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T. de Colombel | November 2023

# Hydraulic Design for Francis Turbines

# GE VERNOVA – Hydro Main Products



Turbines



Generators



Control System & BOP



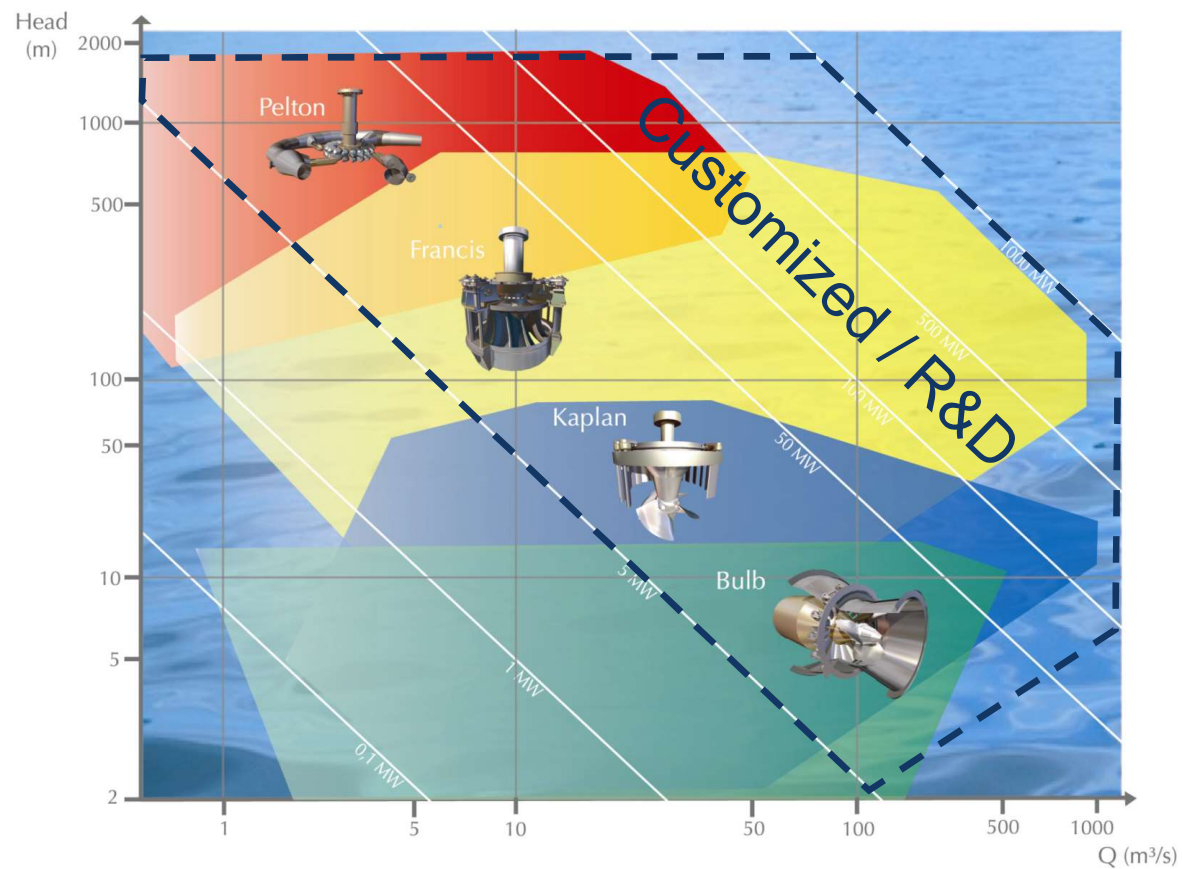
Hydro Mechanical

# +100 years of Hydraulic Turbines in France and all over the world



Hydraulic Laboratory in Grenoble, France

# Main Types of Hydraulic Turbines



# Less common types of turbines

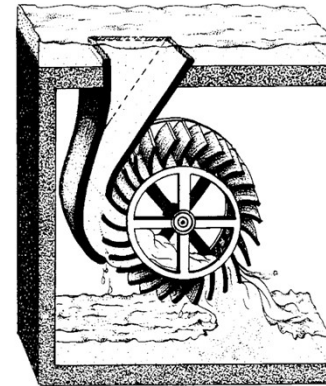
**DERIAZ**



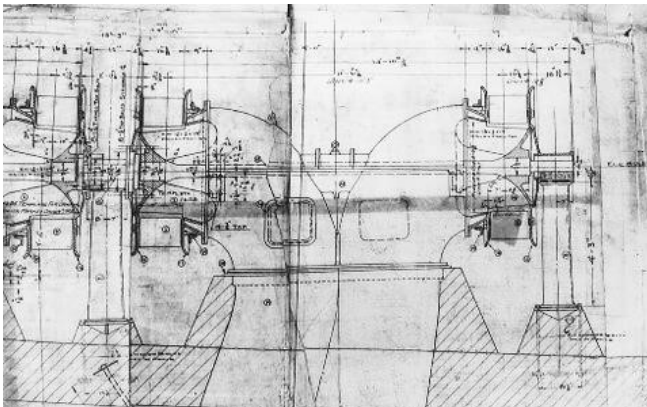
**TURGO**



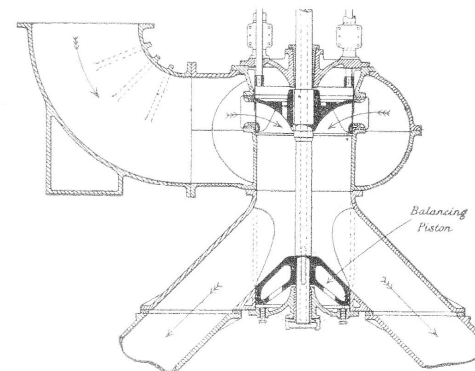
**BANKI**



**CAMEL BACK**



**???**





# How to design a Francis turbine?



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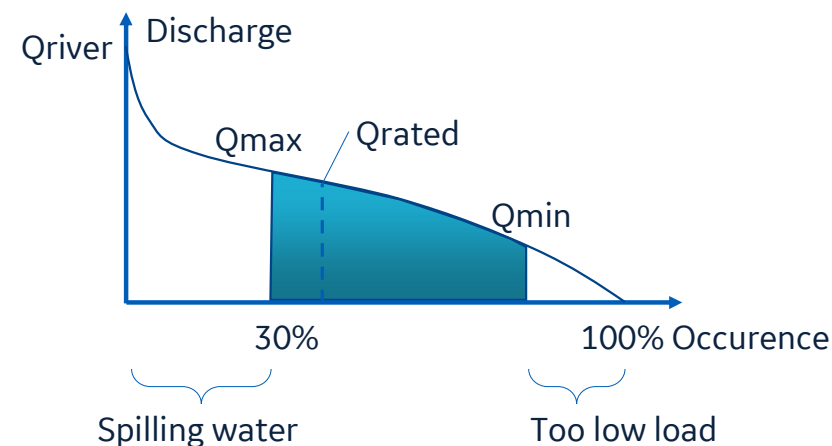
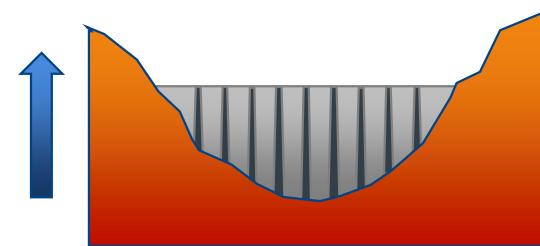
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# First Dimensioning

# First Dimensioning

For a given (new) site, one has to estimate...

- **Max Head** → the higher the dam, the more the potential energy... but the more expensive the **civil work**
- **Max Discharge** → Determined based on the Flow Duration Curve. The higher the max discharge, the higher the max output... but the more expensive the **hydromechanical** supply





# First Dimensioning

**Number of units** will be chosen:

- Less units (more output per unit) → Cheaper!
- For small installations... at least 2 units for maintenance purpose ————— • **Gavet**, France  
(2 x 50MW)
- For big installations... the individual unit size is the limit (roughly ~ 10m diameter for rotor size) ————— • **Three Gorges**, China  
(32 x 700MW)
- Excavation can be the limit for low head installations
- Road access, existing infrastructures... are also to be considered

# First Dimensioning

Once max head + max discharge (per unit) are chosen

→ **Rotation Speed (n)** is to be chosen

→ directly linked to the Velocity Triangles (inlet and outlet of the runner)

The higher the speed, the less poles in the generator... the cheaper (more compact), but:

→ **electrical limit** = output per pole

→ **mechanical limit** = stresses in the rotor at runaway

Introducing the specific speed ( $n_s$ ) of the design:  
(P in kW or in HP)

$$n_s = \frac{n \cdot P}{H_n^{5/4}}$$

# First Dimensioning

**Turbine size** defined by the flow speed...

A rough estimation for a Francis = outlet diameter ( $D_{LP}$ ) of the turbine set so that  $V \sim 12$  to  $15$  m/s

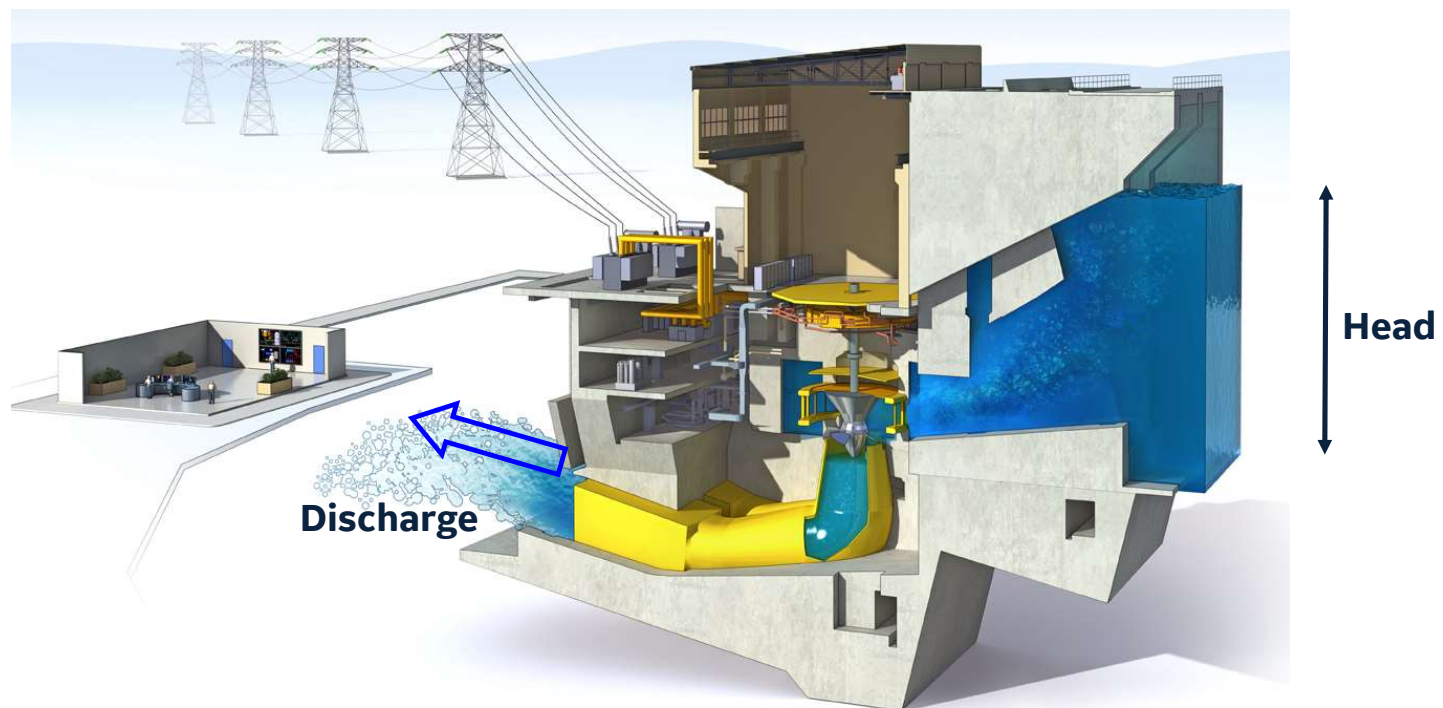
$$V = Q_{max} / \frac{\pi \cdot D_{LP}^2}{4}$$

The higher the flow speed, the higher the need for counterpressure on downstream side (higher NPSH) to avoid **cavitation** at the outlet.

For a given output / discharge, the smaller the unit, the lower (altitude) the setting must be. Once again, a tradeoff between **civil work** and **hydromechanical** supply.

# From the river to the turbine

Geographic locations / Water data / Tailwater level / head losses in penstocks...



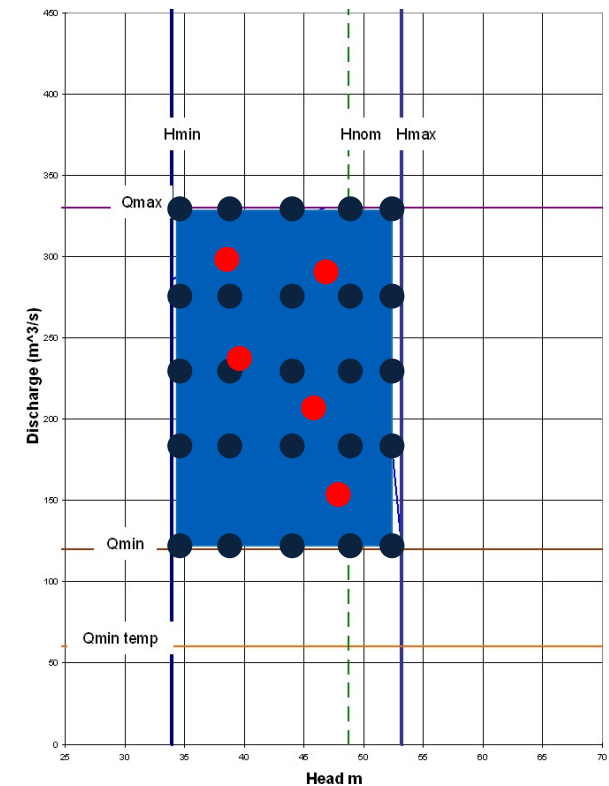
# From the river to the turbine

## Contract and guaranties come from :

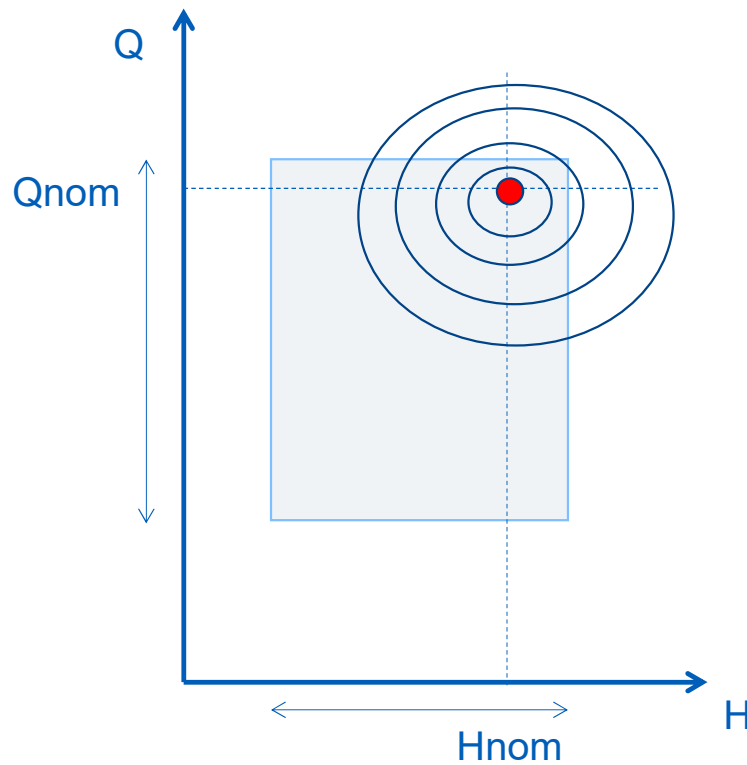
- Site characteristics (discharge/head)
- Economic optimization
- Smooth behavior
- Specific requirements of the customer (fish friendly/erosion...)

## Leading to specific constraints :

- Efficiency
- Maximum Output
- Cavitation margins
- Runaway speed
- Level of pressure fluctuations
- Transient behavior  
(overpressure and overspeed)



# Introduction to an efficiency hill chart



Efficiency  $\rightarrow$  Power

$$P \sim \eta * H * Q$$

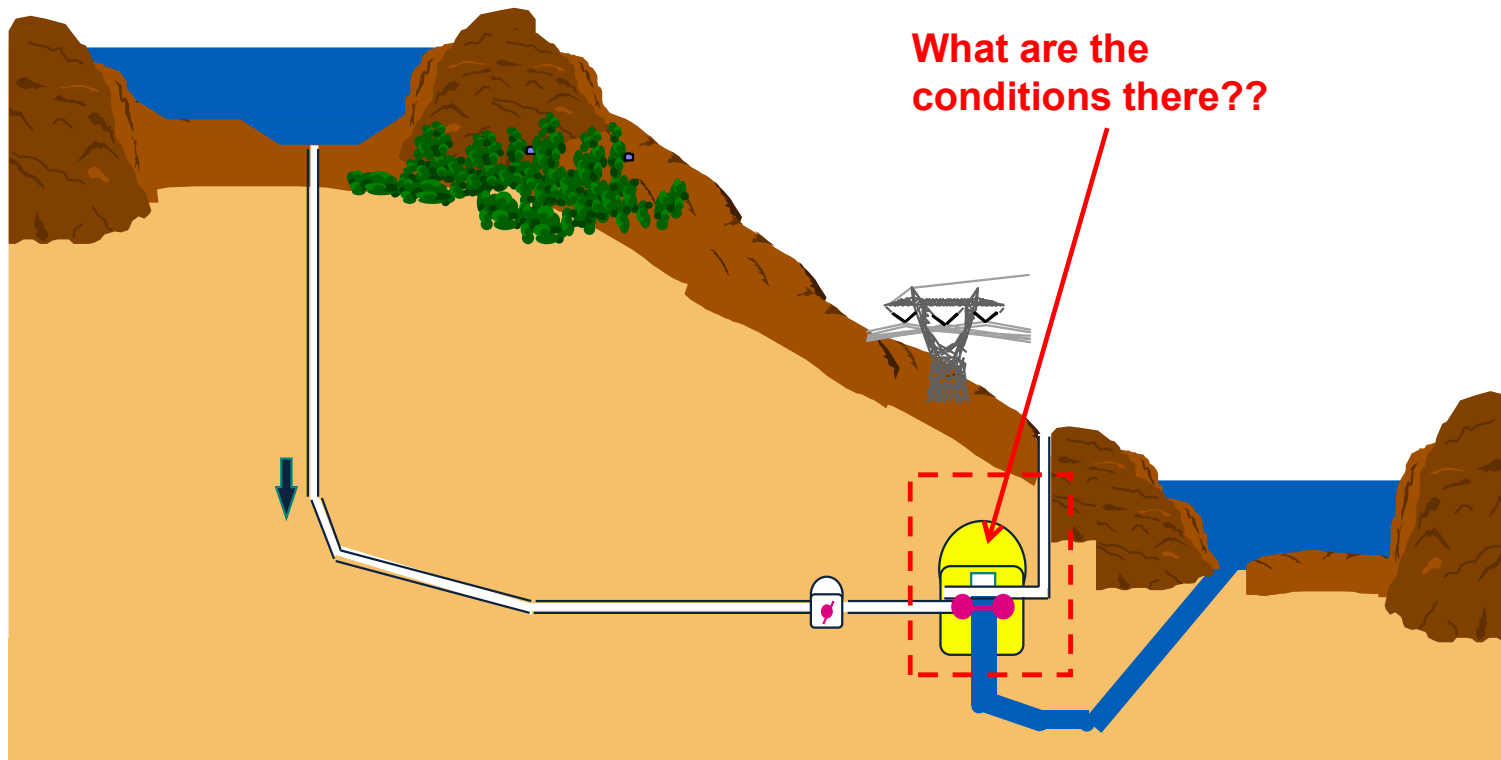
Adapting the hill chart

- $\rightarrow$  Maximizing the **Weighted Average Efficiency**
- $\rightarrow$  Maximizing the power plant productivity

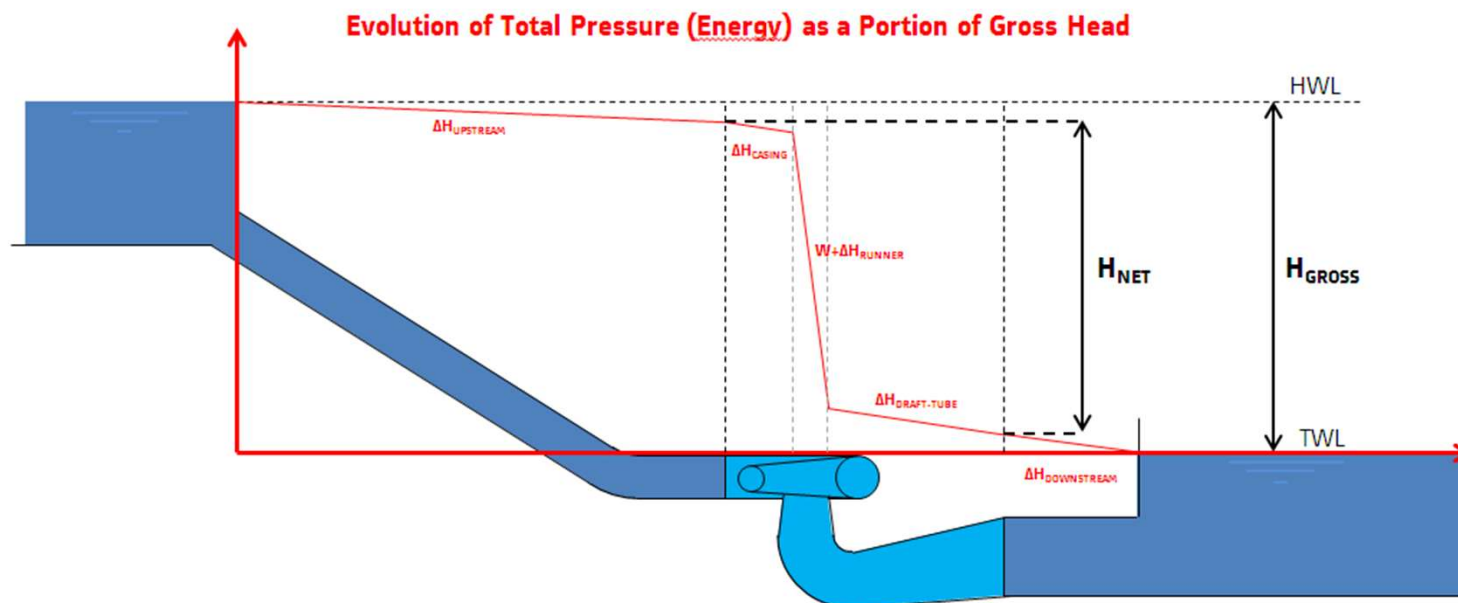


# From the river to the turbine

## Environment of the Turbine



# Energy Evolution in a hydraulic circuit



# Different types of energy losses

## > Head Losses

- Linear losses (friction in tube)  $DH \sim k * V^2$  (flow speed in the tube)  
with  $k \sim L$  (length)

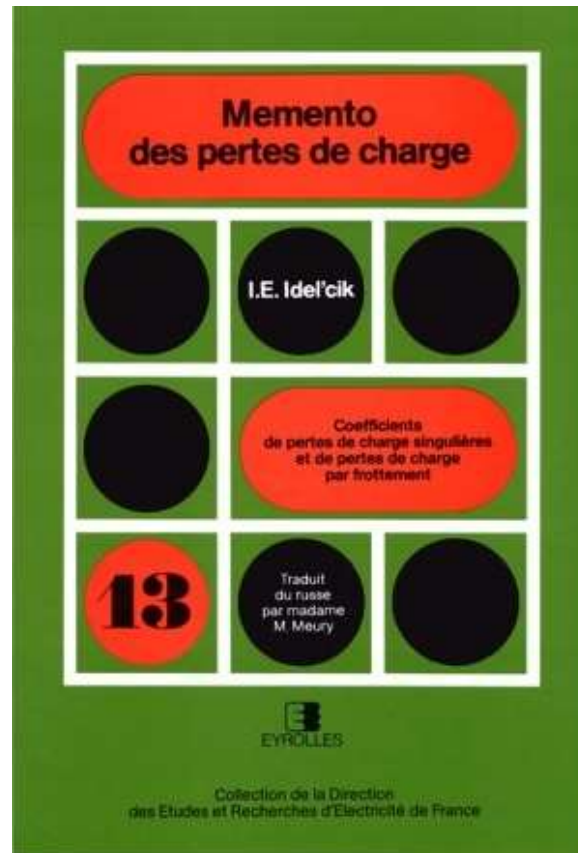
- Singular losses

- . Convergent / Divergent  
→ Controlling water passage: notion of **section law**
- . Incidence / Wake  
→ Shaping the blades: notion of **adaptation**
- . Flow separation (can be seen as a local section law modification)

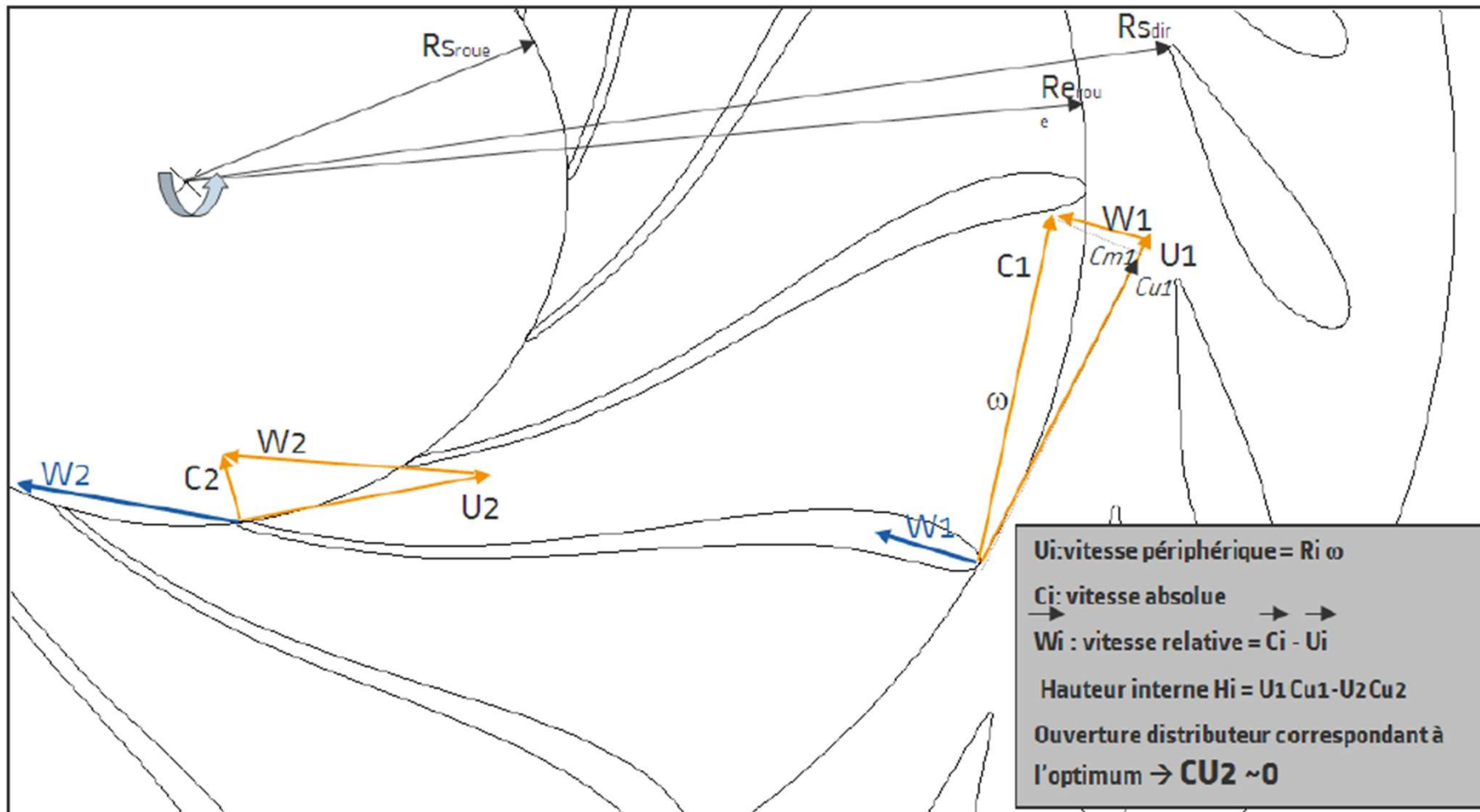
## > Volumetric Losses

## > Other friction Losses

# Bible for head loss coefficient “Idel’cik”



# Runner Design: Velocity triangles



# Two equations daily used by a hydraulic engineer

## → Euler

$E/g = U1.Cu1 - U2.Cu2 = \eta^*H$   
introduction of “internal head” = Work  
 $H_i = E/g = U1.Cu1 - U2.Cu2$   
 $\eta = H_i/H$



## → Bernoulli

Definition of “Total Pressure”  
 $P + \rho g z + \frac{1}{2} \rho V^2$  (in Pa)  
*pressure, potential, kinetic*  
 $P/\rho g + z + V^2/2g$  (in mWC)  
→ constant on a stream line of  
a perfect fluid (no head loss)

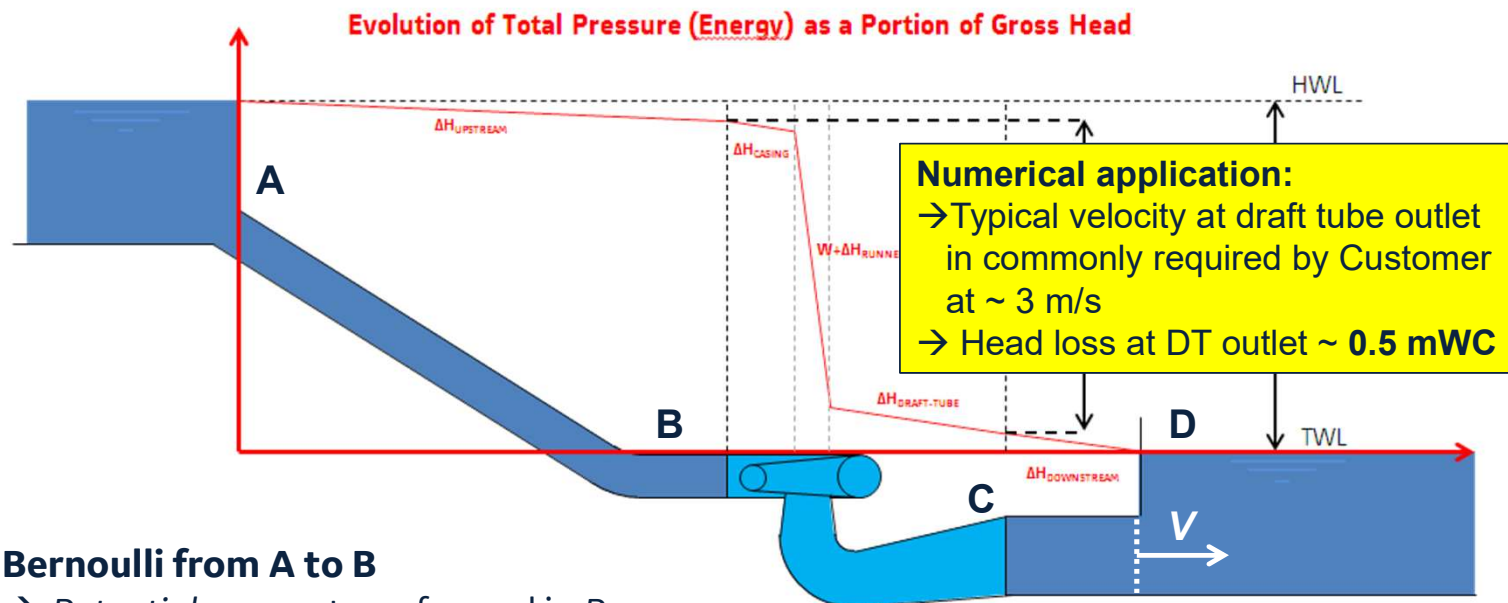


in real life, between A and B :

$$P(A) + \rho g z(A) + \frac{1}{2} \rho V(A)^2 = P(B) + \rho g z(B) + \frac{1}{2} \rho V(B)^2 + \Delta P_{tot}(A \rightarrow B)$$



# Back to the environment of the Turbine



## Bernoulli from A to B

- Potential energy transformed in Pressure
- DH in penstock in  $k \cdot L \cdot V^2$   
“the longer the more losses”  
“the smaller the diameter the more losses”
- Economical optimum

## Bernoulli from C to D

- Pressure in Potential
- Friction losses (in  $kLV^2$ )  
+ Sudden enlargement  
 $DH = V^2/(2g)$

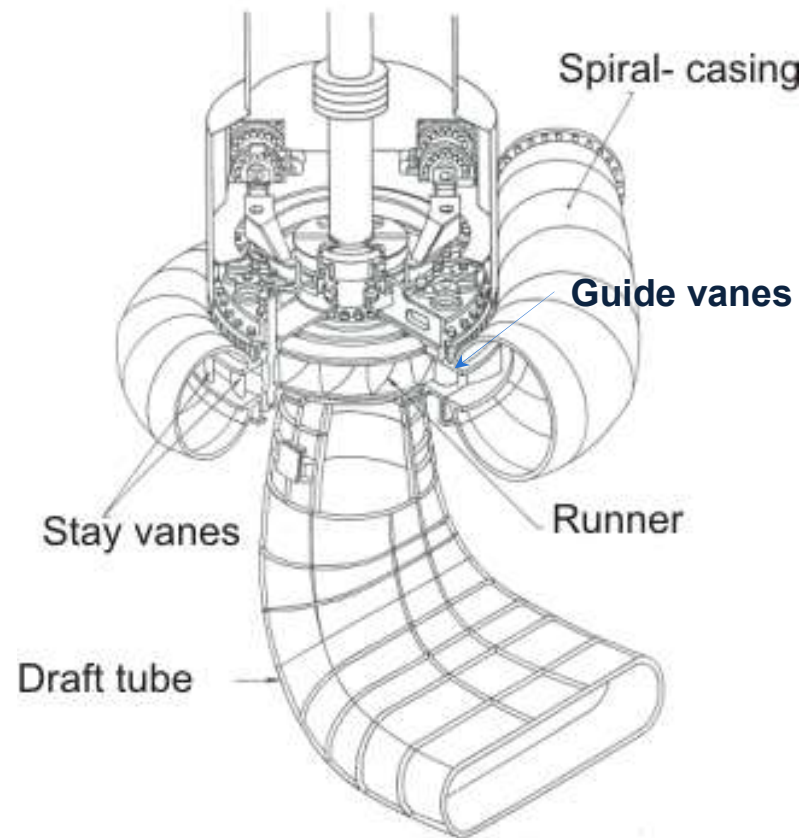


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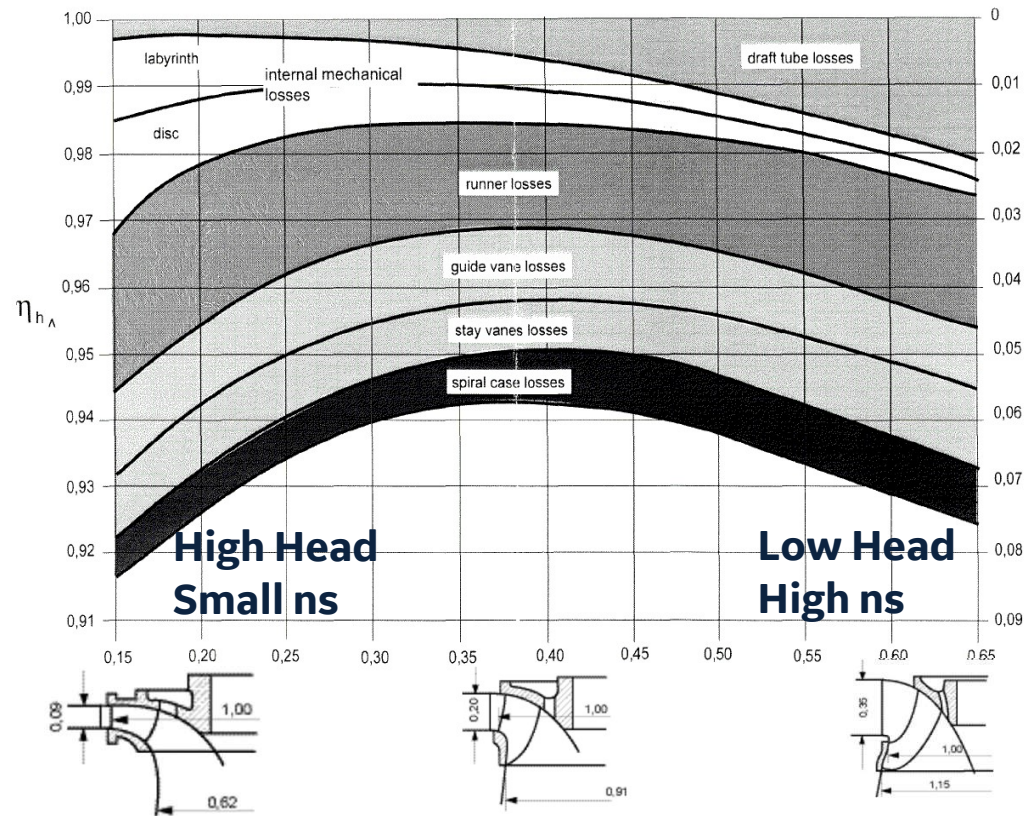
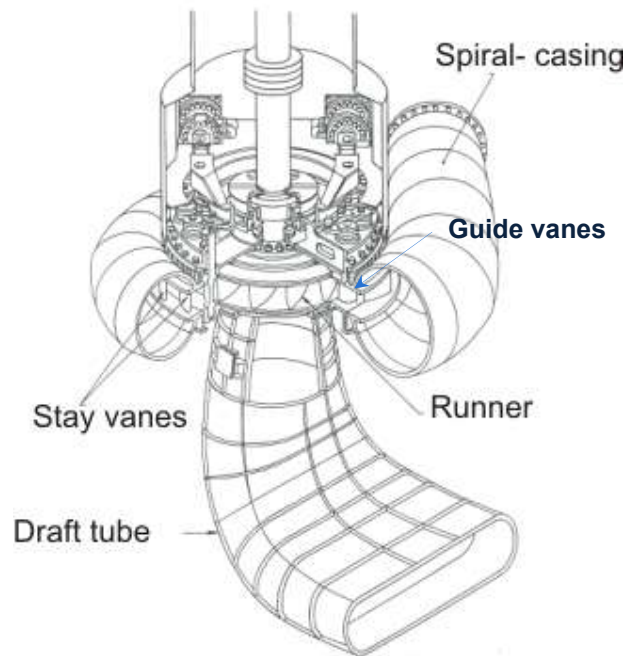
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# — Components overview

# Different parts of the turbine



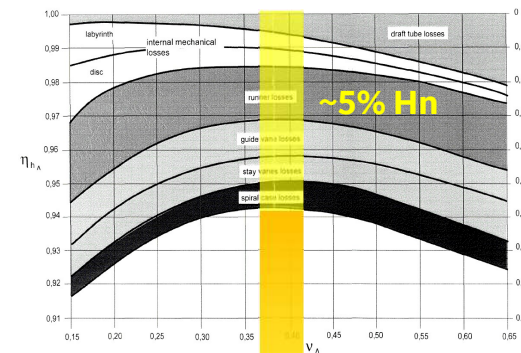
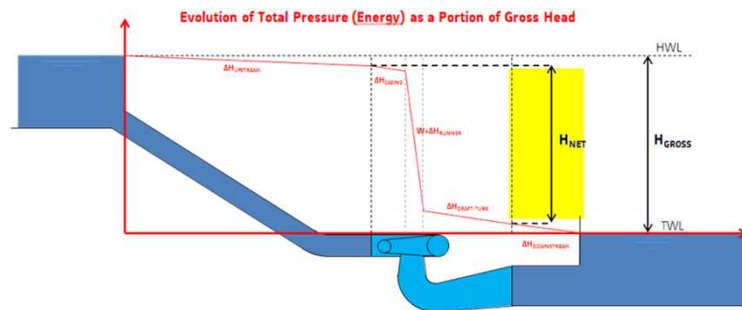
# Loss distribution in a Francis turbine



# What is the main head loss in the hydraulic circuit?



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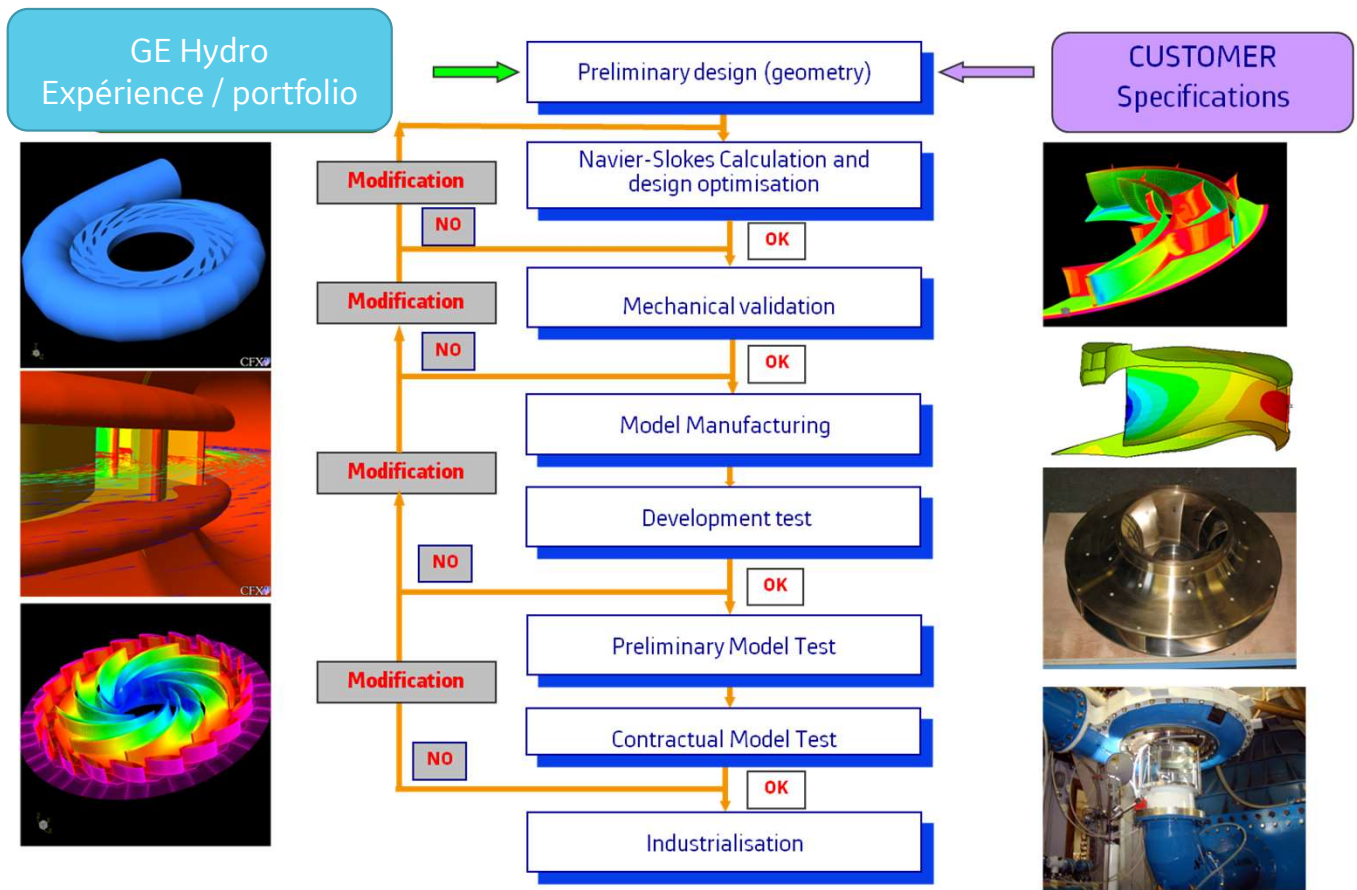


**W**ORK  
recovered by  
the runner  
  
~ 95%  $H_n$   
(~ 90%  $H_g$ )

## Consequences

- Disconnection between upstream and downstream  
“the draft tube doesn’t see the head”
- At the first order, the runner itself grants a good  
flow distribution on the upstream side

# Hydraulic design process





# Main design tools : CFD

Resolving Navier Stokes equations : 
$$\rho \left( \frac{\partial \mathbf{v}}{\partial t} + \mathbf{v} \cdot \nabla \mathbf{v} \right) = -\nabla p + \mu \nabla^2 \mathbf{v} + \mathbf{f}.$$

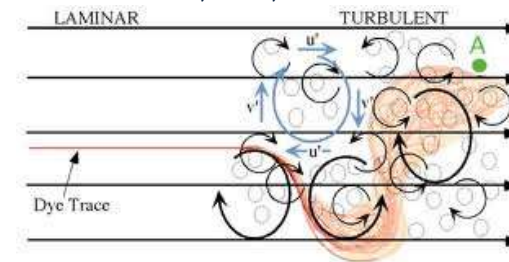
Nonlinear partial differential equations

Turbulence (time dependent chaotic behavior)

No analytics solution → One of the Millenium Prize Problems (US\$1,000,000)

Numerical simulation :

- Discretisation of equation in discritized space
- Significantly different mixing-length scales : Full resolution is not reachable for industrial flows
- Use of statistical model



**Lots of uncertainties during the design  
of hydraulic component**



**It's very important to validate  
performances on the test-rig**



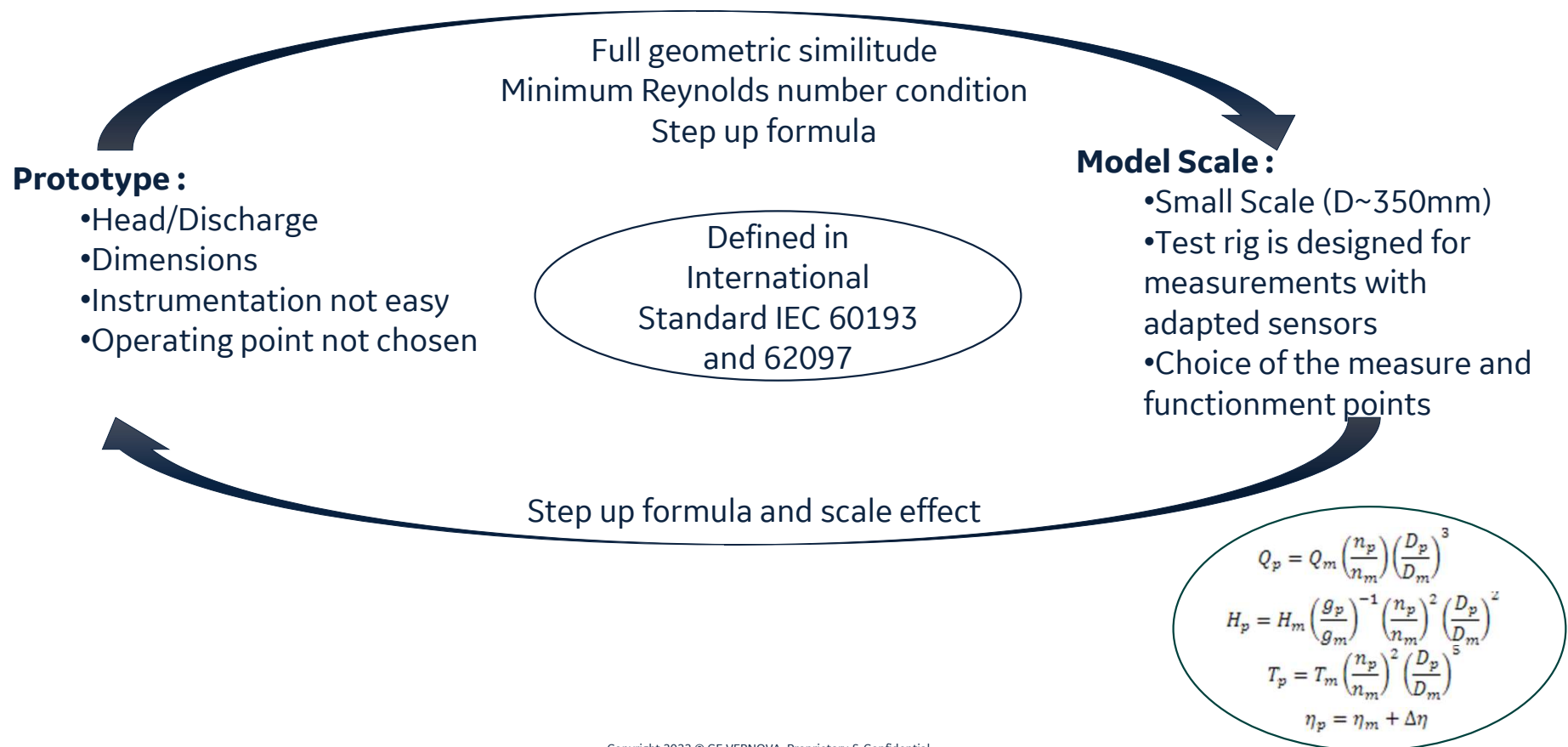
**Especially for off-design points  
(start-up, runaway, low output)**



**Unless very close to a tested  
reference**

# Performance validation by Model tests

## Similitude rules





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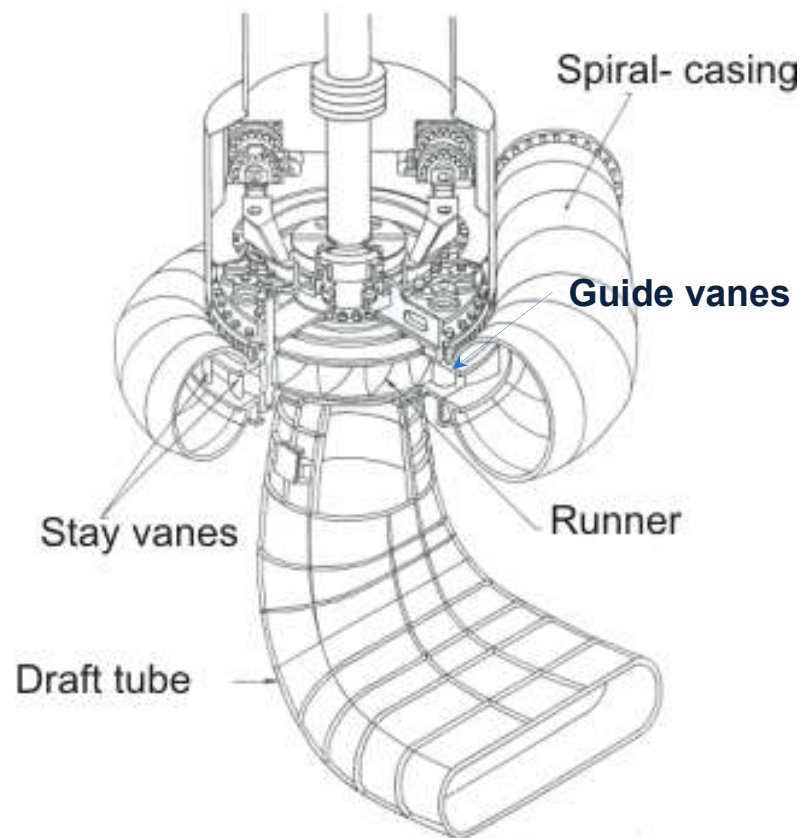
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# Hydraulic Design

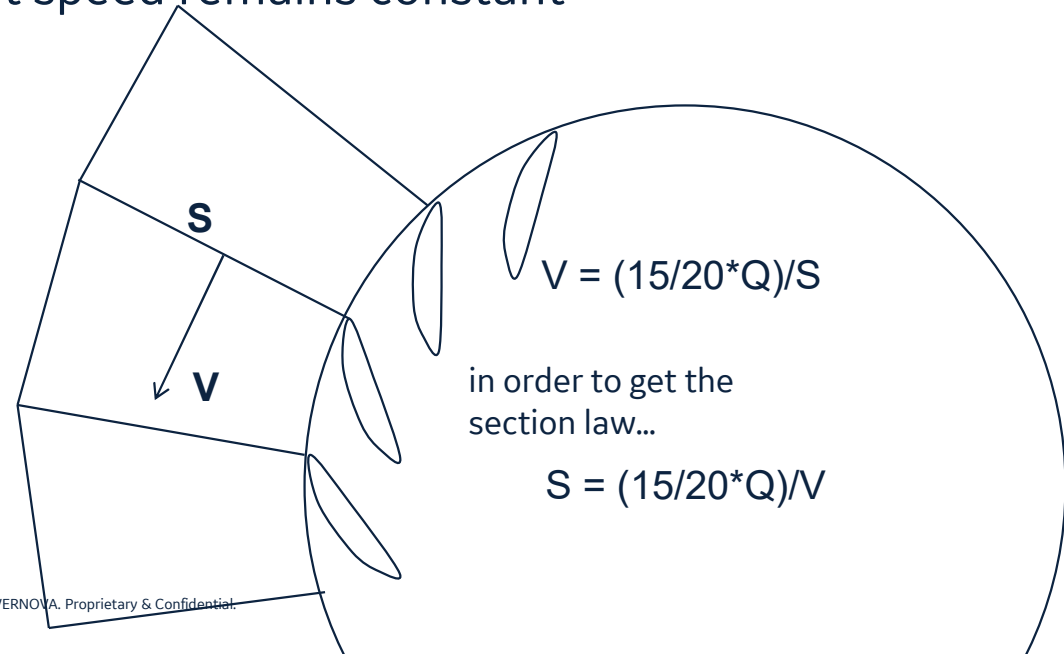
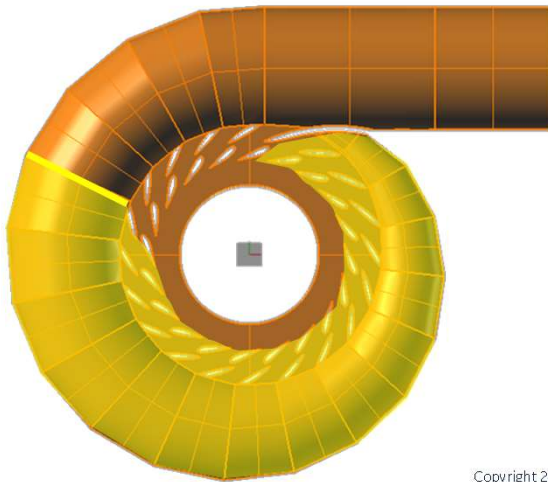
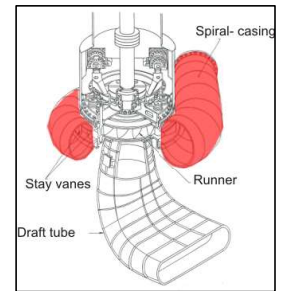
# Let's start!

→ Reminder of lexicon



# Spiral Casing

- Ensure an even flow distribution around the runner
- Hypothesis = runner grants a homogenous flow distribution
  - spiral casing should guarantee a good distribution of **speed** and **flow angles**
  - Section law that will make sure that speed remains constant in the different sections



# Spiral Casing

- Hypothesis 1: uniform flow distribution around the runner
- Hypothesis 2: uniform flow distribution in sections

$$V_{\text{radial}} = Q / S1$$

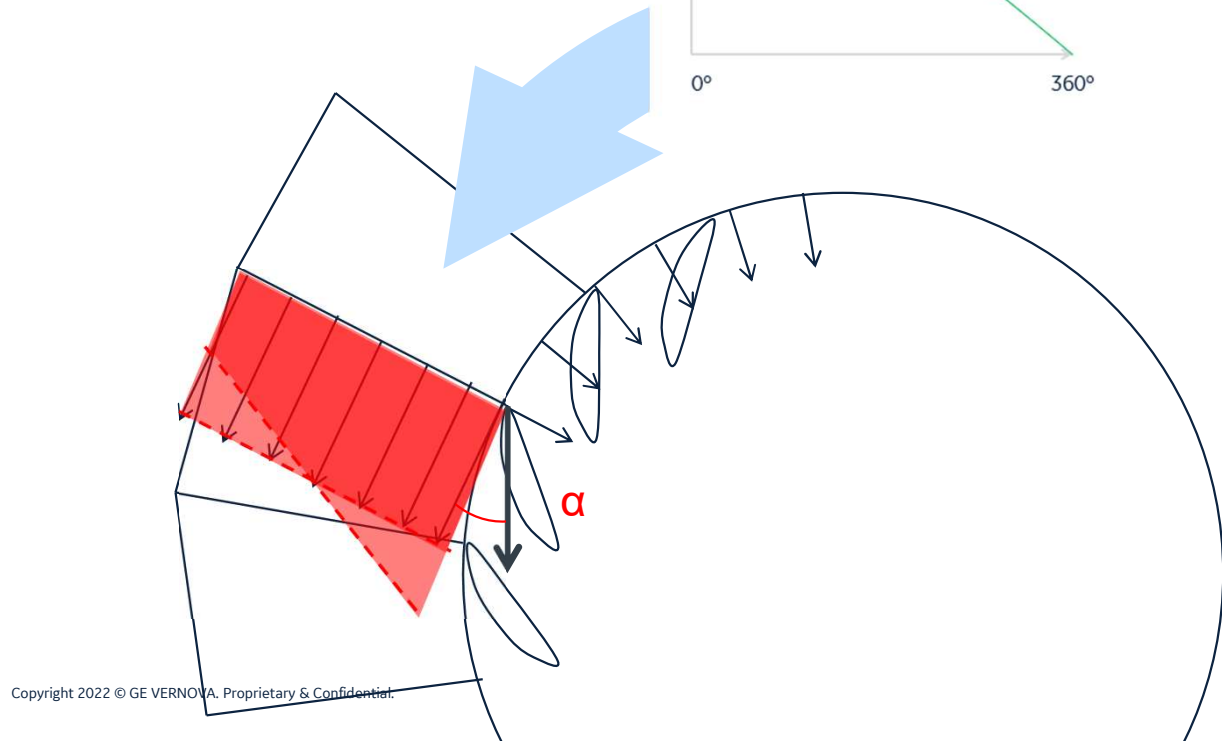
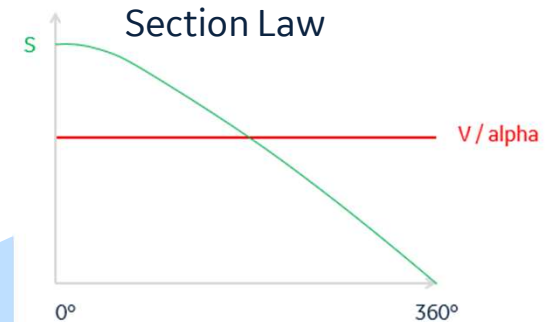
$$V_{\text{tang}} = n/n_{\text{total}} * Q / S2$$

$$\begin{aligned} \rightarrow \alpha &= \text{atan}(V_{\text{radial}}/V_{\text{tang}}) \\ &= \text{atan}(n/n_{\text{total}} * S2/S1) \end{aligned}$$

independent from Q!

Flow Angle at Stay Vane inlet  
is supposed to be constant  
(one profile for all stay vanes)

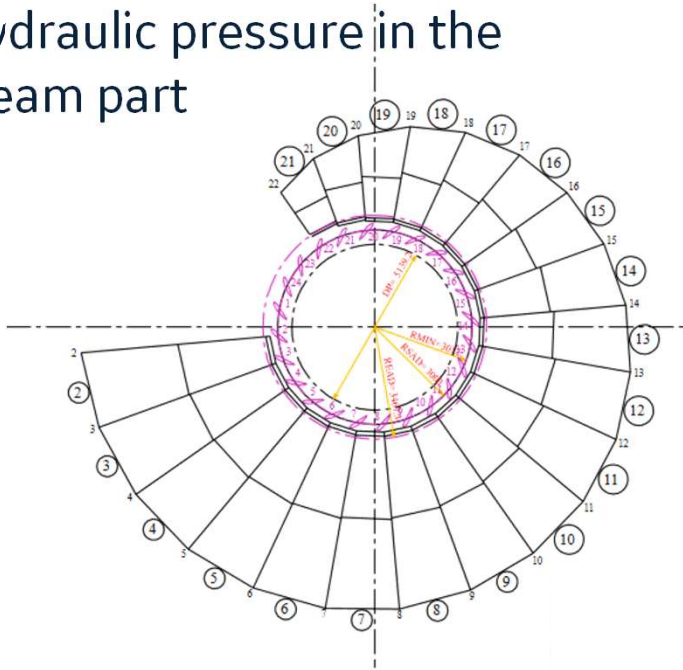
→ Thickness of the Stay Vane  
makes it tolerant to angle  
variation



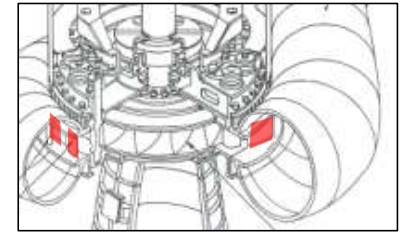
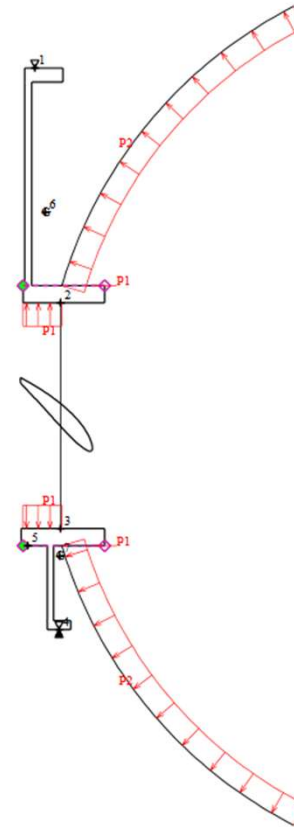


# Stay Vane

- Mechanical function to stand the hydraulic pressure in the upstream part

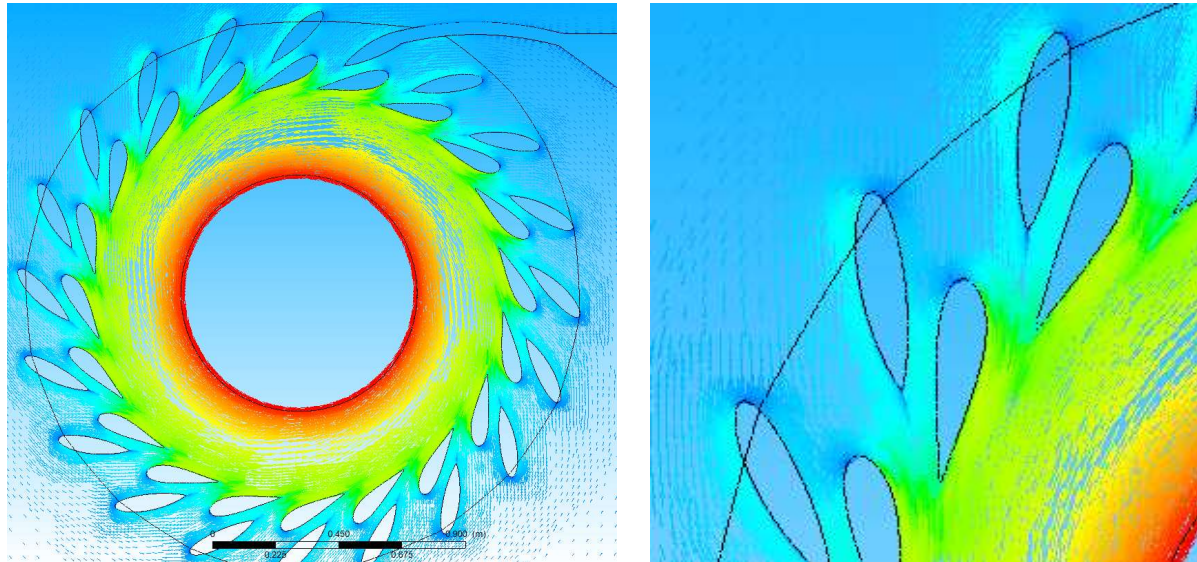
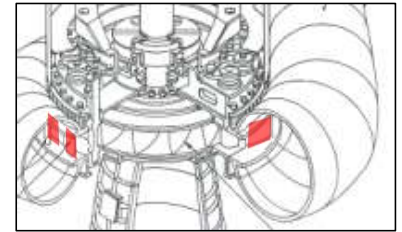


→ Thickness, stiffness, inertia



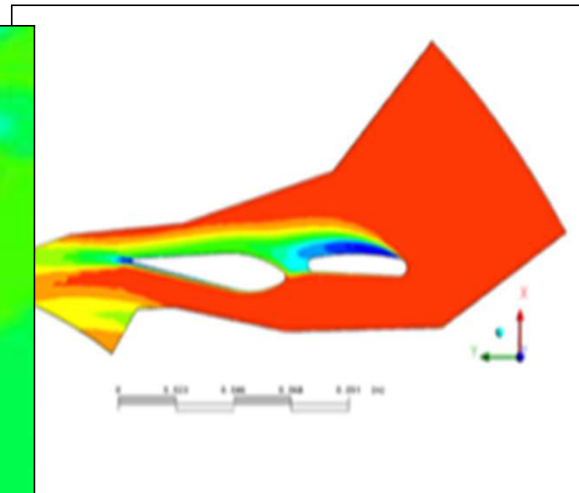
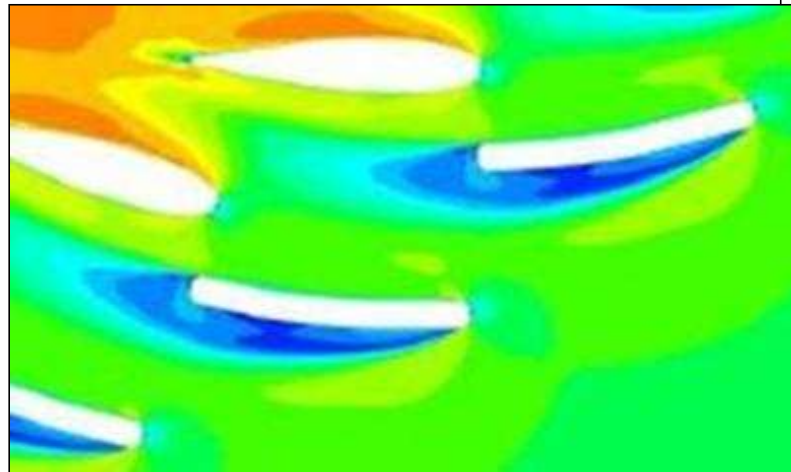
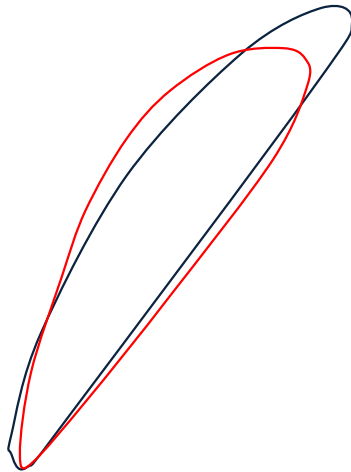
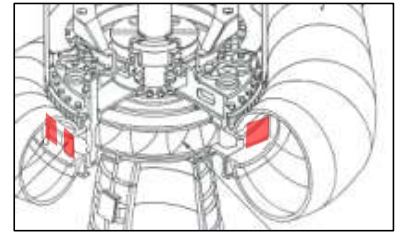
# Stay Vane

- Since it *has to be there*, it is designed to be “hydraulic friendly” 😊
- Thick leading edge to tolerate angle variation (even if small)  
Thin trailing edge to minimize losses (+ Von Karman issues...)

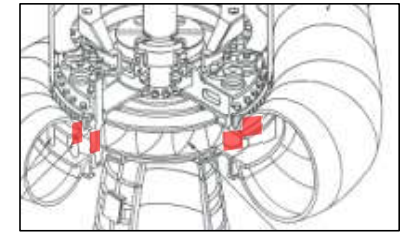


# Stay Vane

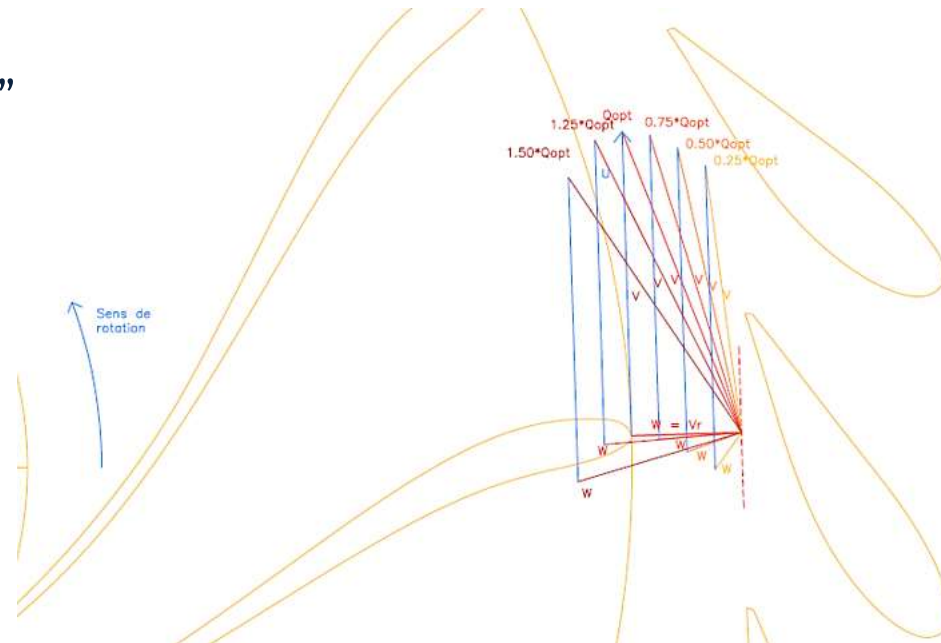
- These two designs are more or less **equivalent** for mechanical purpose... but what consequences on the hydraulic?



# Distributor

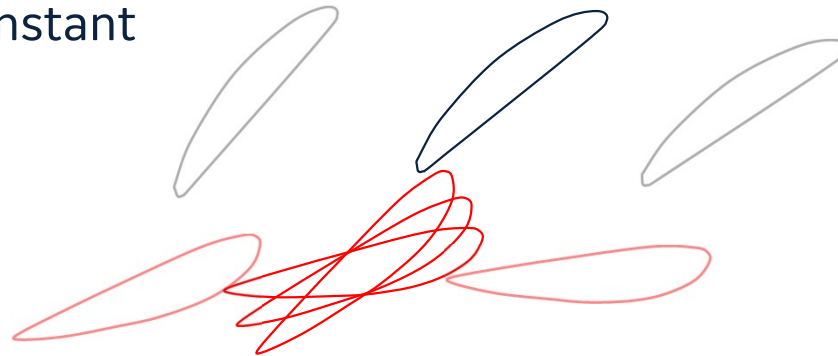
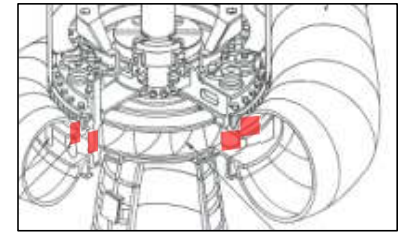


- For a simple regulated turbine (like a Francis), it is the only device to regulate the discharge / power / load
- Its function is to deliver **a flow angle** to the runner
- it is not strictly speaking a “tap” since main head loss still comes from the runner



# Distributor

- Designed to **stand the head** (especially high head machines) and to **accept various flow angles**
- Flow angle coming from stay vane is constant
- But guide vane angle is not constant (from 0 to 30-40°)



- Leading edge needs to be tolerant = thick
- Trailing edge, again, needs to be thin (wake and Karman)



# Runner



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- Transform **kinetic and pressure energy** in **mechanical energy**
- Designed for an optimal Head and an optimal Discharge

## Available Energy (Hydraulic)

$$P_h = \rho g H_n Q$$

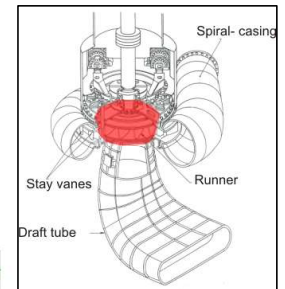
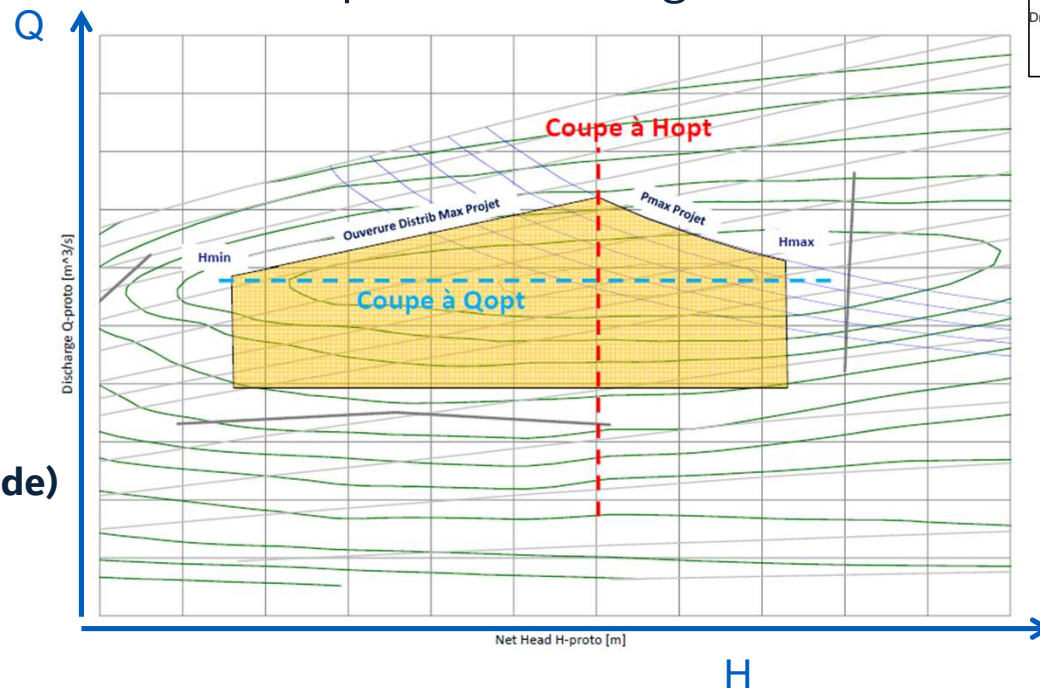
## Transformed Energy (mechanic)

$$P_m = w * T$$

*Rotationnal Speed \* Torque*

## Definition of Efficiency (turbine mode)

$$\eta = P_m / P_h$$



# Runner

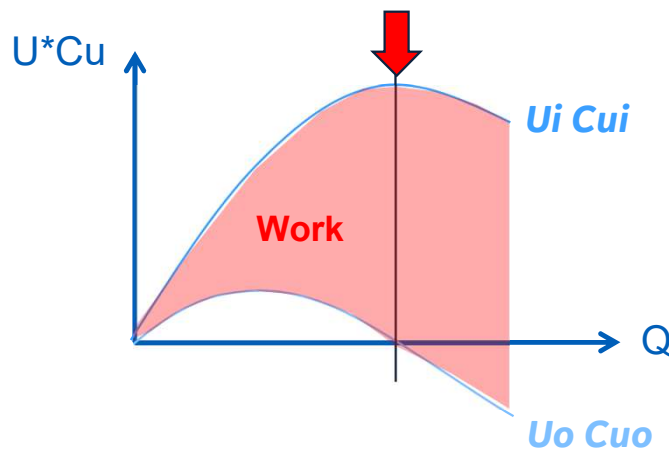
## Available Energy

- $\Delta(P_{tot})$  – Head losses out of Turbine (Inlet + Outlet) =  $\rho g H_n$

## Energy transferred to the Shaft by the Runner

- Moment of Momentum theorem (fluid volume in the runner)
- Mass Energy transferred E (i for Inlet / o for Outlet)

$$E = U_i C_{ui} - U_o C_{uo}$$



$U = r \cdot \omega$   
C absolute velocity  
 $C_u$  : tangential component

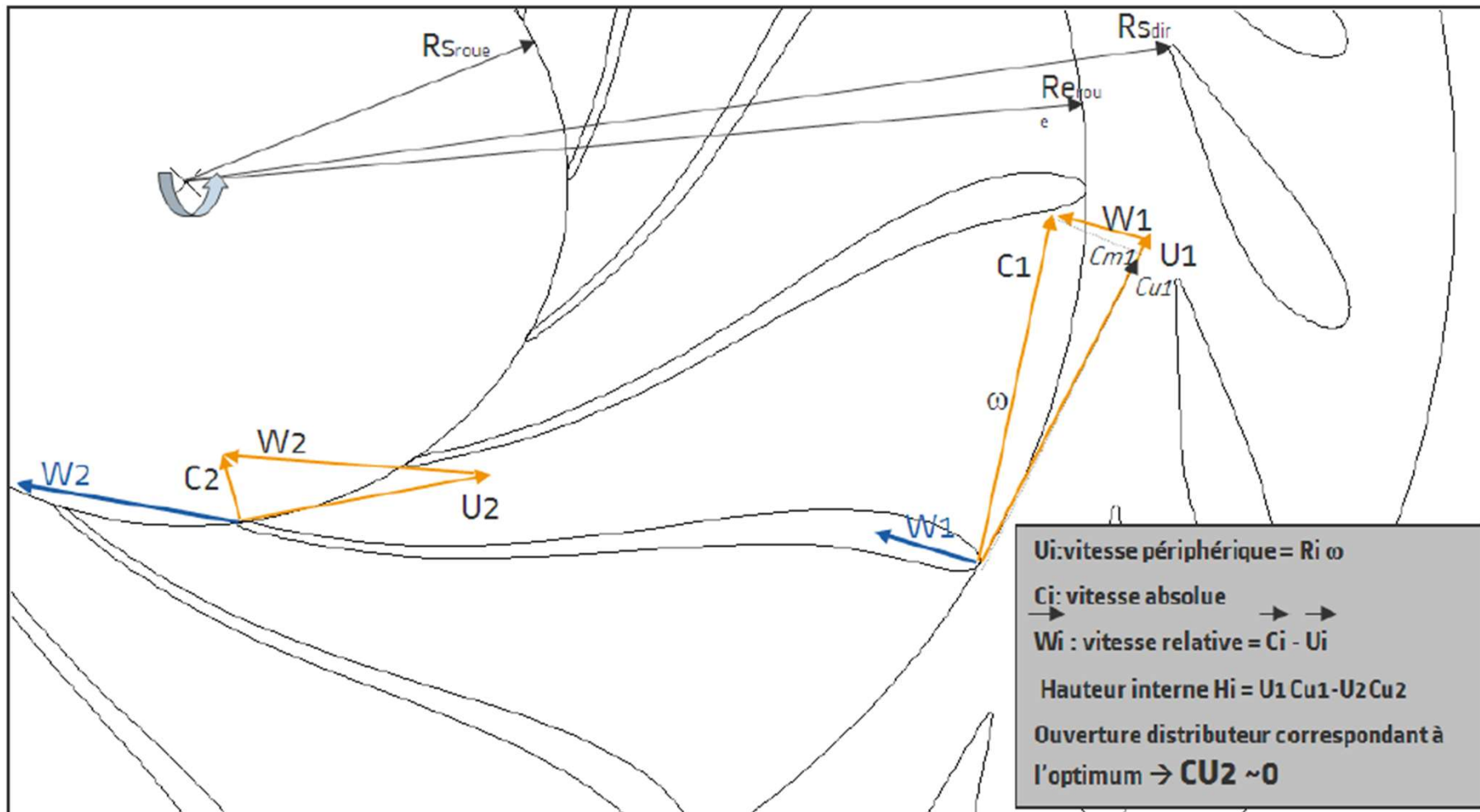
Optimal:

$U C_u$  @inlet maximal

$U C_u$  @outlet null



# Runner Design: Velocity triangles



# Hydraulic design - Runner

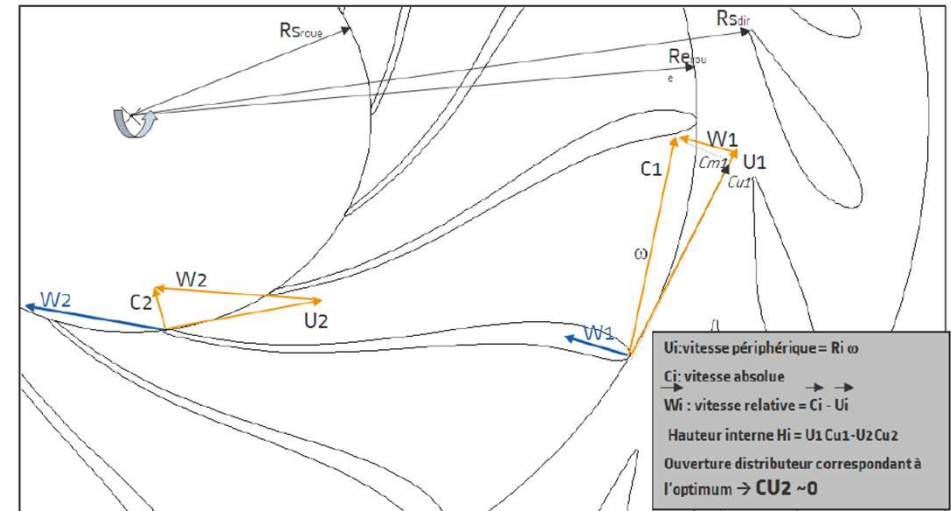
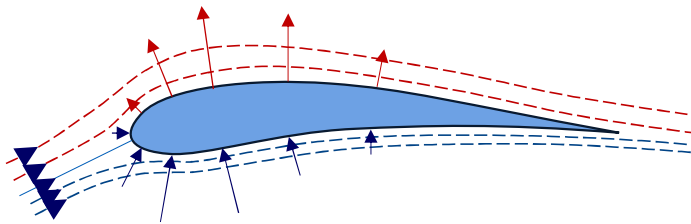
## A second usefull equation : Euler

$$\rightarrow \text{Euler } H_i = \frac{U_{HP} \cdot C_{uHP} - U_{LP} \cdot C_{uLP}}{g}$$

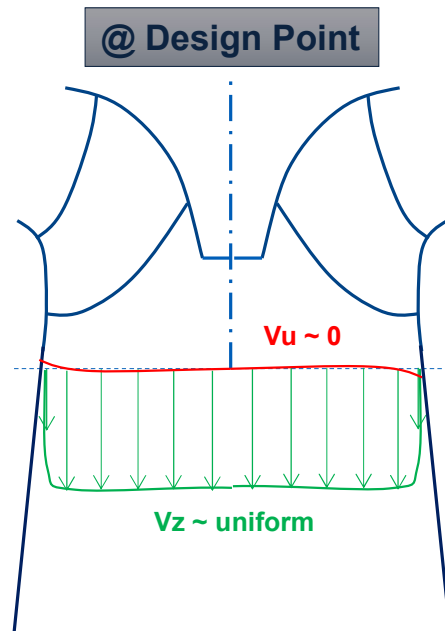
$$\eta_H = \frac{H_i}{H} \text{ (in turbine mode)}$$

The internal head  $H_i$  is a function of the angle evolution

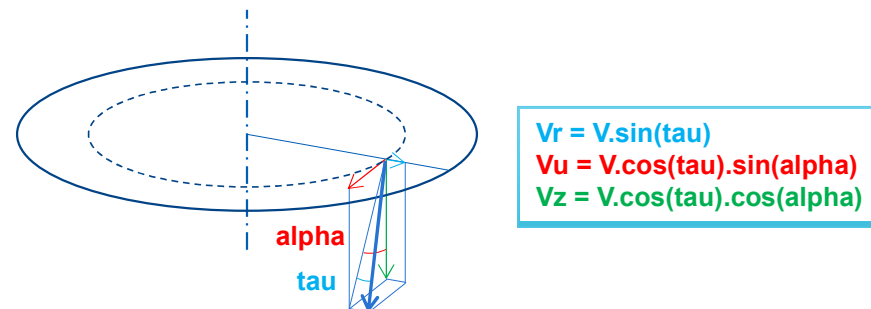
$E = g H_i$  may also be written  
 $\int_{\text{blades}} (p \text{ pressure side} - p \text{ suction side}) ds$



# Velocity Profiles at runner outlet



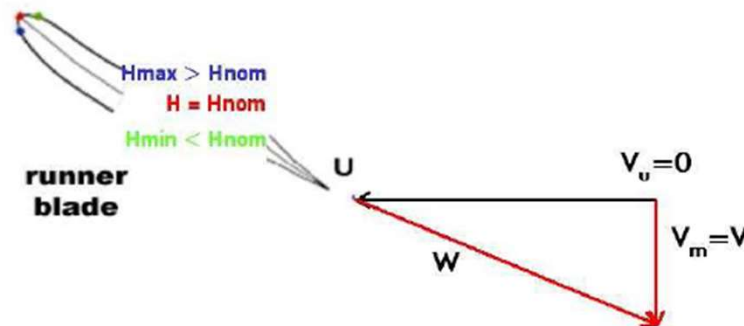
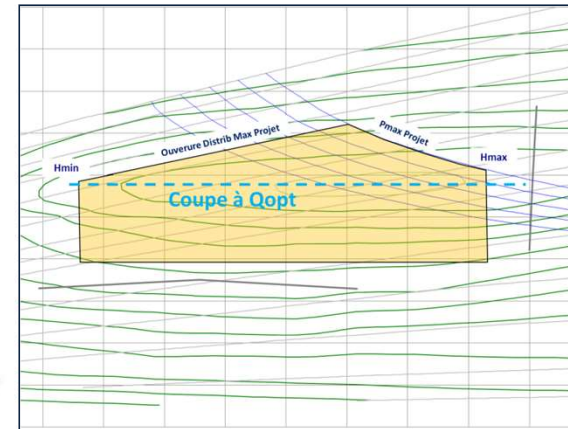
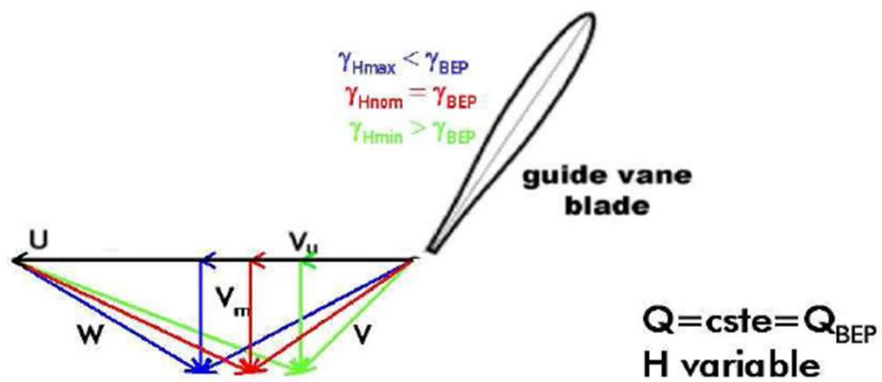
**Axi-symmetry** hypothesis on velocity profiles  
→ Velocity profiles can be described *on a radius*  
→ *Cylindrical* projection is the most appropriated



**If considered on a diameter...** (e.g. x axis)

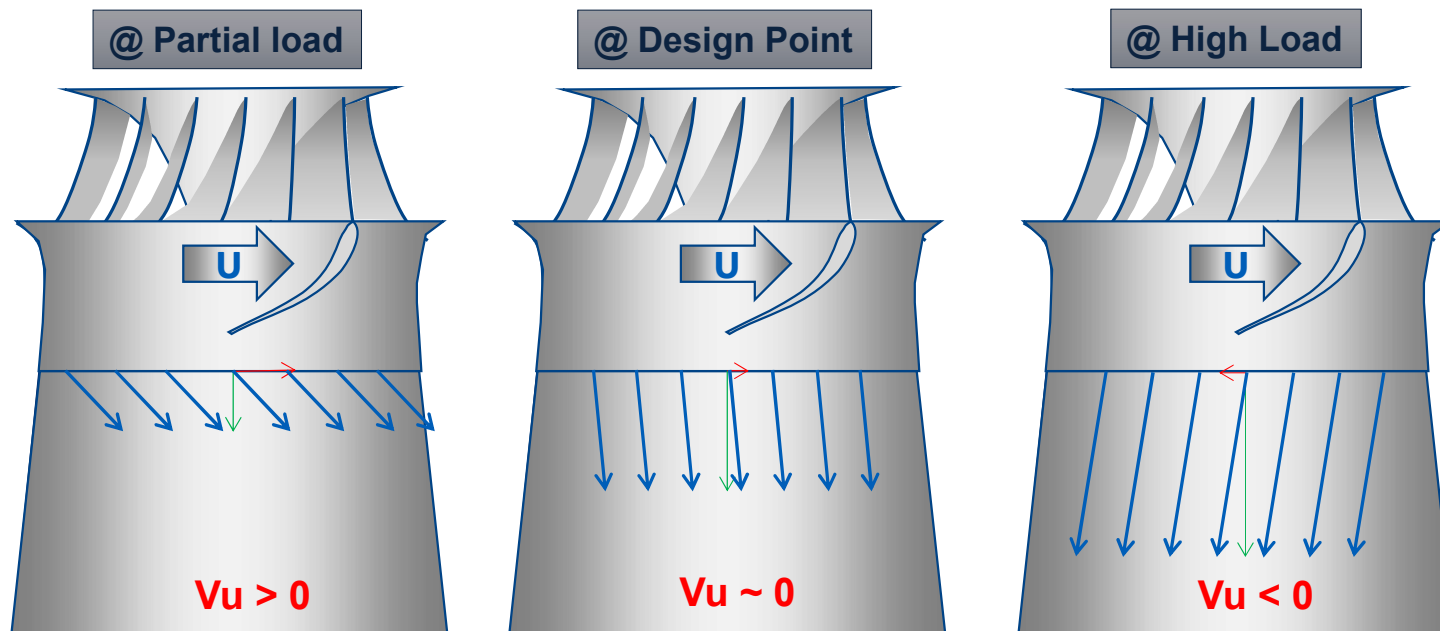
- $V_z$  is an even function of  $x$
- $V_u$  and  $V_r$  are odd functions of  $x$
- “theoretically” on unit axis ( $r = 0$ )  $V_u = V_r = 0$

# Cut at $Q_{opt} \rightarrow$ Head influence

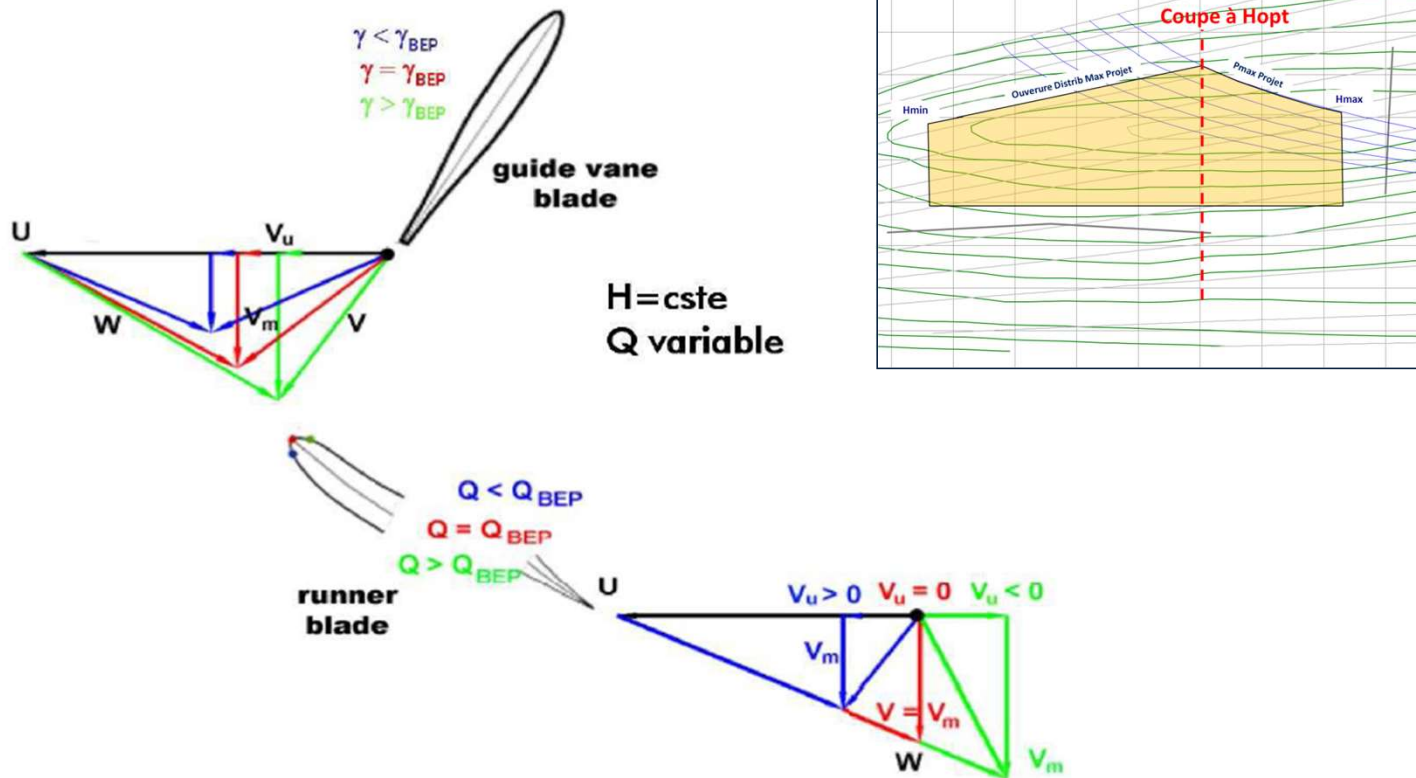


"The Draft tube does not see the head"

# Velocity Profiles at runner outlet



# Cut at Hopt → Discharge influence



# How to design a runner?

## Inlet adaptation

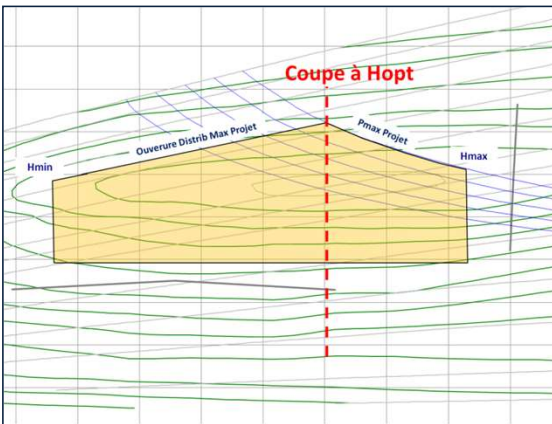
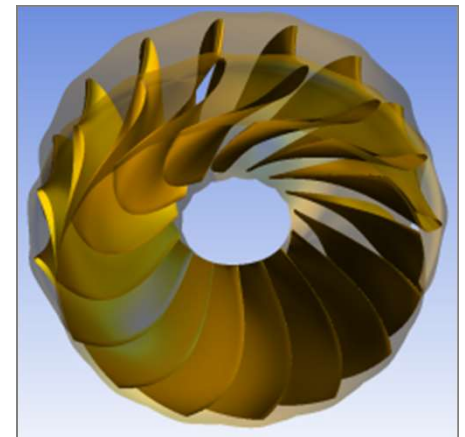
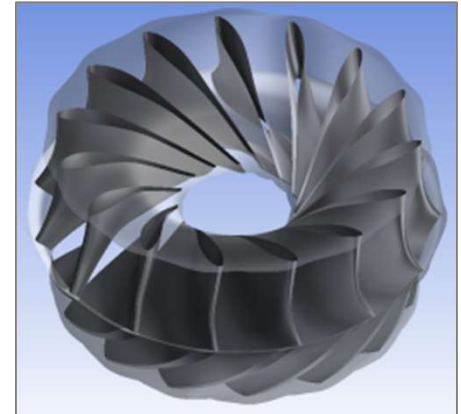
- Designed for optimal head
- Inlet cavitation limits

## Blade loading

- Ensure a proper “meridian equilibrium”

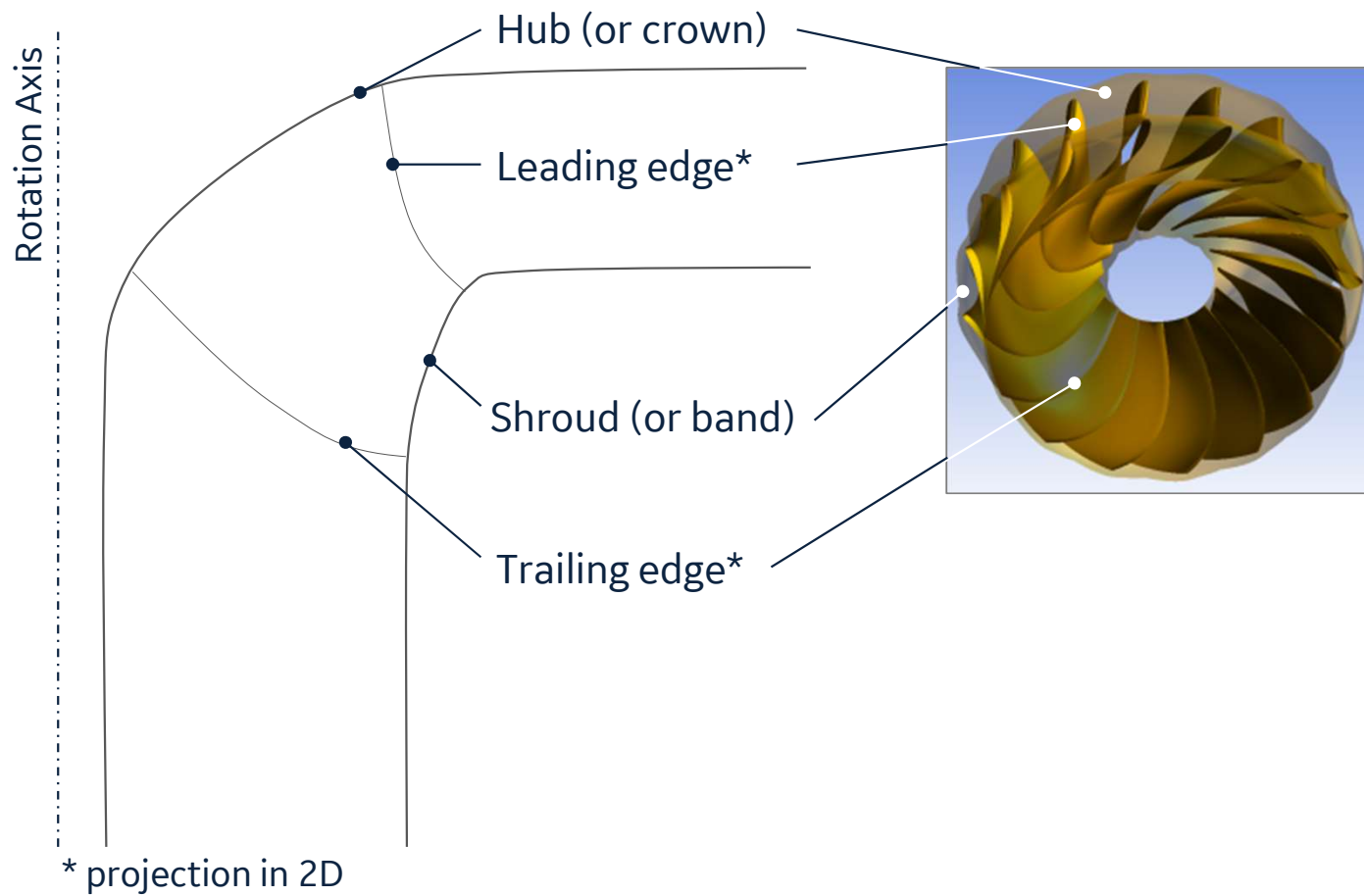
## Outlet adaptation

- Designed to deliver  $C_u = 0$   
(nominal discharge)
- Ensure good margin  
with outlet cavitation

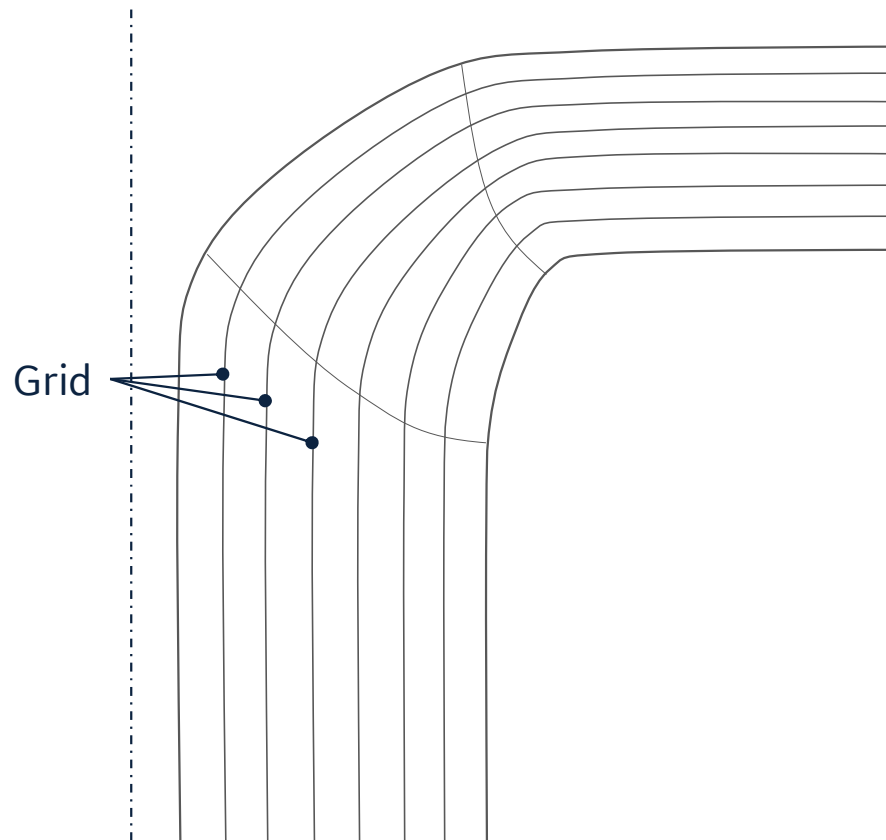




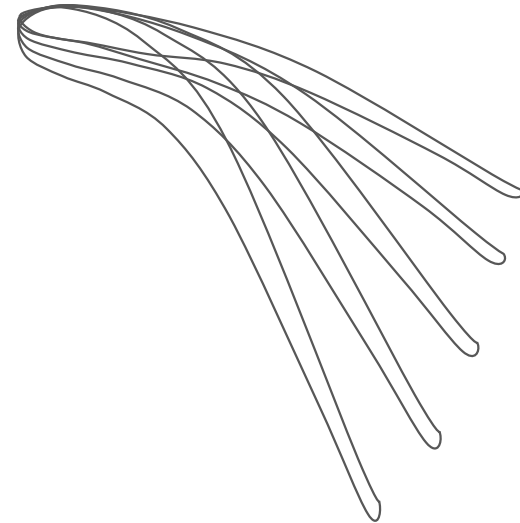
# Runner Design: Meridian Channel



# Runner Design: Meridian Channel



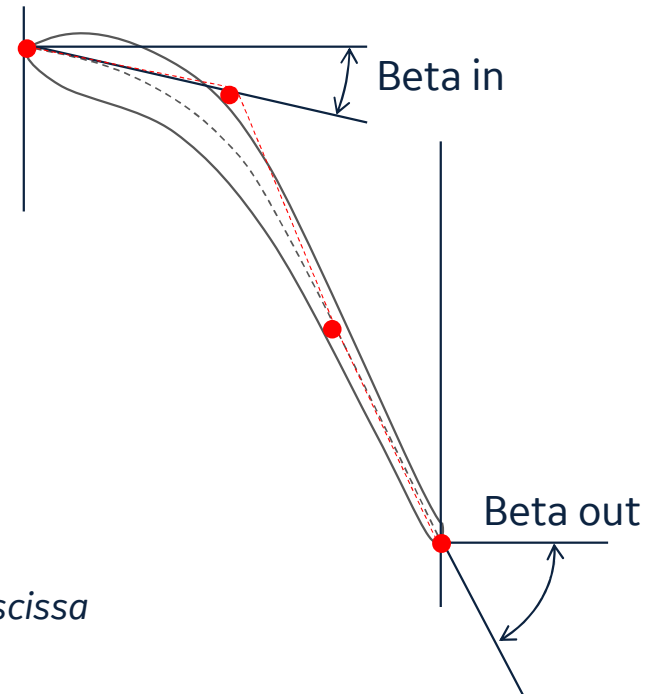
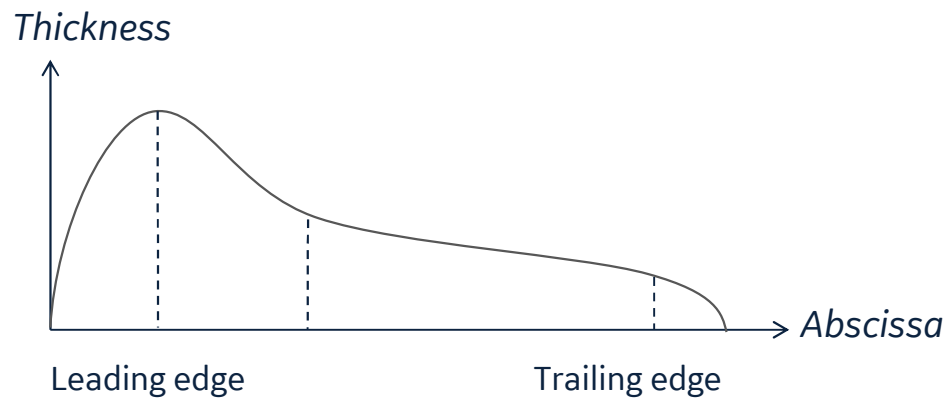
Elementary turbines



# Runner Design: Elementary turbines

## Each elementary turbine defined by:

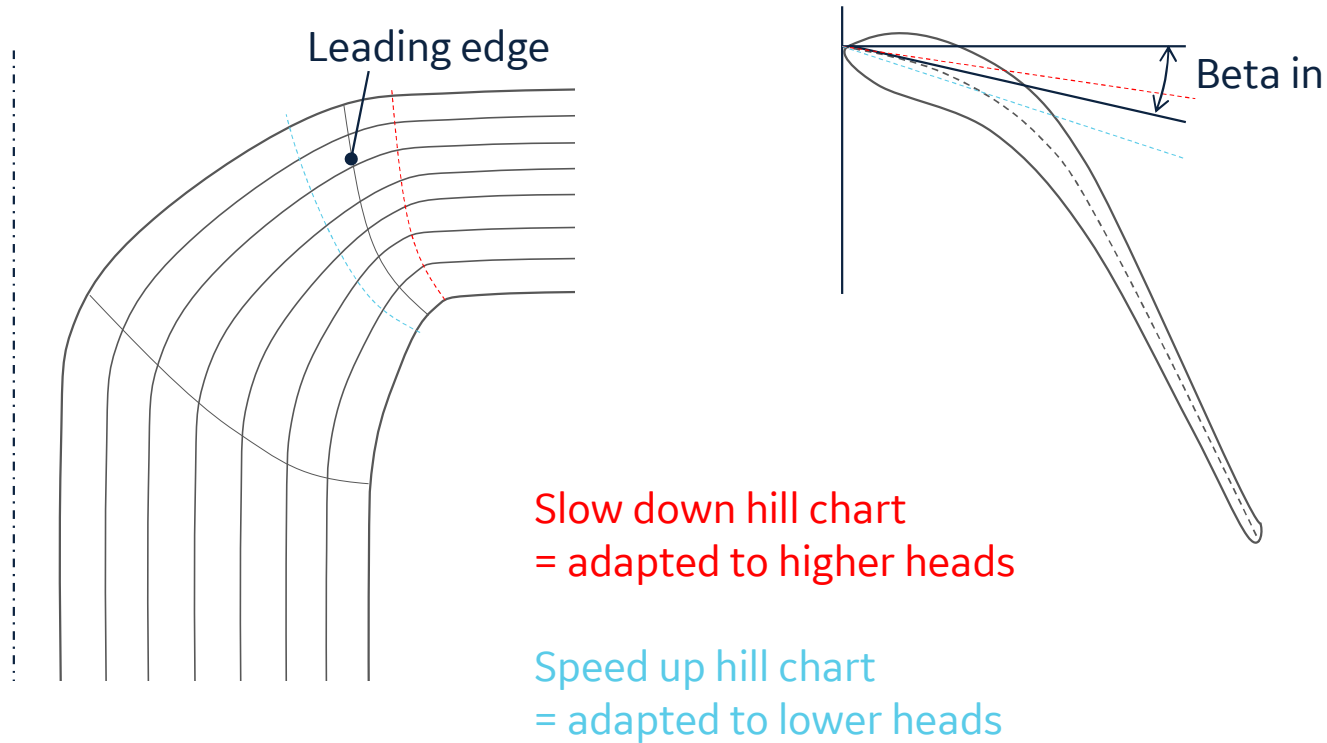
- 4 poles for curvature (6 coordinates)
- 3 abscissa + 3 thickness values



**For a typical Francis runner: 13 elementary turbines**

→ Up to 156 degrees of freedom!

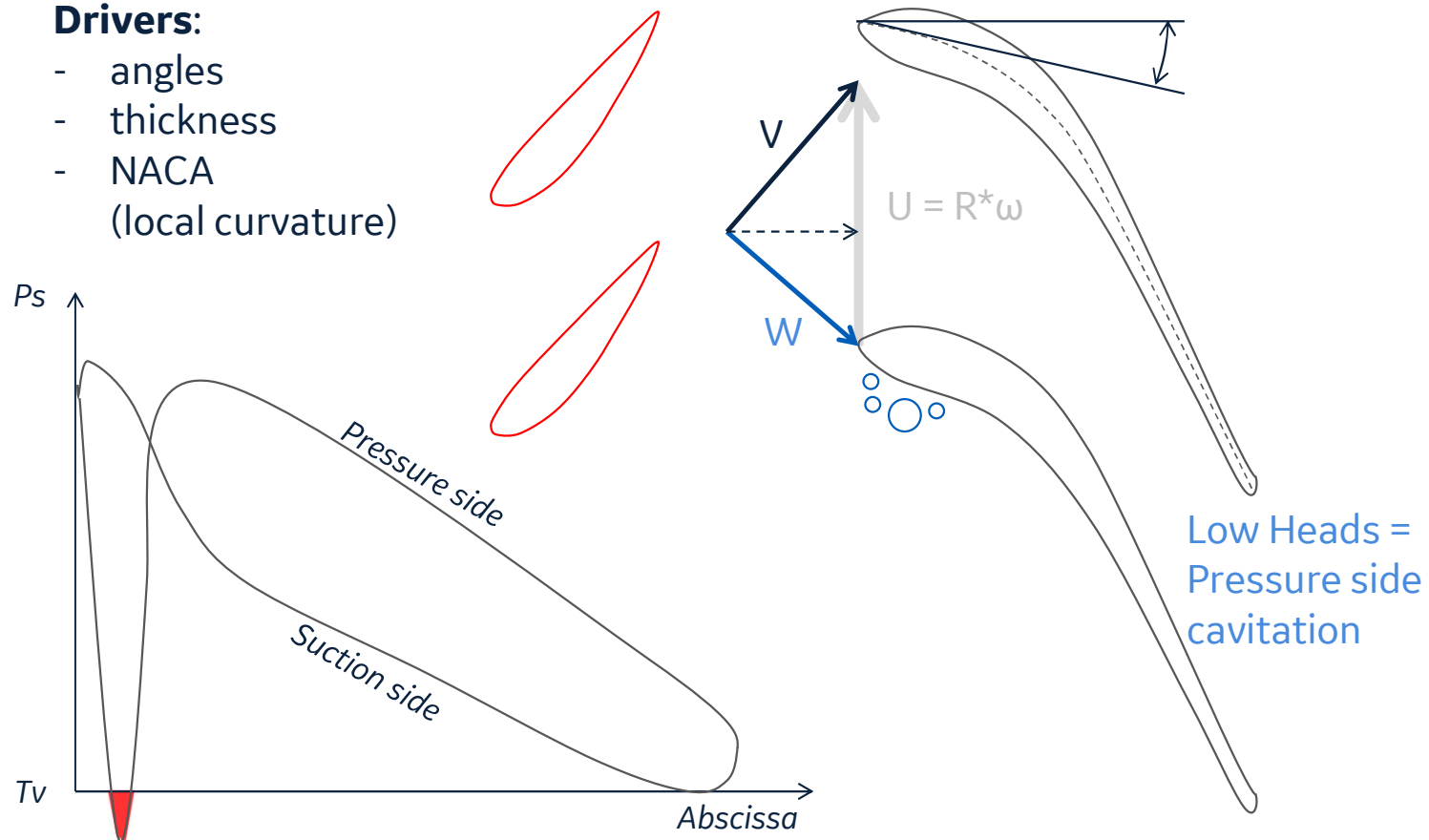
# Runner Design: Head adaptation



# Runner Design: Inlet Cavitation limits

## Drivers:

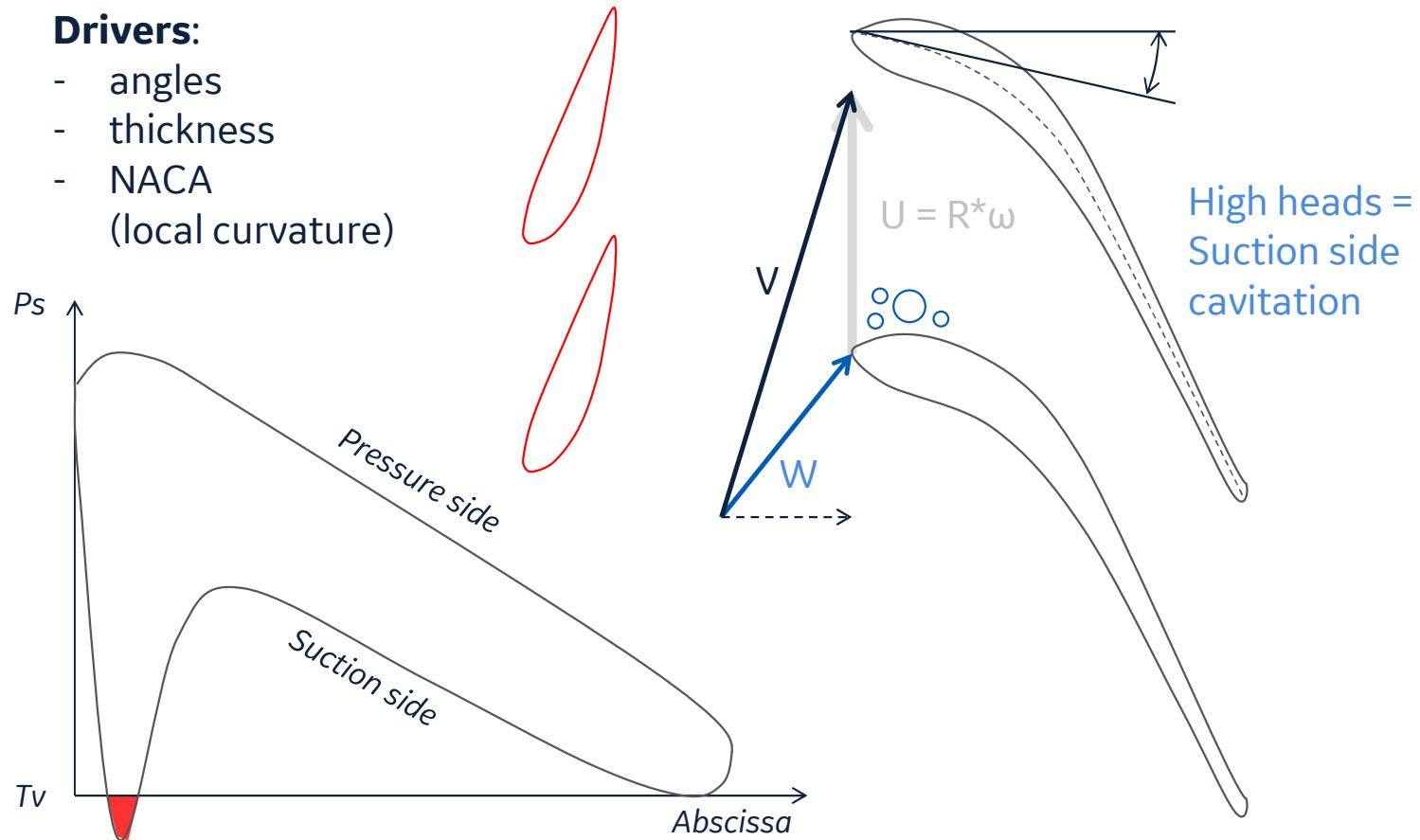
- angles
- thickness
- NACA  
(local curvature)



# Runner Design: Inlet Cavitation limits

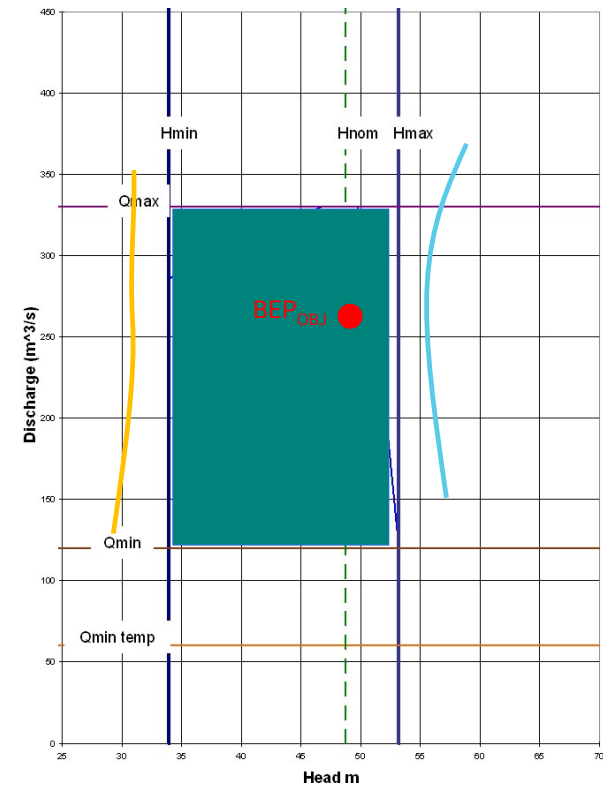
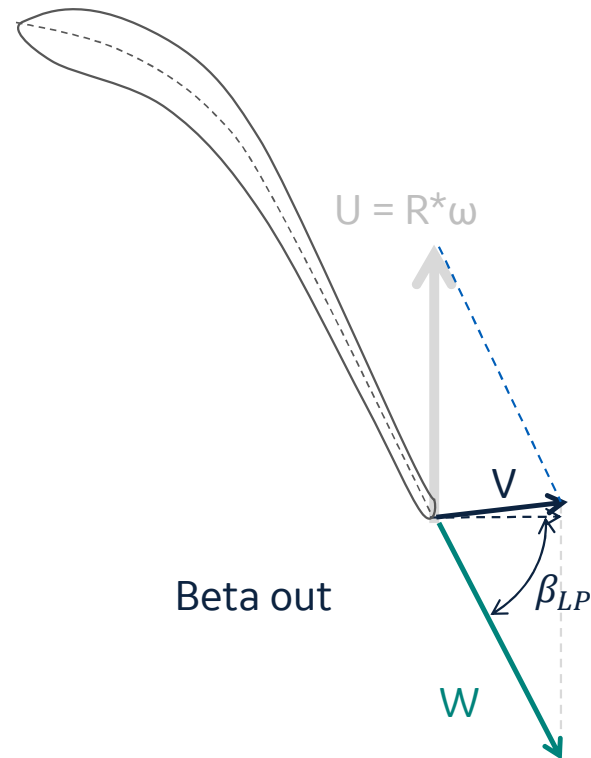
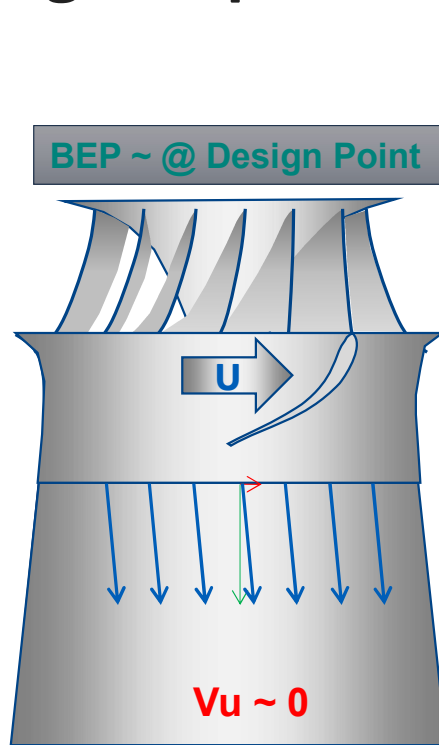
## Drivers:

- angles
- thickness
- NACA  
(local curvature)



# How to design a Francis runner ?

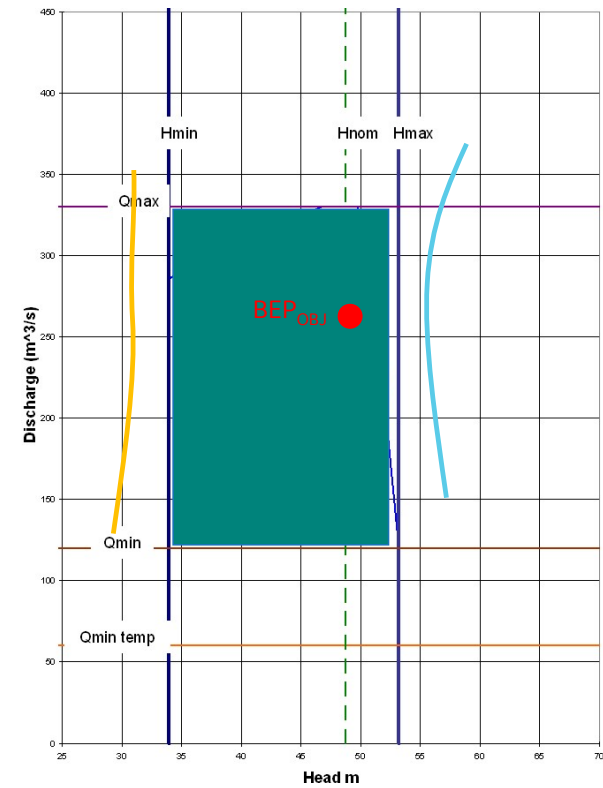
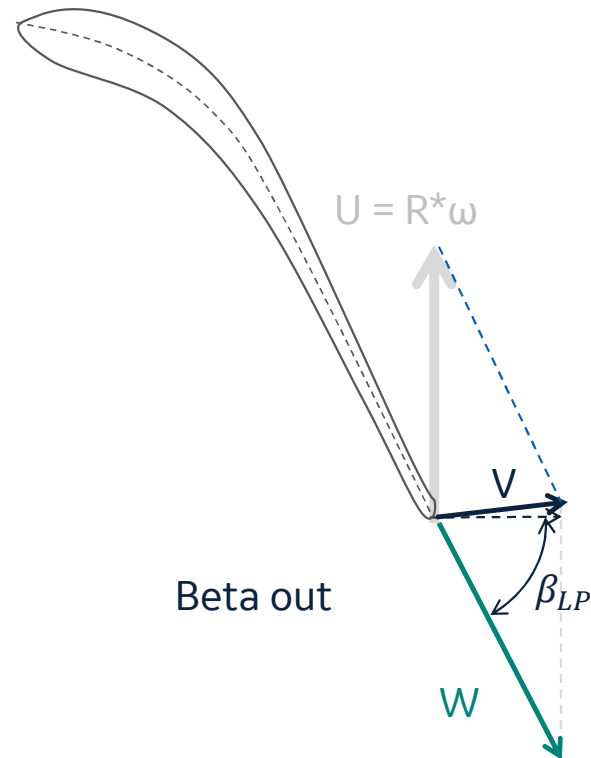
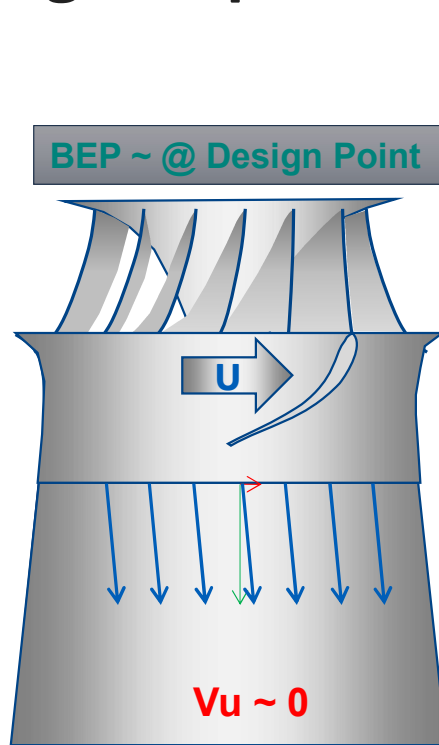
## Discharge adaptation





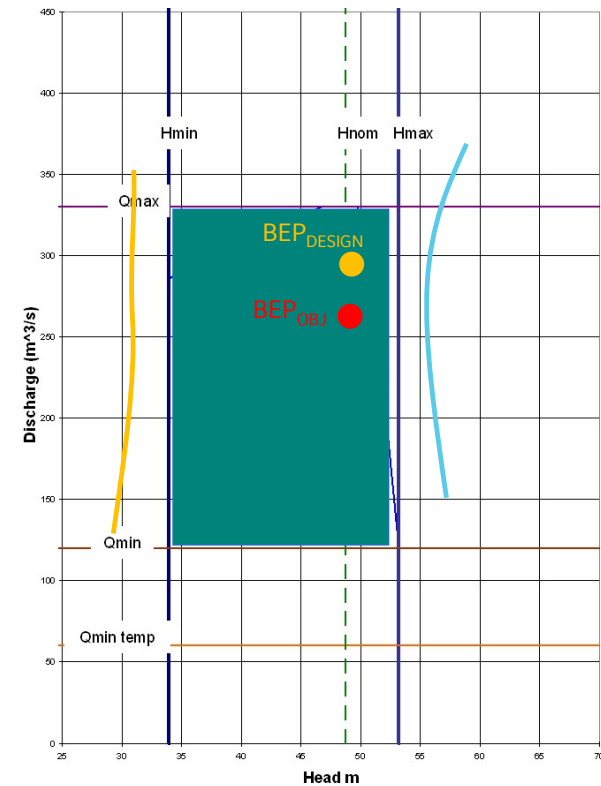
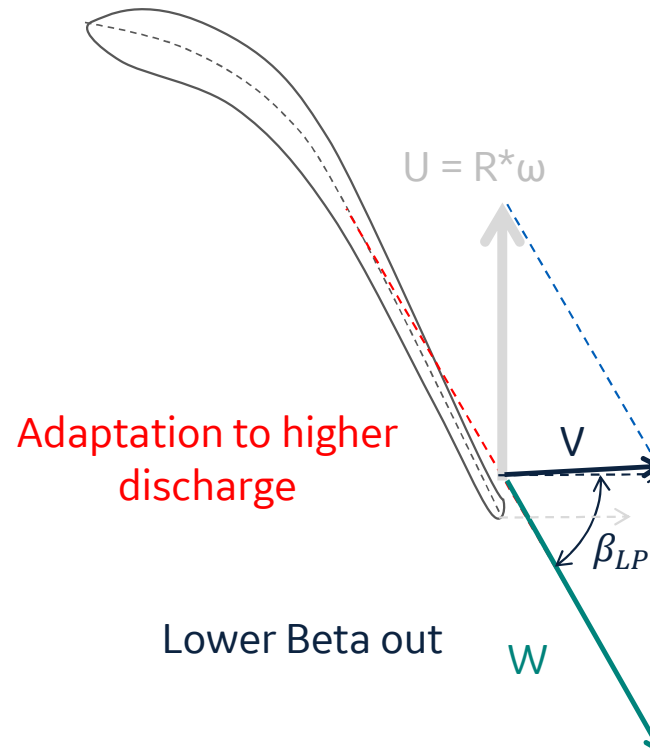
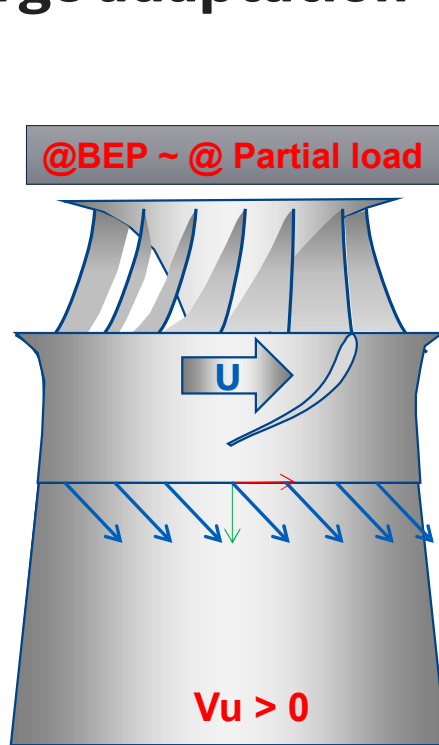
# How to design a Francis runner ?

## Discharge adaptation



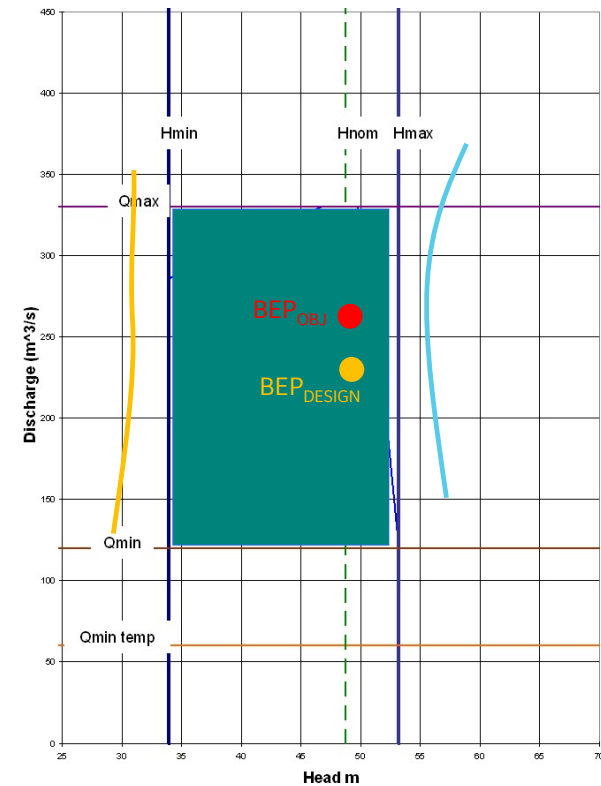
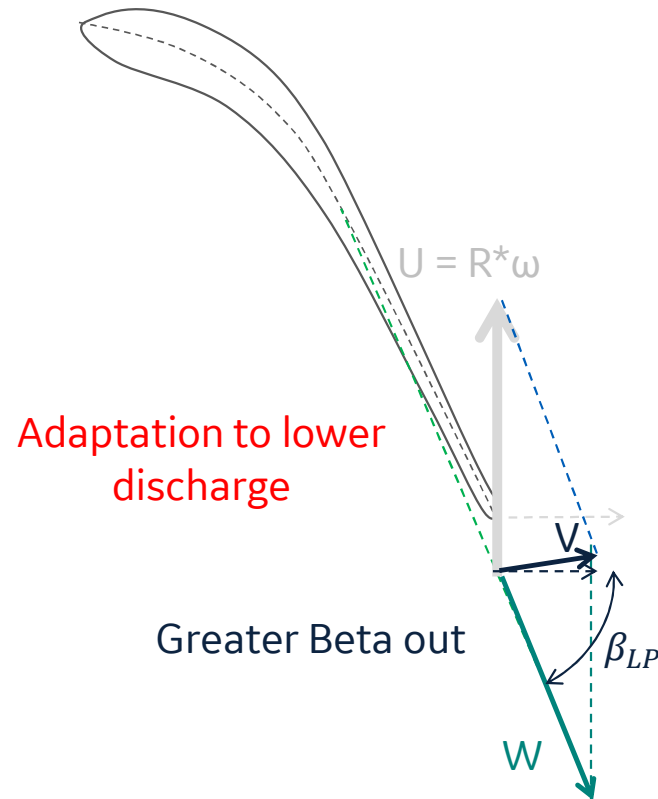
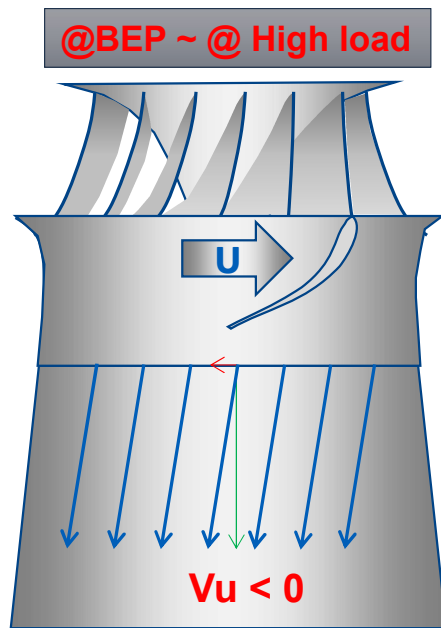
# How to design a Francis runner ?

## Discharge adaptation



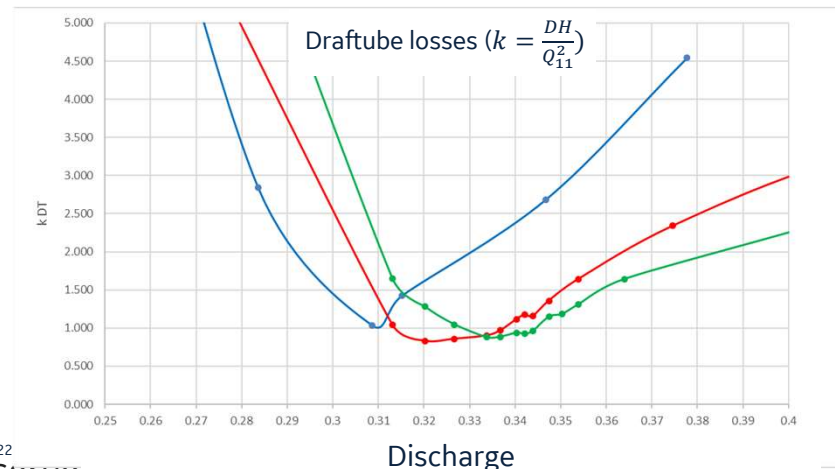
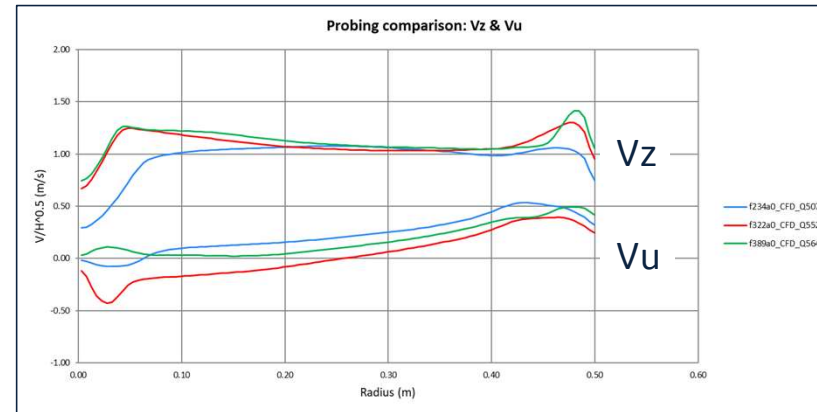
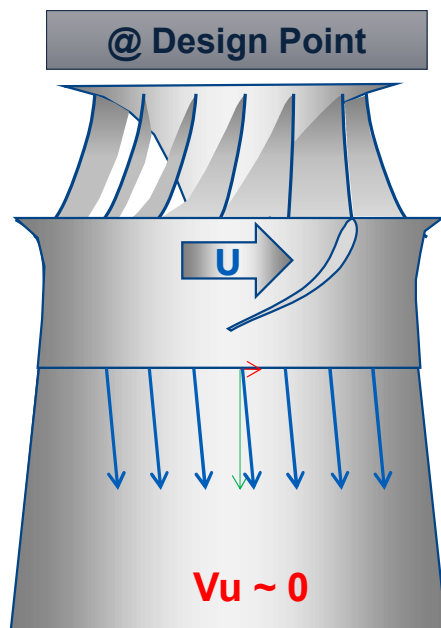
# How to design a Francis runner ?

## Discharge adaptation



# How to design a Francis runner ?

Discharge adaptation, one step further : How to be sure that the DT losses are minimum ?

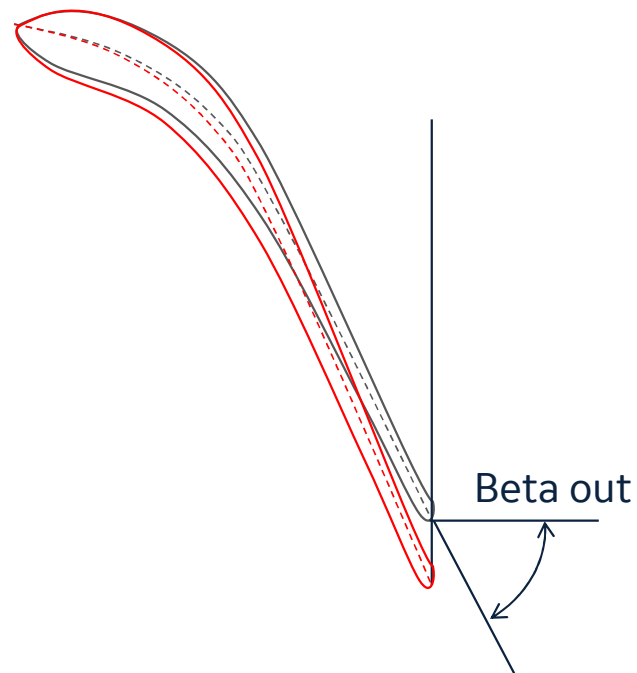
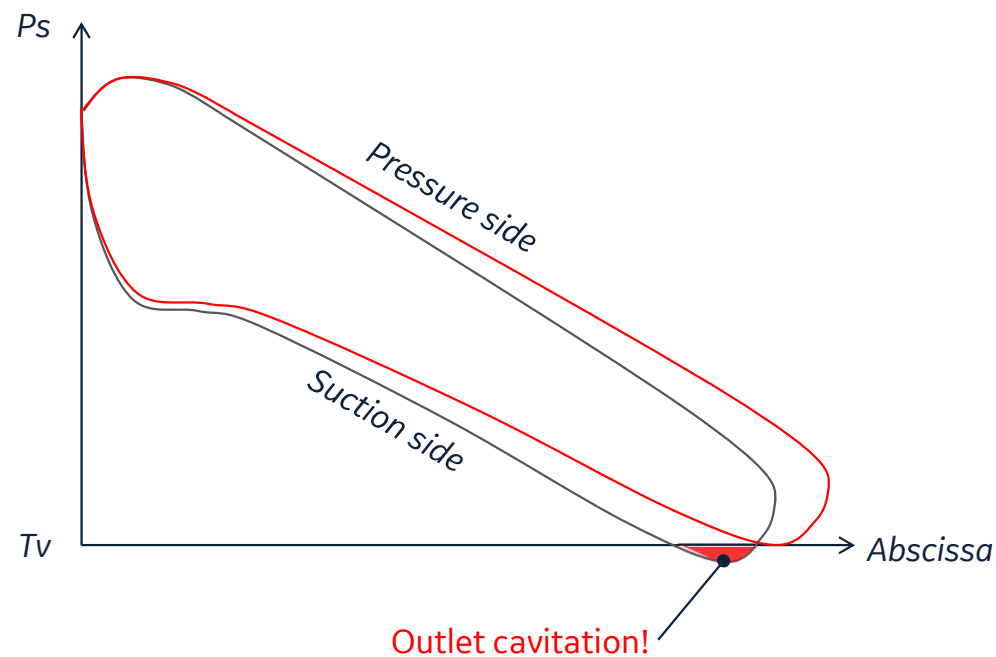


For different probing shape, losses in DT (and  $\eta$ ) can change a lot

# Runner Design: Outlet Cavitation

## Drivers:

- local curvature
- blade length
- number of blades

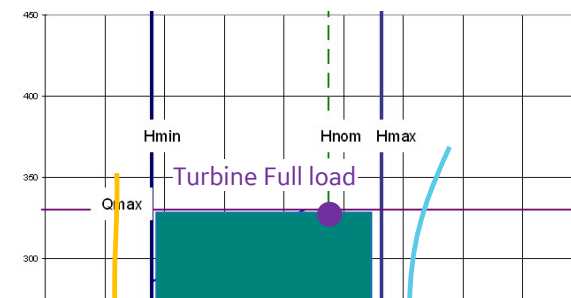
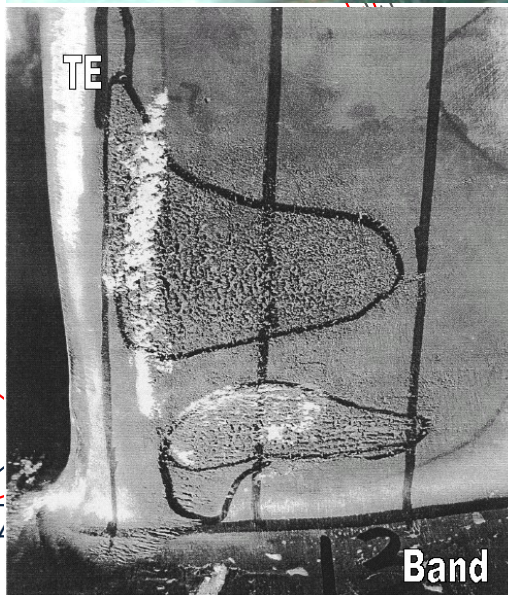
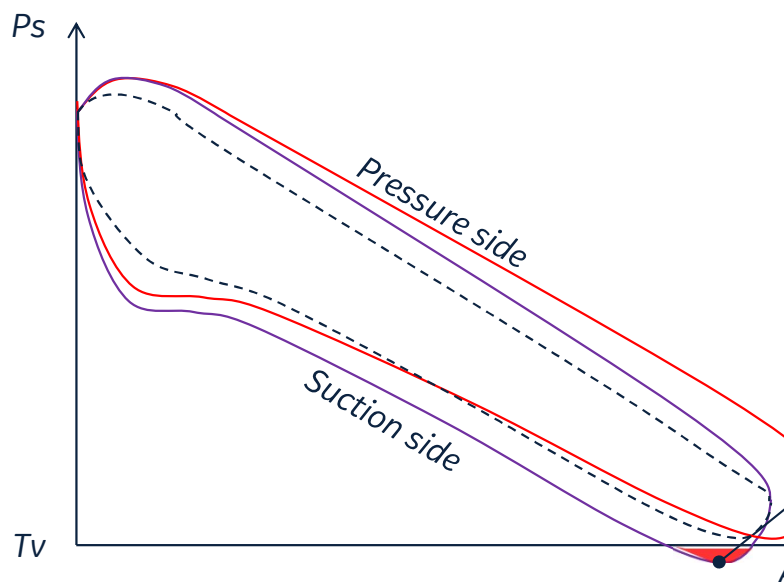


# How to design a Francis runner ?

## Outlet Cavitation limits

### Drivers:

- local curvature
- blade length
- number of blades



# Runner Design: Conclusion

## **Objectives:**

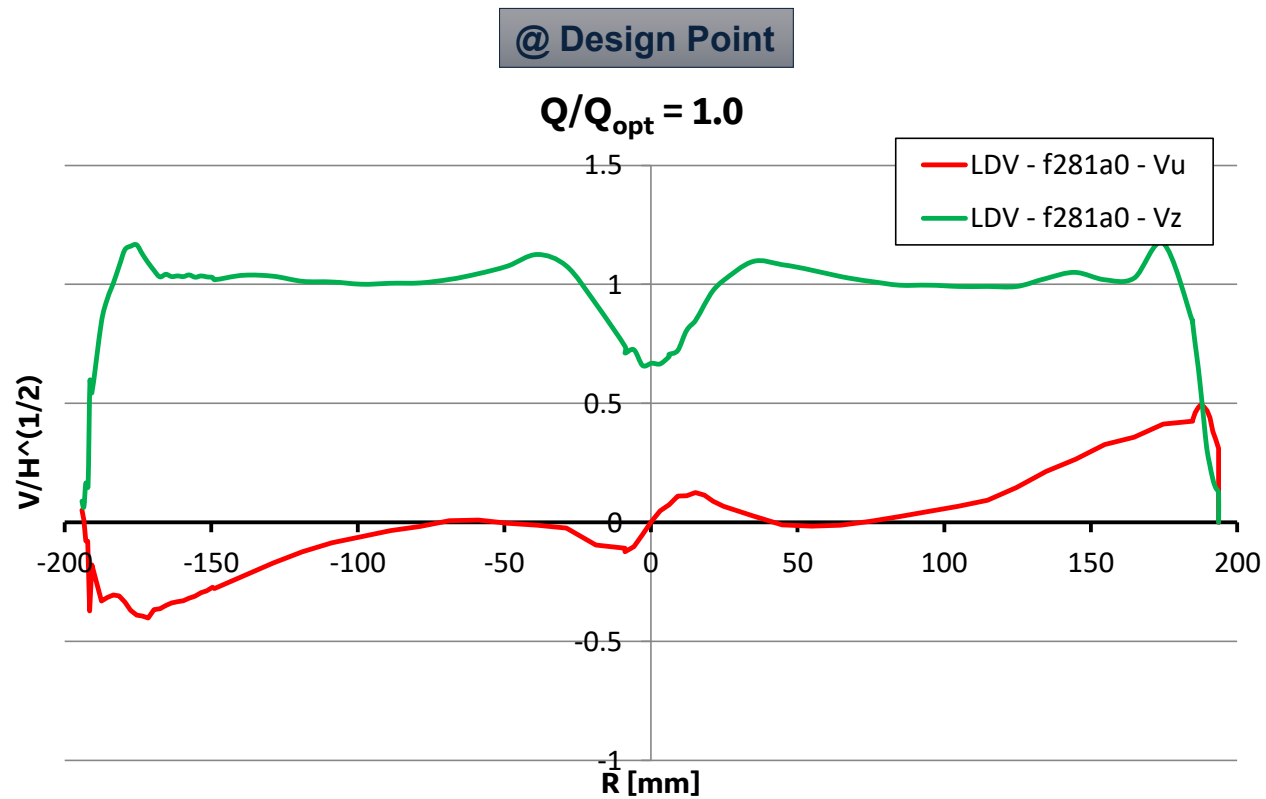
1. Minimize head losses to maximize efficiency (productivity)  
→ Short blades, low number of blades
2. Cavitation free in the whole domain, and especially to maximum discharge  
→ Long blades, high number of blades
3. Cheap solution  
→ Small runner... against 1 & 2

## **→ OPTIMIZATION**

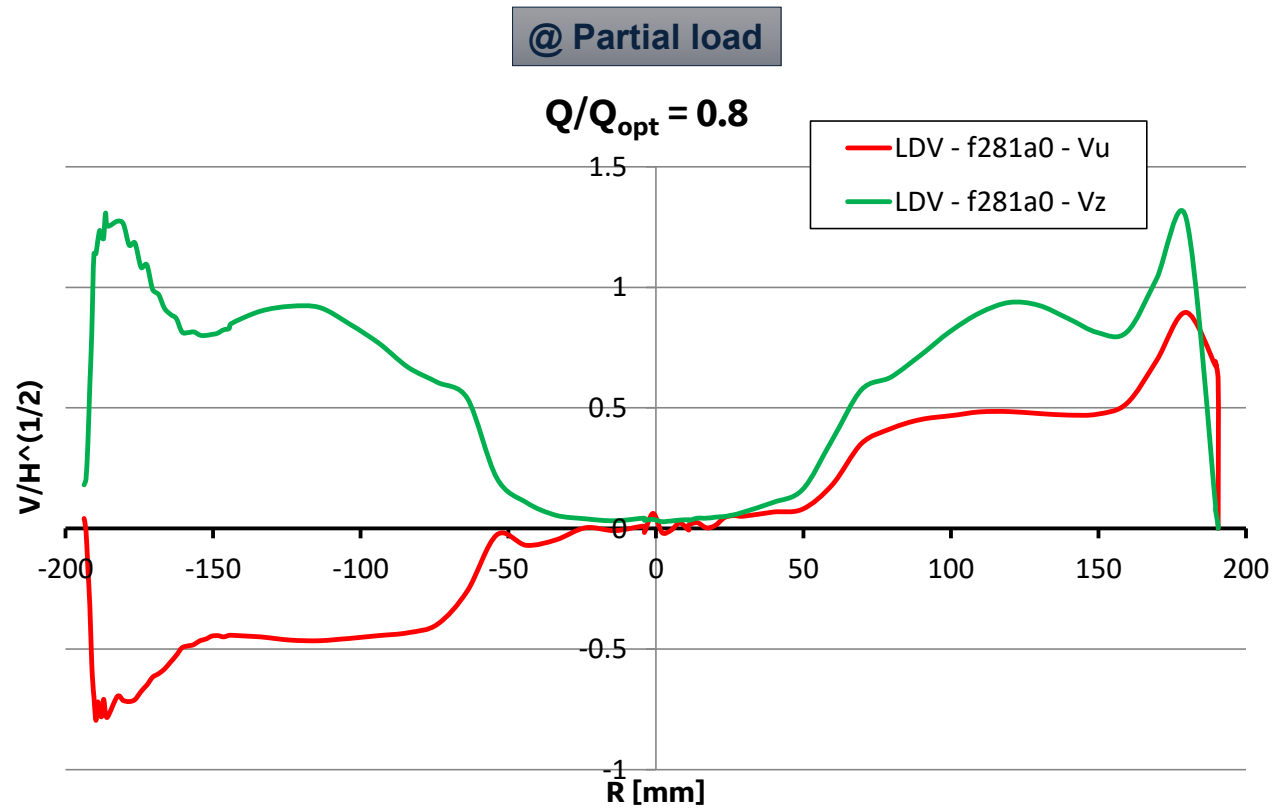
**Note:** In tendering (bidding before contract), the “natural” tendency is to sell the *best* efficiency with the *cheapest* supplies... then during execution stage this optimization might be difficult



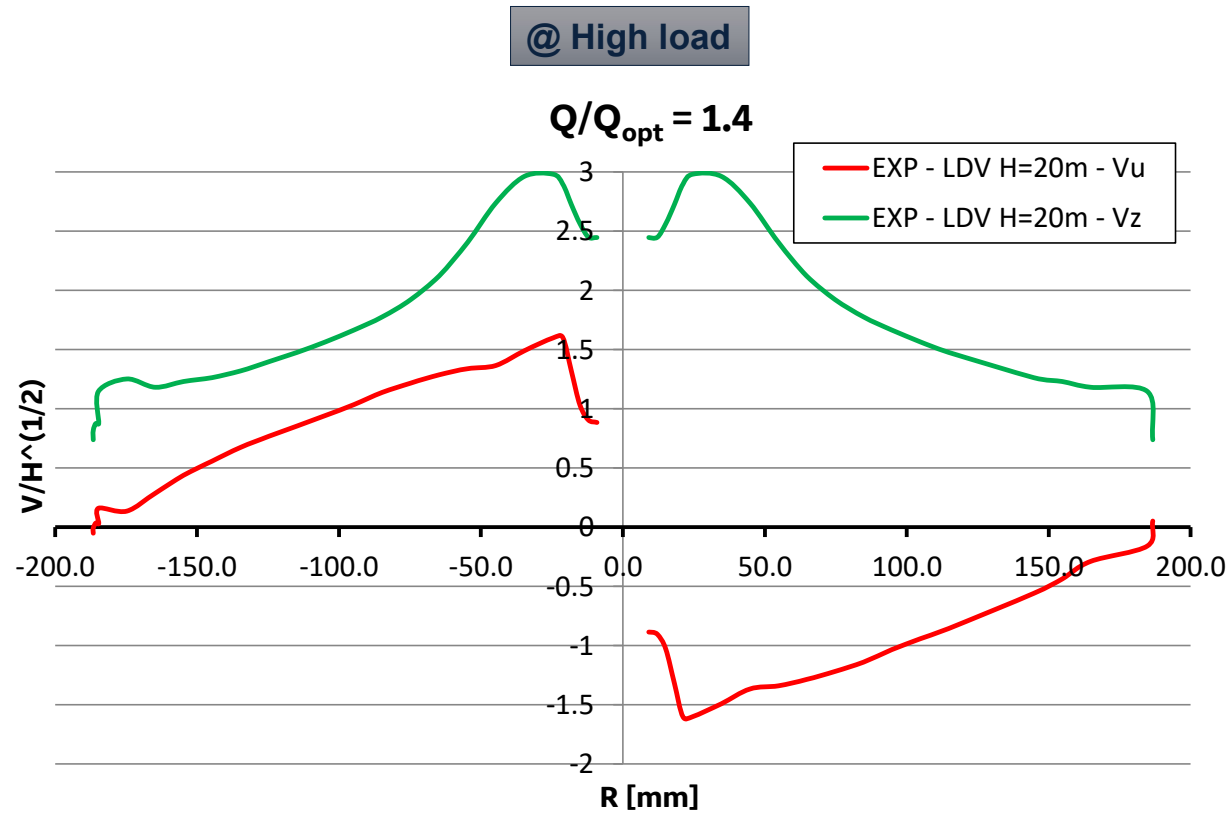
# Real Velocity Profiles (from Test Rig)



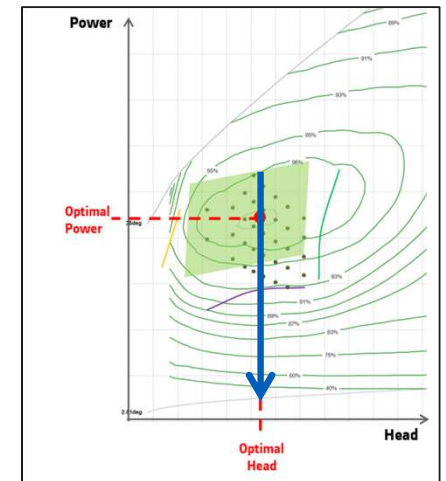
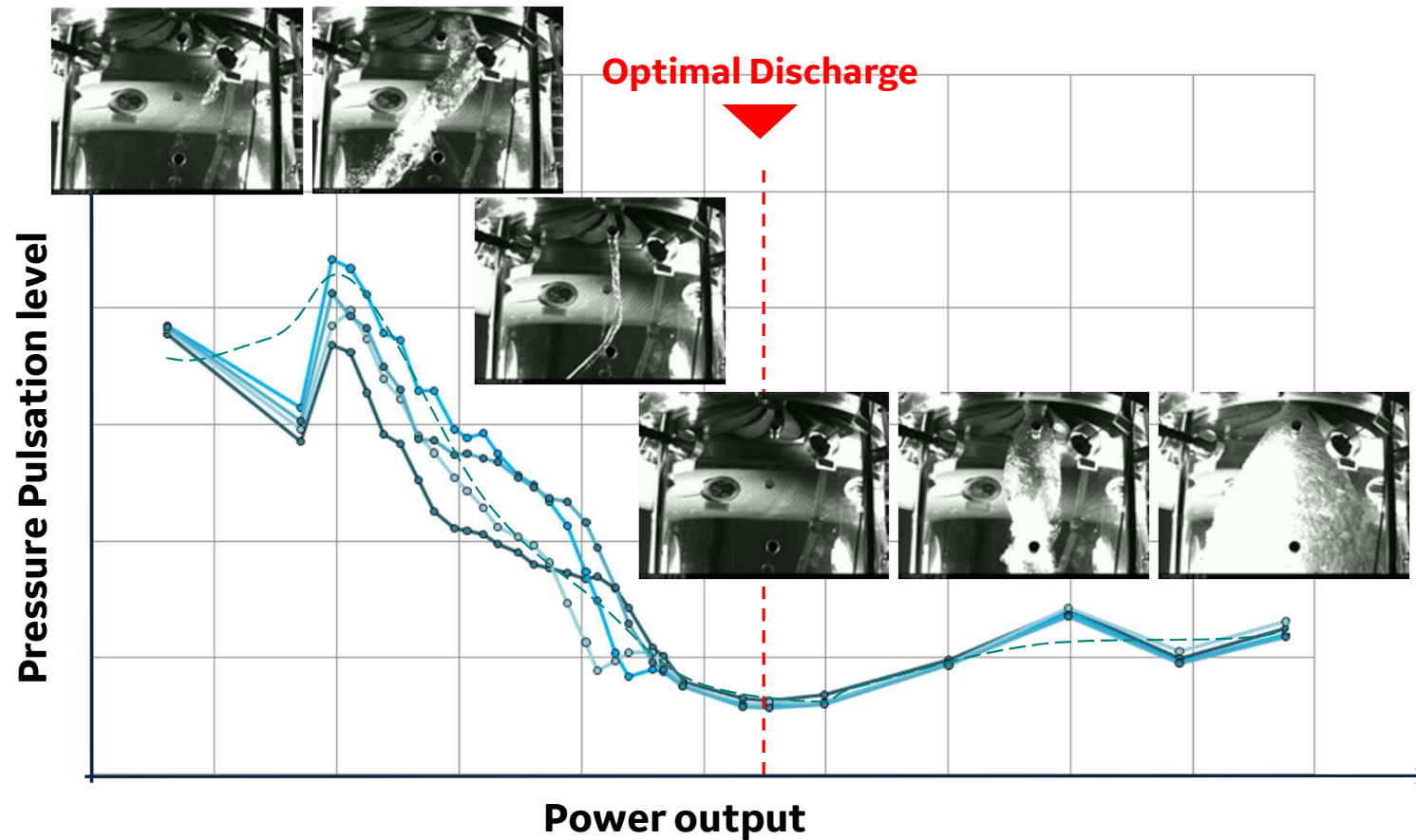
# Real Velocity Profiles (from Test Rig)



# Real Velocity Profiles (from Test Rig)

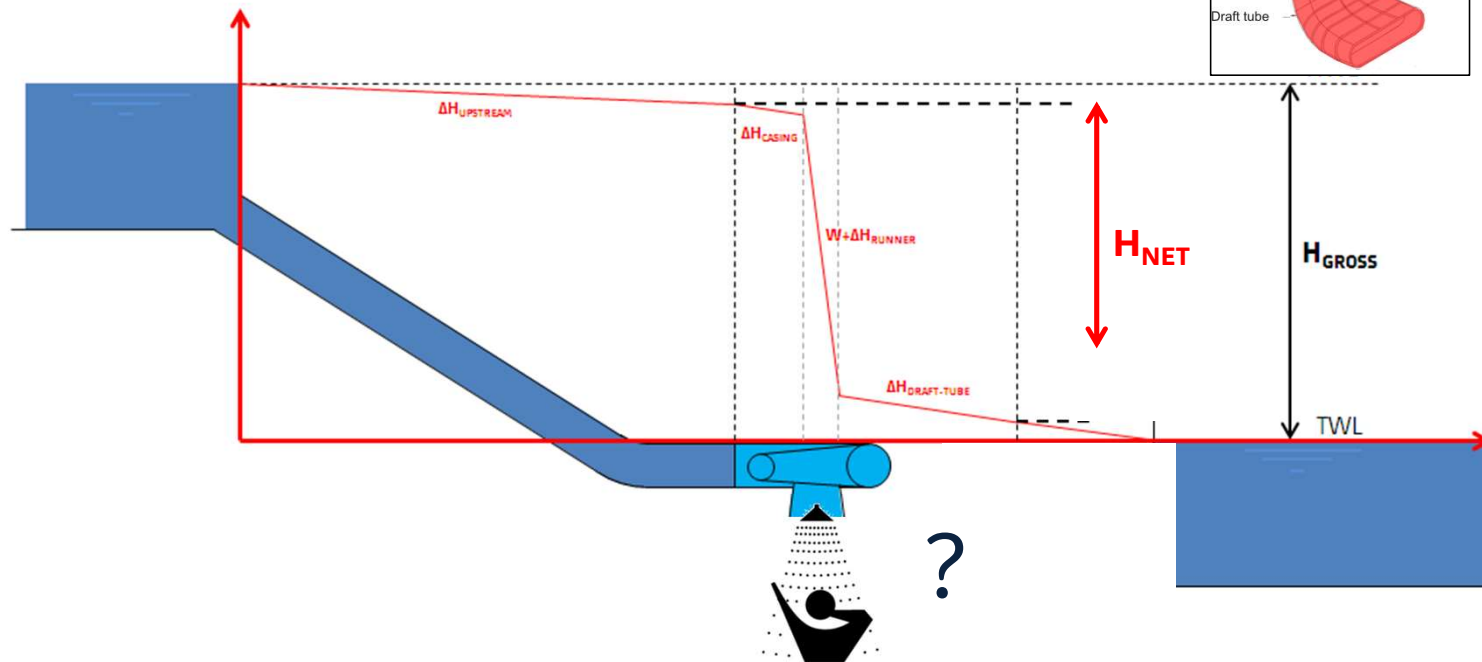


# Flow behaviour at Runner outlet



# Draft Tube what's it for?

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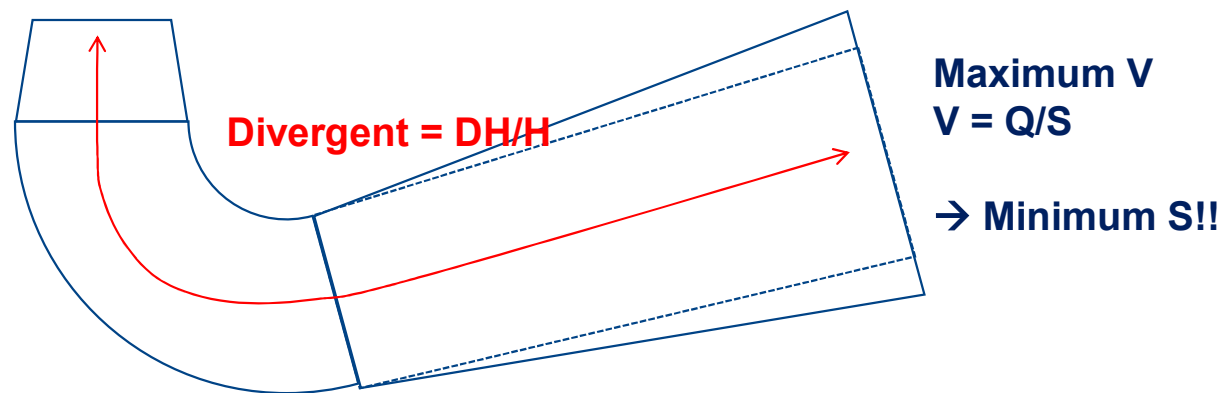
- Net Head**

$$H_n = H_b - \Delta H(A \rightarrow 1) - \Delta H(2 \rightarrow B)$$

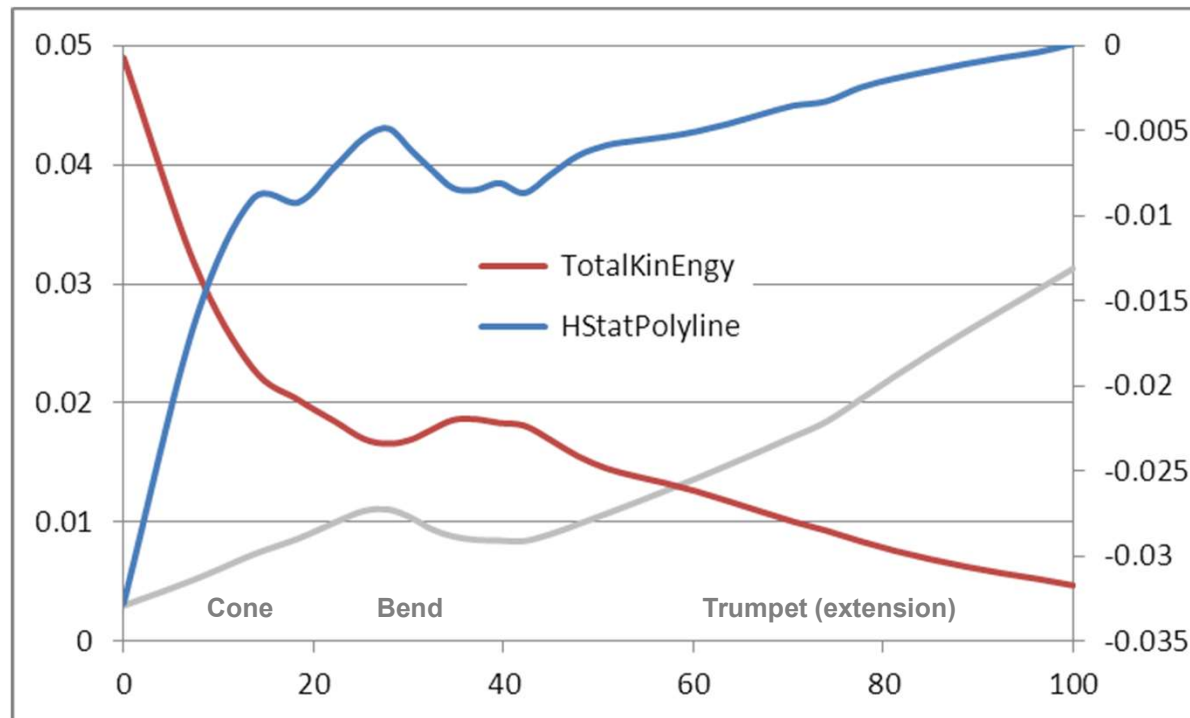
$$= H_b - kV_1^2/(2g) - \textcircled{V_2^2/(2g)}$$

# Draft Tube helps increasing the net head

- This is why Customers usually impose a **maximum flow speed** at draft tube outlet – otherwise the turbine supplier would tend to minimize the outlet section in order to increase its efficiency

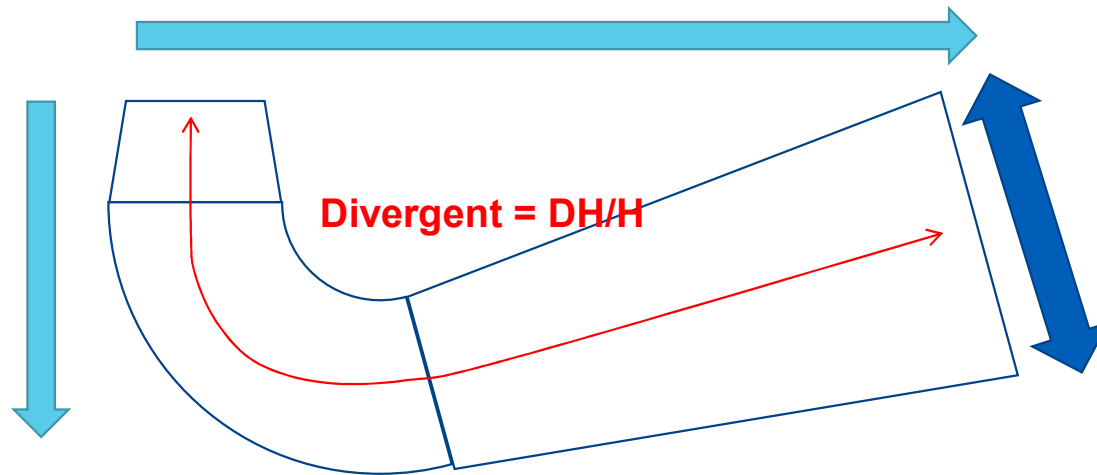


# Kinetic energy / static pressure evolution along the draft tube midline curvature



# What's a good Draft Tube like?

- To be the most divergent (Customer view point)
- To have the smallest head loss (Turbine supplier view)
- To be the most compact possible  
(Customer / Civil Work / Turbine supplier view....)







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# Conclusion on Hydraulic Design

# Conclusion



- Design process can be difficult and **iterative** if specific requirements (e.g. high head and/or discharge variation)
- High number or **degrees of freedom**  
→ makes the process difficult to automate (optimal design)
- Different levels of **trade-off** required at tendering and execution stages
  - Mechanical vs Hydraulic
  - Efficiency vs Cavitation
  - Efficiency vs Cost
- High added value of **experimented** hydraulic designers
- **No “off the shelf”** product: for each project, a specific design

# Elements to consider during a hydraulic design

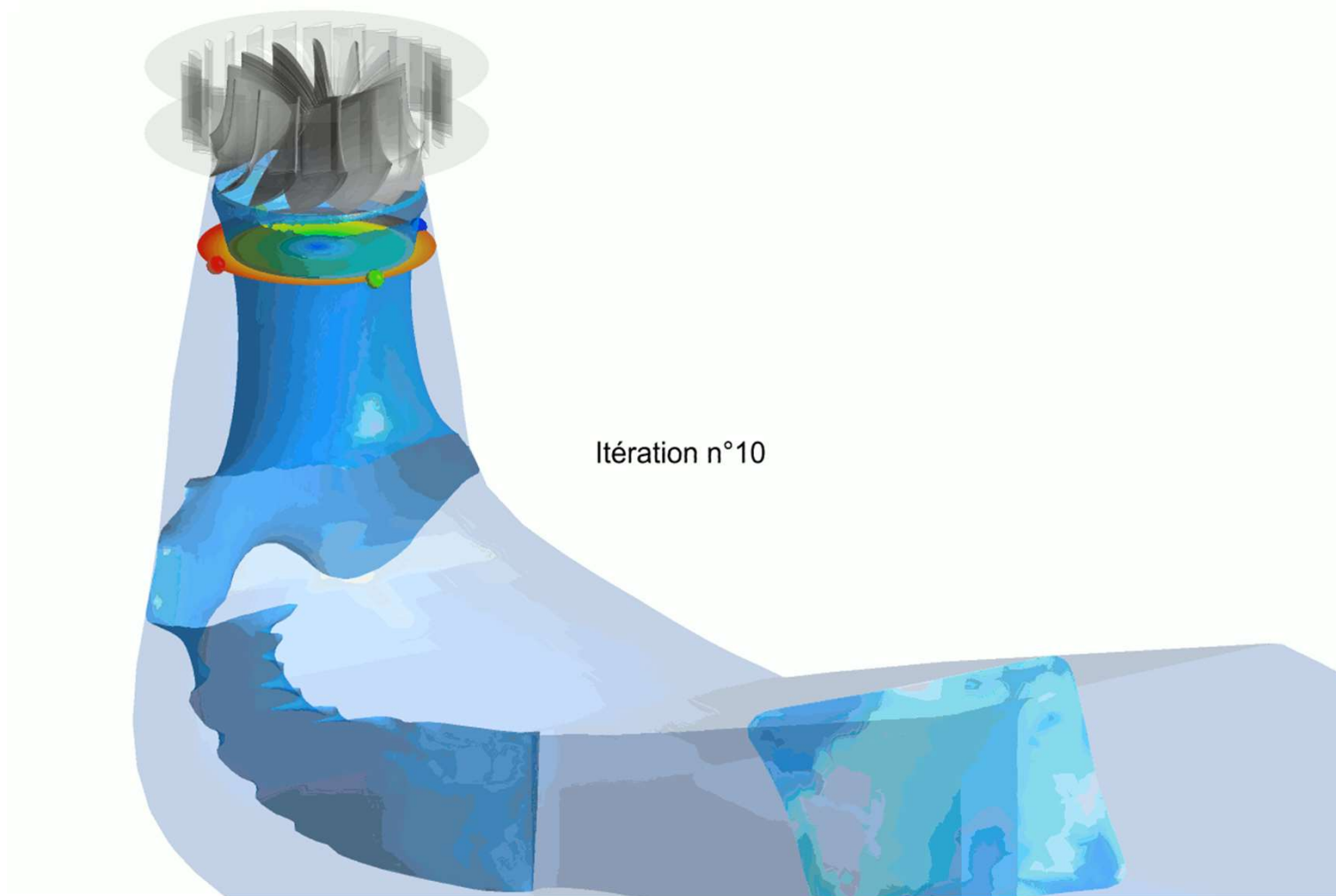


- **Efficiency** (WAE) / Output (different heads)
  - Checked on Model (step-up as per IEC 60193 / 62097) or Prototype (60041)
- **Cavitation** (erosion pitting as per guarantees, IEC 60609)
  - Cavitation margin ( $\sigma_P / \sigma_{s-1} > \dots$ ) on model test
  - Eroded volume on proto after 8000 hours (for ex.)
- **Pressure Pulsations** (limits set by customer)
  - Pressure pulsation level in Casing / Distributor / Draft tube... on model test
  - Pressure pulsation level on proto... but rather vibration (shaft line) and torque fluctuation (at generator outlet)
- **Runaway** (limit can be critical in case of refurbishment!)
  - Checked on model test... usually not on prototype!
- **Torque on Guide Vanes**
  - Checked on model test, dimensioning with margin on proto

# CFD vs Experimental: **Pressure Pulsations**



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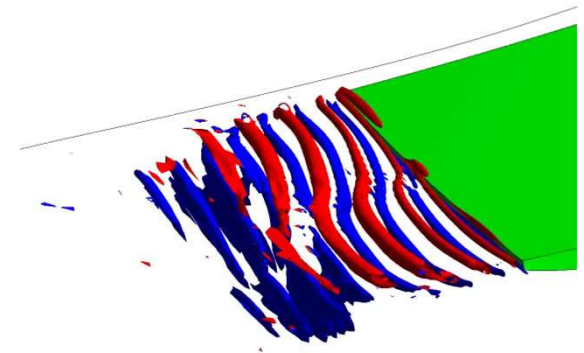
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# — On the mechanical side

# Mechanical impacts on hydraulic design

- Hydraulic profiles must be compatible with mechanical stresses
- Max allowable stresses will depend on the material (carbon steel, stainless steel –different types–) and on the manufacturing type
- What kind of stresses?
  - **Static head** (max when unit is stopped): Casing, Stay Vanes, Guide Vanes
  - **Transient head** (during starts & stops, in particular emergency stops):  
“H+deltaH” → May affect the whole turbine
  - **Centrifugal forces**: Runner at runaway
  - **Fatigue phenomena**:
    - Von Karman vortices (all profiles)
    - Part load Vortex Rope (runner + draft tube)
    - Rotor Stator Interaction (distributor + runner)



# Mechanical impacts on hydraulic design

- Spiral case → no blades, limited impact on hydraulic design
- Stay vanes → meant for mechanical purpose, **inertia** is needed
- Guide vanes → need for hydraulic tolerance, but also **inertia** (especially  $H + \Delta H$  when complex set-up with several units on the same penstock)
- Runner → need to stand  $H_{max}$ ,  $H + \Delta H$ , runaway (centrifugal force), **fatigue** linked to Inter Blade Vortices, Part Load Vortex Rope
- Draft tube → it “does see the head”, but still... elements that are not embedded may suffer **fatigue**, especially because of Part Load Vortex Rope



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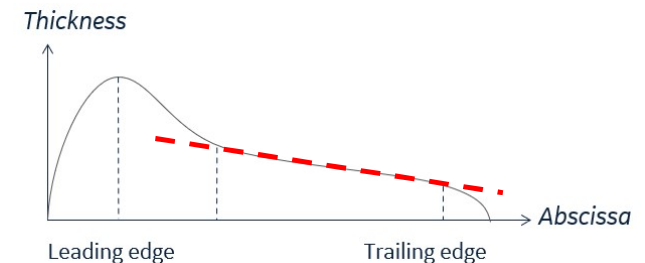
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# Manufacturing considerations



# Manufacturing types for the runner

- **Welded fabricated** → Band and Crown come in forged pieces, Blades are casted, a welding is needed on each side of the blade
- Blades quality might not be optimal especially in the low thickness areas. A specific thickness **slope** is required to grant a good quality during the cooling down.
- Welded zone is the fillet radius (blade vs crown or band), which is precisely the area of stress concentration, some **residual stresses** are to be considered: max allowable stress is lower compared with other manufacturing types
- Classical for big units (some even have to be welded at site!)

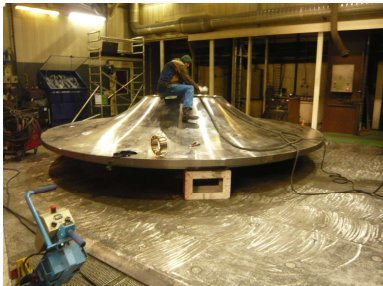


+ Good finish quality (surface finish)

– Expensive, lower admissible stress

# Runner manufacturing

## **Welded Fabricated** with separate elements



Element pre-machining



Element assembling



Pre-heating & welding



Final machining

# Runner manufacturing

## **Welded Fabricated** with separate elements

Runner at site  
in one piece



Or manufactured closed to the site. Ex. Three Gorges runner

# Manufacturing types for the runner

- **Casted Monobloc** → One unique cast for the whole runner
  - Typically used for small units, where no access in between blades for welding... but it has the same problem as the blade casting (average quality)
  - AND the surface finish can hardly be as good all over the hydraulic shapes

+ Cheap and quick to manufacture

– Poor quality (shape and surface)



# Manufacturing types for the runner

- **Forged blocks** → Runner machined in one or several blocks
  - Applicable for medium runner where the surface is fully reachable for machining
  - Bi-blocks can be a solution when a welding is possible in the middle of the blades

+ Excellent material quality (forging)  
+ 3D shape very well respected  
+ No residual stress in the fillet radius

– Expensive, limited in size

# Runner manufacturing

## **Bi-block** with welding in the middle of the blades



- **1650mm diam.**
- **ns ~ 260 HP**

# Runner manufacturing

## **Bi-block** with welding in the middle of the blades



- **2700mm diam.**
- **ns ~ 110 HP**



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