

Computer Security and Privacy (COM-301)

Applied cryptography II

Carmela Troncoso

SPRING Lab

carmela.troncoso@epfl.ch

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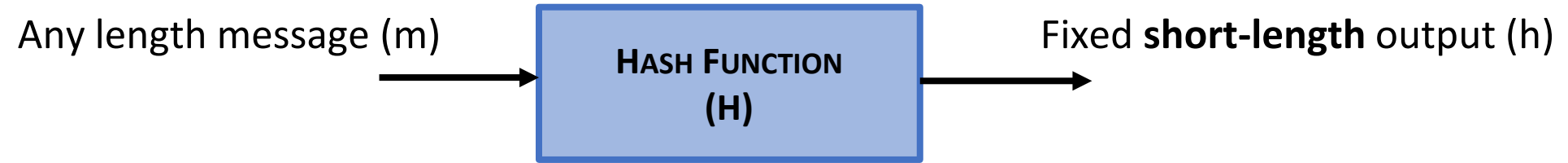
Hash functions

Carmela Troncoso

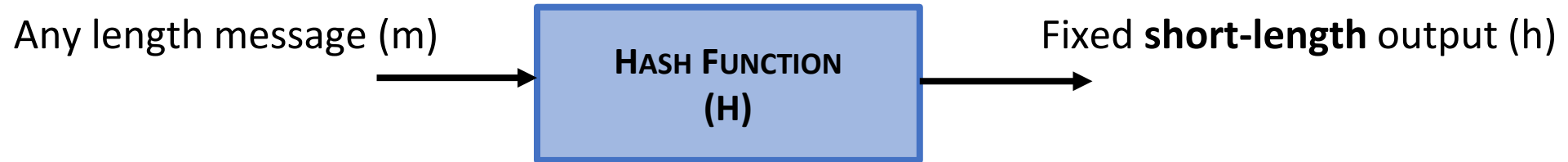
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Hash functions



Hash functions



THREE SECURITY PROPERTIES

PRE-IMAGE RESISTANCE

Given $H(m)$, difficult to find m

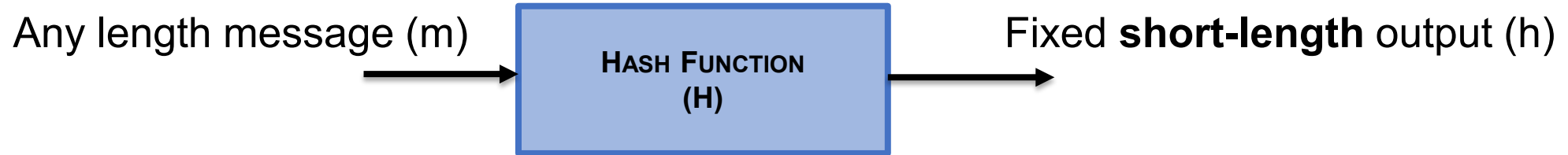
SECOND PRE-IMAGE RESISTANCE

Given m , difficult to find an $m' \neq m$ such that $H(m') = H(m)$

COLLISION RESISTANCE

Difficult to find any m, m' such that $H(m) = H(m')$

Hash functions



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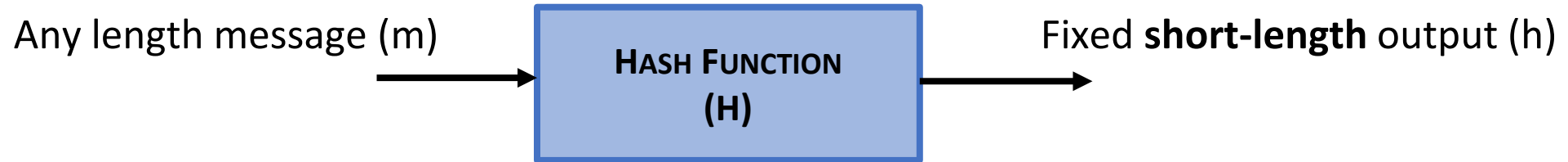
Difficult to find any m, m' such that $H(m) = H(m')$

MD5 (1991): 128 bit hash – insecure
SHA0, SHA1: 160 bits – insecure
SHA-2 (224/256 /384/512) – OK but slow
SHA-3 (224/256 /384/512)

Don't design
your own



Hash functions



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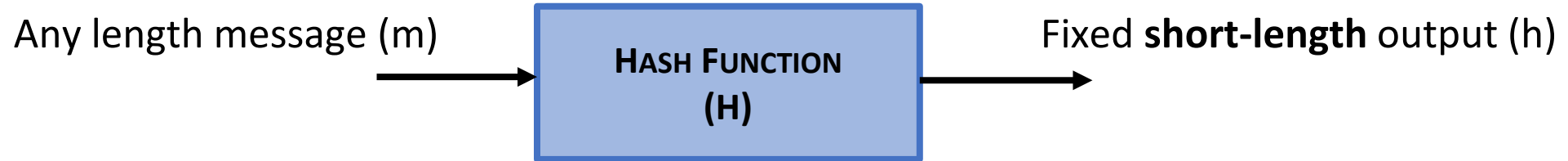
COLLISION RESISTANCE

Difficult to find any m, m' such that $H(m) = H(m')$

USES

Support digital signatures, build HMAC, password storage, file integrity, secure commitments, secure logging, blockchains, ...

Hash functions



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COLLISION RESISTANCE

Difficult to find



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Support digital signatures, build HMAC, password storage, file integrity, secure commitments, secure logging, blockchain,...

Computer Security (COM-301)

Applied cryptography

Asymmetric cryptography

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Symmetric Cryptography

Block ciphers, Stream Ciphers, MACs

Alice and Bob need to **share** a **secret** key

Secure key distribution is a problem!

Asymmetric cryptography

Each participant has **two** keys:

One **secret** key that only they know

One **public** key that they can reveal

Pairs of (secret, public) keys are created with specific algorithms



Secret Key: SK_{Bob}

Public Key: PK_{Bob}

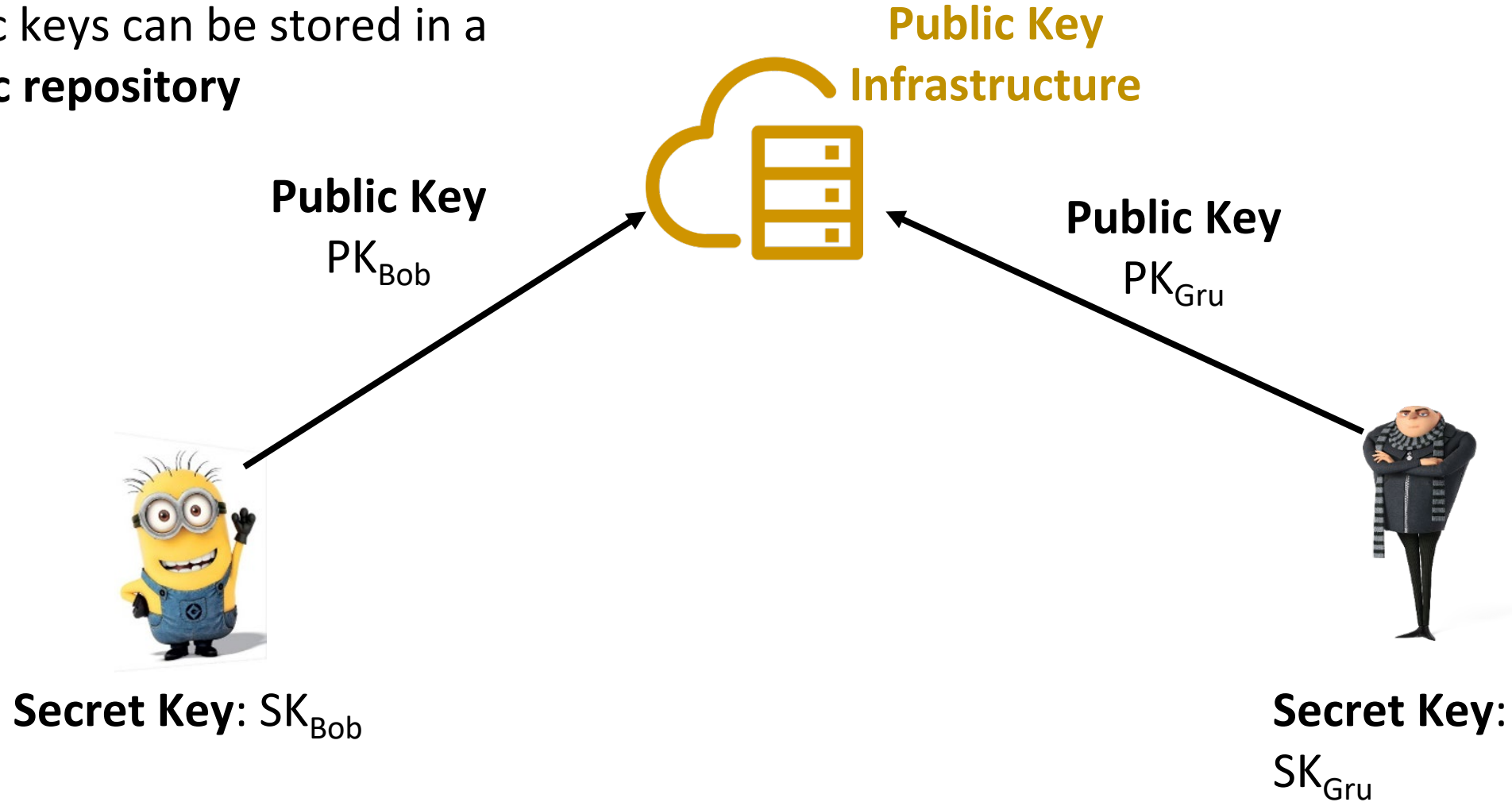


Secret Key: SK_{Gru}

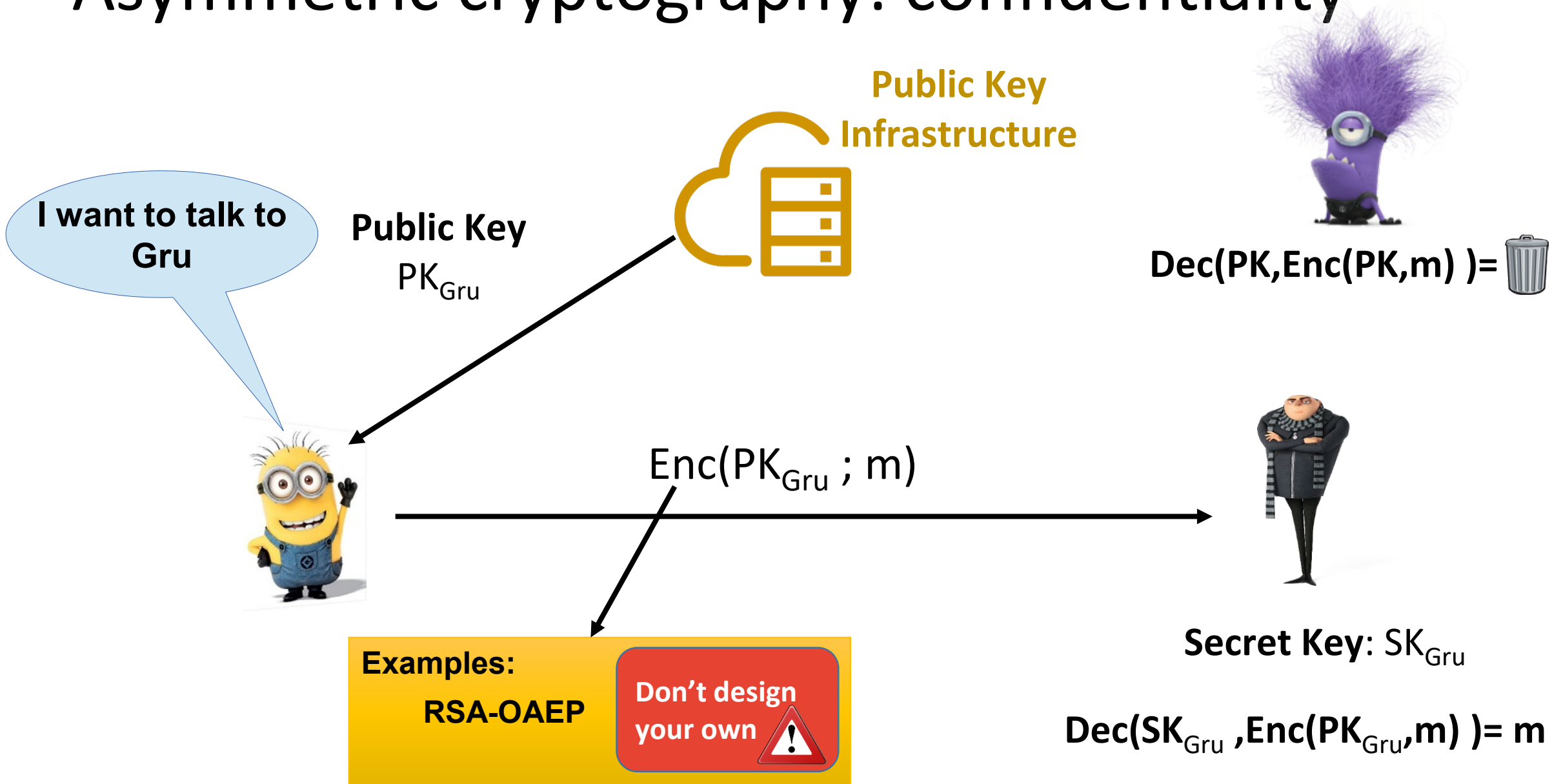
Public Key: PK_{Gru}

Asymmetric cryptography

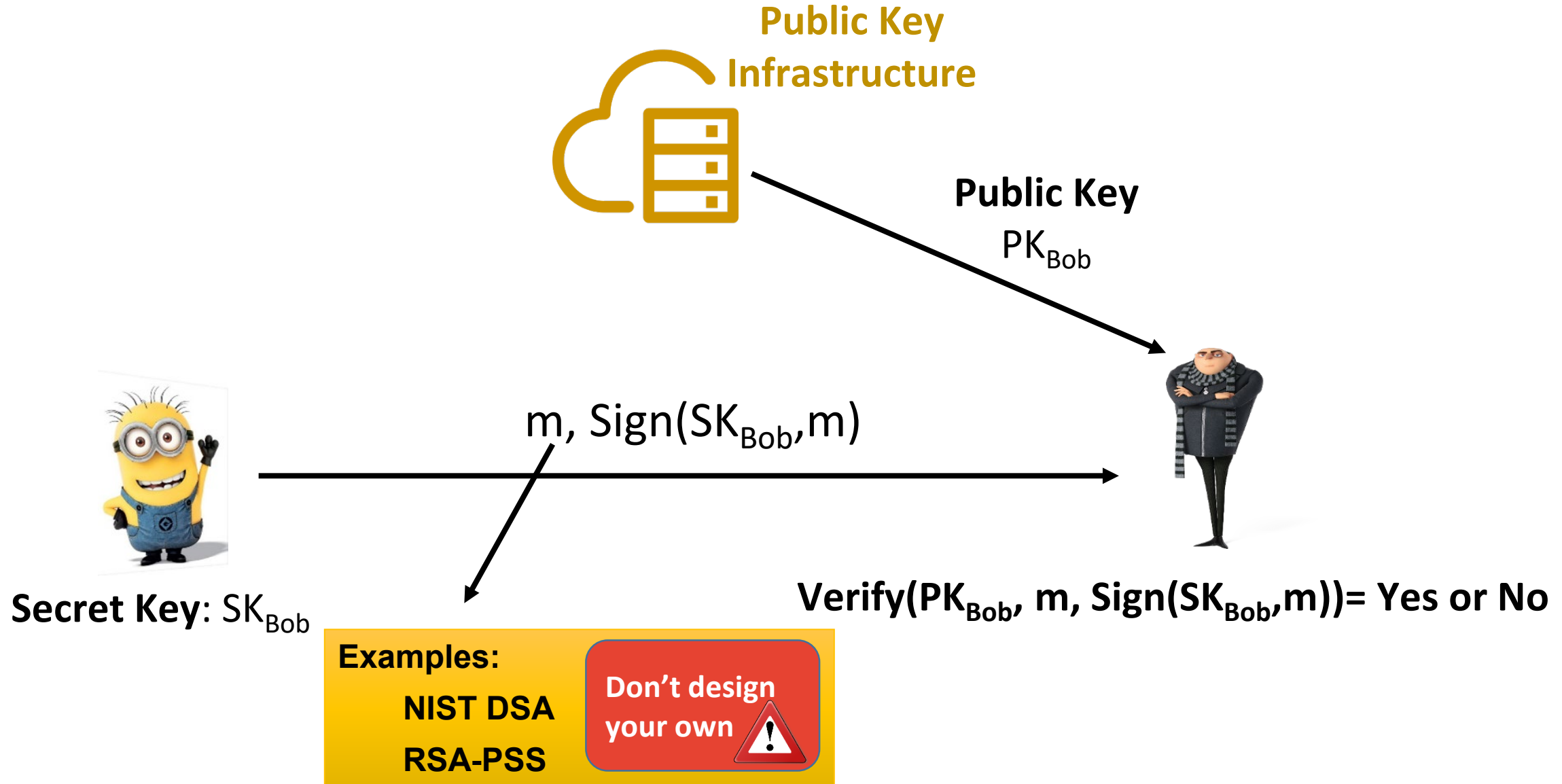
Public keys can be stored in a
public repository



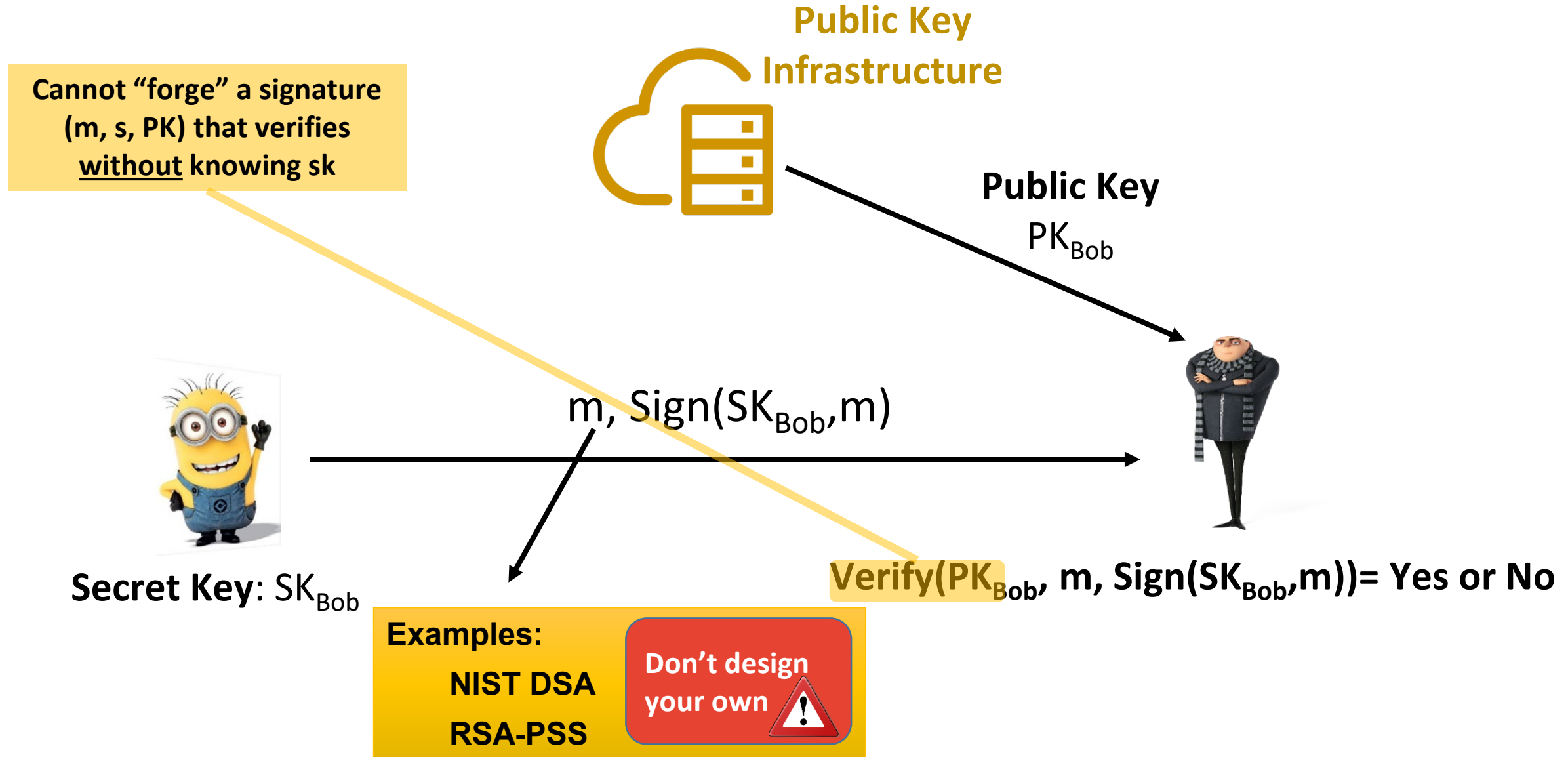
Asymmetric cryptography: confidentiality



Asymmetric cryptography: integrity



Asymmetric cryptography: integrity



Digital Signatures

Properties:

Integrity of message

Authenticity sender

Non-repudiation (why are they different from MACs?)

Application: **Public Key Infrastructure**: Certificates

- (1) Authority signs a mapping between names, or names and encryption public keys.
- (2) Authority signs mapping between names and verification keys.

Digital Signatures

Properties:

Integrity of message

Authenticity sender

Non-repudiation (why are they different from MACs?)

Encryption key pair \neq Signature key pair



Application: **Public Key Infrastructure:** Certificates

- (1) Authority signs a mapping between names, or names and encryption public keys.
- (2) Authority signs mapping between names and verification keys.

All together

ASYMMETRIC CRYPTOGRAPHY

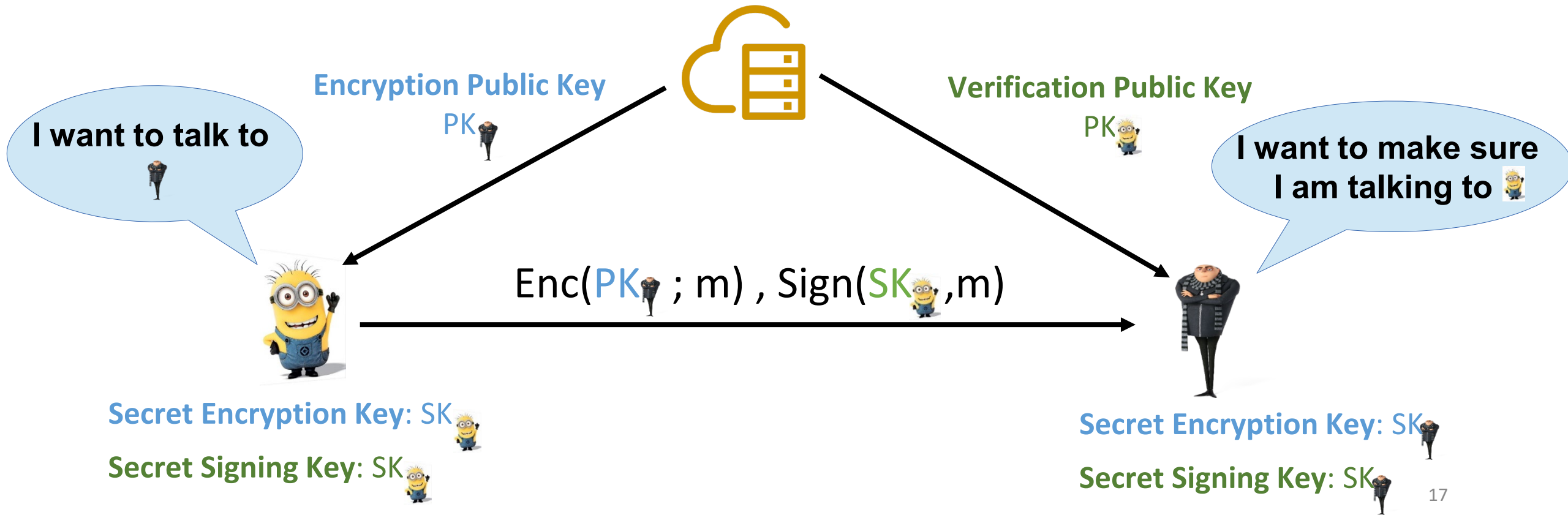
Users have two pairs of keys (secret key SK, public key PK)

Confidentiality

$\text{Dec}(\text{SK}, \text{Enc}(\text{PK}, m)) = m$

Integrity/Authentication

$\text{Sig}(\text{SK}, m) = s; \text{Verify}(\text{PK}, \text{Sig}(\text{SK}, m)) = \text{YES/NO}$



Asymmetric cryptography limitations

Computationally costly compared with most symmetric key algorithms of equivalent security

Signing and encrypting **is slow**

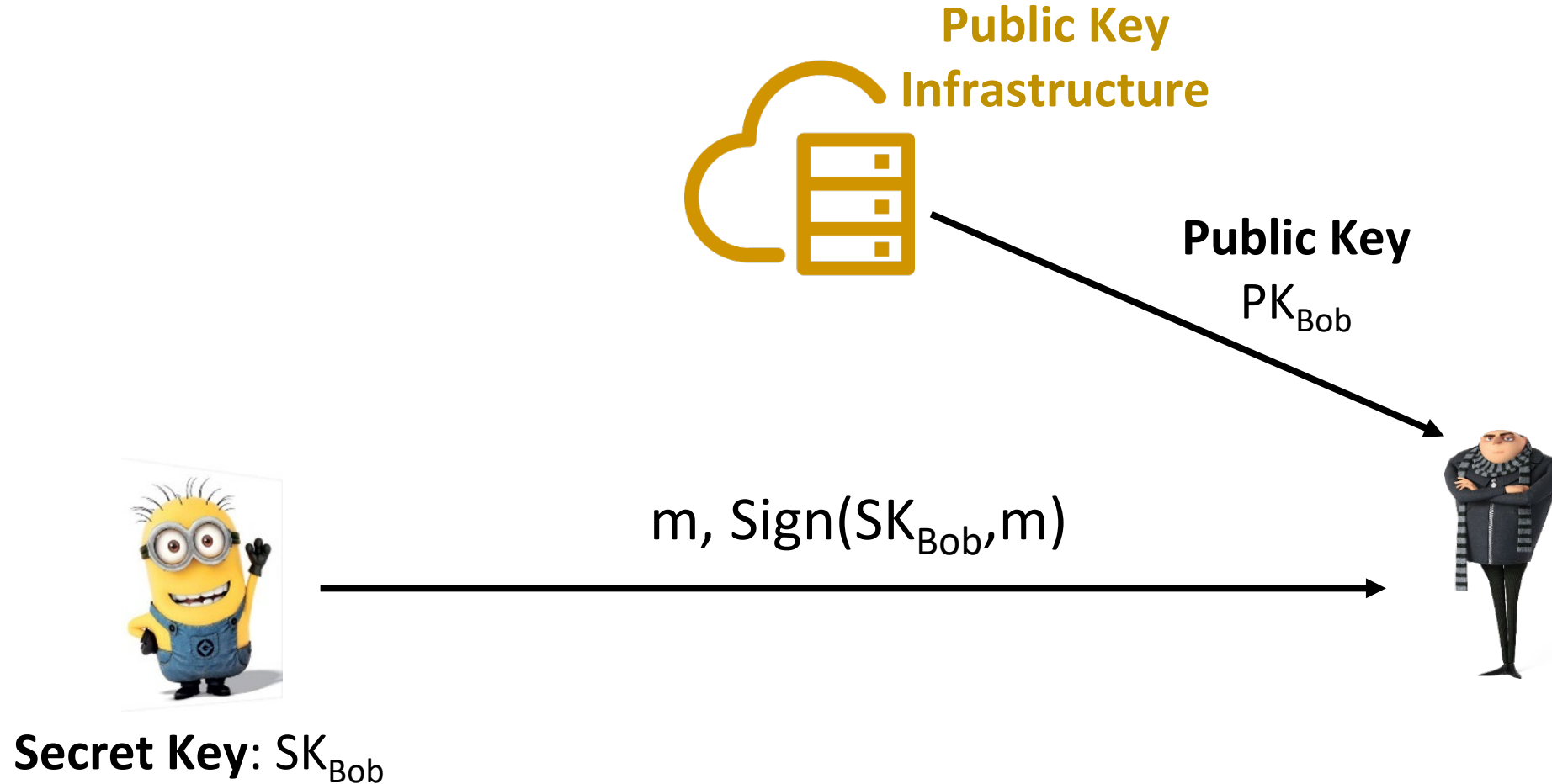
Not suitable to encrypt **large amounts of data**
There are not good “cipher modes”

In practice

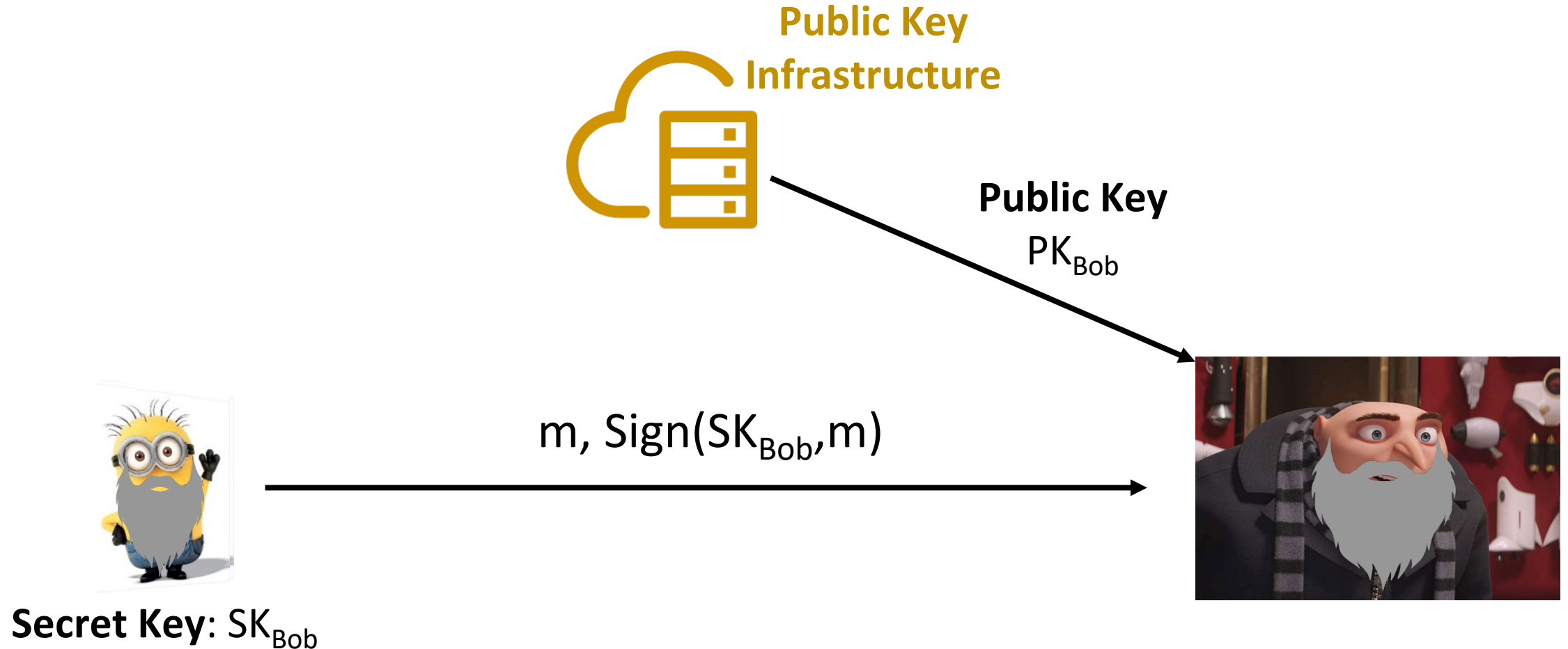
Sign hash of messages

Hybrid encryption
(only encrypt small symmetric key)

Digital signatures on hash functions



Digital signatures on hash functions



Digital signatures on hash functions

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Given $H(m)$, difficult to get m

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Given m , difficult to get an $m' \neq m$ such that $H(m') = H(m)$

COLLISION RESISTANCE

Difficult to find any m, m' such that $H(m) = H(m')$

Refresher

Public Key
Infrastructure



Public Key
 PK_{Bob}

I want to make sure
I am talking to 

$h = H(m)$



Secret Key: SK_{Bob}

$m, \text{Sign}(SK_{Bob}, h)$



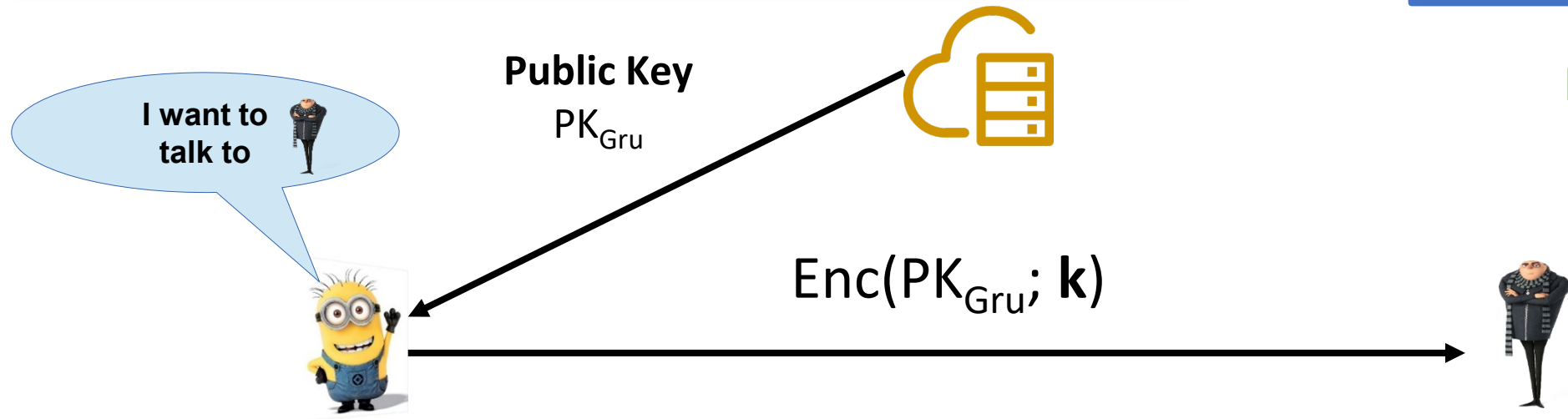
$h = H(m)$

$\text{Verify}(PK_{Bob}, h, \text{Sign}(SK_{Bob}, h)) = \text{Yes or No}$

Hybrid encryption

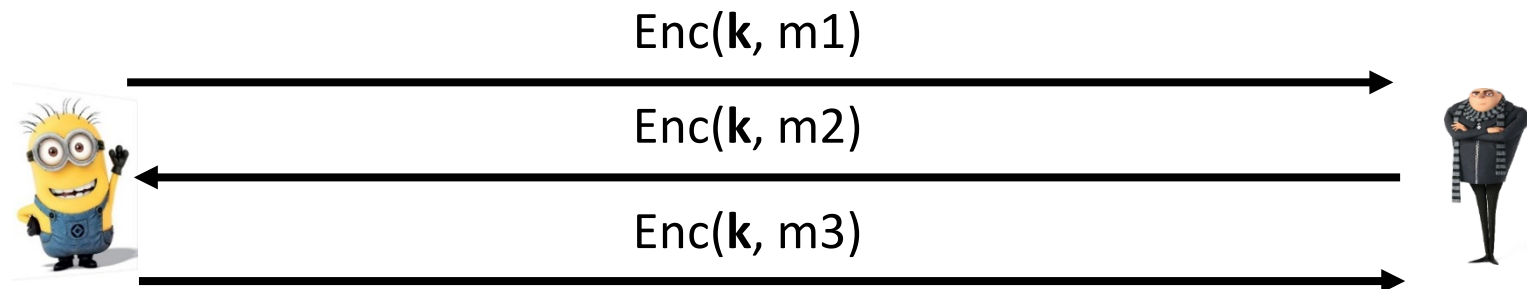
Asymmetric encryption **is slow**, but symmetric **is fast**!

Step 1: establish a shared symmetric key k using “key transport”



For authentication,
add signatures!!

Step 2: use the shared symmetric key k to encrypt the rest of the communication

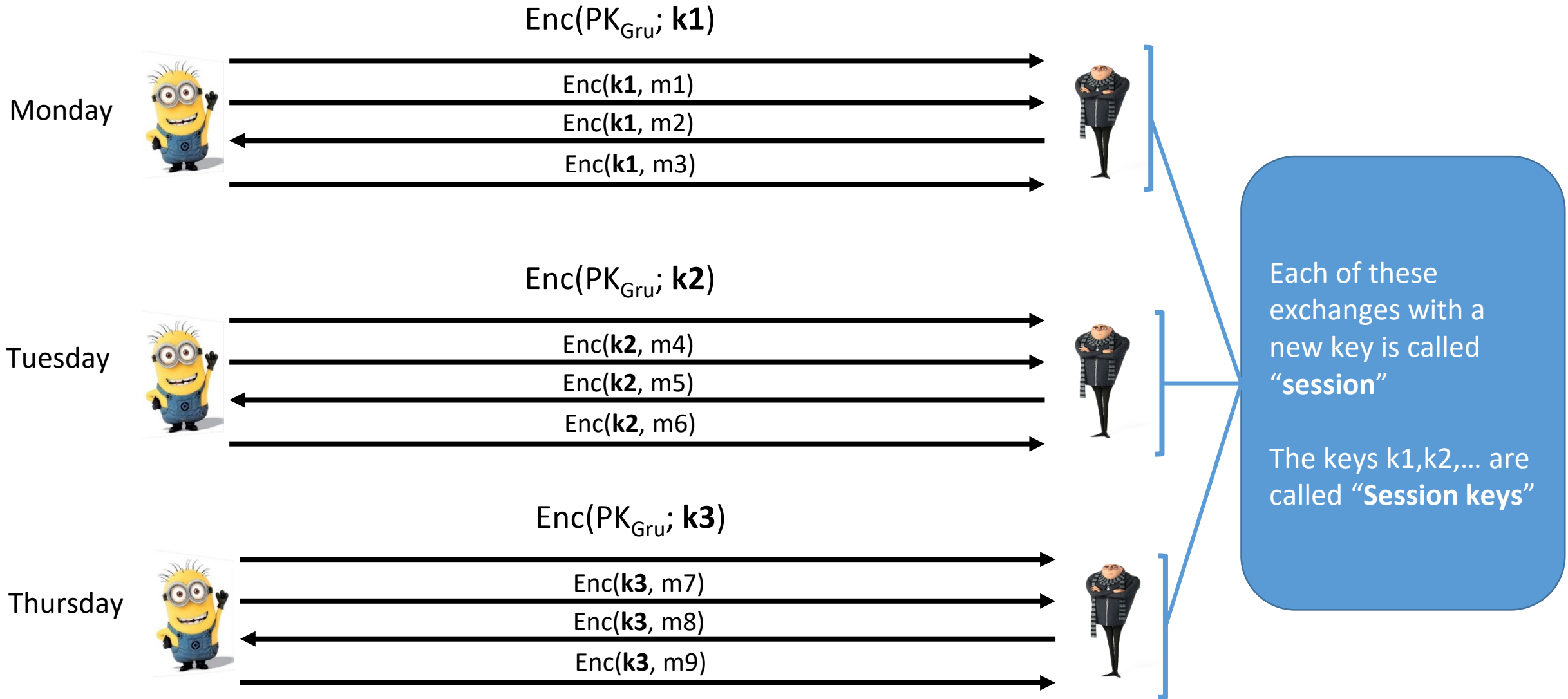


Don't design
your own

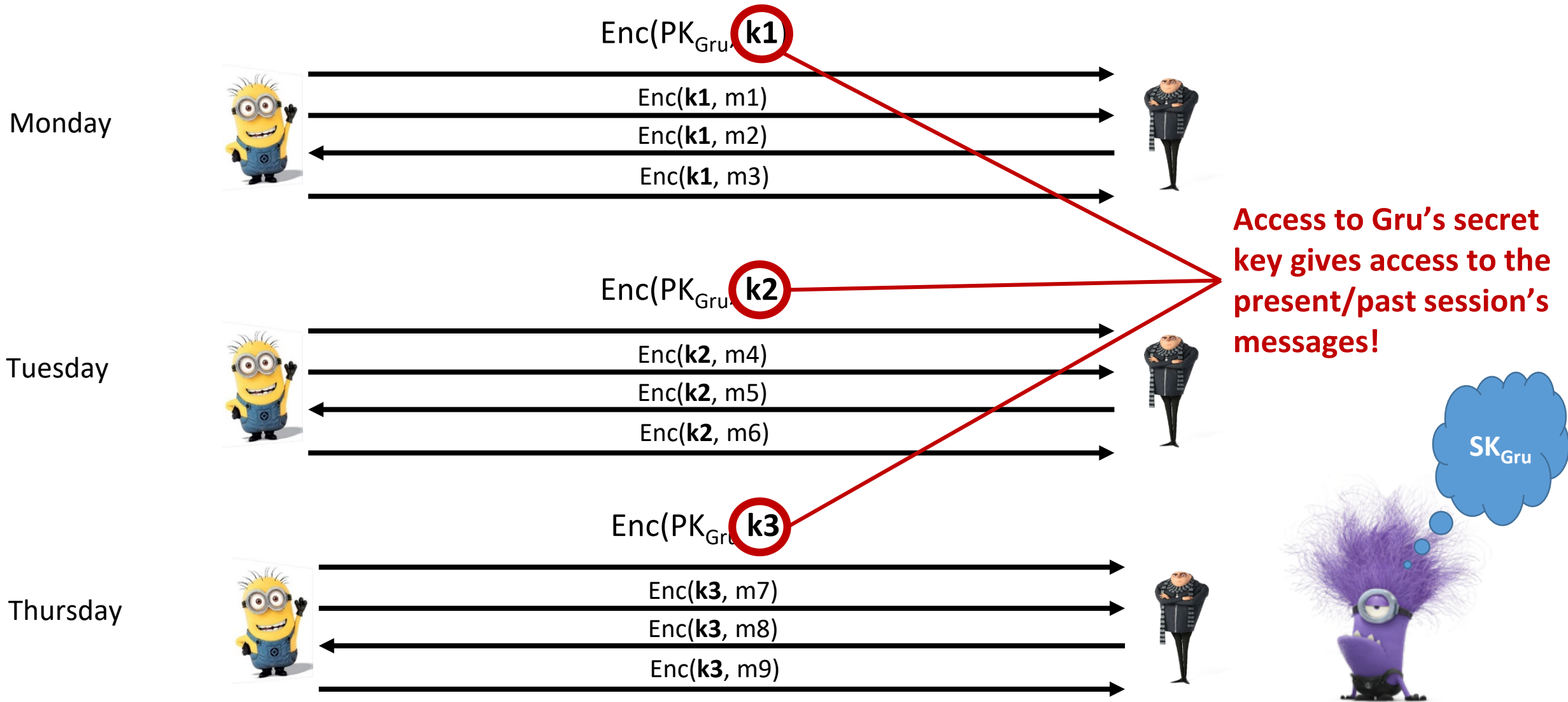


NOT SO SIMPLE!
e.g. ISO 9798-3
TLS

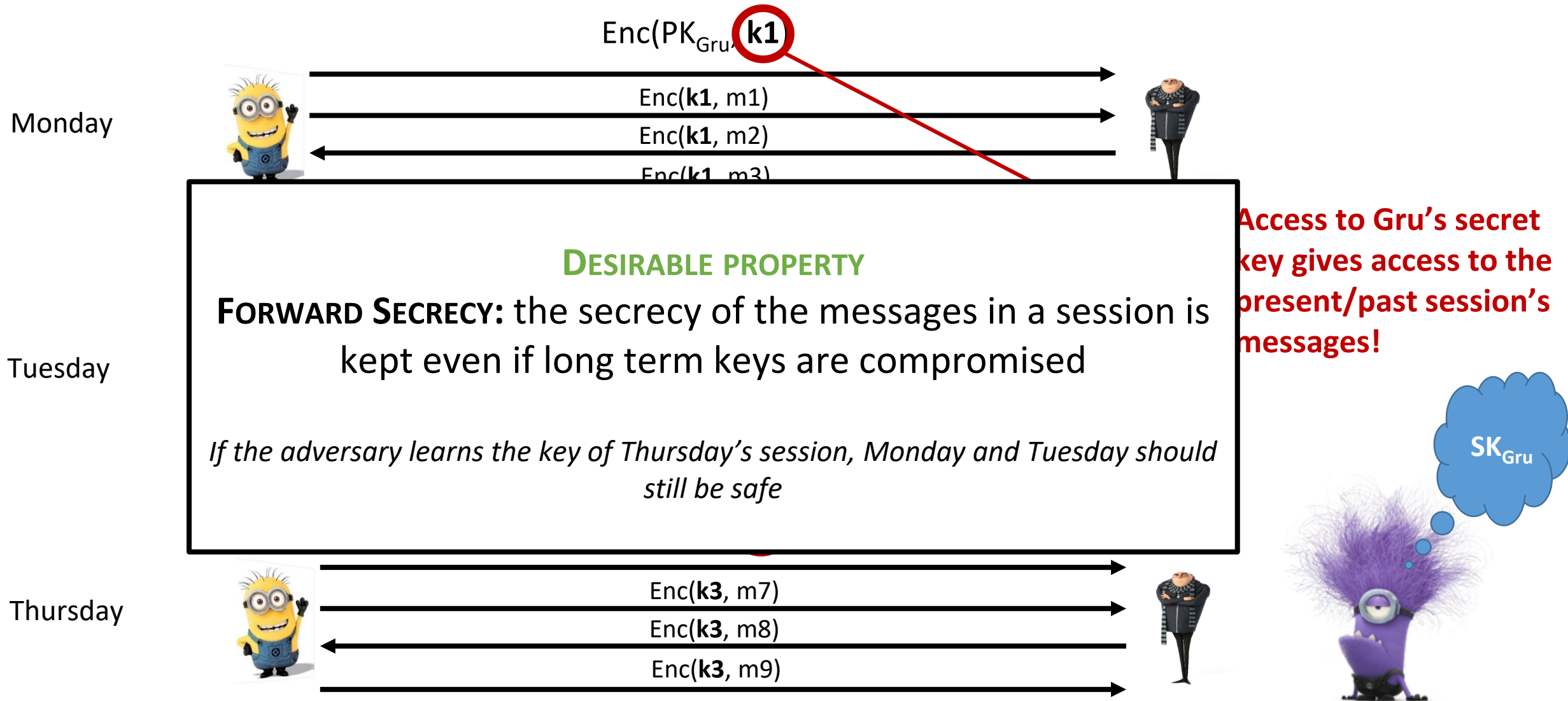
This process is repeated every time Bob wants to talk to Gru



What happens if the adversary gets access to Gru's asymmetric key on Thursday?



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Key agreement for forward secrecy – The Math

Arithmetic modulo a number: clock arithmetic

$$6 \pmod{12} = 6 \pmod{12}$$

$$12 \pmod{12} = 0 \pmod{12}$$

$$14 \pmod{12} = 2 \pmod{12}$$

Arithmetic modulo a large prime p (>1024 bits)

Addition and multiplication \pmod{p} can be computed

Exponentiation can be computed [Given $(a, x) \rightarrow a^x \pmod{p}$]

Discrete logarithms are **HARD**! [Given $(a, a^x \pmod{p}) \rightarrow x$]

Basic Diffie-Hellman key exchange

Every time Bob wants to talk to Gru...

Shared **public** parameters p, g

Because of the discrete logarithm hardness, an adversary observing these values cannot recover x and y , therefore cannot compute k



Secret Key: x (random!)

$$(P_a)^x = g^{xy} \pmod{p}$$

P_b

P_a



Secret Key: y (random!)

$$(P_b)^y = g^{xy} \pmod{p}$$

Shared secret!!

$$k = g^{xy} \pmod{p}$$

To encrypt messages for the session

Basic Di

Every time

After the session has ended, delete the secrets x and y .
The key can never be recovered.
Forward secrecy is achieved!!

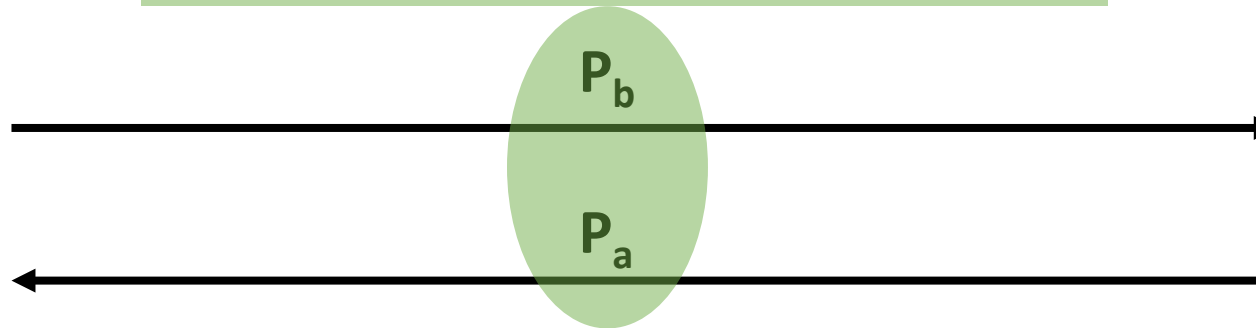
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Secret Key: x (random!)

$$(P_a)^x = g^{xy} \pmod{p}$$



Secret Key: y (random!)

$$(P_b)^y = g^{xy} \pmod{p}$$

Shared secret!!

$$k = g^{xy} \pmod{p}$$

To encrypt messages for the session

Summary of the crypto lectures

Symmetric cryptography

- Confidentiality: Stream ciphers, Block ciphers (modes of operation!)
- Integrity / Authentication: Message Authentication Codes (MACs)

Asymmetric cryptography

- Confidentiality: Encryption
- Integrity / Authentication: Digital signatures

Hash functions

- Three security properties
- Support Digital Signatures + other functions

Hybrid encryption

best both worlds!

Forward secrecy

Diffie Hellman

Why a MAC should not be constructed as $\text{Hash}(k||m)$



TAs & Carmela: Why are they designing their own crypto?!?!?
Why is this designing Crypto? You go from Hash to MAC.

COM-208 Computer networks!!

“Computer Networking: A Top-Down Approach”: $\text{MAC} = \text{Hash}(k||I \text{ am Alice})$



Is it wrong?!?!?!?

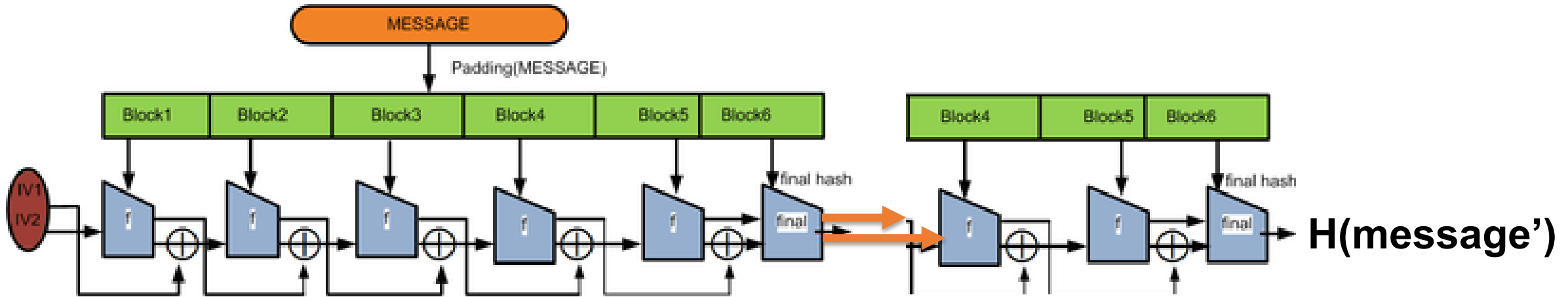
Short answer: Not always

So when is it wrong?

Not exam
material!!

Why a MAC should not be constructed as $\text{Hash}(k||m)$

Many Hash functions (MD5, SHA1, SHA256) are built using **the Merkle-Damgard paradigm**



Hash length extension attacks! (given $H(m)$ obtain $H(m||\text{stuff})$)

Example: $H(k||\text{this is Alice}) \rightarrow H(k||\text{this is Alice, First of her name, Queen of the Andals and the First Men})$

**$\text{MAC} = H(k||\text{Alice})$ does not guarantee integrity
for Merkle-Damgard hash functions**

Not exam
material!!

Why a MAC should not be constructed as $\text{Hash}(k||m)$

Many Hash functions (MD5, SHA1, SHA256) are built using **the Merkle-Damgard paradigm**



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