

DISPERSIVE PDE 23, PROBLEM SET 7

- (1) Carefully prove that if $(f, g) \in H^s(\mathbb{R}^n) \times H^{s-1}(\mathbb{R}^n)$, $s \geq 1$, and ψ is given by the formal wave propagator in Prop. 1.3 of lecture 4.pdf, then in fact

$$\psi \in C^1(\mathbb{R}, H^{s-1}(\mathbb{R}^n)),$$

by showing that the expression obtained by formally time differentiating the wave propagator is the time derivative of ψ in the sense of Definition 1.2 of lecture 4.pdf.

- (2) Complete the proof of Proposition 1.5 by showing the assertion for the linear wave equation.
- (3) Give the proof of Proposition 2.4 in lecture 4.pdf.