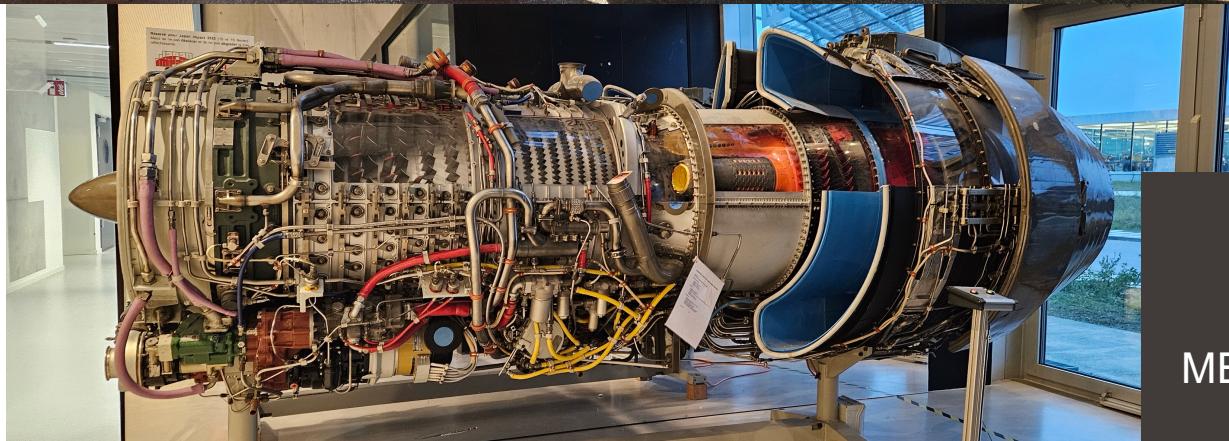




# Chapter 11: Compressible machines



ME-342 Introduction to  
turbomachinery

- 17<sup>th</sup> June 9:15-12:15
- The **equation sheet** will be available in Moodle **this week**
  - You should still learn what it means and how they are derived
  - **Do Not Bring it to the exam** → You will get the same copy in the exam
- You need to know the concepts and definitions
- Based on the exercises (in-class/exercise sessions)
- Bring a calculator!
- Lecture notes from Chap. 2 – Chap. 12 (next week included)

### Euler equation, Pumps and Turbines

- Shaft Work per Unit Mass:

$$w_s = U_2 V_{\theta 2} - U_1 V_{\theta 1}$$

- Shaft Power:

$$\dot{W}_{\text{shaft}} = -\dot{m}_1 (U_1 V_{\theta 1}) + \dot{m}_2 (U_2 V_{\theta 2})$$

- Euler Turbomachine Equation (Torque form):

$$T_{\text{shaft}} = -\dot{m}_1 (r_1 V_{\theta 1}) + \dot{m}_2 (r_2 V_{\theta 2})$$

- Total Head:

$$H = \frac{U_2 V_{\theta 2} - U_1 V_{\theta 1}}{g}$$

- Power gained by/from fluid:

$$P = \gamma Q H$$

- Ideal head rise pump:

$$h_i = \frac{U_2 V_{\theta 2} - U_1 V_{\theta 1}}{g}$$

- Actual head rise pump:

$$h_a = \frac{p_2 - p_1}{\gamma} + z_2 - z_1 + \frac{V_2^2 - V_1^2}{2g}$$

- Available Net Positive Suction Head (NPSHA):

$$\text{NPSHA} = \frac{p_{\text{atm}} - p_v}{\gamma} - z_s + \sum h_L$$

- Flow, Head and Power Coefficients:

$$C_Q = \frac{Q}{\omega D^3}, \quad C_H = \frac{gh_a}{\omega^2 D^2}, \quad C_{\mathcal{P}} = \frac{\dot{W}_{\text{shaft}}}{\rho \omega^3 D^5}$$

- Specific Speed (Dimensionless):

$$N_s = \frac{\omega \sqrt{Q}}{(gh_a)^{3/4}}$$

- Power Specific Speed (Hydraulic Turbines):

$$N'_s = \frac{\omega \sqrt{\dot{W}_{\text{shaft}} / \rho}}{(gh_a)^{5/4}}$$

- (static) Enthalpy and Stagnation enthalpy:

$$\tilde{h} = \tilde{u} + \frac{p}{\rho}, \quad \tilde{h}_0 = \tilde{h} + \frac{V^2}{2} + gz$$

- Degree of Reaction:

$$R = \frac{\dot{h}_{\text{rotor}}}{\dot{h}_{\text{stage}}}$$

- Head available at the turbine inlet relative to the surface of the tailrace:

$$H_E = h_g - h_{LP}$$

- Turbine Efficiency:

$$\eta_{\text{turbine}} = \frac{\dot{W}_{\text{shaft}}}{\gamma Q H_E}$$

$$\eta_h = \frac{|w_{\text{shaft}}|}{g H_E} = \frac{|-U_1 V_{\theta 1} + U_2 V_{\theta 2}|}{g H_E}$$

- Pump Efficiency:

$$\eta_{\text{pump}} = \frac{\gamma Q h_a}{\dot{W}_{\text{shaft}}}$$

- Thoma Cavitation Factor:

$$\sigma = \frac{\text{NPSHA}}{H_E}$$

### Compressible turbomachines

- Ideal gas law

$$\rho = \frac{p}{\mathcal{R} T}$$

# Compressible Flow Turbomachines

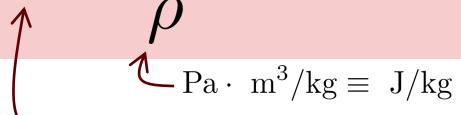
- Similar in principle to incompressible pumps and turbines
- **Key difference:** Fluid  changes significantly from inlet to the outlet  
→ unique consequences, benefits, and challenges
- **Energy and angular momentum** principles still apply
- **Thermodynamics** is essential for understanding compressible flow behaviour
- Unlike liquids, **temperature change matters greatly** in gases/vapours

## Compressor vs. Turbine Behaviour

- **Compressors** (like pumps):
  - Add energy to the gas
  - Cause **pressure, density, and temperature** to
- **Turbines**:
  - Extract energy from the gas
  - Cause **pressure, density, and temperature** to

**(static) Enthalpy:** internal energy and flow work

$$\check{h} = \check{u} + \frac{p}{\rho} \quad [\text{J/kg}]$$


  
 Internal energy

**Ideal gas law** → when can we use this?

$$\rho = \frac{p}{RT} \quad \begin{aligned} &\text{- Low pressure/high-temperature gases} \\ &\text{- Superheated steam (T>200 °C)} \end{aligned}$$

$R$  is the specific gas constant (not Reaction)

T in Kelvin, [K]

Side note..

$pV = nR'T$  R': universal gas constant, n: number of mols

$pV = mRT$  R: specific gas constant, m: mass

Reaction

$$R = \frac{\text{static enthalpy change in rotor}}{\text{stage static enthalpy change}} = \frac{\check{h}_2 - \check{h}_3}{\check{h}_1 - \check{h}_3}$$

# Compressor and Turbine

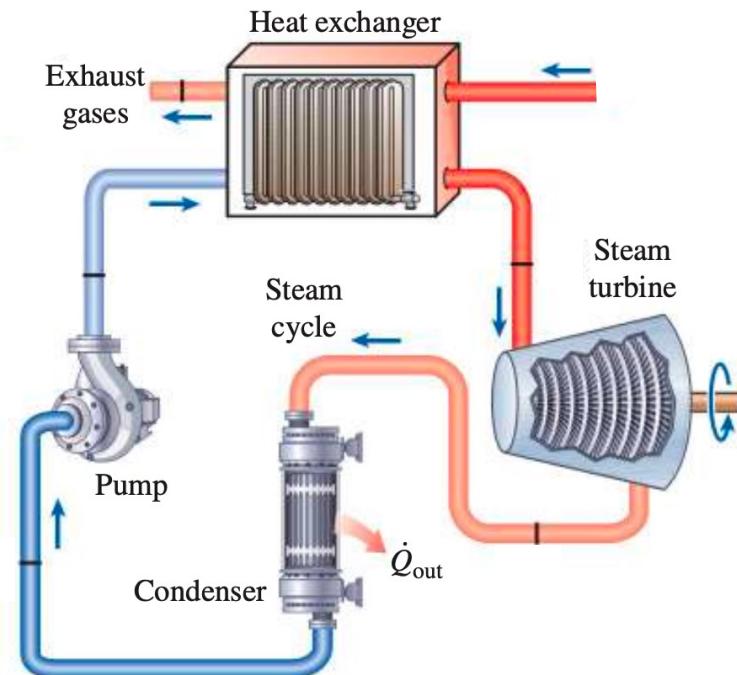
- “**Gas turbine**” usually refers to a **full** gas turbine engine:
  - Includes **compressor**, **combustor**, and **turbine**
  - Common in **aircraft propulsion** and **power generation**
- “**Steam turbine**” usually refers to a turbine driven by high-pressure steam:
  - **Part of the steam cycle** (usually Rankine cycle)
  - Steam is generated in a boiler, then expanded in the turbine
  - **Only includes the turbine itself**, not the boiler or condenser
  - Common in thermal power plants (coal, nuclear, solar thermal, and combined cycle)



## Rankine Cycle — Steam Turbine

- **Working fluid:** water/steam
- **Main components:**
  - **Boiler/Heat Recovery Steam Generator (HRSG):** uses heat from gas turbine exhaust to create steam
  - **Steam turbine:** expands steam to produce power
  - **Condenser:** condenses steam back to water
  - **Pump:** returns water to the boiler
- The maximum fluid temperature at the turbine inlet  $\sim 620^\circ\text{C}$
- **Efficiency:**  $\sim 30\text{--}40\%$  (on its own)

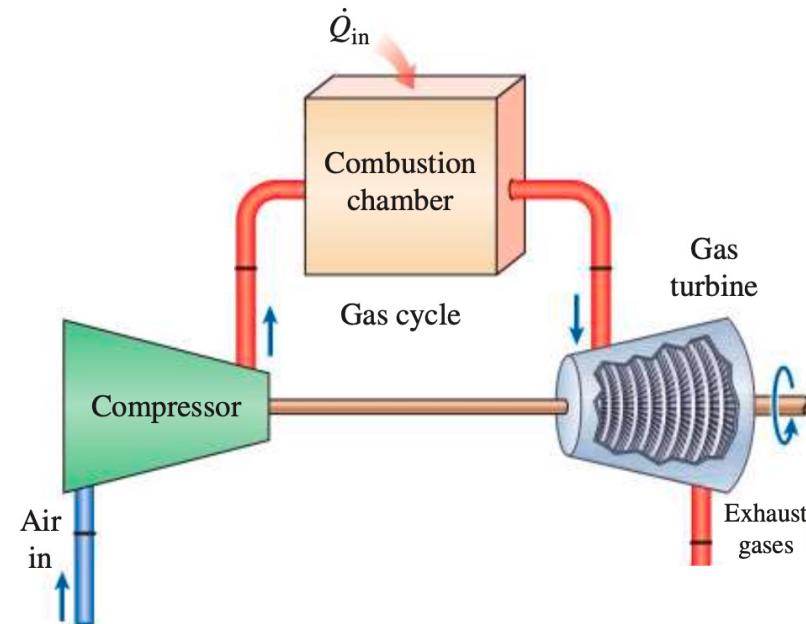
**Key idea:** Steam run a turbine to extract energy



## Brayton Cycle (a.k.a. Joule Cycle) — Gas Turbine

- **Working fluid:** air (and combustion gases)
- **Main components:**
  - **Compressor** (compresses air)
  - **Combustor** (burns fuel to heat air)
  - **Turbine** (expands hot gases to generate power)
- The maximum fluid temperature at the turbine inlet  $\sim 1425^{\circ}\text{C}$
- **Real-world example:** Jet engines, gas turbines
- **Efficiency:**  $\sim 30\text{--}40\%$

**Key idea:** High-temperature gas spins the turbine  $\rightarrow$  generates electricity/thrust.



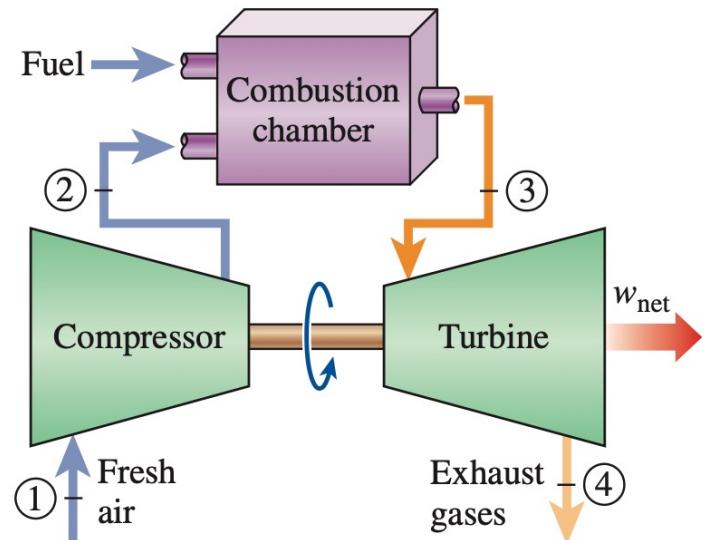
## Combined Cycle = Brayton + Rankine

- **How it works:**
  - Burn fuel  $\rightarrow$  gas turbine (Brayton)  $\rightarrow$  electricity
  - Use the hot exhaust  $\rightarrow$  heat water  $\rightarrow$  steam turbine (Rankine)  $\rightarrow$  more electricity
- **Total efficiency:**  $\sim 55\text{--}60\%$ , much higher than either cycle alone.

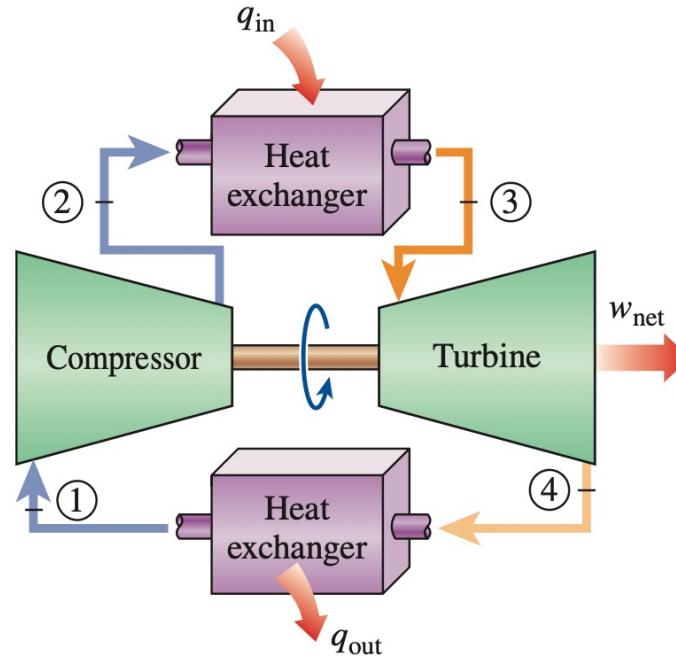
# Brayton Cycle

- THE IDEAL CYCLE FOR GAS-TURBINE ENGINES

An **open-cycle** gas-turbine engine



A **closed-cycle** gas-turbine engine

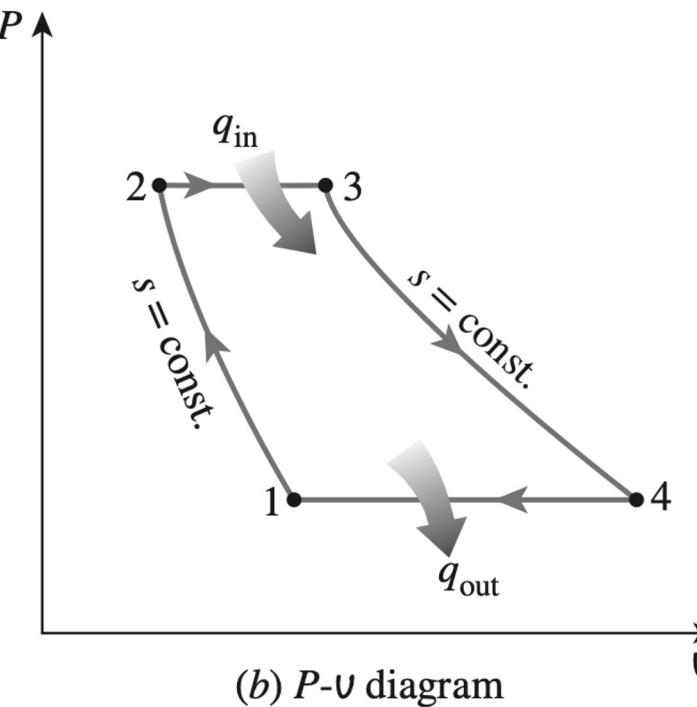
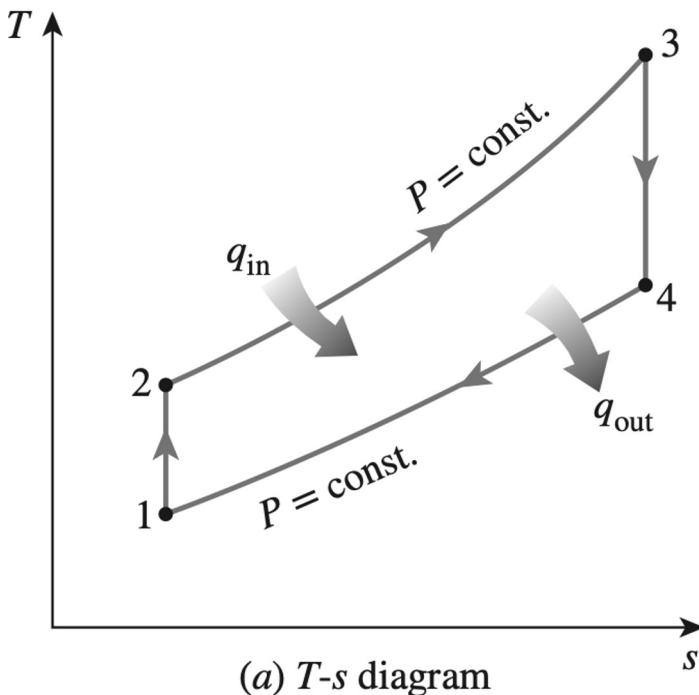
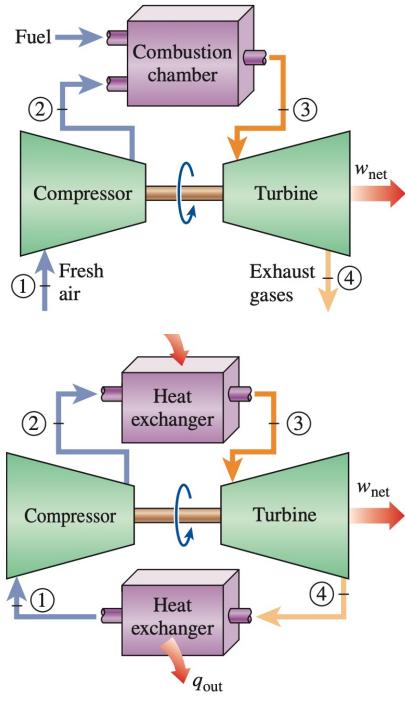


**Isentropic:** adiabatic and reversible ( $\Delta s=0$ )

$$\frac{T_2}{T_1} = \left( \frac{P_2}{P_1} \right)^{\frac{k-1}{k}}$$

Specific heat ratio:  $k = c_p/c_v$ , (air  $\sim 1.4$ )

- 1  $\rightarrow$  2 Isentropic compression (in a compressor)
- 2  $\rightarrow$  3 Constant-pressure heat addition
- 3  $\rightarrow$  4 Isentropic expansion (in a turbine)
- 4  $\rightarrow$  1 Constant-pressure heat rejection



$P$  = pressure,  $v$  = volume,  $T$  = temperature,  $s$  = entropy,  $q$  = the heat added to or rejected by the system

### Radial-Flow (Centrifugal) Compressors

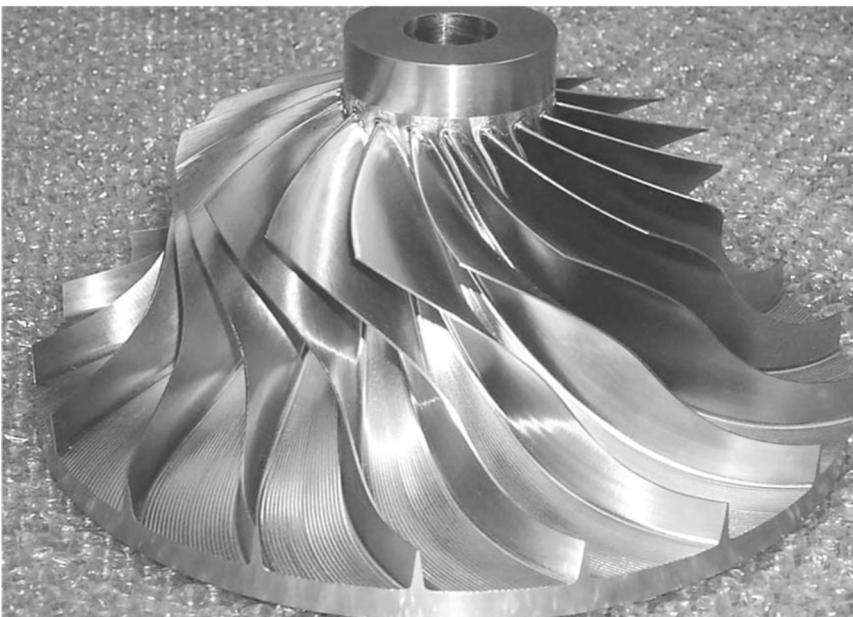
- Turbocompressors **continuously compress** flowing gas
- Compression leads to significant **increases in pressure, density, and temperature**
- Operate like centrifugal pumps, but with **gas instead of liquid**
- Typical features:
  - **High pressure rise**
  - **Low flowrate**
  - **Axially compact**
- **Total Pressure Ratio (PR):**  $PR = \frac{p_{T2}}{p_{T1}}$  in absolute pressure

Total pressure:

$$p_T = p + \frac{1}{2}\rho V^2 + \gamma z \simeq p + \frac{1}{2}\rho V^2$$

- Example:  $PR = 3.0 \rightarrow$  Air compressed from 101.3 kPa to  $\sim 304$  kPa  
Accompanied temperature rise?

Isentropic compression  $\frac{T_2}{T_1} = \left(\frac{P_2}{P_1}\right)^{\frac{k-1}{k}} = PR^{\frac{k-1}{k}}$



### Multi-Stage Compression

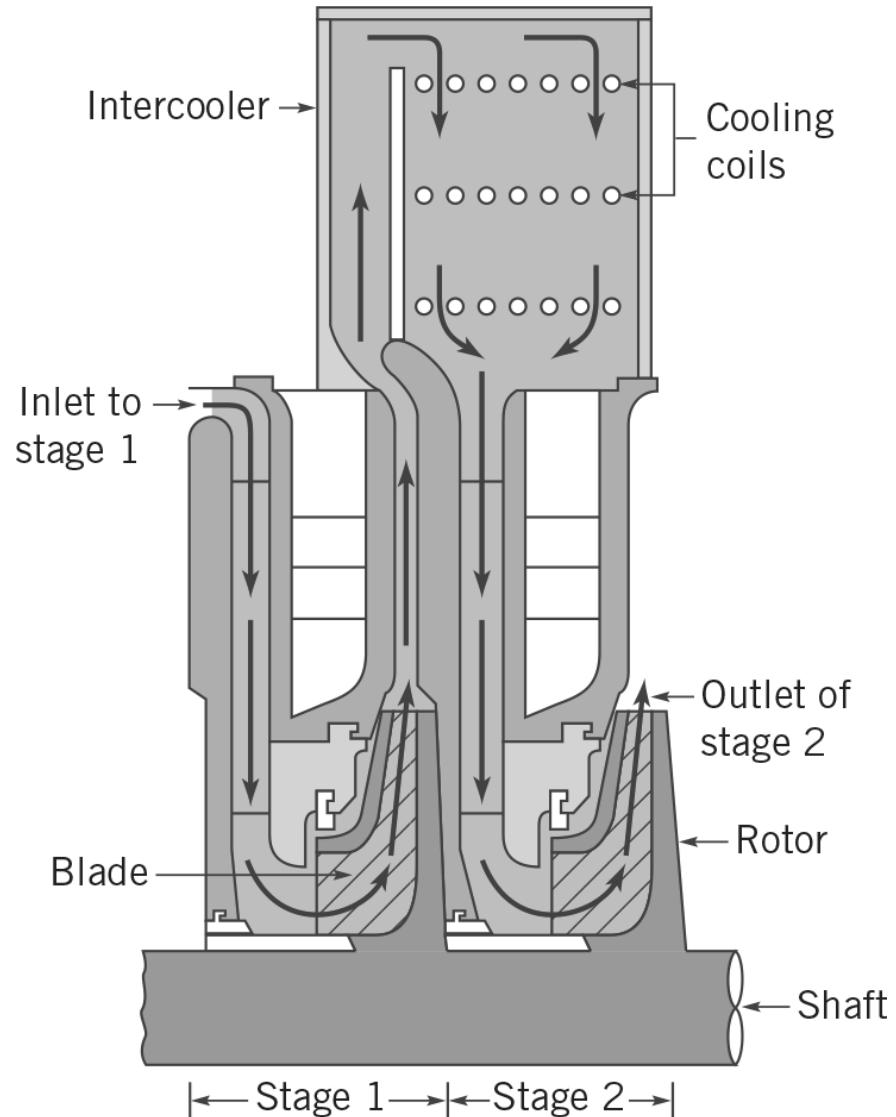
- Higher compression ratio
- For similar PR per stage,

$$\text{Overall PR} = (PR_{\text{stage}})^n$$

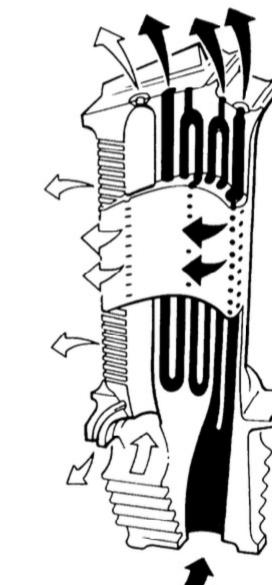
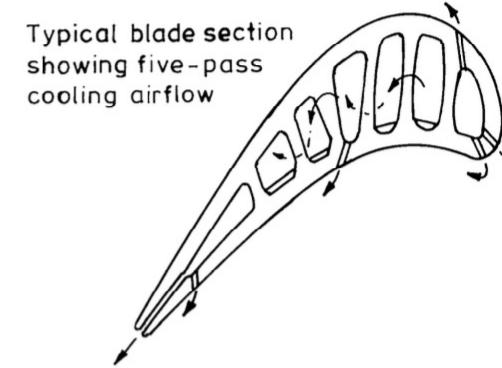
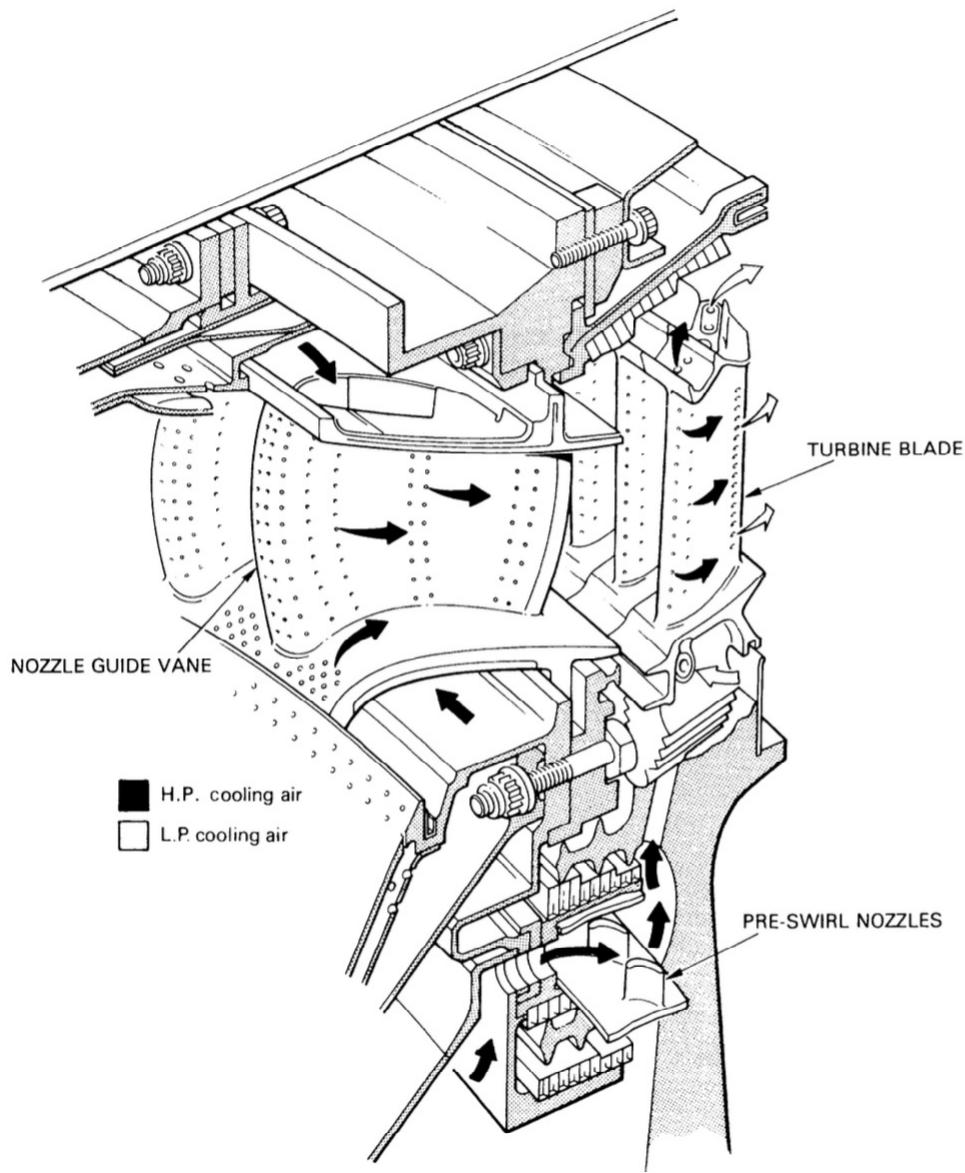
- Example: 4 stages with  $PR_{\text{stage}} = 2.0 \rightarrow PR_{\text{overall}} = 2^4 = 16$   
→ Compress air from 101.3 kPa to 1620 kPa

### Thermodynamic Considerations

- **Adiabatic compression** (Brayton cycle)  
→ temperature increases, more work needed
- **Isothermal compression** (ideal)  
→ less work
- **Intercooler** between stages:
  - Reduces temperature before next stage
  - Lowers required compression work

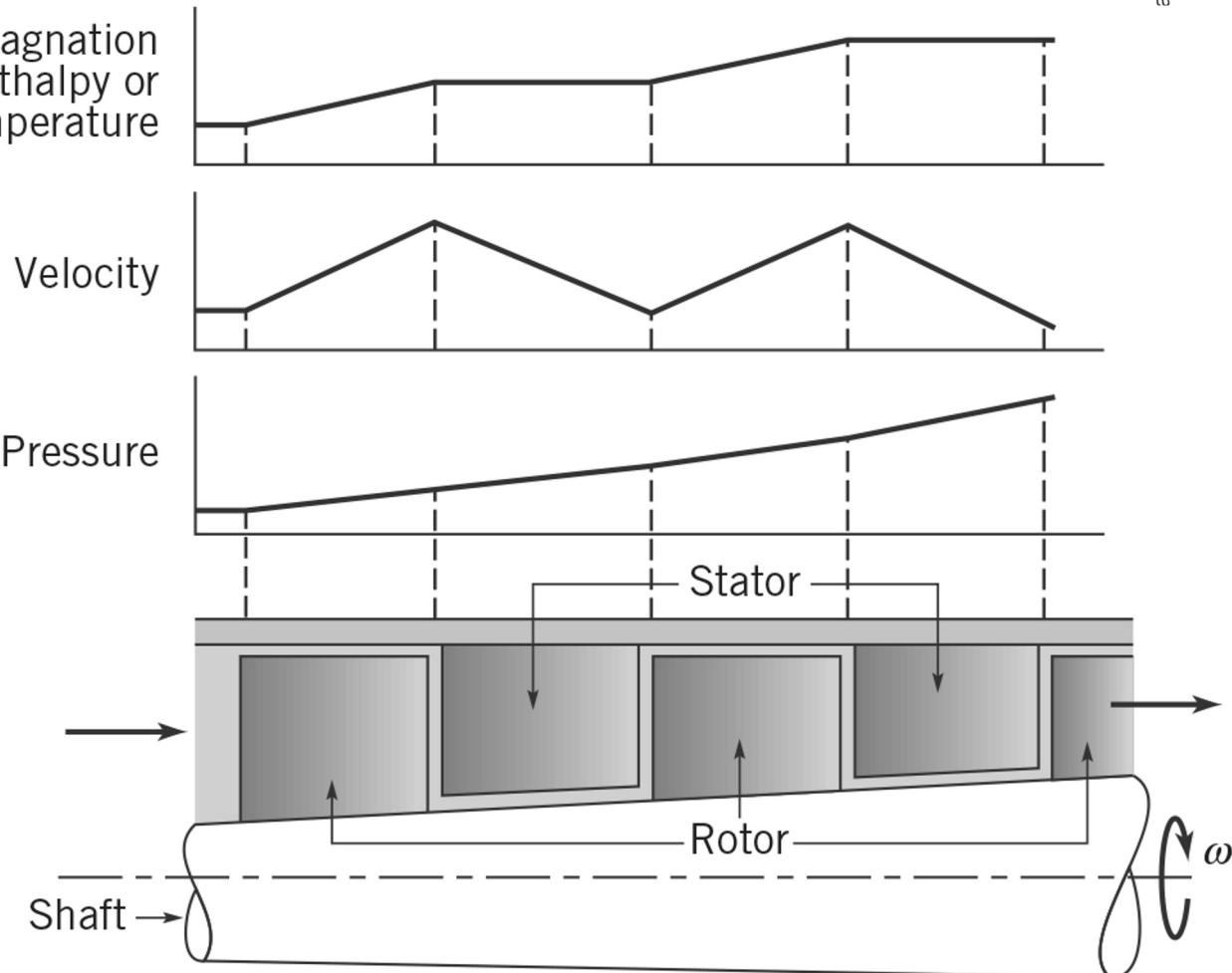


# Blade cooling

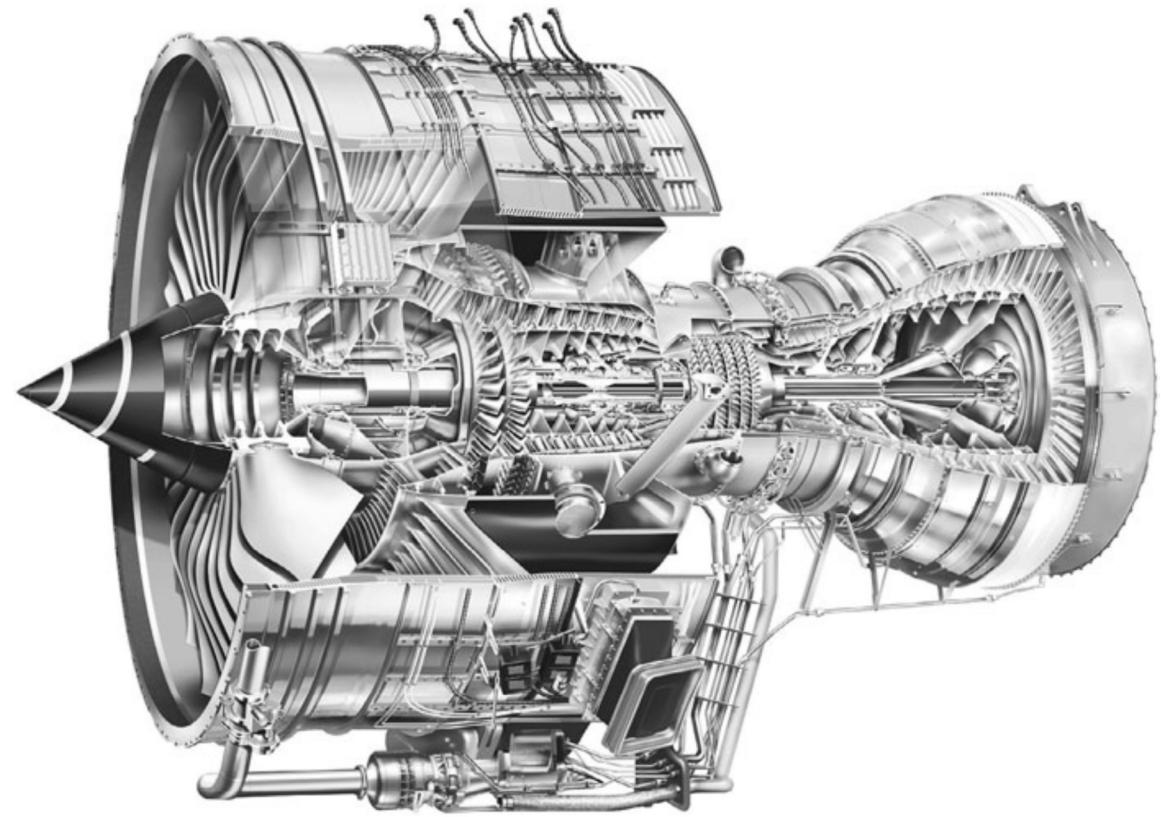


QUINTUPLE PASS,  
MULTI-FEED  
INTERNAL COOLING  
WITH EXTENSIVE  
FILM COOLING

- Widely used **compressor type** in turbomachinery
- Compared to centrifugal compressors:
  - **Lower pressure rise per stage**
  - **Higher flowrate**
  - More **radially compact**
- Usually **multiple stages**
  - Usually,  $PR_{\text{stage}}$  varies across the stages  
 $\rightarrow PR_{\text{overall}} = PR_{\text{st1}} \times PR_{\text{st2}} \cdots PR_{\text{stn}}$
- As gas is compressed:
  - **Density increases**
  - **Cross-sectional area decreases**
  - **Blade height reduces** from inlet to outlet
- $\rightarrow$  Why do compressor blades shrink?  
 $\dot{m} = \rho A V = \text{constant}$

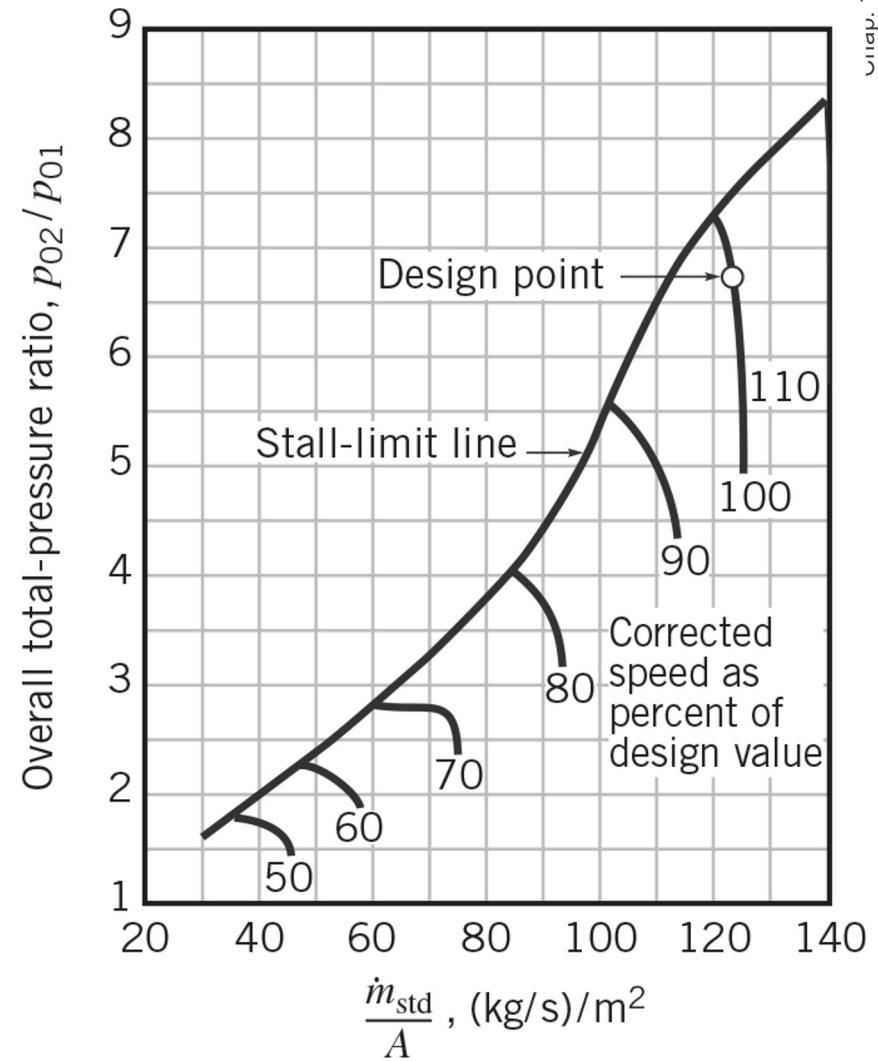


- **Inlet Guide Vanes (IGVs):**
  - Located **before the first rotor**
  - **Redirect flow** away from purely axial direction
  - Optimize **relative velocity** into rotor blades
- **Rotor Blades:**
  - Rotate, pushing gas **rearward and outward**
  - **Add energy** to the flow (like an axial pump)
  - Increase **total pressure and enthalpy**
- **Stator Blades:**
  - **Stationary**, act as **diffusers**
  - **Turn flow back** toward axial direction
  - Increase **static pressure**
  - Cannot add energy (no rotation)

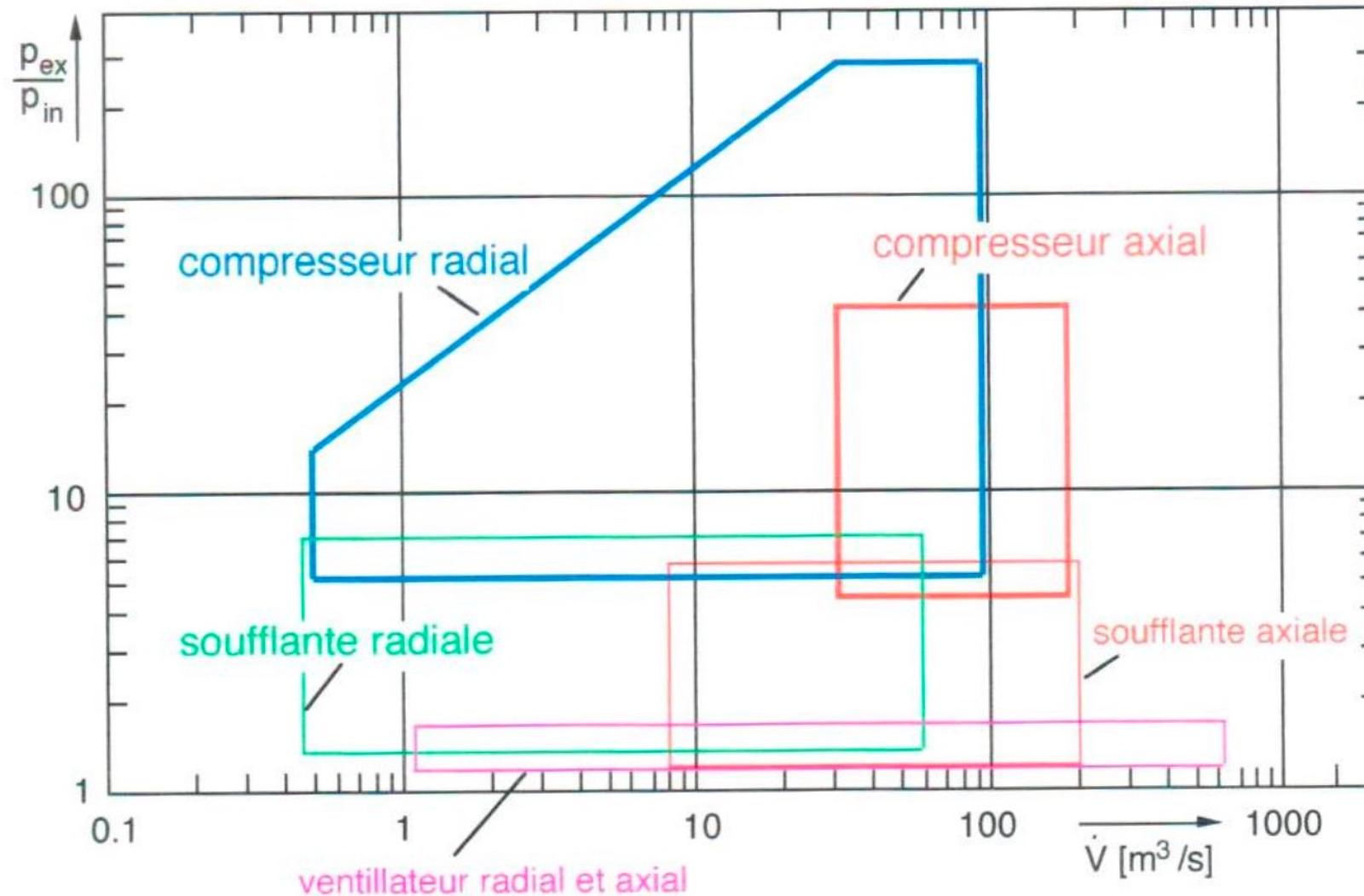


Axial-flow compressor multistaging requires less frontal area but more length than centrifugal compressors.

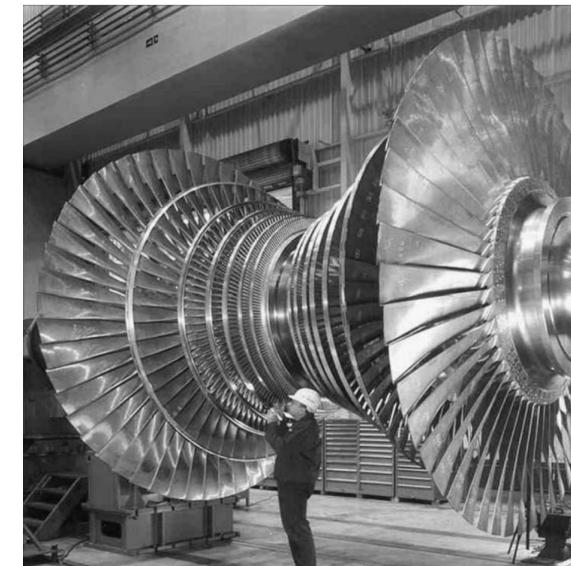
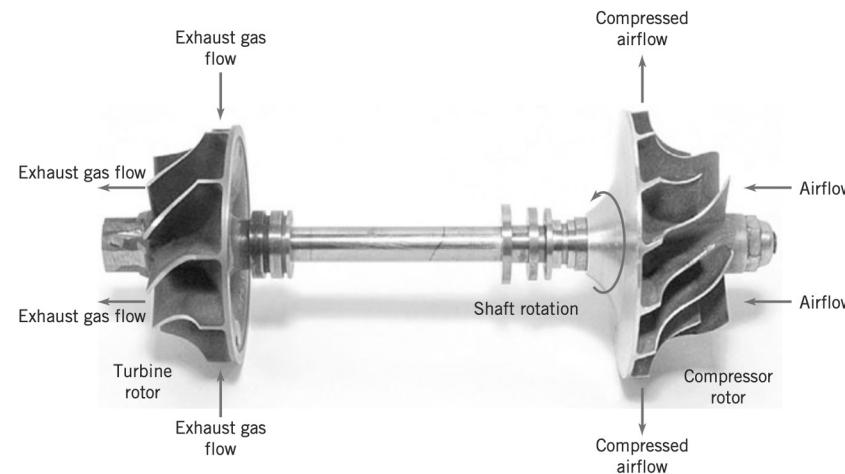
- **Axial-Flow Compressor Blade Behavior**
  - Blades are shaped like **airfoils** (like airplane wings)
    - Designed to generate **lift** and manage **drag**
  - Operate best at **design flowrate**
- **Compressor Stall and Surge**
  - At reduced flowrate:
    - **Angle of incidence** (between flow and blade) **increases**
    - **Relative flow hits blade at a steeper angle**
  - If incidence is too large:
    - **Blade stall** occurs (like wing stall in aircraft)
    - Leads to **compressor surge or stall**:
      - **Unstable flow**
      - Can cause:
        - **Excessive vibration**
        - **Noise**
        - **Performance loss**
        - **Mechanical damage**
  - **Operating Limits**
    - Lower flowrate bound is set by **onset of stall/surge**



# Compressor map



- Similar in principle to **hydraulic turbines**
- Use a **gas** or **vapor** as a working fluid → **fluid expands** during flow
- Can be:
  - **Impulse** or **reaction** type
  - **Axial**, **radial**, or **mixed-flow**



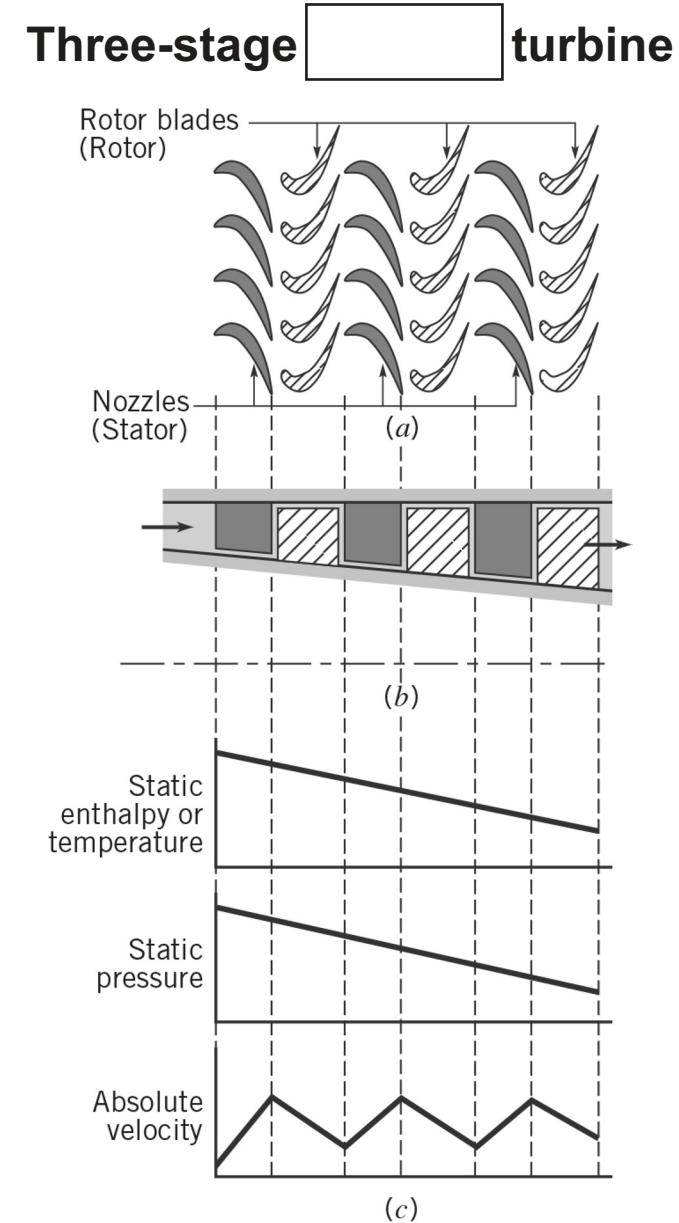
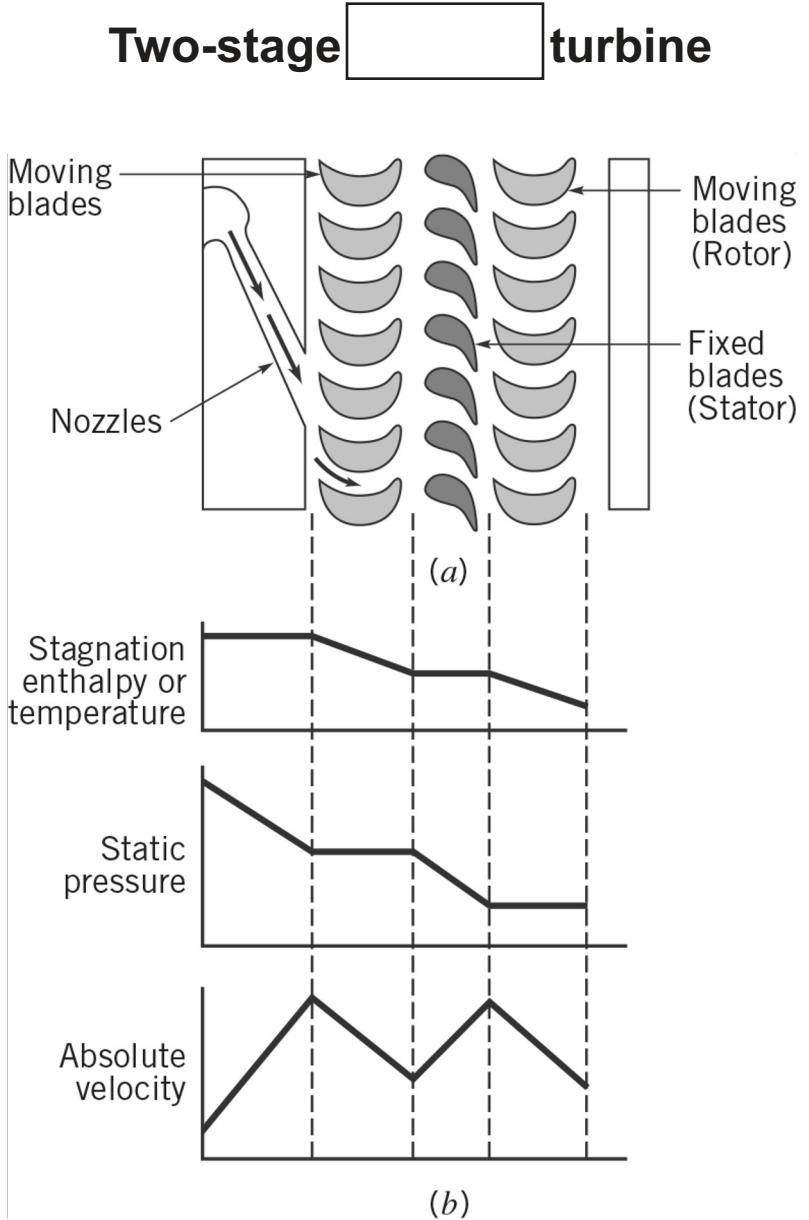
## Radial-Inflow Turbines

- Example: **Turbocharger** turbine (automotive)
- Advantages:
  - **Robust & durable**
  - **Axially compact**
  - **Cost-effective**
- Disadvantages:
  - Generally **lower efficiency** than axial-flow turbines

## Axial-Flow Turbines

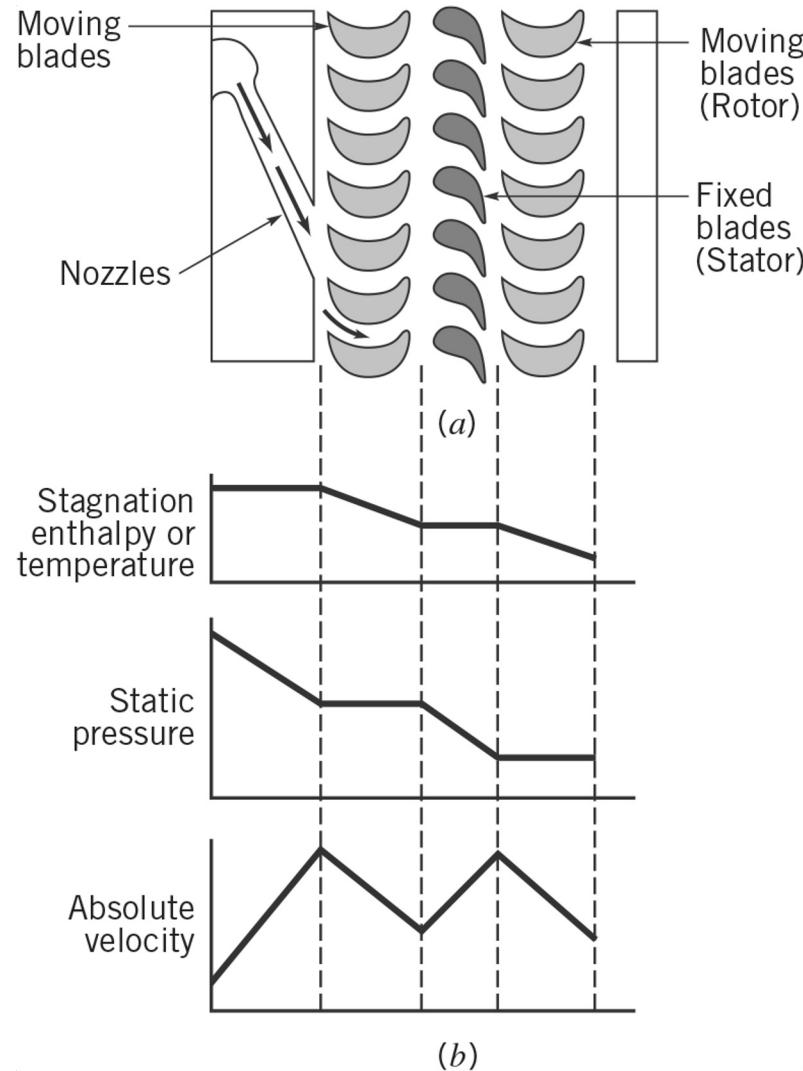
- **Steam and gas power plants**
- **Marine propulsion**
- **Gas turbine engines**
- Can be:
  - **Single-stage** or **multistage**
  - **Impulse** or **reaction** type

# Impulse or Reaction?



# Impulse turbine

## Two-stage impulse turbine



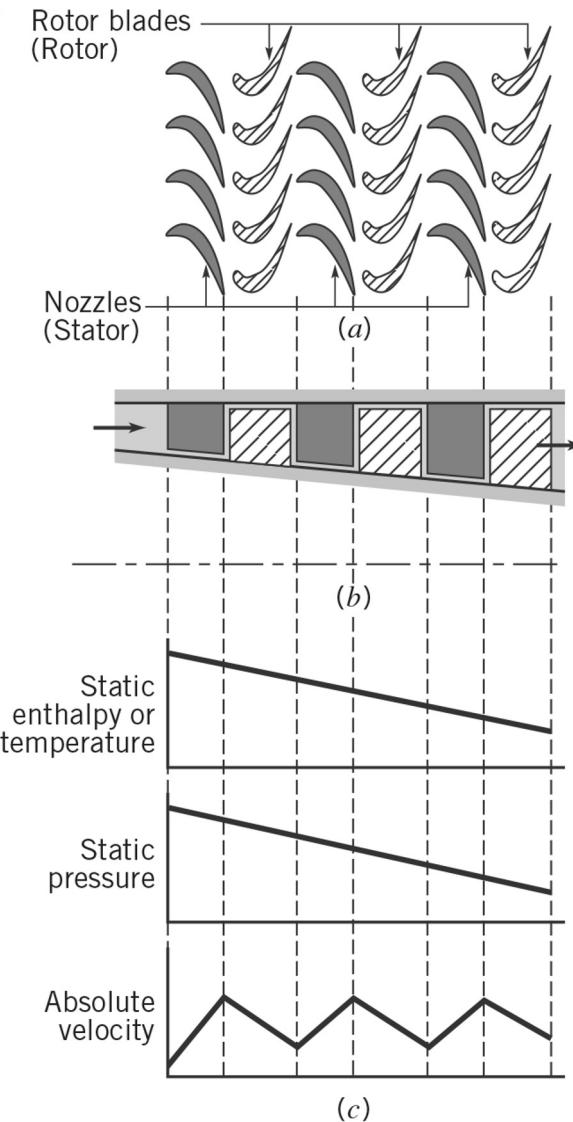
- Pressure drop happens mostly across **nozzles (stators)**
- Rotor blades operate at nearly constant pressure

- **Stators only guide and accelerate flow** (adiabatic → no energy loss)
- **Stagnation enthalpy (or temperature) remains constant across stators**
- Due to **gas expansion** (pressure ↓), **density ↓**
- To maintain mass flow, **passage area increases** from inlet to outlet
- Seen clearly in reaction turbine geometries

→ Why Do Turbine Blades Expand?

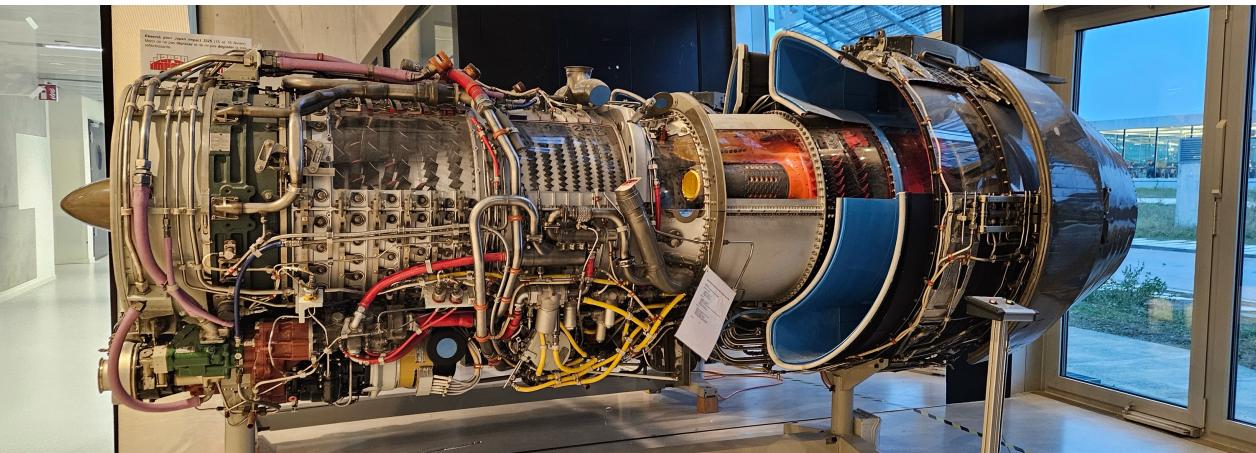
$$\dot{m} = \rho A V = \text{constant}$$

### Three-stage reaction turbine

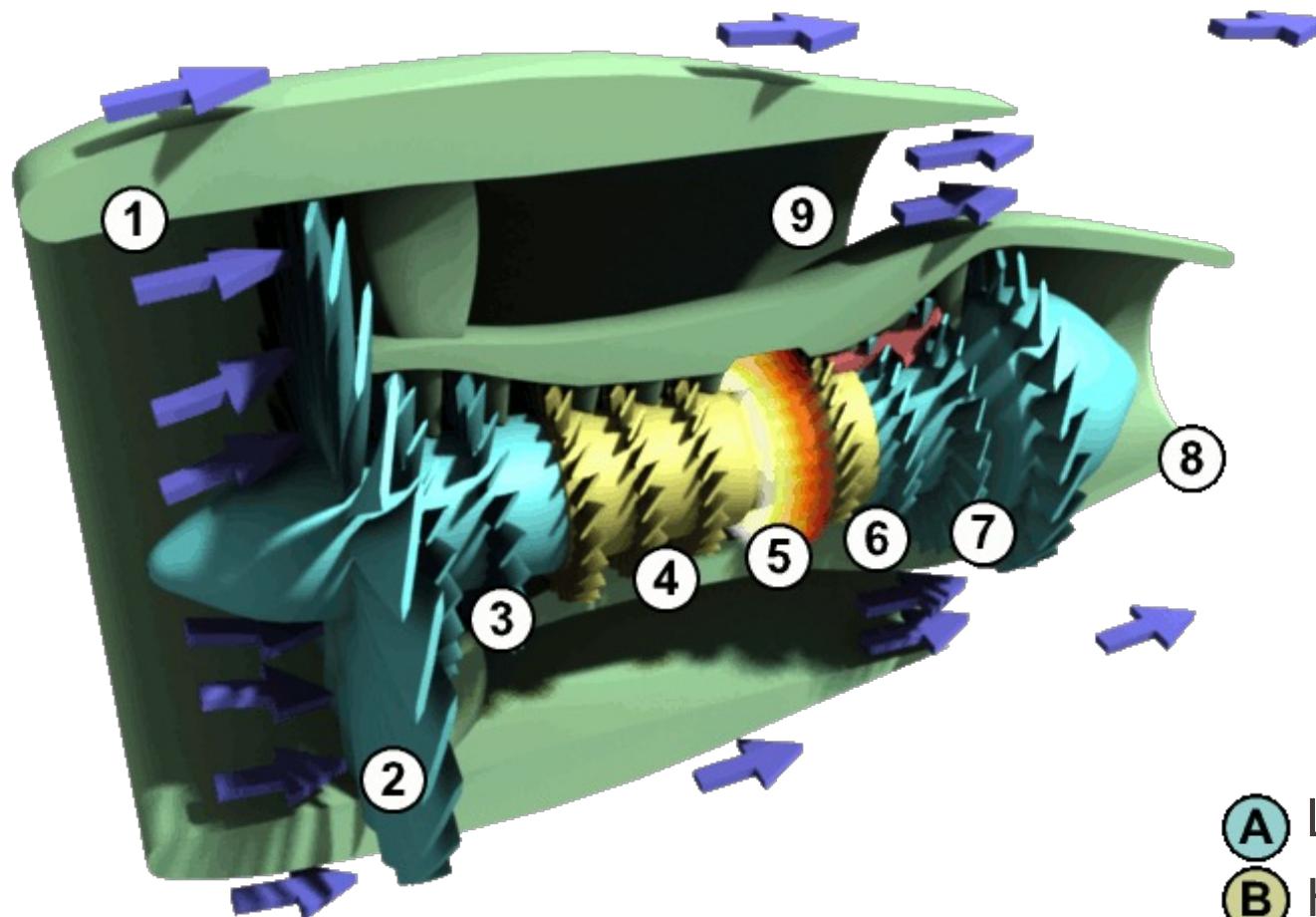


**Our Compressible Turbomachines - next week!**

- Guided tour + exercise
  - Lecture on our turbomachines
    - Visit together the machines
  - Two groups
    - Group 1: exercise + tour
    - Group 2: tour + exercise



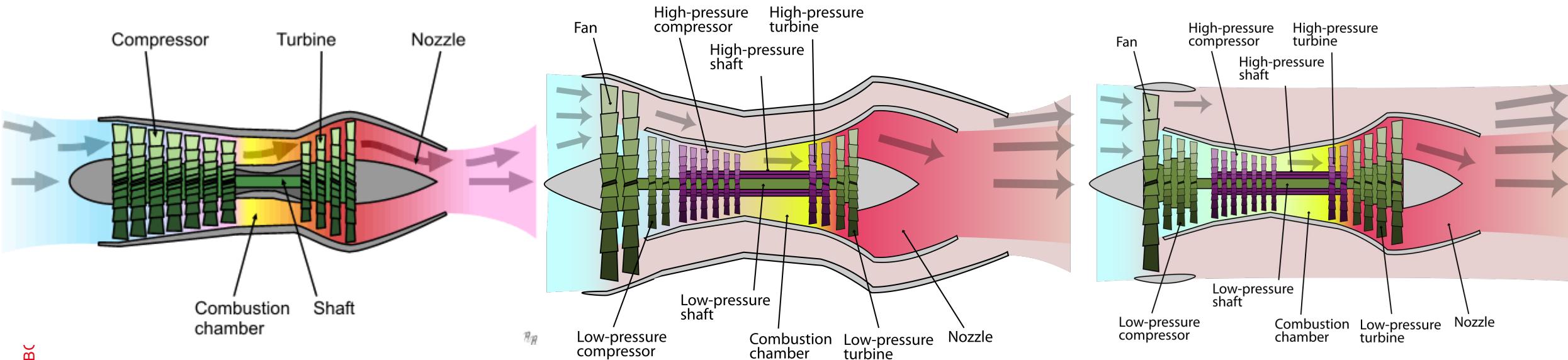
# Multiple spools (shafts)



1. Nacelle
2. Fan
3. Low-pressure compressor
4. High-pressure compressor
5. Combustion chamber
6. High-pressure turbine
7. Low-pressure turbine
8. Core nozzle
9. Fan nozzle

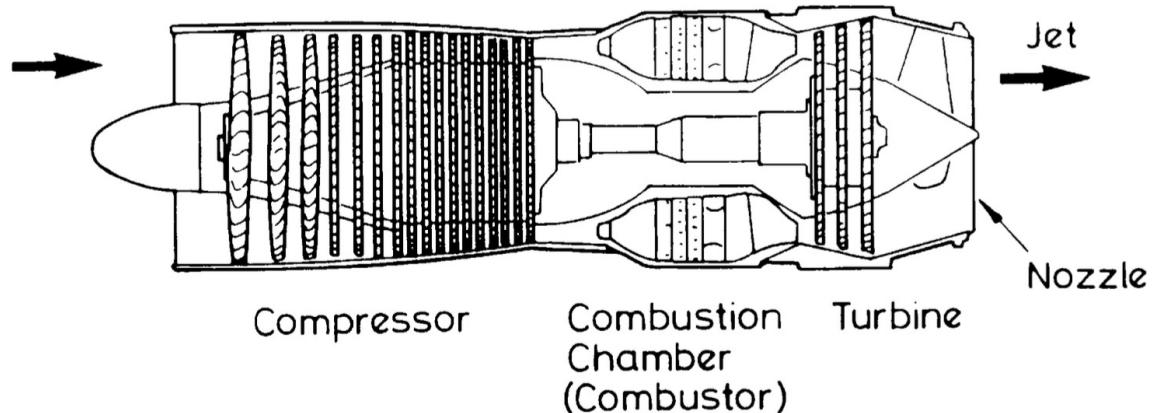
- A** Low-pressure spool
- B** High-pressure spool
- C** Stationary components

- **turbofan** a jet engine with a bypass stream.
- **turbojet** a jet engine with no bypass stream – these were the earliest type of jet engines and are still used for very highspeed propulsion.



- Multiple shafts system is also required
  - Large diameter of fan, slow speed (Low pressure compressors, LP turbines)
  - Small diameter, faster speed (High pressure compressors, HP turbines)

# Turbofan: Bypass ratio

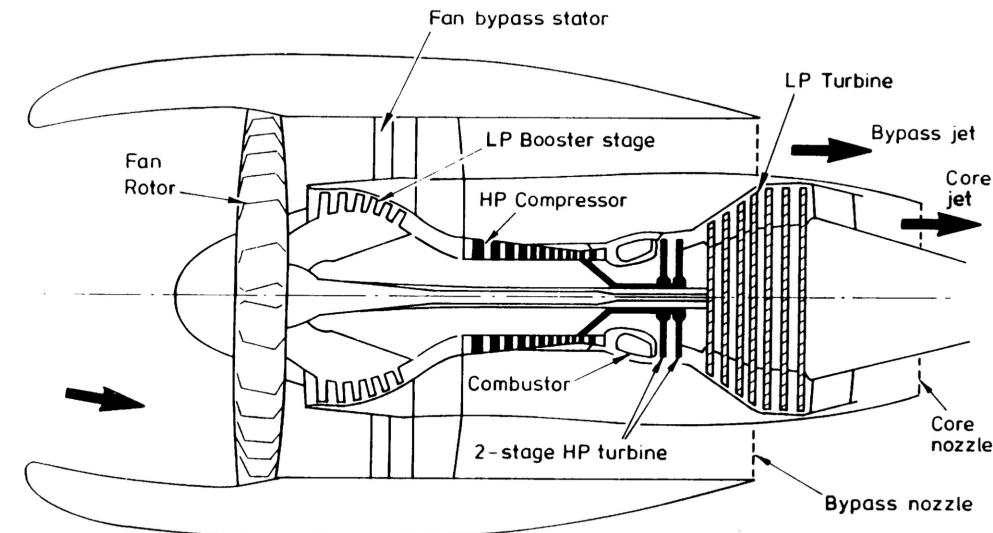


**A single-shaft turbojet engine (no bypass)**

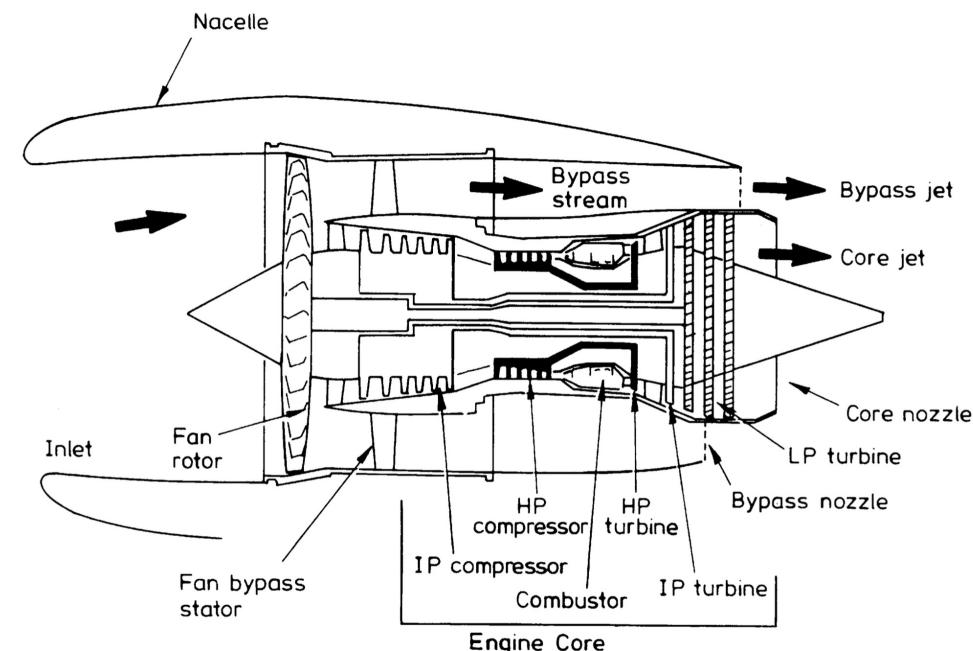
**Low-Pressure (LP)** First compression from ambient to intermediate

**Intermediate (IP)** Compression to medium pressure

**High-Pressure (HP)** Final compression before combustion



**A two-shaft high bypass engine**



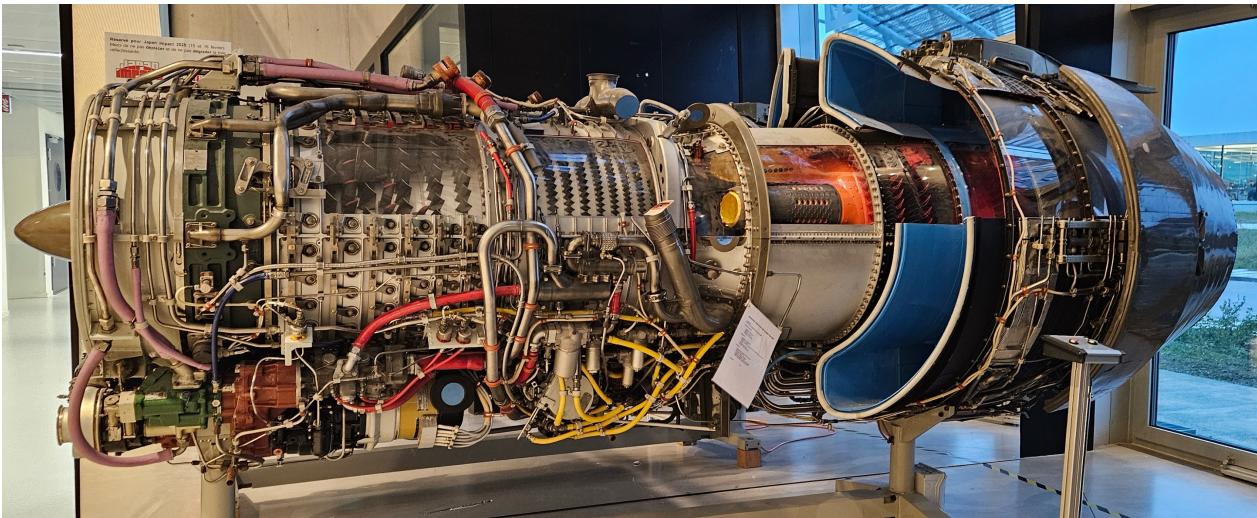
**A three-shaft high bypass engine**

# Bypass ratio

**GE CJ805-23**

Bypass ratio 1.46

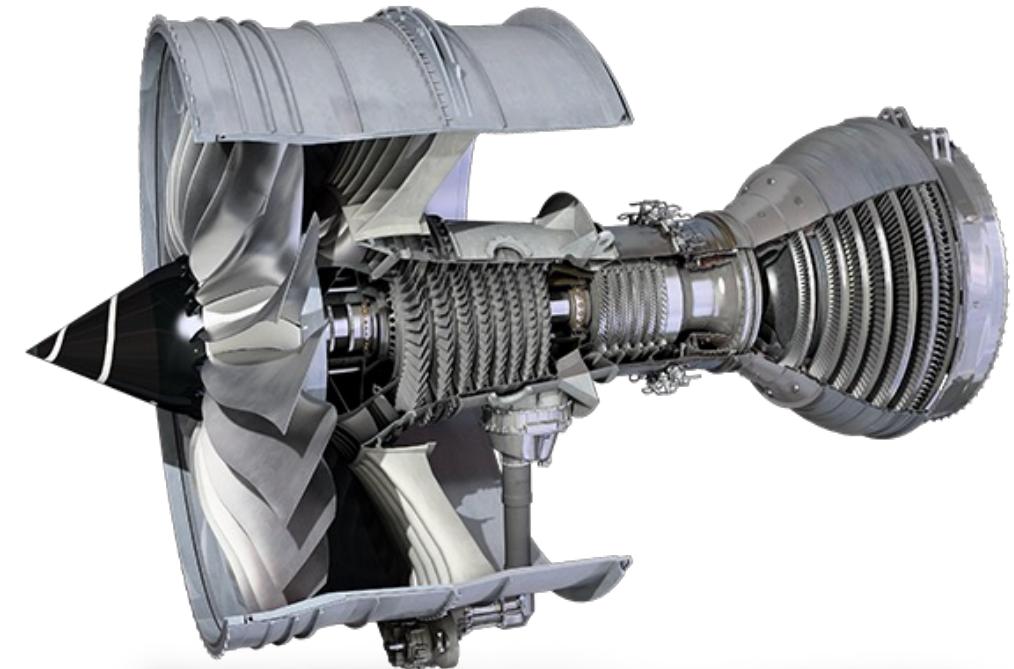
Overall Pressure ratio 13



**Rolls-Royce Trent 1000**

Bypass ratio 9.0–12.5

Overall Pressure ratio 50



# Next Week - High-Pressure Sulzer Gas Turbine

