

Heat Pump Systems

Summary W10

Prof. J. Schiffmann

Radial Compressor Geometry

- Typical geometric features
 - Impeller tip width ratio

$$0.02 < b_4/r_4 < 0.2$$
 - Relative impeller tip clearance

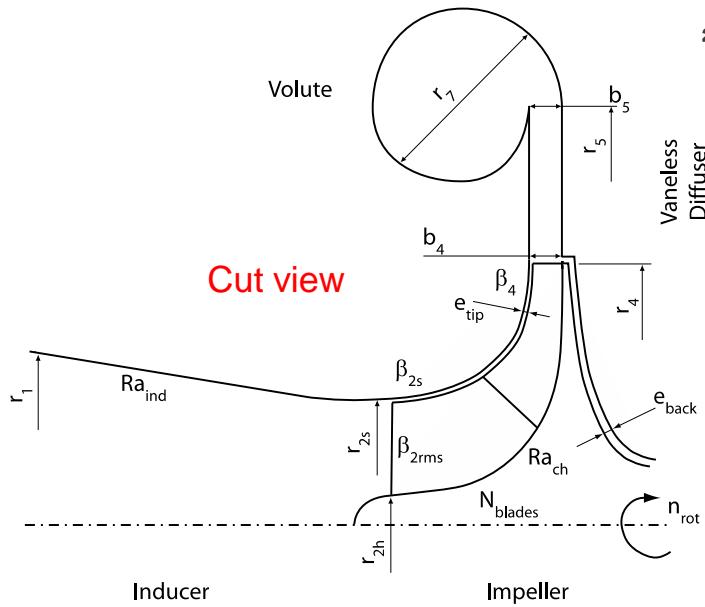
$$e_{tip}/b_4 < 0.05$$
 - Number of blades

$$12 < N_{blades} < 32$$
 - Axial length

$$L/r_4 \approx 0.35$$
 - Inlet diameter ratio

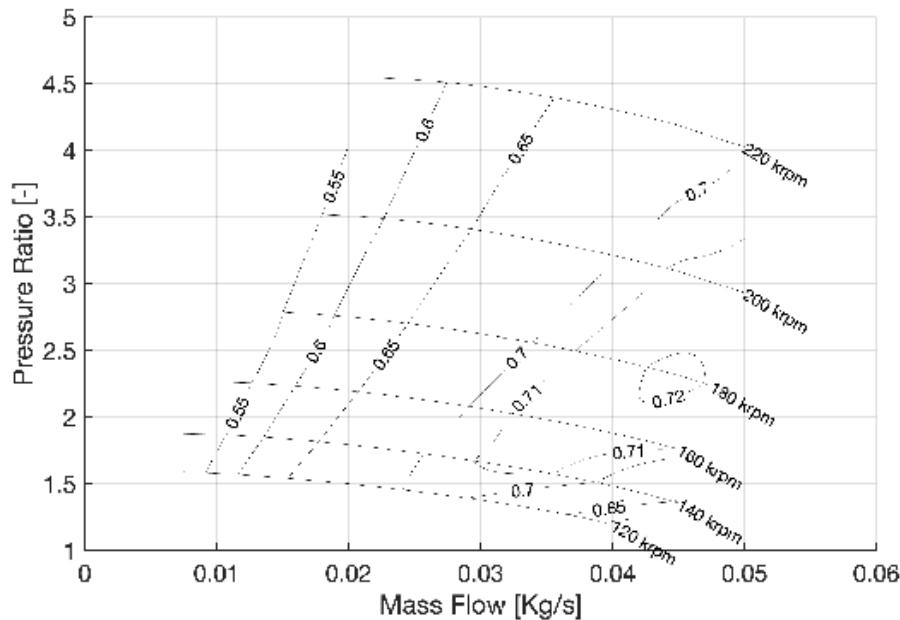
$$0.3 < r_{2s}/r_4 < 0.7$$
 - Blade angles

$$\beta_{2s} = -60^\circ \quad \beta_4 \approx -40^\circ$$



Typical Compressor Map

- Map limited towards lower mass flows by surge and towards higher mass by choke



- Choke defines upper mass flow for each speed line
 - Reducing back pressure increases velocity until it reaches the speed of sound in smallest passage
 - Further reduction in back pressure yields no increase in mass flow
 - Speed line is vertical after choking has occurred
 - Choking can occur at inlet, impeller, or diffuser
 - Higher speeds shift choke to higher mass flows until inlet is choked
 - Throat usually near impeller inlet or diffuser inlet

- Surge line marks the low flow limit of region of stable operation
 - Caused by increase in loading as mass flow is reduced (lower mass flow → increased incidence → increased loading → separation)
 - Depends on compressor itself & system configuration
- Instability can have several forms
 - Rotating Stall: separation in blade rows which jumps from one blade to next → mass flow nearly constant with small high-frequency pressure fluctuations
 - Mild Surge: Pulsations in mass flow and pressure without backflow
 - Deep Surge: Strong periodic backflow through compressor with large pressure and mass flow variations → should be avoided



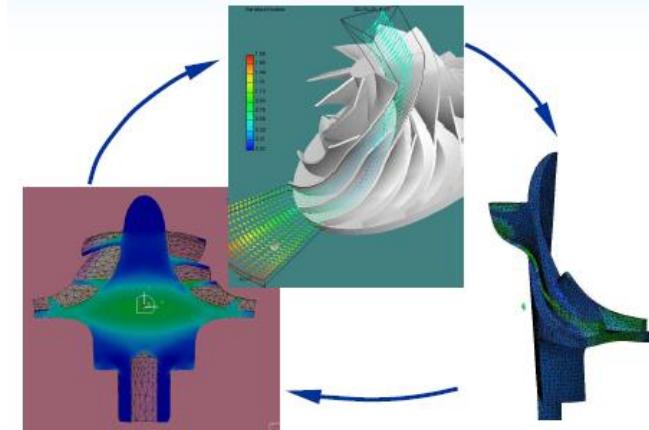
Heat Pump Systems

On the Modeling of
Centrifugal
Compressors

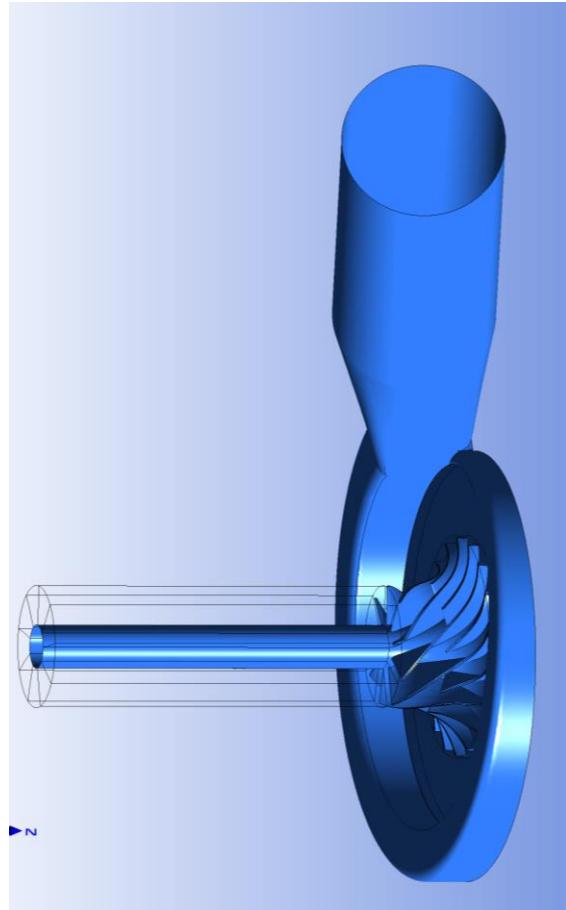
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Design Process of Turbomachinery

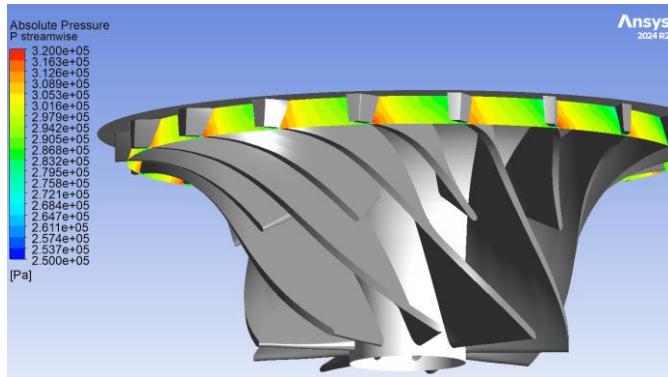
- Design of turbocompressor is interdisciplinary task
 - Aerodynamics
 - Mechanical stress
 - Dynamics
 - Thermal
- Flow in turbomachinery is highly complex



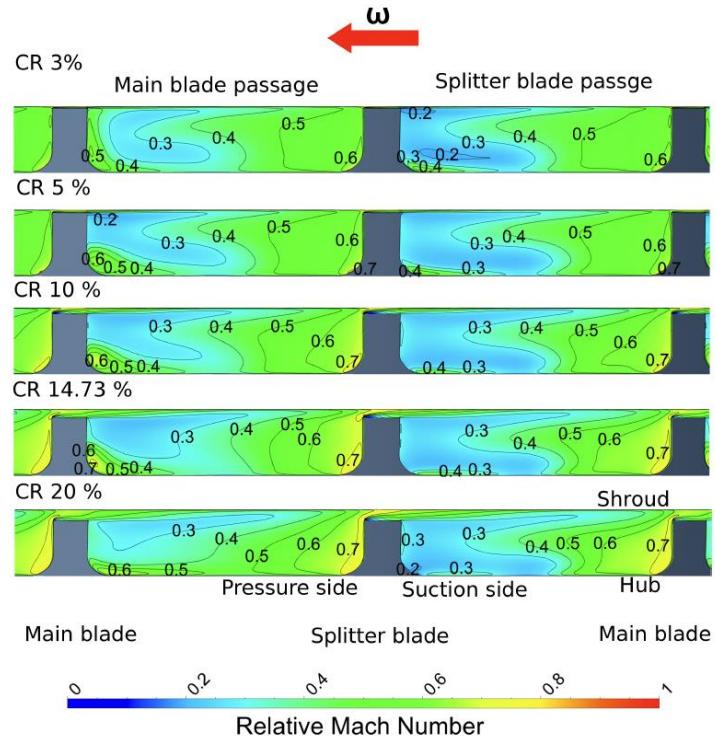
- Mesh of 30 million nodes
→ 15h computational time for one operating point → computational resources
- Not well suited for design



- Great for visualizing detailed flow features and analysis

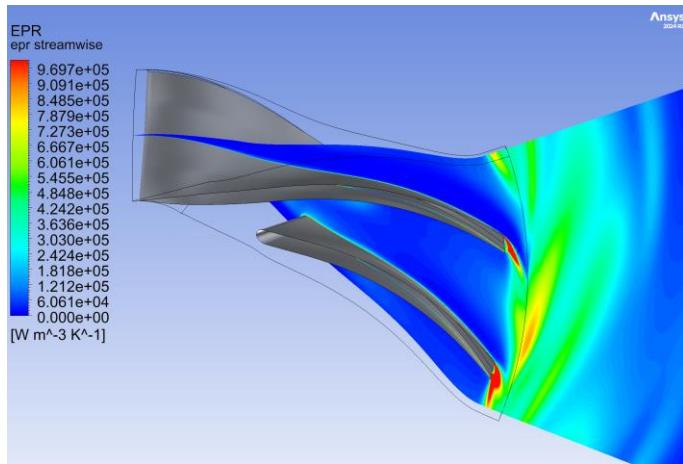


Pressure on pressure side larger than on suction side

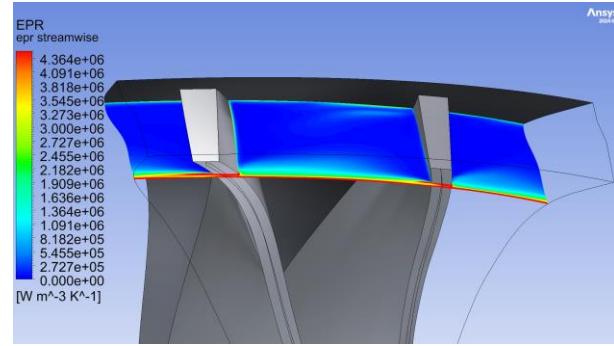


Accumulation of low momentum fluid close to suction side \rightarrow jet-wake pattern \rightarrow mixing losses into diffuser

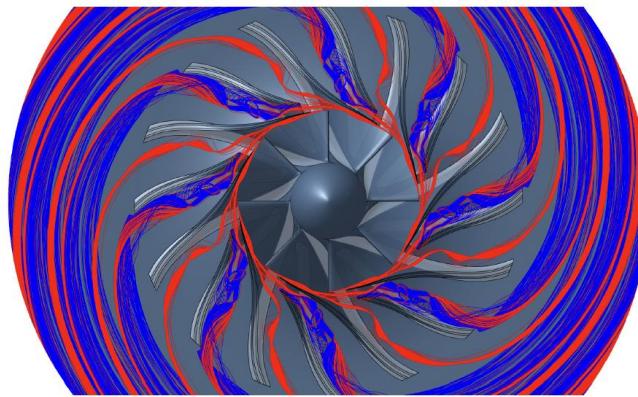
- Great for visualizing detailed flow features and analysis



Trailing edge mixing into diffuser



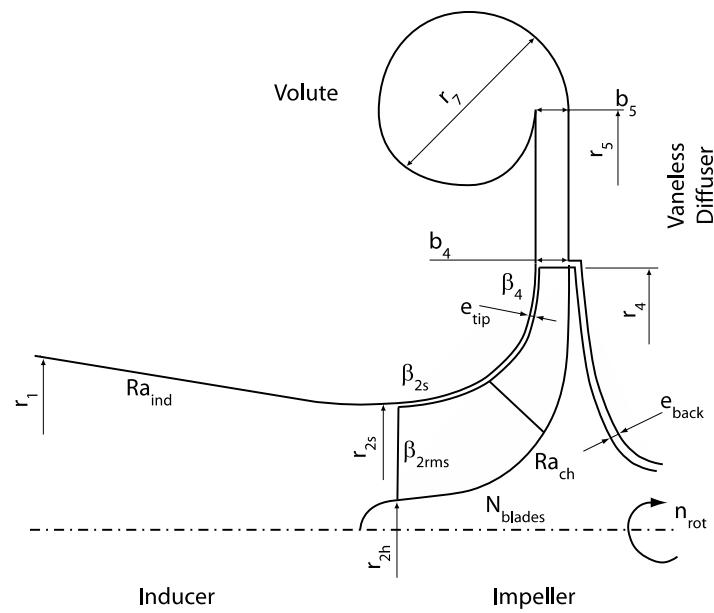
Entropy production rate highest in tip gap and on surfaces → skin friction



Trajectories of main (red streamlines) and splitter blade (blue streamlines) tip leakage vortices

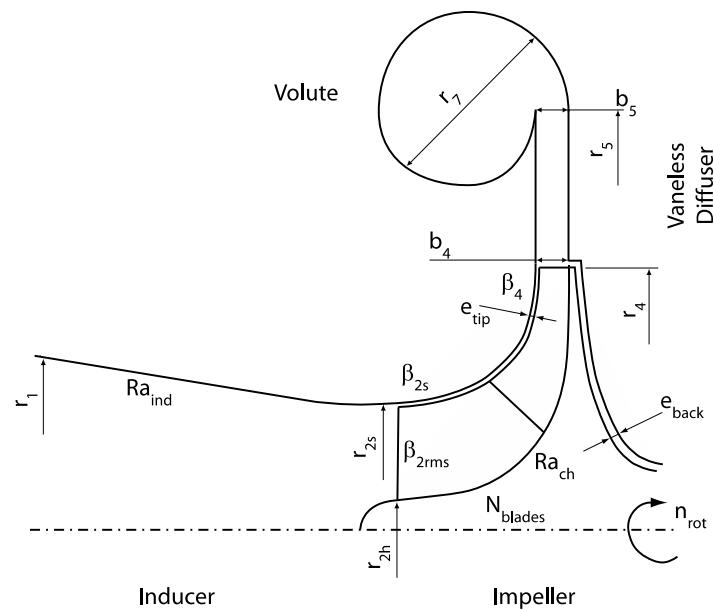
1D – Meanline Model

- Modeling along flow direction, component by component
- Based on velocity triangles, mass- & energy conservation, h-s-diagram
- Representation of losses through empirical correlations



- Proven Empirical Loss Correlations

- Skin Friction } Inducer
- Incidence } Impeller
- Skin Friction } Impeller
- Diffusion } Impeller
- Clearance } Impeller
- Disk friction } Impeller
- Recirculation } Impeller
- Skin Friction } Diffuser
- Trailing edge mixing } Diffuser



- Further effects
 - Slip \rightarrow flow does not follow blade angle \rightarrow causes a decrease in work input

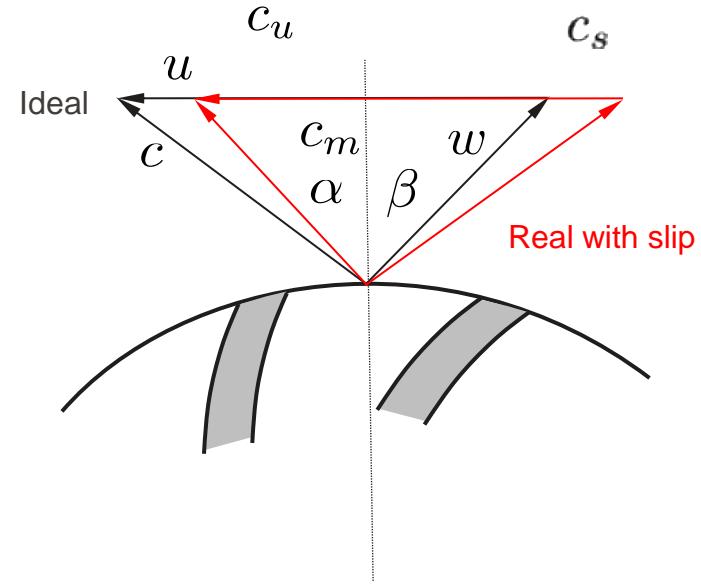
$$\frac{c_s}{u_4} = \frac{\sqrt{\cos \beta_{4bl}}}{N_{bl}^{0.7}}$$

- Aerodynamic blockage

$$B_i = A_{\text{eff}}/A_{\text{geom}}$$

- Surge in vaneless diffuser

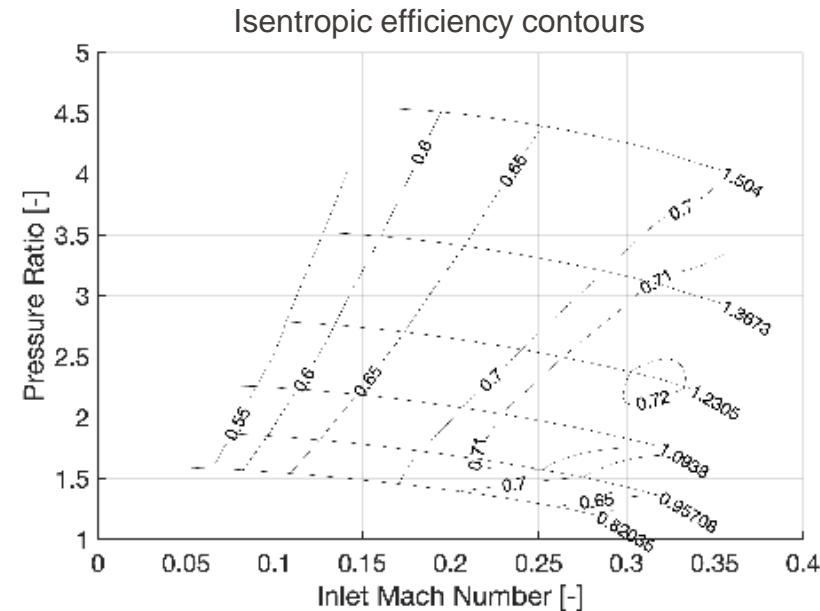
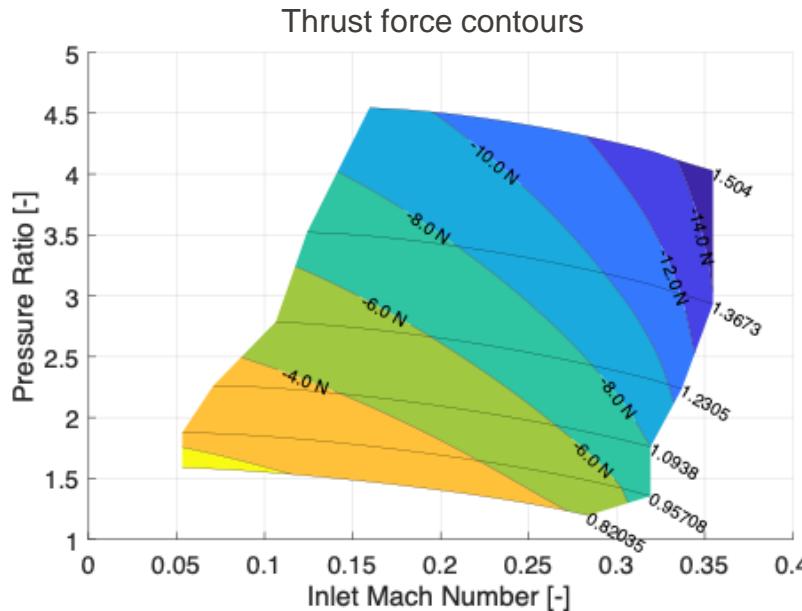
$$\alpha_{\text{crit}} = f(M_4, b_4/r_4, r_5/r_4)$$



1D – Meanline Model

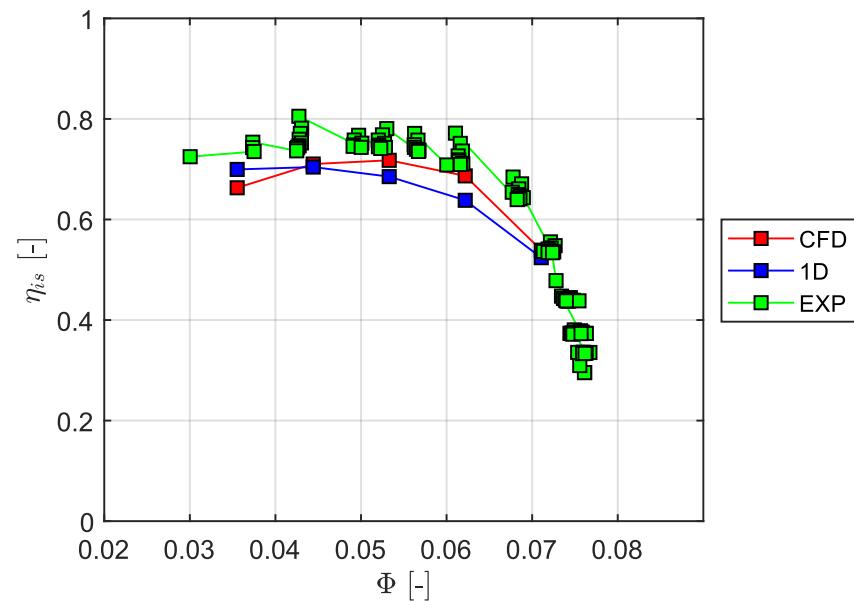
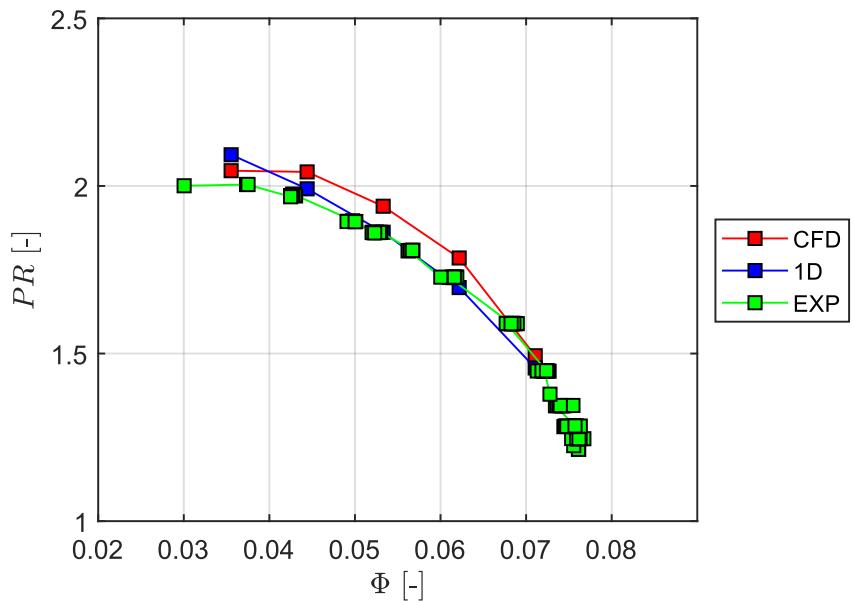
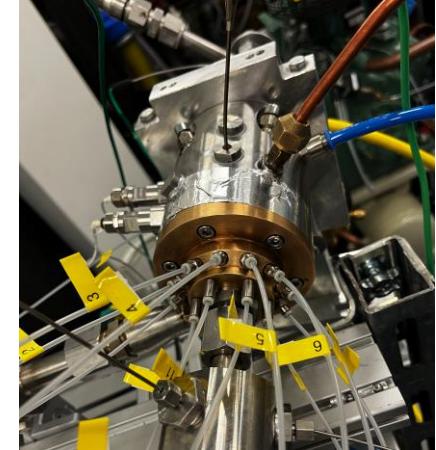
$$[PR, \eta_{is}, \text{surge}, \text{choke}] = f(\dot{m}, N_{rot}, P_{01}, T_{01}, \text{Fluid}, \text{Geom})$$

- Fast compressor map prediction → great for design
- No capturing of 3D flow patterns



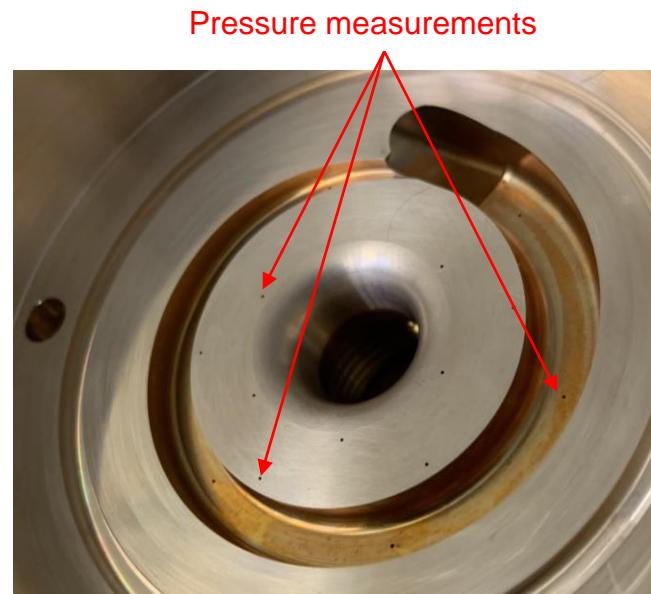
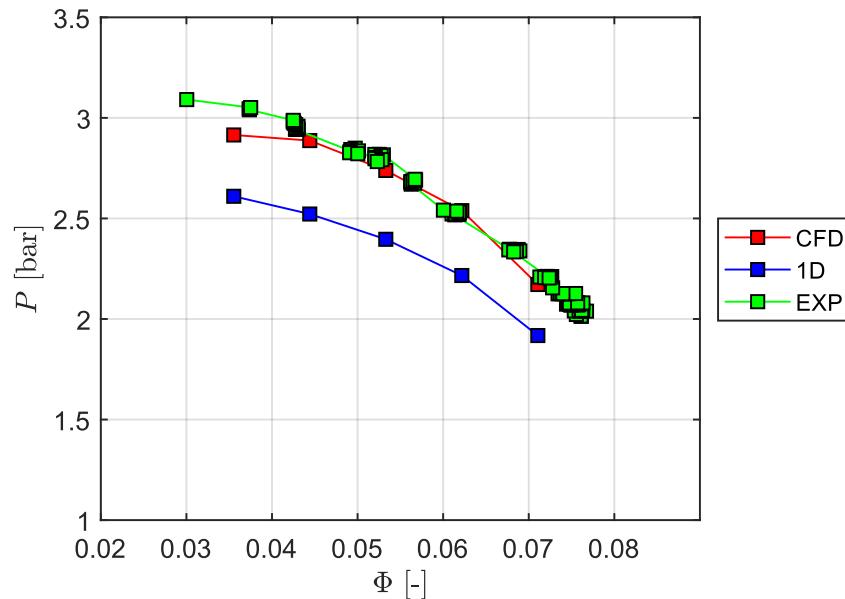
Comparison CFD – Meanline Model

- Excellent overall (out-in) agreement between experimental data, CFD, and meanline-model

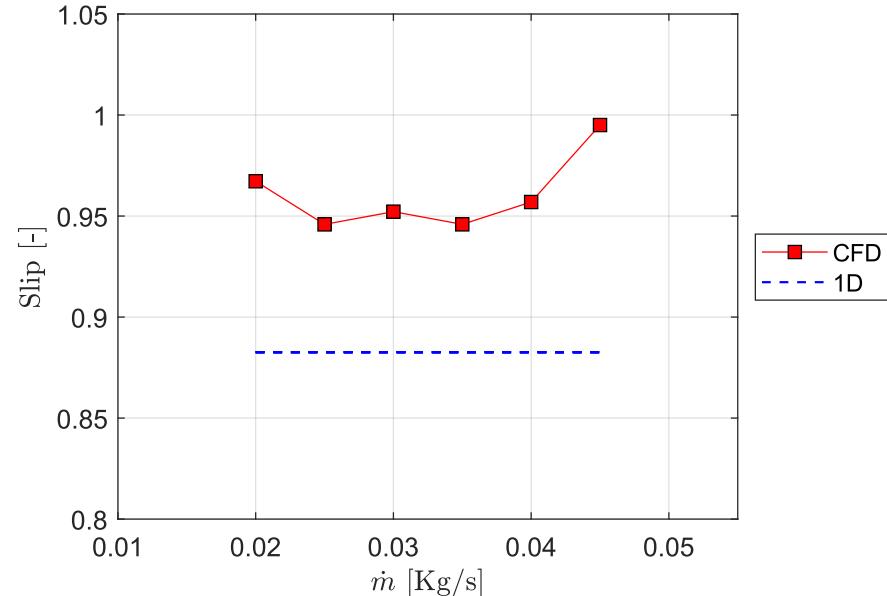
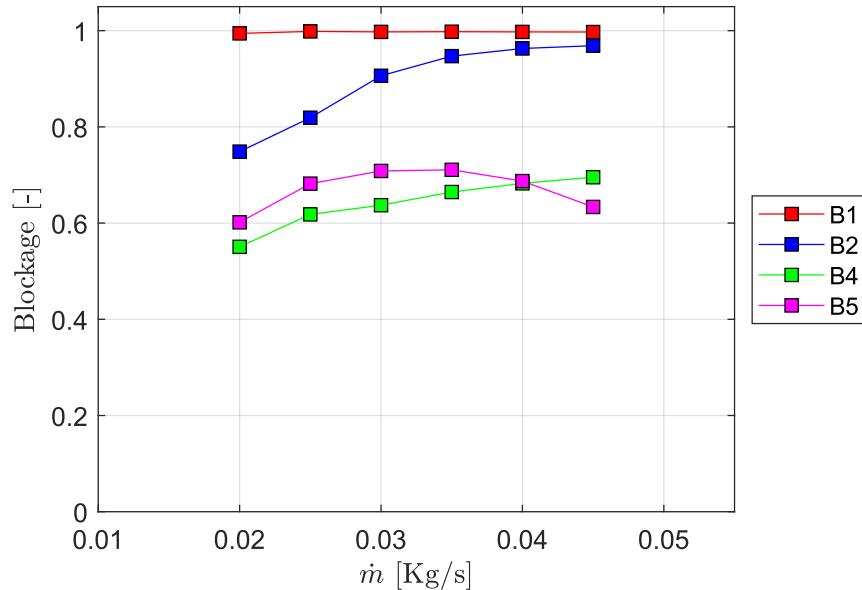


Comparison CFD – Meanline Model

- Inconsistency between meanline model, CFD & experiments at component level Impeller pressure ratio

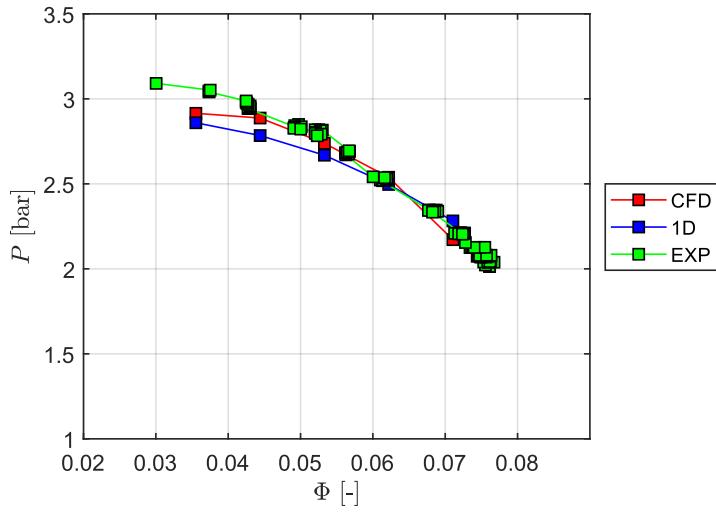
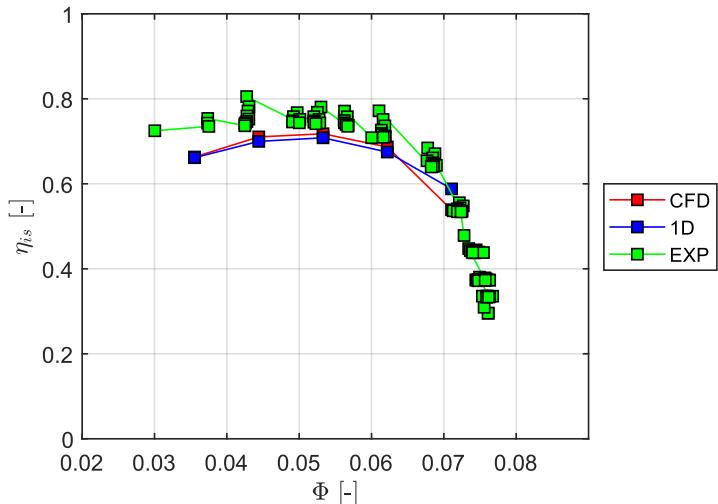


- Correction of aerodynamic blockage factors, slip, and losses based on CFD data

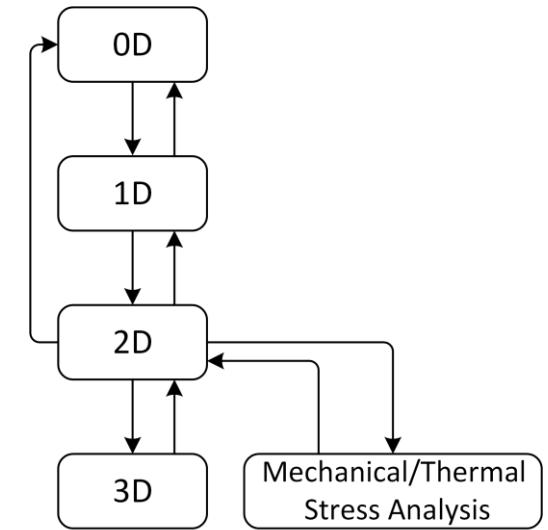


Calibrated Meanline Model

- Good agreement at a component level and overall
- Meanline models are very efficient but may need calibration



- Iterative combination of increasingly complex models
 - 0D: Overall dimensions – based on empirical performance maps
 - 1D: Details of inlet and exhaust areas → meanline model
 - 2D: Definition of blade geometry
 - 3D: Assessment of detailed flow patterns
- Accurate starting point (0D) key for efficient design process
 - Requires design maps



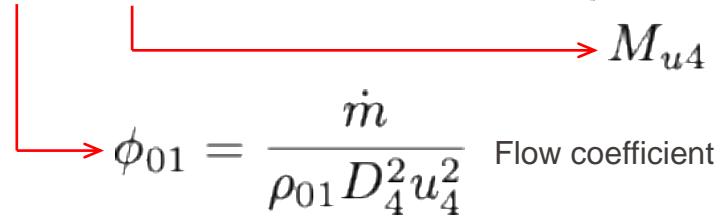
- Parameters influencing compressor performance

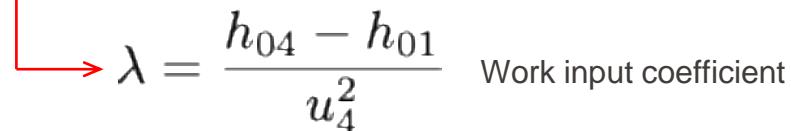
$$[PR, \eta_{is}, \text{surge, choke}] = f(\dot{m}, N_{rot}, P_{01}, T_{01}, \text{Fluid, Geom})$$

- Using dimensional analysis

$$[\lambda, \eta_{is}] = f(\phi_{01}, M_{u4}, Re, \text{Fluid, Geom})$$


$$M_{u4} = \frac{u_4}{a_{01}} \text{ Machine Mach number}$$


$$\phi_{01} = \frac{\dot{m}}{\rho_{01} D_4^2 u_4^2} \text{ Flow coefficient}$$

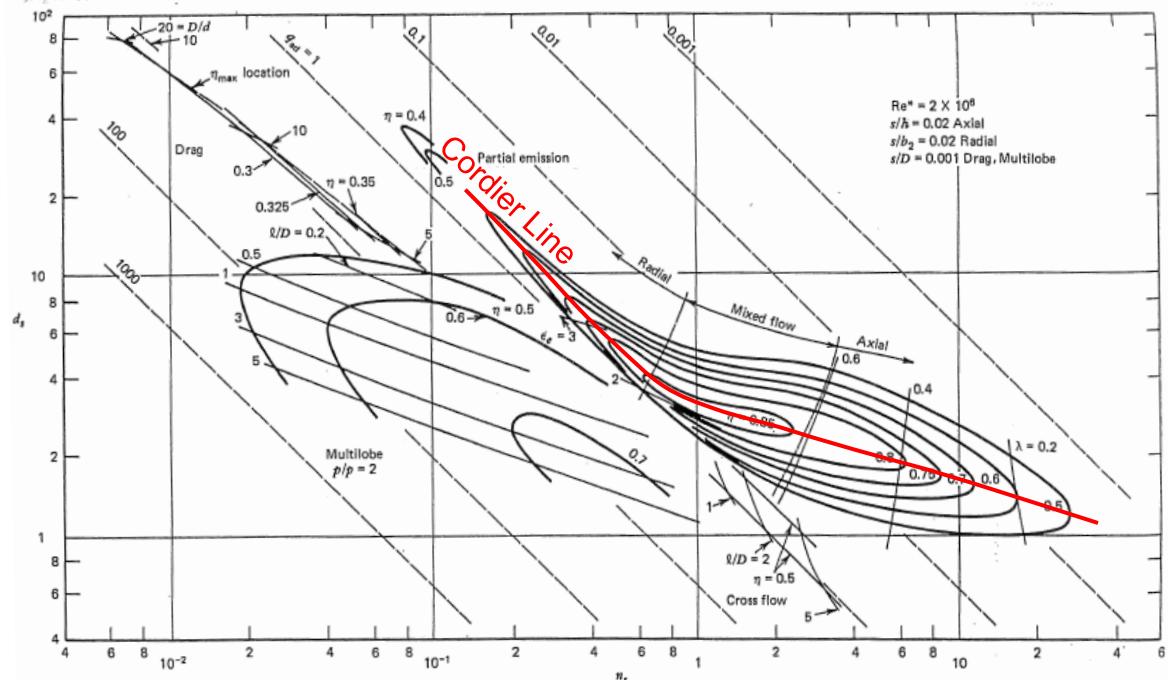

$$\lambda = \frac{h_{04} - h_{01}}{u_4^2} \text{ Work input coefficient}$$

Compressor Design Maps

- Specific speed and diameter alternative set of dimensionless parameters

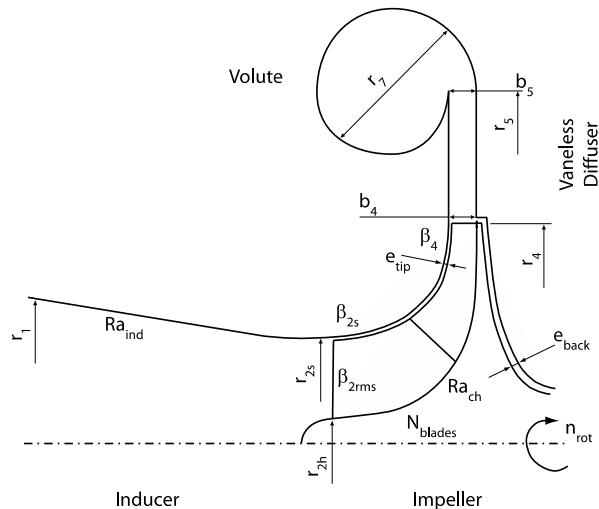
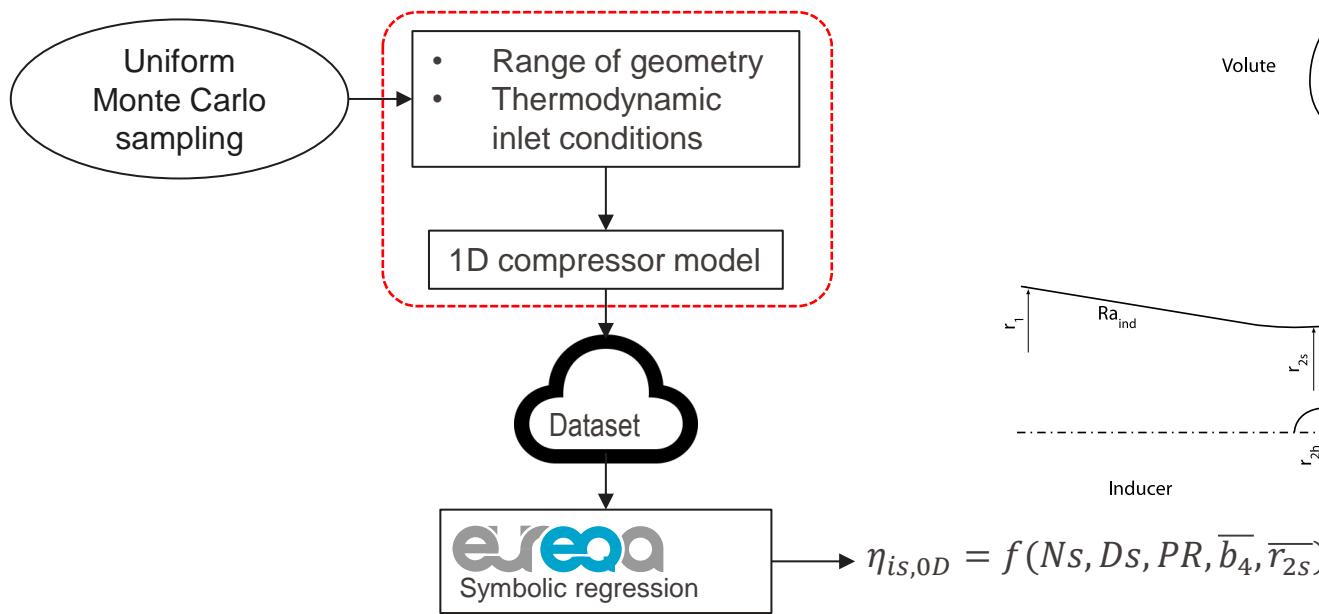
$$n_s = \omega \frac{\dot{V}_{01}^{0.5}}{\Delta h_{is}^{0.75}}$$

$$d_s = d_4 \frac{\Delta h_{is}^{0.25}}{\dot{V}_{01}^{0.5}}$$



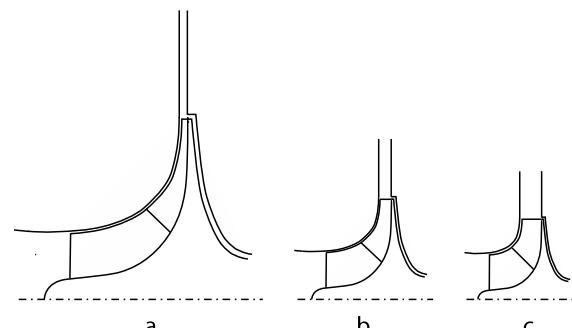
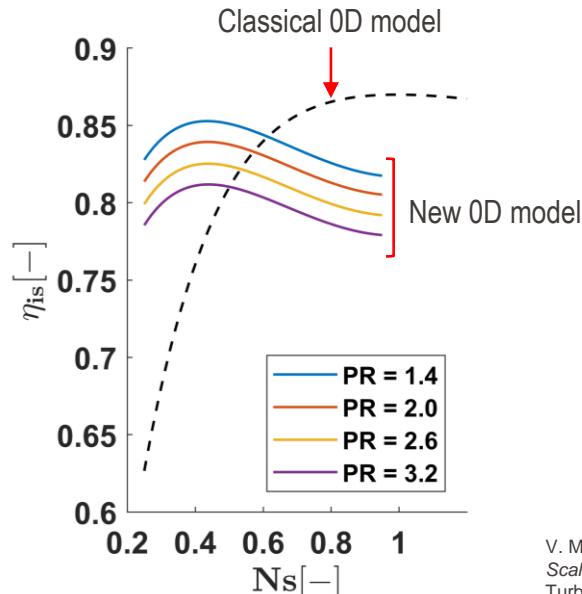
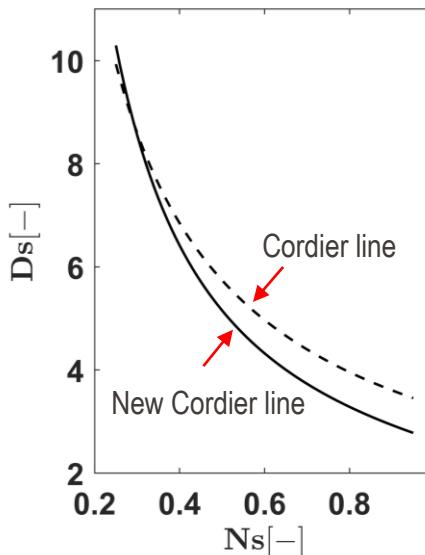
Updated Compressor Design Maps

- Experimentally validated tool used to generate surrogate model



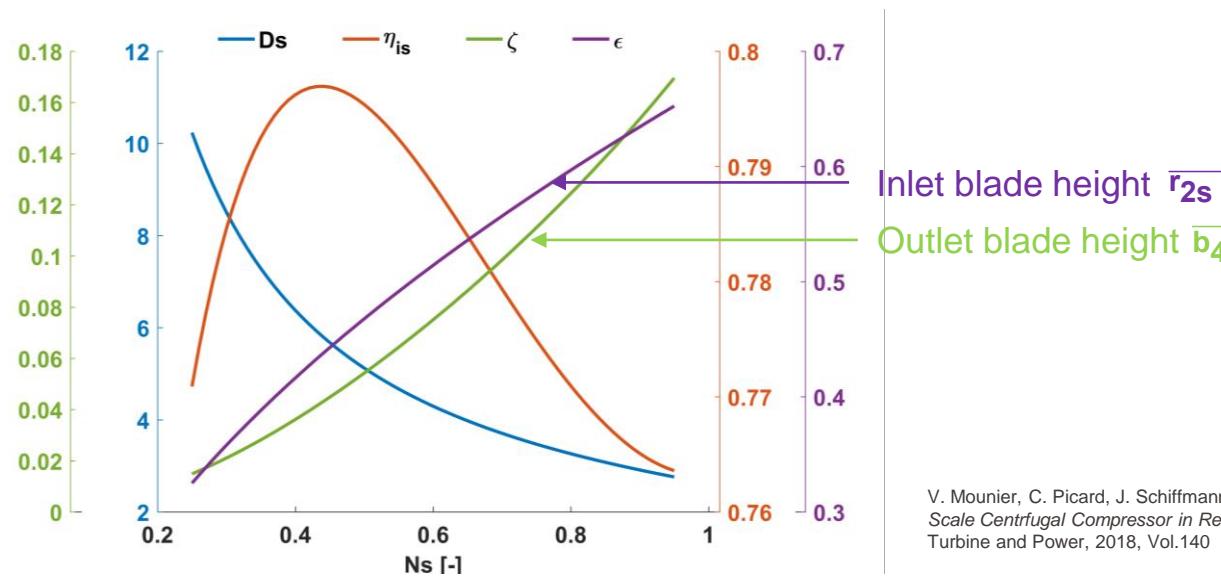
Updated Design Maps

- Updated model for reduced scale compressors deviates from literature
- New model includes additional design variables → more information

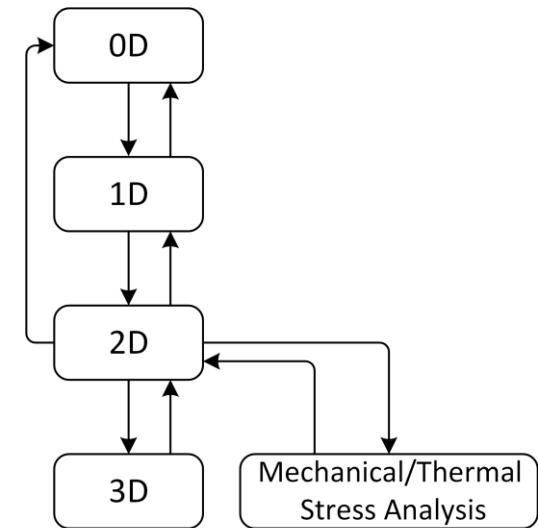


Impact of Updated Design Maps

- Compared to classical tools new model yields more design information
- Data driven tool improves starting point and bypasses 1D design loop
- New tool is 1'500 x faster than meanline model with similar accuracy



- Design of radial compressor is iterative process
- Involves aerodynamic, mechanical, and thermal aspects
- Design starts with “first guess” and evolves by engaging increasingly complex models
- Research efforts
 - Improve meanline models
 - Increase speed of high-fidelity models
 - Surge prediction
 - Behavior of turbomachinery at small scale

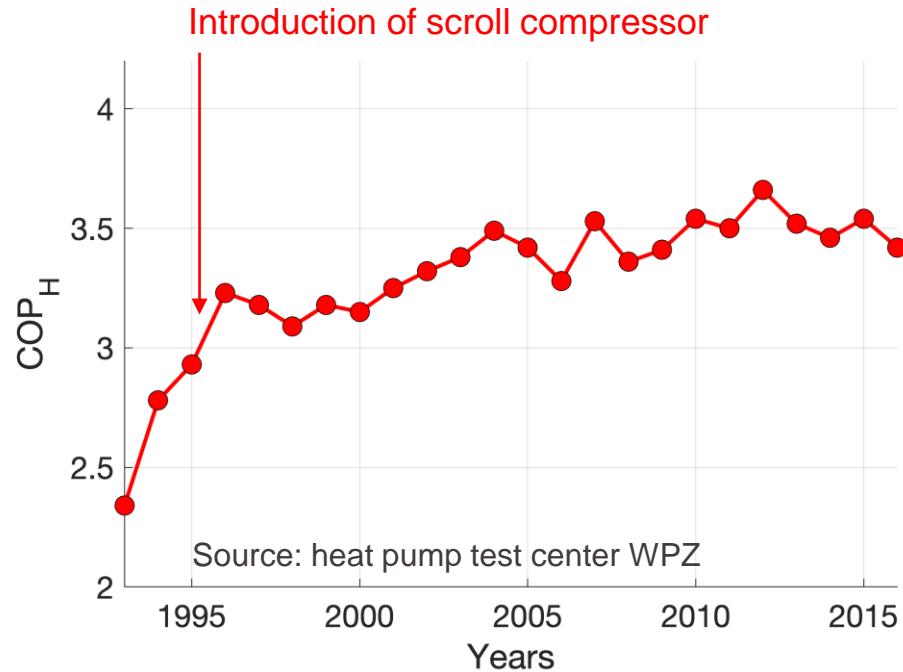


Heat Pump Systems

On Small-Scale
Turbocompressors
for Heat Pumps

Prof. J. Schiffmann

Historic Evolution of COP Trends

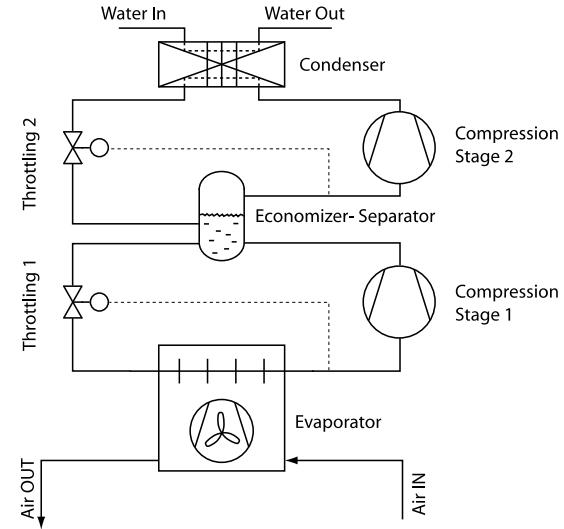


$$COP_H = \frac{q_h^-}{e^+}$$

- Since introduction of scroll compressors, COP has been rising slowly
- Key question: can another step-change be achieved and if so, how?

Key Challenges

- Assessment of losses in heat pump cycles
 - Compression 50%
 - Expansion 30%
 - Heat transfer 20%
- Possible ways to reduce losses
 - Increase compressor efficiency
 - Use oil-free technology
 - Implement multistage cycles
- Potential enabler
 - Turbocompressors on oil-free bearings

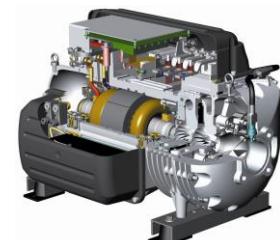
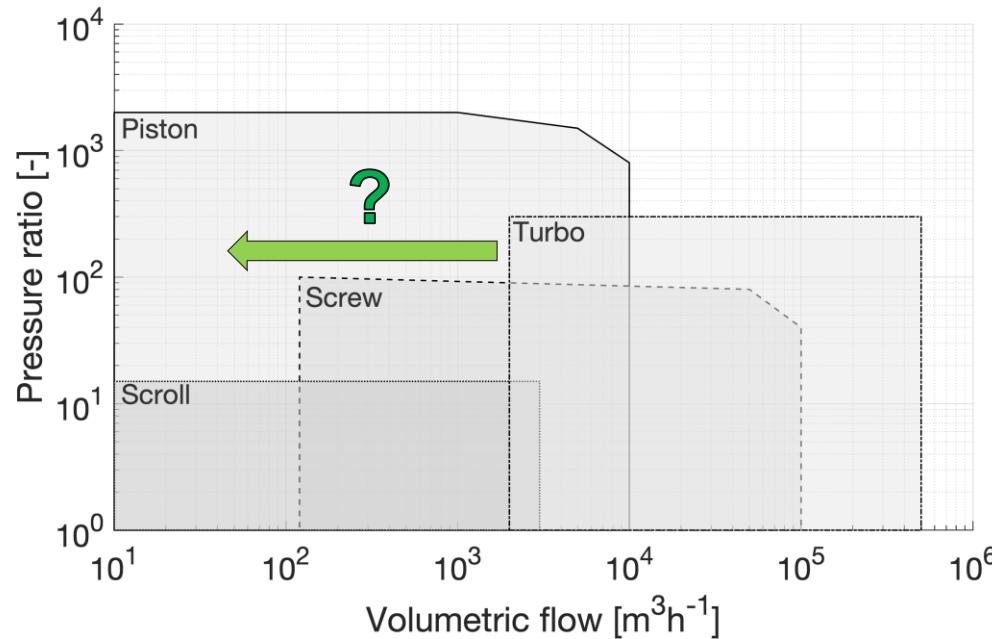


Compressor Technology Selection

- Positive displacement machines preferred for small capacity, dynamic compressors traditionally for high capacities

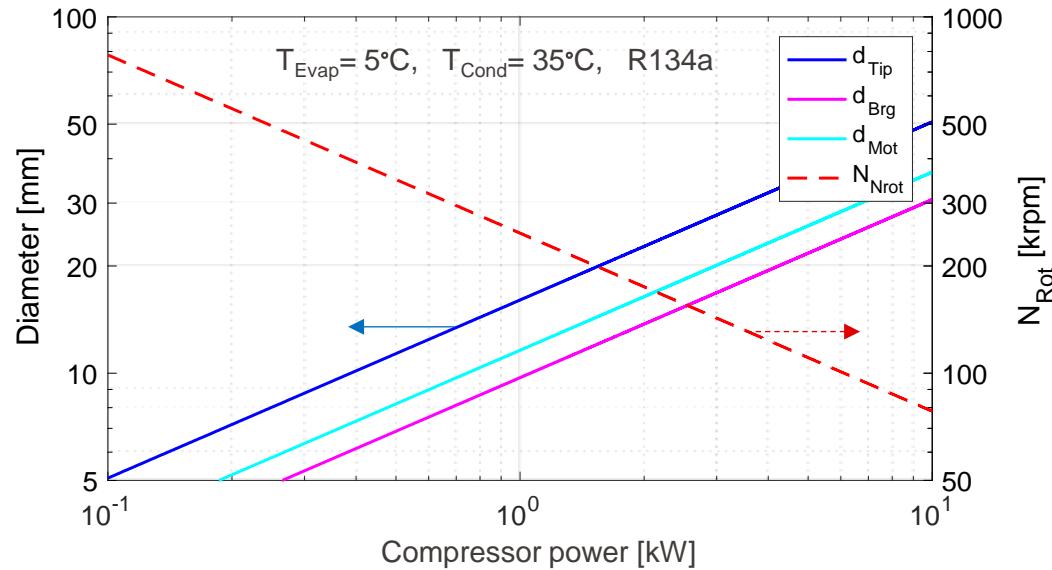


atlascopco.ch

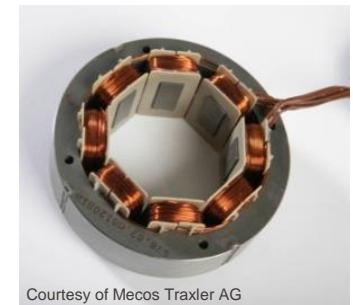


turbocor.com

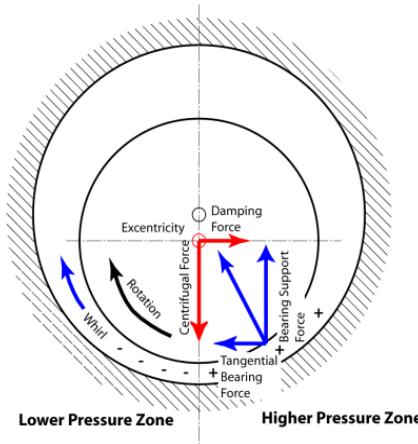
- Downscaling power increases N_{Rot} and decreases size
 - Constant tip speeds → no mechanical issues
- Aerodynamic challenges
 - Increased friction due to lower Re-number and higher roughness
 - Larger relative tip-clearance
 - Non-adiabatic operation
- Bearings
 - Need to support high speed and high lifetime



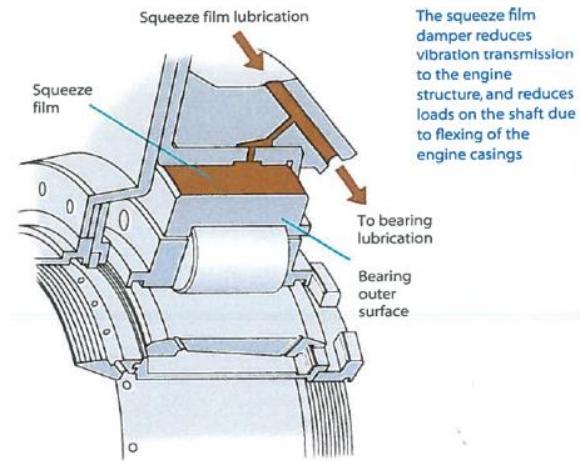
- Rolling element bearings
- Magnetic bearings
- Fluid film bearings



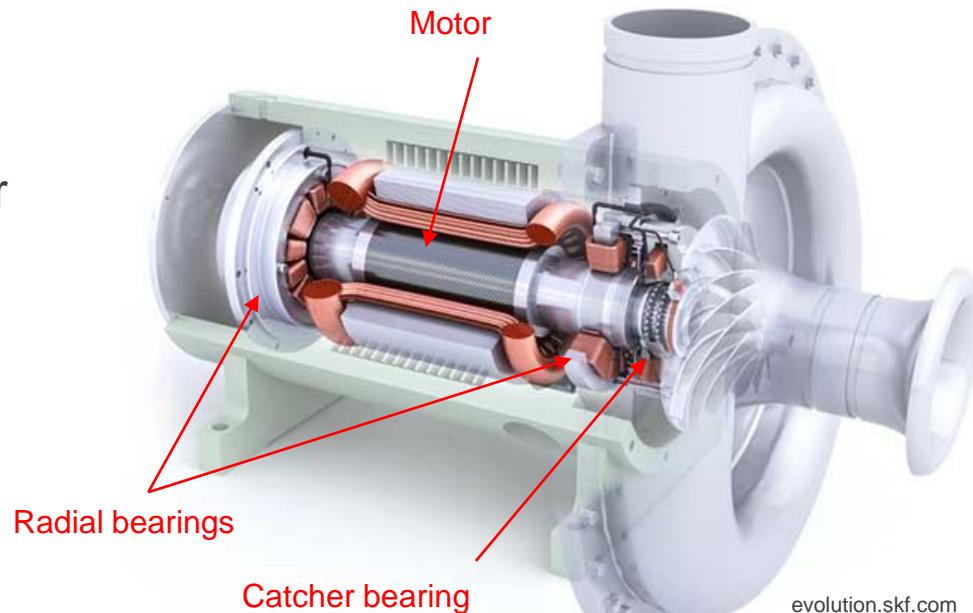
Courtesy of Mecos Traxler AG



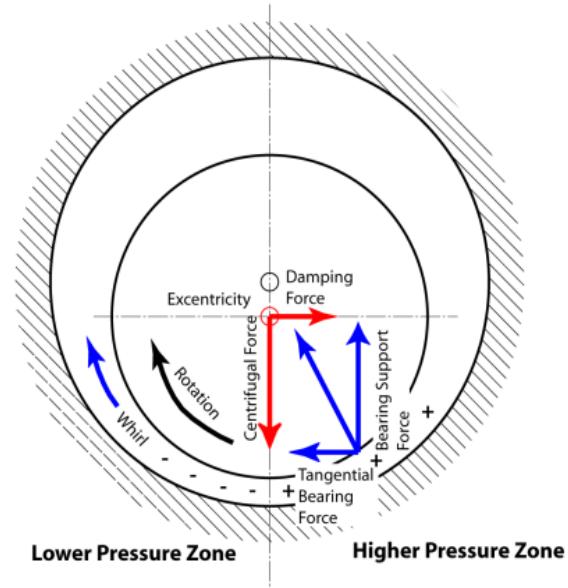
- Standardized and robust technology
- Needs controlled lubrication
- Offers little damping
- Limited lifetime at high speeds (inertial forces)



- No mechanical contact
- Work in vacuum
- Requires no lubrication
- Needs probes and controller
- Expensive and bulky
- Requires catcher bearings



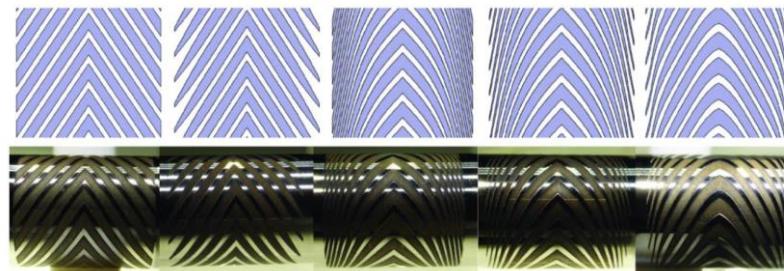
- Compressible and incompressible lubricants
- Externally pressurized or dynamic
- Very simple geometry → ease of downscaling
- No wear after liftoff
- Low mechanical losses
- No cycle contamination
- Low specific load capacity and damping
- Rotordynamic stability issues



- Herringbone groove journal bearings
 - Rigid bearing bushings with v-shaped grooves
 - Tight clearances
 - Perfect alignment required
 - Accurate rotor position → low tip clearances possible
 - Very high stability threshold
 - Enhanced grooves suggested to improve performance



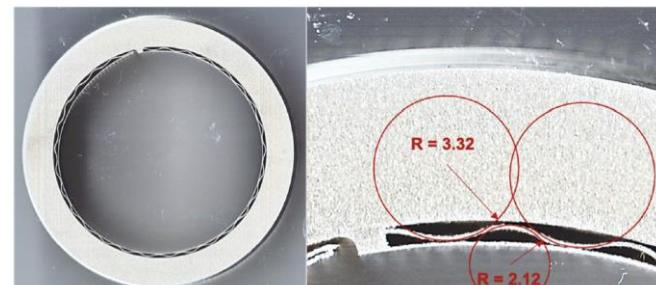
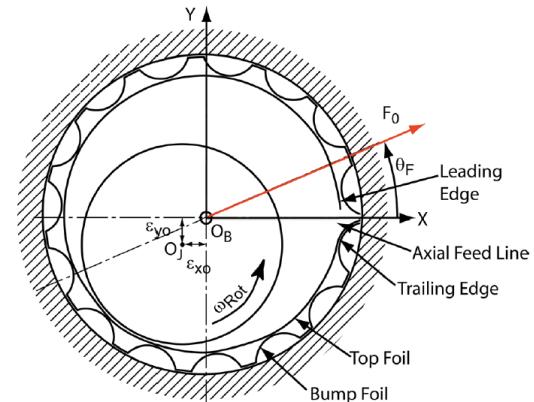
www.epfl.ch



Bättig, P. K., Wagner, P. H., and Schiffmann, J. A. (March 18, 2022). "Experimental Investigation of Enhanced Grooves for Herringbone Grooved Journal Bearings." *ASME. J. Tribol.* September 2022; 144(9): 091801.

- **Foil bearings**

- Soft support structure makes outer fluid film surface compliant
- Tolerant to misalignment and thermal gradients
- Friction between foils generates external damping
- Rotor needs large orbits to generate damping
→ large tip clearances → large losses
- Highly non-linear behavior
- Prone to unstable behavior
- Repeatable and reproducible manufacturing challenging
- 3D-printable



Shalash, K., and Schiffmann, J. "Experimental Assessment of a 3D-Printed Stainless Steel Gas Foil Bearing." ASME. J. Tribol. August 2020; 142(8): 081802.

- Tilting pad bearings

- Composed of several pads, each with tilting degree of freedom
- Tilting avoids cross-coupled stiffness → ultra-high stability
- Lower load capacity
- Expensive & time-consuming manufacturing
- Complex dynamic behavior



Proof of Concept

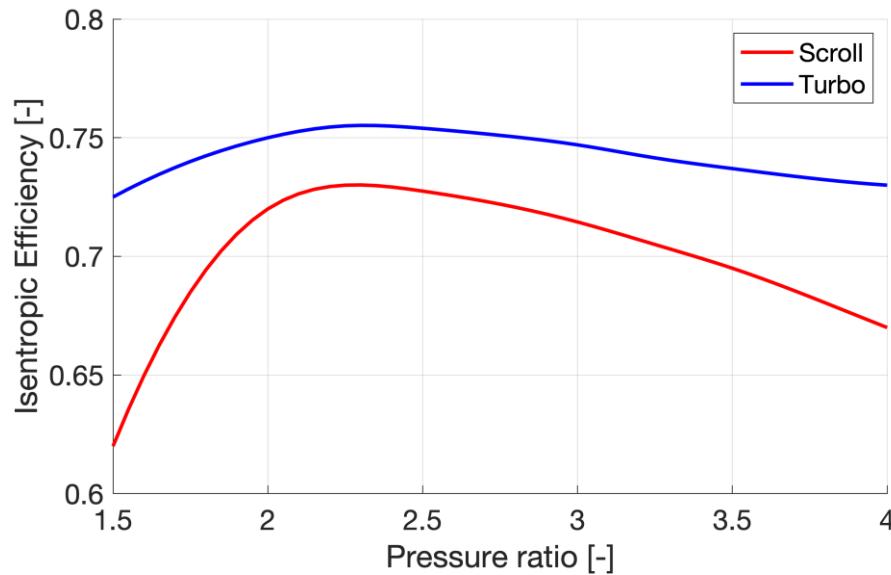
Single Stage Compressor

- Experimental demonstration of small-scale turbocompressor
 - Ø20 mm impeller, 210 krpm, 2 kW, Π 3.3, η_{IS-TT} 0.8
 - Oil-free, R134a-lubricated bearings
 - Herringbone grooved journal bearings
 - Increased specific power compared to scroll (x10)
 - 500'000 stop & go



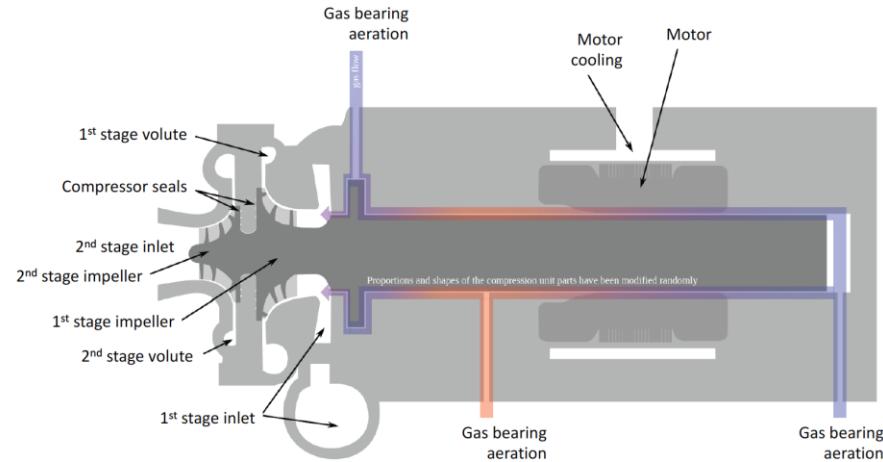
Proof of Concept Comparison

- Turbocompressor achieves higher peak efficiency than positive displacement compressor and improves off-design operation



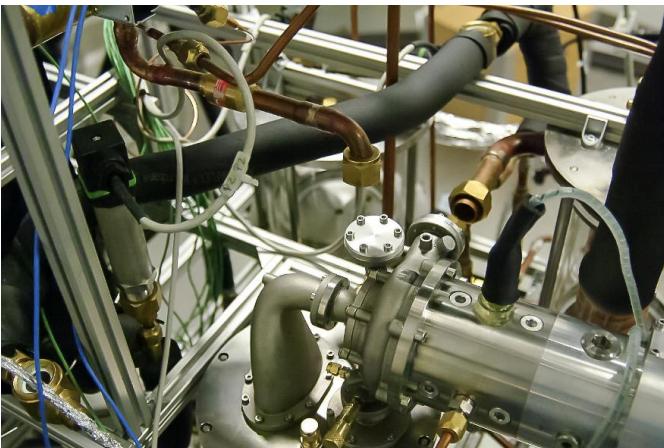
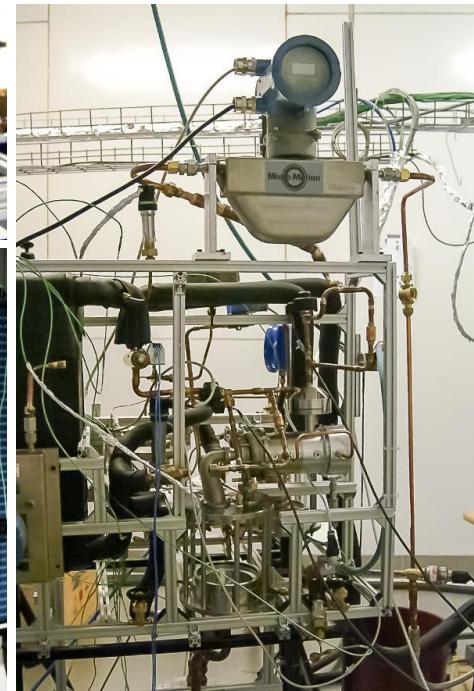
Twin Stage Heat Pump Compressor

- Experimental investigation of twin stage turbocompressor for high temperature lift heat pumps
 - Both impellers on same rotor, 180 krpm, 6 kW
 - Oil-free, R134a-lubricated bearings



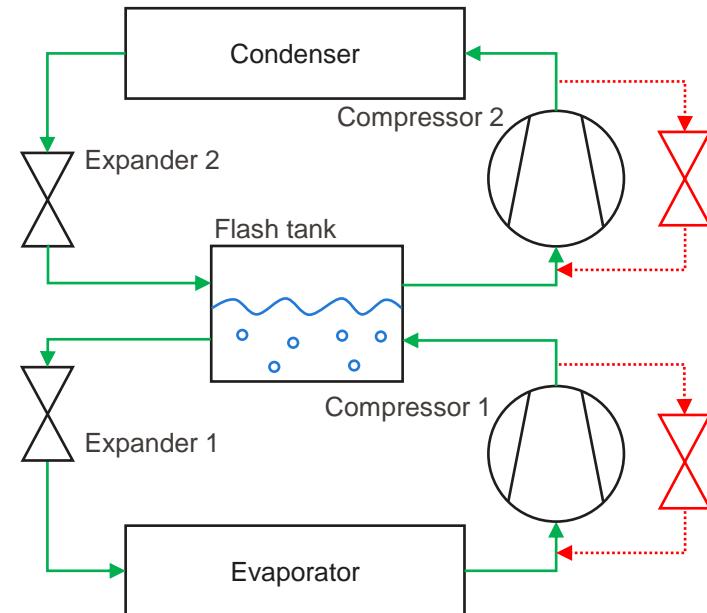
Twin Stage Heat Pump Compressor

- Air-water heat pump
- Twin-sage cycle with open flash tank
- Challenging flash tank design
- Competitive performance a A-7W35



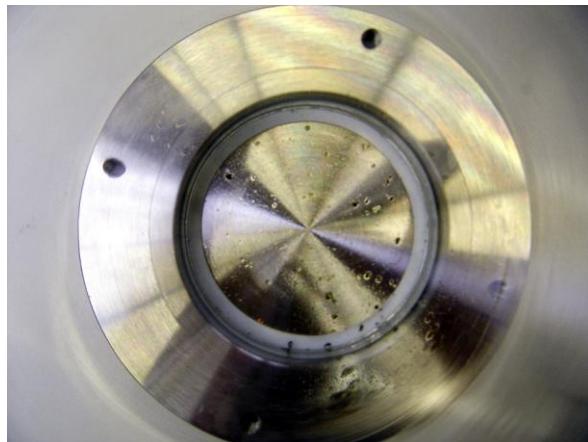
Twin Stage Heat Pump Compressor Experimental Challenges

- Thrust forces & surge
 - Compressor surge perturbs the complete cycle
 - Compressor by-pass required for hot start & stop to avoid compressor surge
 - Additional safety for compressor



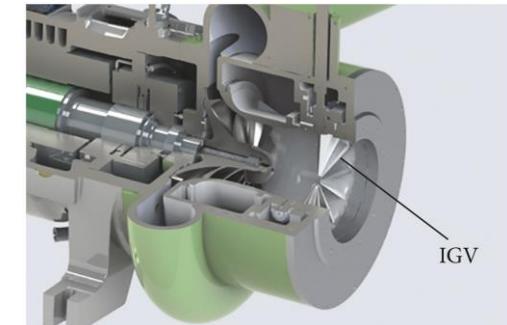
Twin Stage Heat Pump Compressor Experimental Challenges

- Cycle pollution
 - Cycle contamination caused by heat exchanger and valve manufacturing process or polluted working fluid
 - Pollution may lead to bearing failure



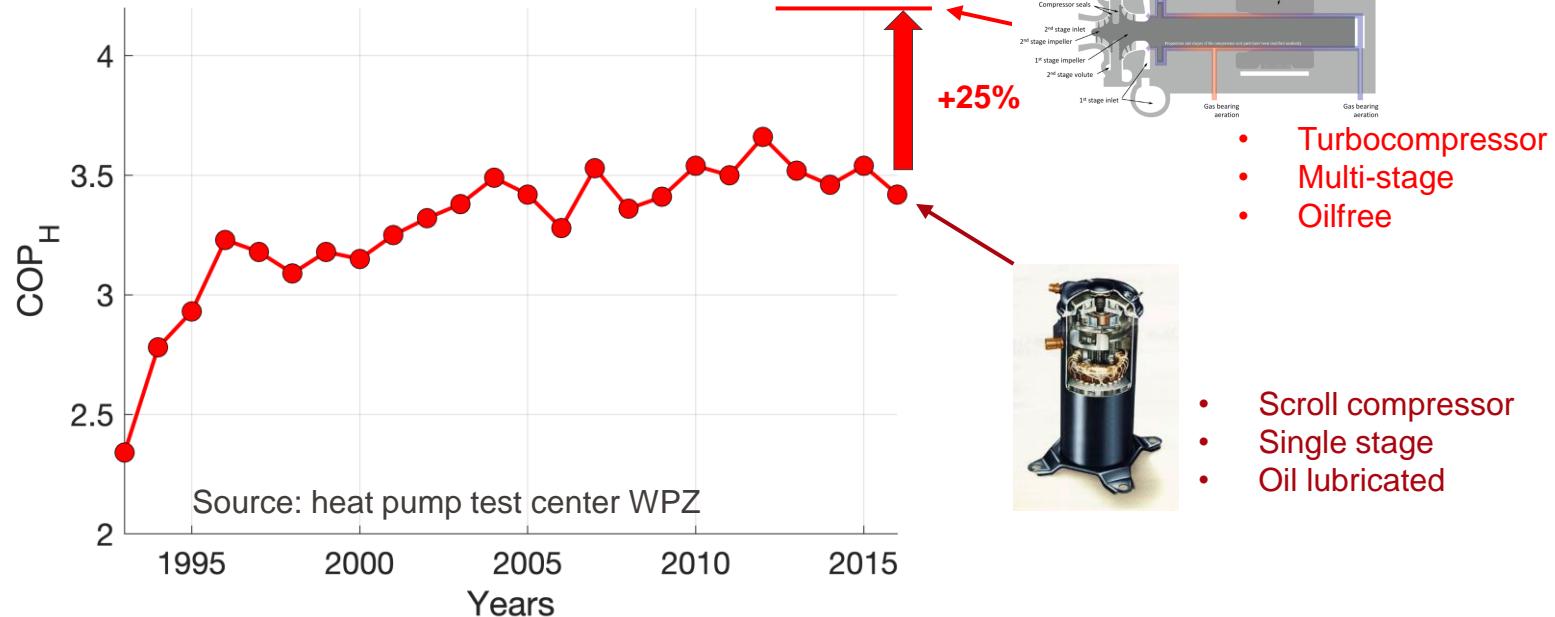
Twin Stage Heat Pump Compressor Experimental Challenges

- Compressor map matching
 - Energy balance across economizer driven by mass-flow-ratio
 - Accurate compressor matching required to achieve stable economizer pressure
 - Additional control degree of freedom needed



Sun, Q., Ji, C., Fang, J., Li, C., Zhang, X., Optimization Design of IGV Profile in Centrifugal Compressor, *Mathematical Problems in Engineering*, 2017, 8437325, 9 pages, 2017

Potential of Oilfree Turbocompressors on COP



- Key question: can another step-change be achieved and if so, how?
- With multi-stage heat pump cycles driven by oilfree turbocompressors

Summary of Challenges of Reduced-Scale Turbomachinery

- Gas lubricated bearings require small clearances to achieve stable operation → manufacturing cost → industrialization challenging
- Low bearing clearances require clean working fluids
- Reduced scale compressors efficiency suffers from Re-number effects, increased relative surface roughness and large tip clearances
- Reduced scale turbomachinery more sensitive to heat fluxes
- Leakage between stages is increased due to scaling effects

- Heat exchanger design

- Comprehension questions
- Centrifugal compressor analysis
- Flow through a turbine runner