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- $\check{\pi}$  the automorphism on  $\mathbb{P}$ -names induced by some permutation (for **ZFA**), page 364
- axiom of Atoms** the axiom of atoms (for **ZFA**), page 361
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- $\mathbf{M}^\mathbb{P}$    the class of all  $\mathbb{P}$ -names of  $\mathbf{M}$ , page 238
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**ZFA** set theory with atoms, page 361

**ZFC** Zermelo-Fraenkel set theory with axiom of choice, page 13

$\mathcal{Z}^{\text{HS}_\kappa}$  the permutation model induced by  $\mathcal{Z}$  and  $\mathcal{F}_\Delta$ , page 387