

# Lecture 4

## Embedded system design

### Timing closure

CS476 - ESD  
March 11, 2024

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Clock Trees

Timing closure

Fine-grain paralyzing

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Multi-cycling

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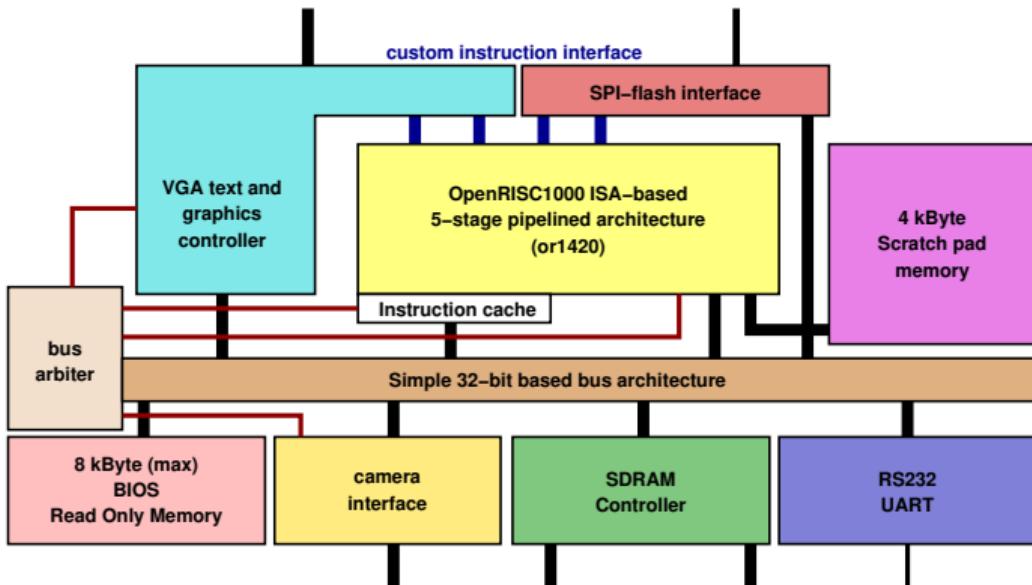
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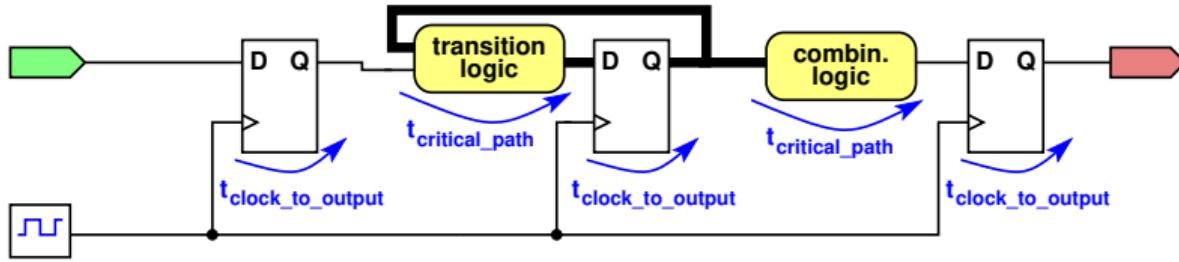
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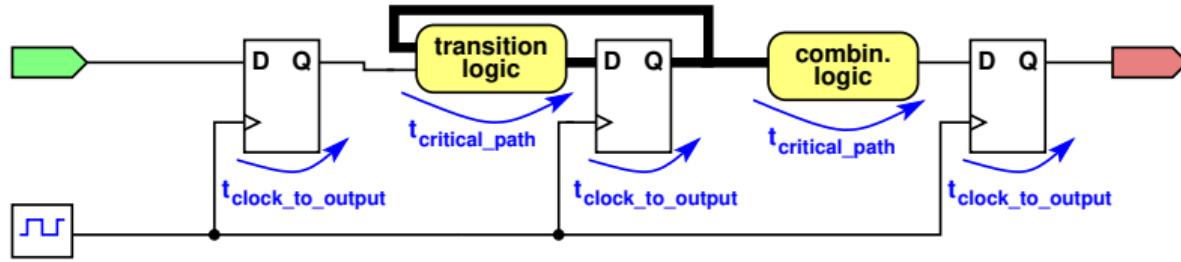
- Once we finished our architectural choices, we have to get the system running at the required frequency.
- We have to go into a phase which is called *timing closure*.
- To fully understand the timing closure we have first to go into some details of the final ASIC to be able to understand what is going on.

## Remember: RTL design



- ▶ All our designs we design synchronously using the Register Transfer Level (RTL) methodology.
- ▶ Hence all our circuits look like the simplified circuit above, where all flipflops are connected to the same clock source (throughout our chip).

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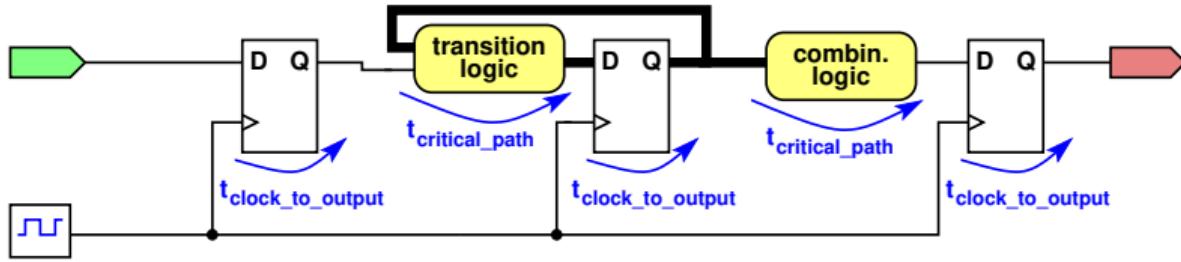
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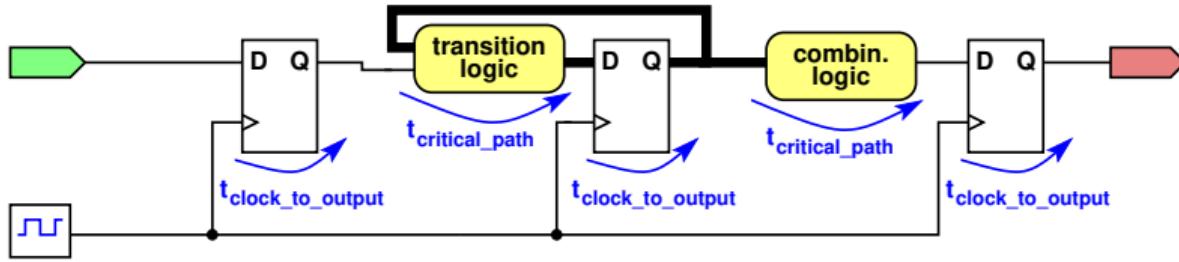
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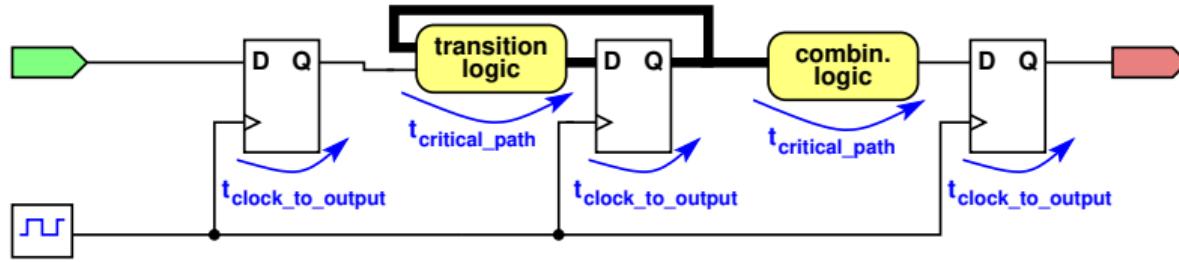
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## Remember: RTL design

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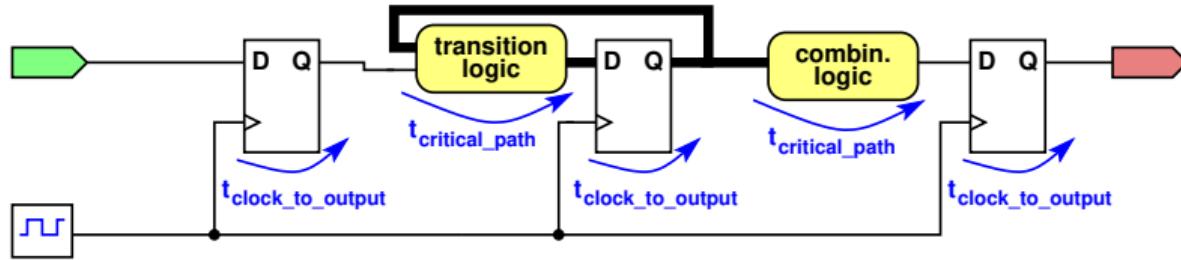
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- ▶ The longest combinational path hence represents the critical path.
- ▶ The one thing that we did not consider yet is the question: *What happens with the clock line?*
- ▶ Just putting a wire over the whole chip probably will not work as:
  1. The clock line would have a big capacitive load.
  2. The RTL-design method assumes that the rising edge of the clock arrives at all flipflops at the same time.

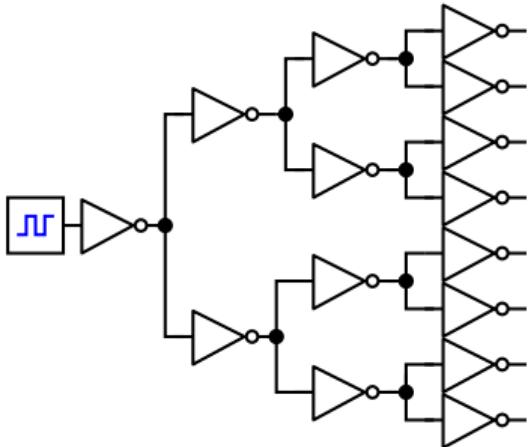
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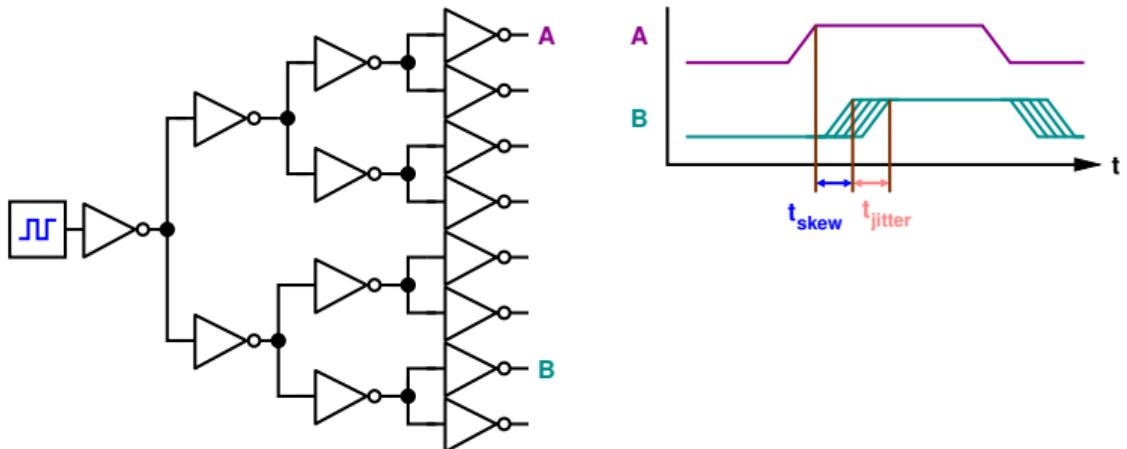
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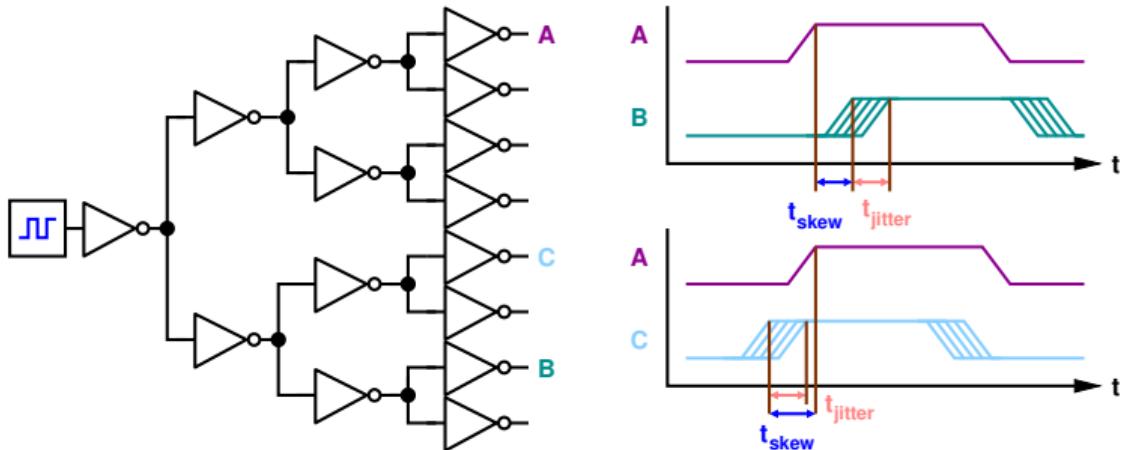
- ▶ Let's look into the first point: reducing the big capacitive load:
- ▶ Using a binary tree of inverters will reduce the load on each output, however, what is the result of this operation?

# Avoiding big capacitive load



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- ▶ Using a binary tree of inverters will reduce the load on each output, however, what is the result of this operation?
- ▶ We will introduce at the flipflop levels a clock-skew due to the fact that not all inverters have the same delay and line-length-mismatches.
- ▶ We also will have a jitter.

# Avoiding big capacitive load



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- We also will have a jitter.
- Note that we can also have a negative skew that reduces the influence of the jitter.

# Reducing jitter and skew

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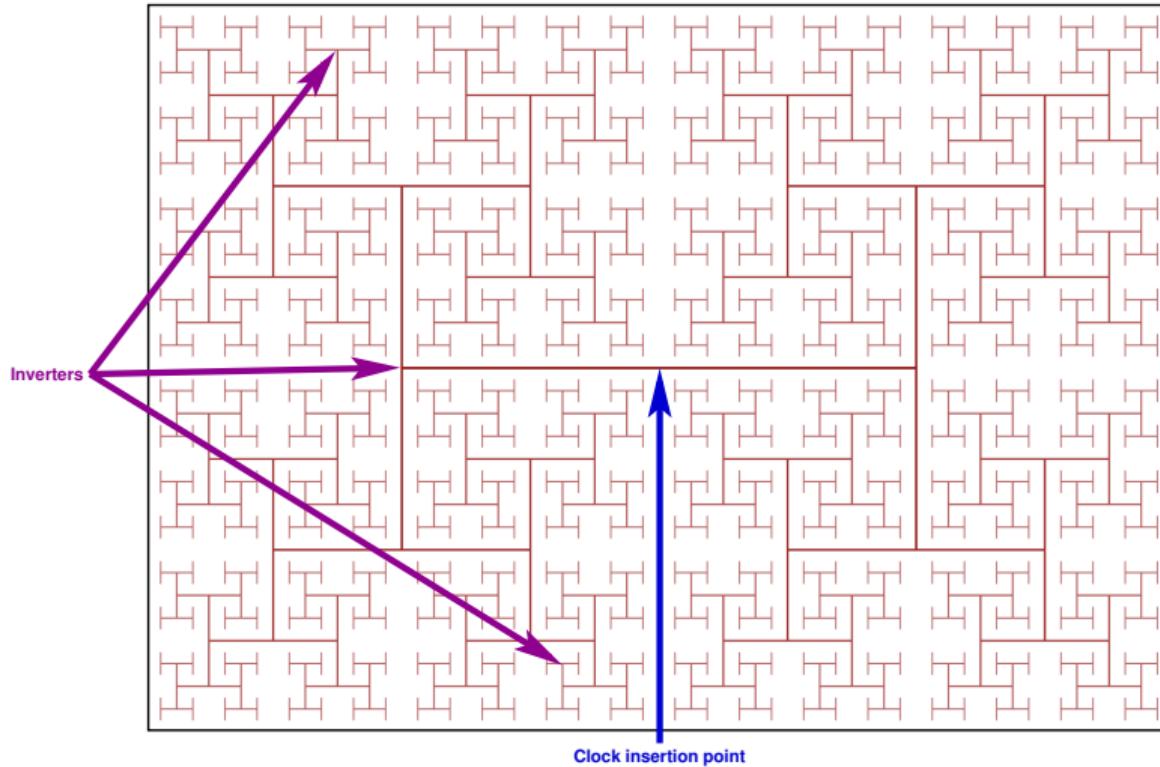
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- One of the methods is to make a *clock tree* in form of a H-tree.
- However, we still have a clock-uncertainty of approx.  $2 \cdot t_{\text{skew}} + t_{\text{jitter}}$ .

## Remember: Setup and hold

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Clock Trees

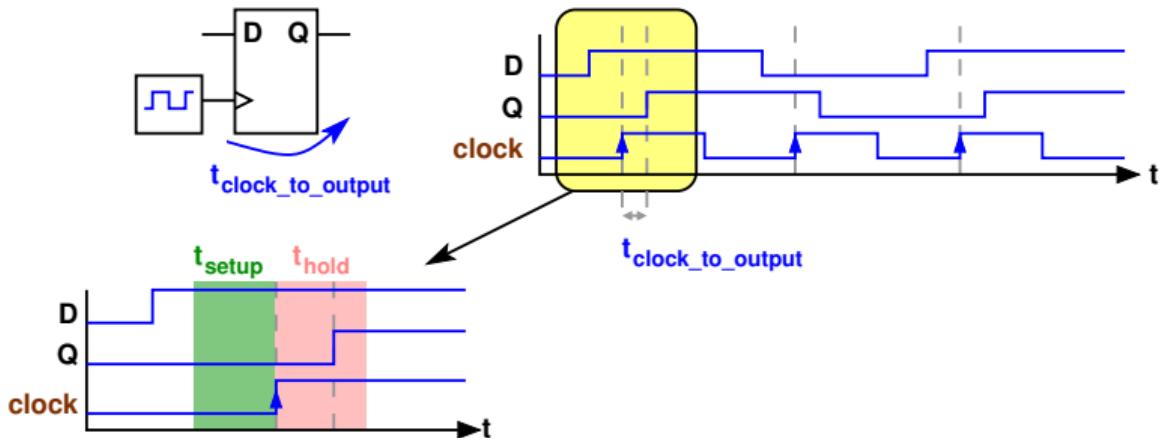
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- ▶ Remember: a real flip flop has a setup and hold time in which the D-input needs to be kept stable (otherwise the flip flop goes into meta stable state).

## Remember: Setup and hold

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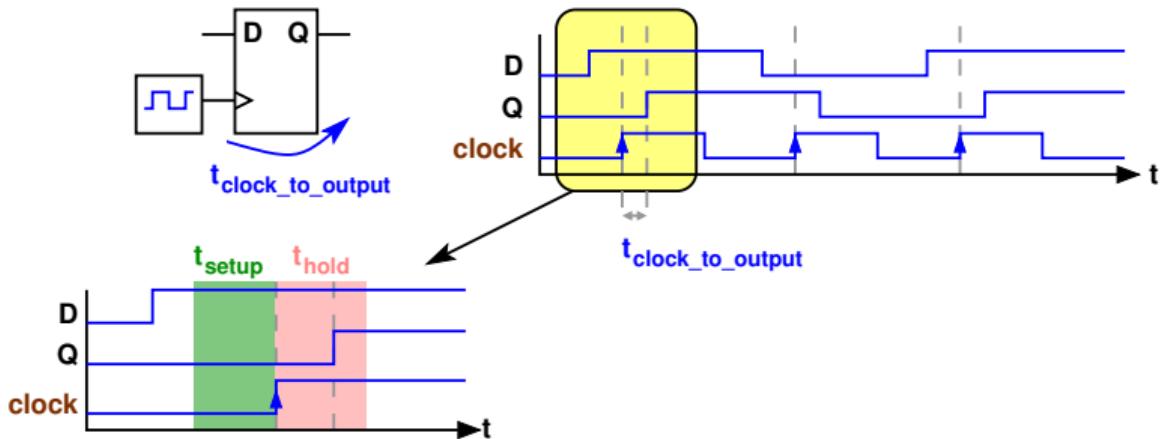
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- ▶ Remember: a real flipflop has a setup and hold time in which the D-input needs to be kept stable (otherwise the flipflop goes into meta stable state).
- ▶ So which kind of situation we now can have in the real-world taking into account the *clock tree*:
  1. The path is too fast (race-condition).
  2. The path is too slow (frequency cannot be met).

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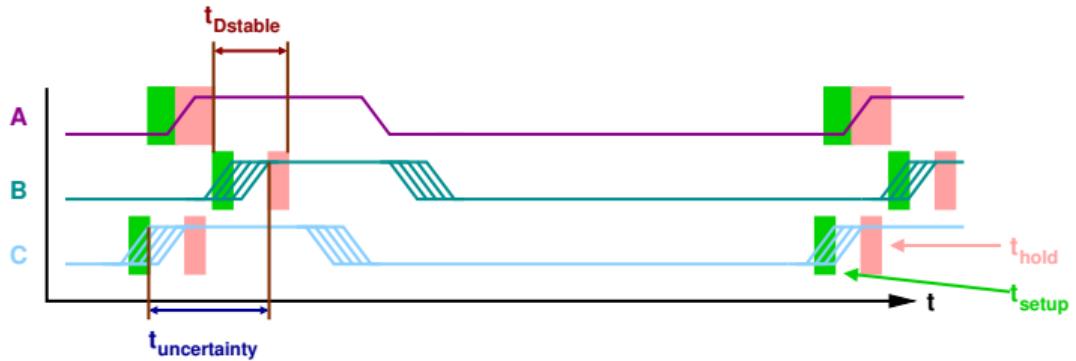
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- ▶ Putting it all together gives us the above timing diagram.

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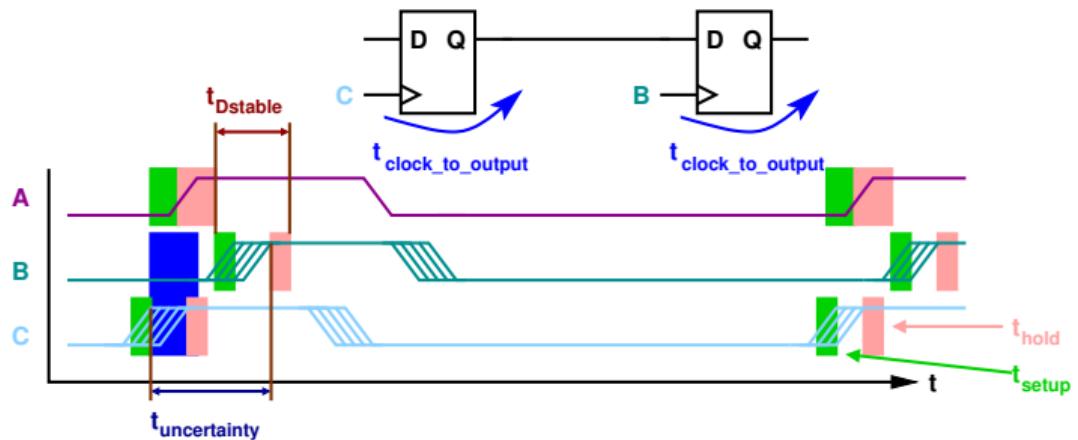
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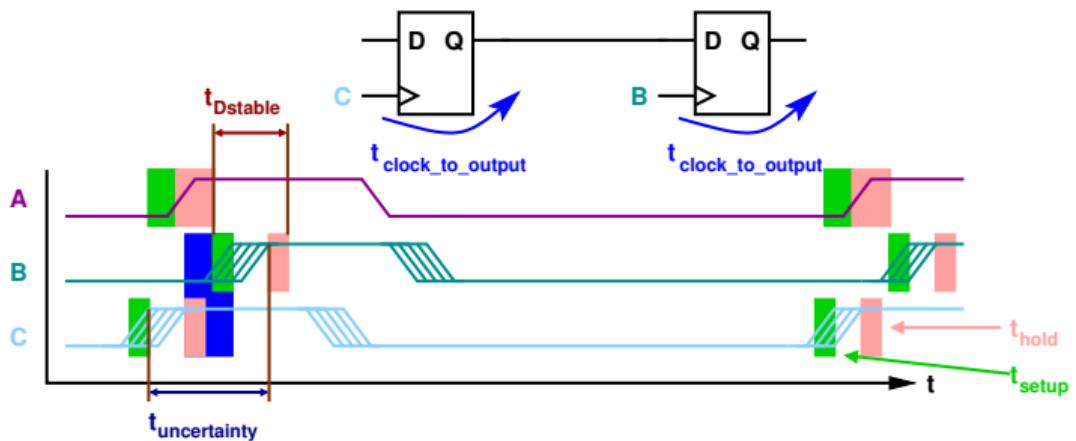
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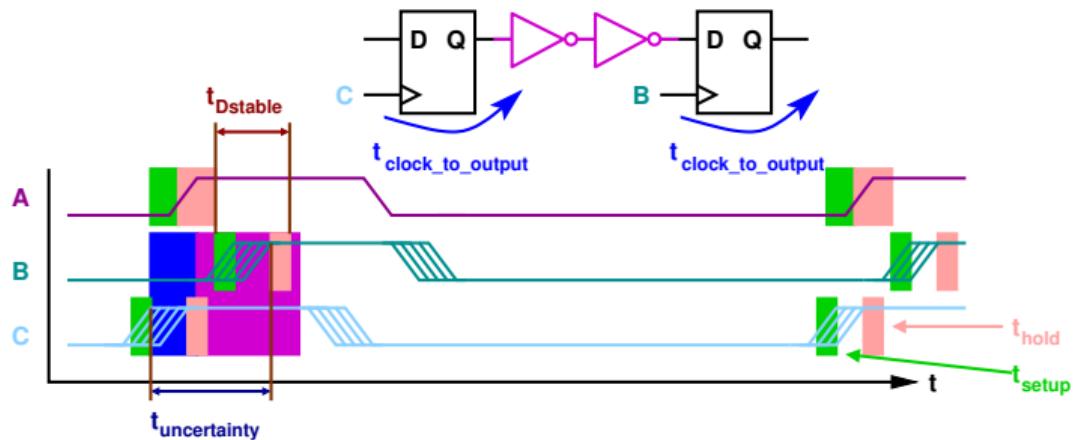
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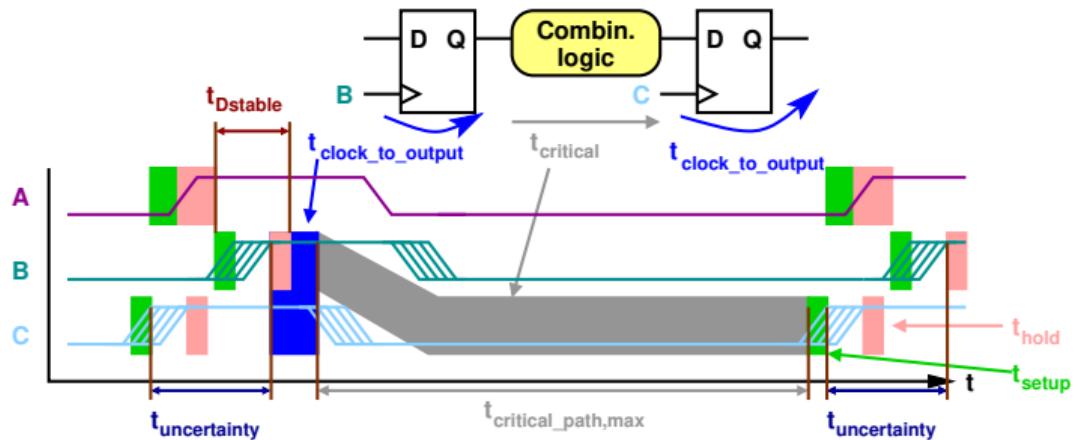
- ▶ Putting it all together gives us the above timing diagram.
- ▶ Let's take as example a shift-register, there are now two situation that can happen:
  1. The output of flipflop C changes before the setup-time of flipflop B, hence we have a functional error as the data is too early available!



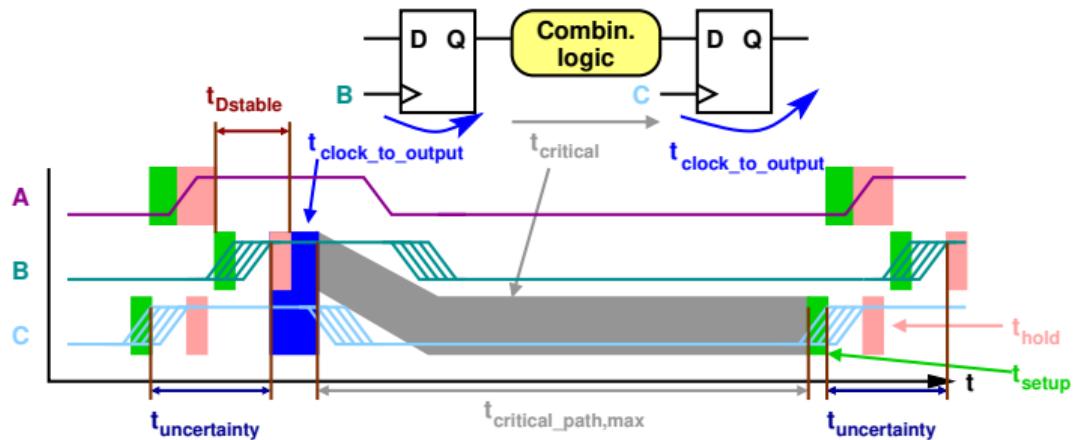
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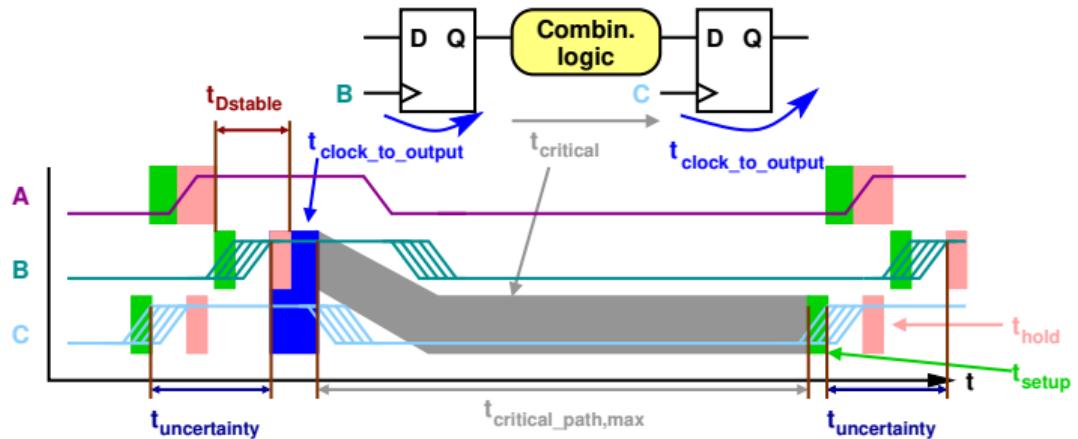
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- ▶ This problem can be solved by inserting a delay between the flipflops C and B. Fortunately this is done for us by the synthesis and/or P&R-tools.



- The other situation is shown above (hence  $t_{p,clock} = t_{clock\_to\_output} + t_{critical,max} + t_{setup} + t_{uncertainty}$ ).
- We know that during the critical path time we may have hazards on the D-input of flipflop C, and that the correct value is available after  $t_{critical\_path}$ .



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- Timing is not met when there exists at least one combinational logic path with a  $t_{critical\_path} > t_{critical\_path,max}$ .

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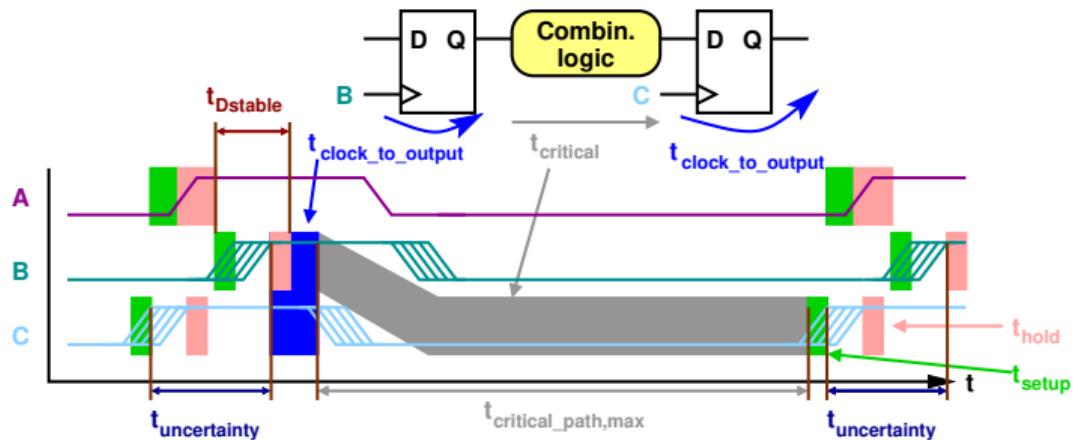
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- *Timing closure* is the process of getting all  $t_{critical\_paths} < t_{critical\_path,max}$ .

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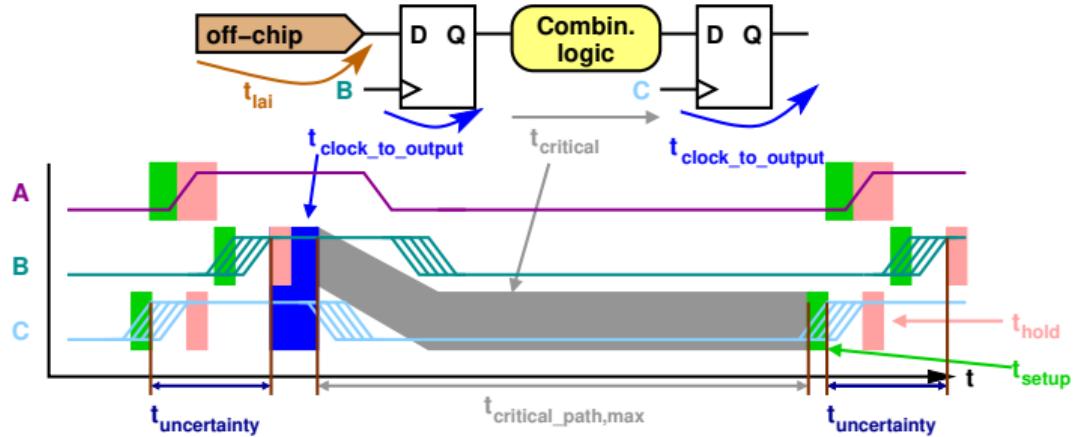
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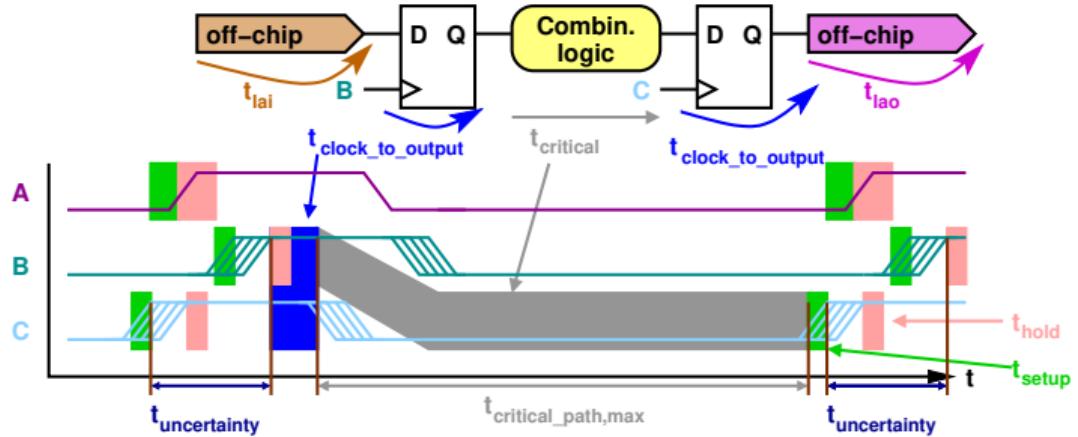
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- ▶ *Timing closure* is the process of getting all  $t_{critical\_paths} < t_{critical\_path,max}$ .
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  1. The latest arrival of an external input signal ( $t_{lai}$ ) to the flipflop with respect to the positive clock edge.



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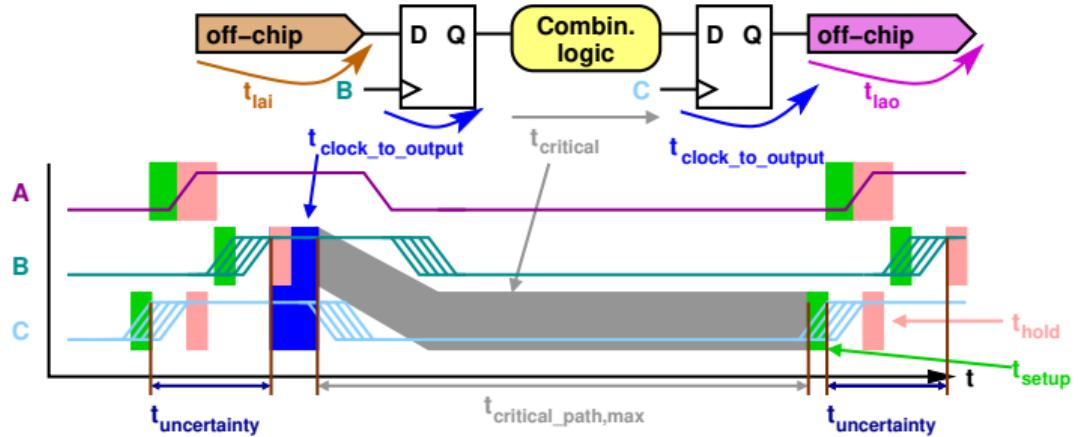
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- ▶ These two numbers depend on the chips connected to this one and are in general more difficult to determine.

# Timing closure off-chip

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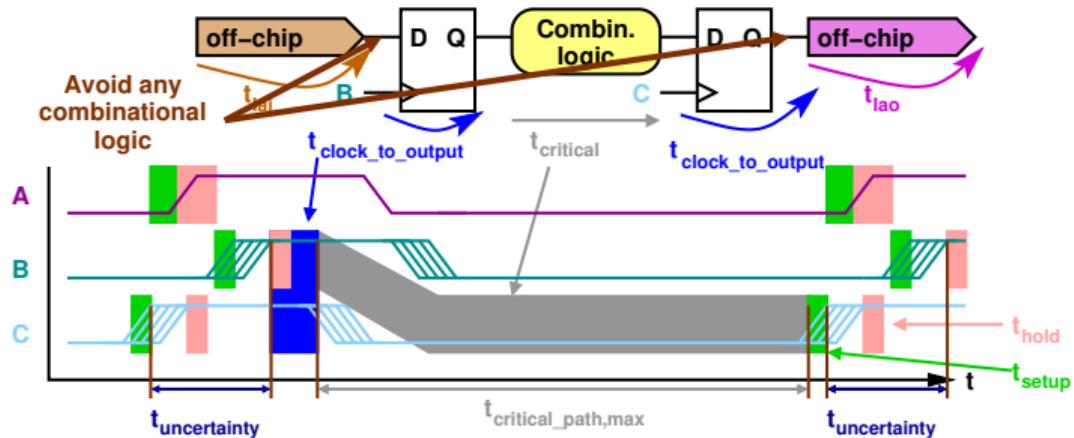
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- The later aspect is “easily” solved by not using any combinational logic between the input(s) and the first flipflop(s) and no combinational logic between the last flipflop(s) and the output(s).
- This has the advantage that you do not have any hazards outside of your chip (good thing!).

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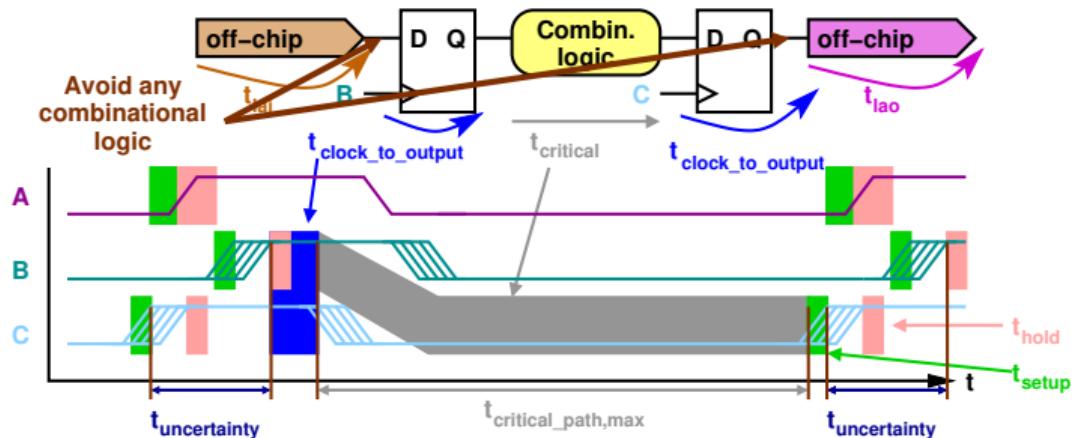
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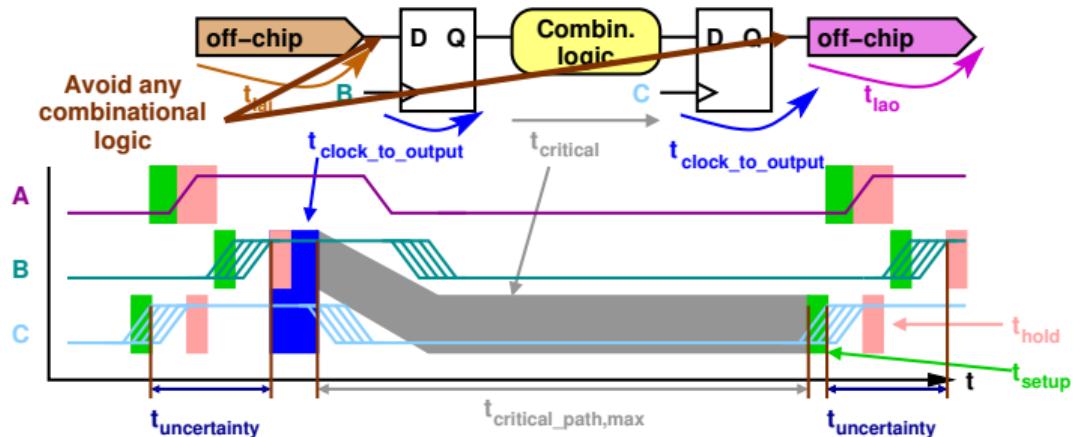
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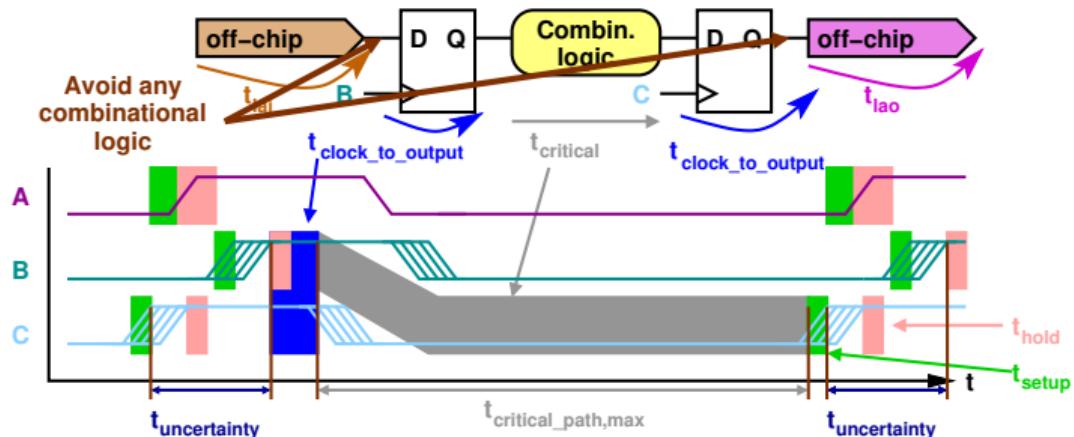
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  2. Adding extra delays in some of the outputs to meet external timings.
- Note: even your internal delays due to the clock-tree may impose problems.....

# Timing closure on-chip

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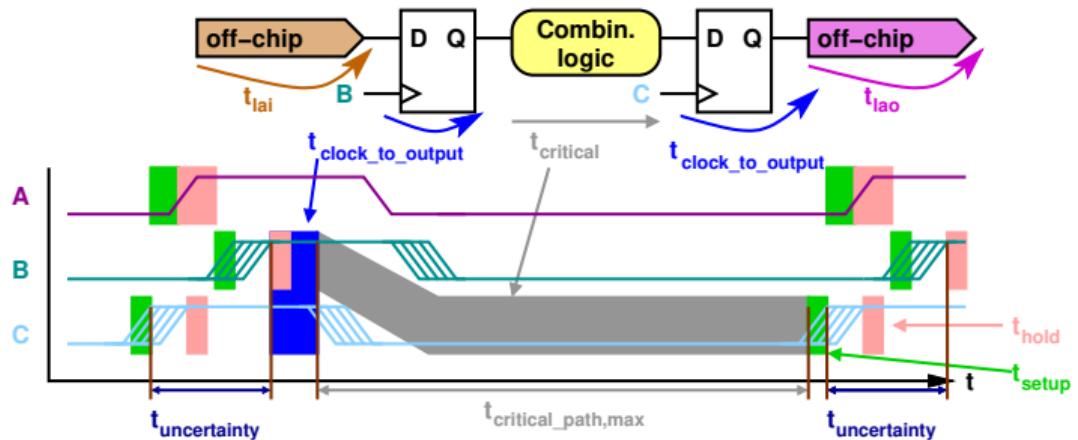
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- ▶ The on-chip aspect has some methods that you can use, but be aware, the synthesis tool might be more “intelligent” than you are (compare the compiler for a programming language).
- ▶ These methods are more for things that the synthesizer does not know about (for example what does your program do):
  - ▶ Fined-grain paralyzing.
  - ▶ Multi-cycling.
  - ▶ Pipelining.

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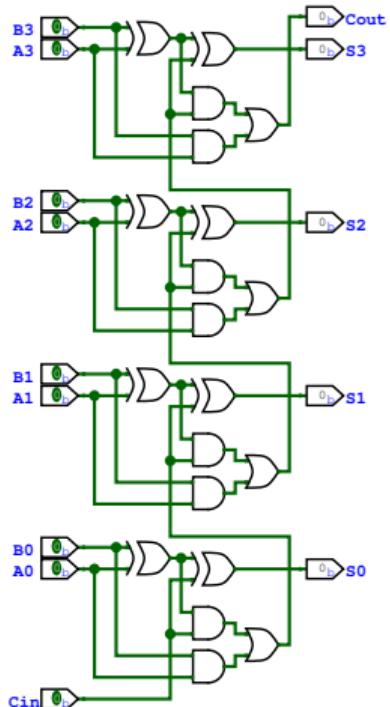
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- ▶ As example we take a 4-bit *carry-ripple adder (CRA)*.
- ▶ Assume that this adder is in the critical path.

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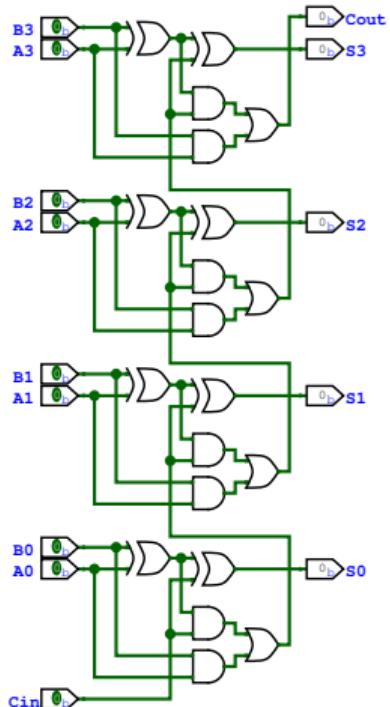
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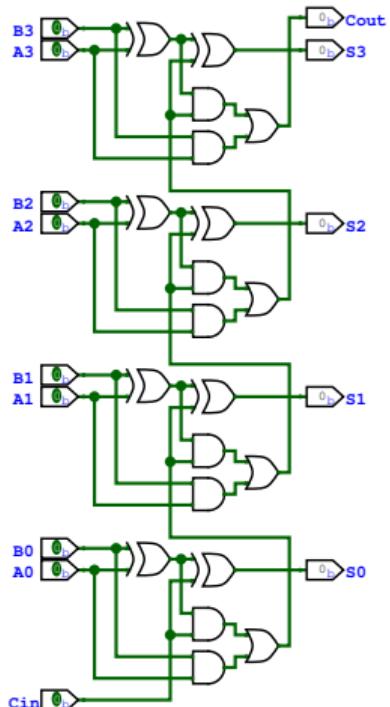
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- ▶ The critical path from this adder goes from Cin through the and- and or-gates up to Cout/S3.
- ▶ So what can we do to speed-up this circuit, there are basically three methods:
  - ▶ Trading-off bigger area/energy consumption against speed.

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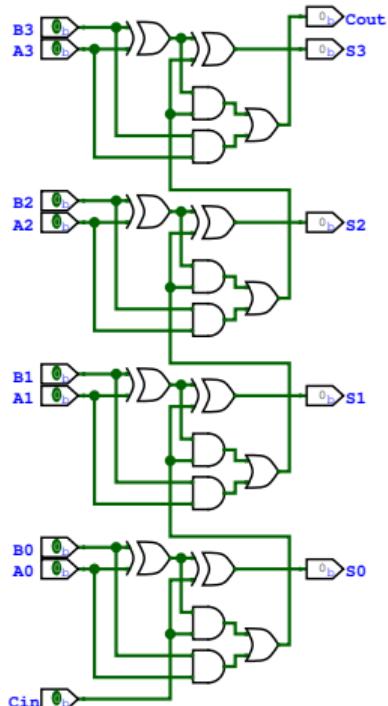
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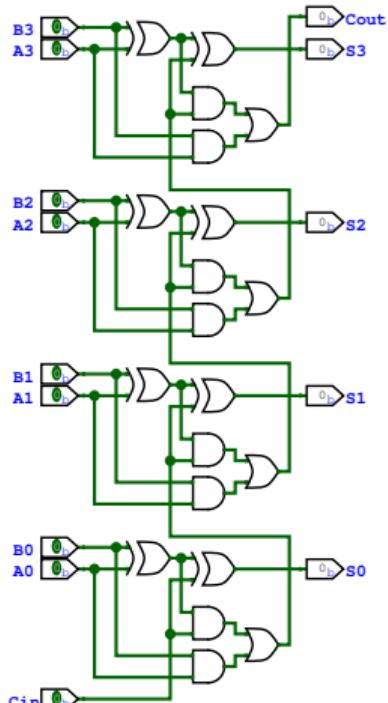
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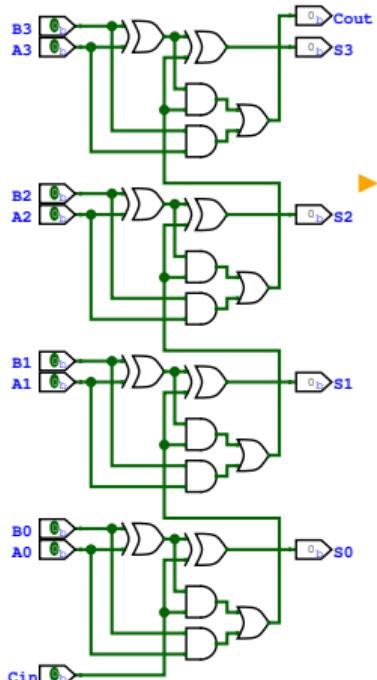
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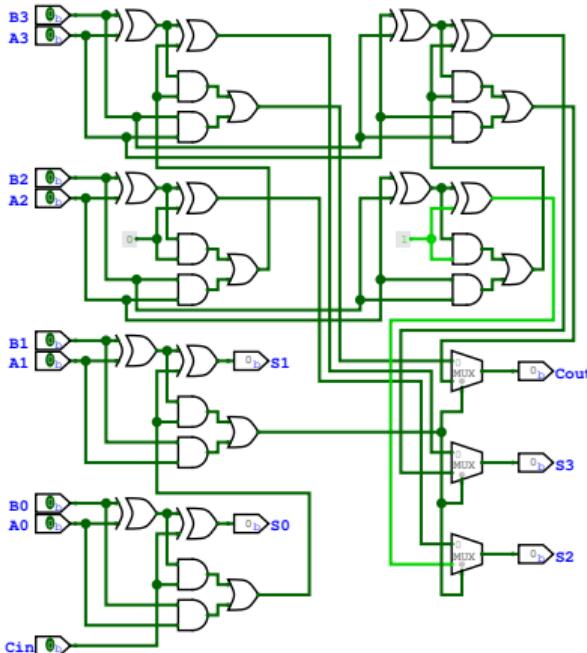


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  - ▶ Trading-off speed against area/energy consumption.
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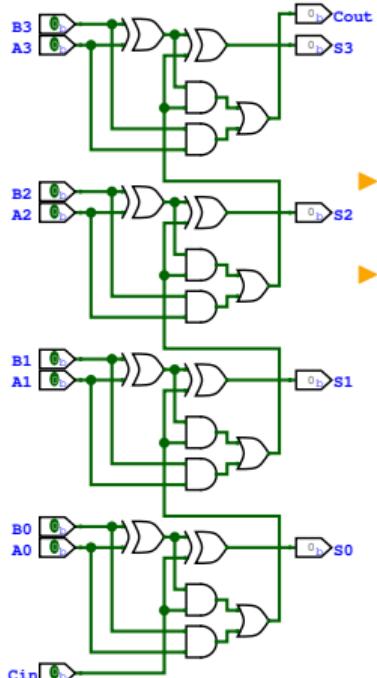
## Finer grain paralyzing



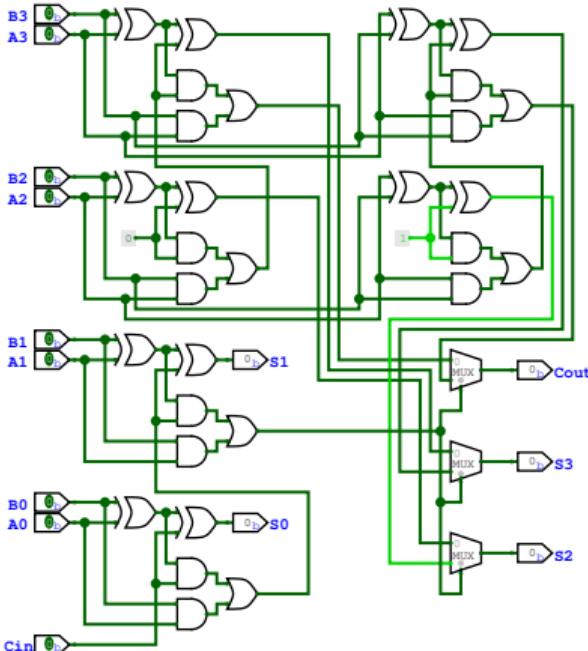
In this method we cut the circuit (critical path) in 2 (or more) parts.



## Finer grain paralyzing



- In this method we cut the circuit (critical path) in 2 (or more) parts.
- The above part is duplicated and calculates the two answers depending the result of the carry.



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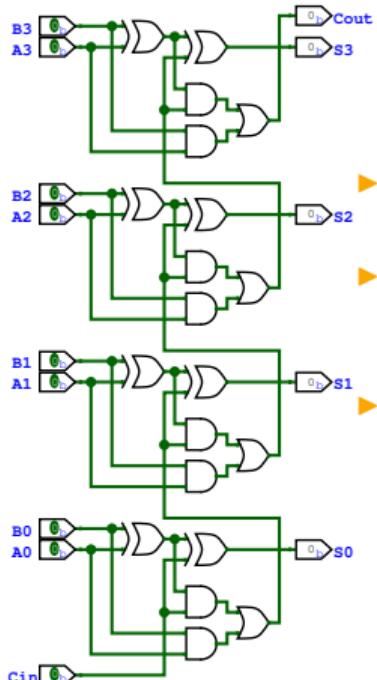
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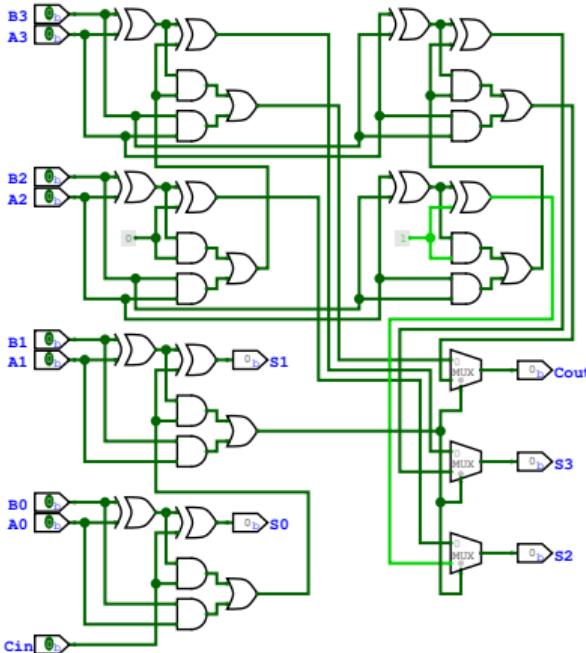
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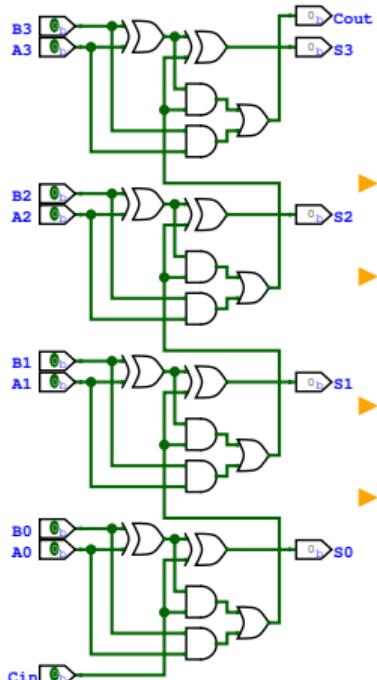
## Finer grain paralyzing



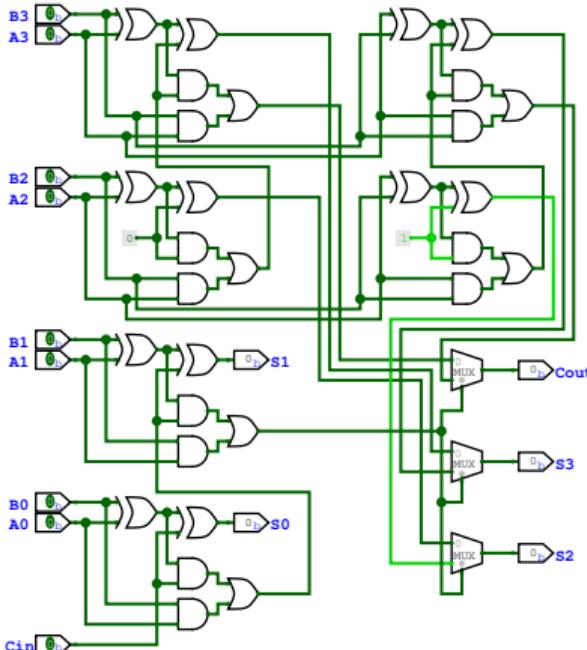
- In this method we cut the circuit (critical path) in 2 (or more) parts.
- The above part is duplicated and calculates the two answers depending the result of the carry.
- Finally the real carry selects the correct result.



## Finer grain paralyzing



- ▶ In this method we cut the circuit (critical path) in 2 (or more) parts.
- ▶ The above part is duplicated and calculates the two answers depending the result of the carry.
- ▶ Finally the real carry selects the correct result.
- ▶ We now have a *carry select adder* (CSA) that is almost twice as fast.



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Timing closure

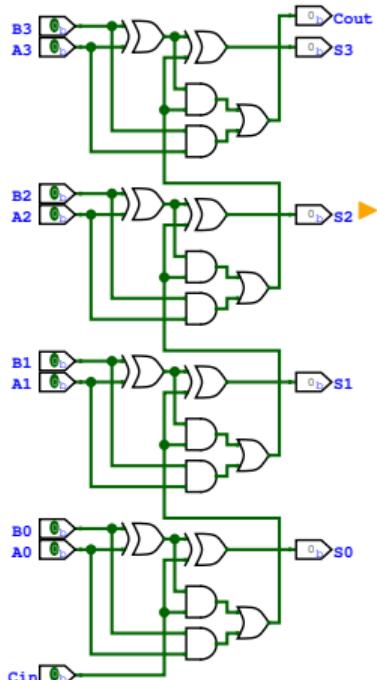
Fined-grain paralyzing

Pipelining

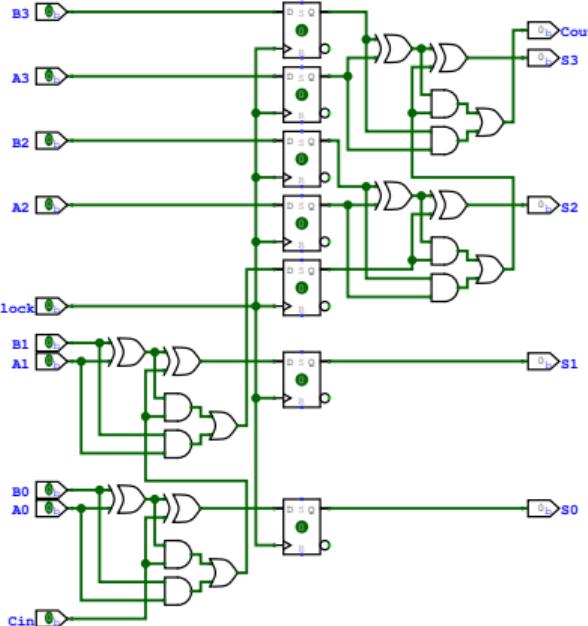
Multi-cycling

Conclusion

# Pipelining



In this method we divide the critical path in 2 (or more) parts and place a row of flipflops between the parts.



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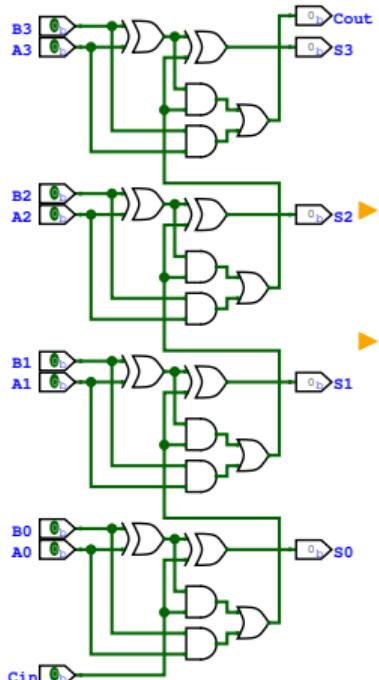
Fined-grain paralyzing

Pipelining

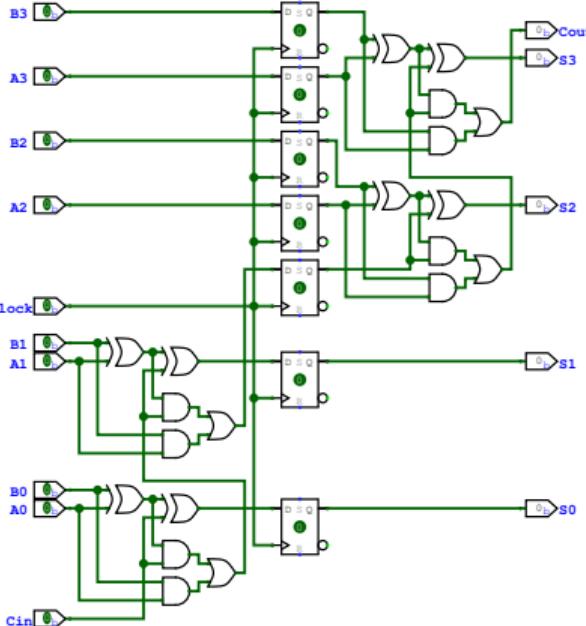
Multi-cycling

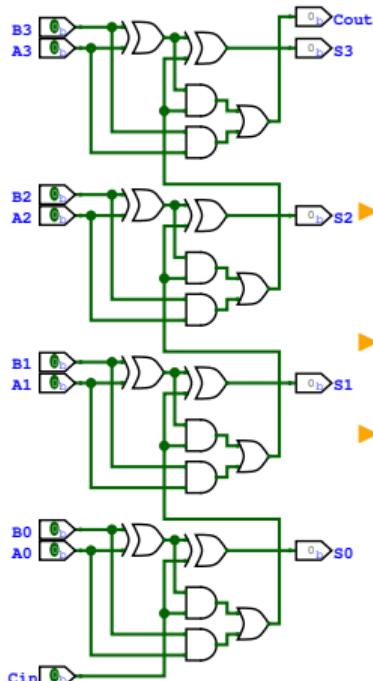
Conclusion

# Pipelining

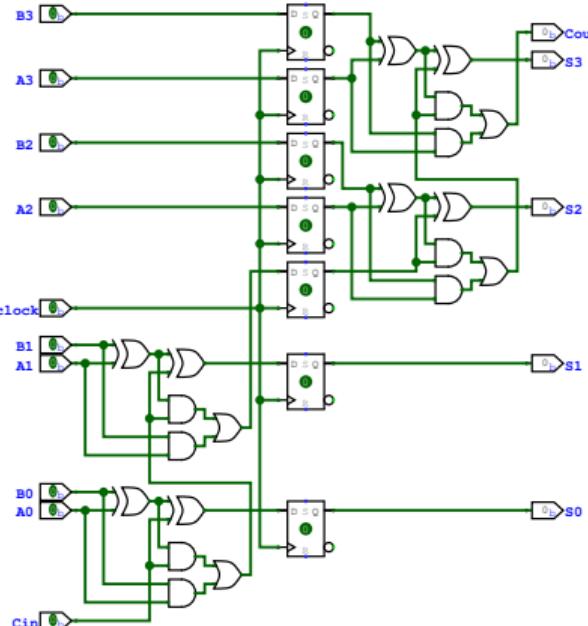


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- The advantage is that we can do a calculation each cycle.





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- The advantage is that we can do a calculation each cycle.
- However, we introduce a latency. This could cause problems in case of a feed-back loop.



# Multi-cycling

Introduction

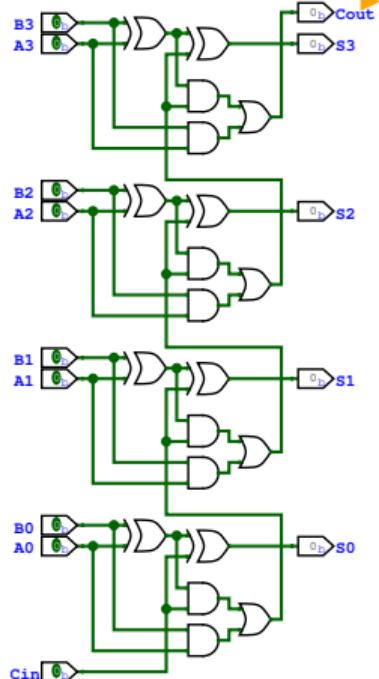
Clock Trees

Timing closure

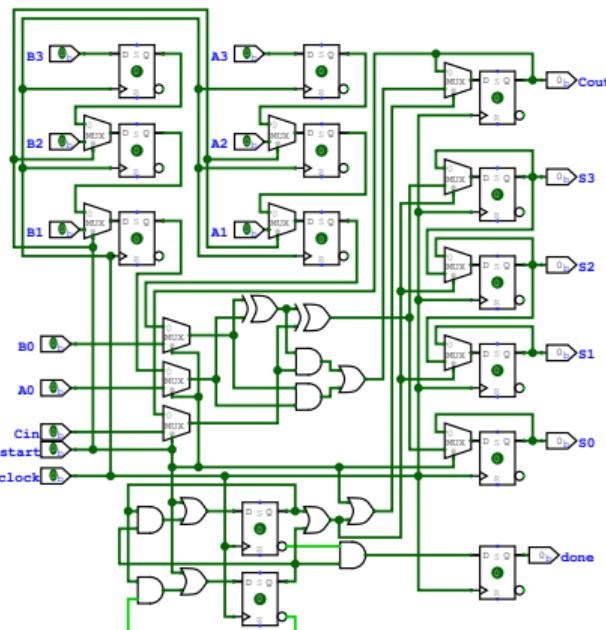
Fined-grain paralyzing  
Pipelining

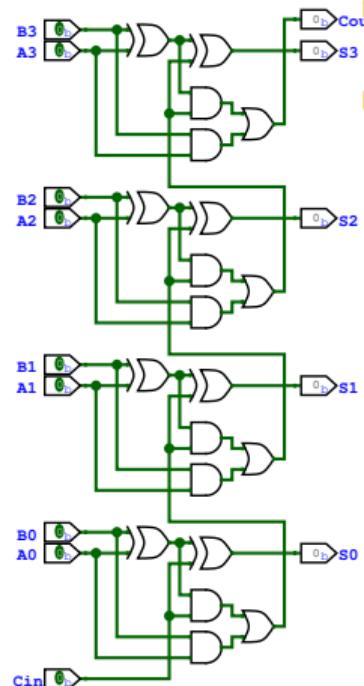
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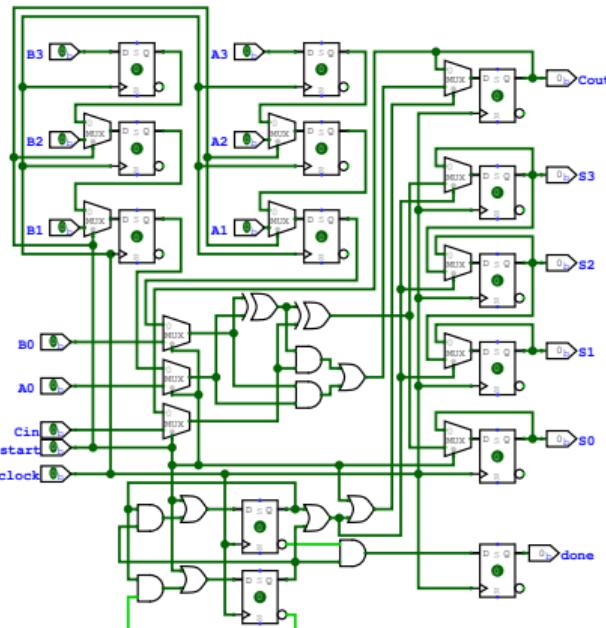
In this method we calculate at each cycle one bit.



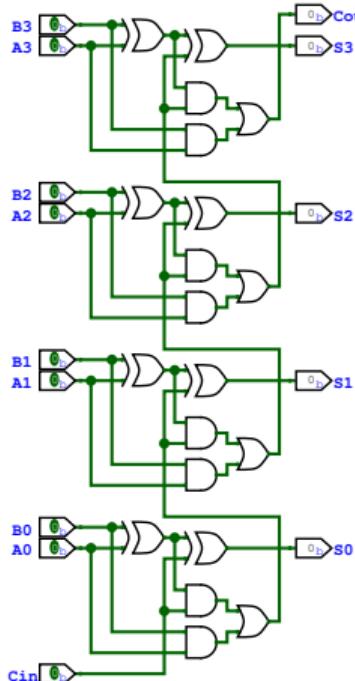


In this method we calculate at each cycle one bit.

Of course this has an impact on the performance, as now the addition takes 4 cycles instead of a single cycle.

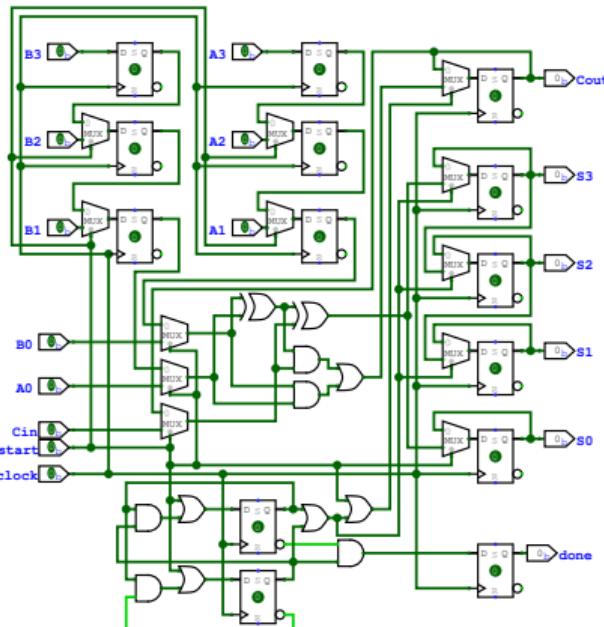


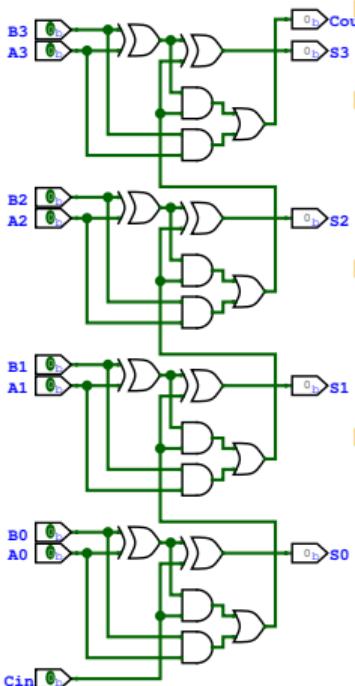
## Multi-cycling



In this method we calculate at each cycle one bit.

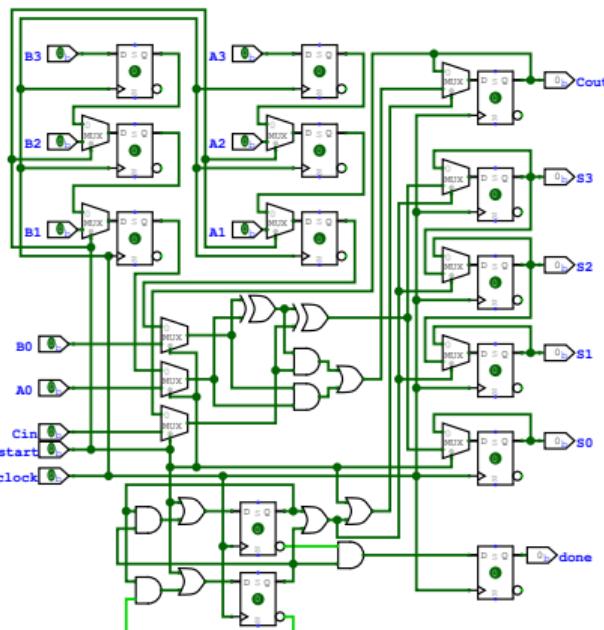
- Of course this has an impact on the performance, as now the addition takes 4 cycles instead of a single cycle.
- But think of the alternative, slowing down all the other functions as we need to reduce the maximum frequency of the CPU.

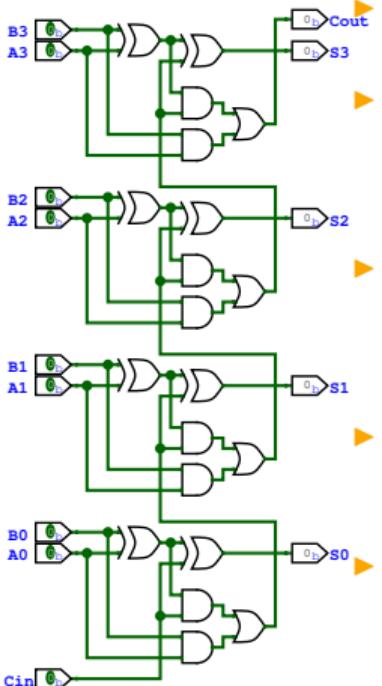




In this method we calculate at each cycle one bit.

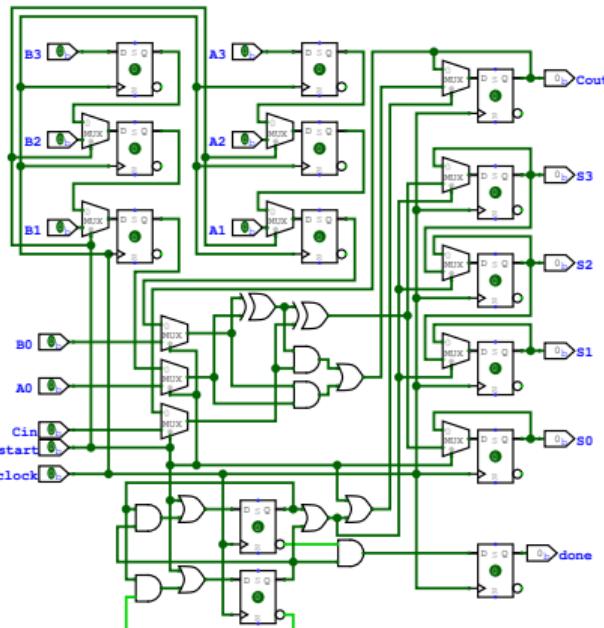
- Of course this has an impact on the performance, as now the addition takes 4 cycles instead of a single cycle.
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- ▶ Very often we perform a *radix-N* multi-cycle operation where at each cycle N-bits are determined.
- ▶ Of course, when A and B are guaranteed to be constant between start and done, we can replace the input shift-registers by a multiplexer.



- We have seen the details that determine the maximum speed with which we can safely operate a circuit.

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- ▶ We have seen the details that determine the maximum speed with which we can safely operate a circuit.
- ▶ We also have visited three methods how to speed-up a critical path.

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- ▶ Each of these methods makes a trade-off between area, energy consumption, complexity and speed.

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- ▶ We have seen the details that determine the maximum speed with which we can safely operate a circuit.
- ▶ We also have visited three methods how to speed-up a critical path.
- ▶ Each of these methods makes a trade-off between area, energy consumption, complexity and speed.
- ▶ It depends on the requirements which of these methods can be applied to a given hot-spot.