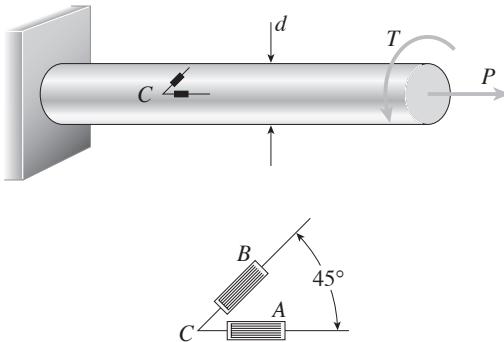


**Exercise 1**Figure 1: Circular bar and strain gauges  $A$  and  $B$ 

A solid circular bar with a diameter of  $d = 32$  mm is subjected to an axial force  $P$  and a torque  $T$  (see Figure 1). Strain gauges  $A$  and  $B$  mounted on the surface of the bar give readings  $\varepsilon_A = 140 \times 10^{-6}$  and  $\varepsilon_B = -60 \times 10^{-6}$ . The bar is made of steel having  $E = 210$  GPa and  $\nu = 0.29$ .

- Determine the axial force  $P$  and the torque  $T$ .
- Determine the maximum shear strain  $\gamma_{max}$  and the maximum shear stress  $\tau_{max}$  in the bar.

## Exercise 2

**Reminder about non overconstrained systems :** There is no need to use the displacement stiffness method when the system is not overconstrained.

We consider a cylindrical beam made out of two materials as depicted Fig.3a. Its radius is  $r$ , young modulus are  $E_1, E_2$  and Poisson ratio are  $\nu_1, \nu_2$ .

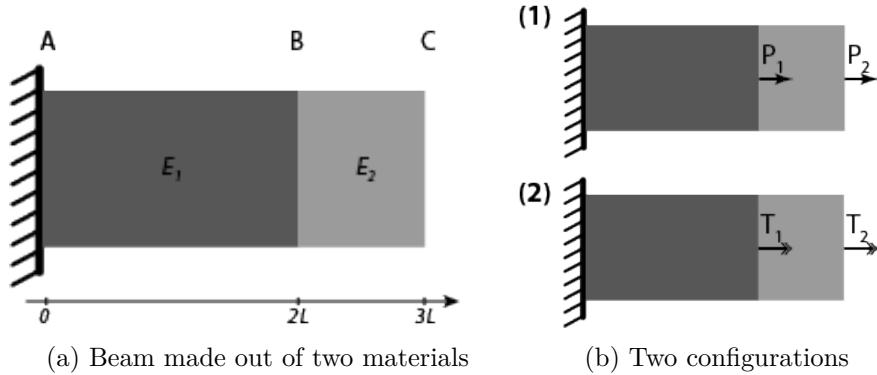


Figure 2

a) For the configuration 1 in Fig.3a (forces),

- What is the internal force in the beam ?
- What is and where is the maximum stress ?
- What is the displacement of points A, B and C ?

b) For the configuration 2 in Fig.3b (torques),

- What is the internal torque in the beam ?
- What is and where is the maximum shear stress ?
- What is the angle of points A, B and C ?