

## ENV-413: Thermodynamics of the Earth systems

### Exercise session for Lecture 10

4. Consider a two-component system consistent of  $\text{H}_2\text{O}$  and  $\text{NaCl}$ . Write the Gibbs phase rule for this two-component system.
5. To conveniently represent the phase diagram on a graph, we can eliminate one degree of freedom if we examine the system only at constant pressure. For the two-component system at constant pressure, what is the maximum number of thermodynamic degrees of freedom for this system?

9. Matching:

- |       |                             |                               |
|-------|-----------------------------|-------------------------------|
| _____ | latent heat of fusion       | a. $677 \text{ cal g}^{-1}$   |
| _____ | latent heat of vaporization | b. $597.3 \text{ cal g}^{-1}$ |
| _____ | latent heat of sublimation  | c. $77.7 \text{ cal g}^{-1}$  |

10. During a phase change from liquid to vapor, state whether the following variables increase, decrease, or remain the same

Temperature \_\_\_\_\_

Pressure \_\_\_\_\_

Specific Volume \_\_\_\_\_

Entropy \_\_\_\_\_

Enthalpy \_\_\_\_\_

Gibbs energy \_\_\_\_\_

1. Nucleation of a pure phase of one component is referred to as

- a) homogeneous
- b) heterogeneous

2. Most of the nucleation processes in the atmosphere is

- a) homogeneous nucleation
- b) heterogeneous nucleation

#### Surface tension work

3. Write an expression for surface tension work

4. What are the units for surface tension?

5a. The effect of surface tension on the internal energy of a droplet is (greater than, less than, the same) for a smaller drop.

6a. How much work is required to break a 1 cm cube of water into drops with radius 10  $\mu\text{m}$ ? (use surface tension 0.076 N  $\text{m}^{-1}$ .)

16. Refer to Fig. 5.3, which is a graph of Kelvin's equation

$$r^* = \frac{2\sigma_{lv}}{\rho_l R_v T \ln S} \quad (5.14a)$$

- a) Has a drop with radius  $1 \times 10^{-3}$   $\mu\text{m}$  and  $S=1.5$  been activated (i.e. will it grow spontaneously)?
- b) Has a drop with radius  $1 \times 10^{-3}$   $\mu\text{m}$  and  $S=4$  been activated (i.e. will it grow spontaneously)?

17. The formation of pure water droplets requires a vapor pressure that is (less than, equal to, greater than) the saturation vapor pressure over a plane surface of pure water

18. If the relative humidity of the air is 100%, droplets of pure water will

- a) evaporate
- b) grow further by condensation
- c) remain the same size

19. Are values of  $S=1.5$  and  $S=4$  observed in the atmosphere? What is a realistic maximum value of  $S$  that is observed in the atmosphere?