

Chapter II - Sound perception and noise

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Exercise 1.

1. $L_{Global} = 10 \log(10^{\frac{L_1}{10}} + 10^{\frac{L_2}{10}} + 10^{\frac{L_3}{10}} + 10^{\frac{L_4}{10}} + 10^{\frac{L_5}{10}} + 10^{\frac{L_6}{10}})$
2. See table.
3. The A-weighting reflects the human ear sensitivity. (§ 2.3.15)
4. See table.
5. See table.

Bandes (Hz)	125	250	500	1000	2000	4000	Global
L_1 (dB)	84.3	80.5	77.3	72.0	69.3	68.0	86.7
L_2 (dB)	68.0	69.3	72.0	77.3	80.5	84.3	86.7
A-weighting (dB)	-16	-8.5	-3	0	+1	+1	
$L_{1,A}$ (dB(A))	68.3	72.0	74.3	72.0	70.3	69.0	79.2
$L_{2,A}$ (dB(A))	52.0	60.8	69.0	77.3	81.5	85.3	87.3

6. Remarks : here we can see the weight importance since two sounds with the same equivalent level in dB but with two different spectra give two A-weighted levels completely different. However these levels are more representative for ears.

Exercise 2.

1. Octave bands :

$$f_c = f_{min} \times \sqrt{2} = f_{max} / \sqrt{2}$$

$$f_{c_{sup}} = 2f_{c_{inf}}$$

Central frequencies (Hz)	125	250	500
Min - Max frequencies (Hz)	88	177	354

Bandes (Hz)	125	250	500	Global
Niveau (dB)	84.0	87.0	80.0	89.3
Niveau (dB(A))	68.0	78.5	77.0	81.0

2. & 3.

4. Equivalent level in the engine shop :

$$L_{tot,A} = 10 \log(4 \cdot 10^{\frac{L_{dB(A)}}{10}}) = 10 \log(4 \cdot 10^{\frac{81.5}{10}}) = 87.0 \text{ dB(A)}$$

5.

$$E_{A,T} = \int p_A^2(t) dt$$

$$L_A = 10 \log\left(\frac{p_A^2}{p_0^2}\right) \implies p_A^2 = p_0^2 \cdot 10^{\frac{L_A}{10}}, \text{ with } p_0 = 2 \cdot 10^{-5} \text{ Pa}$$

$$E_{tot,A} = p_A^2 \cdot t = p_0^2 \cdot 10^{\frac{L_{tot,A}}{10}} \cdot t = ((2 \cdot 10^{-5})^2 \cdot 10^{\frac{87}{10}})(8 \cdot 3600) \approx 5'774 \text{ Pa}^2 \cdot \text{s}$$

The law is not respected.

6.

$$\begin{aligned} E_{A,T} &= p_{1,A}^2 \cdot t_1 + p_{2,A}^2 \cdot t_2 = p_0^2(10^{\frac{L_{1,A}}{10}} t_1 + 10^{\frac{L_{2,A}}{10}} t_2) \\ &= (2 \cdot 10^{-5})^2(10^{\frac{87.0}{10}}(7 \cdot 3600) + 10^{\frac{55}{10}}(1 \cdot 3600)) \approx 5'052 \text{ Pa}^2 \cdot \text{s} \end{aligned}$$

The law is respected now.

Exercise 3.

1. $L(1000\text{Hz}) = 90 \text{ dB} \rightarrow L_N(1000\text{Hz}) = 90 \text{ phones}$

$L(63\text{Hz}) = 100 \text{ dB} \rightarrow L_N(63\text{Hz}) = 90 \text{ phones}$

The two sounds are perceived at the same level.

Calculation of the corresponding loudnesses :

$$N = 2^{(L_N - 40)/10}$$

$$L_N(63\text{Hz}) = 90 \text{ phones} \rightarrow N(63\text{Hz}) = 32 \text{ sones}$$

2. New level :

$$\Delta L = 10 \log\left(\frac{1}{10000}\right) = -40 \text{ dB}$$

$$L'(1000\text{Hz}) = 50 \text{ dB} \rightarrow L'_N(1000\text{Hz}) = 50 \text{ phones}$$

$$L'(63\text{Hz}) = 60 \text{ dB} \rightarrow L'_N(63\text{Hz}) = 40 \text{ phones}$$

1000 Hz is perceived louder than 63 Hz.

Calculation of the new loudnesses :

$$L'_N(1000\text{Hz}) = 50 \text{ phones} \rightarrow N'(1000\text{Hz}) = 2 \text{ sones}$$

$$L'_N(63\text{Hz}) = 40 \text{ phones} \rightarrow N'(63\text{Hz}) = 1 \text{ sones}$$

1000 Hz is perceived 2 times louder than 63 Hz.

Exercise 4.

An average level of $L_{limit,A} = 93 \text{ dB(A)}$ during one hour (3'600 s) corresponds to the noise dose : $d_{limit} = p_A^2 \cdot \Delta t = (20 \cdot 10^{-6})^2 10^{L_{limit,A}/10} \cdot 3600 = 2'873,2 \text{ Pa}^2 \cdot \text{s}$.

If the DJ already had 30 minutes with 97 dB(A), the corresponding noise dose is : $d = (20 \cdot 10^{-6})^2 10^{97/10} \cdot 1800 = 3'608,5 \text{ Pa}^2 \cdot \text{s}$. The limit value is then already exceeded.

Exercise 5.

In one hour we have 450 times 5 sec with level 65 dB(A) + 50 times 5 seconds with level 75 dB(A). The remaining of the hour is considered silent (or at least sufficiently lower than 65 dB(A)).

The equivalent level $L_{eq,1h}$ corresponding to a measurement duration of 1 hour is then :

$$L_{eq,1h} = 10 \log_{10} \frac{1}{3600} \left(450 \times 5 \times 10^{65/10} + 50 \times 5 \times 10^{75/10} \right) = 66,2 \text{ dB(A)}$$

Exercise 6.

The displayed value for a given integration time T can be derived as :

$$L_{display} = 10 \log_{10} \left(\frac{1}{T} \int_{t=0}^T \frac{\hat{p}^2}{p_0^2} dt \right).$$

FAST setting : $T = 125 \text{ ms}$

⇒ Display : for signal durations of 1 s and 500 ms, $L_{display} = 100 \text{ dB(A)}$

for signal durations of 100 ms, $L_{display} = 99 \text{ dB(A)}$

for signal durations of 50 ms, $L_{display} = 96 \text{ dB(A)}$

SLOW setting : $T = 1 \text{ s}$

⇒ Display : for signal durations of 1 s = 100 dB(A)

for signal durations of 500 ms, $L_{display} = 97 \text{ dB(A)}$

for signal durations of 100 ms, $L_{display} = 90 \text{ dB(A)}$

for signal durations of 50 ms, $L_{display} = 87 \text{ dB(A)}$

