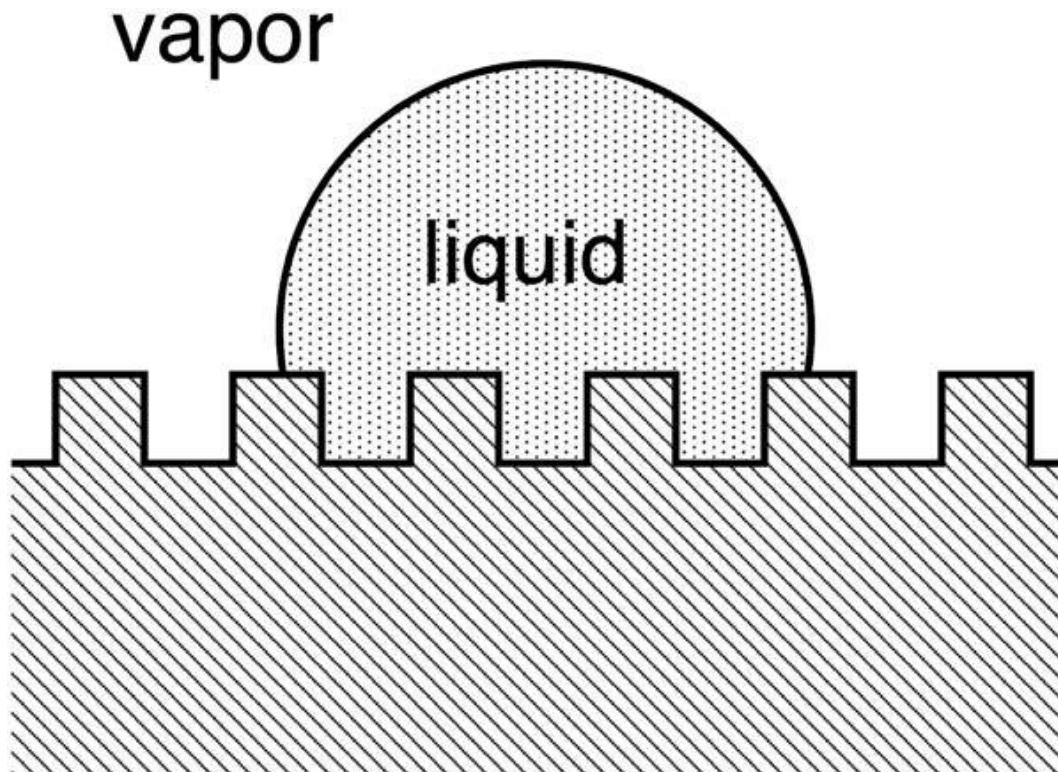


Last Time

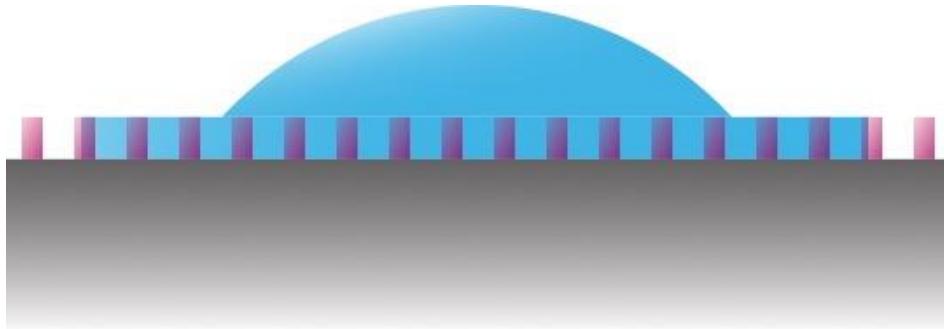


Wenzel state

Liquid penetrates through the surface structure underneath the droplet, yet not spreading further

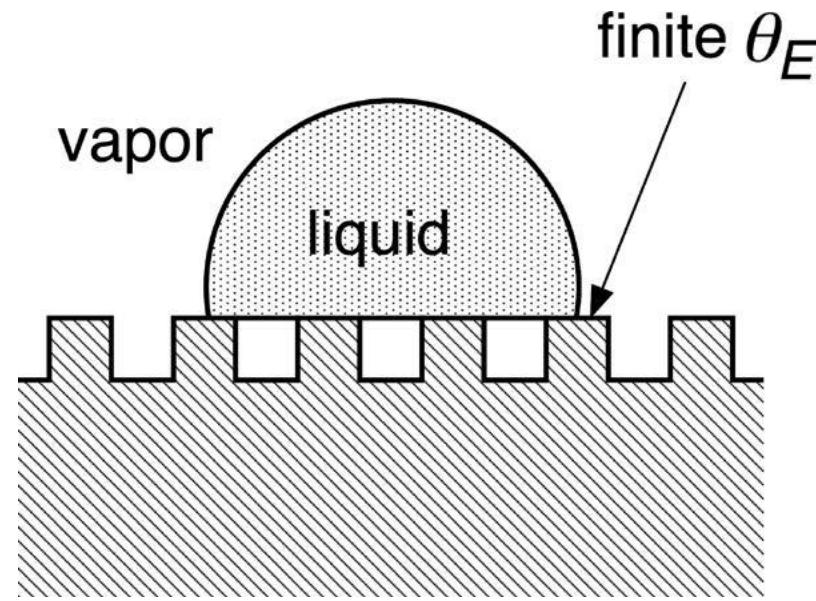
Figure 3.19 in Carey

Hemi-Spreading State



Liquid penetrates into surface structures
ahead of macroscopic contact lines

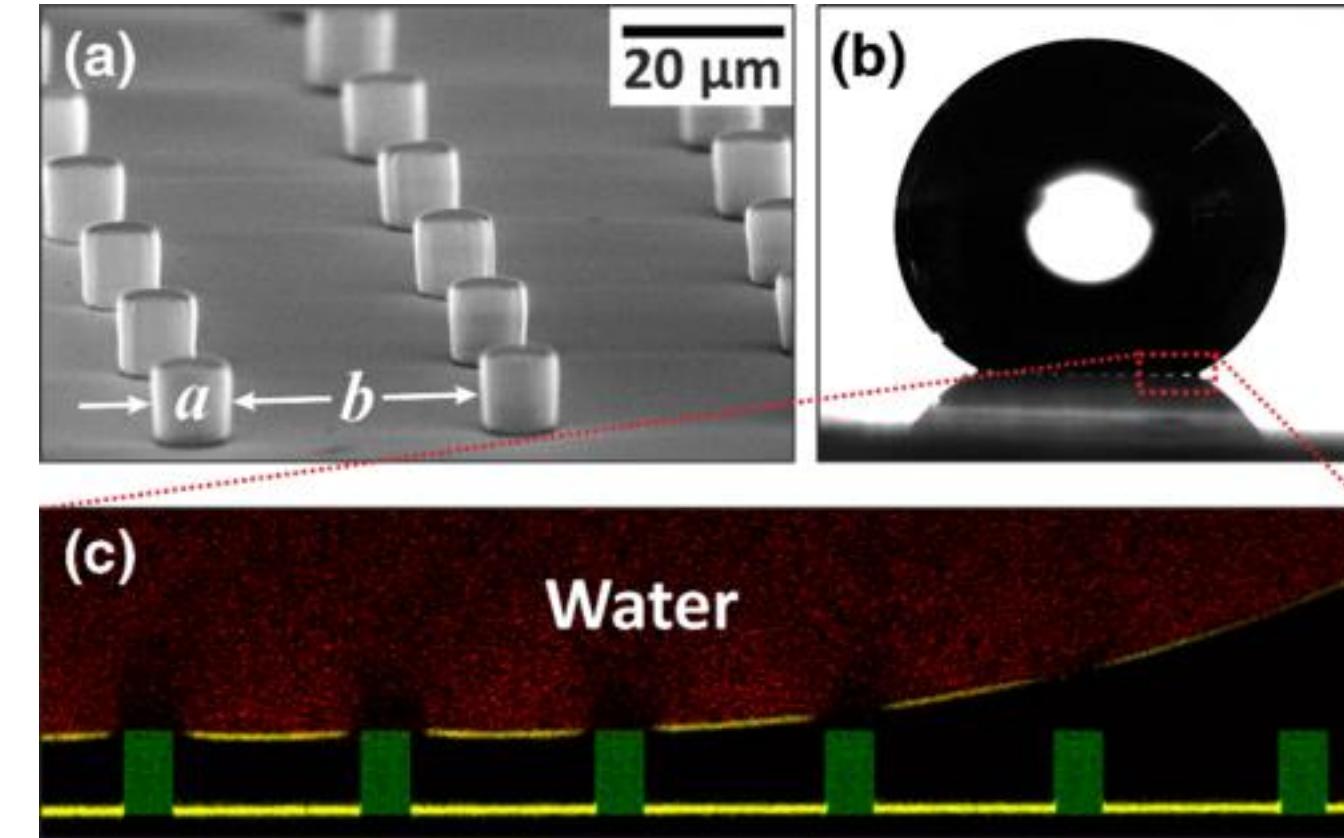
Cassie-Baxter State



Air/vapor trapped between the roughness elements underneath the droplet

Figure 3.23 in Carey

Conditions for Air Pocket Formation



Capillary pressure
preventing liquid from
entering surface structures

Schellenberger et al., *Physical Review Letters* 2016

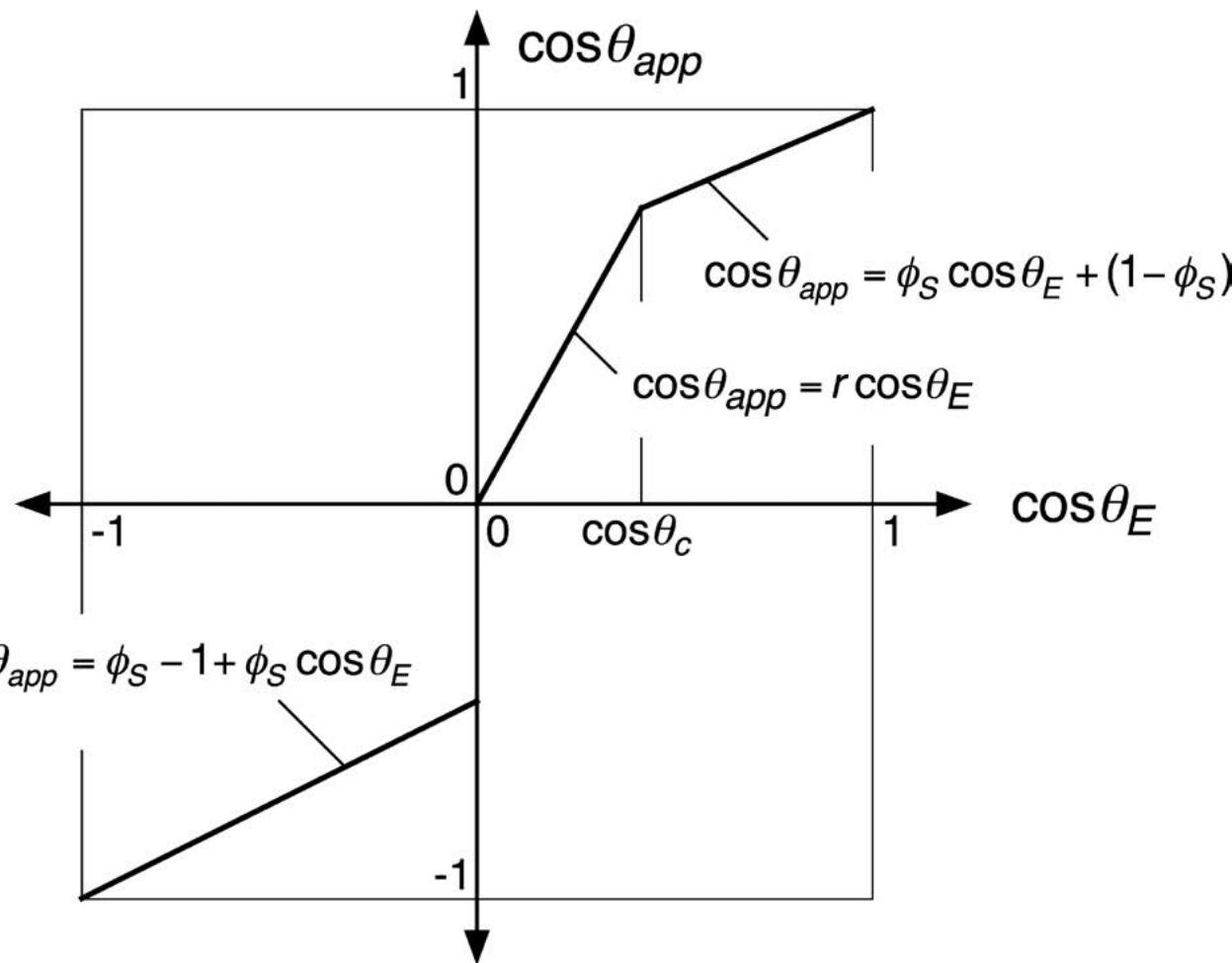
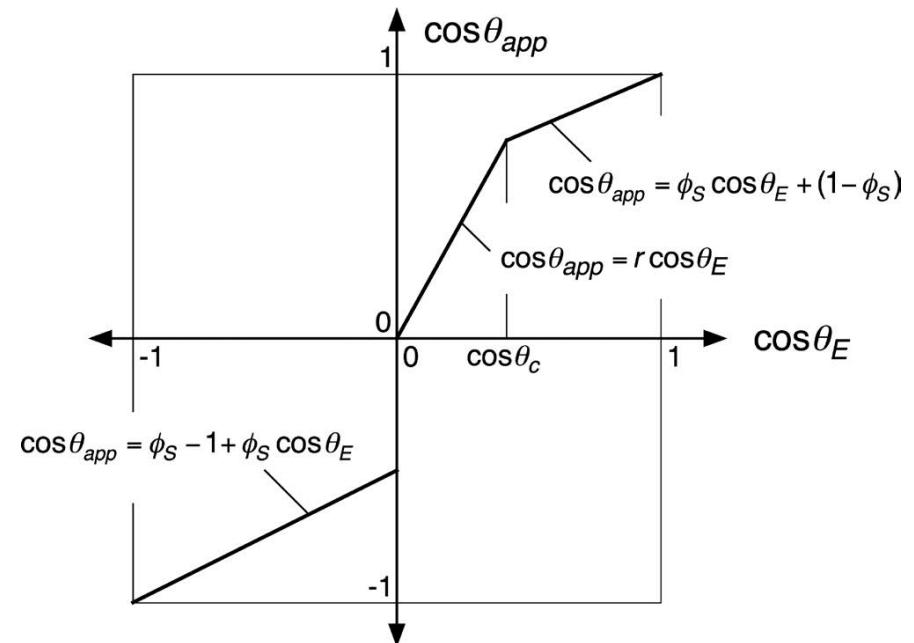


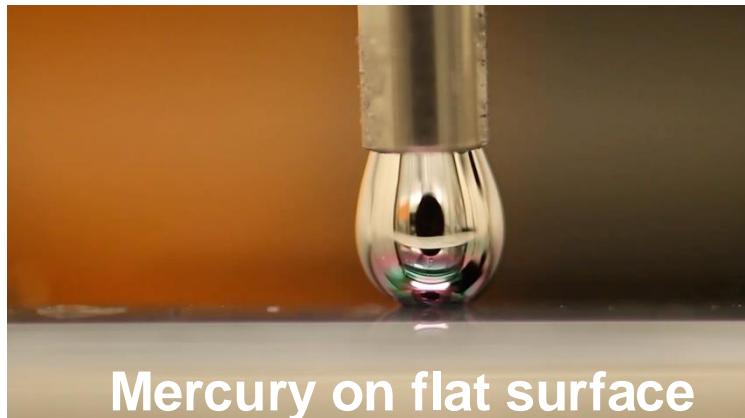
Figure 3.24 in Carey

Omniphobic Surfaces

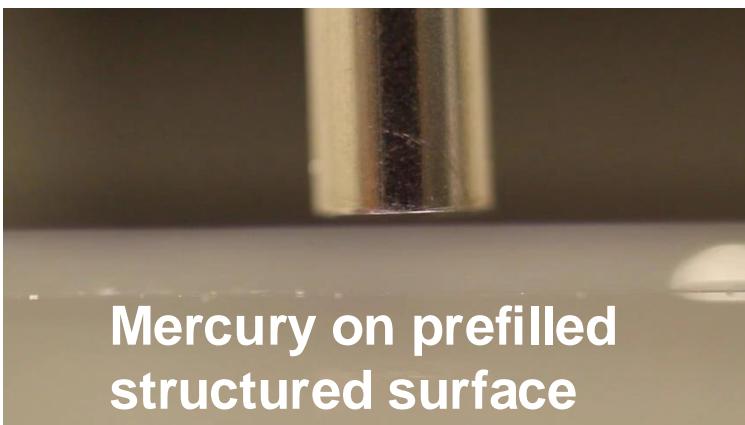


Liu *et al.*, *Science* 2014

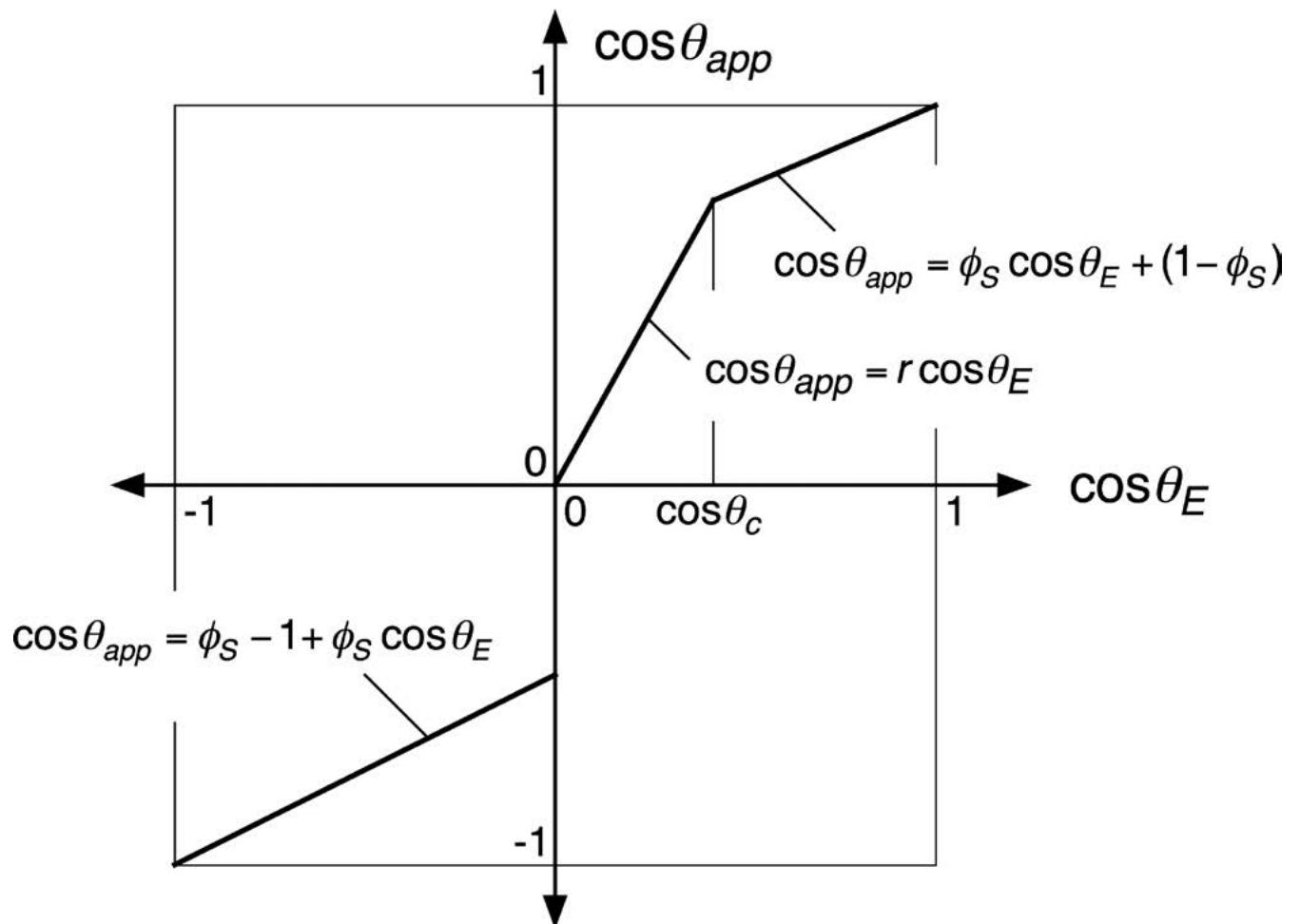
Omniphilic Surfaces



Mercury on flat surface



Mercury on prefilled
structured surface



Intended Learning Objectives Today

- Explain and apply the **Fick's Law of Diffusion**
- Apply heat and mass transfer analogy to **convective mass transfer**
- Explain the **coffee ring effect**

Reading materials: **Lienhard** Chapter 11, **Bird** Chapter 17

Fundamental Picture of Evaporation in Air



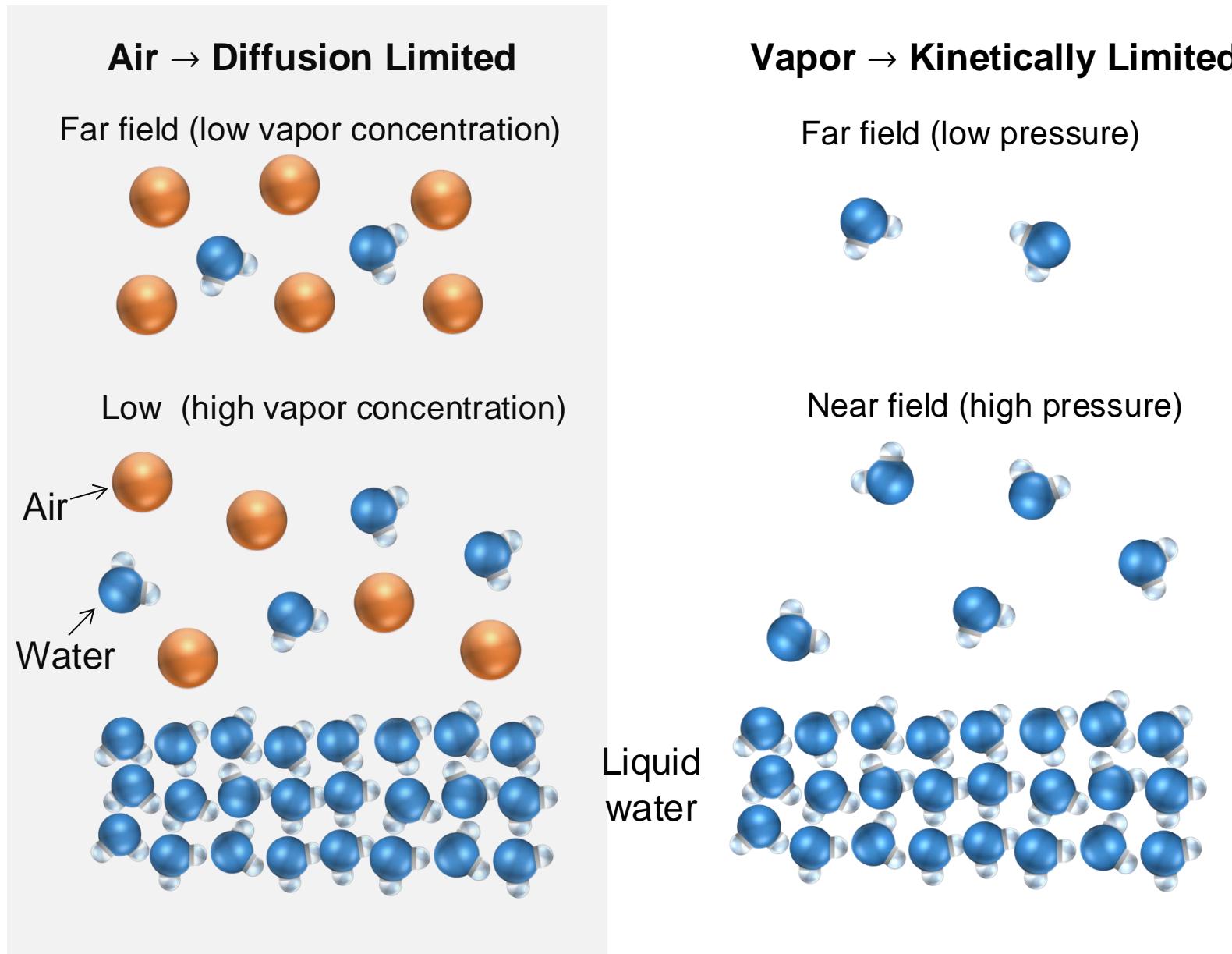
Evaporative cooling tower

Fundamental Picture of Evaporation in Vapor



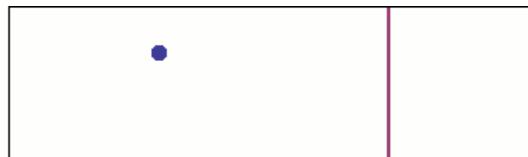
Vapor chamber cooler

Fundamental Picture of Evaporation

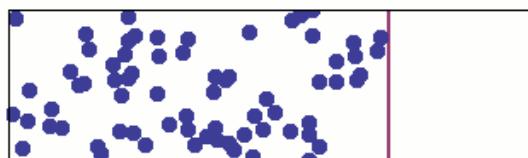


Transport of Water Vapor in Air

- Moist air modeled as a binary mixture: **water vapor + dry air**
- **Molecular diffusion:**



Molecules in the mixture move around randomly

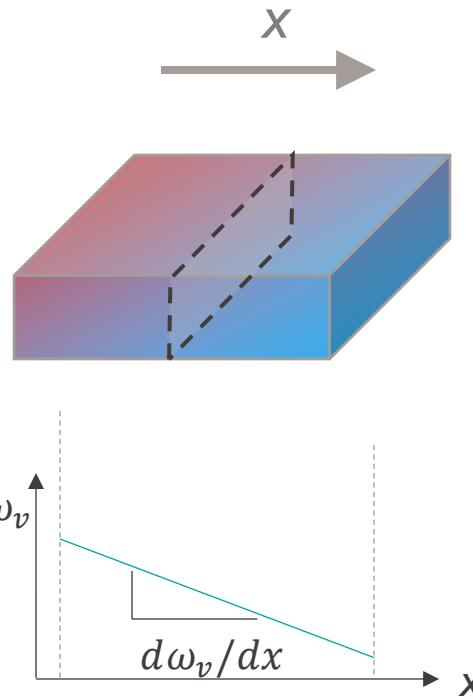


Spontaneous mass transfer from more concentrated region to less concentrated region



Fick's law wiki page

Fick's Law of Diffusion for Moist Air



$$j_{\text{vd}} = -\rho D_{\text{va}} \frac{d\omega_v}{dx}$$

Mixture Mass Average Velocity

Applying the gradient operator ∇ onto a scalar field gives you the direction and in which the scalar value increases most quickly

The magnitude determines how fast the increase is in that direction

What Affects D_{va}

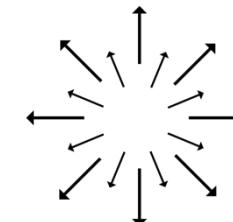
- Temperature
- Total gas pressure
- Composition of the mixture
- Correlation can be found in literature (Eq. 11.34 in Lienhard)



Applying the divergence operator $\nabla \cdot$ onto a vector field gives you the local sink term for the field flux:

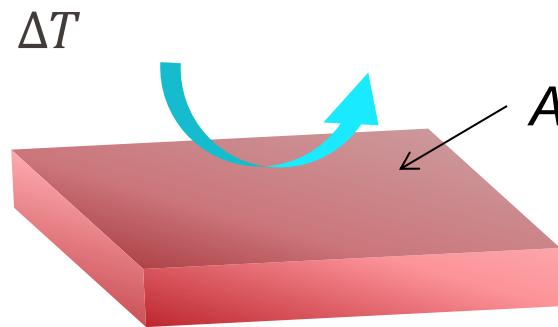
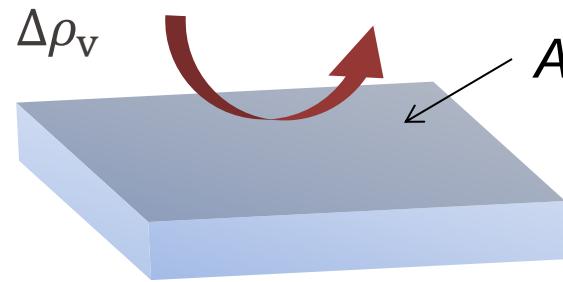
$\nabla \cdot (\text{Mass flux})$ = local mass “outgoingness”

$\nabla \cdot (\text{Energy flux})$ = local energy “outgoingness”

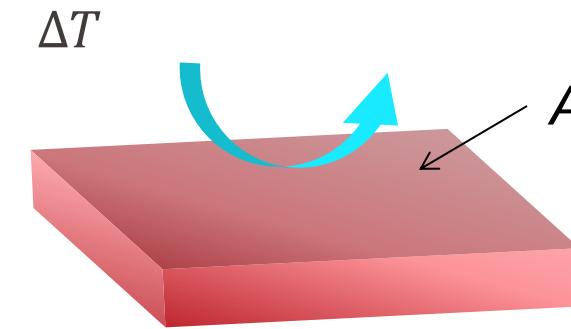
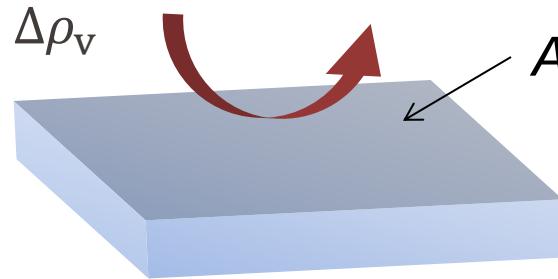


$$\nabla \cdot (\psi \vec{A}) = \psi (\nabla \cdot \vec{A}) + (\nabla \psi) \cdot \vec{A}$$

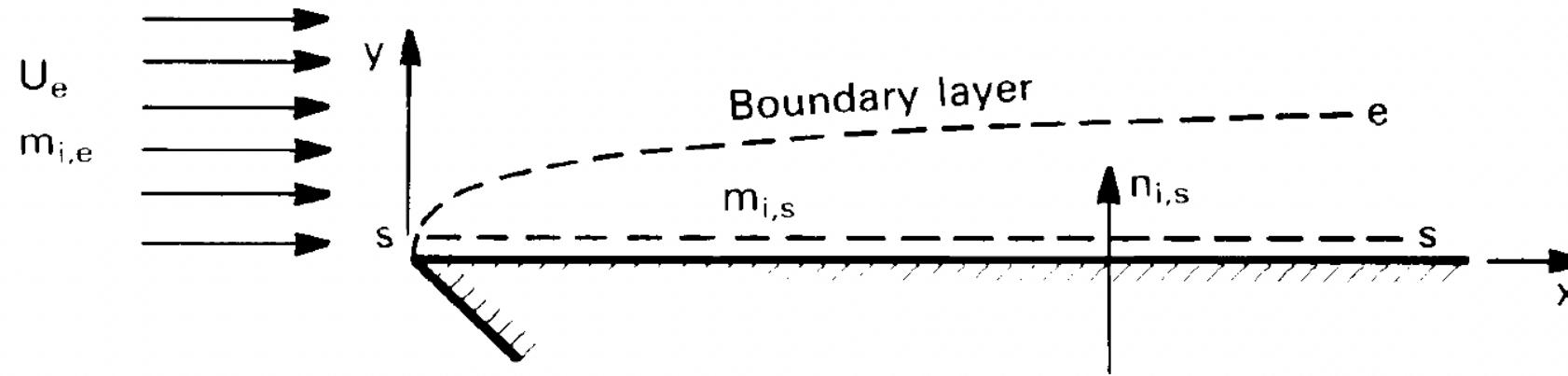
Heat and Mass Transfer Analogy



Heat and Mass Transfer Analogy



Example



Lienhard, Figure 11.12

$$Nu_x = 0.332 \sqrt{Re_x} \sqrt[3]{Pr}$$

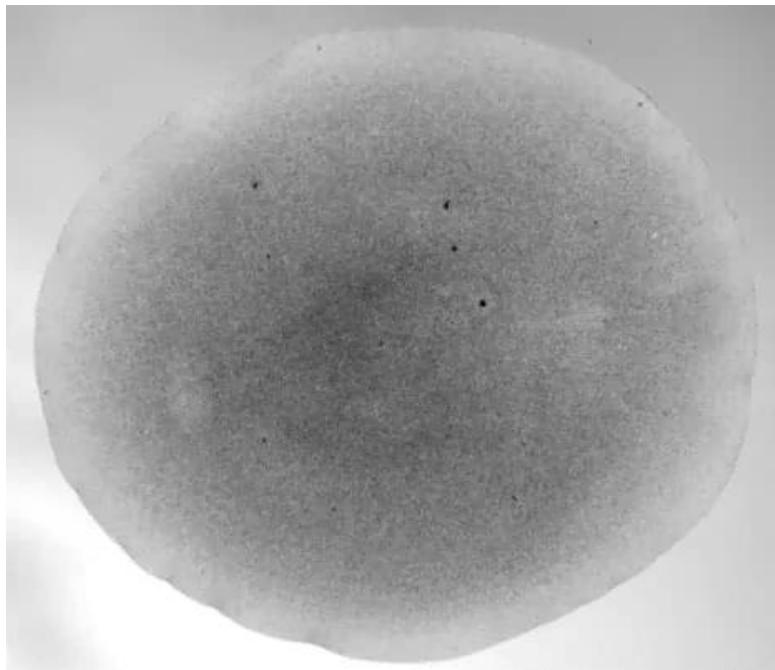
$$Sh_x = 0.332 \sqrt{Re_x} \sqrt[3]{Sc}$$

Coffee Ring Effect



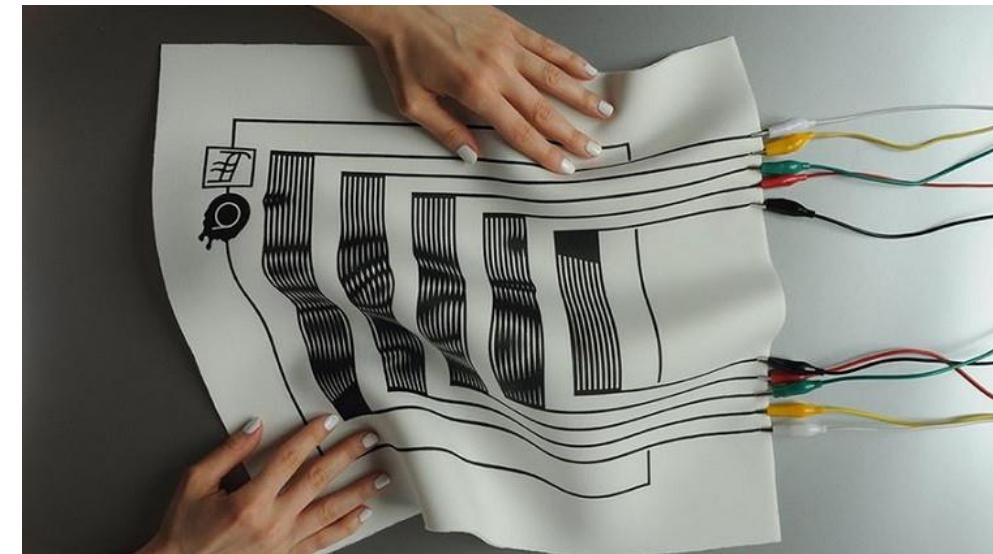
CC BY-NC

Coffee Ring Effect



Yunker *et al.*, *Nature* (2011)

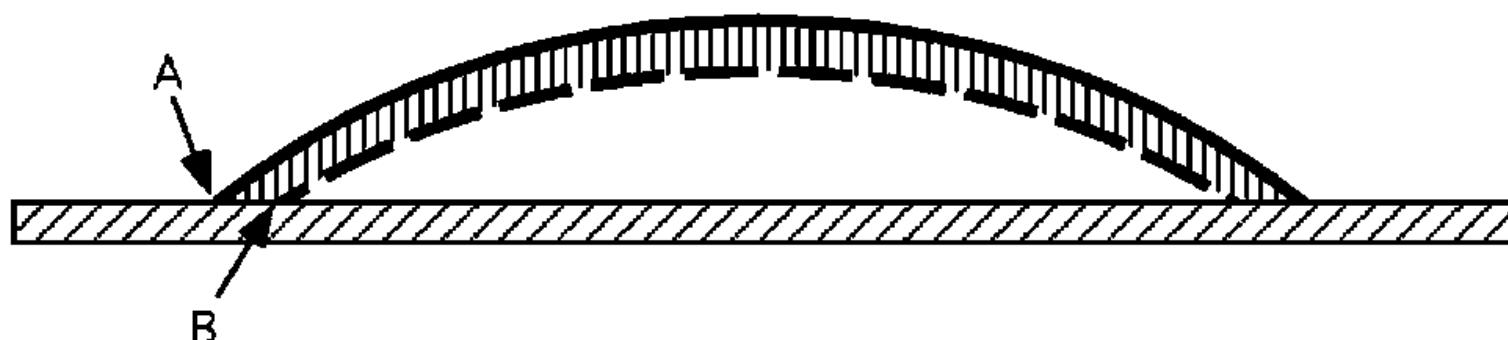
Printed electronics



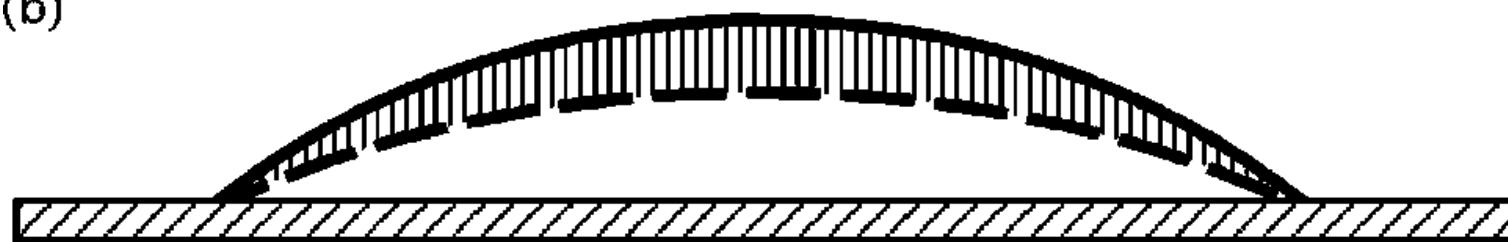
Karim *et al.*, *Scientific Reports* (2019)

Contact Line Pinning

(a)



(b)



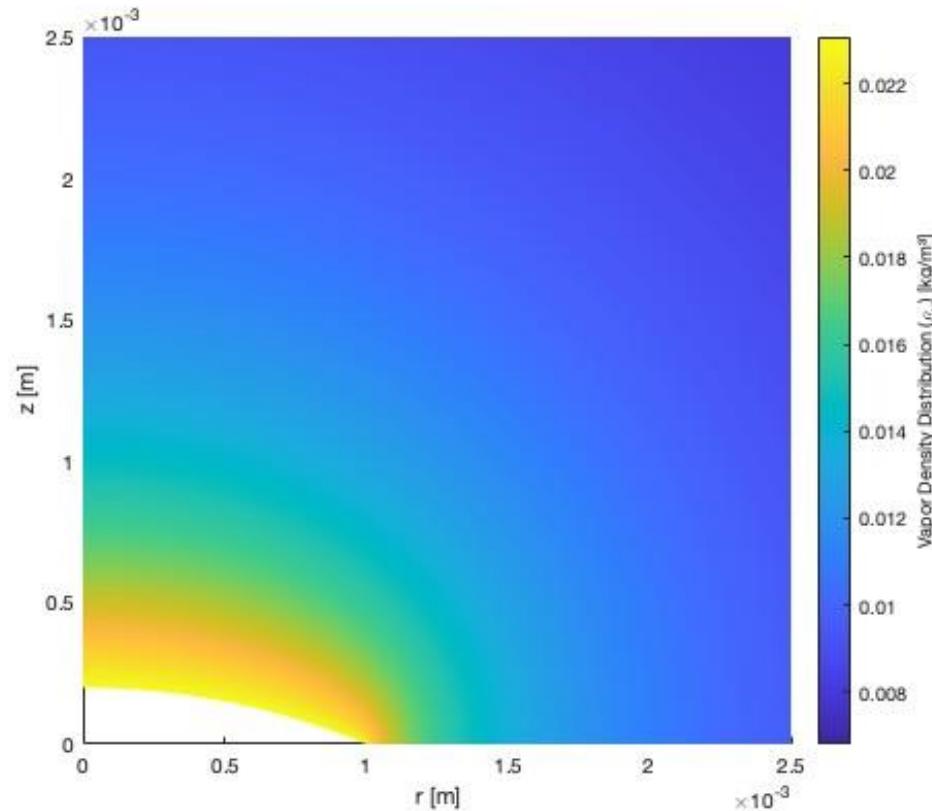
Deegan *et al.*, *Physical Review E* (2000)

Evaporative Transport



Lightening rod

Evaporative Transport

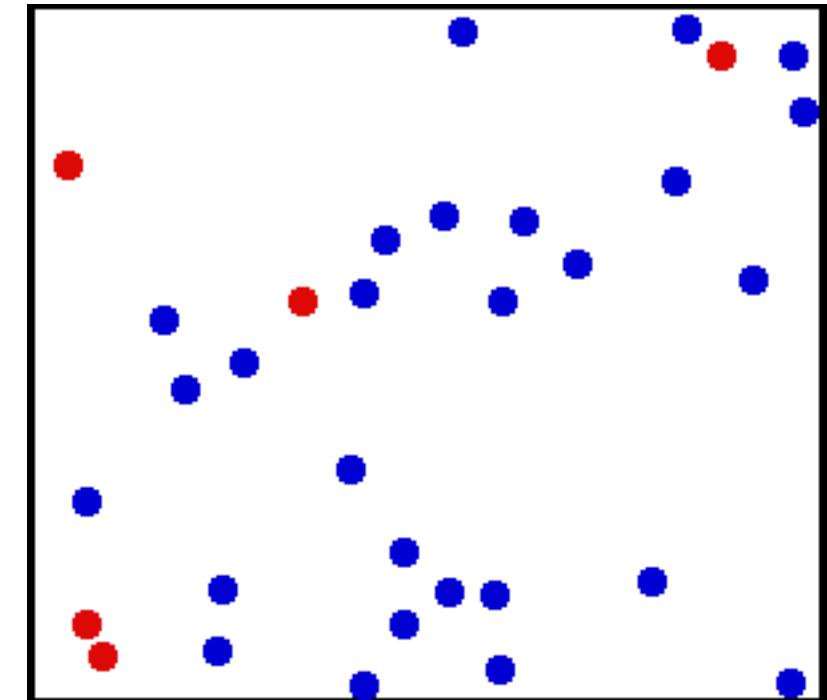


Lightening rod

- **Fick's Law of Diffusion**
- **Heat and mass transfer analogy**
- **Coffee ring effect**

Crash Course on Kinetic Theory of Gases

- Consider gas as a **large number of randomly moving particles** that collide with one another every now and then
- Collisions are elastic: **kinetic energy is conserved** before and after
- **Ideal gas**: molecules with negligible sizes and not interacting with each other other than collision



Credit: A. Greg