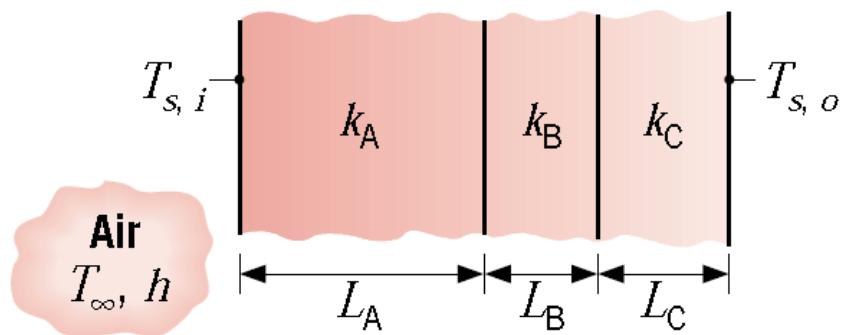


## Exercise 1(Points: 5.5)

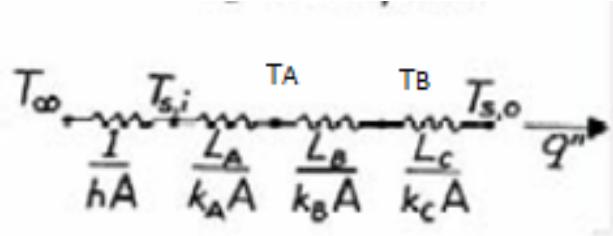
The composite wall of an oven consists of three materials (A,B and C) two of which are of known thermal conductivity,  $k_A = 20W/mK$  and  $k_C = 50W/mK$ , and known thickness,  $L_A = 0.3m$  and  $L_C = 0.15m$ . The third material, B, which is sandwiched between material A and C, is of known thickness  $L_B = 0.15m$  but unknown thermal conductivity  $k_B$ . Under steady-state operating conditions, measurements reveal an outer surface temperature of  $T_{s,o} = 20C$ , an inner surface temperature  $T_{s,i} = 600C$  and an oven air temperature  $T_\infty = 800C$ . The inside convection coefficient is known and equal to  $h_i = 25W/m^2K$ .

- Draw the equivalent electrical circuit for the entire system (oven and wall). Indicate clearly the relevant temperatures in the circuit.
- Write the expression for every thermal resistance in the system
- Calculate the heat flux flowing through the wall as well as the temperatures at the interfaces within the wall
- Determine the thermal conductivity of the layer B



## Solution

a) **1pt** : 0.5 for the three conduction resistors, 0.5 for the convection resistor.



b) **1pt**: 0.25pts for every resistance expression

$$R_{conv} = \frac{1}{h_i}$$

$$R_{cond,A} = \frac{L_A}{k_A}$$

$$R_{cond,B} = \frac{L_B}{k_B}$$

$$R_{cond,C} = \frac{L_C}{k_C}$$

c) **2.5pt** : 0.5 for realizing that the heat transfer through the wall is the same as by convection; 0.5 for the expression and 0.5 for the value; 0.5 for  $T_A$  and 0.5 for  $T_B$  (0.25 for expression and 0.25 for value).

$$q'' = h_i(T_\infty - T_{s,i})$$

$$q'' = 25W/mK(800 - 600) = 5000W/m^2$$

$$q'' = \frac{k_A}{L_A}(T_{s,i} - T_A)$$

$$T_A = 525K = 798K$$

$$q'' = \frac{k_C}{L_C}(T_B - T_{s,o})$$

$$T_B = 35K = 308K$$

d) **1pt**: 0.5 for the expression and 0.25 for  $k_B$  expression and 0.25 for the value

$$q'' = \frac{T_{s,i} - T_{s,o}}{R_{cond,A} + R_{cond,B} + R_{cond,C}} = \frac{T_{s,i} - T_{s,o}}{\frac{L_A}{k_A} + \frac{L_B}{k_B} + \frac{L_C}{k_C}}$$

$$k_B = L_B \left( \frac{T_{s,i} - T_{s,o}}{q''} - \frac{L_A}{k_A} - \frac{L_C}{k_C} \right)^{-1} = 1.53W/mK$$

or

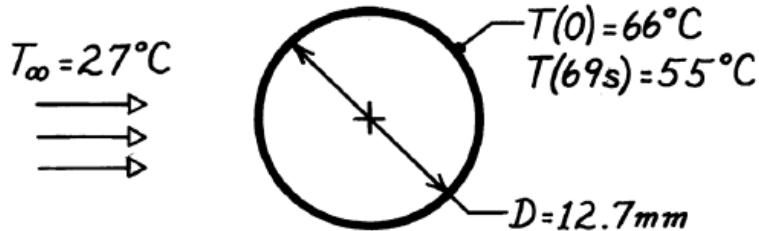
$$k_B = \frac{q'' L_B}{T_A - T_B} = 1.53W/mK$$

## Exercise 2(Points 5.5)

The heat transfer coefficient for air flowing over a sphere is to be determined by observing the temperature-time history of a sphere fabricated from pure copper. The sphere, which has a diameter of  $D = 12.7\text{mm}$  is at an initial temperature of  $T_i = 66\text{C}$  before it is inserted into an airstream having a temperature of  $T_\infty = 27\text{C}$ . After  $69\text{s}$  in the airstream, a thermocouple on the outer surface of the sphere indicates  $55\text{C}$ .

- a) After choosing a suitable reference temperature, and justifying your choice, list the following thermophysical properties of copper: density, specific heat and thermal conductivity.
- b) Assume that the sphere behaves as an isothermal object and calculate the heat transfer coefficient
- c) Verify that the assumption of part b) was correct

## Solution



a) **1.5pt** : 0.25 for choosing  $T_{mean,Cu}$ , 0.25 for right  $T_s$ , 0.25 for  $T_{mean,Cu}$  value. 0.25 for each correct interpolation.

$$T_{ref,Cu} = T_{mean,Cu} = (66 + 55)/2 + 273.15 = 333.65K$$

. From Table A1 (interpolation):

$$\rho = 8933 \text{ kg/Km}$$

$$c_p = 389 \text{ J/kgK}$$

$$k = 398 \text{ W/mK}$$

b) **2.5pt**: 0.5 for lumped capacitance model; 0.5 for correct expression; 0.25 for volume and 0.25 for area; 0.5 for recognizing  $T(69s) = 55^\circ\text{C}$ ; 0.5 for calculating  $h$  (0.25 for  $\tau$  and 0.25 for  $h$ ).

Isothermal sphere implies we can use the lumped capacitance model.

$$\frac{\theta(t)}{\theta_0} = \frac{T(t) - T_\infty}{T_i - T_\infty} = \exp\left(-\frac{hA_s}{\rho V c_p} t\right) = \exp\left(-\frac{t}{\tau}\right)$$

where

$$V = \frac{\pi D^3}{6}$$

$$A_s = \pi D^2$$

At  $t = 69\text{s}$ :

$$\frac{\theta(69s)}{\theta_0} = \frac{T(69s) - T_\infty}{T(0) - T_\infty} = \frac{55 - 27}{66 - 27} = 0.718$$

Solving for  $\tau$  we have:

$$\tau = -\frac{69s}{\ln(0.718)} = 208s$$

Therefore from the expression of tau we obtain:

$$h = \frac{\rho V c_p}{A_s \tau} = \frac{8933(\pi 0.0127^3/6)389}{\pi 0.0127^2 208} = 35.3 \text{ W/m}^2\text{K}$$

c) **1.5pt** ; 0.5 for choosing to calculate  $Bi$ ; 0.5 for the right value; 0.5 for the conclusion

$$Bi = \frac{hV}{kA} = \frac{hD}{6k} = 0.000188 \ll 0.1$$

Therefore the initial assumption is valid.

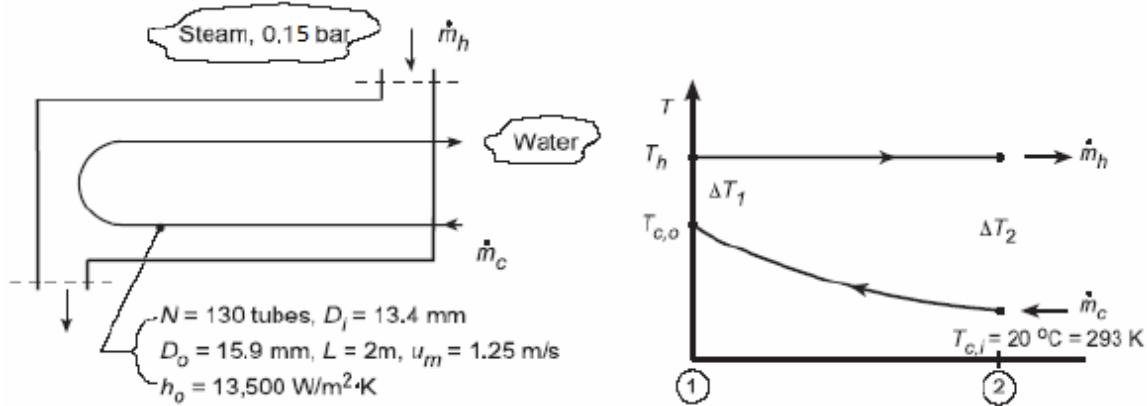
### Exercise 3(Points: 13)

Saturated steam at  $0.15\text{bar}$  is condensed in a shell-and-tube heat exchanger with one shell pass and two tube passes consisting of 130 brass (i.e Copper - Zinc alloy with 70/30 composition) tubes, each with a length per pass of  $L = 2\text{m}$ . The tubes have inner and outer diameters of  $D_i = 13.4\text{mm}$  and  $D_o = 15.9\text{mm}$ , respectively. Cooling water enters the tubes at  $20\text{C}$  with a mean velocity of  $v = 1.25\text{m/s}$ . The heat transfer coefficient for condensation on the outer surfaces of the tubes is  $h_o = 13500\text{W/m}^2\text{K}$ .

- a) On the same graph, draw a qualitative sketch of the evolution of the steam and water temperatures as the two fluids go through the heat exchanger
- b) Using a reference average temperature for the water side equal to  $T_{ref,c} = 305\text{K}$ , list the values of density, specific heat  $c_p$ , viscosity, thermal conductivity, Prandtl.
- c) For the steam side indicate the reference temperature  $T_{ref,h}$  and list the values of latent heat and specific heat  $c_p$ .
- d) List the value of the thermal conductivity of the brass tubes estimated at the average temperature between the hot and cold side reference temperatures ( $T_{ref,h}$  and  $T_{ref,c}$ ).
- e) Write the expression for the overall heat transfer coefficient and calculate its value with respect to the outside area of the tube. Clearly explain your choice of the convection correlations.
- f) Determine the cooling water outlet temperature
- g) Determine the steam condensation rate

## Solution

a) **1.5pt:** 1 for constant temperature of the steam side; 0.5 for the water side.



b) **1.5pt:** 0.5 for  $\rho$ ; 0.25 for each of the other 4 values

From table A6 with  $T_{ref,c} = 305 \text{ K}$ :

$$\rho = 1/v_f = 995 \text{ kg/m}^3$$

$$c_p = 4178 \text{ J/kgK}$$

$$\mu = 769 \cdot 10^{-6} \text{ Ns/m}^2$$

$$k = 0.620 \text{ W/mK}$$

$$Pr = 5.2$$

c) **1pt:** 0.5 for the ref temperature; 0.25 for each of the 2 values

From table A6 we estimate the steam properties at (interpolation):

$$T_{ref,h} = T_{sat}(0.15 \text{ bar}) = 327 \text{ K}$$

$$h_{fg} = 2373 \text{ kJ/kg} = 2.373 \cdot 10^6 \text{ J/kg}$$

$$c_p = 1906 \text{ J/kgK}$$

d) **0.5pt:** 0.25 for the reference temperature value; 0.25 for the value

From table A1:

$$T_{ref,tube} = (T_{ref,c} + T_{ref,h})/2 = 316 \text{ K}$$

$$k = 119.4 \text{ W/mK}$$

e) **4.5pt:** 2.25 U expression (0.5 for each term (3x0.5) - 0.25 for type of resistance, 0.25 for expression - and 0.75 for the correct areas: 0.25 for N in  $A_o$ , 0.25 for  $2L$  and 0.25 for N in  $R_{cond}$ ); 0.25 for convection type; 0.25 for Re value; 0.25 for flow condition; 0.25 for convection correlation; 0.25 for correct exponent; 0.25 for value of Nu; 0.25 for value of h; 0.5 for value of U.

$$\frac{1}{U_o A_o} = \frac{1}{A_o h_o} + \frac{1}{2\pi k(2L)N} \ln \frac{r_o}{r_i} + \frac{1}{A_i h_i} = \frac{1}{\pi D_o (2L) N h_o} + \frac{1}{2\pi k(2L)N} \ln \frac{r_o}{r_i} + \frac{1}{\pi D_i (2L) N h_i}$$

$$U_o = \left[ \frac{1}{h_o} + \frac{r_o}{k} \ln \frac{r_o}{r_i} + \frac{r_o}{r_i} \frac{1}{h_i} \right]^{-1}$$

Forced internal convection (circular tubes)

$$Re_{D,i} = \frac{\rho v D_i}{\mu} = 21673 >> 2300$$

The flow is turbulent.

$$Nu_D = \frac{h_i D_i}{k_f} = 0.023 Re_D^{0.8} Pr_f^n$$

The water is heating:

$$n = 0.4$$

$$Nu_D = 0.023 \cdot (21673)^{0.8} \cdot (5.2)^{0.4} = 130.9$$

$$h_i = \frac{k_f}{D_i} Nu_D = 6057 W/m^2 K$$

and so:

$$U_o = \left[ \frac{1}{13500} + \frac{15.9 \cdot 10^{-3}}{119.4} \ln \frac{15.9}{13.4} + \frac{15.9}{13.4} \frac{1}{6057} \right]^{-1} = 3557 W/m^2 K$$

f) **3.5pt:** 0.5 expression for the energy balance on cold side  $Q$ ; 0.5 choice of  $\epsilon - NTU$  method (expression of  $Q = \epsilon Q_{max}$ ); 0.25 for  $C_h$  and 0.5 for  $C_c$  values - 0.25 for mass flow rate expression and 0.25 for value; 0.25 for correct  $C_{min}$ ; 0.25 for  $NTU$  value; 0.5 for correct  $\epsilon$  expression; 0.25 for  $\epsilon$  value; 0.5 for correct  $T_{c,o}$  value

Energy balance on the cold (water) side:

$$Q = C_c (T_{c,o} - T_{c,i})$$

We use  $\epsilon - NTU$  method:

$$Q = \epsilon Q_{max} = \epsilon C_{min} (T_{h,i} - T_{c,i})$$

$$C_h \rightarrow \infty$$

$$C_c = (\dot{m} c_p)_c = (\rho A v N c_p)_c = (\rho \pi D_i^2 / 4 v N c_p)_c = 22.8 \cdot 4178 = 95270 W/K$$

$$C_{min} = C_c$$

$$NTU = \frac{U_o A_o}{C_{min}} = \frac{U_o (\pi D_o 2LN)}{C_{min}} = \frac{3557(\pi 0.0159 \cdot 4 \cdot 130)}{95270} = 0.968$$

From Table 11.3

$$\epsilon = 1 - epx(-NTU) = 0.62$$

$$T_{c,o} = T_{c,i} + \epsilon(T_{h,i} - T_{c,i}) = 20 + 0.62(327 - 293) = 41.1C$$

g) **0.5pt**: 0.25 expression, 0.25 value

The condensation rate is

$$\dot{m}_h = Q/h_{fg} = C_c(T_{c,o} - T_{c,i})/h_{fg} = 95270(41.1 - 20)/(2.373 \cdot 10^6) = 0.85 \text{ kg/s}$$

## Exercise 4(Points: 10)

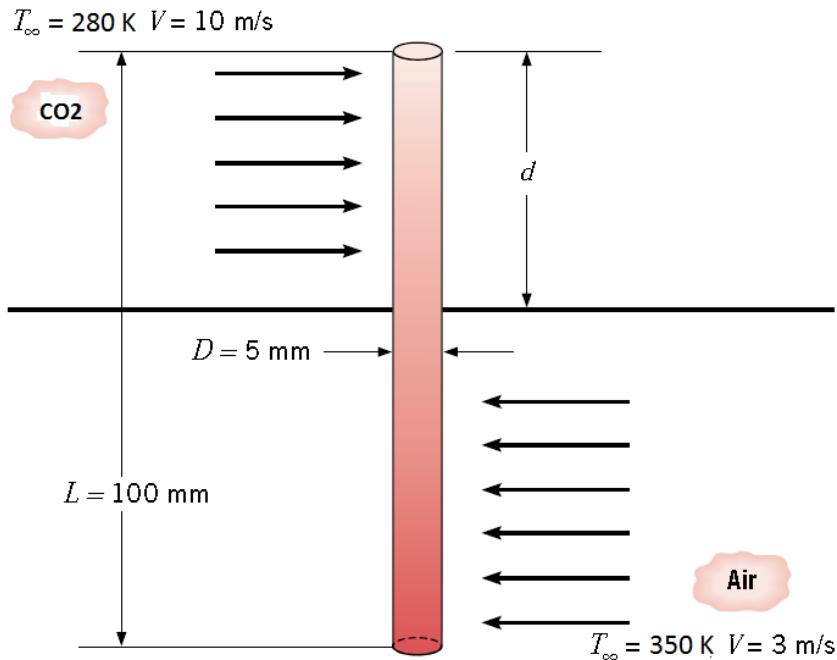
To augment the heat transfer between two flowing fluids, it is proposed to insert a 2024 aluminum pin ( $L = 100\text{mm}$ ,  $D = 5\text{mm}$ ) through the wall separating the two fluids. The pin is inserted to a depth of  $d = 50\text{mm}$  into fluid 1. Fluid 1 is carbon dioxide ( $CO_2$ ) with a mean temperature of  $280K$  and uniform velocity of  $10\text{m/s}$ . Fluid 2 is air with a mean temperature of  $350K$  and mean velocity of  $3\text{m/s}$ .

- List the values of the physical properties of the fluids and solid. For Fluid 1 and 2 use their temperatures as reference. For the aluminum pin use the average temperature between the hot and cold air streams as reference temperature.
- Motivating your choice of the convection correlation, determine the convection coefficients between  $CO_2$  and the pin on one side and the air and the pin on the other side
- Treating the pin as a fin, write the expression for the heat transfer rate between the pin and the fluid on each side
- Determine the temperature at the base of the fin (i.e. at the wall)
- Determine the heat transfer rate from the warm air to the cool air through the pin-fin

*Note:* remember that the hyperbolic functions have the following expressions:

$$\sinh(x) = \frac{e^x - e^{-x}}{2}$$

$$\cosh(x) = \frac{e^x + e^{-x}}{2}$$



## Solution

a) **1.5pt:** 0.5 for all values of CO<sub>2</sub>, 0.5 for all values Air and 0.25 for ref temperature for Al and 0.25 for the k value of aluminum

Table A4 CO<sub>2</sub> ( $T_{f1} = 280K$ ):

$$\begin{aligned}\rho_1 &= 1.9022 \text{ kg/m}^3 \\ \mu_1 &= 140 \cdot 10^{-7} \text{ Ns/m}^2 \\ k_1 &= 0.0152 \text{ W/mK} \\ Pr_1 &= 0.765 \\ c_p &= 830 \text{ J/Kkg} \\ \nu &= 7.36 \cdot 10^{-6} \text{ m}^2/\text{s} \\ \alpha &= 9.63 \cdot 10^{-6} \text{ m}^2/\text{s}\end{aligned}$$

Table A4 Air ( $T_{f2} = 350K$ ):

$$\begin{aligned}\rho_2 &= 0.995 \text{ kg/m}^3 \\ \mu_2 &= 208.2 \cdot 10^{-7} \text{ Ns/m}^2 \\ k_2 &= 0.03 \text{ W/mK} \\ Pr_2 &= 0.7 \\ c_p &= 1009 \text{ J/Kkg} \\ \nu &= 20.92 \cdot 10^{-6} \text{ m}^2/\text{s} \\ \alpha &= 29.9 \cdot 10^{-6} \text{ m}^2/\text{s}\end{aligned}$$

Table A1, Aluminum 2024 ( $T_{Al} = (280 + 350)/2 = 315K$ ):

$$k_{Al} = 176.23 \text{ W/mK}$$

b) **2.5pt:** 0.25 for forced external convection; 0.25 for cylinder geometry; 0.5 for right correlation; 0.5 for Re (0.25 each); 0.5 for Nu (0.25 each); 0.5 for convection coeff (0.25 each).

External forced convection around a cylinder (Churchill-Bernstein correlation):

$$Nu_D = 0.3 + \frac{0.62 Re_D^{1/2} Pr^{1/3}}{[1 + (0.4/Pr)^{2/3}]^{1/4}} \left[ 1 + \left( \frac{Re_D}{282000} \right)^{5/8} \right]^{4/5}$$

We get:

$$\begin{aligned}Re_1 &= \frac{\rho_1 v_1 D}{\mu_1} = 6793 \\ Re_2 &= \frac{\rho_2 v_2 D}{\mu_2} = 716.9\end{aligned}$$

$$Nu_{D,1} = 44.7$$

$$h_1 = \frac{Nu_{D,1} k_1}{D} = 135.88 \text{ W/m}^2\text{K}$$

$$Nu_{D,2} = 13.48$$

$$h_2 = \frac{Nu_{D,2} k_2}{D} = 80.9 \text{ W/m}^2\text{K}$$

c) **1pt:** 0.25 for the correct boundary condition; 0.25 for  $L = d$  and 0.5 for  $k = k_{Al}$

Each half of the pin behaves as a fin. Convection occurs onto the entire surface so the correct boundary condition is convection at the tip.

$$Q_1 = M_1 \frac{\sinh(m_1 d) + (h_1/m_1 k_{Al}) \cosh(m_1 d)}{\cosh(m_1 d) + (h_1/m_1 k_{Al}) \sinh(m_1 d)}$$

$$Q_2 = M_2 \frac{\sinh(m_2 d) + (h_2/m_2 k_{Al}) \cosh(m_2 d)}{\cosh(m_2 d) + (h_2/m_2 k_{Al}) \sinh(m_2 d)}$$

as  $L_1 = L_2 = L/2 = d = 0.05m$

d) **4pt:** 1 for the heat transfer equality condition (0.5 for equality, 0.5 for sign), 0.25 for P and 0.25 for Ac, 0.5 for re-writing the equality as a function for  $T_b$ , 0.5 for the 2 values of m, 0.5 for the 2 values of B, 1 for the value of  $T_b$

The base of the fin is coincident for the two sides. Also:

$$Q_1 = -Q_2$$

The fin is cylindrical with  $P = \pi D$  and  $A_c = \pi D^2/4$  so:

$$m_i = \sqrt{\frac{h_i P}{k A_c}} = 2 \sqrt{\frac{h_i}{k_{Al} D}}$$

$$M_i = \sqrt{h_i P k A_c} \theta_{b,i} = \sqrt{h_i D k} \frac{\pi D}{2} (T_b - T_{\infty,i})$$

So:

$$\sqrt{h_1 D k} \frac{\pi D}{2} (T_b - T_{\infty,1}) \frac{\sinh(m_1 L_1) + (h_1/m_1 k) \cosh(m_1 L_1)}{\cosh(m_1 L_1) + (h_1/m_1 k) \sinh(m_1 L_1)} =$$

$$-\sqrt{h_2 D k} \frac{\pi D}{2} (T_b - T_{\infty,2}) \frac{\sinh(m_2 L_2) + (h_2/m_2 k) \cosh(m_2 L_2)}{\cosh(m_2 L_2) + (h_2/m_2 k) \sinh(m_2 L_2)}$$

This can be re-written as:

$$\sqrt{h_1} (T_b - T_{\infty,1}) B_1 = -\sqrt{h_2} (T_b - T_{\infty,2}) B_2$$

Solving for  $T_b$  we get:

$$T_b = \frac{\sqrt{h_1} B_1 T_{\infty,1} + \sqrt{h_2} B_2 T_{\infty,2}}{\sqrt{h_1} B_1 + \sqrt{h_2} B_2}$$

Substituting the values of the physical parameters:

$$m_1 = 22.74$$

$$m_2 = 19.16$$

So:  $m_1 d = 1.137$  and  $m_2 d = 0.958$ . Also:  $\sinh(m_1 d) = 1.398$ ,  $\cosh(m_1 d) = 1.719$ ,  $\sinh(m_2 d) = 1.111$  and  $\cosh(m_2 d) = 1.495$ . Finally  $\frac{h_1}{m_1 k_{Al}} = 0.0284$  and  $\frac{h_2}{m_2 k_{Al}} = 0.024$ .

Hence:

$$B_1 = 0.823$$

$$B_2 = 0.753$$

And

$$T_b = 310.5K$$

e) **1pt:** 0.5 for the values of M, 0.5 for the value of Q

We just need to calculate:

$$Q = Q_1 = -Q_2 = \sqrt{h_1 D k} \frac{\pi D}{2} (T_b - T_{\infty,1}) \frac{\sinh(m_1 L_1) + (h_1/m_1 k) \cosh(m_1 L_1)}{\cosh(m_1 L_1) + (h_1/m_1 k) \sinh(m_1 L_1)}$$

Substituting the values of the physical parameters:

$$M_1 = 0.0789(T_b - 280K)$$

$$M_2 = 0.0663(T_b - 350K)$$

Therefore:

$$Q = Q_1 = M_1 B_1 = 1.98W$$

or

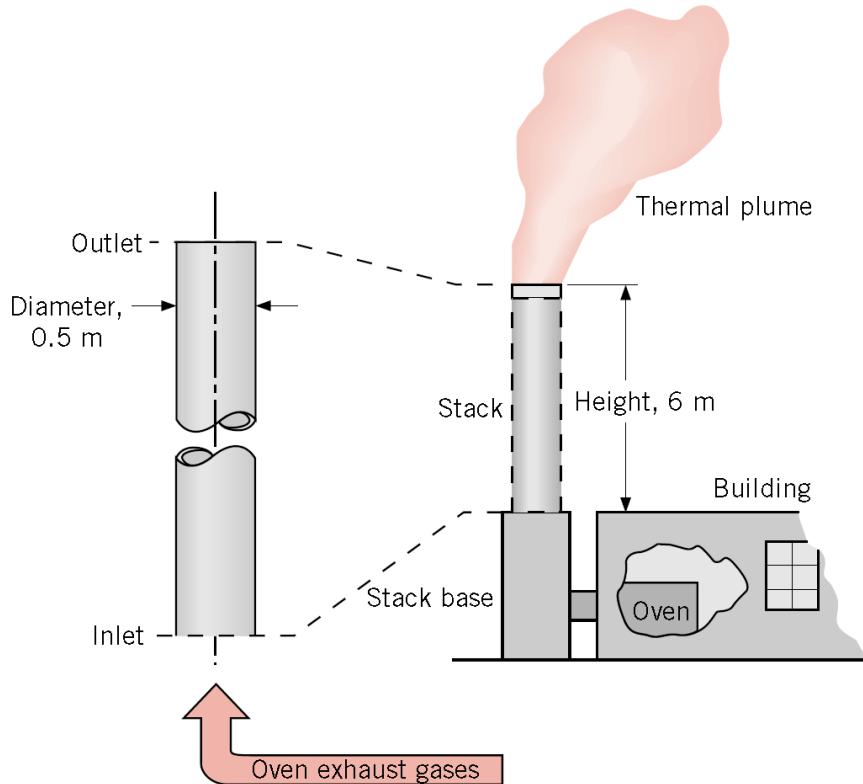
$$Q = -Q_2 = -M_2 B_2 = 1.972W$$

## Exercise 5(Points: 9)

Exhaust gases from a wire processing oven are discharged into a tall stack. Knowledge of the outlet gas temperature  $T_{m,o}$  is useful for predicting the dispersion of effluents in the thermal plume while knowledge of the outlet stack surface temperature  $T_{s,o}$  indicates whether condensation of the gas products will occur. The thin walled cylindrical stack has a diameter  $D = 0.5\text{m}$  and a height  $H = 6\text{m}$ . The exhaust gas flow rate is  $\dot{m} = 0.5\text{kg/s}$  and the inlet gas temperature is  $T_{m,i} = 600\text{C}$ . The environmental conditions outside the stack are characterized by an air temperature of  $T_\infty = 4\text{C}$  and a wind velocity of  $v = 5\text{m/s}$ .

Assuming that the exhaust gas has the same thermophysical properties of air and assuming that the wall of the stack has a negligible thermal resistance:

- Using an average temperature of  $T_{m,g} = 550\text{C}$ , list the values of specific heat, viscosity, thermal conductivity and Prandtl number for the exhaust gases.
- Assuming a reference surface temperature of the stack of  $T_{ref,s} = 250\text{C}$ , calculate the reference temperature for the air boundary layer on the outside of the stack and list the values of density, specific heat, viscosity, thermal conductivity and Prandtl number.
- Calculate the inner and outer convection coefficients,  $h_i$  and  $h_o$ . Write clearly the motivation for your choice of a specific correlation.
- Calculate the average gas outlet temperature,  $T_{m,o}$
- Calculate the outlet stack surface temperature,  $T_{s,o}$
- Comment on how adequate are the reference temperatures we used to estimate the thermophysical properties.



## Solution

a) **1pt:** 0.25 for every value

From table A1, at  $T_{m,g} = 823K$  (interpolation):

$$c_{p,g} = 1.104 \text{ kJ/kgK} = 1104 \text{ J/kgK}$$

$$\mu_g = 376.4 \cdot 10^{-7} \text{ Ns/m}^2$$

$$k_g = 0.0584 \text{ W/mK}$$

$$Pr_g = 0.712$$

b) **0.5pt:** 0.25 for the correct reference temperature; 0.25 for the values

The boundary layer reference temperature is:

$$T_f = (T_\infty + T_{s,o})/2 = 400K$$

From table A4 we obtain:

$$\rho_f = 0.8711 \text{ kg/m}^3$$

$$c_{p,f} = 1.014 \text{ kJ/kgK}$$

$$\mu_f = 2.3 \cdot 10^{-5} \text{ Ns/m}^2$$

$$k_f = 0.0338 \text{ W/mK}$$

$$Pr_f = 0.690$$

c) **3pt:** 0.25 for type of convection; 0.25 for converting Re as a function of mass flow rate; 0.25 for value of Re; 0.25 for recognizing the turbulent flow choosing the right correlation; 0.25 for the choice of the right exponent; 0.25 for the value of  $Nu_i$ ; 0.25 for the value of  $h_i$ . 0.25 for type of convection; 0.25 for the choice of the correlation; 0.25 for the value of Re; 0.25 for the value of  $Nu_o$ ; 0.25 for the value of  $h_o$ .

*Internal Flow.* Forced internal convection  $\rightarrow$  calculate Re

$$Re_{D,i} = \frac{\rho_g v D}{\mu_g} = \frac{4\dot{m}}{\pi D \mu_g}$$

$$Re_{D,i} = \frac{4 \cdot 0.5}{\pi \cdot 0.5 \cdot 376.4 \cdot 10^{-7}} = 33827 >> 2300$$

The flow is turbulent and  $Re_{D,i} > 10000$ :

$$Nu_i = 0.023 Re_{D,i}^{4/5} Pr_g^n$$

The exhaust gas is cooling:

$$n = 0.3$$

$$Nu_i = \frac{h_i D}{k_g} = 87.26$$

$$h_i = \frac{k}{D} 0.023 Re_{D,i}^{4/5} Pr_g^{0.3} = \frac{58.4 \cdot 10^{-3}}{0.5} 0.023 (33827)^{4/5} (0.712)^{0.3} = 10.2 \text{ W/m}^2 \text{ K}$$

*External Flow.* Forced external convection. Flow around a cylinder.

$$Nu_{D,o} = 0.3 + \frac{0.62 Re_{D,o}^{1/2} Pr^{1/3}}{[1 + (0.4/Pr_f)^{2/3}]^{1/4}} \left[ 1 + \left( \frac{Re_o}{282000} \right)^{5/8} \right]^{4/5}$$

where

$$Re_{D,o} = \frac{\rho v D}{\mu} = \frac{5 \cdot 0.5}{26.41 \cdot 10^{-6}} = 94660$$

$$Nu_{D,o} = 205$$

$$h_o = \frac{Nu_{D,o} k_f}{D} = \frac{0.0338205}{0.5} = 13.9 W/m^2 K$$

d) **2pt:** 0.5 for choosing the right equation; 0.25 for the right expression of the external area; 1 for the right expression of U (0.25 for each convection term, 0.25 for neglecting the conduction, 0.25 for the U value or UA); 0.25 for the value for  $T_{m,o}$ .

Internal convection in a cylindrical pipe with heat removed by external convection:

$$\frac{T_\infty - T_{m,o}}{T_\infty - T_{m,i}} = \exp \left( -\frac{UA}{\dot{m}c_{p,g}} \right)$$

where

$$A = PH = \pi DH$$

Negligible conduction at the wall. The overall heat transfer coefficient:

$$R_{tot} = \frac{1}{UA} = \frac{1}{Ah_i} + \frac{1}{Ah_o}$$

$$UA = 55.33 W/K$$

or

$$U = \frac{1}{\frac{1}{h_i} + \frac{1}{h_o}} = 5.88$$

$$T_{m,o} = T_\infty - (T_\infty - T_{m,i}) \exp \left( -\frac{UA}{\dot{m}c_{p,g}} \right) = 4 - (4 - 600) \exp \left( -\frac{5.88 \cdot \pi 0.5 \cdot 6}{0.5 \cdot 1104} \right) = 543C = 816K$$

e) **1.5:** 1.25 for the expression of heat transfer from the gas to the air at the outlet section (0.5 for each side of the equation and 0.25 for the equality); 0.25 for the value of the outlet temperature

At the outlet section:

$$\ddot{q}_o = h_i(T_{m,o} - T_{s,o}) = h_o(T_{s,o} - T_\infty)$$

$$T_{s,o} = \frac{h_i T_{m,o} + h_o T_\infty}{h_i + h_o} = \frac{10.2543 + 13.94}{10.2 + 13.9} = 232C = 505K$$

f) **1pt**

The temperatures used to estimate the fluid properties were adequate ( $T_{m,g} = (600 + 543)/2 = 571.5C \approx 550C$  and  $T_{s,o} = 232C \approx T_{ref,s} = 250C$ )