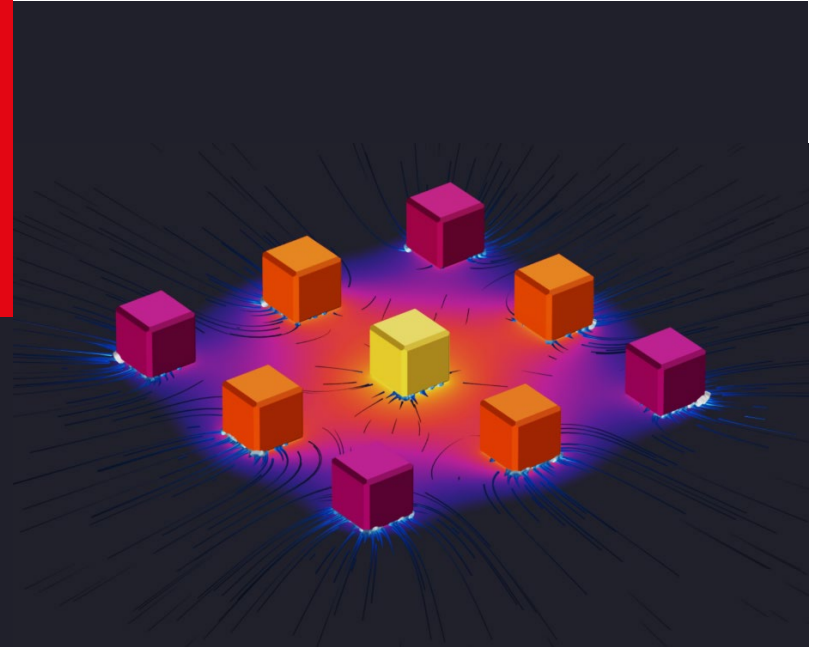


# Heat and Mass Transfer ME-341

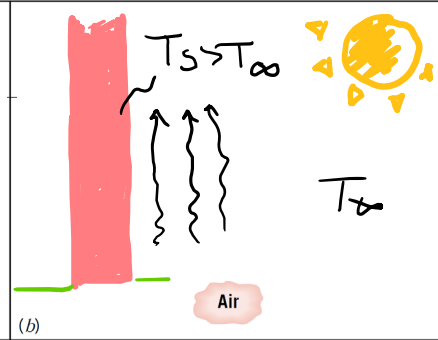
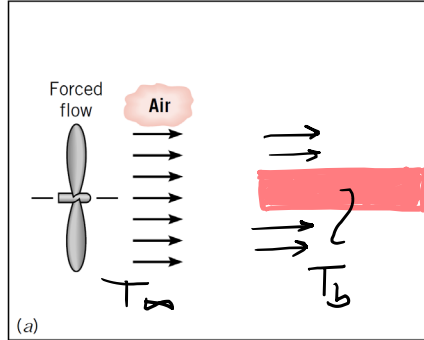
*Instructor:* Giulia Tagliabue



Spring Semester

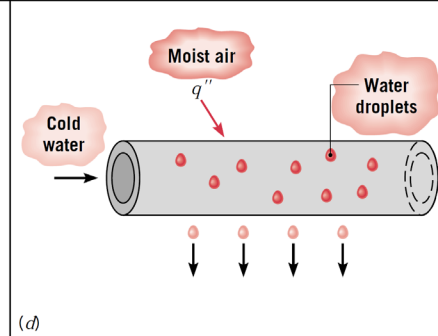
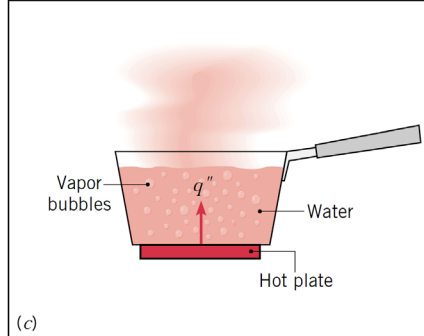
# This Week

## 1. Forced Convection



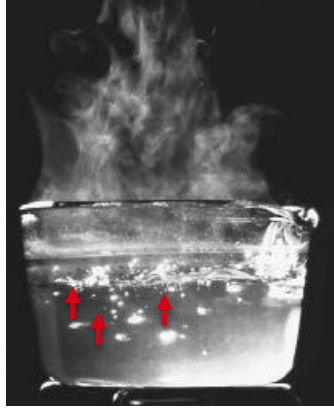
## 2. Natural (Free) Convection

## 3. Boiling



## 4. Condensation

# Introduction to Boiling and Condensation



Boiling: heat transfer from the wall to the fluid



Condensation: heat transfer from the fluid to the wall

Fluid motion controlled by:

- Surface tension  $\sigma$  at the liquid-vapor interface
- Density difference (buoyancy) between liquid/vapor phases

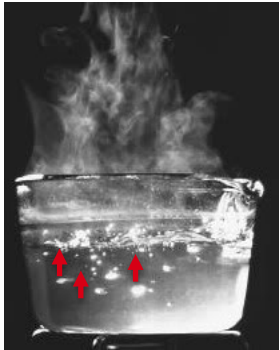
Phase Transition = Isothermal Process

**Latent heat** ( $h_{fg}$ ) is exchanged between solid and fluid  
Small solid/fluid  $\Delta T$

# Introduction to Boiling

Boiling occurs when the surface temperature exceeds the saturation temperature at that pressure.

$$q_s'' = h(T_s - T_{sat}) = h\Delta T_e \quad \Delta T_e \text{ excess temperature}$$



## Fluid Dynamics

### Pool boiling

the liquid is initially quiescent and only free convection occurs

### Forced boiling

the fluid is moving while it boils (e.g. inside a pipe)

## Heat Transfer

### Saturated Boiling

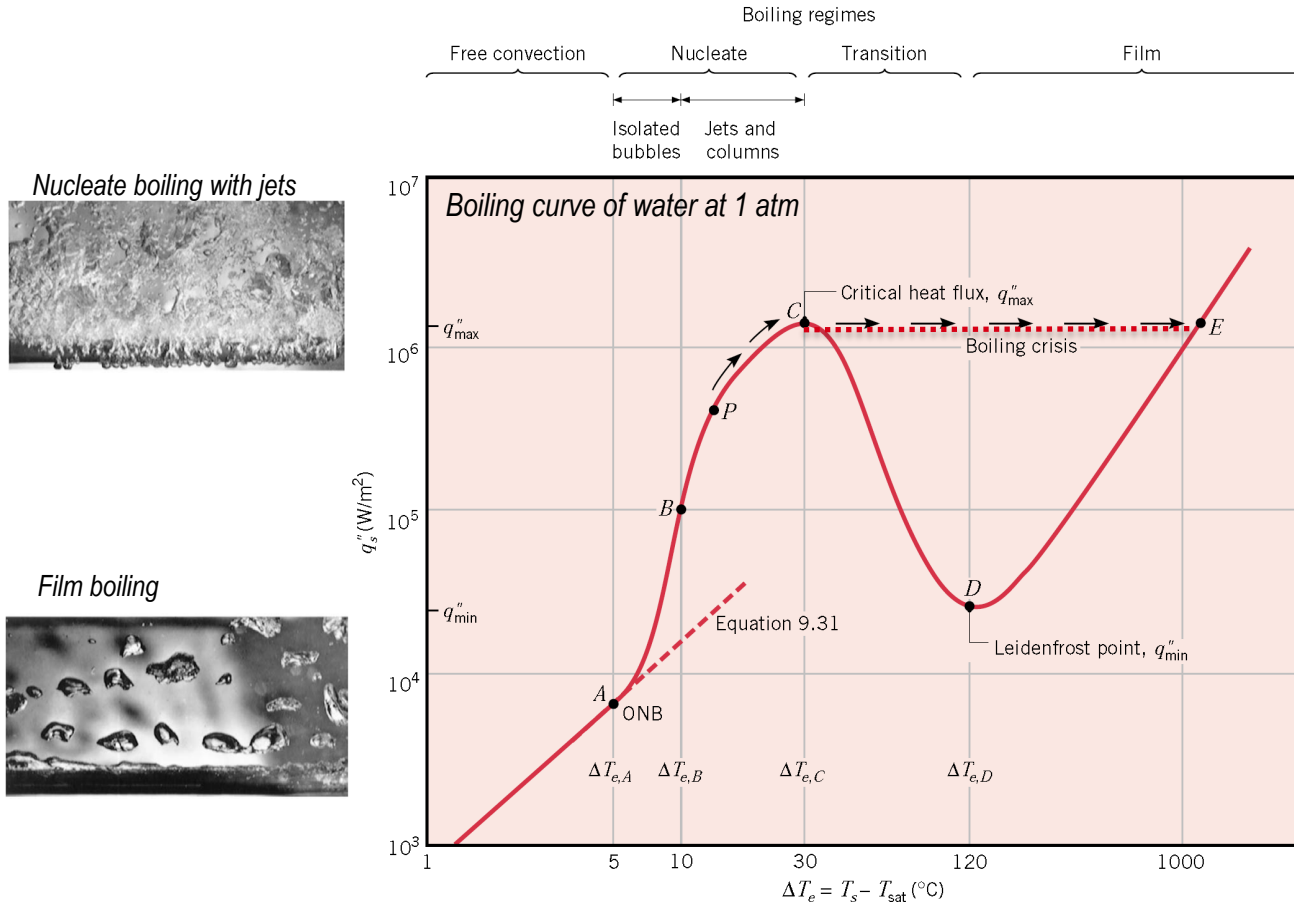
$T_s > T_{sat}$ , the bubble must rise

### Subcooled Boiling

$T_s < T_{sat}$ , the bubbles can re-condense in the liquid

# Saturated Pool Boiling

$$q_s'' = h(T_s - T_{sat}) = h\Delta T_e$$



The solid curve is followed when we control  $\Delta T_e$ . However in most applications we control  $q_s''$ . In such a case (as in the previous experiment) we observe:

C → E : boiling crisis - past the critical heat flux a film of vapor rapidly replaces isolated bubbles. The thermal conductivity of the vapor film is much less than that of the liquid and the surface temperature suddenly increases to much higher values

This can cause the failure of the component. Hence, when designing a heat exchanger we must be sure not to surpass the critical heat flux condition.

# This Lecture

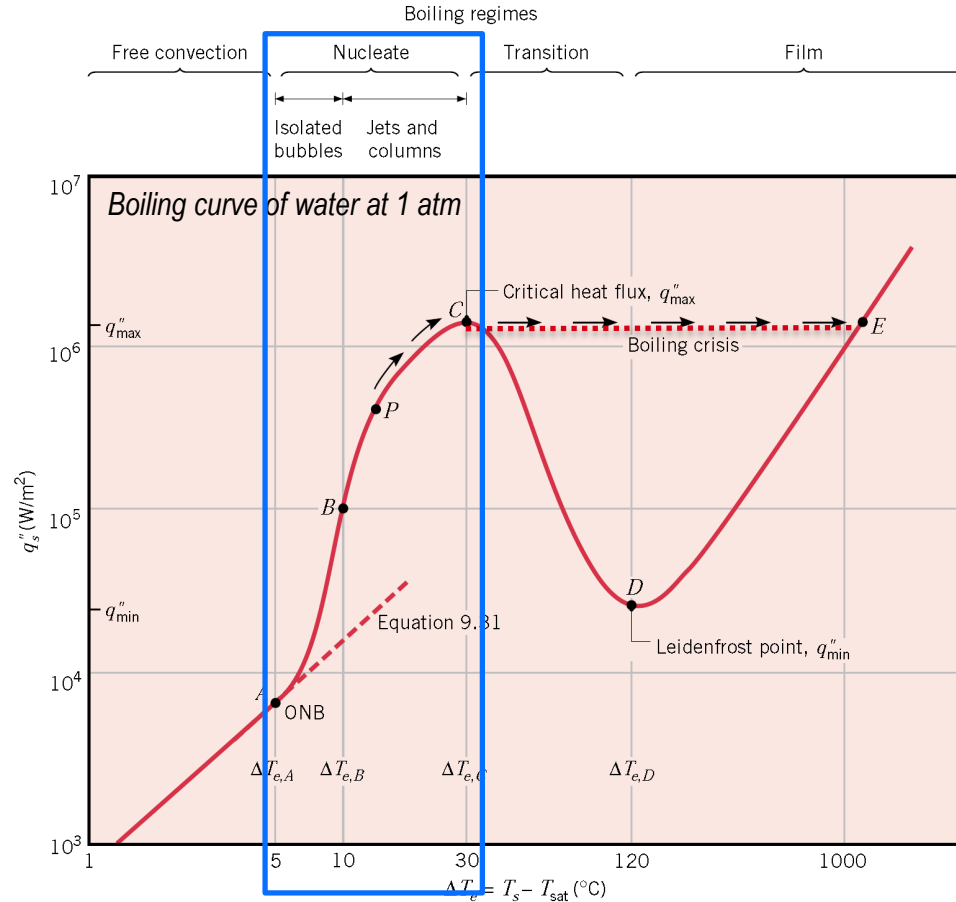
- ❑ Correlations for Nucleate and Film Pool Boiling

Learning Objectives:

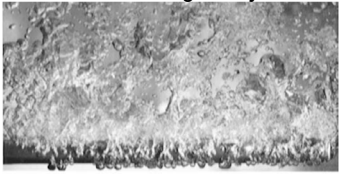
- ❑ Calculate heat flux and temperature difference during boiling

# Saturated Pool Boiling

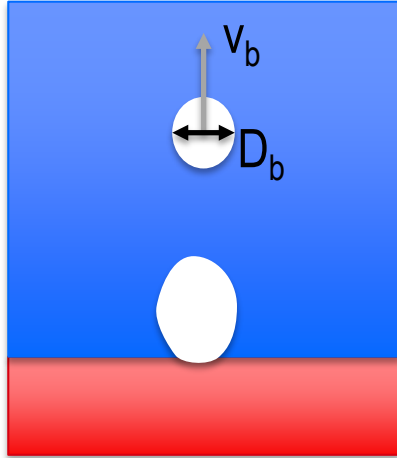
$$q_s'' = h(T_s - T_{sat}) = h\Delta T_e$$



Nucleate boiling with jets



# Nucleate Pool Boiling Correlations



Bubbles can be considered to cause forced convection

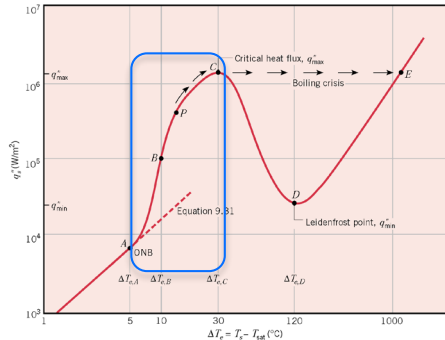
Define a characteristic length and velocity to calculate Re and Nu for boiling

Characteristic length:  $D_b \propto \sqrt{\frac{\sigma}{g(\rho_l - \rho_v)}}$  Ratio of surface tension and buoyancy

Characteristic velocity:  $V \propto \frac{D_b}{t_b}$  Distance travelled by the liquid to fill the void of a bubble  
Time interval between bubble detachment

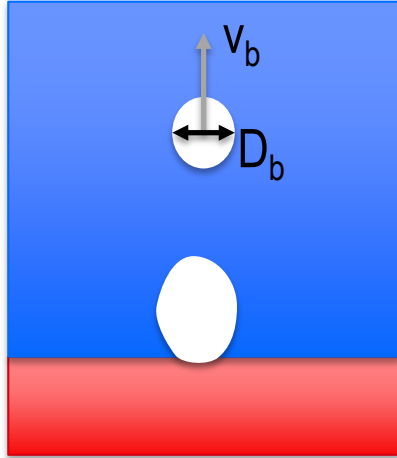
$V \propto \frac{D_b}{\left( \frac{\rho_l h_{fg} D_b^3}{q_s'' D_b^2} \right)}$  Energy it takes to form a bubble  
Heat transferred from the solid to the vapor

→  $V \propto \frac{q_s''}{\rho_l h_{fg}}$





# Nucleate Pool Boiling Correlations



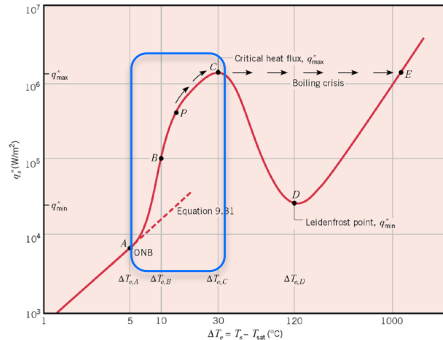
$$q_s'' = \mu_l h_{fg} \left[ \frac{g(\rho_l - \rho_v)}{\sigma} \right]^{1/2} \left( \frac{c_{p,l} \Delta T_e}{C_{s,f} h_{fg} Pr_l^n} \right)^3$$

$h_{fg}$  = (latent) heat of vaporization (Table A6)

!!Units in tables are [kJ/kg] !!

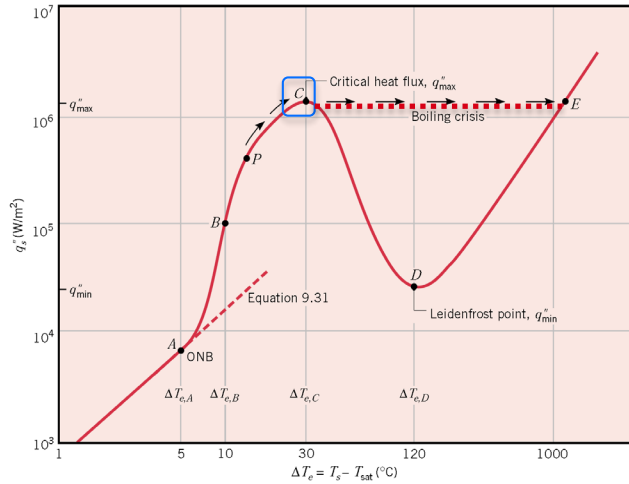
**TABLE 10.1** Values of  $C_{s,f}$  for various surface–fluid combinations [5–7]

Surface–Fluid Combination	$C_{s,f}$	$n$
Water–copper		
Scored	0.0068	1.0
Polished	0.0128	1.0
Water–stainless steel		
Chemically etched	0.0133	1.0
Mechanically polished	0.0132	1.0
Ground and polished	0.0080	1.0
Water–brass	0.0060	1.0
Water–nickel	0.006	1.0
Water–platinum	0.0130	1.0
<i>n</i> -Pentane–copper		
Polished	0.0154	1.7
Lapped	0.0049	1.7
Benzene–chromium	0.0101	1.7
Ethyl alcohol–chromium	0.0027	1.7



The Rohsenow correlation applies only for clean surfaces. When it is used to estimate the heat flux, errors can amount to  $\pm 100\%$ . However, since  $\Delta T_e \propto (q_s'')^{1/3}$ , this error is reduced by a factor of 3 when the expression is used to estimate  $\Delta T_e$  from knowledge of  $q_s''$ . Also, since  $q_s'' \propto h_{fg}^{-2}$  and  $h_{fg}$  decreases with increasing saturation pressure (temperature), the nucleate boiling heat flux will increase as the liquid is pressurized.

# Pool Boiling Critical Heat Flux



$$q''_{max} = Ch_{fg}\rho_v \left[ \frac{\sigma g(\rho_l - \rho_v)}{\rho_v^2} \right]^{1/4}$$

$C = \pi/24$  for large horizontal cylinders, spheres, and finite heated surfaces

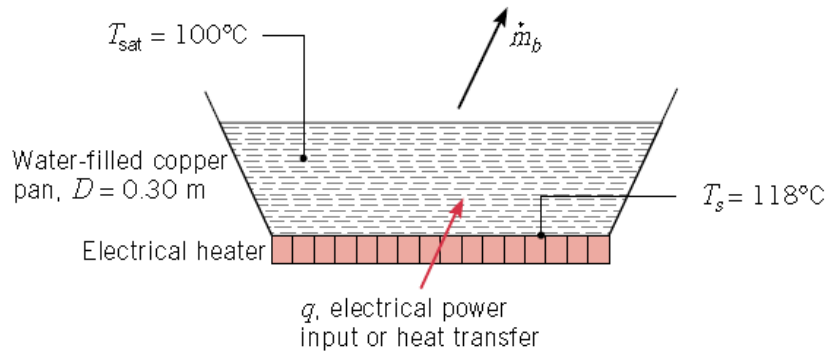
$C = 0.149$  for large horizontal plates

The properties are evaluated at the saturation temperature

Note that the critical heat flux depends on pressure.

# Nucleate Pool Boiling – Example

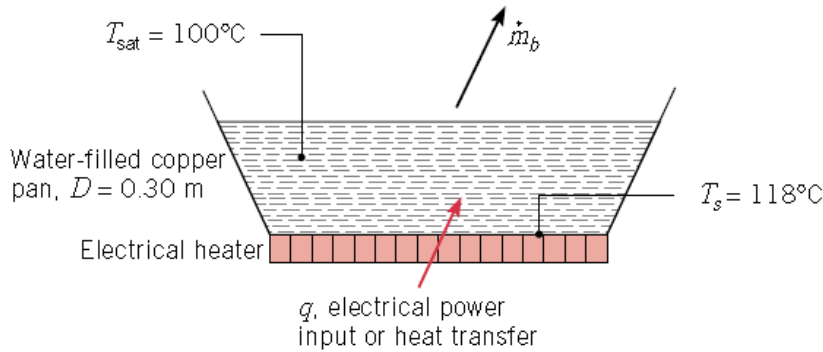
The bottom of a copper pan, 0.3 m in diameter, is maintained at  $118^\circ\text{C}$  by an electric heater. Estimate the power required to boil water in this pan. What is the evaporation rate? Estimate the critical heat flux.



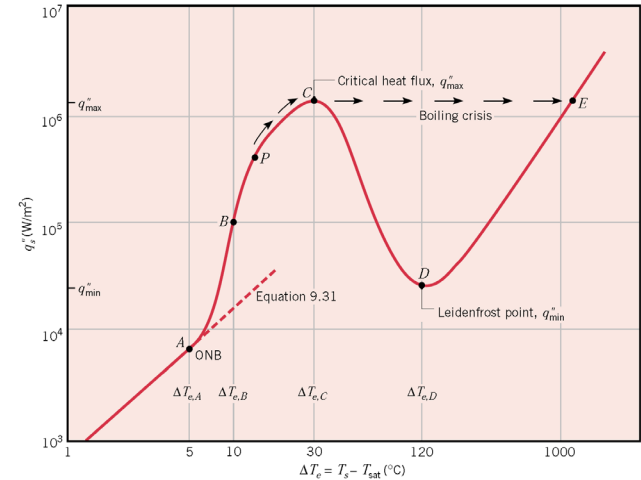
1. Steady-state conditions.
2. Water exposed to standard atmospheric pressure, 1.01 bar.
3. Water at uniform temperature  $T_{\text{sat}} = 100^\circ\text{C}$ .
4. Large pan bottom surface of polished copper.
5. Negligible losses from heater to surroundings.

# Nucleate Pool Boiling – Example

The bottom of a copper pan, 0.3 m in diameter, is maintained at  $118^\circ\text{C}$  by an electric heater. Estimate the power required to boil water in this pan. What is the evaporation rate? Estimate the critical heat flux.



**Properties:** Table A.6, saturated water, liquid ( $100^\circ\text{C}$ ):  $\rho_l = 1/v_f = 957.9\text{ kg/m}^3$ ,  $c_{p,l} = c_{p,f} = 4.217\text{ kJ/kg} \cdot \text{K}$ ,  $\mu_l = \mu_f = 279 \times 10^{-6}\text{ N} \cdot \text{s/m}^2$ ,  $Pr_l = Pr_f = 1.76$ ,  $h_{f,g} = 2257\text{ kJ/kg}$ ,  $\sigma = 58.9 \times 10^{-3}\text{ N/m}$ . Table A.6, saturated water, vapor ( $100^\circ\text{C}$ ):  $\rho_v = 1/v_g = 0.5956\text{ kg/m}^3$ .



$$\Delta T_e \equiv T_s - T_{\text{sat}} = 118^\circ\text{C} - 100^\circ\text{C} = 18^\circ\text{C}$$

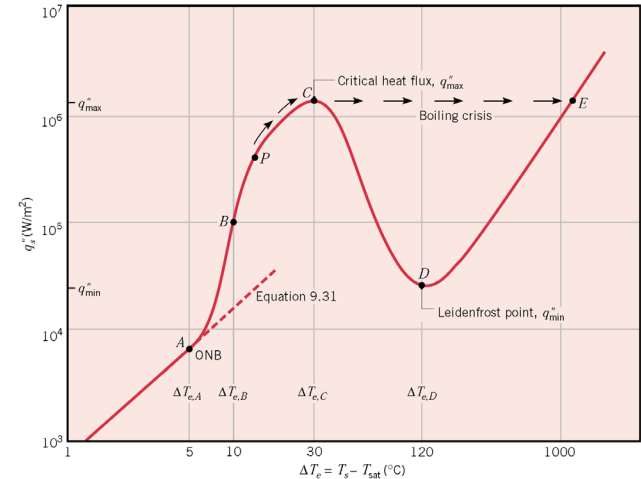
# Nucleate Pool Boiling – Example

The bottom of a copper pan, 0.3 m in diameter, is maintained at 118°C by an electric heater. Estimate the power required to boil water in this pan. What is the evaporation rate? Estimate the critical heat flux.

$$q_s'' = \mu_l h_{fg} \left[ \frac{g(\rho_l - \rho_v)}{\sigma} \right]^{1/2} \left( \frac{c_{p,l} \Delta T_e}{C_{s,f} h_{fg} Pr_l^n} \right)^3$$

**TABLE 10.1** Values of  $C_{s,f}$  for various surface–fluid combinations [5–7]

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$$\Delta T_e \equiv T_s - T_{sat} = 118^\circ\text{C} - 100^\circ\text{C} = 18^\circ\text{C}$$

# Nucleate Pool Boiling – Example

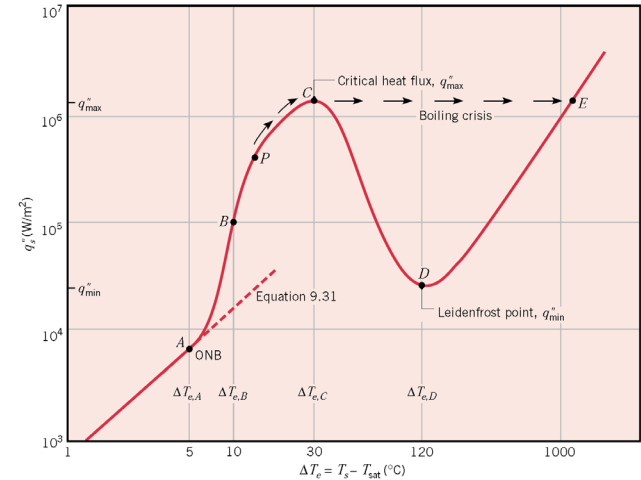
The bottom of a copper pan, 0.3 m in diameter, is maintained at 118°C by an electric heater. Estimate the power required to boil water in this pan. What is the evaporation rate? Estimate the critical heat flux.

$$q_s'' = 279 \times 10^{-6} \text{ N} \cdot \text{s/m}^2 \times 2257 \times 10^3 \text{ J/kg} \\ \times \left[ \frac{9.8 \text{ m/s}^2 (957.9 - 0.5956) \text{ kg/m}^3}{58.9 \times 10^{-3} \text{ N/m}} \right]^{1/2} \\ \times \left( \frac{4.217 \times 10^3 \text{ J/kg} \cdot \text{K} \times 18^\circ\text{C}}{0.0128 \times 2257 \times 10^3 \text{ J/kg} \times 1.76} \right)^3 = 836 \text{ kW/m}^2$$



$$q_s = q_s'' \times A = q_s'' \times \frac{\pi D^2}{4}$$

$$q_s = 836 \times 10^3 \text{ W/m}^2 \times \frac{\pi (0.30 \text{ m})^2}{4} = 59.1 \text{ kW}$$



$$\Delta T_e \equiv T_s - T_{\text{sat}} = 118^\circ\text{C} - 100^\circ\text{C} = 18^\circ\text{C}$$

# Nucleate Pool Boiling – Example

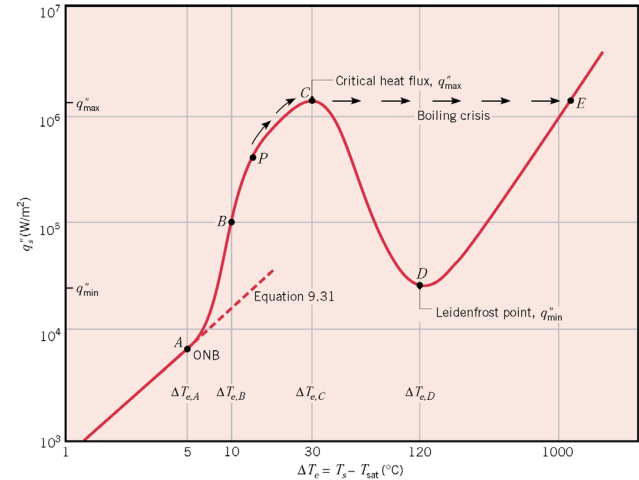
The bottom of a copper pan, 0.3 m in diameter, is maintained at 118°C by an electric heater. Estimate the power required to boil water in this pan. What is the evaporation rate? Estimate the critical heat flux.

Under steady-state conditions all heat addition to the pan will result in water evaporation from the pan. Hence

$$q_s = \dot{m}_b h_{fg}$$

where  $\dot{m}_b$  is the rate at which water evaporates from the free surface to the room. It follows that

$$\dot{m}_b = \frac{q_s}{h_{fg}} = \frac{5.91 \times 10^4 \text{ W}}{2257 \times 10^3 \text{ J/kg}} = 0.0262 \text{ kg/s} = 94 \text{ kg/h}$$



$$\Delta T_e \equiv T_s - T_{\text{sat}} = 118^\circ\text{C} - 100^\circ\text{C} = 18^\circ\text{C}$$

# Nucleate Pool Boiling – Example

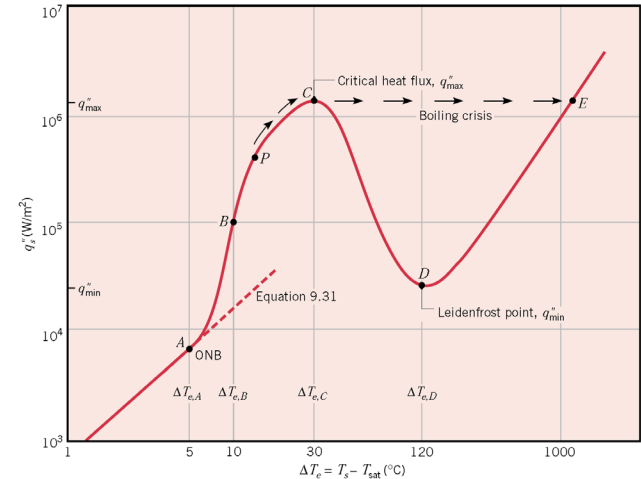
The bottom of a copper pan, 0.3 m in diameter, is maintained at 118°C by an electric heater. Estimate the power required to boil water in this pan. What is the evaporation rate? Estimate the critical heat flux.

$$q''_{\max} = Ch_{fg}\rho_v \left[ \frac{\sigma g(\rho_l - \rho_v)}{\rho_v^2} \right]^{1/4} \quad C = 0.149 \text{ for large horizontal plates}$$

$$q''_{\max} = 0.149 h_{fg} \rho_v \left[ \frac{\sigma g(\rho_l - \rho_v)}{\rho_v^2} \right]^{1/4}$$

$$q''_{\max} = 0.149 \times 2257 \times 10^3 \text{ J/kg} \times 0.5956 \text{ kg/m}^3 \times \left[ \frac{58.9 \times 10^{-3} \text{ N/m} \times 9.8 \text{ m/s}^2 (957.9 - 0.5956) \text{ kg/m}^3}{(0.5956)^2 (\text{kg/m}^3)^2} \right]^{1/4}$$

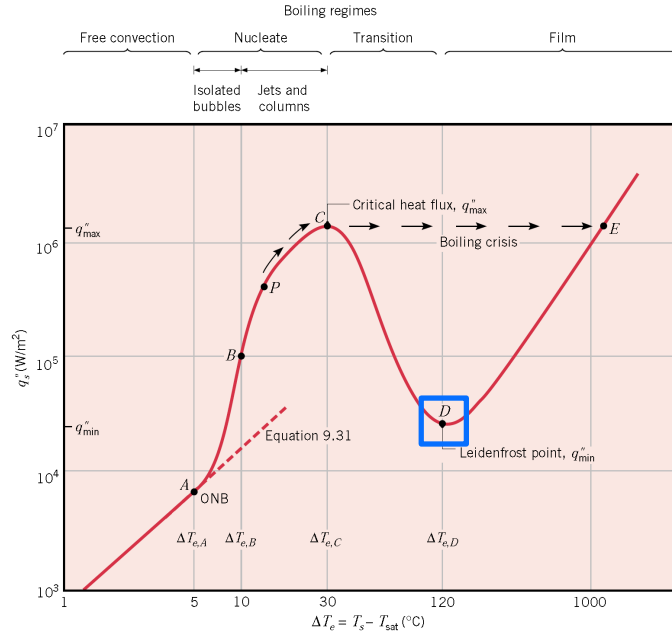
$$q''_{\max} = 1.26 \text{ MW/m}^2$$



$$\Delta T_e \equiv T_s - T_{\text{sat}} = 118^\circ\text{C} - 100^\circ\text{C} = 18^\circ\text{C}$$



# Minimum Heat Flux



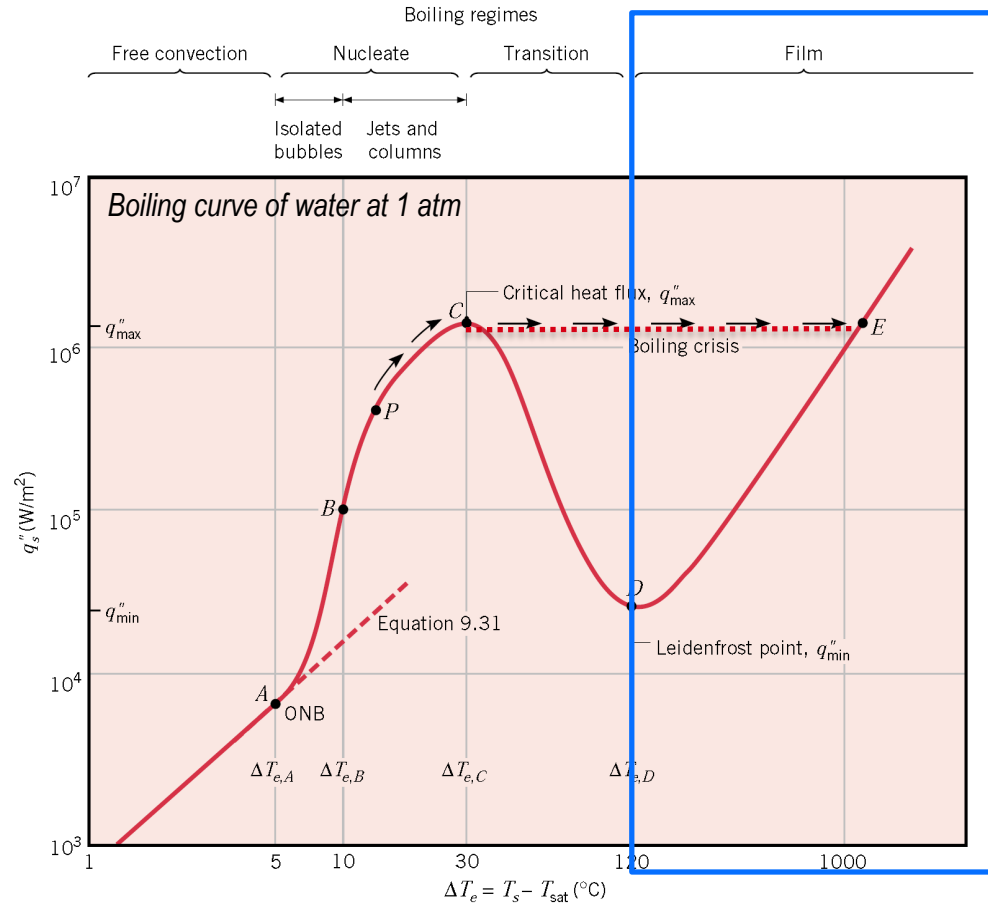
Zuber [10] used stability theory to derive the following expression for the minimum heat flux,  $q''_{s,D} = q''_{min}$ , from a large horizontal plate.

$$q''_{min} = C \rho_v h_{fg} \left[ \frac{g \sigma (\rho_l - \rho_v)}{(\rho_l + \rho_v)^2} \right]^{1/4} \quad (10.7)$$

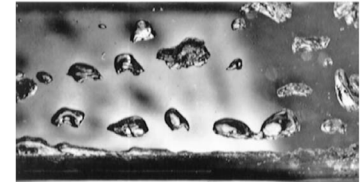
where the properties are evaluated at the saturation temperature. The constant,  $C = 0.09$ , has been experimentally determined by Berenson [14]. This result is accurate to approximately 50% for most fluids at moderate pressures but provides poorer estimates at higher pressures [15]. A similar result has been obtained for horizontal cylinders [16].

# Film Pool Boiling

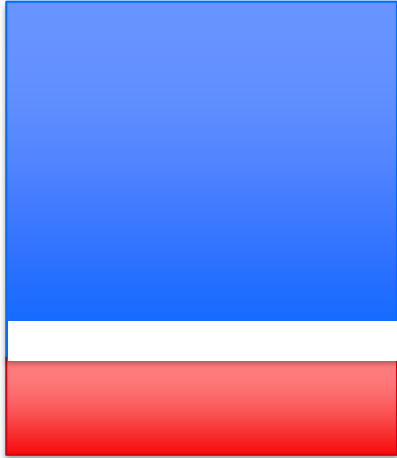
$$q_s'' = h(T_s - T_{sat}) = h\Delta T_e$$



Film boiling



# Film Pool Boiling



$$\overline{Nu}_D = C \left[ \frac{g \rho_v (\rho_l - \rho_v) h'_{fg} D^3}{\mu_v k_v (T_s - T_{sat})} \right]^{1/4}$$

Where  $h'_{fg} = h_{fg} + 0.8 c_{p,v} (T_s - T_{sat})$

$C = 0.62$  for horizontal cylinders

$C = 0.67$  for spheres

With properties estimated at  $T_f = \frac{(T_s + T_{sat})}{2}$

If  $T_s > 300C$ , radiation is also present. We estimate the total convection coefficient as:

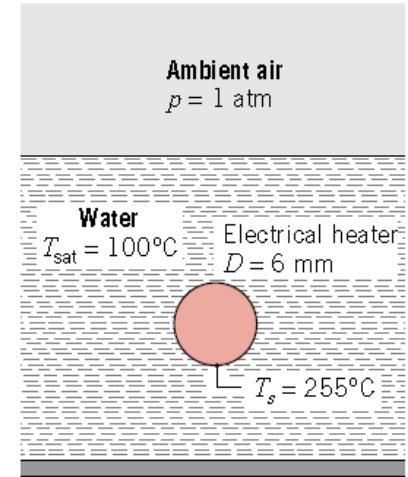
$$\bar{h} = \overline{h_{conv}} + \frac{3}{4} \overline{h_{rad}}$$

where  $\overline{h_{conv}}$  has to be estimated with the previous correlation and  $\overline{h_{rad}} = [\epsilon \sigma (T_s^4 - T_{sat}^4)] / (T_s - T_{sat})$

# Film Pool Boiling – Example

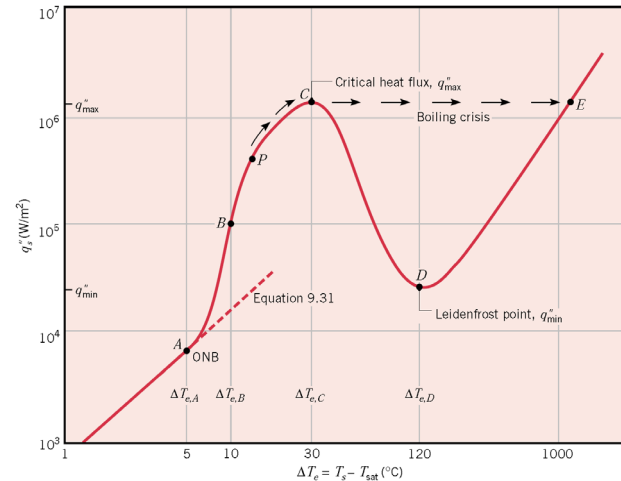
A metal-clad heating element of 6-mm diameter and emissivity  $\varepsilon = 1$  is horizontally immersed in a water bath. The surface temperature of the metal is  $255^\circ\text{C}$  under steady-state boiling conditions. Estimate the power dissipation per unit length of the heater.

**Properties:** Table A.6, saturated water, liquid ( $100^\circ\text{C}$ ):  $\rho_l = 1/\nu_f = 957.9 \text{ kg/m}^3$ ,  $h_{fg} = 2257 \text{ kJ/kg}$ . Table A.4, water vapor at atmospheric pressure ( $T_f \approx 450 \text{ K}$ ):  $\rho_v = 0.4902 \text{ kg/m}^3$ ,  $c_{p,v} = 1.980 \text{ kJ/kg} \cdot \text{K}$ ,  $k_v = 0.0299 \text{ W/m} \cdot \text{K}$ ,  $\mu_v = 15.25 \times 10^{-6} \text{ N} \cdot \text{s/m}^2$ .



The excess temperature is

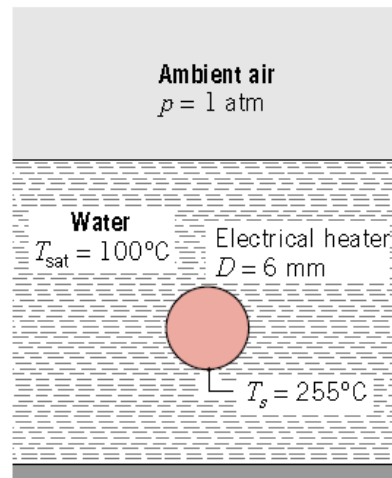
$$\Delta T_e = T_s - T_{\text{sat}} = 255^\circ\text{C} - 100^\circ\text{C} = 155^\circ\text{C}$$



# Film Pool Boiling – Example

A metal-clad heating element of 6-mm diameter and emissivity  $\varepsilon = 1$  is horizontally immersed in a water bath. The surface temperature of the metal is  $255^\circ\text{C}$  under steady-state boiling conditions. Estimate the power dissipation per unit length of the heater.

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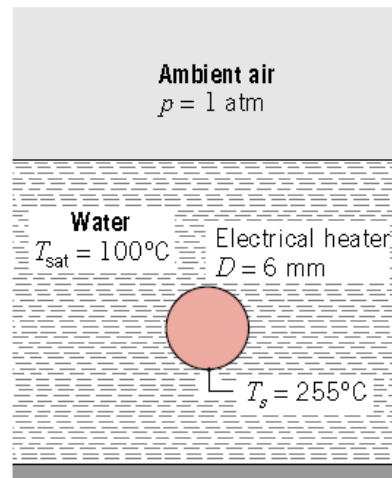


$$\begin{aligned}
 q'_s &= q''_s \pi D = \bar{h} \pi D \Delta T_e \\
 \bar{h}^{4/3} &= \bar{h}_{\text{conv}}^{4/3} + \bar{h}_{\text{rad}} \bar{h}^{1/3} \\
 \bar{h}_{\text{conv}} &= 0.62 \left[ \frac{k_v^3 \rho_v (\rho_l - \rho_v) g (h_{fg} + 0.8 c_{p,v} \Delta T_e)}{\mu_v D \Delta T_e} \right]^{1/4} \\
 &= 0.62 \times \left[ \frac{(0.0299)^3 (\text{W/m} \cdot \text{K})^3 \times 0.4902 \text{ kg/m}^3 (957.9 - 0.4902) \text{ kg/m}^3 \times 9.8 \text{ m/s}^2}{1} \right. \\
 &\quad \times \left. \frac{(2257 \times 10^3 \text{ J/kg} + 0.8 \times 1.98 \times 10^3 \text{ J/kg} \cdot \text{K} \times 155^\circ\text{C})}{15.25 \times 10^{-6} \text{ N} \cdot \text{s/m}^2 \times 6 \times 10^{-3} \text{ m} \times 155^\circ\text{C}} \right]^{1/4} \\
 &= 238 \text{ W/m}^2 \cdot \text{K}
 \end{aligned}$$

# Film Pool Boiling – Example

A metal-clad heating element of 6-mm diameter and emissivity  $\varepsilon = 1$  is horizontally immersed in a water bath. The surface temperature of the metal is  $255^\circ\text{C}$  under steady-state boiling conditions. Estimate the power dissipation per unit length of the heater.

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$$q'_s = q''_s \pi D = \bar{h} \pi D \Delta T_e$$

$$\bar{h}_{\text{rad}} = \frac{\varepsilon \sigma (T_s^4 - T_{\text{sat}}^4)}{T_s - T_{\text{sat}}}$$

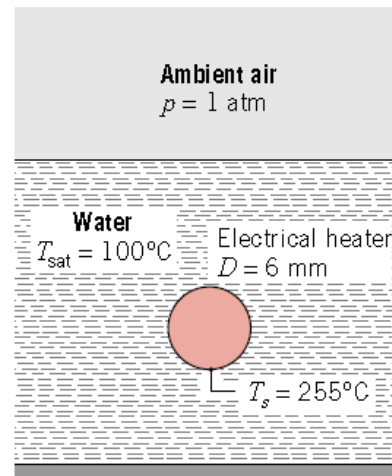
$$\bar{h}^{4/3} = \bar{h}_{\text{conv}}^{4/3} + \bar{h}_{\text{rad}} \bar{h}^{1/3}$$

$$= \frac{5.67 \times 10^{-8} \text{ W/m}^2 \cdot \text{K}^4 (528^4 - 373^4) \text{ K}^4}{(528 - 373) \text{ K}} = 21.3 \text{ W/m}^2 \cdot \text{K}$$

# Film Pool Boiling – Example

A metal-clad heating element of 6-mm diameter and emissivity  $\varepsilon = 1$  is horizontally immersed in a water bath. The surface temperature of the metal is  $255^\circ\text{C}$  under steady-state boiling conditions. Estimate the power dissipation per unit length of the heater.

**Properties:** Table A.6, saturated water, liquid ( $100^\circ\text{C}$ ):  $\rho_l = 1/v_f = 957.9 \text{ kg/m}^3$ ,  $h_{fg} = 2257 \text{ kJ/kg}$ . Table A.4, water vapor at atmospheric pressure ( $T_f \approx 450 \text{ K}$ ):  $\rho_v = 0.4902 \text{ kg/m}^3$ ,  $c_{p,v} = 1.980 \text{ kJ/kg} \cdot \text{K}$ ,  $k_v = 0.0299 \text{ W/m} \cdot \text{K}$ ,  $\mu_v = 15.25 \times 10^{-6} \text{ N} \cdot \text{s/m}^2$ .



$$q'_s = q''_s \pi D = \bar{h} \pi D \Delta T_e$$

$$\bar{h}^{4/3} = \bar{h}_{\text{conv}}^{4/3} + \bar{h}_{\text{rad}} \bar{h}^{1/3} \quad \Rightarrow \quad \bar{h}^{4/3} = 238^{4/3} + 21.3 \bar{h}^{1/3} \quad \Rightarrow \quad \bar{h} = 254.1 \text{ W/m}^2 \cdot \text{K}$$

$$q'_s = 254.1 \text{ W/m}^2 \cdot \text{K} \times \pi \times 6 \times 10^{-3} \text{ m} \times 155^\circ\text{C} = 742 \text{ W/m}$$

# This Lecture



Correlations for Nucleate and Film Pool Boiling

Learning Objectives:



Calculate heat flux and temperature difference during boiling



# Next Lecture

- ❑ Forced Convection Boiling
  - ❑ External
  - ❑ Internal

## Learning Objectives:

- ❑ Calculate heat flux and convection coefficient in forced convection