

Environmental Economics

Prof. Philippe Thalmann

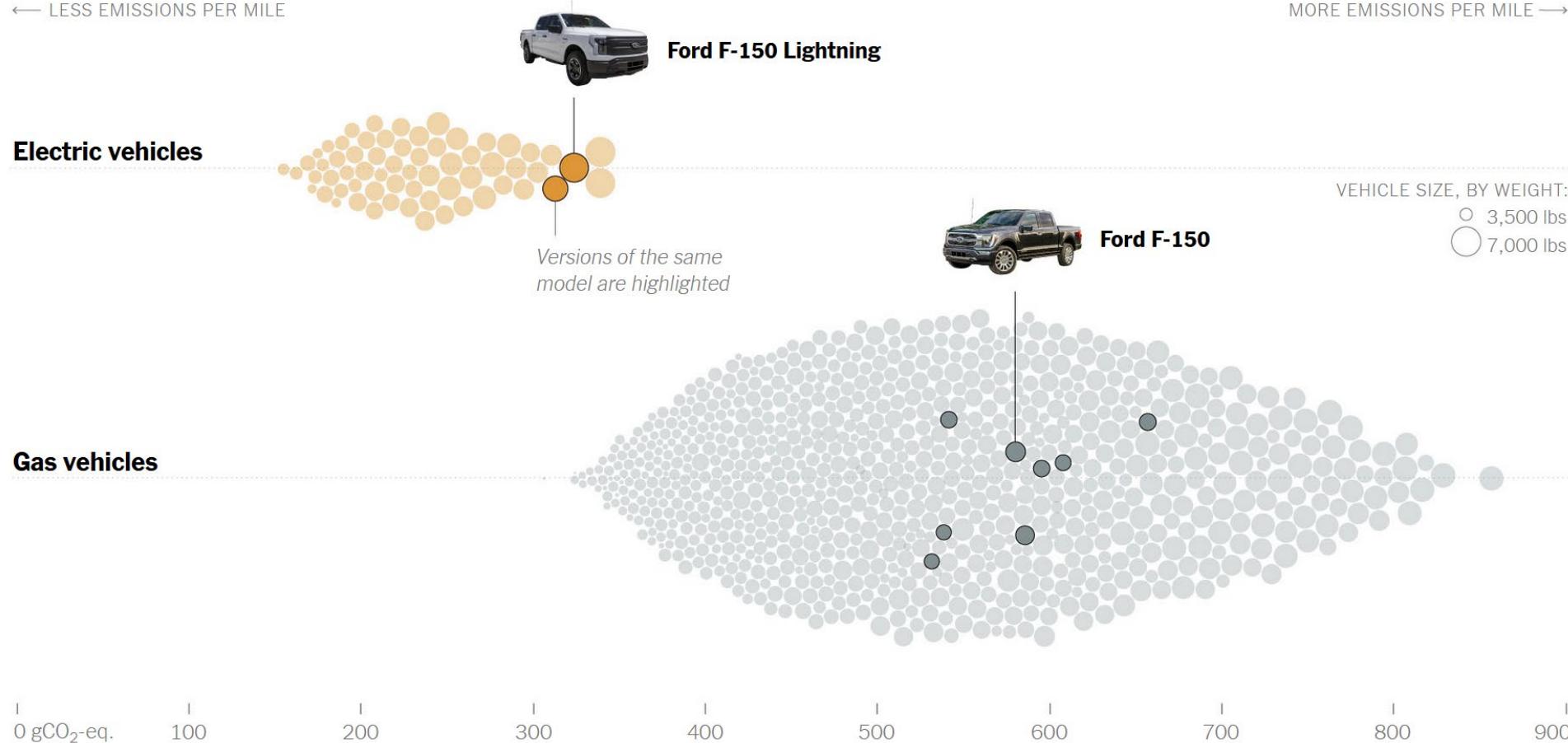
EPFL ENAC LEUrE

ENV-471

Master semester 2 or 4

COMPARING OPTIONS THAT INVOLVE INTERTEMPORAL PAYMENTS

EV vs ICE comparison on cradle-to-grave greenhouse gas emissions



Only the heaviest electric SUVs and pickups are 'worse' than the lightest ICE ('gas') cars

New York Times, "Just How Good for the Planet Is That Big Electric Pickup Truck?", 18 Feb. 2023

Source of data: carboncounter.com by the MIT Trancik Lab. Greenhouse gas emissions account for the entire life cycle of the vehicle, including vehicle and battery manufacturing, supply chain of raw materials, gas consumption, and electricity generation. Emissions from electricity generation reflect the average values from grids across the U.S.

Comparing the costs of a BE and an ICE car*



Cost factors	Hyundai IONIQ Elektro Trend	Hyundai i30 1.4 T-GDI Trend
One-off costs		
Purchase price	33 300 €	24 550 €
Charging infrastructure	1 100 €	0 €
Subsidy / purchase premium	4 000 €	0 €
Recurring costs (per year)		
Energy costs	662 €	1 170 €
Car ownership tax	0 €	98 €
Insurance	969 €	1 260 €
Maintenance / servicing	552 €	744 €
Residual value		
Resale price after 5 years	7 100 €	6 070 €

What is the total cost of ownership (TCO) of each car?

*

BE = battery electric

ICE = internal combustion engine

Method 1: sum of costs

Cost factors	Hyundai IONIQ Elektro Trend	Hyundai i30 1.4 T-GDI Trend
One-off costs		
Purchase price	33 300 €	24 550 €
Charging infrastructure	1 100 €	0 €
Subsidy / purchase premium	4 000 €	0 €
Recurring costs (per year)		
Energy costs	662 €	1 170 €
Car ownership tax	0 €	98 €
Insurance	969 €	1 260 €
Maintenance / servicing	552 €	744 €
Residual value		
Resale price after 5 years	7 100 €	6 070 €
Net acquisition cost	30 400 €	24 550 €
5 years of annual costs	10 915 €	16 360 €
Residual value	-7 100 €	-6 070 €
Total costs	34 215 €	34 840 €

Discuss:

- Need for public support: why? how much?
- Form of public support: what support is provided? alternative forms? advantages and drawbacks?
- No discounting

Method 2: present value of costs

Cost factors	Hyundai IONIQ Elektro Trend	Hyundai i30 1.4 T-GDI Trend
One-off costs		
Purchase price	33 300 €	24 550 €
Charging infrastructure	1 100 €	0 €
Subsidy / purchase premium	4 000 €	0 €
Recurring costs (per year)		
Energy costs	662 €	1 170 €
Car ownership tax	0 €	98 €
Insurance	969 €	1 260 €
Maintenance / servicing	552 €	744 €
Residual value		
Resale price after 5 years	7 100 €	6 070 €

Discount factor = $(1+i)^{-\text{Discount years}}$

			Discount rate:	4.0%	Discounted costs	
	Hyundai IONIQ Elektro Trend	Hyundai i30 1.4 T-GDI Trend	Discount years	Discount factor	Hyundai IONIQ Elektro Trend	Hyundai i30 1.4 T-GDI Trend
Start year 1	30 400 €	24 550 €	0	1.00	30 400 €	24 550 €
Costs year 1	2 183 €	3 272 €	0.5	0.98	2 141 €	3 208 €
Costs year 2	2 183 €	3 272 €	1.5	0.94	2 058 €	3 085 €
Costs year 3	2 183 €	3 272 €	2.5	0.91	1 979 €	2 966 €
Costs year 4	2 183 €	3 272 €	3.5	0.87	1 903 €	2 852 €
Costs year 5	2 183 €	3 272 €	4.5	0.84	1 830 €	2 743 €
End year 5	-7 100 €	-6 070 €	5	0.82	-5 836 €	-4 989 €
Total costs at start of year 1				34 475 €	34 416 €	

Sensitivity analysis

- Given the uncertainty relative to some key parameters, it is desirable to test the robustness of the main results (here, the ranking of the alternatives) to changes in these key parameters
- Here we test the sensitivity to the discount rate and the resale price premium of the BE car

	Hyundai IONIQ Elektro Trend	Hyundai i30 1.4 T-GDI Trend
Discount rate = 0%	34 215 €	34 840 €
Discount rate = 4%	34 475 €	34 416 €
Discount rate = 8%	34 626 €	33 996 €
Resale price premium = 515	34 898 €	34 416 €
Resale price premium = 1030	34 475 €	34 416 €
Resale price premium = 2060	33 629 €	34 416 €

- A higher discount rate makes the BE car relatively more expensive, because the later cost savings and resale price premium are less valuable
- A somewhat higher resale price premium would make the BE car cheaper than the ICE car

Method 3: average annual cost

- The one-off costs and resale price are divided by the number of years of operation (5 years)
- Beware of the signs!

	Hyundai IONIQ Elektro Trend	Hyundai i30 1.4 T-GDI Trend
One-off costs		
Purchase price	6 660 €	4 910 €
Charging infrastructure	220 €	0 €
Subsidy / purchase premium	- 800 €	0 €
Recurring costs (per year)		
Energy costs	662 €	1 170 €
Car ownership tax	0 €	98 €
Insurance	969 €	1 260 €
Maintenance / servicing	552 €	744 €
Residual value		
Resale price after 5 years	-1 420 €	-1 214 €
Total yearly costs	6 843 €	6 968 €

'Total yearly costs' is equal to the simple sum of costs divided by the number of years of operation

Method 4: average annual costs with discounting

- The challenge is to convert a one-off cost into a stream of constant annual costs whose present value is equal
- In finance, this is known as an 'annuity' calculation
- This is the general formula:

$$PV(A; i; n) = \sum_{t=1}^n \frac{A}{(1+i)^t} = \frac{A}{i} \times \frac{(1+i)^n - 1}{(1+i)^n} = C$$

$$A = C \times \frac{i \times (1+i)^n}{(1+i)^n - 1}$$

- The fraction multiplying C is called the **capital recovery factor** (CRF)
- One-off costs or revenues that occur after 'date 0' must first be discounted to 'date 0'
- E.g., for the resale price P_n in year n: $A = \frac{P_n}{(1+i)^n} \times \frac{i \times (1+i)^n}{(1+i)^n - 1} = P_n \times \frac{i}{(1+i)^n - 1}$

Method 4: average annual costs with discounting

	Hyundai IONIQ Elektro Trend	Hyundai i30 1.4 T-GDI Trend
Net acquisition cost	30 400 €	24 550 €
Annuity of acquisition cost	6 829 €	5 515 €
Resale price after 5 years	7 100 €	6 070 €
PV of resale price	5 836 €	4 989 €
Annuity of resale price	1 311 €	1 121 €

	Hyundai IONIQ Elektro Trend	Hyundai i30 1.4 T-GDI Trend
One-off costs		
Annuity of acquisition cost	6 829 €	5 515 €
Recurring costs (per year)		
Energy costs	662 €	1 170 €
Car ownership tax	0 €	98 €
Insurance	969 €	1 260 €
Maintenance / servicing	552 €	744 €
Residual value		
Annuity of resale price	-1 311 €	-1 121 €
Total yearly costs	7 701 €	7 666 €

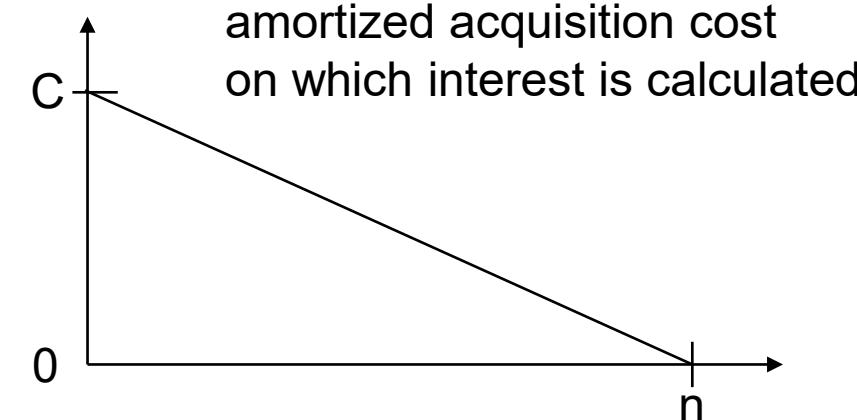
The annuity of 6 829 € compares with acquisition cost / 5 = 6 080 €

The annuity of 1 311 € compares with resale price / 5 = 1 420 €

With discounting, the annual costs are higher, because there is an interest cost counted in the acquisition cost

Method 5: simplified calculation of interest cost

- The annuity is made of two components: (1) 'amortization' of the initial investment and (2) interest on outstanding (= not yet amortized) investment
- $\text{Amortization} = C/n$
- Interest is due on the surface of the triangle below = $C \times n/2 \rightarrow C \times i/2$ per year



- Simplified annuity = $C/n + C \times i/2$
- For the acquisition cost of the BE car, simplified annuity = 6 688 €, to be compared with exact annuity = 6 829 € and with $C/5 = 6 080$ €

Method 5: average annual costs with simplified annuity calculation

	Hyundai IONIQ Elektro Trend	Hyundai i30 1.4 T- GDI Trend
One-off costs		
Simplified annuity of acquisition cost minus resale price	5 126 €	744 €
Recurring costs (per year)		
Energy costs	662 €	1 170 €
Car ownership tax	0 €	98 €
Insurance	969 €	1 260 €
Maintenance / servicing	552 €	744 €
Total yearly costs	7 309 €	4 016 €

'C' in the simplified annuity calculation $C/n + C \times i/2$ is net acquisition cost minus resale price: this is the amount to be amortized and interest paid on

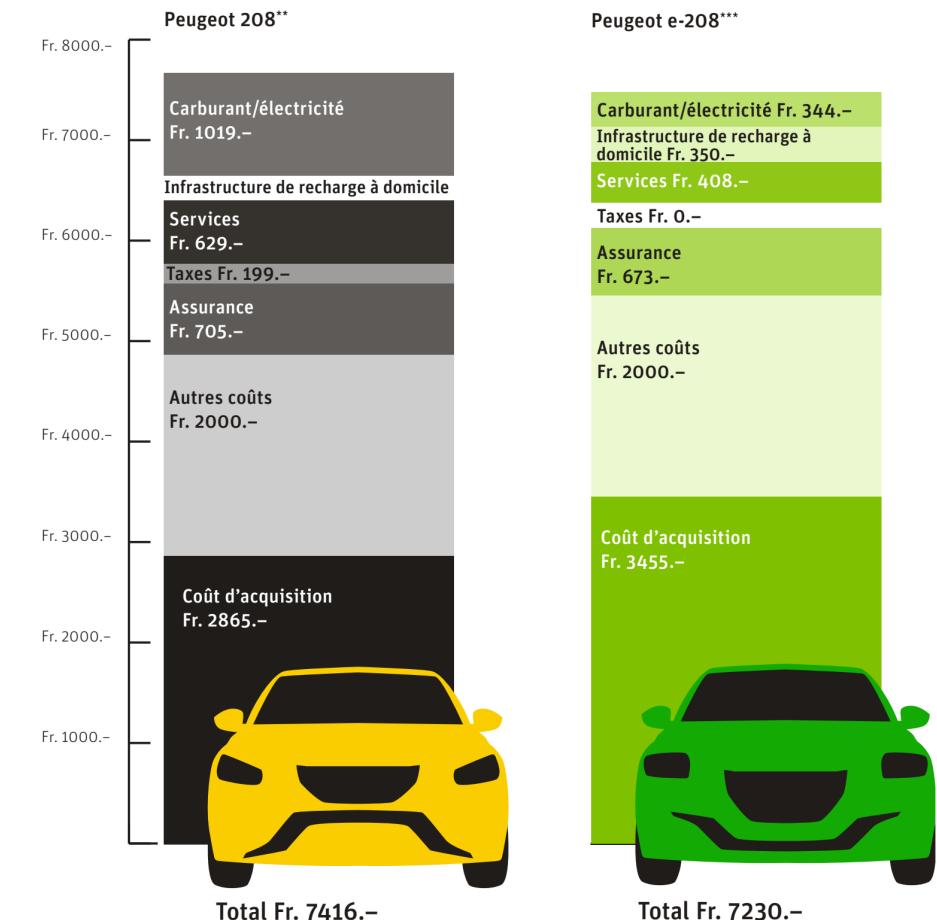
- For the BE car, TCO with simplified annuity calculation = 7 309 €, to be compared with TCO with exact annuity = 7 701 € and with TCO based on simple average = 6 843 €

Cost comparisons in practice

Sum of costs (undiscounted)

Cost factors	Hyundai IONIQ Elektro Trend	Hyundai i30 1.4 T-GDI Trend DCT
One-off costs		
Purchase price	33.300 €	24.550 €
Charging infrastructure	1.100 €	0 €
Subsidy / purchase premium	-9.000 €	0 €
Recurring costs (per year)		
Consumption costs	662 €	1.170 €
Car tax	0 €	98 €
Insurance	969 €	1.260 €
Maintenance / servicing	552 €	744 €
Residual value	7.100 €	6.070 €
Total costs	34.213 €	34.840 €

Mean annual costs (undiscounted)



The Mobility House, copied on 8.5.23, subsidy mistaken,
https://www.mobilityhouse.com/int_en/knowledge-center/cost-comparison-electric-car-vs-petrol-which-car-costs-more-annually

Magazine ATE 2/2022

INVESTMENT DECISION

Investing into the costlier option

- Buying the more expensive BE car rather than the ICE can be interpreted as an investment, with returns in the form of lower running costs and a higher residual value

	Hyundai IONIQ Elektro Trend	Hyundai i30 1.4 T-GDI Trend	ICE - BE
Net acquisition cost	30 400 €	24 550 €	-5 850 €
Running costs year 1	2 183 €	3 272 €	1 089 €
Running costs year 2	2 183 €	3 272 €	1 089 €
Running costs year 3	2 183 €	3 272 €	1 089 €
Running costs year 4	2 183 €	3 272 €	1 089 €
Running costs year 5	2 183 €	3 272 €	1 089 €
Residual value	-7 100 €	-6 070 €	1 030 €

- Is this a profitable investment?

Net value and net present value (NPV)

- The investment is profitable if incomes (here: cost savings and resale premium) exceed the investment
- Proper calculation discounts all payments to the same date
- Investing into BE is not profitable with 4% discount rate

	ICE - BE
Net acquisition cost	-5 850 €
Running costs year 1	1 089 €
Running costs year 2	1 089 €
Running costs year 3	1 089 €
Running costs year 4	1 089 €
Running costs year 5	1 089 €
Residual value	1 030 €
Net value (no discounting)	625 €

	ICE - BE	Discount rate: 4.0%	Present value
	ICE - BE	Discount years	Discount factor
Net acquisition cost	-5 850 €	0	1.00
Running costs year 1	1 089 €	0.5	0.98
Running costs year 2	1 089 €	1.5	0.94
Running costs year 3	1 089 €	2.5	0.91
Running costs year 4	1 089 €	3.5	0.87
Running costs year 5	1 089 €	4.5	0.84
Residual value	1 030 €	5	0.82
NET PRESENT VALUE			- 59 €

Net Present Value (NPV)

- Definition
 - The NPV is the sum of discounted payments (incomes or benefits minus costs and other outlays) over the period

$$NPV = (B - C)_0 + \frac{(B - C)_1}{(1 + i)^1} + \frac{(B - C)_2}{(1 + i)^2} + \dots + \frac{(B - C)_n}{(1 + i)^n} = \sum_{t=0}^n \frac{(B - C)_t}{(1 + i)^t} = \sum_{t=0}^n f_t (B - C)_t$$

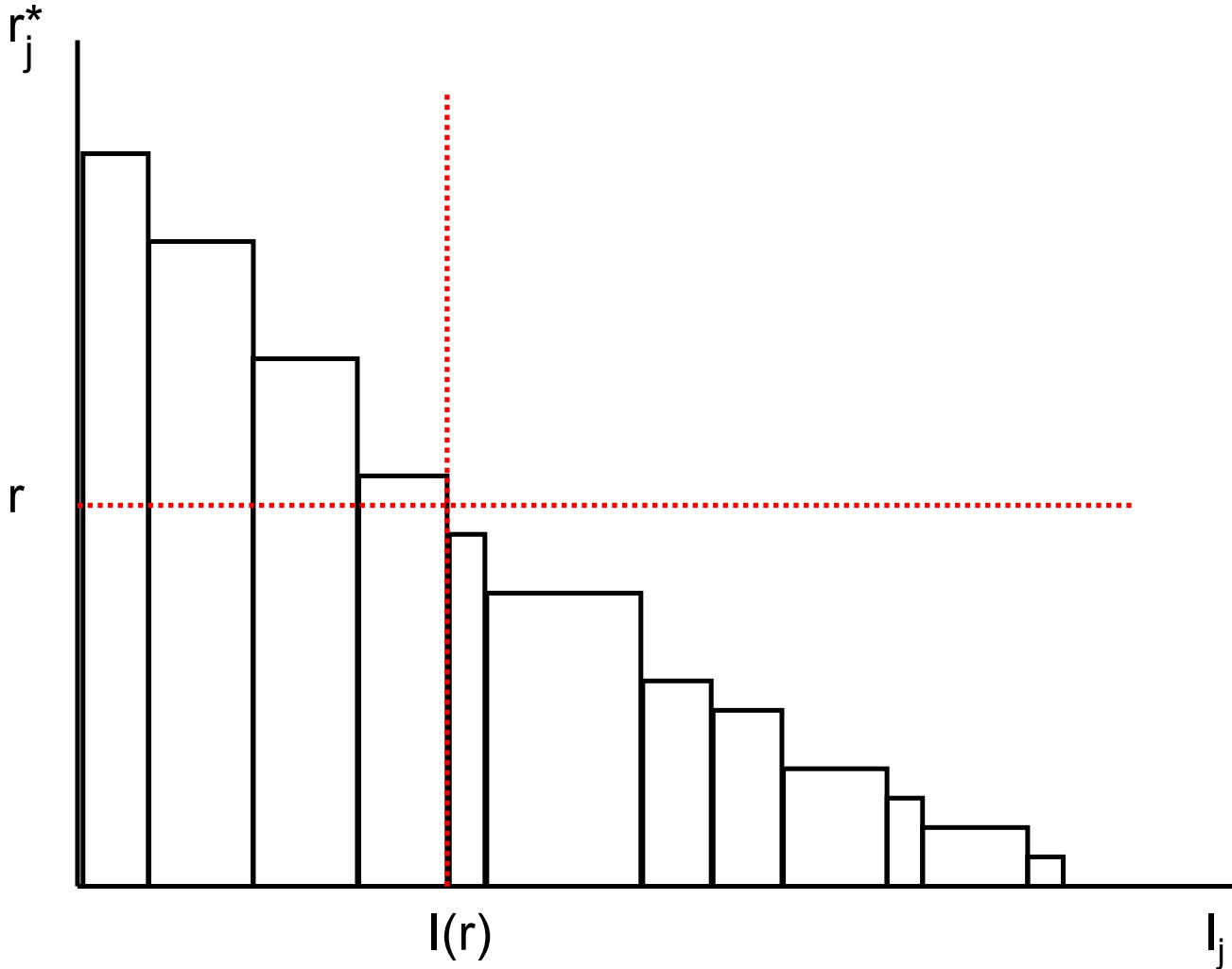
- Decision rule
 - For unique project: approve the project if $NPV \geq 0$
 - For competing projects requiring investments of similar magnitude: select the project with the highest NPV, if its $NPV \geq 0$
- Advantages: simple use, easy selection of rival projects (if all C&B included)
- Disadvantages: need to select discount rate i

Internal rate of return (IRR)

- Investing in the more expensive BE car is profitable at 0% discount rate but not at 4% discount rate
- There must be a discount rate at which the investment just breaks even ($NPV = 0$)
- This is the **internal rate of return**
- It can be found by trial and error (vary discount rate until $NPV = 0$) or with the IRR function of the calculation tool
- For the BE over ICE 'investment', $IRR = 3.62\%$
- Is this enough? Set a '**hurdle rate**', which can then serve as discount rate!

Hurdle rate

RANKING OF INVESTMENT PROJECTS
BASED ON THEIR INTERNAL RATE OF RETURN



- The **hurdle rate** is the required rate of return for this type of investment
- $I(r)$ is the amount that can be invested with (expected) IRR greater than hurdle rate r
- Anything that lowers the hurdle rate or raises the IRR of projects triggers more investment

Internal Rate of Return (IRR)

- Alternative method which is useful for proposals for which it is very difficult to determine a suitable discount rate i
- Definition: The IRR is the discount rate r which would give an NPV of zero, given expected benefits and costs

$$0 = (B - C)_0 + \frac{(B - C)_1}{(1 + r)^1} + \frac{(B - C)_2}{(1 + r)^2} + \dots + \frac{(B - C)_n}{(1 + r)^n} = \sum_{t=0}^n \frac{(B - C)_t}{(1 + r)^t}$$

- Decision rule for competing proposals: pick the project with the highest IRR, if $\text{IRR} \geq 0$
- Advantage: no need to choose a discount rate
- Disadvantage: the size of the project is not considered; a small project with a NPV of CHF1,000 and an IRR of 25% would be preferred to a large project with a NPV of CHF1,000,000 and an IRR of 20%

Benefit-Cost Ratio (BC ratio)

- Definition :
 - The BC ratio is the ratio between discounted benefits and discounted costs over the period of n years, given the discount rate i
 - BC ratio > 1 implies $NPV > 0$

$$\text{BC ratio} = \frac{\sum_{t=0}^n \frac{B_t}{(1+i)^t}}{\sum_{t=0}^n \frac{C_t}{(1+i)^t}}$$

- Decision rule :
 - Unique project: approve the project if $BC \text{ ratio} \geq 1$
 - For competing proposals: picking the projects with the highest BC ratio, provided $BC \text{ ratio} \geq 1$
- Advantage/disadvantage: equivalent to NPV

Benefit-Cost Ratio

	ICE - BE	Discount rate: 4.0%	Discount years	Discount factor	Present value
Net acquisition cost	-5 850 €		0	1.00	-5 850 €
Running costs year 1	1 089 €		0.5	0.98	1 068 €
Running costs year 2	1 089 €		1.5	0.94	1 027 €
Running costs year 3	1 089 €		2.5	0.91	987 €
Running costs year 4	1 089 €		3.5	0.87	949 €
Running costs year 5	1 089 €		4.5	0.84	913 €
Residual value	1 030 €		5	0.82	847 €
NET PRESENT VALUE					- 59 €

$$\text{Discount factor} = (1+i)^{-\text{Discount years}}$$

PV of costs	5 850 €
PV of benefits	5 791 €
B/C ratio	0.99 €

- Investors sometimes want to compare total benefits to total costs
- Netting out creates some confusion between costs and benefits

Payback period

- Definition: number of years until the benefits exceed the initial cost
- Very popular in the private sector
- It is a measure of time, not a measure of value
- To illustrate with BE vs ICE example, the fixed holding period and the residual value must be abandoned, unless there is a physical or legal end-of-life

Payback period for BE car

		Discount rate:		4.0%			
		ICE - BE	Sum of payments	Discount years	Discount factor	Present value	NPV
Net acquisition cost	-5 850 €	-5 850 €		0	1.00	-5 850 €	-5 850 €
Running costs year 1	1 089 €	-4 761 €		0.5	0.98	1 068 €	-4 782 €
Running costs year 2	1 089 €	-3 672 €		1.5	0.94	1 027 €	-3 755 €
Running costs year 3	1 089 €	-2 583 €		2.5	0.91	987 €	-2 768 €
Running costs year 4	1 089 €	-1 494 €		3.5	0.87	949 €	-1 819 €
Running costs year 5	1 089 €	- 405 €		4.5	0.84	913 €	- 906 €
Running costs year 6	1 089 €	684 €		5.5	0.81	878 €	- 28 €
Running costs year 7	1 089 €	1 773 €		6.5	0.77	844 €	816 €
Running costs year 8	1 089 €	2 862 €		7.5	0.75	811 €	1 627 €

- The NPV in the last column is the present value of all 'payments' up to that year
- The NPV turns positive with year 7, i.e., the BE is the better choice for a user who plans to use her car for 7 years at least
- Without discounting, payback period = 6 years

Levelized cost of electricity and payback period for a CCGT plant in UK

Hurdle rate	Project start		Construction start		Operation start																												
	2020	2021	2022	2023	2024	2025	2026	2027	2028	2029	2030	2031	2032	2033	2034	2035	2036	2037	2038	2039	2040	2041	2042	2043	2044	2045	2046	2047	2048	2049			
	7.5%	100.0%	93.0%	86.5%	80.5%	74.9%	69.7%	64.8%	60.3%	56.1%	52.2%	48.5%	45.1%	42.0%	39.1%	36.3%	33.8%	31.4%	29.2%	27.2%	25.3%	23.5%	21.9%	20.4%	18.9%	17.6%	16.4%	15.3%	14.2%	13.2%	12.3%		
Discount factor																																	
Development cost	£m	5.2	6.8																														
Construction cost	£m			288.0	288.0	144.0																											
Fixed O&M	£m					24.2	24.2	24.2	24.2	24.2	24.2	24.2	24.2	24.2	24.2	24.2	24.2	24.2	24.2	24.2	24.2	24.2	24.2	24.2	24.2	24.2	24.2	24.2	24.2	24.2	24.2		
Variable O&M	£m					19.6	19.6	19.6	19.6	19.6	19.6	19.6	19.6	19.6	19.6	19.6	19.6	19.6	19.6	19.6	19.6	19.6	19.6	19.6	19.6	19.6	19.6	19.6	19.6	19.6	19.6	19.6	
Fuel costs	£m					403.6	354.7	366.9	373.0	385.2	391.3	397.5	403.6	409.7	415.8	421.9	421.9	421.9	421.9	421.9	421.9	421.9	421.9	421.9	421.9	421.9	421.9	421.9	421.9	421.9	421.9	421.9	
Social cost of carbon	£m					280.2	280.2	280.2	280.2	280.2	280.2	280.2	280.2	280.2	280.2	280.2	280.2	280.2	280.2	280.2	280.2	280.2	280.2	280.2	280.2	280.2	280.2	280.2	280.2	280.2	280.2		
TOTAL COST	£m	5.2	6.8	288.0	288.0	144.0	727.5	678.6	690.8	697.0	709.2	715.3	721.4	727.5	733.7	739.8	745.9	745.9	745.9	745.9	745.9	745.9	745.9	745.9	745.9	745.9	745.9	745.9	745.9	745.9	745.9		
Discounted costs	£m	5.2	6.4	249.2	231.8	107.8	506.8	439.7	416.4	390.8	369.9	347.1	325.6	305.5	286.5	268.8	252.1	234.5	218.1	202.9	188.8	175.6	163.3	151.9	141.3	131.5	122.3	113.8	105.8	98.5	91.6		
Power generation	GWh					9 776	9 776	9 776	9 776	9 776	9 776	9 776	9 776	9 776	9 776	9 776	9 776	9 776	9 776	9 776	9 776	9 776	9 776	9 776	9 776	9 776	9 776	9 776	9 776	9 776	9 776		
Discounted power gen. MWh						6 810	6 335	5 893	5 482	5 099	4 743	4 412	4 105	3 818	3 552	3 304	3 073	2 859	2 660	2 474	2 301	2 141	1 992	1 853	1 723	1 603	1 491	1 387	1 290	1 200			
Sum discounted costs	£m		6 649																														
Sum disc. power gen.	GWh		81 600																														
LCOE	£/MWh		81.5																														
Price of electricity	£/MWh		81.5																														
Revenue from electr.	£m					796.6	796.6	796.6	796.6	796.6	796.6	796.6	796.6	796.6	796.6	796.6	796.6	796.6	796.6	796.6	796.6	796.6	796.6	796.6	796.6	796.6	796.6	796.6	796.6	796.6	796.6		
Disc. revenue	£m					554.9	516.2	480.2	446.7	415.5	386.5	359.6	334.5	311.1	289.4	269.2	250.5	233.0	216.7	201.6	187.5	174.5	162.3	151.0	140.4	130.6	121.5	113.0	105.2	97.8			
Disc. revenue-costs	£m	-5.2	-6.4	-249.2	-231.8	-107.8	48.1	76.5	63.8	55.9	45.6	39.5	34.0	29.0	24.6	20.7	17.2	16.0	14.8	13.8	12.8	11.9	11.1	10.3	9.6	8.9	8.3	7.7	7.2	6.7	6.2		
NPV	£m	-5.2	-11.5	-260.7	-492.6	-600.4	-552.3	-475.8	-412.0	-356.1	-310.5	-271.0	-237.1	-208.1	-183.5	-162.8	-145.6	-129.7	-114.8	-101.0	-88.2	-76.2	-65.1	-54.8	-45.2	-36.2	-27.9	-20.1	-12.9	-6.2	0.0		
<i>Results for price = 82.5</i>																																	
Disc. revenue-costs	£m	-5.2	-6.4	-249.2	-231.8	-107.8	55.0	82.9	69.7	61.4	50.8	44.3	38.4	33.2	28.5	24.3	20.5	19.1	17.7	16.5	15.3	14.3	13.3	12.4	11.5	10.7	9.9	9.3	8.6	8.0	7.4		
NPV	£m	-5.2	-11.5	-260.7	-492.6	-600.4	-545.4	-462.5	-392.7	-331.3	-280.5	-236.3	-197.8	-164.7	-136.2	-112.0	-91.5	-72.4	-54.6	-38.1	-22.8	-8.5	4.8	17.1	28.6	39.3	49.2	58.5	67.1	75.1	82.6		
<i>Results for price = 80.5</i>																																	
Disc. revenue-costs	£m	-5.2	-6.4	-249.2	-231.8	-107.8	41.4	70.2	57.9	50.5	40.6	34.8	29.6	25.0	20.8	17.2	13.9	12.9	12.0	11.2	10.4	9.7	9.0	8.4	7.8	7.2	6.7	6.3	5.8	5.4	5.0		
NPV	£m	-5.2	-11.5	-260.7	-492.6	-600.4	-559.0	-488.8	-430.8	-380.3	-339.8	-305.0	-275.4	-250.4	-229.6	-212.4	-198.6	-185.6	-173.6	-162.4	-152.0	-142.4	-133.4	-125.0	-117.2	-110.0	-103.2	-96.9	-91.1	-85.7	-80.6		

Data from <https://www.gov.uk/government/publications/electricity-generation-costs-2023>, Annex B <02.05.2024>

A particular type of payback period: energy or CO₂ recovery

- Many measures serving to reduce energy consumption or CO₂ emissions involve new equipment and/or construction work (e.g. replacing machines, insulating buildings)
- These measures cause energy use and CO₂ emissions → 'embodied energy or CO₂', 'grey energy or CO₂'
- Spending energy to save energy, emitting CO₂ to reduce CO₂ emissions...
- This only makes sense if the energy savings thus obtained exceed embodied energy, and the CO₂ emissions avoided exceed embodied CO₂
- How many years of these savings are needed to offset the embodied pollution?
- Example: typical energy refurbishment of buildings 'costs' 440 kgCO₂/m², which corresponds to 10 years of thus avoided CO₂ emissions

EXAMPLE – PV ON YOUR ROOF

Illustrative data for PV on single-family houses in Switzerland (early 2022)

	Costs and benefits (CHF)
One-off costs	
Investment cost	30 000
Subsidy	4 500
Tax rebate	5 000
Annual benefits and costs	
Electricity saving	600
Revenue from electricity sales	630
Maintenance	180



Assumption: 25% self-consumption
Typical life expectancy: 25 years

Cleaning up costs and incomes

	Costs and benefits (CHF)
One-off costs	
Investment cost	30 000
Subsidy	4 500
Tax rebate	5 000
Annual benefits and costs	
Electricity saving	600
Revenue from electricity sales	630
Maintenance	180

Initial investment	-20 500
Yearly net income	1 050

- Direct rate of return: $1050 / 20\ 500 = 5.1\%$
- What is the problem with this number?

discount rate:		0.0%			
		Discount Payments	Discount years	Discount factor	Discounted payments
Initial investment	-20 500	0	1.00	-20 500	
Income year 1	1 050	1	1.00	1 050	
Income year 2	1 050	2	1.00	1 050	
Income year 3	1 050	3	1.00	1 050	
Income year 4	1 050	4	1.00	1 050	
Income year 5	1 050	5	1.00	1 050	
Income year 6	1 050	6	1.00	1 050	
Income year 7	1 050	7	1.00	1 050	
Income year 8	1 050	8	1.00	1 050	
Income year 9	1 050	9	1.00	1 050	
Income year 10	1 050	10	1.00	1 050	
Income year 11	1 050	11	1.00	1 050	
Income year 12	1 050	12	1.00	1 050	
Income year 13	1 050	13	1.00	1 050	
Income year 14	1 050	14	1.00	1 050	
Income year 15	1 050	15	1.00	1 050	
Income year 16	1 050	16	1.00	1 050	
Income year 17	1 050	17	1.00	1 050	
Income year 18	1 050	18	1.00	1 050	
Income year 19	1 050	19	1.00	1 050	
Income year 20	1 050	20	1.00	1 050	
Income year 21	1 050	21	1.00	1 050	
Income year 22	1 050	22	1.00	1 050	
Income year 23	1 050	23	1.00	1 050	
Income year 24	1 050	24	1.00	1 050	
Income year 25	1 050	25	1.00	1 050	
NPV			5 750		

NPV

discount rate:		4.0%			
		Discount Payments	Discount years	Discount factor	Discounted payments
Initial investment	-20 500	0	1.00	-20 500	
Income year 1	1 050	1	0.96	1 010	
Income year 2	1 050	2	0.92	971	
Income year 3	1 050	3	0.89	933	
Income year 4	1 050	4	0.85	898	
Income year 5	1 050	5	0.82	863	
Income year 6	1 050	6	0.79	830	
Income year 7	1 050	7	0.76	798	
Income year 8	1 050	8	0.73	767	
Income year 9	1 050	9	0.70	738	
Income year 10	1 050	10	0.68	709	
Income year 11	1 050	11	0.65	682	
Income year 12	1 050	12	0.62	656	
Income year 13	1 050	13	0.60	631	
Income year 14	1 050	14	0.58	606	
Income year 15	1 050	15	0.56	583	
Income year 16	1 050	16	0.53	561	
Income year 17	1 050	17	0.51	539	
Income year 18	1 050	18	0.49	518	
Income year 19	1 050	19	0.47	498	
Income year 20	1 050	20	0.46	479	
Income year 21	1 050	21	0.44	461	
Income year 22	1 050	22	0.42	443	
Income year 23	1 050	23	0.41	426	
Income year 24	1 050	24	0.39	410	
Income year 25	1 050	25	0.38	394	
NPV			5 750		

NPV

- At 0% discount rate, the NPV is positive over 25 years
- At 4% discount rate, the NPV is negative over 25 years
- $IRR = 2.0\%$
- Payback period without discounting < 25 years
- Payback period with 4% discounting > 25 years
- Payback period with 2% discounting $= 25$ years

Payback period with discounting

- NPV only turns positive with 39 years of incomes
- How patient is an investor discounting at 4%?
- Is it reasonable to assume constant income?
- Relationship between discount rate and evolution of incomes...

		discount rate:	4.0%			
	Payments	Discount years	Discount factor	Discounted payments	NPV	
Initial investment	-20 500	0	1.00	-20 500	-20 500	
Income year 1	1 050	1	0.96	1 010	-19 490	
Income year 2	1 050	2	0.92	971	-18 520	
Income year 3	1 050	3	0.89	933	-17 586	
Income year 4	1 050	4	0.85	898	-16 689	
Income year 5	1 050	5	0.82	863	-15 826	
Income year 6	1 050	6	0.79	830	-14 996	
Income year 7	1 050	7	0.76	798	-14 198	
Income year 8	1 050	8	0.73	767	-13 431	
Income year 9	1 050	9	0.70	738	-12 693	
Income year 10	1 050	10	0.68	709	-11 984	
Income year 31	1 050	31	0.30	311	-2 032	
Income year 32	1 050	32	0.29	299	-1 733	
Income year 33	1 050	33	0.27	288	-1 445	
Income year 34	1 050	34	0.26	277	-1 168	
Income year 35	1 050	35	0.25	266	- 902	
Income year 36	1 050	36	0.24	256	- 646	
Income year 37	1 050	37	0.23	246	- 400	
Income year 38	1 050	38	0.23	237	- 164	
Income year 39	1 050	39	0.22	227	64	
Income year 40	1 050	40	0.21	219	282	

DISCUSSION

Which decision rule to adopt?

- NPV, benefit-cost ratio, IRR or payback period?
- What discount rate or hurdle rate?
- What horizon?
- How to handle risk?
- What importance for this financial calculation?
- Other criteria (liquidity constraint)?
- Influence of personal characteristics and practices on 'profitability'
- Multiple objectives