

Ex. 10.1
a)

	Sum of Squares	DF	Mean Square	F	Sig	R-Square
Regression	813.3	$k=5$	$813.3/5=162.66$	$162.66/49$	0.0103^*	$813.3/3753.3$
Residual	2940.0	$65-5=60$	$2940/60=49$	$= 3.3196$		$= 0.2167$
Total	3753.3	$N-1=65$				Root MSE $\sqrt{49}=7$

Variable	Parameter Estimate	Standard Error	t	Sig
Intercept	70.0000		$0.1000/6.0450=2.22$	0.03^*
x1	0.1000	0.0450	-2	0.050033^*
x2	-0.1500	0.0750	0.5	0.619
x3	0.1000	0.2000	-0.5	0.426
x4	-0.0400	0.0500	2.4	0.0195^*
x5	0.1200	0.0500		

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Example 5.1

Step-by-step explanation

a. SS model = SS total - SS residual

$$\text{SS model} = 3753.3 - 2940$$

$$\text{SS model} = 813.3$$

df model = number of dependent variables = $k = 5$

$$\text{df residual} = N - k - 1 = 66 - 5 - 1 = 60$$

$$\text{df total} = N - 1 = 66 - 1 = 65$$

$$\text{MS model} = \text{SS model} / \text{df model} = 813.3 / 5 = 162.66$$

$$\text{MS residual} = \text{SS residual} / \text{df residual}$$

$$\text{MS residual} = 2940 / 60 = 49$$

Number of obs = 5

$$F = \text{MS model} / \text{MS residual}$$

$$F = 162.66 / 49 = 3.3196$$

$$\text{Prob} > F = 0.0103$$

$$R^2 = \text{SS model} / \text{SS total}$$

$$R^2 = 813.3 / 3753.3$$

$$\text{Prob} > F = 0.0103$$

$$R^2 = \text{SS model} / \text{SS total}$$

$$R^2 = 813.3 / 3753.3$$

$$R^2 = 0.2167$$

$$\text{Root MSE} = \sqrt{49} = 7$$

b. equation from the coefficients is

$$Y = 70 + 0.1X_1 - 0.15X_2 + 0.1X_3 - 0.04X_4 - 0.12X_5$$

Interpretation of X_1 : A 1% increase of adult residents owning homes with all other variables held constant results to an increase of 0.10% in adult residents who are registered to vote.

c. Since only p values of X_1 , X_2 , and X_5 are less than 0.05 alpha level, only these variables are significant in explaining Y

d. C.I. interval is expressed as

$$\text{C.I.} = X_1 \text{ coefficient} \pm t_{\text{crit}} \cdot \text{se}$$

t_{crit} at 0.05 alpha level and $df = 60$ is equal to 2

$$\text{C.I.} = 0.1 \pm 2 \cdot 0.045$$

$$\text{C.I.} = (0.01, 0.19)$$

e. CI: $(50 \times 0.01, 50 \times 0.19) \rightarrow (0.05, 9.5)$

d. For the global test of

$$H_0: \beta_1 = \dots = \beta_5 = 0$$

vs. A : At least 1 $\beta_i \neq 0, i=1, \dots, 5$

Since, $p_{\text{obs}} < 0.05 \Rightarrow \text{Reject } H_0$

e. For the test of $H_0: \beta_1 = 0$ vs. $A: \beta_1 \neq 0$
 $p_{\text{obs}} < 0.05 \Rightarrow \text{Reject } H_0$

Ex. 10.2

Source	df	SS	MS	F
Treatments	4-1	1520.88	506.96	16.848
Residuals	36-4	962.86	30.09	
Total	36-1	2483.74		

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> anova(lm(strength ~ mortar.type))
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Analysis of Variance Table

Response: strength

	Df	Sum Sq	Mean Sq	F value	Pr(>F)
mortar.type	3	1520.88	506.96	16.848	9.576e-07 ***
Residuals	32	962.86	30.09		

$$MS(UM)_{Treatments}: 506.96 = SS(SC) / df \approx SS(SC) \\ = 506.96 \times 3 = 1520.88$$

$$SS(SC)_{Residual} = SST - SS_{Treatments} = 2483.74 - 1520.88 \\ = 962.86$$

$$MS(UM)_{Residual} = SS / df = 962.86 / 32 = 30.09$$

$$F_{obs} = MS(UM)_{Treatments} / MS(UM)_{Residuals} = 506.96 / 30.09 \\ = 16.848$$

$$p_{obs} \approx 9.6 \times 10^{-7}$$