

Computer Graphics

Character Animation I

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Geometric Computing Laboratory

Real-Time Characters



EA FIFA

Offline Characters



<http://www.avatarmovie.com>

Offline Motion Capturing

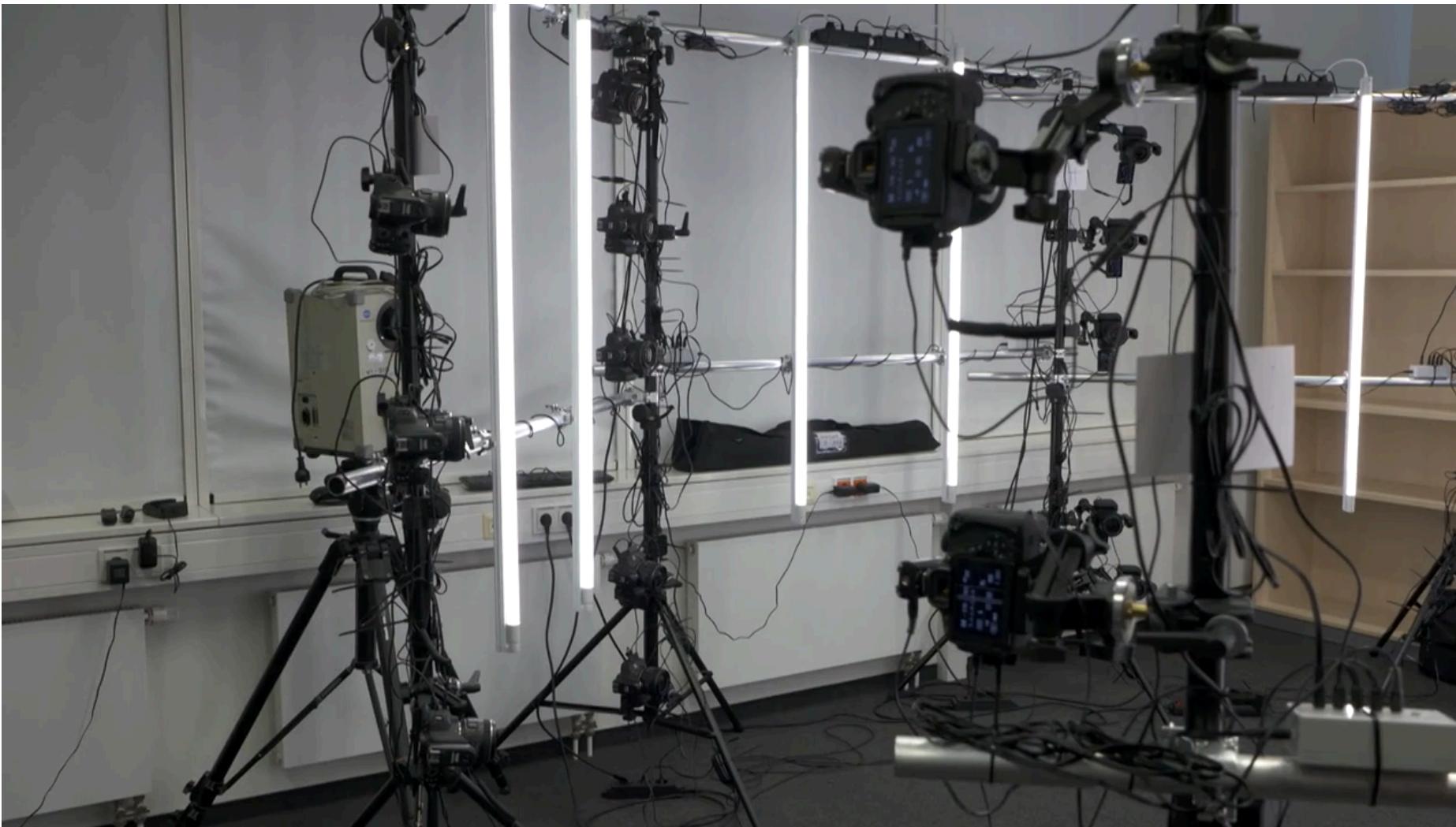


Lord of the Rings, Weta Digital

Real-Time Motion Capturing



Character Scanning

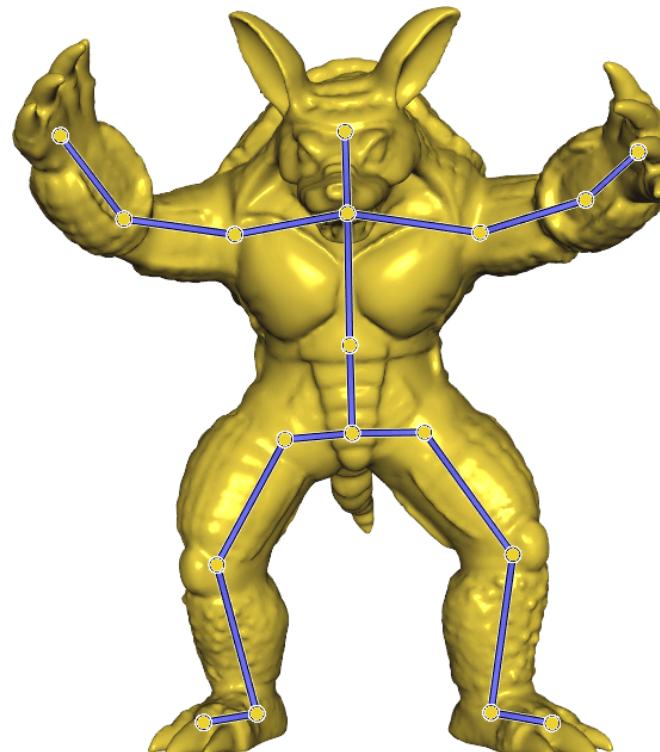


Offline Kicking

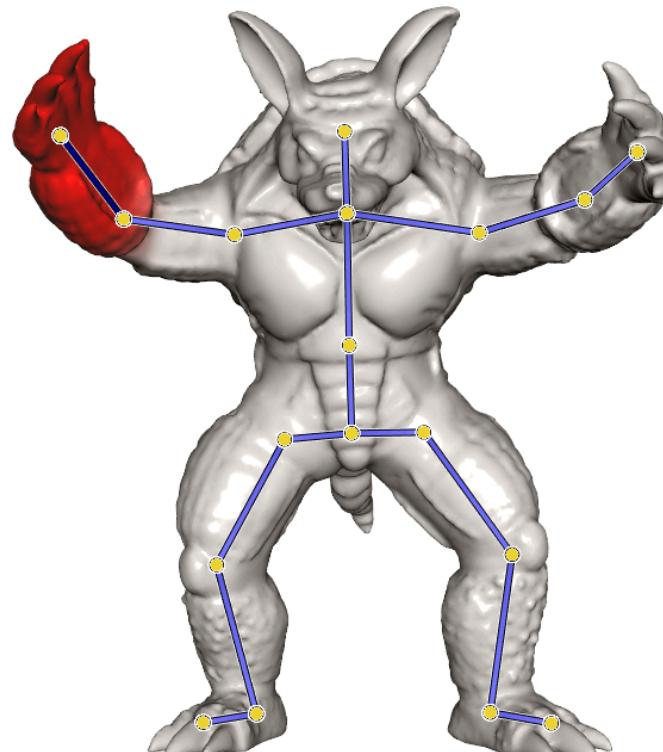


Skeleton-Based Animation

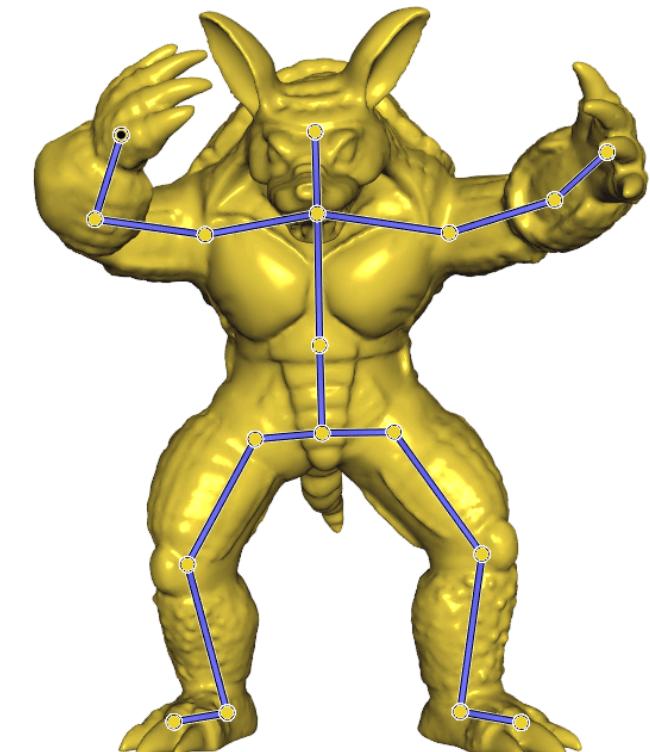
Skeleton-Based Animation



Embed skeleton



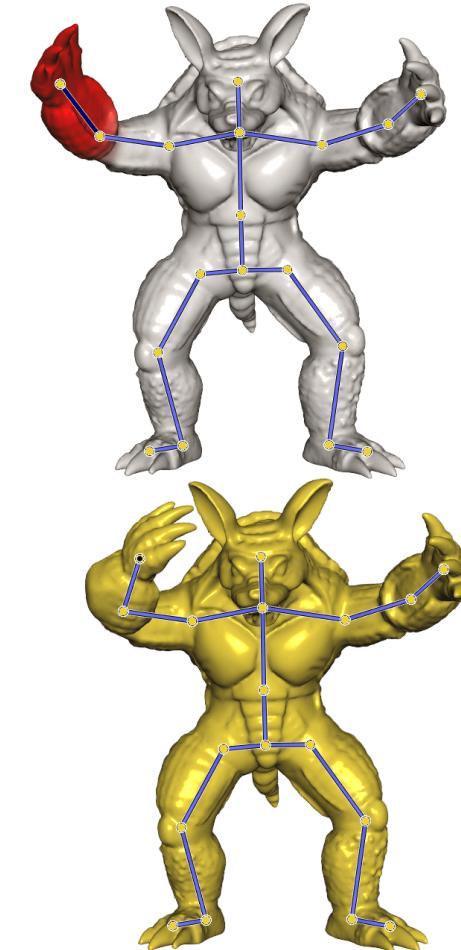
Define bone weights



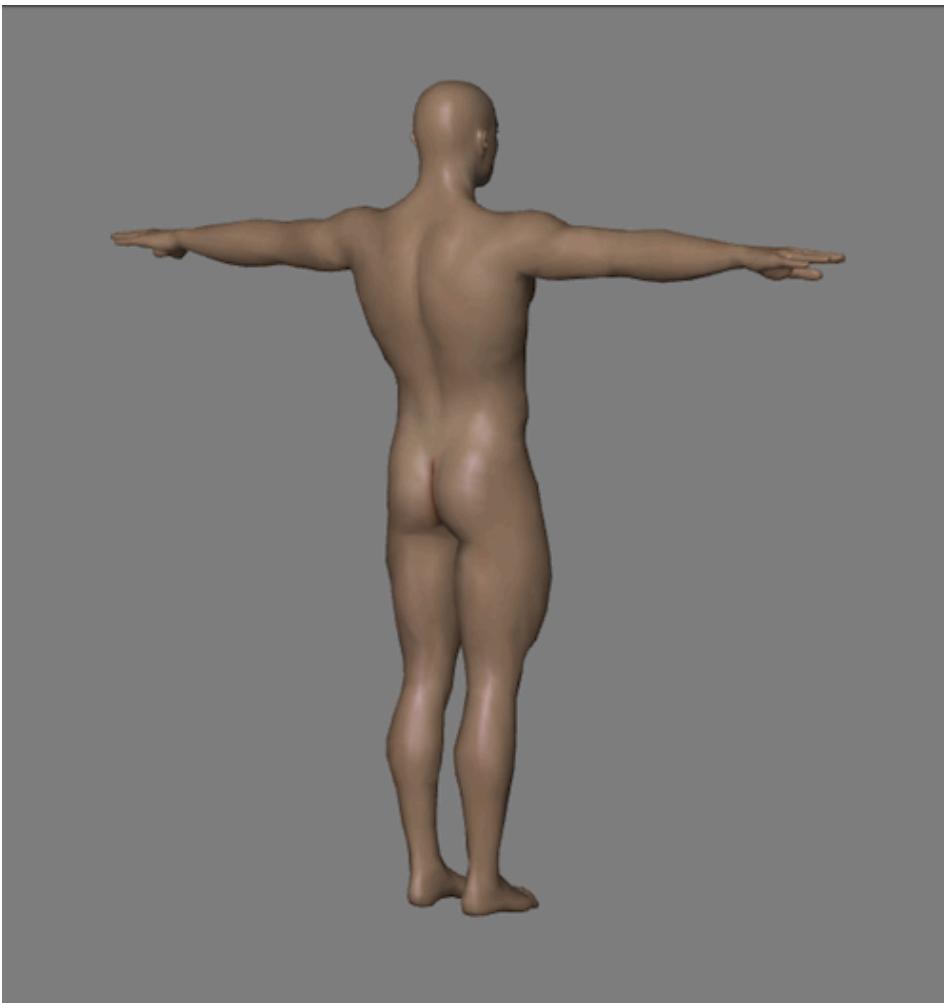
Pose skeleton, deform skin

Skeleton-Based Animation

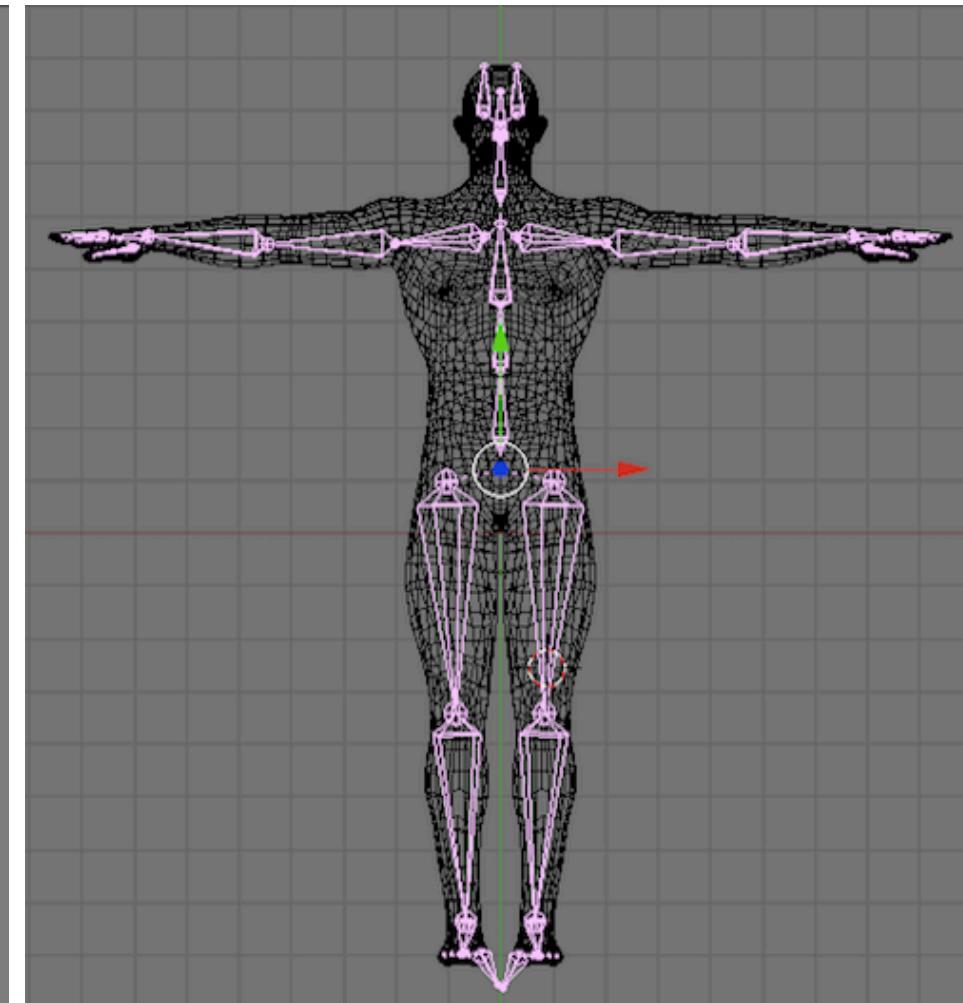
- **Rigging**
 - Embed skeleton
 - Define bone weights
- **Pose skeleton**
 - Forward Kinematics
 - Inverse Kinematics
 - Motion Capture
- **Skinning**
 - Deform skin based on deformed skeleton



Rigging

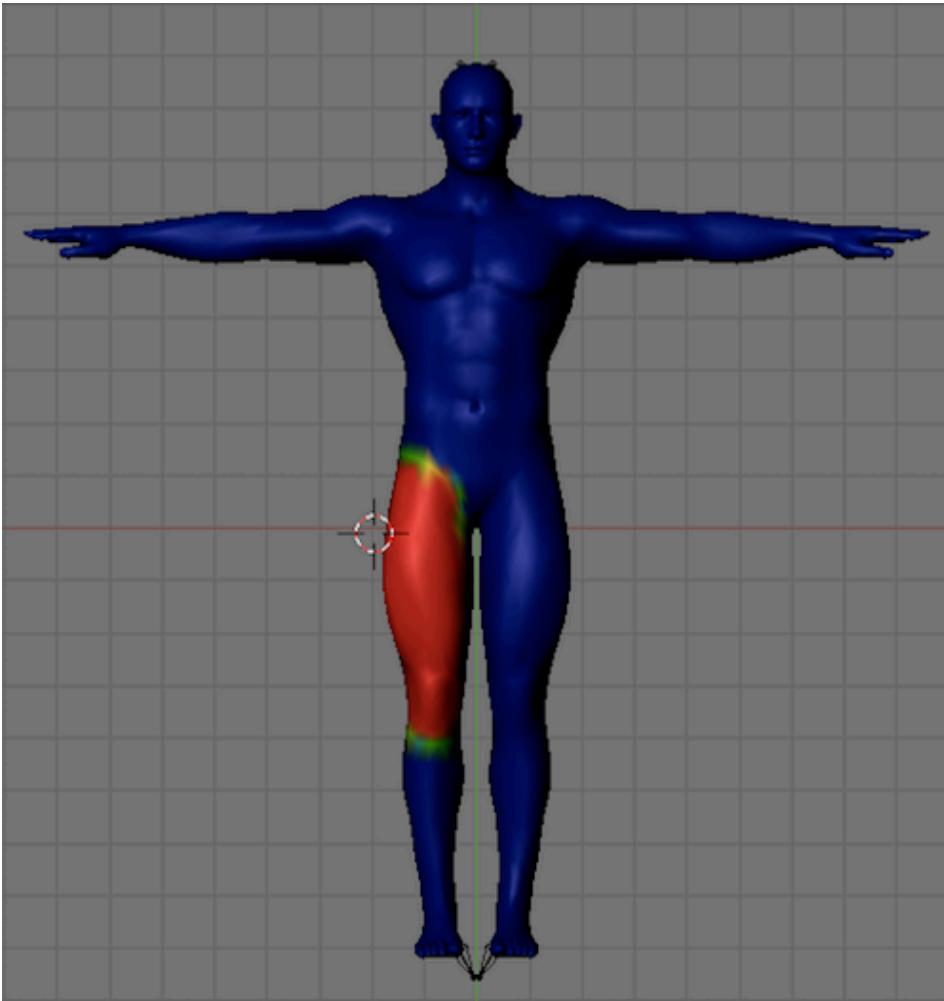


1. Design a character mesh

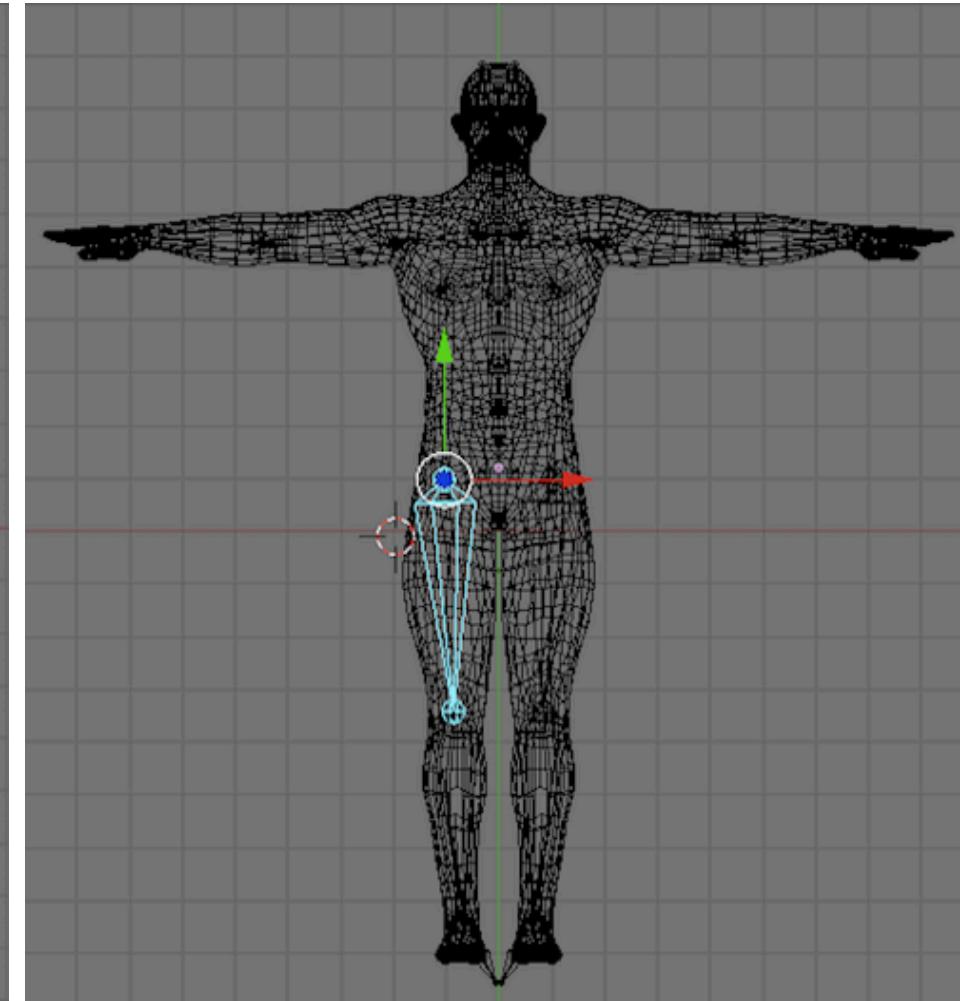


2. Embed a control skeleton

Rigging



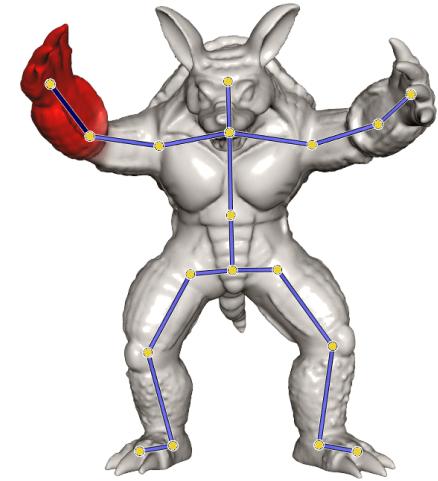
3. Assign mesh vertices...



...to skeleton bones

Rigging

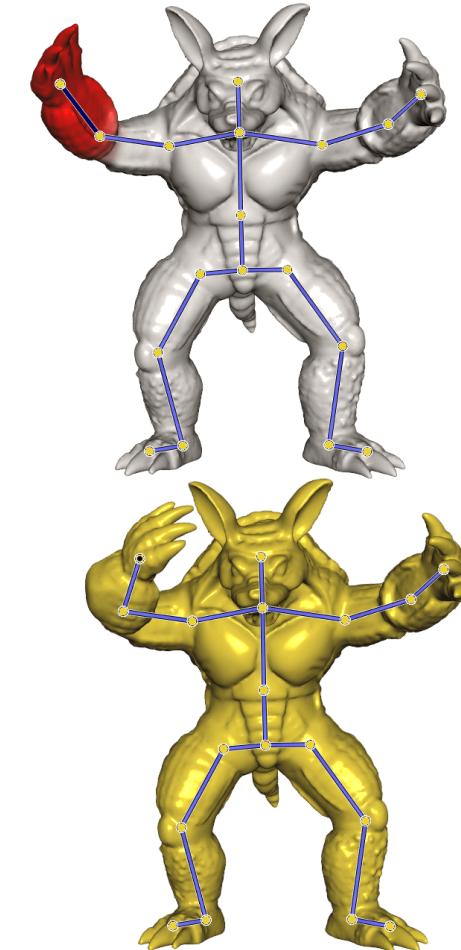
- Skinning weights (bone weights, joint weights)
 - weight $w_{i,j}$ defines the influence of bone j on vertex i
 - Weights must sum up to one: $\sum_j w_{i,j} = 1$
 - Weights should be non-negative: $w_{i,j} \geq 0$
 - Weights build *convex combination* per vertex
- How to compute weights?
 - Bone Heat method [[Baran & Popovic 2007](#)]
 - Bounded Biharmonic Weights [[Jacobson et al 2011](#)]
 - Or paint them manually...



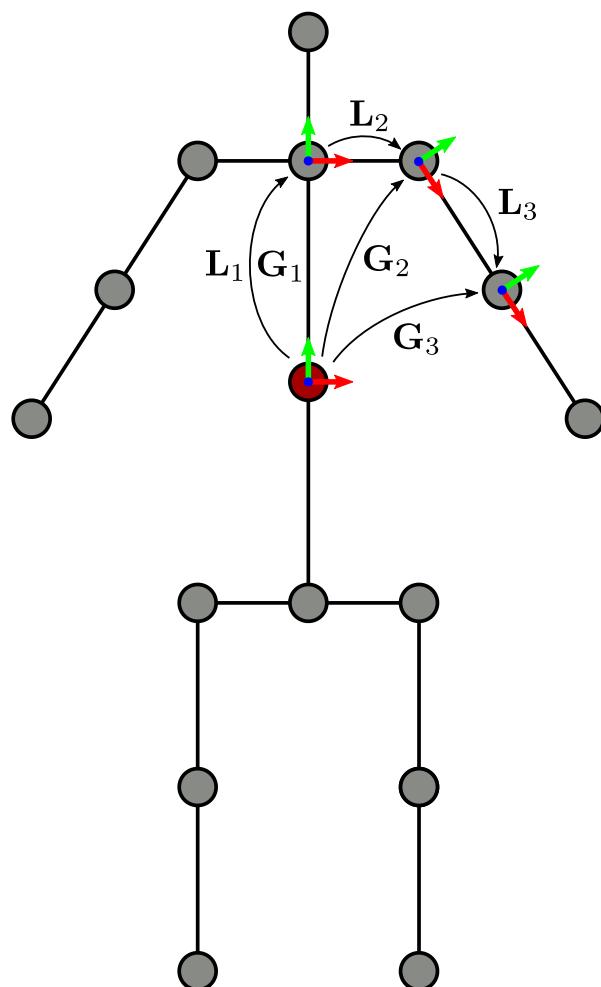
Let's try

Skeleton-Based Animation

- **Rigging**
 - Embed skeleton
 - Define bone weights
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 - Deform skin based on deformed skeleton



Skeleton Forward Kinematics

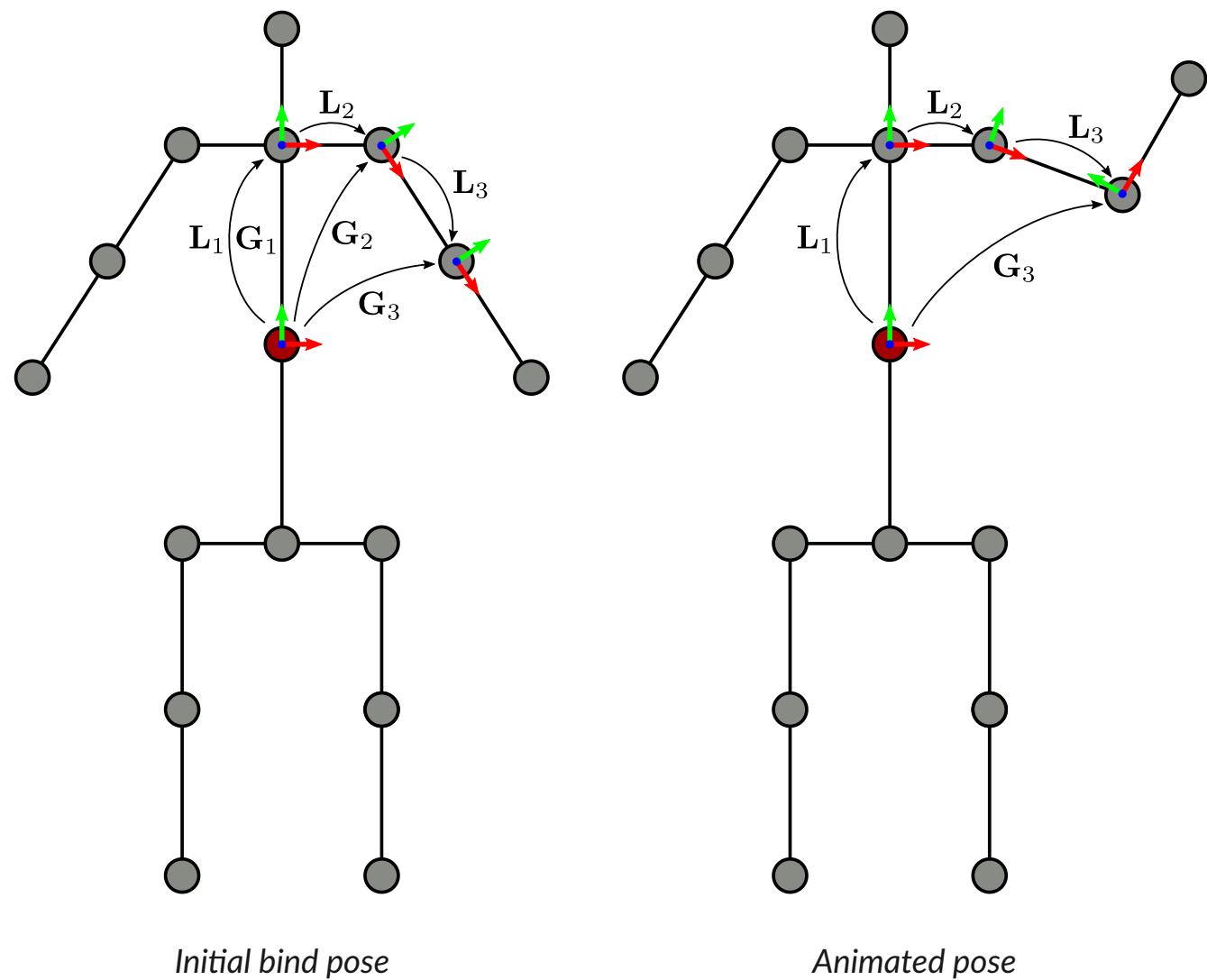


Skeleton hierarchy

- Each joint j has a local coordinate system
- Local matrix \mathbf{L}_j maps from j 's coordinate system to parent's coordinates (rot+trans)
- Global matrix \mathbf{G}_j maps from j 's coordinate system to root coordinates (rot+trans)
- Compute global matrices through forward kinematics

$$\mathbf{G}_j = \mathbf{L}_1 \mathbf{L}_2 \cdots \mathbf{L}_j = \mathbf{G}_{j-1} \mathbf{L}_j$$

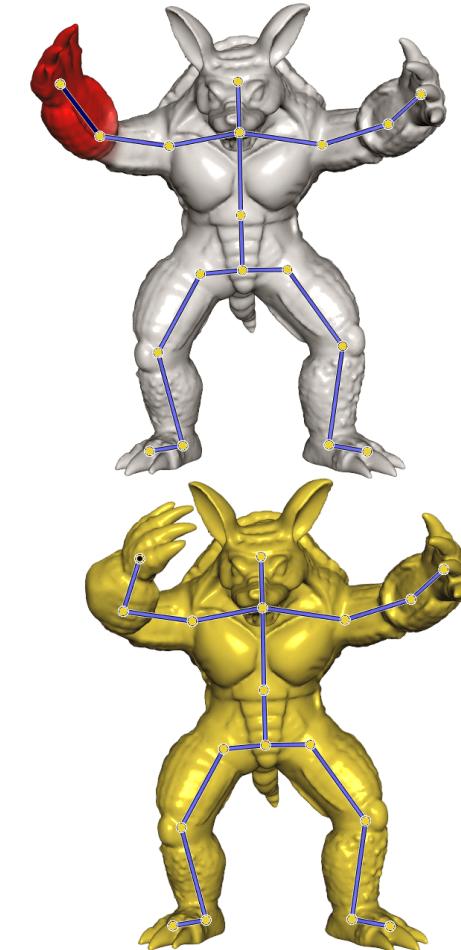
Skeleton Forward Kinematics



- Compute and store global matrix $\bar{\mathbf{G}}_j$ in initial pose
- Local matrices \mathbf{L}_j change during animation and update global matrices \mathbf{G}_j
- Matrix $\mathbf{T}_j = \mathbf{G}_j \bar{\mathbf{G}}_j^{-1}$ maps from global initial coordinates through j 's local coordinates to animated global coordinates
- Give \mathbf{T}_j to skinning algorithm

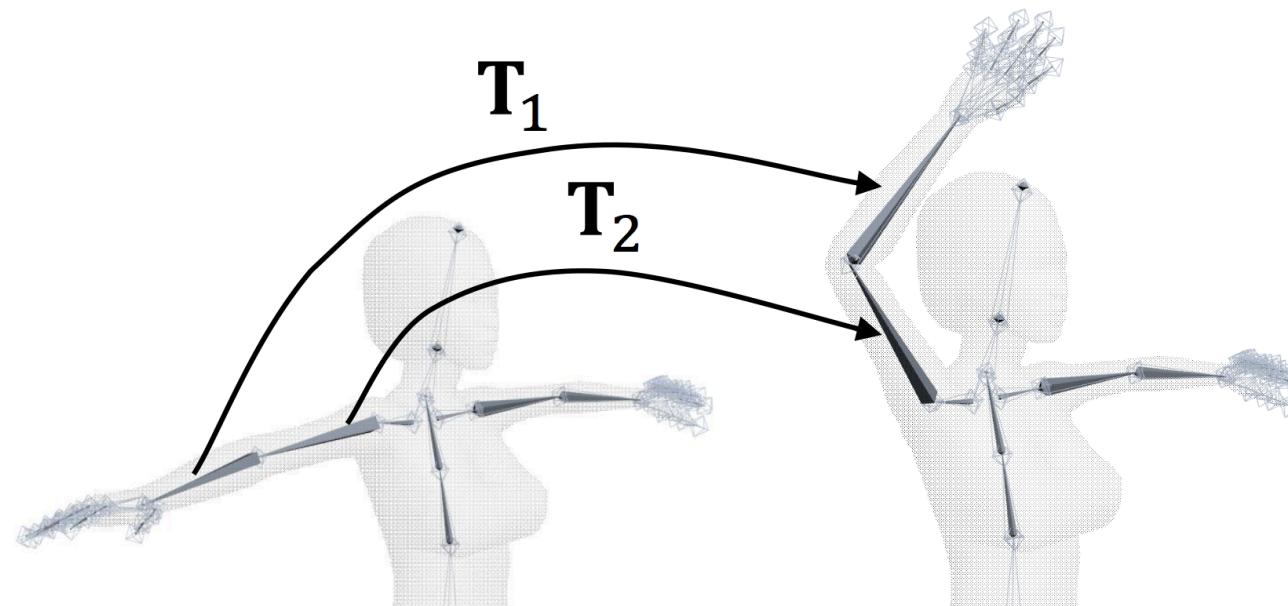
Skeleton-Based Animation

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Skinning

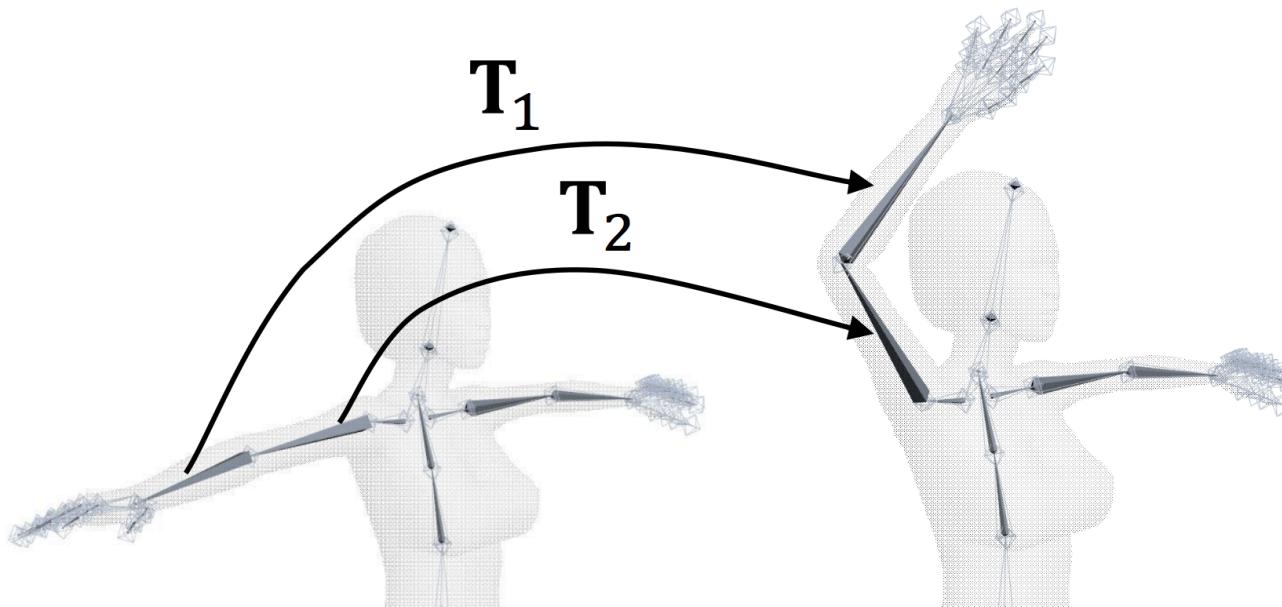
- Deform skin mesh to follow embedded skeleton
- Each bone j has an associated transformation matrix \mathbf{T}_j , which consist of rotation and translation (*rigid motion*)



“Rigid Skinning”

- Transform a vertex \mathbf{x}_i that depends on **only one** bone j

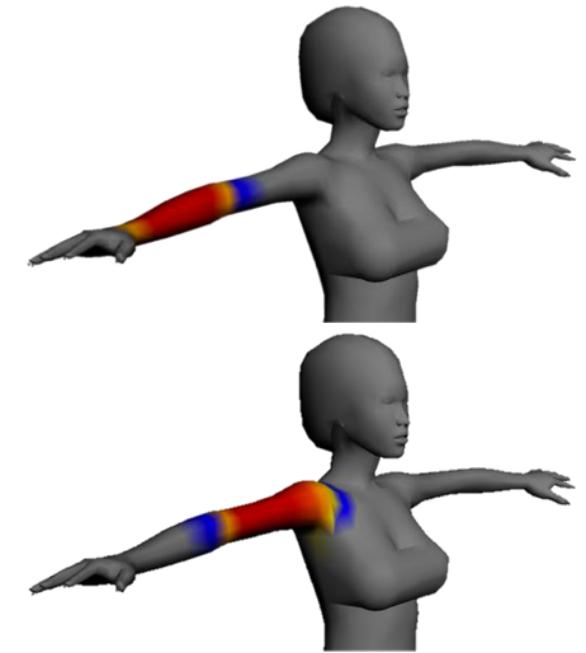
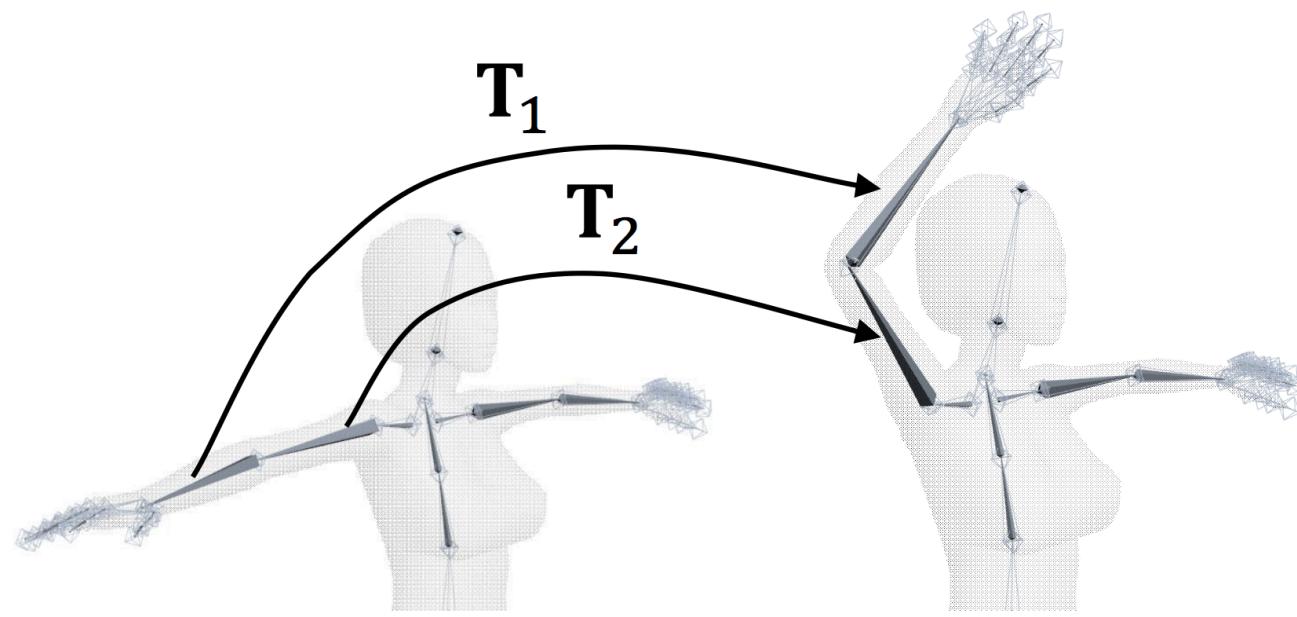
$$\begin{pmatrix} \mathbf{x}'_i \\ 1 \end{pmatrix} = \mathbf{T}_j \begin{pmatrix} \mathbf{x}_i \\ 1 \end{pmatrix}$$



Linear Blend Skinning

- Transform a vertex \mathbf{x}_i that depends on **several** bones

$$\begin{pmatrix} \mathbf{x}'_i \\ 1 \end{pmatrix} = \sum_{j=1}^m w_{i,j} \mathbf{T}_j \begin{pmatrix} \mathbf{x}_i \\ 1 \end{pmatrix}$$



Let's try

Linear Blend Skinning

- Transform a vertex \mathbf{x}_i that depends on several bones

$$\begin{pmatrix} \mathbf{x}'_i \\ 1 \end{pmatrix} = \sum_{j=1}^m w_{i,j} \mathbf{T}_j \begin{pmatrix} \mathbf{x}_i \\ 1 \end{pmatrix}$$

- Leads to well-known problems at joints



“candy wrapper”



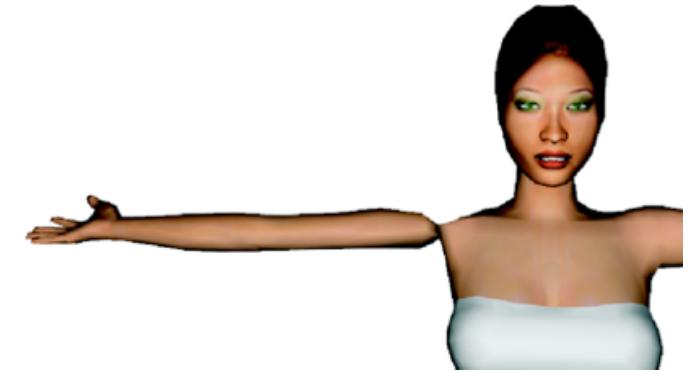
“collapsing joint”

Where do these problems come from?

Linear Blend Skinning

- Extreme 2D example: Blend between identity and 180° rotation:

$$\frac{1}{2} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix} + \frac{1}{2} \begin{pmatrix} -1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$



- Linear combination of rigid motions

$$\sum_{j=1}^m w_{i,j} \mathbf{T}_j$$

is not a rigid motion anymore!

How to blend rigid motions? Dual Quaternion Skinning!

Summary Skeleton-Based Animation

- **Rigging**
 - Bone weights define influence of bones on vertices
 - Weights must sum up to one and should be non-negative
- **Skeleton Forward Kinematics**
 - Local matrices map from joint coordinates to parent coordinates
 - Global matrices map from joint coordinates to root coordinates
 - Define 4×4 rigid transformation \mathbf{T}_j for each joint j .
- **Linear Blend Skinning**
 - Convex combination of rigid transformations: $\mathbf{T} = \sum_j w_j \mathbf{T}_j$
 - Resulting transformation \mathbf{T} is **not rigid** anymore
 - Artifacts: candy-wrapper and joint collapse 😢
 - Advanced Method: [Dual Quaternion Skinning](#)

Let's try

Literature

- **Skeleton Animation**

- Kavan et al, *Skinning with Dual Quaternions*, Symposium on Interactive 3D Graphics and Games 2007
- Jacobson et al, *Skinning: Real-time Shape Deformation*, Course at SIGGRAPH 2014

Quiz: Linear Blend Skinning

What is the reason for the skinning artifacts?

What does it have to do with the blended matrix $\mathbf{T} := \sum_j w_{i,j} \mathbf{T}_j$?

A: \mathbf{T} is not symmetric anymore

B: \mathbf{T} is not orthogonal anymore

C: \mathbf{T} is not rigid motion anymore

D: \mathbf{T} is not invertible anymore

