

Discrete choice and machine learning

Two complementary methodologies

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Mathematical Modeling of Behavior



Discrete choice and machine learning

Motivation

- ▶ The success stories obtained by machine learning methods in many disciplines have motivated several researchers to apply them on choice data.
- ▶ In this lecture, we discuss the differences between the two approaches. We also identify a couple of pitfalls that have to be avoided.

Machine learning

Supervised learning / classification

- ▶ Population partitioned into J classes.
- ▶ Training set: features + true class.
- ▶ Classifier: given the features, predicts the class.
- ▶ Types: logistic regression, support vector machine, decision trees, neural networks, etc.

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Discrete choice

- ▶ Choice set with J alternatives.
- ▶ Training set: explanatory variables + choice.
- ▶ Choice model: given the variables, predicts the choice.
- ▶ Types: logit, nested logit, mixtures, etc.

Advantages of machine learning

Model specification

- ▶ DC: hand-crafted, simple (linear utility, few interactions).
- ▶ ML: complex functional form, data driven.

Model development

- ▶ DC: incremental, trial-and-errors.
- ▶ ML: systematic.

Model selection

- ▶ DC: statistical theory.
- ▶ ML: out-of-sample validation.

Pitfalls of machine learning for choice data

Probability that an item n belongs to a class i

Choice models

Probability is used in applications.

Discrete classification

- ▶ Typically, class with highest probability is selected.
- ▶ “Optimal decision rule”

Severe aggregation bias

Example: classify 1000 items in two classes.

Simple data generation process

51% class 1 / 49% class 2

Perfect ML model

After projection: always predicts class 1

Total number of items in class 1

- ▶ In reality: 510
- ▶ Predicted: 1000
- ▶ Even if the model is acceptable at a disaggregate level, it suffers from a strong aggregation bias.

Aggregation bias increases with the number of classes

Example: classify N items in K classes.

Data generation process

$\frac{1+\varepsilon}{K}$ class 1 / $\frac{K-1-\varepsilon}{K(K-1)}$ class i

Perfect ML model

After projection: always predicts class 1

Total number of items in class 1

- ▶ In reality: $N \frac{1+\varepsilon}{K}$
- ▶ Predicted: N
- ▶ The problem increases with the number of classes.

Machine learning for choice data

Probabilistic classification methods

- ▶ Bayes classifiers,
- ▶ logistic regression,
- ▶ multi-layer perceptrons,
- ▶ etc.

Recommendation

Use the probabilistic output for aggregation. Do not project on 0/1.

Panel data

Out-of-sample validation

- ▶ Data randomly split between training and validation set.
- ▶ Validation set: not seen during estimation.
- ▶ If the data is panel, selection must be based on individuals n and not on observations nt .
- ▶ If split on observations, strong correlation between validation set and training set.
- ▶ Superiority of ML over DC in prediction has been amplified in the literature based on this mistake.

[Hillel et al., 2021], [Hillel, 2020]

Discrete choice

Important aspects to keep in mind

- ▶ Extrapolation.
- ▶ Policy analysis.
- ▶ Sampling.
- ▶ Interpretability.

Notations

Variables

- ▶ Explanatory: x
- ▶ Choice: i

Models

- ▶ Data generating process: $p(i, x)$.
- ▶ Discrete choice: theory: $P(i|x; \theta)$
- ▶ Machine learning: data-driven:

$$Q(i|x) \approx \frac{p(i, x)}{p(x)}$$

Extrapolation

Objective

Predict i for values of x outside the training data.

Machine learning

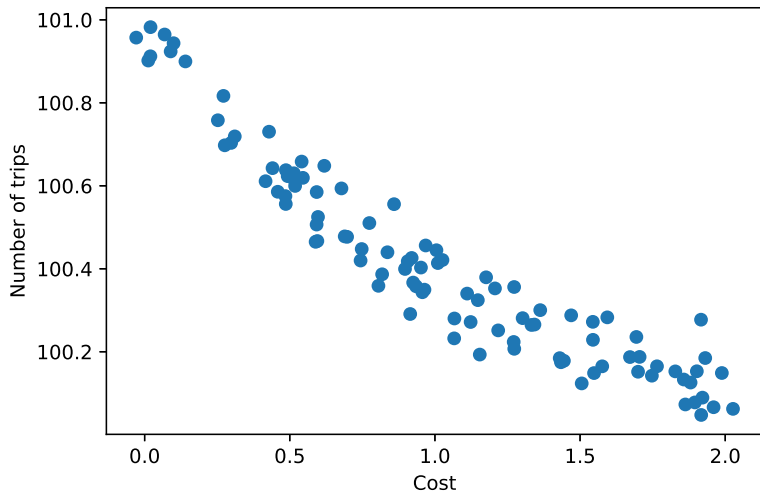
- ▶ Focus on goodness of fit.
- ▶ Usually good for interpolation.
- ▶ May be poor in extrapolation.

Illustration

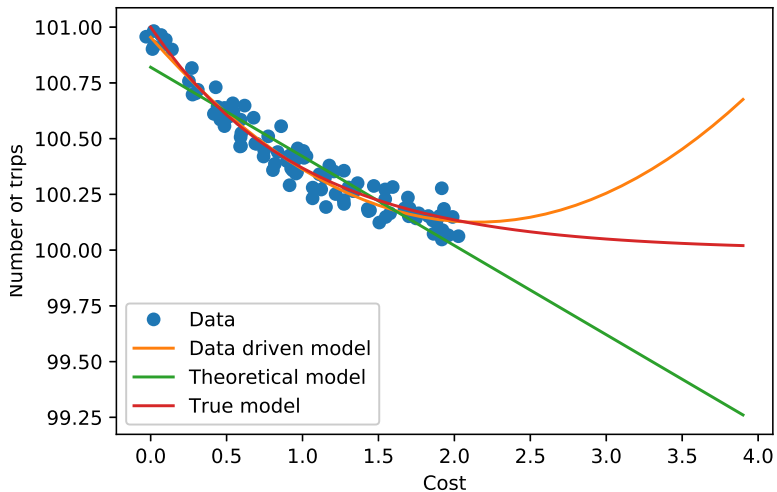
Setup

- ▶ Regression (for the sake of illustration).
- ▶ For a detailed discrete choice example, see the video [Survival of the fittest... or not](https://youtu.be/_w7RxZIUBqI) [youtu.be/_w7RxZIUBqI]
- ▶ Predict number of trips vs. cost of public transportation.
- ▶ Data generation process: $t = 100 + \exp(-c)$.
- ▶ Theoretical model: $t = \theta_1 + \theta_2 c$.
- ▶ Theoretical argument: t decreases when c increases: $\theta_2 < 0$.

Data



Models



Extrapolation

H. Varian, Berkeley — Chief Economist at Google

Naive empiricism can only predict what has happened in the past. It is the theory — the underlying model — that allows us to extrapolate.

[Varian, 1993]

What-if analysis

Policy analysis

- ▶ Impact of new taxes, subsidies.
- ▶ Impact of investments that improve the level of service or quality.
- ▶ Impact of restrictions, constraints.
- ▶ Impact of modifications of the choice set.

What-if analysis

Discrete choice

- ▶ Model: $P(i|x; \theta)$.
- ▶ Assumption: causal effect is behavioral, and stable over time.
- ▶ x can be manipulated at will, within the scope of validity of the model.

Machine learning

- ▶ Model: $p(i, x)/p(x)$
- ▶ Assumption: captures the correlation in the data.
- ▶ Used to predict with x drawn from $p(x)$.
- ▶ Does not work if $p(x)$ is modified.

Representativity of the sample

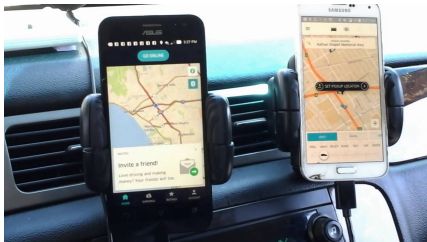
Machine Learning: data processing

- ▶ Data is the universe.
- ▶ Representativity is assumed.
- ▶ Main argument: the size of the data set is very large.
- ▶ In general, the research question is posterior to the data collection.

Discrete choice: inference

- ▶ A population is identified.
- ▶ A research question is proposed.
- ▶ Data collection strategies are designed.
- ▶ Potential sampling biases are corrected.

Potential implications



Classification

- ▶ Bias of the parameters.
- ▶ Not necessarily an issue for interpolation.
- ▶ May amplify the extrapolation problem.

Aggregation

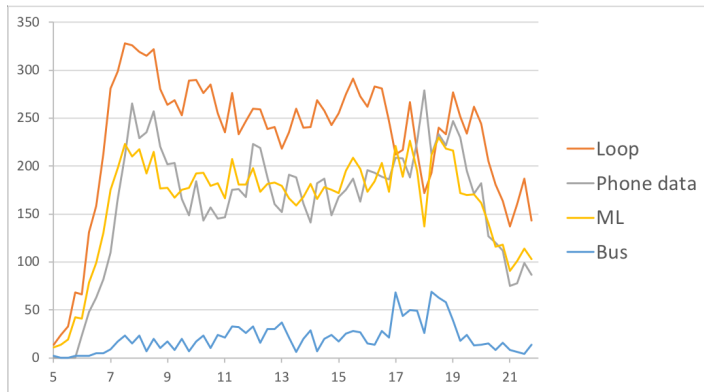
- ▶ Counting.
- ▶ Aggregation biases may be severe.

Example

City of Geneva

- ▶ Data for March 2, 2017.
- ▶ Phone data: boundary flows, between adjacent zones.
- ▶ ML: results of the ML learning algorithm of the phone company.
- ▶ Compared with loop detectors: flows of cars

Results



Source: Montesinos Ferrer, Lamotte, Geroliminis

Interpretation

Beyond prediction

- ▶ Models are used to derive quantitative indicators.
- ▶ Examples: willingness to pay, social welfare, elasticities, etc.
- ▶ Requires a theory, a structure.

Sanity check

- ▶ Comparison with published results.
- ▶ Communication with practitioners (trust).
- ▶ Open the box.

Indicators with ML models

Elasticities

- ▶ Point elasticity: OK $\partial Q(i|x)/\partial x_k \cdot x_k / Q(i|x)$.
- ▶ Arc elasticity: same issue as “what-if analysis”.

Willingness-to-pay and social welfare

- ▶ Concepts based on utility theory.
- ▶ Requires a combination of ML and utility theory [Sifringer et al., 2018]

Summary

	Discrete choice	Machine Learning
Driven by	theory	data
Captures	causality	correlation
Focus on	interpretability	accuracy
Model:	choice model	classifier
Model selection:	hypothesis testing	out-of-sample validation
Main usage:	what-if analysis	interpolation

Research trends

ML for choice data

- ▶ [Brathwaite et al., 2017]
- ▶ [Wong et al., 2018]
- ▶ [Semenova, 2018]
- ▶ [Lee et al., 2018]
- ▶ [Hillel et al., 2021]




Using ML strengths in discrete choice

- ▶ [Sifringer et al., 2018]
- ▶ [Lederrey et al., 2021]



Assistance to specification

- ▶ [Hillel et al., 2019]
- ▶ [Aboutaleb, 2019]
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