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EE-559

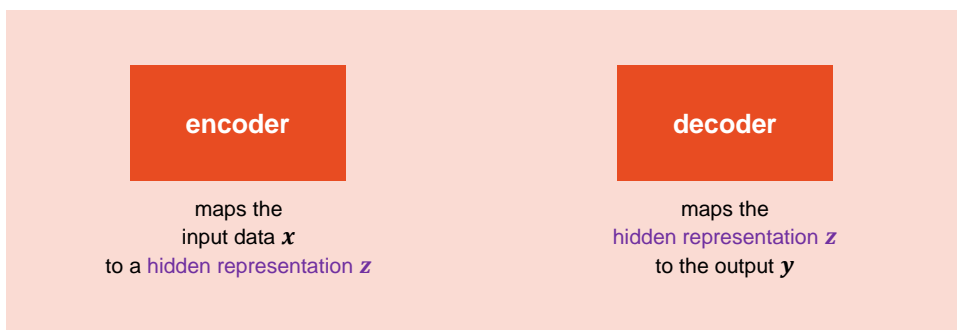
Deep Learning

What's on today?

- **Deterministic autoencoders**: on discovering structure within the data
- **Variational autoencoders**: on using a continuous latent space
- **Vector quantised-variational autoencoder**: on using discrete latents
- **Diffusion probabilistic models**: on learning noise removal
- **Instruction-following diffusion models**: on editing with language
- **Exercises**: autoencoders and variational autoencoders

Deterministic autoencoders

Auto-associative neural network

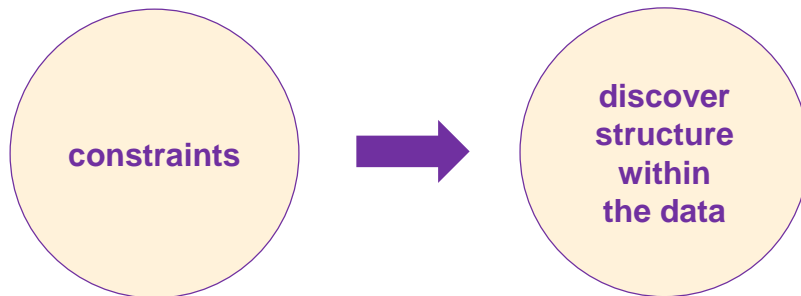


trained to generate an output y that is as close as possible to x

Concepts:

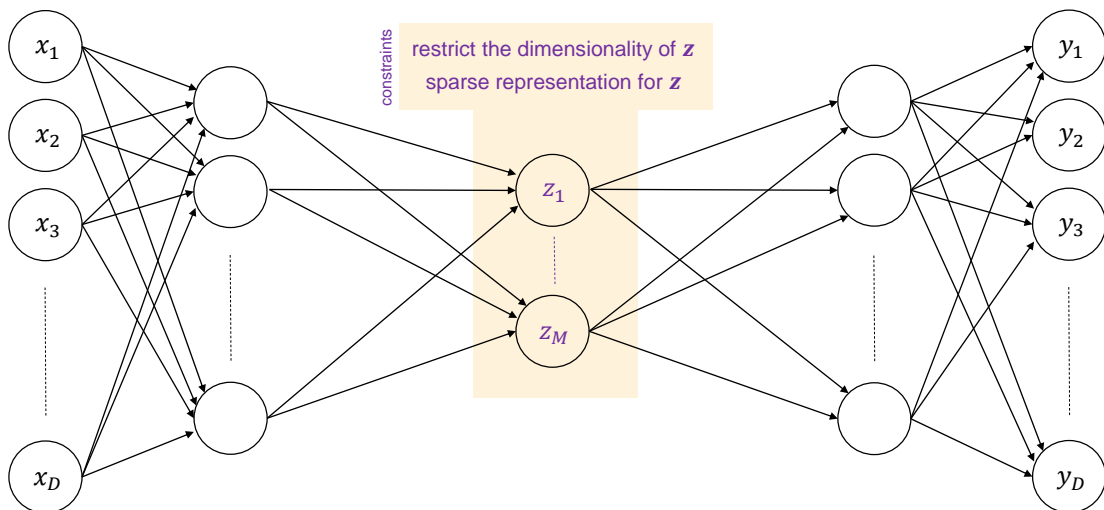
Same number of input and output units; internal representation $z(x)$ of each new input.

Autoencoder

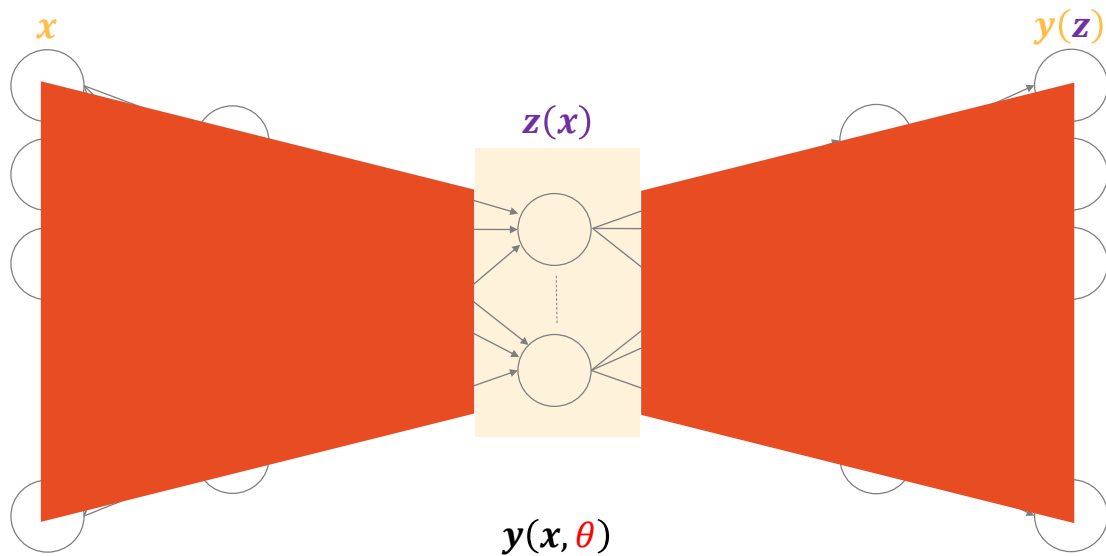


Concept:
Non-linear form of Principal Component Analysis (PCA)

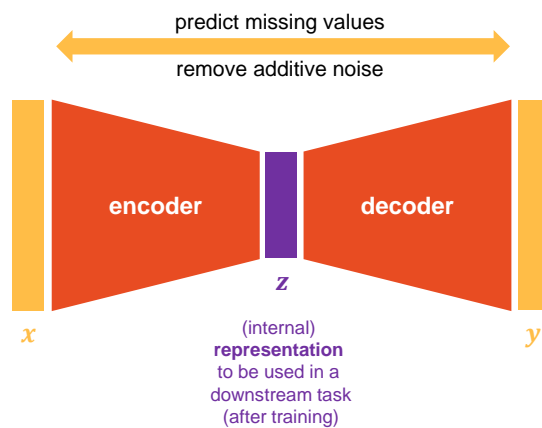
Autoencoder: network diagram



Autoencoder



Autoencoder: training



Concepts: Self-supervision; modify the training process to *undo* corruptions of the input vector x ; dimensionality of subspace to be defined *before* training the network.

Denoising autoencoders

$$\mathbf{x}_n \xrightarrow{\text{noise}} \tilde{\mathbf{x}}_n$$

examples

set a random amount ρ of input variables to 0 $0 \leq \rho \leq 1$

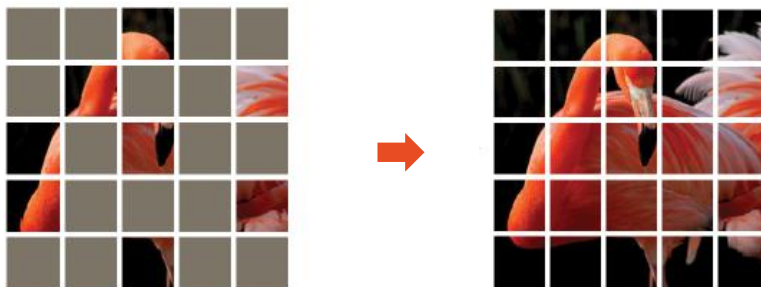
add *independent* zero-mean Gaussian noise to each input variable

$$E(\theta) = \sum_{n=1}^N ||\mathbf{y}(\tilde{\mathbf{x}}_n, \theta) - \mathbf{x}_n||^2$$

Concept:

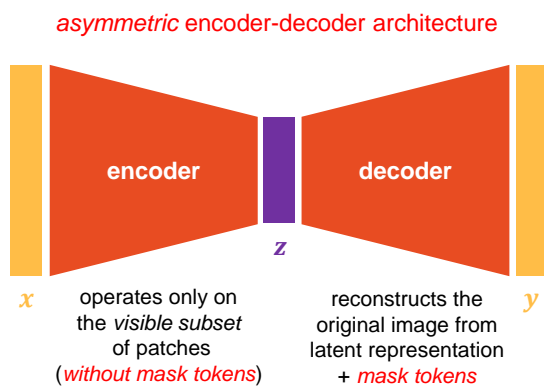
Network encouraged to learn (aspects of) the structure of the data by learning to denoise the input data.

Masked autoencoders



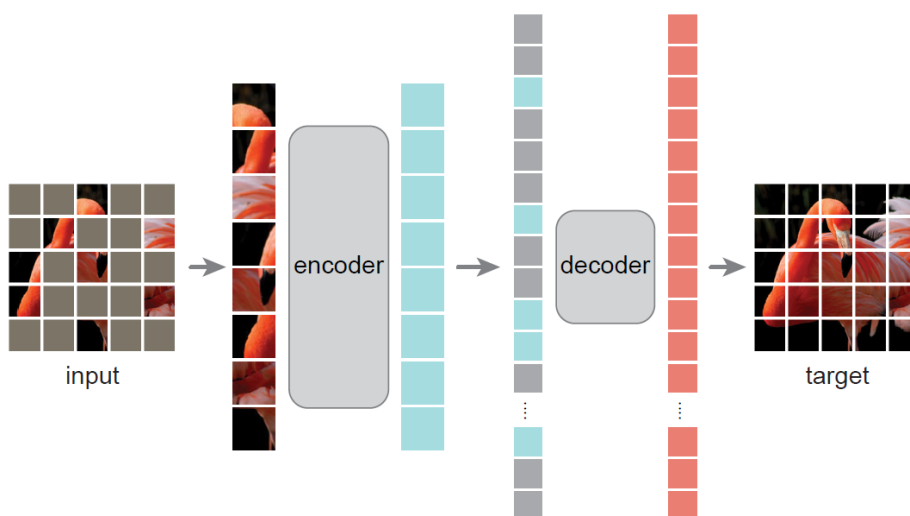
[arXiv:2111.06377](https://arxiv.org/abs/2111.06377)

Masked autoencoders



Concepts: Pass only randomly selected input patches (as low as 25% of an image); each mask token is augmented with positional encoding.

Masked autoencoders



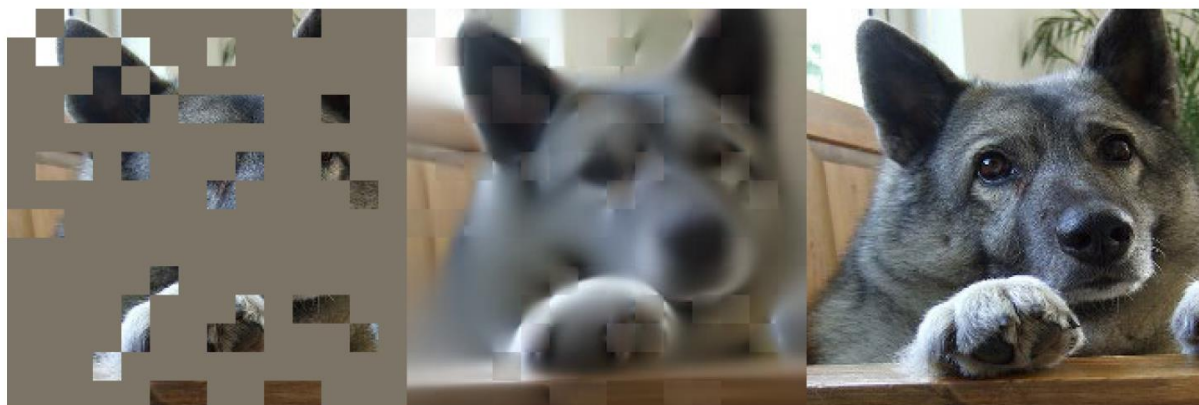
[arXiv:2111.06377](https://arxiv.org/abs/2111.06377)

Masked autoencoder: example



[arXiv:2111.06377](https://arxiv.org/abs/2111.06377)

Masked autoencoder: example



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Sparse autoencoders

regularizer to encourage sparse representation

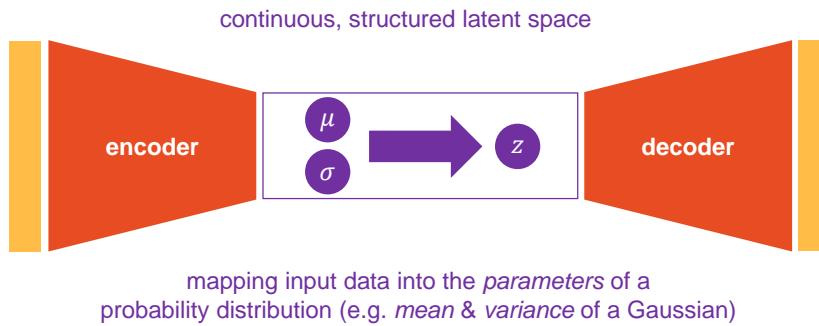
$$\tilde{E}(\theta) = \underset{\text{un-regularized error}}{E(\theta)} + \lambda \sum_{k=1}^K \underset{\text{regularizer applied to the unit activations of a hidden layer}}{|z_k|}$$

Concept:

To constrain the internal representation with a regularizer.

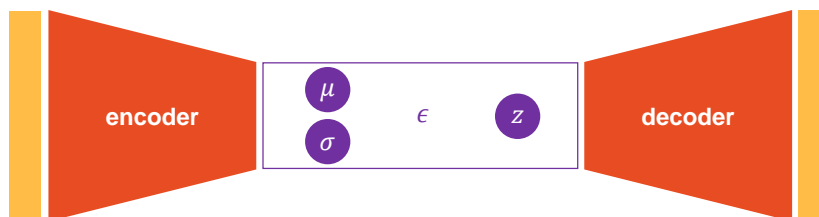
Variational autoencoders

VAE



[arXiv:1312.6114](https://arxiv.org/abs/1312.6114)

VAE: flow of gradients during training



ϵ Gaussian **random variable** with *zero mean* and *unit variance*

$z = \sigma\epsilon + \mu$ reparametrization trick (**replaces** direct sample of z)

z Gaussian distribution with *mean* μ and *variance* σ^2

[arXiv:1312.6114](https://arxiv.org/abs/1312.6114)

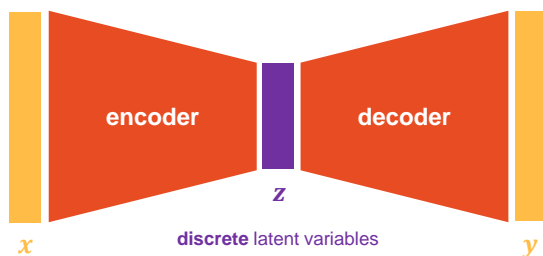
Vector Quantised-Variational Autoencoder

Neural discrete representation learning



Concepts: Parameterization of the posterior distribution of (discrete) latent variables given an observation; vector quantisation is used to learn a discrete latent.

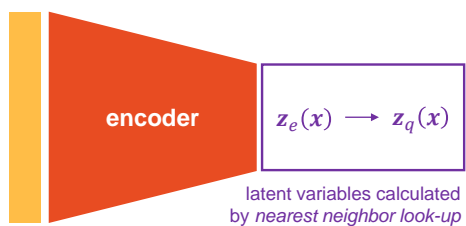
VQ-VAE



Concepts: Categorical posterior and prior distributions; samples (drawn from these distributions) index an embedding.

Discrete latent variables

$e \in \mathbb{R}^{K \times D}$ latent embedding space
 K size of the discrete latent space
 D dimensionality of each latent embedding vector



posterior categorical distribution (one-hot)

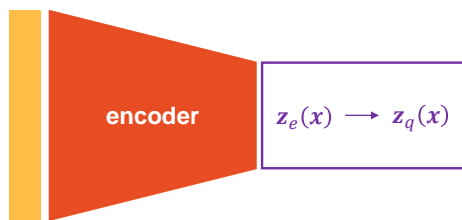
$$q(z = k | x) = \begin{cases} 1 & \text{for } k = \operatorname{argmin}_j \|z_e(x) - e_j\|_2 \\ 0 & \text{otherwise} \end{cases}$$

output of the encoder network
embedding vector
 $e_i \in \mathbb{R}^D \ i = 1, 2, \dots, K$

$$z_q(x) = e_k \quad \text{where } k = \operatorname{argmin}_j \|z_e(x) - e_j\|_2$$

[arXiv:1711.00937](https://arxiv.org/abs/1711.00937)

Learning



$e \in \mathbb{R}^{K \times D}$ latent embedding space
 K size of the discrete latent space
 D dimensionality of each latent embedding vector

$$z_q(x) = e_k \quad \text{where } k = \operatorname{argmin}_j \|z_e(x) - e_j\|_2$$

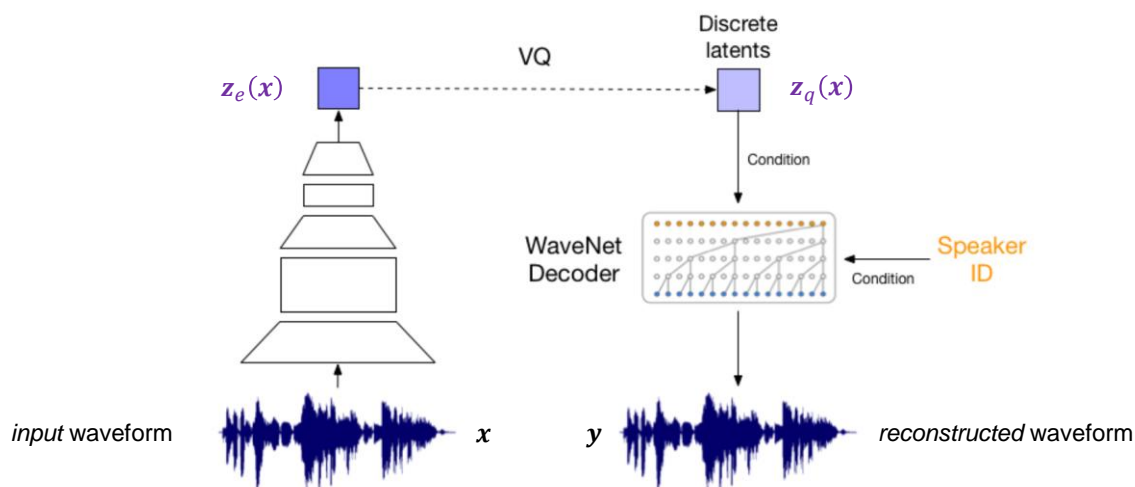
no gradient defined for this mapping!



copy gradients from decoder input $z_q(x)$
 to encoder output $z_e(x)$

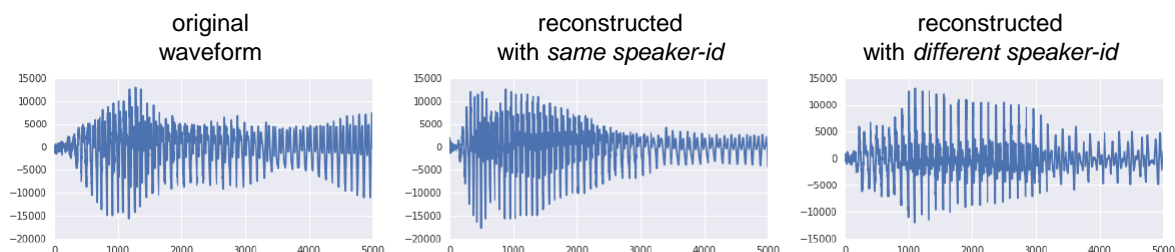
[arXiv:1711.00937](https://arxiv.org/abs/1711.00937)

VQ-VAE: example



[arXiv:1711.00937](https://arxiv.org/abs/1711.00937)

VQ-VAE: example

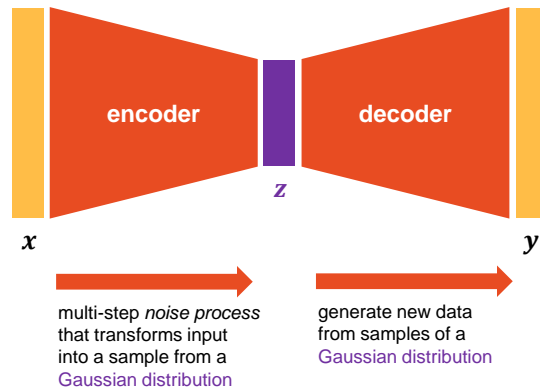


the **contents** of the three waveforms are the **same**

[arXiv:1711.00937](https://arxiv.org/abs/1711.00937)

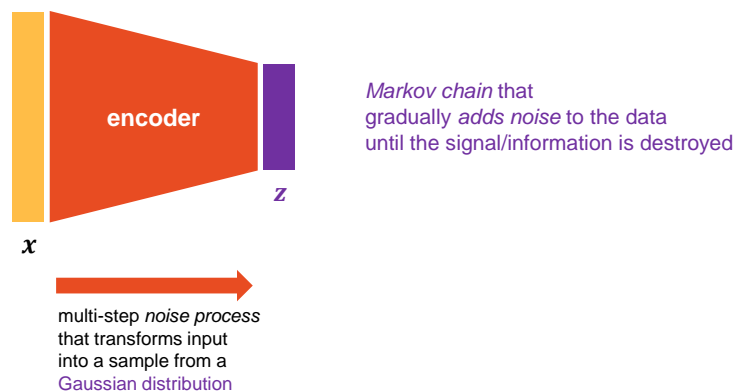
Diffusion probabilistic models

Denoising diffusion probabilistic models



Concepts: Hierarchical variational autoencoder; encoder distribution is fixed (*defined by the noise process*); only the generative distribution of the decoder is learned.

Diffusion process



Diffusion (forward) process

$$q(\mathbf{x}_{1:T}|\mathbf{x}_0) = \prod_{t=1}^T q(\mathbf{x}_t|\mathbf{x}_{t-1})$$

posterior

$$q(\mathbf{x}_t|\mathbf{x}_{t-1}) = \mathcal{N}(\mathbf{x}_t; \sqrt{1 - \beta_t}\mathbf{x}_{t-1}, \beta_t \mathbf{I})$$

fixed Markov chain that gradually adds Gaussian noise

β_1, \dots, β_T variance schedule (the β_i are fixed)

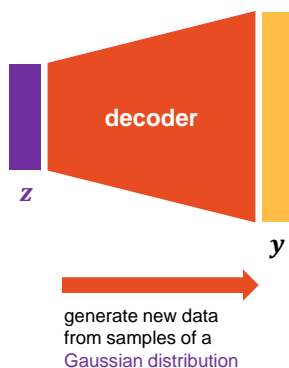
[arXiv:2006.11239](https://arxiv.org/abs/2006.11239)

Reverse process

if diffusion consists of small amounts of Gaussian noise,
then it suffices to set the *sampling chain transitions*
to conditional Gaussians too



simple neural network parameterization!



[arXiv:2006.11239](https://arxiv.org/abs/2006.11239)

Reverse process

$$p_{\theta}(\mathbf{x}_{0:T}) = p(\mathbf{x}_T) \prod_{t=1}^T p_{\theta}(\mathbf{x}_{t-1}|\mathbf{x}_t) \quad \text{reverse process (joint distribution)}$$

$$p(\mathbf{x}_T) = \mathcal{N}(\mathbf{x}_T; \mathbf{0}, \mathbf{I}) \quad \text{start of the Markov chain}$$

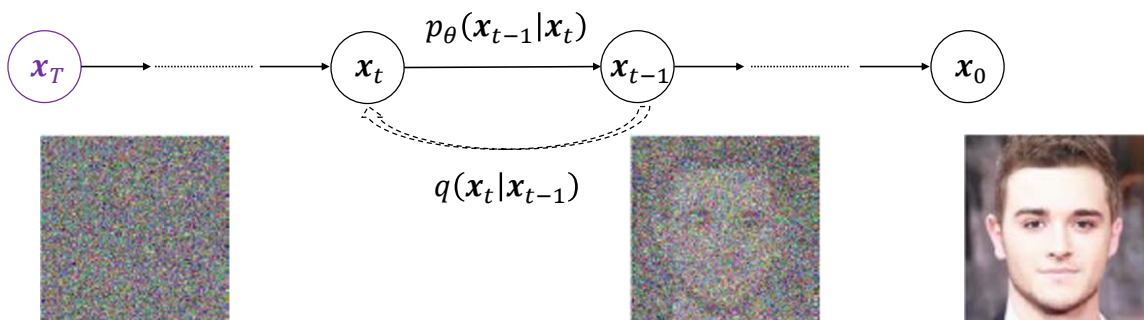
$$p_{\theta}(\mathbf{x}_{t-1}|\mathbf{x}_t) = \mathcal{N}(\mathbf{x}_{t-1}; \mu_{\theta}(\mathbf{x}_t, t), \Sigma_{\theta}(\mathbf{x}_t, t)) \quad \text{learned Gaussian transitions}$$

$\mathbf{x}_1, \mathbf{x}_2, \dots, \mathbf{x}_T$ latents of the same dimension as the data \mathbf{x}_0

[arXiv:2006.11239](https://arxiv.org/abs/2006.11239)

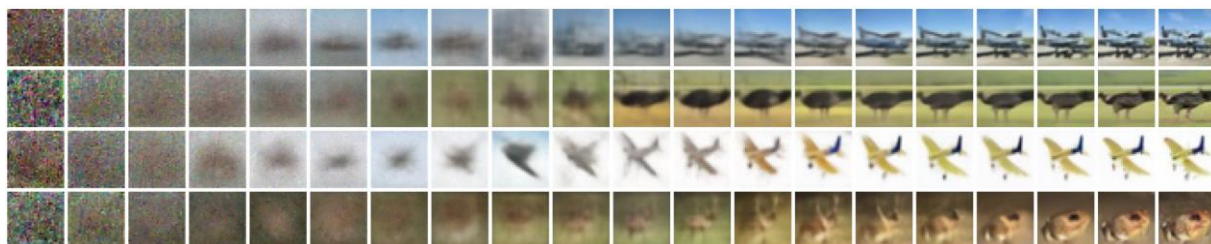
Diffusion probabilistic models

Reverse process:
parameterized Markov chain
trained using variational inference



[arXiv:2006.11239](https://arxiv.org/abs/2006.11239)

Reverse process: examples



[arXiv:2006.11239](https://arxiv.org/abs/2006.11239)

**Instruction-
following
diffusion models**

Text-to-image diffusion



"Teddy bears swimming at the Olympics 400m Butterfly event"

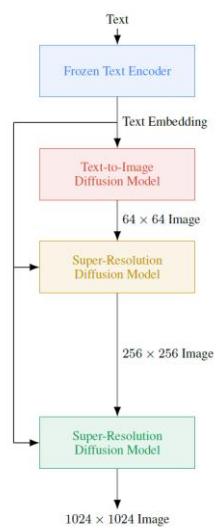
encoding text for image synthesis

image-text alignment

capturing complexity & compositionality of arbitrary natural language text inputs

[arXiv:2205.11487](https://arxiv.org/abs/2205.11487)

Text-to-image diffusion



"A Golden Retriever dog wearing a blue checkered beret and red dotted turtleneck."



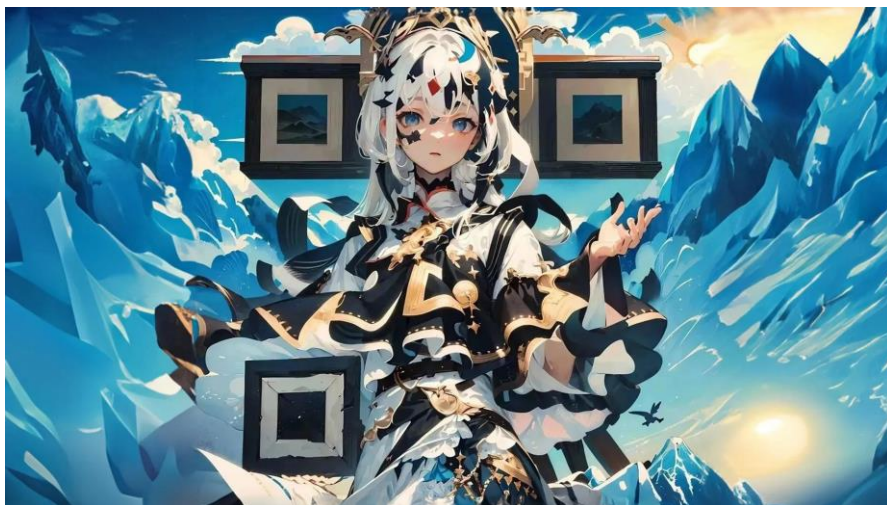
[arXiv:2205.11487](https://arxiv.org/abs/2205.11487)

Anime quick response codes



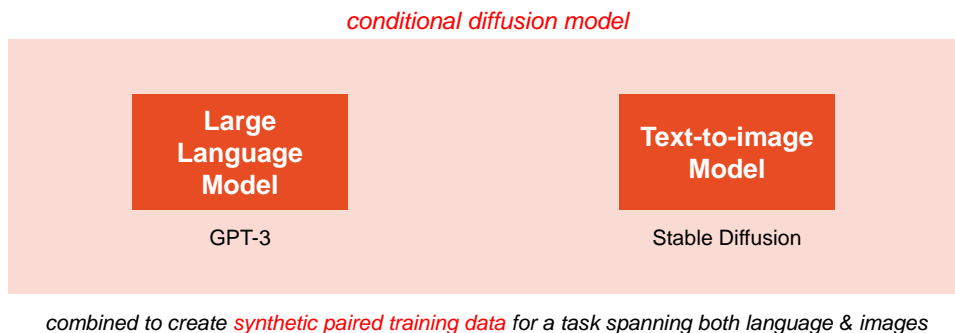
<https://arstechnica.com/information-technology/2023/06/redditor-creates-working-anime-qr-codes-using-stable-diffusion>

Anime quick response codes



<https://arstechnica.com/information-technology/2023/06/redditor-creates-working-anime-qr-codes-using-stable-diffusion>

Editing images from human instructions



[arXiv:2211.09800](https://arxiv.org/abs/2211.09800)

Synthetic multi-modal training data



[arXiv:2211.09800](https://arxiv.org/abs/2211.09800)

Instruction-following diffusion model



"turn her into a snake lady"



[arXiv:2211.09800](https://arxiv.org/abs/2211.09800)

Cross-attention control for editing

cross-attention maps bind pixels & tokens extracted from the prompt text



inject the cross-attention maps during the *diffusion process*
controlling which pixels attend to which tokens of the prompt text
during which diffusion steps



change a single token's value in the prompt
(e.g. *cat* to *dog*)
fix the cross-attention maps
to preserve the scene composition



globally edit an image
(e.g. change the style)
add new words to the prompt
freeze the attention on previous tokens
allow new attention to flow to the new tokens

[arXiv:2208.01626](https://arxiv.org/abs/2208.01626)

Cross-attention control for editing: example

*"Photo of a **cat** riding on a bicycle."*



source image



cat > dog



cat > chicken



cat > squirrel



cat > elephant

no need for model training, fine-tuning, extra data, or optimization

[arXiv:2208.01626](https://arxiv.org/abs/2208.01626)

Practice exercises

Today's practice exercises

- Autoencoders for anomaly detection
- Variational autoencoders for image generation

What did we learn today?

- Deterministic autoencoders
- Variational autoencoders
- Vector quantised-variational autoencoder
- Diffusion probabilistic models
- Instruction-following diffusion models
- Exercises

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Deep Learning

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