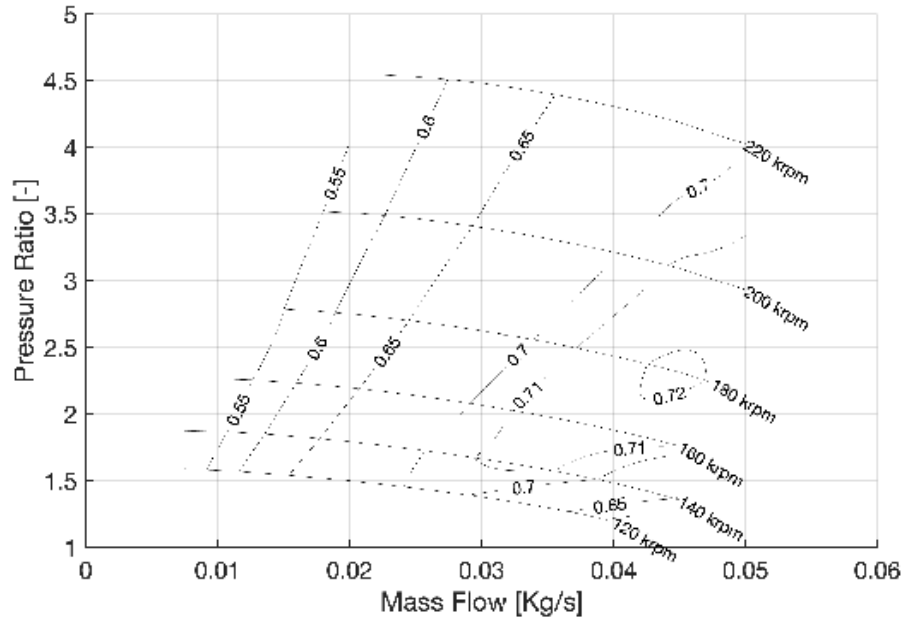
$$L/r_4 \approx 0.35$$
- Inlet diameter ratio

$$0.3 < r_{2s}/r_4 < 0.7$$
- Blade angles

$$\beta_{2s} = -60^\circ \quad \beta_4 \approx -40^\circ$$



- Map limited towards lower mass flows by surge and towards higher mass by choke



- Choke defines upper mass flow for each speed line
 - Reducing back pressure increases velocity until it reaches the speed of sound in smallest passage
 - Further reduction in back pressure yields no increase in mass flow
 - Speed line is vertical after choking has occurred
 - Choking can occur at inlet, impeller, or diffuser
 - Higher speeds shift choke to higher mass flows until inlet is choked
 - Throat usually near impeller inlet or diffuser inlet

- Surge line marks the low flow limit of region of stable operation
 - Caused by increase in loading as mass flow is reduced (lower mass flow → increased incidence → increased loading → separation)
 - Depends on compressor itself & system configuration

- Instability can have several forms
 - Rotating Stall: separation in blade rows which jumps from one blade to next → mass flow nearly constant with small high-frequency pressure fluctuations
 - Mild Surge: Pulsations in mass flow and pressure without backflow
 - Deep Surge: Strong periodic backflow through compressor with large pressure and mass flow variations → should be avoided



Heat Pump Systems

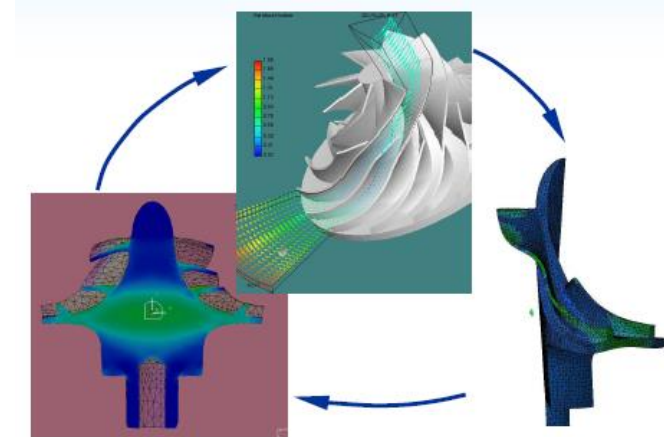
On the Modeling of
Centrifugal
Compressors

Prof. J. Schiffmann

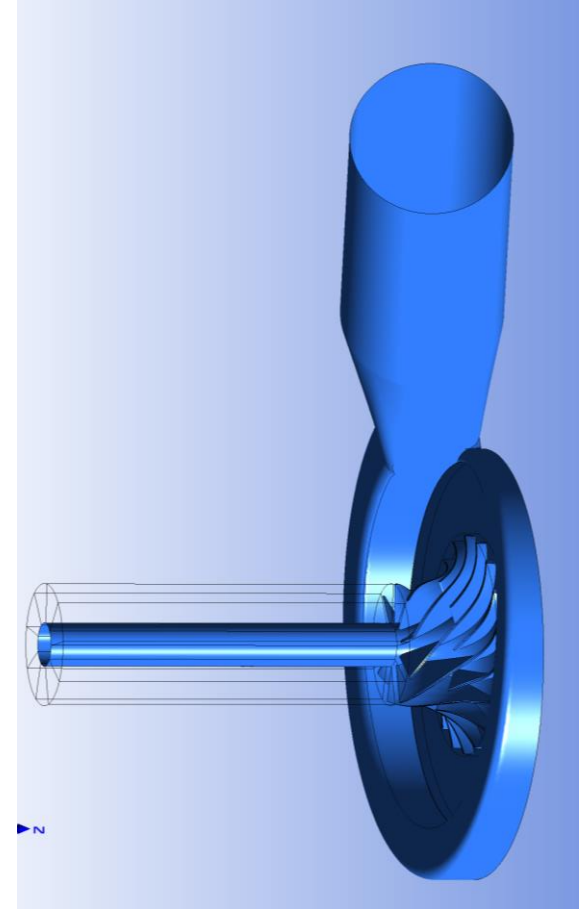
Design Process of Turbomachinery

- Design of turbocompressor is interdisciplinary task
 - Aerodynamics
 - Mechanical stress
 - Dynamics
 - Thermal

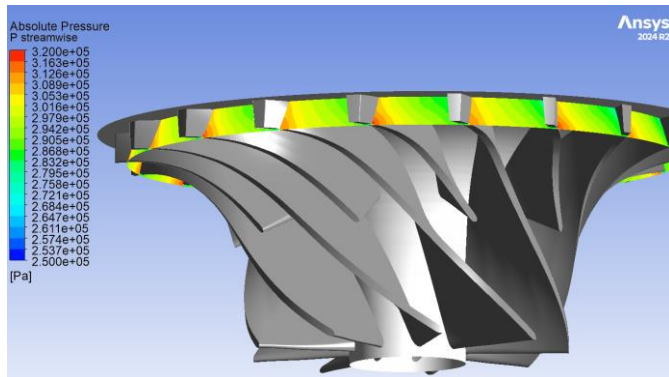
- Flow in turbomachinery is highly complex



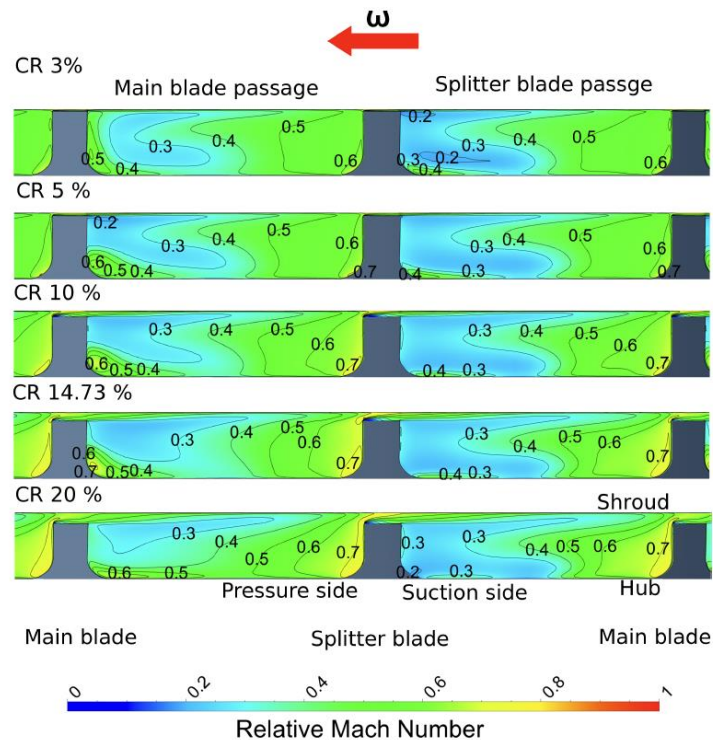
- Mesh of 30 million nodes
→ 15h computational time for one operating point → computational resources
- Not well suited for design



- Great for visualizing detailed flow features and analysis

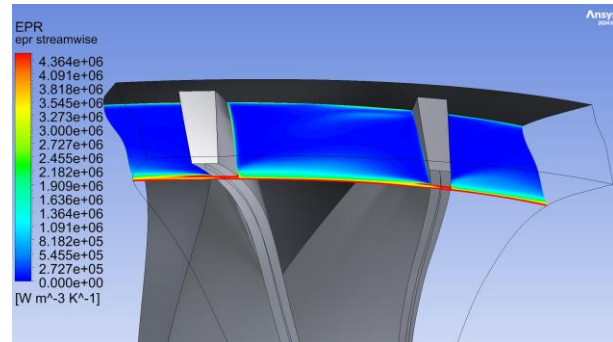


Pressure on pressure side larger than on suction side

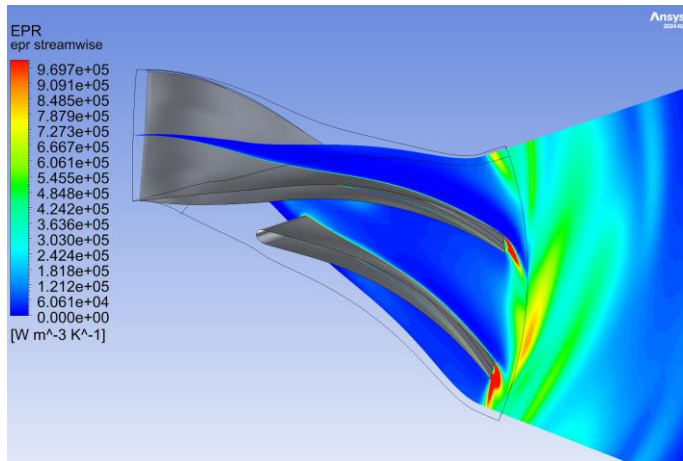


Accumulation of low momentum fluid close to suction side → jet-wake pattern
→ mixing losses into diffuser

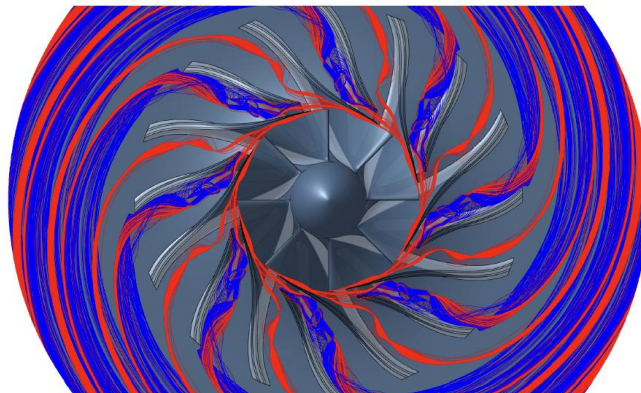
- Great for visualizing detailed flow features and analysis



Entropy production rate highest in tip gap and on surfaces \rightarrow skin friction

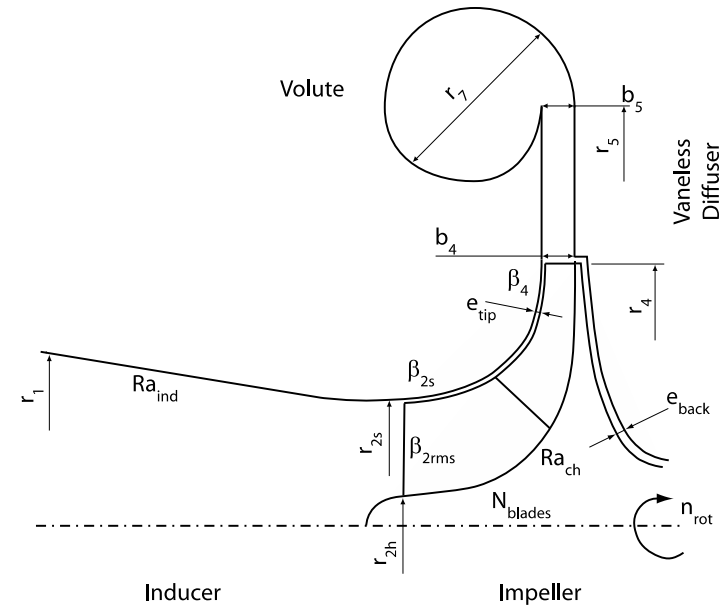


Trailing edge mixing into diffuser



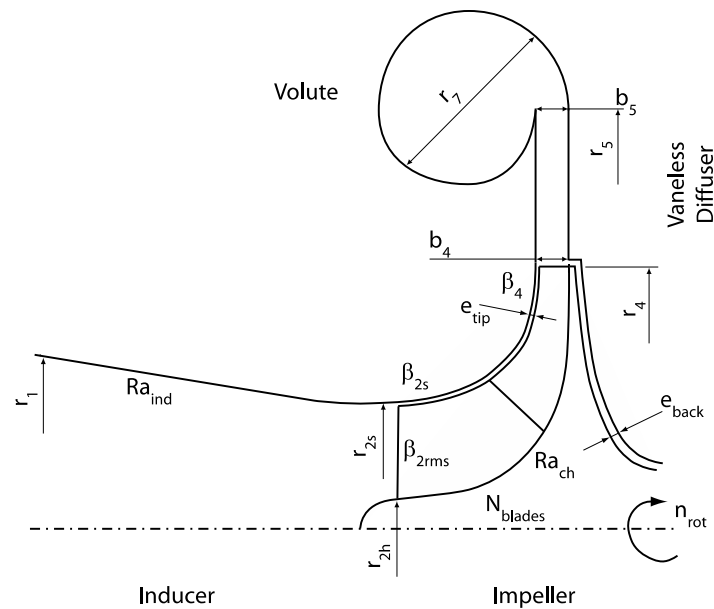
Trajectories of main (red streamlines) and splitter blade (blue streamlines) tip leakage vortices

- Modeling along flow direction, component by component
- Based on velocity triangles, mass- & energy conservation, h-s-diagram
- Representation of losses through empirical correlations



■ Proven Empirical Loss Correlations

- Skin Friction } Inducer
- Incidence
- Skin Friction
- Diffusion
- Clearance
- Disk friction
- Recirculation } Impeller
- Skin Friction
- Trailing edge mixing } Diffuser



- Further effects
 - Slip \rightarrow flow does not follow blade angle
 \rightarrow causes a decrease in work input

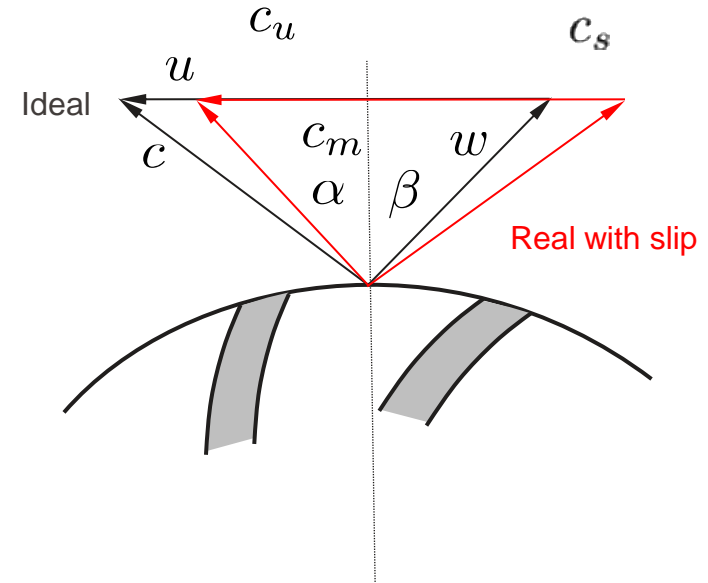
$$\frac{c_s}{u_4} = \frac{\sqrt{\cos \beta_{4bl}}}{N_{bl}^{0.7}}$$

- Aerodynamic blockage

$$B_i = A_{\text{eff}}/A_{\text{geom}}$$

- Surge in vaneless diffuser

$$\alpha_{\text{crit}} = f(M_4, b_4/r_4, r_5/r_4)$$

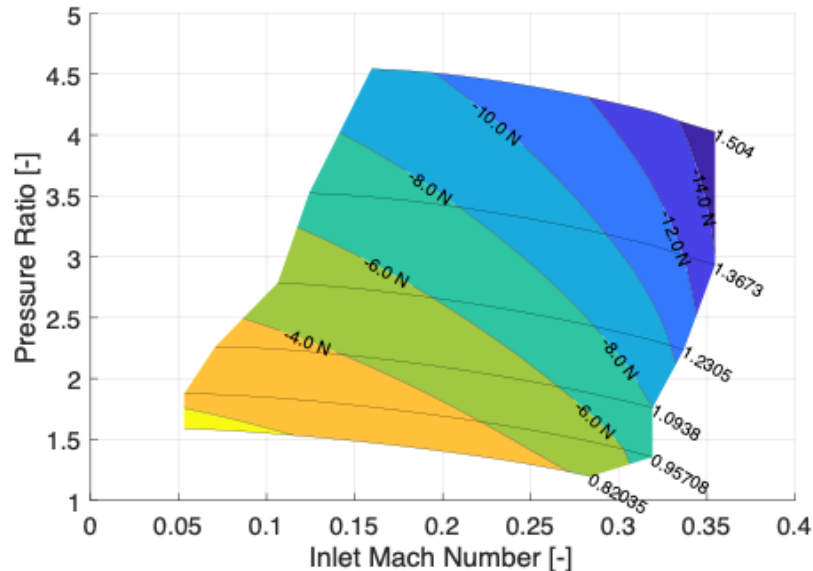


1D – Meanline Model

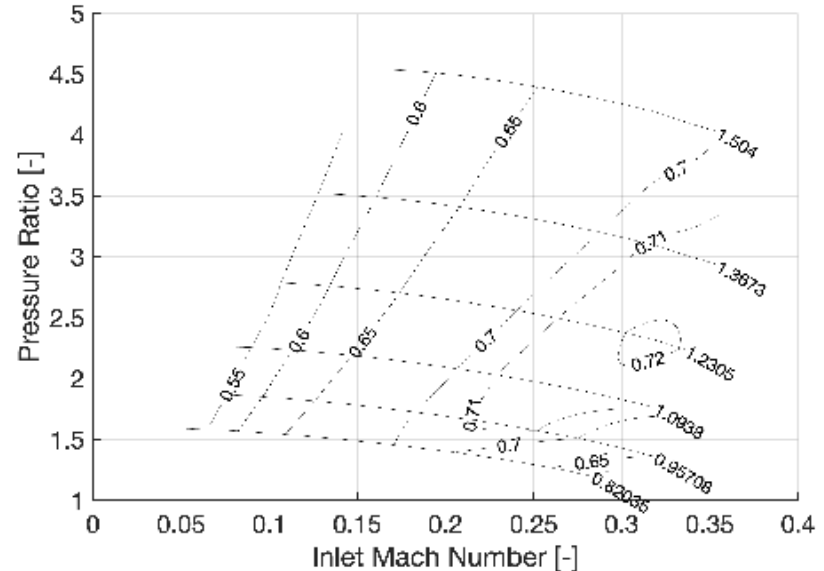
$$[PR, \eta_{is}, \text{surge}, \text{choke}] = f(\dot{m}, N_{rot}, P_{01}, T_{01}, \text{Fluid}, \text{Geom})$$

- Fast compressor map prediction → great for design
- No capturing of 3D flow patterns

Thrust force contours

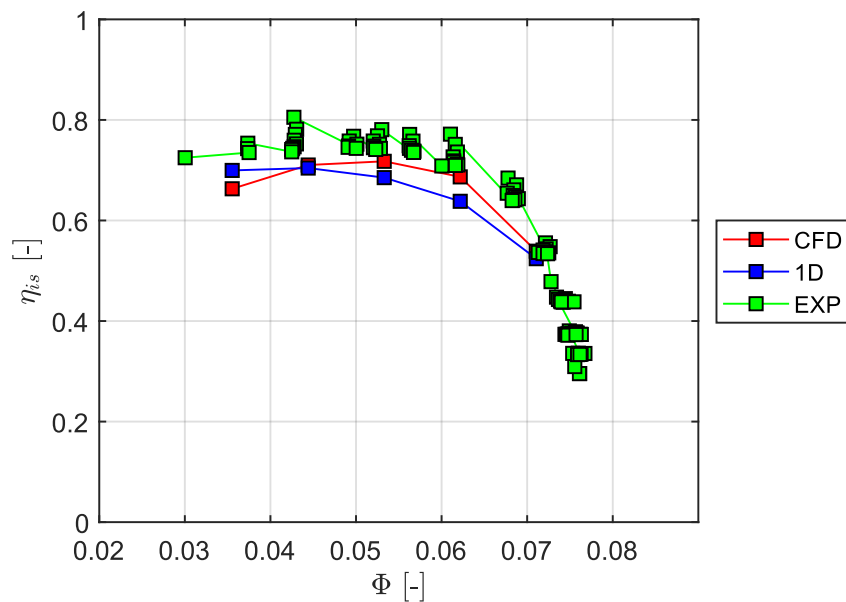
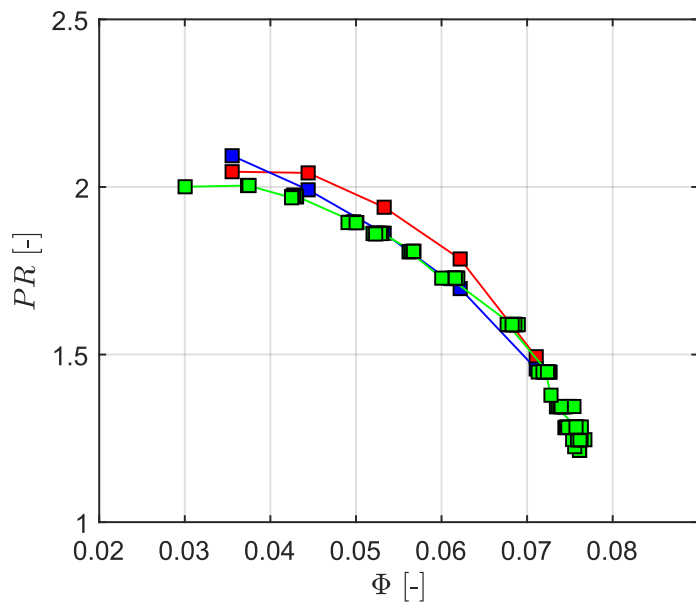
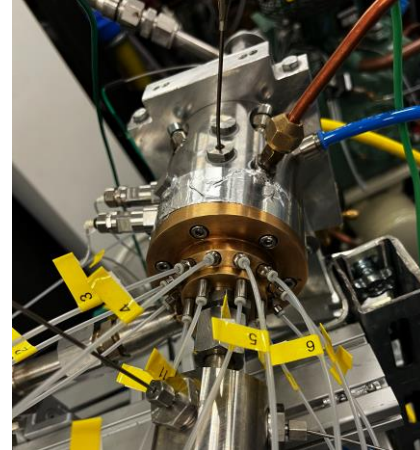


Isentropic efficiency contours



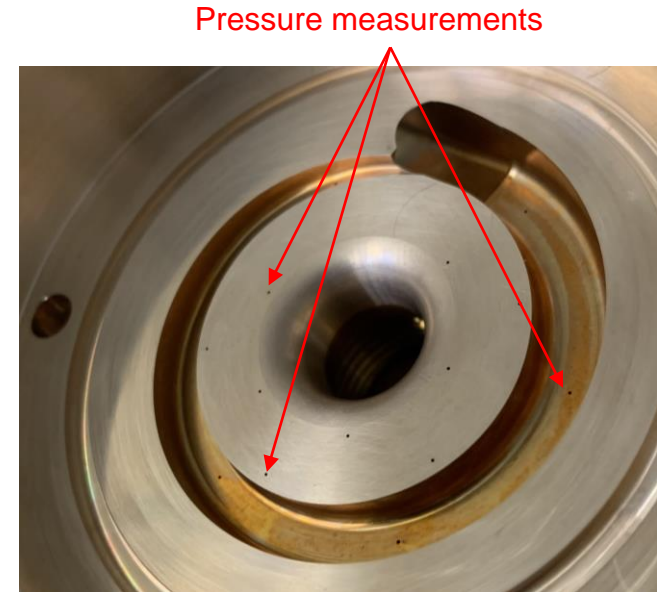
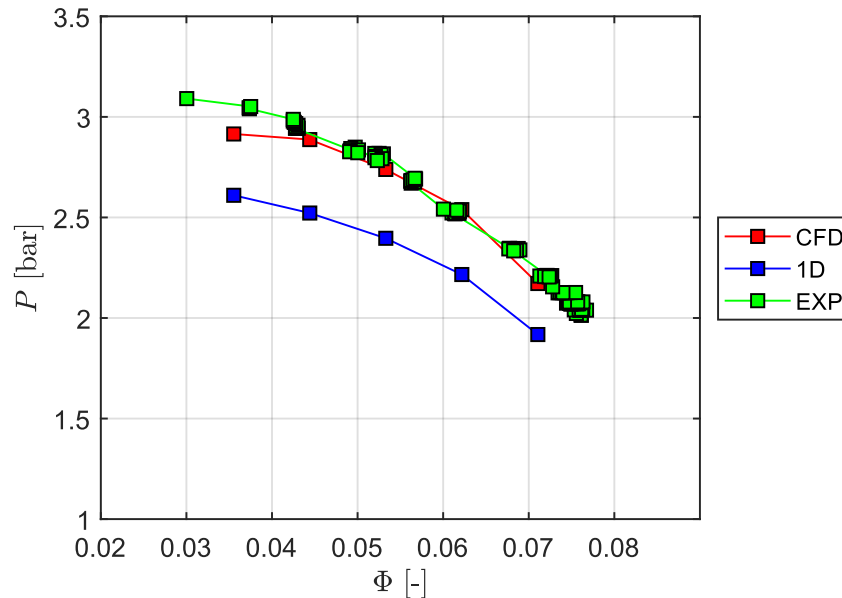
Comparison CFD – Meanline Model

- Excellent overall (out-in) agreement between experimental data, CFD, and meanline-model



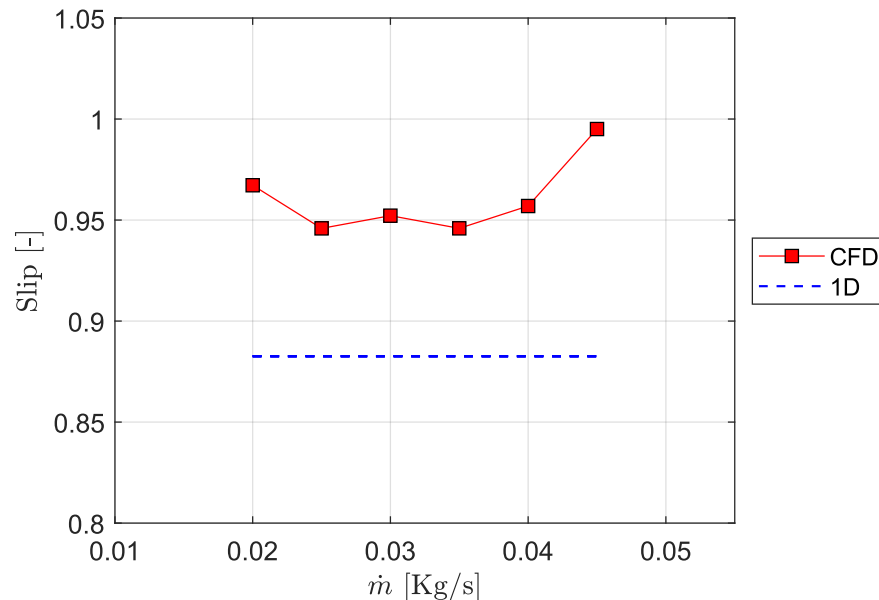
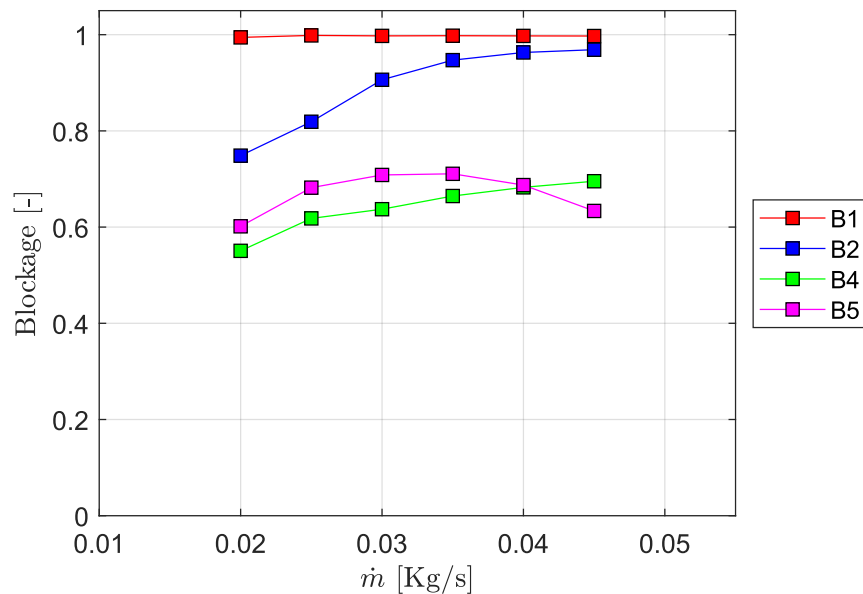
Comparison CFD – Meanline Model

- Inconsistency between meanline model, CFD & experiments at component level Impeller pressure ratio



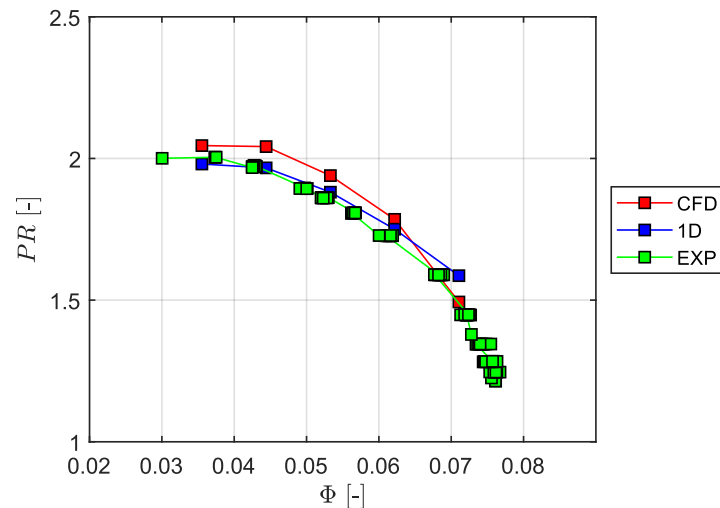
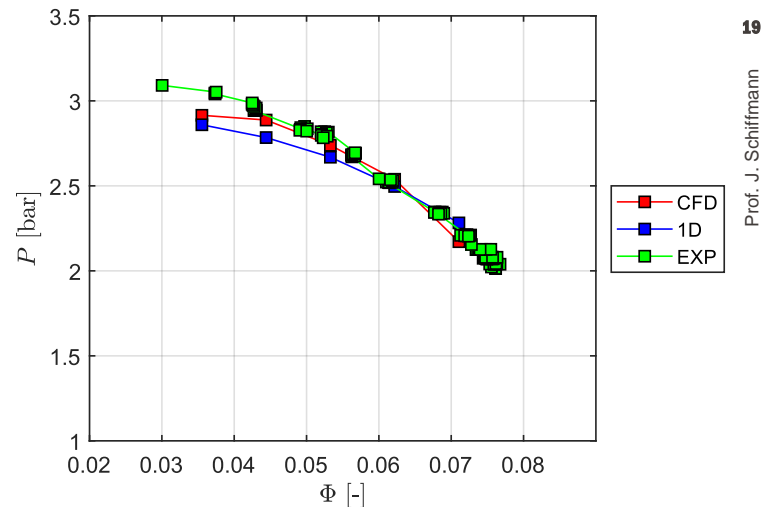
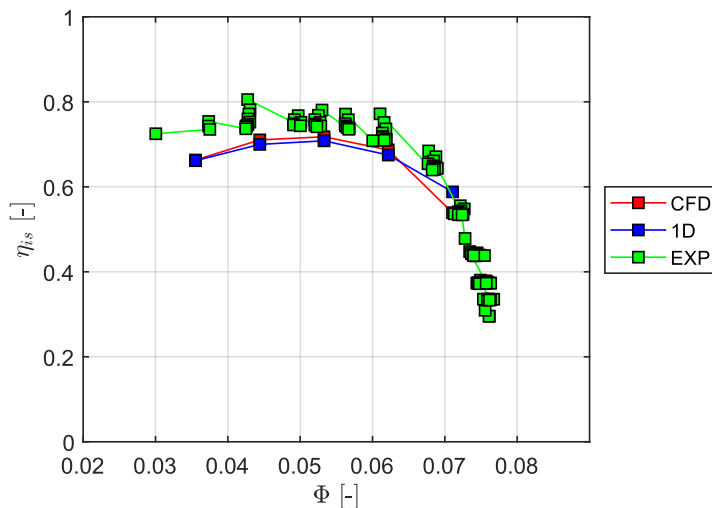
Meanline Model Calibration

- Correction of aerodynamic blockage factors, slip, and losses based on CFD data



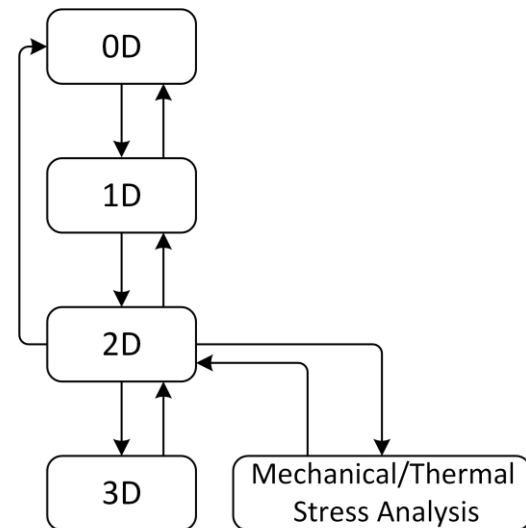
Calibrated Meanline Model

- Good agreement at a component level and overall
- Meanline models are very efficient but may need calibration



Design Process of Turbomachinery

- Iterative combination of increasingly complex models
 - 0D: Overall dimensions – based on empirical performance maps
 - 1D: Details of inlet and exhaust areas → meanline model
 - 2D: Definition of blade geometry
 - 3D: Assessment of detailed flow patterns
- Accurate starting point (0D) key for efficient design process
 - Requires design maps



- Parameters influencing compressor performance

$$[PR, \eta_{is}, \text{surge}, \text{choke}] = f(\dot{m}, N_{rot}, P_{01}, T_{01}, \text{Fluid}, \text{Geom})$$

- Using dimensional analysis

$$[\lambda, \eta_{is}] = f(\phi_{01}, M_{u4}, Re, \text{Fluid}, \text{Geom})$$

$\lambda = \frac{h_{04} - h_{01}}{u_4^2}$
 Work input coefficient

$\phi_{01} = \frac{\dot{m}}{\rho_{01} D_4^2 u_4^2}$
 Flow coefficient

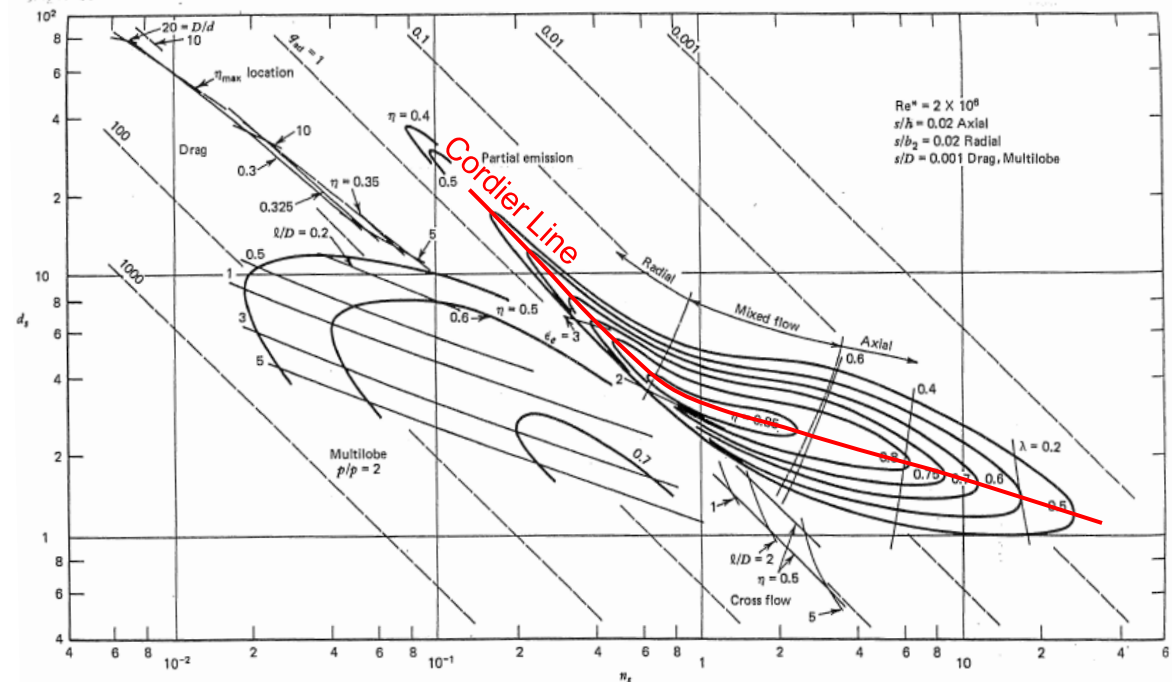
$M_{u4} = \frac{u_4}{a_{01}}$
 Machine Mach number

Compressor Design Maps

- Specific speed and diameter alternative set of dimensionless parameters

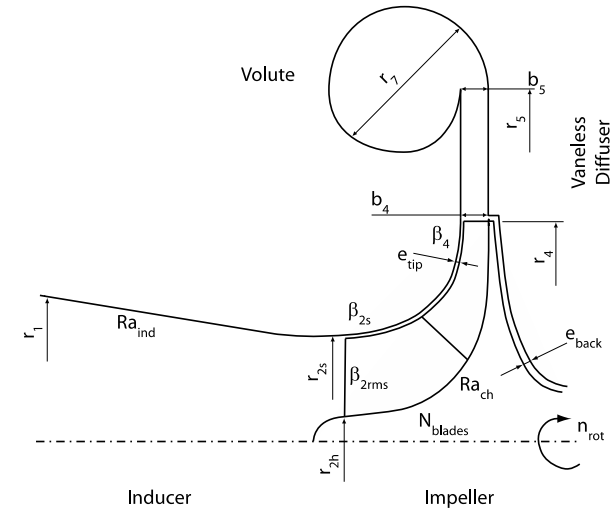
$$n_s = \omega \frac{\dot{V}_{01}^{0.5}}{\Delta h_{is}^{0.75}}$$

$$d_s = d_4 \frac{\Delta h_{is}^{0.25}}{\dot{V}_{01}^{0.5}}$$



O. Balje, Turbomachines: A guide to design, selection and theory, 1981, Wiley

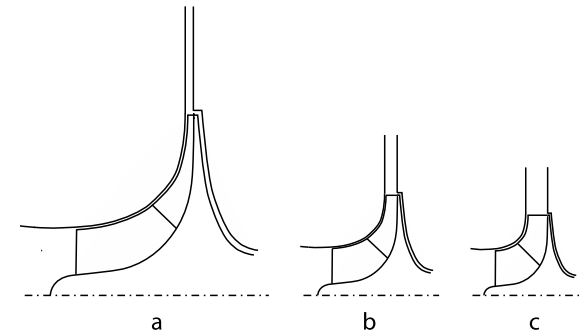
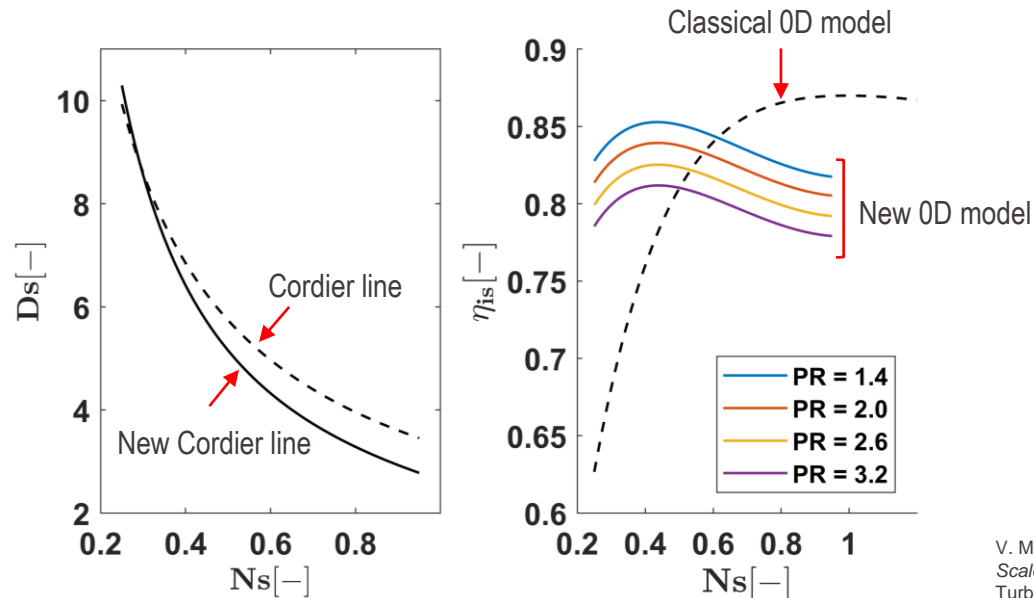
-
- ```
graph TD; A([Uniform Monte Carlo sampling]) --> B[• Range of geometry
• Thermodynamic inlet conditions]; B --> C[1D compressor model]; C --> D((Dataset)); D --> E[eureka
Symbolic regression];
```
- The flowchart illustrates the Eureka symbolic regression workflow. It begins with 'Uniform Monte Carlo sampling' in an oval, which points to a box containing a list of parameters: 'Range of geometry' and 'Thermodynamic inlet conditions'. This box is part of a larger dashed red rectangle that also contains a '1D compressor model' box below it. An arrow points from the parameter box to the model box. From the model box, an arrow points down to a cloud-shaped icon labeled 'Dataset'. Finally, an arrow points from the dataset to a box at the bottom containing the 'eureka' logo and the text 'Symbolic regression'.



$$\eta_{iS,0D} = f(N_S, D_S, PR, \overline{b_4}, \overline{r_{2S}})$$

# Updated Design Maps

- Updated model for reduced scale compressors deviates from literature
- New model includes additional design variables → more information

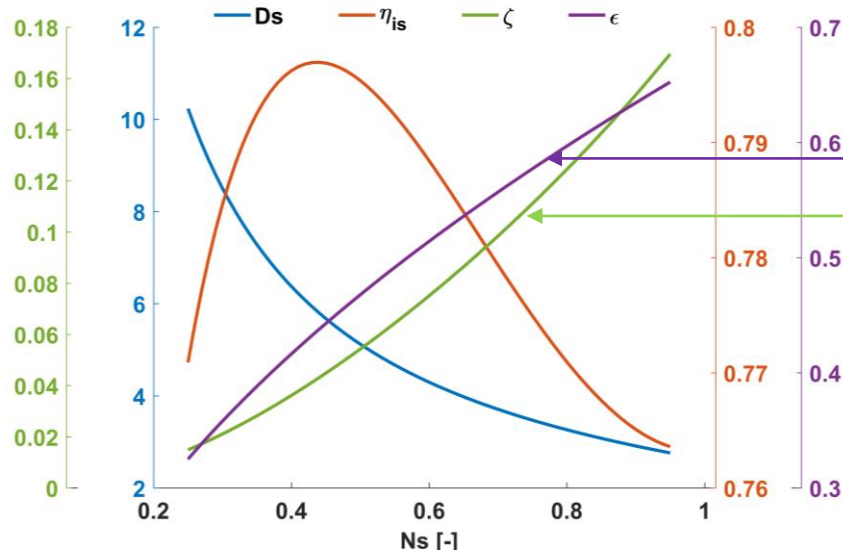


V. Mounier, C. Picard, J. Schiffmann, *Data-Driven Predesign Tool for Small-Scale Centrifugal Compressor in Refrigeration*, Journal for Engineering of Gas Turbine and Power, 2018, Vol.140



# Impact of Updated Design Maps

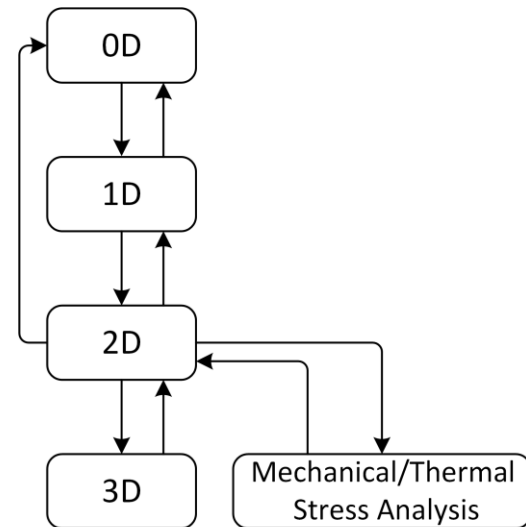
- Compared to classical tools new model yields more design information
- Data driven tool improves starting point and bypasses 1D design loop
- New tool is 1'500 x faster than meanline model with similar accuracy



Inlet blade height  $\overline{r_{2s}}$   
Outlet blade height  $\overline{b_4}$

V. Mounier, C. Picard, J. Schiffmann, *Data-Driven Predesign Tool for Small-Scale Centrifugal Compressor in Refrigeration*, Journal for Engineering of Gas Turbine and Power, 2018, Vol.140

- Design of radial compressor is iterative process
- Involves aerodynamic, mechanical, and thermal aspects
- Design starts with “first guess” and evolves by engaging increasingly complex models
- Research efforts
  - Improve meanline models
  - Increase speed of high-fidelity models
  - Surge prediction
  - Behavior of turbomachinery at small scale

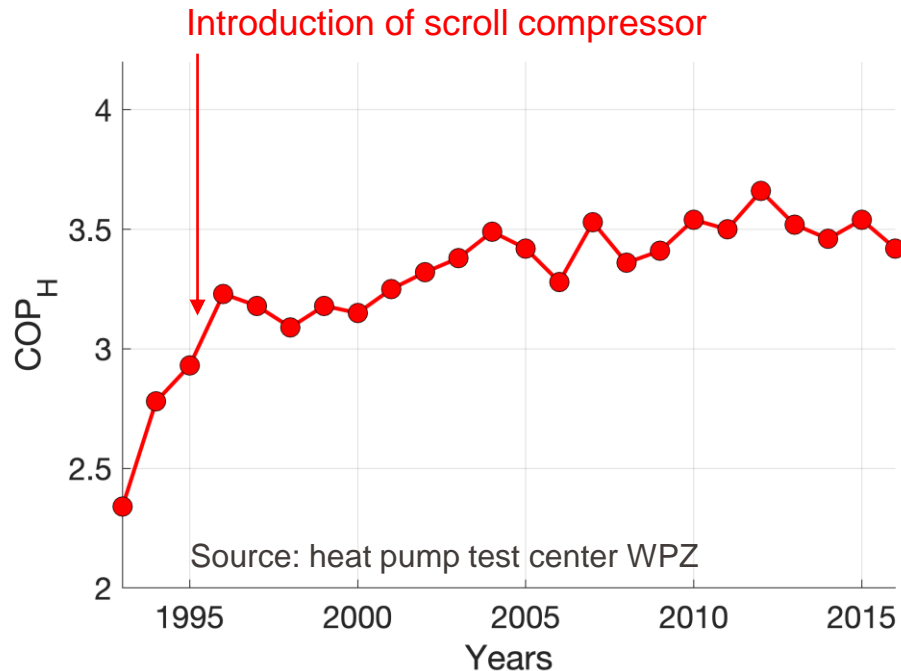


# Heat Pump Systems

On Small-Scale  
Turbocompressors  
for Heat Pumps

Prof. J. Schiffmann

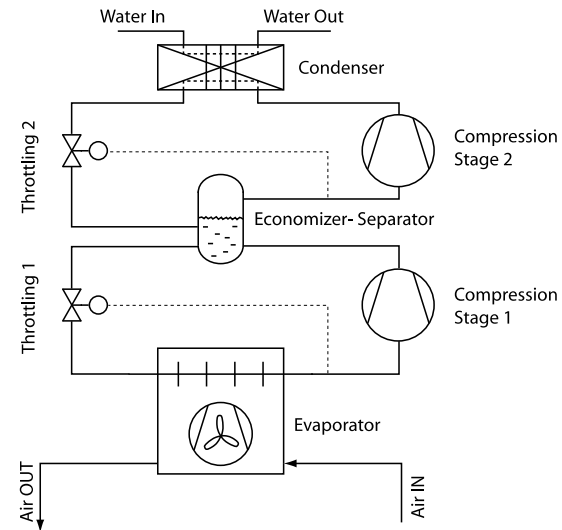
# Historic Evolution of COP Trends



$$COP_H = \frac{q_h^-}{e^+}$$

- Since introduction of scroll compressors, COP has been rising slowly
- Key question: can another step-change be achieved and if so, how?

- Assessment of losses in heat pump cycles
  - Compression 50%
  - Expansion 30%
  - Heat transfer 20%
- Possible ways to reduce losses
  - Increase compressor efficiency
  - Use oil-free technology
  - Implement multistage cycles
- Potential enabler
  - Turbocompressors on oil-free bearings



# Compressor Technology Selection

- Positive displacement machines preferred for small capacity, dynamic compressors traditionally for high capacities



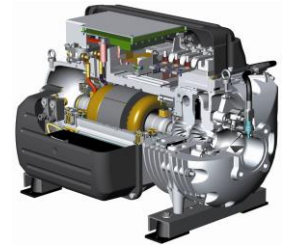
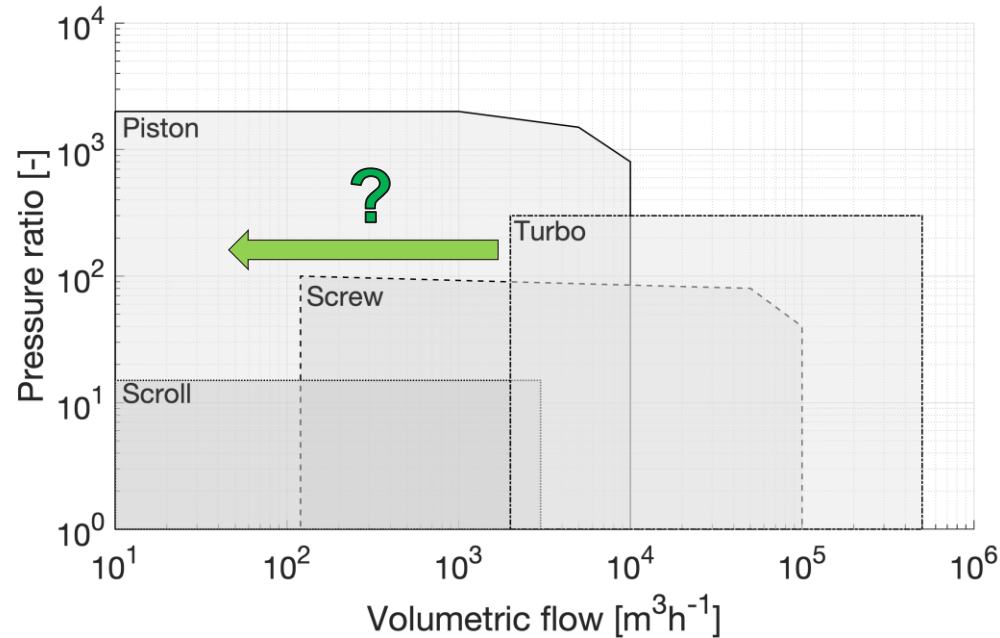
weiku.com



bitzer.de

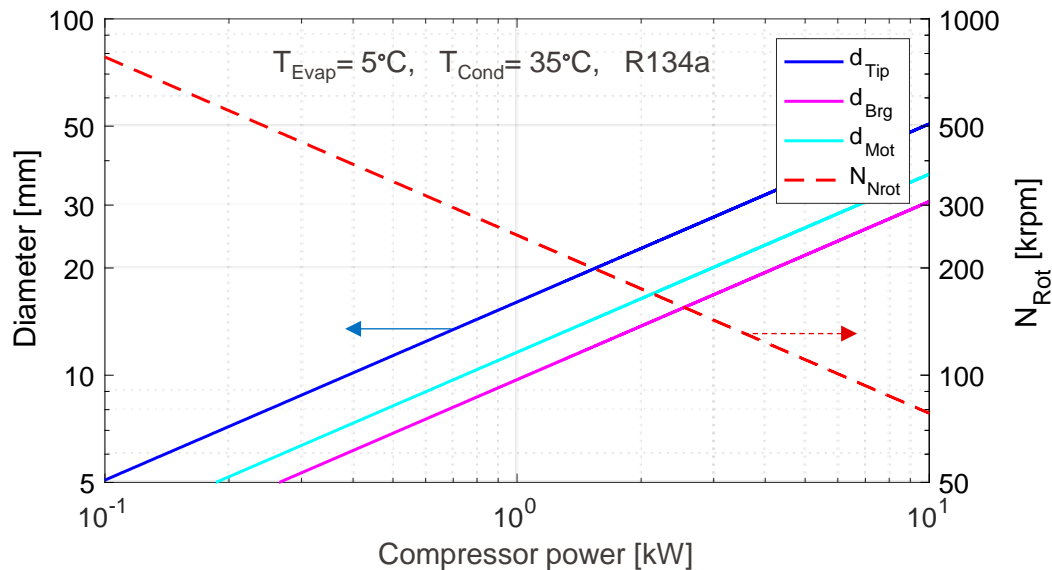


atlascopco.ch



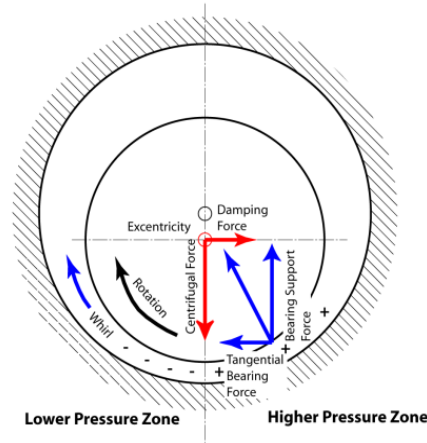
turbocor.com

- Downscaling power increases  $N_{\text{Rot}}$  and decreases size
  - Constant tip speeds  $\rightarrow$  no mechanical issues
- Aerodynamic challenges
  - Increased friction due to lower Re-number and higher roughness
  - Larger relative tip-clearance
  - Non-adiabatic operation
- Bearings
  - Need to support high speed and high lifetime



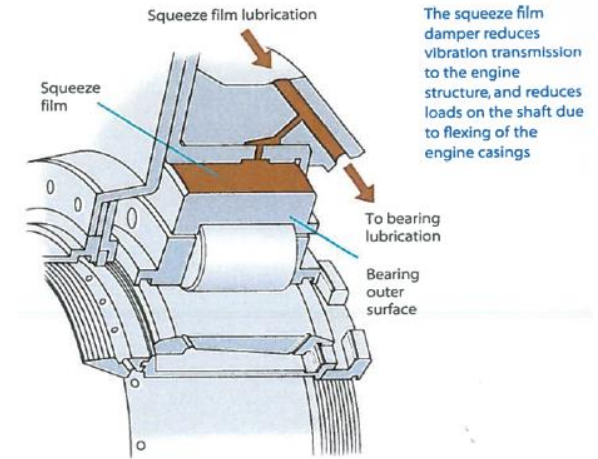
# High Speed Bearing Classes

- Rolling element bearings
- Magnetic bearings
- Fluid film bearings

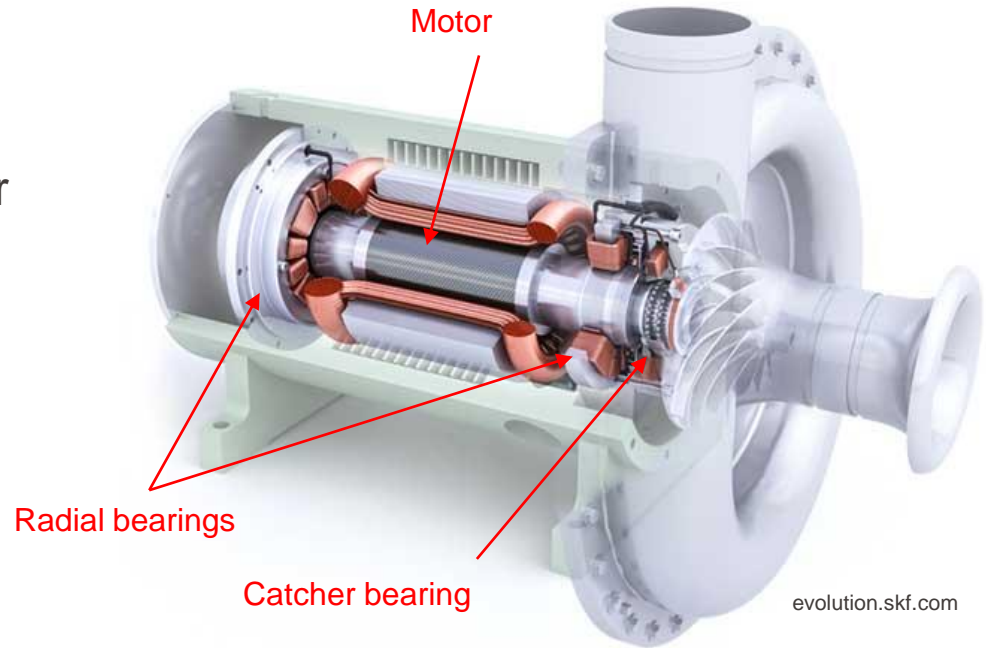




- Standardized and robust technology
- Needs controlled lubrication
- Offers little damping
- Limited lifetime at high speeds (inertial forces)

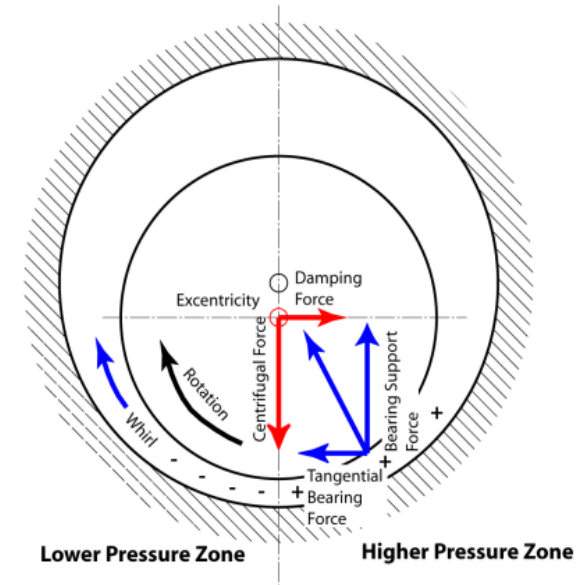


- No mechanical contact
- Work in vacuum
- Requires no lubrication
- Needs probes and controller
- Expensive and bulky
- Requires catcher bearings



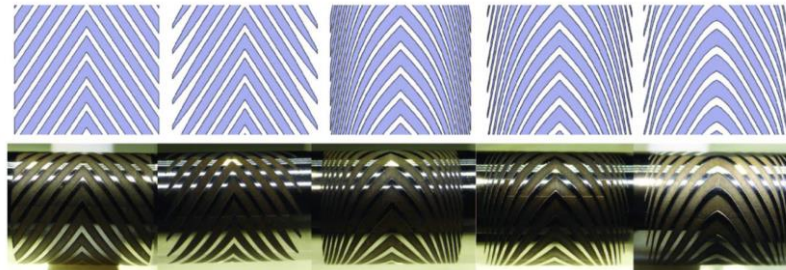
evolution.skf.com

- Compressible and incompressible lubricants
- Externally pressurized or dynamic
- Very simple geometry → ease of downscaling
- No wear after liftoff
- Low mechanical losses
- No cycle contamination
- Low specific load capacity and damping
- Rotordynamic stability issues



# Dynamic Gas Lubricated Bearings

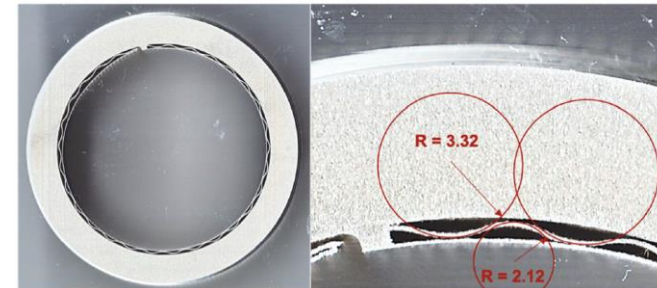
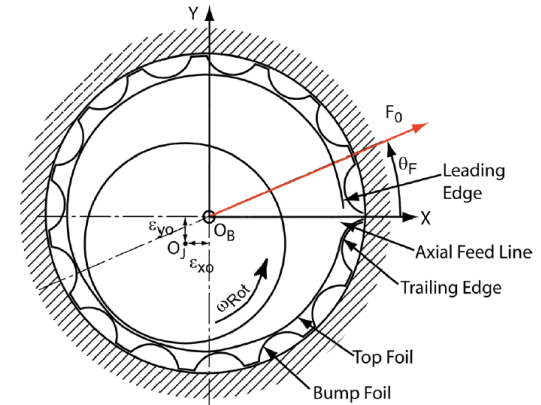
- Herringbone groove journal bearings
  - Rigid bearing bushings with v-shaped grooves
  - Tight clearances
  - Perfect alignment required
  - Accurate rotor position → low tip clearances possible
  - Very high stability threshold
  - Enhanced grooves suggested to improve performance



Bättig, P. K., Wagner, P. H., and Schiffmann, J. A. (March 18, 2022). "Experimental Investigation of Enhanced Grooves for Herringbone Grooved Journal Bearings." ASME. *J. Tribol.* September 2022; 144(9): 091801.

## ■ Foil bearings

- Soft support structure makes outer fluid film surface compliant
- Tolerant to misalignment and thermal gradients
- Friction between foils generates external damping
- Rotor needs large orbits to generate damping  
→ large tip clearances → large losses
- Highly non-linear behavior
- Prone to unstable behavior
- Repeatable and reproducible manufacturing challenging
- 3D-printable



Shalash, K., and Schiffmann, J. "Experimental Assessment of a 3D-Printed Stainless Steel Gas Foil Bearing." *ASME. J. Tribol.* August 2020; 142(8): 081802.

# Dynamic Gas Lubricated Bearings

- Tilting pad bearings
  - Composed of several pads, each with tilting degree of freedom
  - Tilting avoids cross-coupled stiffness → ultra-high stability
  - Lower load capacity
  - Expensive & time-consuming manufacturing
  - Complex dynamic behavior



<https://www.bearingsplus.com>



<https://www.bearingsplus.com>

# Proof of Concept Single Stage Compressor

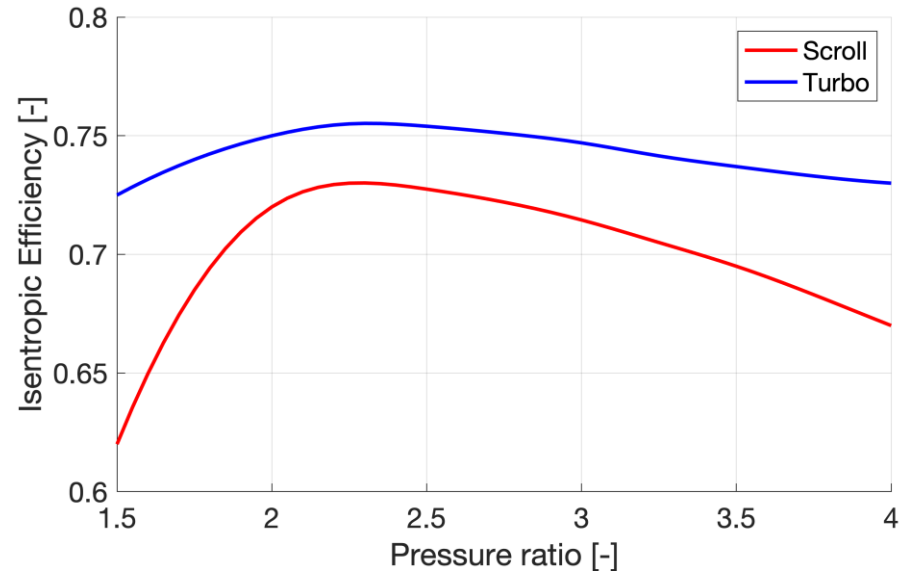
- Experimental demonstration of small-scale turbocompressor
  - $\varnothing 20$  mm impeller, 210 krpm, 2 kW,  $\Pi$  3.3,  $\eta_{IS-IT}$  0.8
  - Oil-free, R134a-lubricated bearings
  - Herringbone grooved journal bearings
  - Increased specific power compared to scroll (x10)
  - 500'000 stop & go





# Proof of Concept Comparison

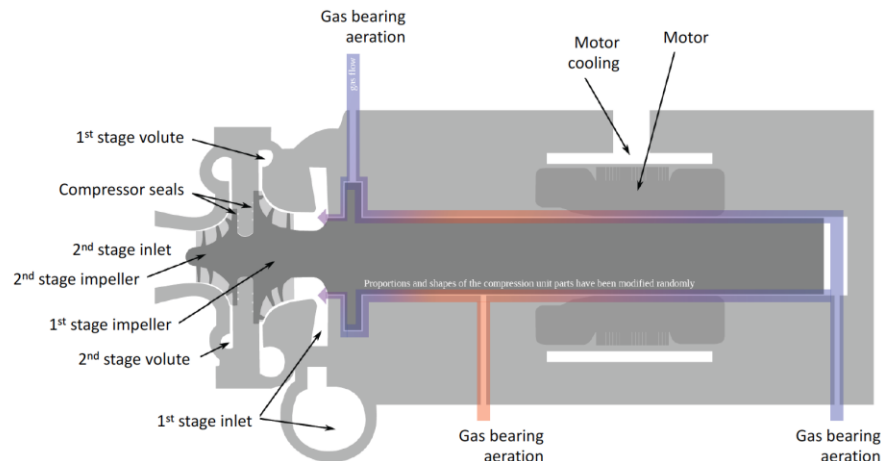
- Turbocompressor achieves higher peak efficiency than positive displacement compressor and improves off-design operation





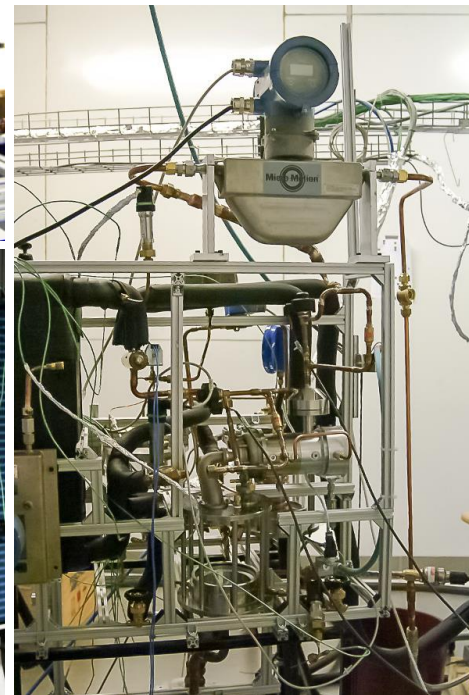
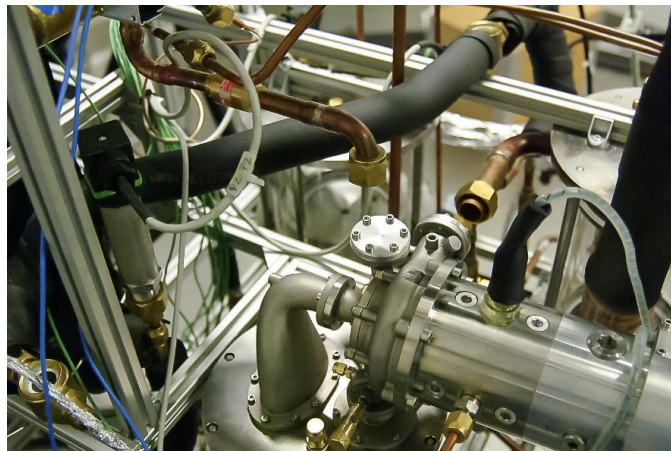
# Twin Stage Heat Pump Compressor

- Experimental investigation of twin stage turbocompressor for high temperature lift heat pumps
  - Both impellers on same rotor, 180 krpm, 6 kW
  - Oil-free, R134a-lubricated bearings



# Twin Stage Heat Pump Compressor

- Air-water heat pump
- Twin-stage cycle with open flash tank
- Challenging flash tank design
- Competitive performance a A-7W35

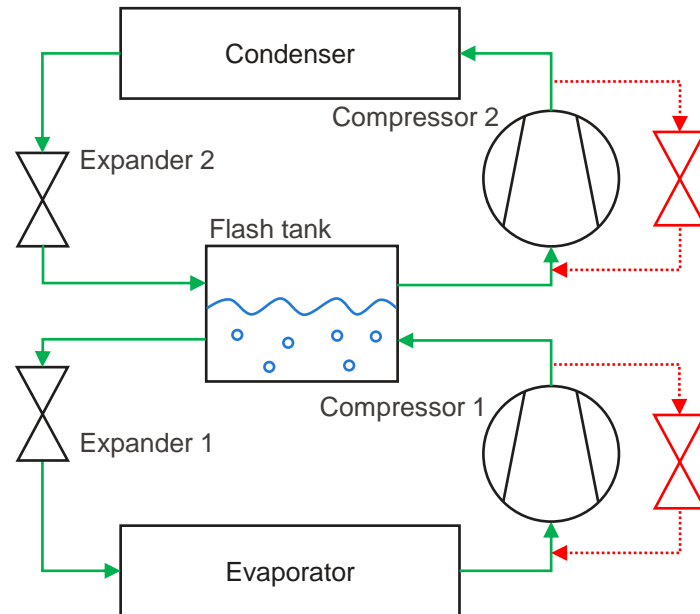


EPFL-Thesis 6764, Jean-Baptiste Carré,  
Experimental investigation of domestic  
heat pumps equipped with a twin-stage  
oil-free radial compressor

# Twin Stage Heat Pump Compressor

## Experimental Challenges

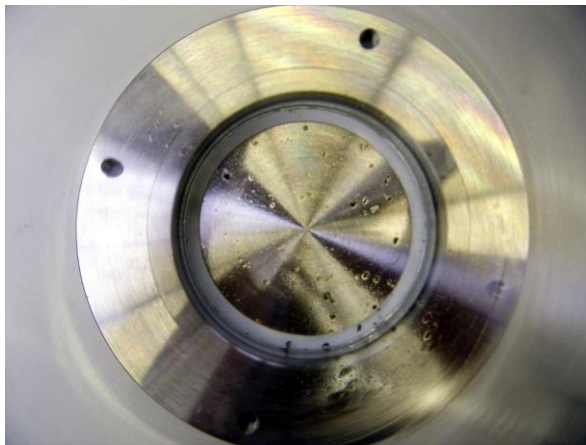
- Thrust forces & surge
  - Compressor surge perturbs the complete cycle
- Compressor by-pass required for hot start & stop to avoid compressor surge
- Additional safety for compressor



# Twin Stage Heat Pump Compressor

## Experimental Challenges

- Cycle pollution
  - Cycle contamination caused by heat exchanger and valve manufacturing process or polluted working fluid
  - Pollution may lead to bearing failure

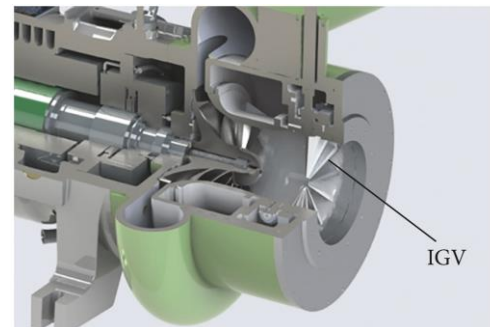


EPFL-Thesis 6764, Jean-Baptiste Carré,  
Experimental investigation of domestic  
heat pumps equipped with a twin-stage  
oil-free radial compressor

# Twin Stage Heat Pump Compressor

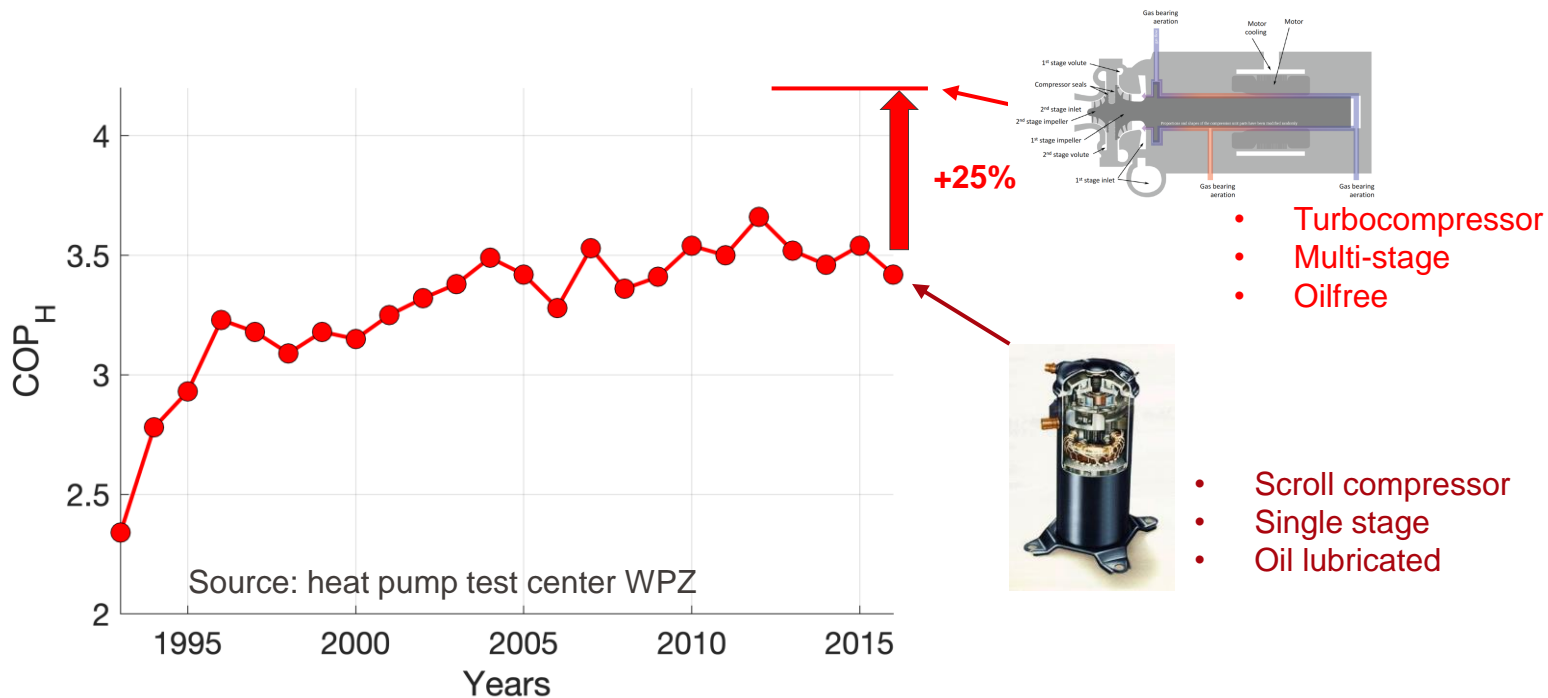
## Experimental Challenges

- Compressor map matching
  - Energy balance across economizer driven by mass-flow-ratio
  - Accurate compressor matching required to achieve stable economizer pressure
  - Additional control degree of freedom needed



Sun, Q., Ji, C., Fang, J., Li, C., Zhang, X., Optimization Design of IGV Profile in Centrifugal Compressor, *Mathematical Problems in Engineering*, 2017, 8437325, 9 pages, 2017

# Potential of Oilfree Turbochargers on COP



- Key question: can another step-change be achieved and if so, how?
- With multi-stage heat pump cycles driven by oilfree turbochargers



# Summary of Challenges of Reduced-Scale Turbomachinery

- Gas lubricated bearings require small clearances to achieve stable operation → manufacturing cost → industrialization challenging
- Low bearing clearances require clean working fluids
- Reduced scale compressors efficiency suffers from Re-number effects, increased relative surface roughness and large tip clearances
- Reduced scale turbomachinery more sensitive to heat fluxes
- Leakage between stages is increased due to scaling effects

- Heat exchanger design



- Comprehension questions
- Centrifugal compressor analysis
- Flow through a turbine runner