

## Solutions to Exercise 8

**Problem 1.**

- Figure 1. Yes. An equivalent serial execution is  $T_2 \cdot T_1$ .
- Figure 2. Yes. An equivalent serial execution is  $T_2 \cdot T_1$ .
- Figure 3. Yes. An equivalent serial execution is  $T_2 \cdot T_1$ .
- Figure 4. No. The execution is not opaque because  $T_3$  observes results of  $T_1$ 's actions even though  $T_1$  is aborted. One way to make it opaque is to have the read operations in  $T_3$  return 0. In this case an equivalent sequential execution is  $T_1 \cdot T_3 \cdot T_2$ .
- Figure 5. No. The execution is not opaque because if  $T_1$  is serialized before  $T_2$ , then  $T_2$  does not observe the write to  $y$ ; and if  $T_2$  is serialized before  $T_1$ , then  $T_1$  does not observe the write to  $x$ . One way to make the execution opaque is to abort one of the transactions. Another is to have read operation in  $T_1$  return 1. In this case an equivalent serial execution is  $T_2 \cdot T_1$ .
- Figure 6. Yes. An equivalent sequential execution is  $T_1 \cdot T_2$ .

**Problem 2.** To implement these objects using transactional memory, we only need to enclose their sequential specification in an atomic block.

Snapshot:

```
uses: array[M]
upon Snapshot do
  begintransaction;
  for i = 1 to M do
    ret[i] ← array[i];
  endtransaction;
  return ret
```

Counter:

```
initially: count = 0
upon Inc do
  begintransaction;
  ret ← count;
  count ← count + 1;
  endtransaction;
  return ret
```

CASN:

```
uses: array[M]
upon CASN(idx, oldv, newv) do
  begintransaction;
  L ← length(idx);
  for i = 1 to L do
    if array[idx[i]] ≠ oldv[i] then
      endtransaction;
      return array
    for i = 1 to L do
      array[idx[i]] ← newv[i]
    endtransaction;
    return array
```