

Computer Security and Privacy (COM-301)

Applied cryptography II

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Computer Security (COM-301)

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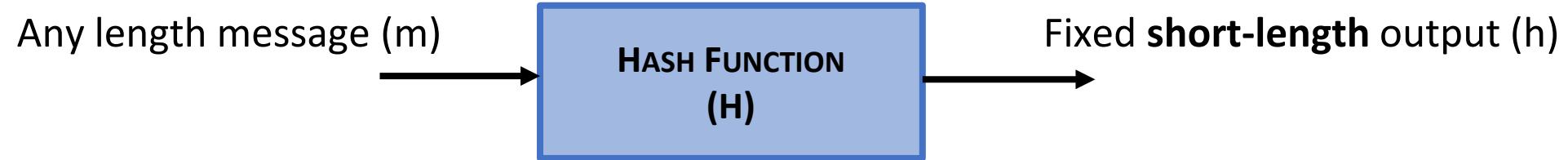
Hash functions

Carmela Troncoso

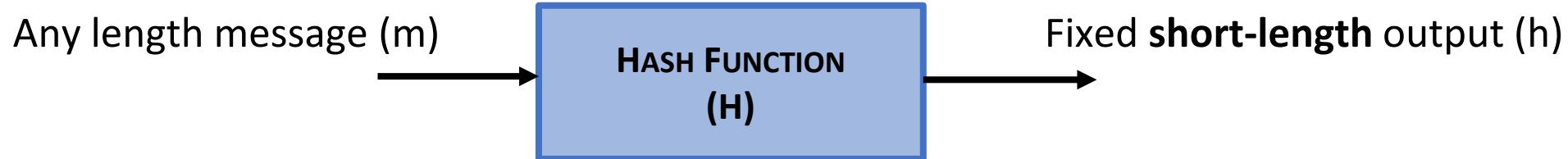
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Hash functions



Hash functions



THREE SECURITY PROPERTIES

PRE-IMAGE RESISTANCE

Given $H(m)$, difficult to find m

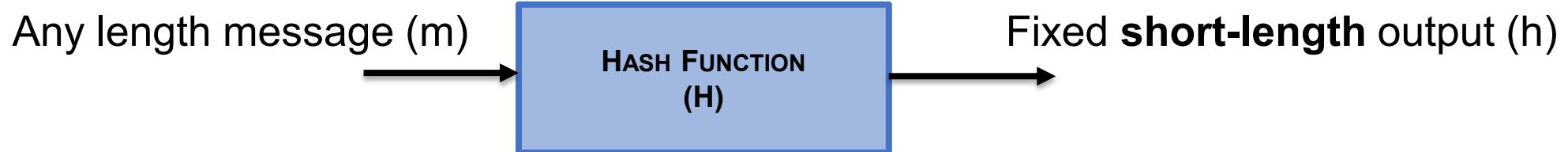
SECOND PRE-IMAGE RESISTANCE

Given m , difficult to find an $m' \neq m$ such that $H(m') = H(m)$

COLLISION RESISTANCE

Difficult to find any m, m' such that $H(m) = H(m')$

Hash functions



THREE SECURITY PROPERTIES

PRE-IMAGE RESISTANCE

Given $H(m)$, difficult to find m

SECOND PRE-IMAGE RESISTANCE

Given m , difficult to find an $m' \neq m$ such that $H(m') = H(m)$

COLLISION RESISTANCE

Difficult to find any m, m' such that $H(m) = H(m')$

MD5 (1991): 128 bit hash – insecure

SHA0, SHA1: 160 bits – insecure

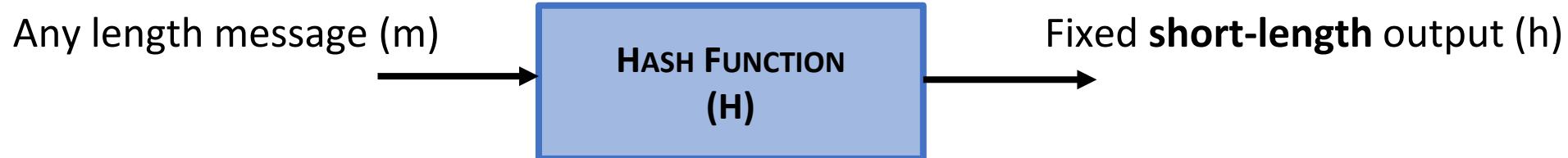
SHA-2 (224/256 /384/512) – OK but slow

SHA-3 (224/256 /384/512)

Don't design
your own



Hash functions



THREE SECURITY PROPERTIES

PRE-IMAGE RESISTANCE

Given $H(m)$, difficult to find m

SECOND PRE-IMAGE RESISTANCE

Given m , difficult to find an $m' \neq m$ such that $H(m') = H(m)$

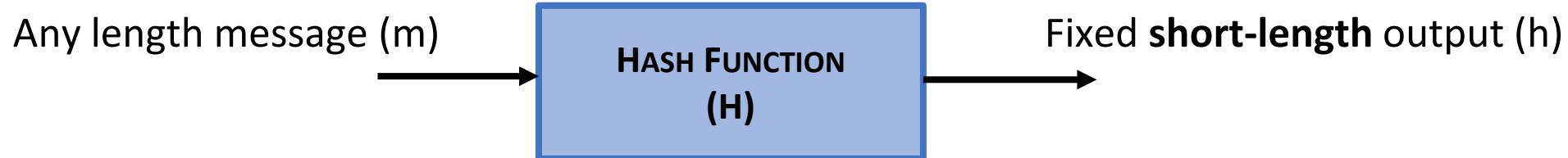
COLLISION RESISTANCE

Difficult to find any m, m' such that $H(m) = H(m')$

USES

Support digital signatures, build HMAC, password storage, file integrity, secure commitments, secure logging, blockchains, ...

Hash functions



THREE SECURITY PROPERTIES

PRE-IMAGE RESISTANCE

Given $H(m)$, difficult to get m

SECOND PRE-IMAGE RESISTANCE

Given m , difficult to get an $m' \neq m$ such that $H(m') = H(m)$

COLLISION RESISTANCE

Difficult to find $m_1 \neq m_2$ such that $H(m_1) = H(m_2)$

USES

Support digital signatures, build HMAC, password storage, file integrity, secure commitments, secure logging, blockchain,...



Computer Security (COM-301)

Applied cryptography

Asymmetric cryptography

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Symmetric Cryptography

Block ciphers, Stream Ciphers, MACs

Gru and Bob need to **share a secret** key

Secure key distribution is a problem!

Asymmetric cryptography

Each participant has **two** keys:

- One **secret** key that only they know
- One **public** key that they can reveal

Pairs of (secret, public) keys are created with specific algorithms



Secret Key: SK_{Bob}

Public Key: PK_{Bob}

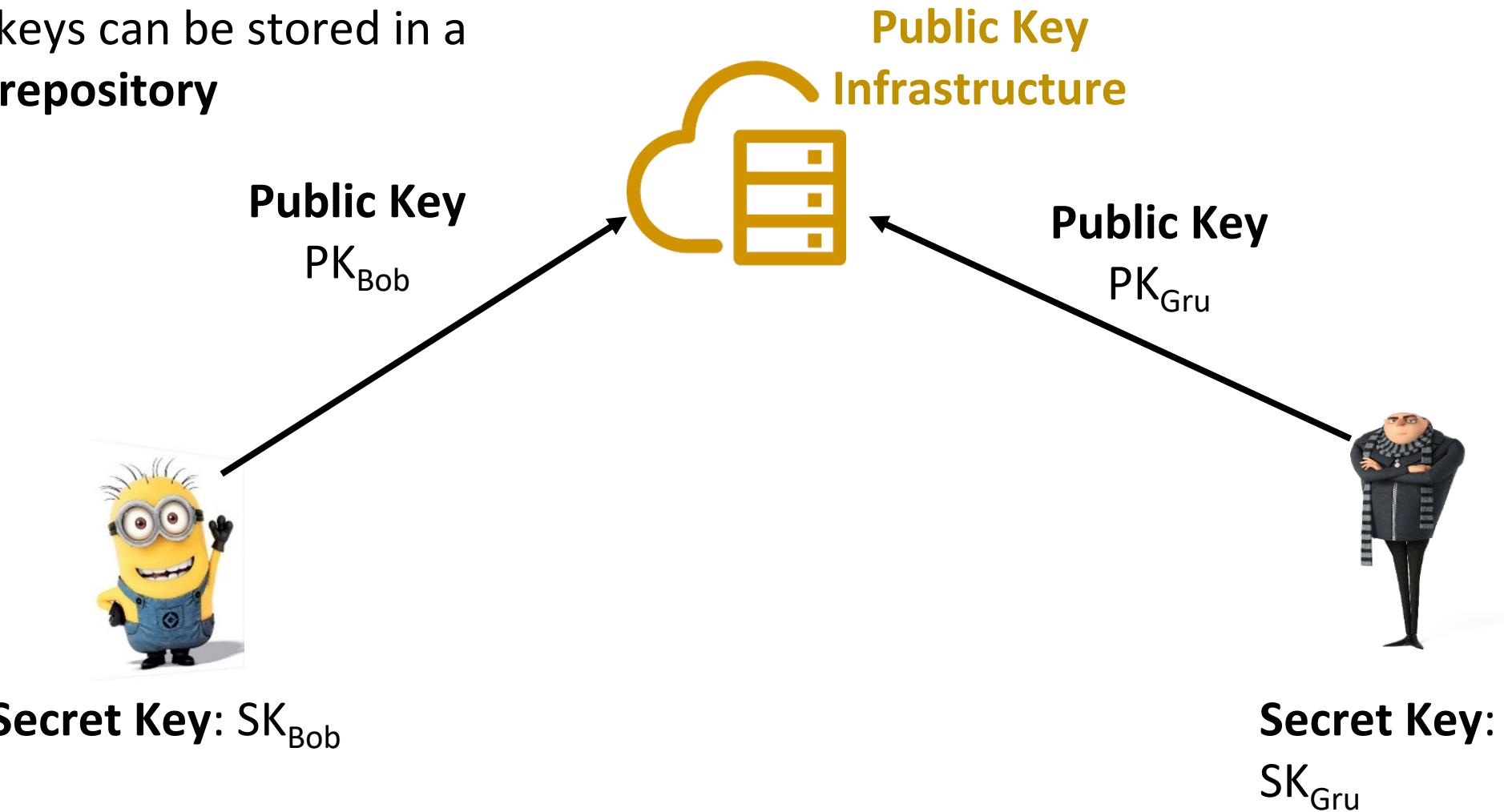


Secret Key: SK_{Gru}

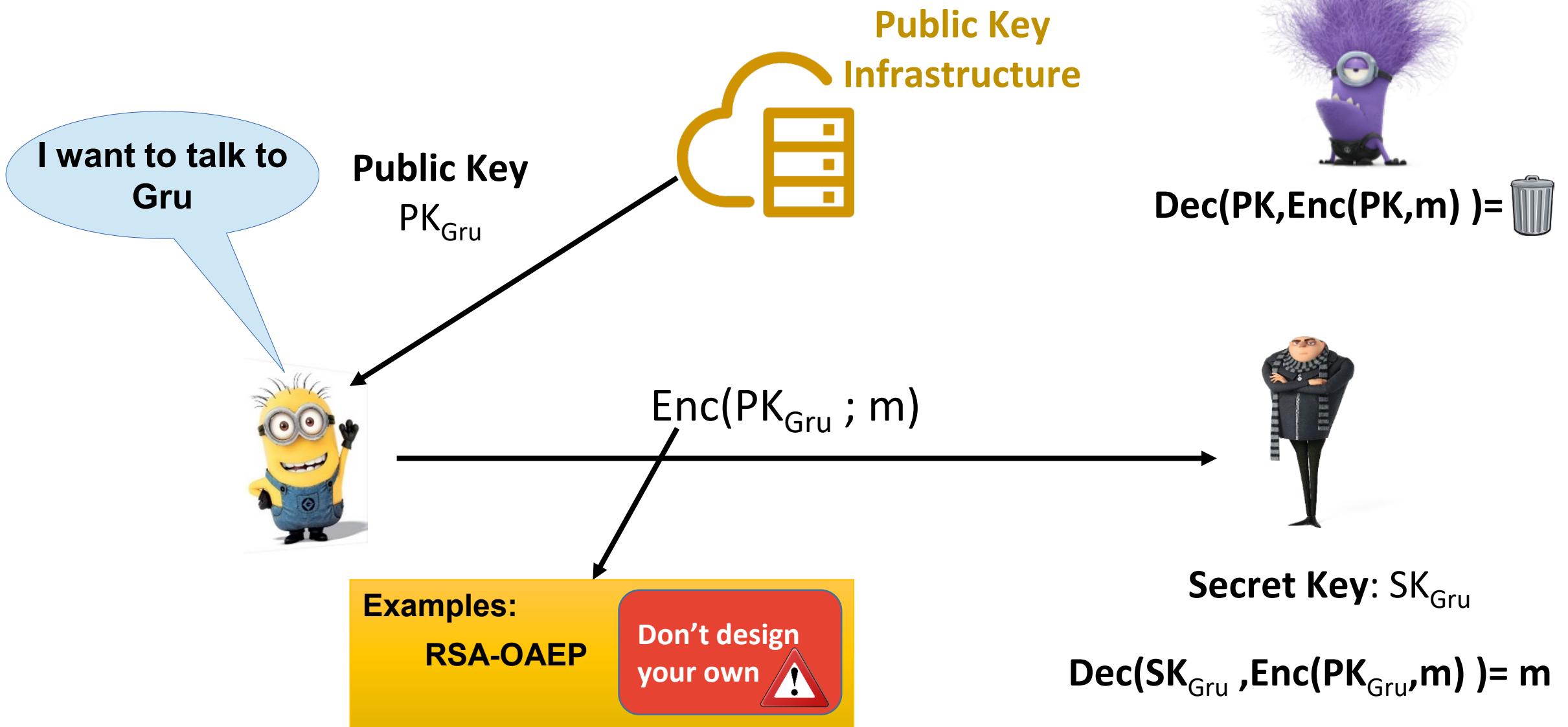
Public Key: PK_{Gru}

Asymmetric cryptography

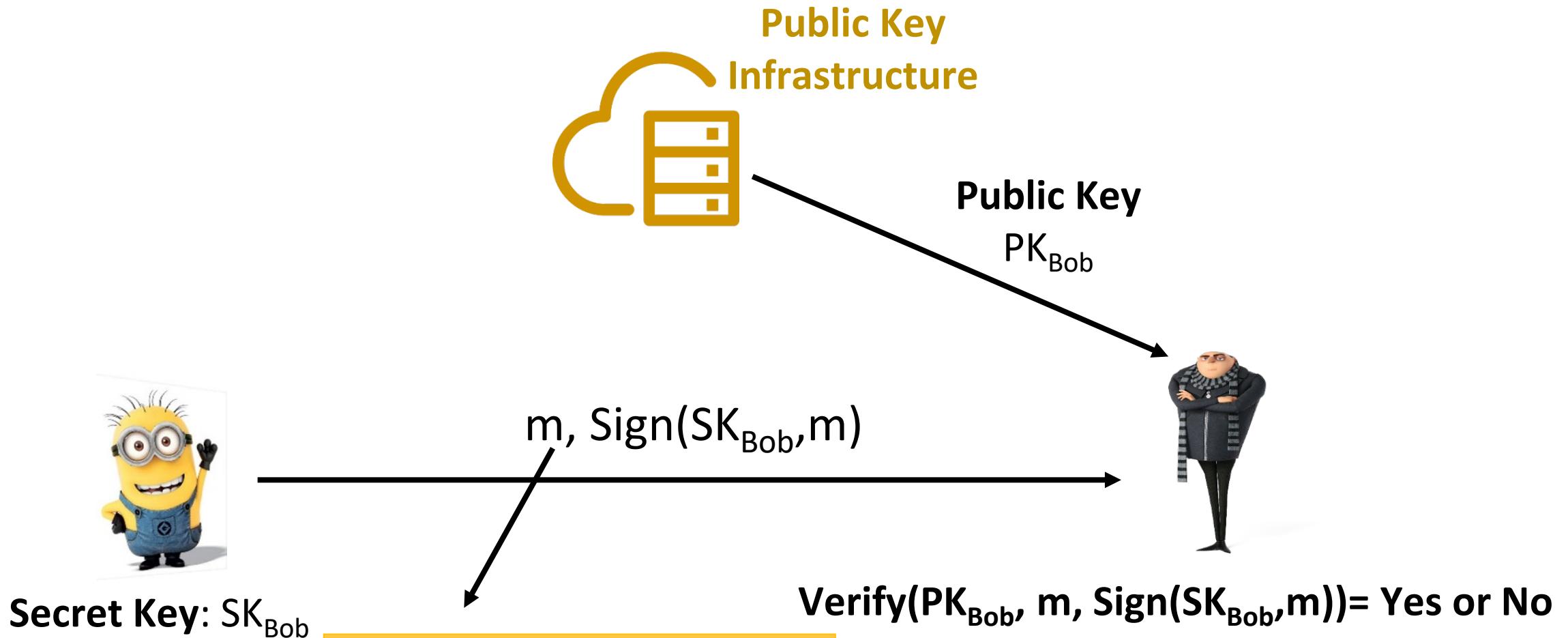
Public keys can be stored in a
public repository



Asymmetric cryptography: confidentiality



Asymmetric cryptography: integrity



Examples:

NIST DSA
RSA-PSS

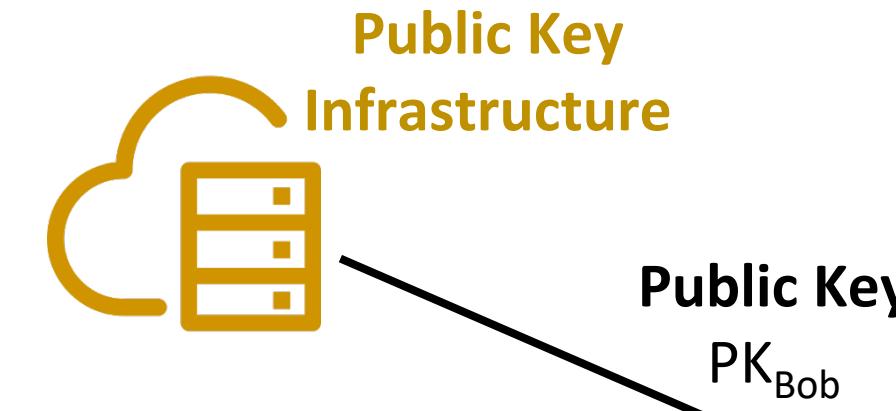
Don't design
your own

Asymmetric cryptography: integrity

Cannot “forge” a signature
(m, s, PK) that verifies
without knowing sk



Secret Key: SK_{Bob}



$m, \text{Sign}(SK_{Bob}, m)$



$\text{Verify}(PK_{Bob}, m, \text{Sign}(SK_{Bob}, m)) = \text{Yes or No}$

Examples:

NIST DSA
RSA-PSS

Don't design
your own



Digital Signatures

Properties:

Integrity of message

Authenticity sender

Non-repudiation ([why are they different from MACs?](#))

Application: **Public Key Infrastructure: Certificates**

- (1) Authority signs a mapping between names, or names and encryption public keys.
- (2) Authority signs mapping between names and verification keys.

Digital Signatures

Properties:

Integrity of message

Authenticity sender

Non-repudiation (why are they different from MACs?)

Encryption key pair \neq Signature key pair



Application: **Public Key Infrastructure: Certificates**

(1) Authority signs a mapping between names, or names and encryption public keys.

(2) Authority signs mapping between names and verification keys.

All together

ASYMMETRIC CRYPTOGRAPHY

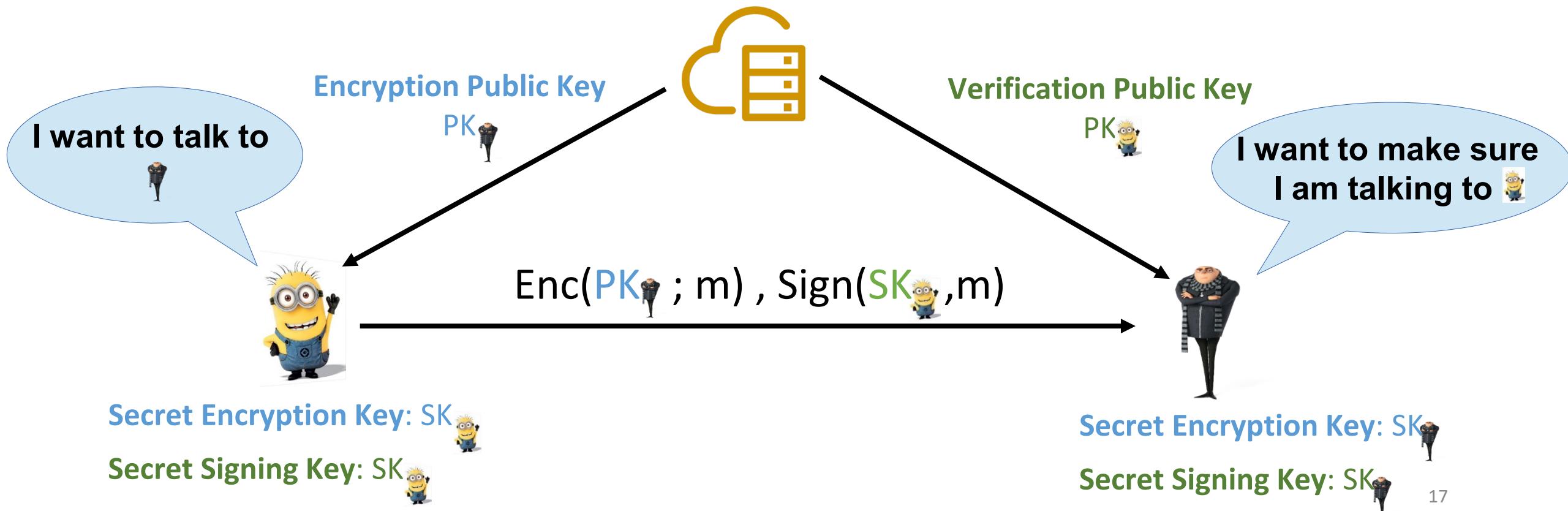
Users have two pairs of keys (secret key SK, public key PK)

Confidentiality

$\text{Dec}(\text{SK}, \text{Enc}(\text{PK}, m)) = m$

Integrity/Authentication

$\text{Sig}(\text{SK}, m) = s; \text{ Verify}(\text{PK}, \text{Sig}(\text{SK}, m)) = \text{YES/NO}$



Asymmetric cryptography limitations

Computationally costly compared with most symmetric key algorithms of equivalent security

Signing and encrypting **is slow**

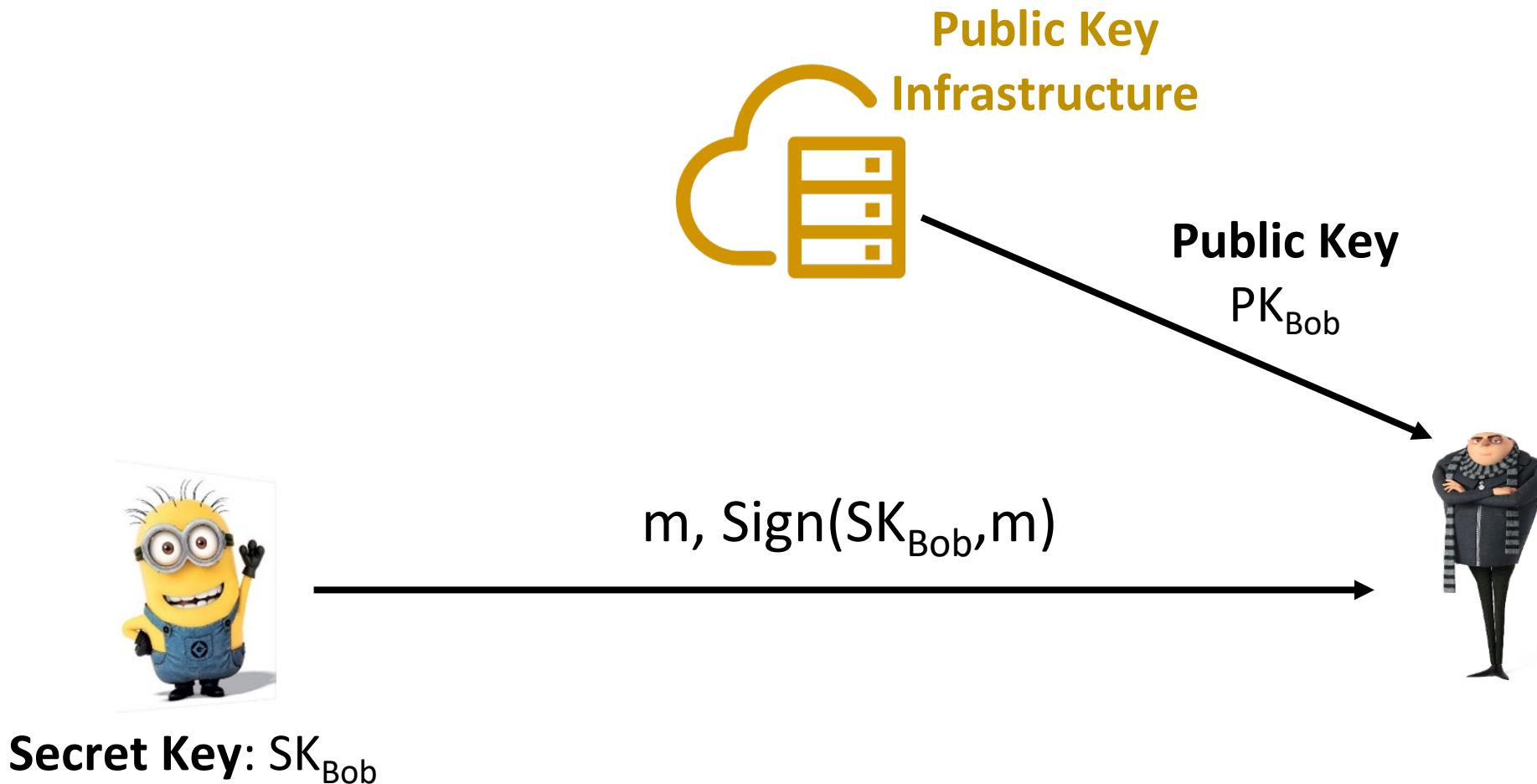
Not suitable to encrypt large amounts of data
There are not good “cipher modes”

In practice

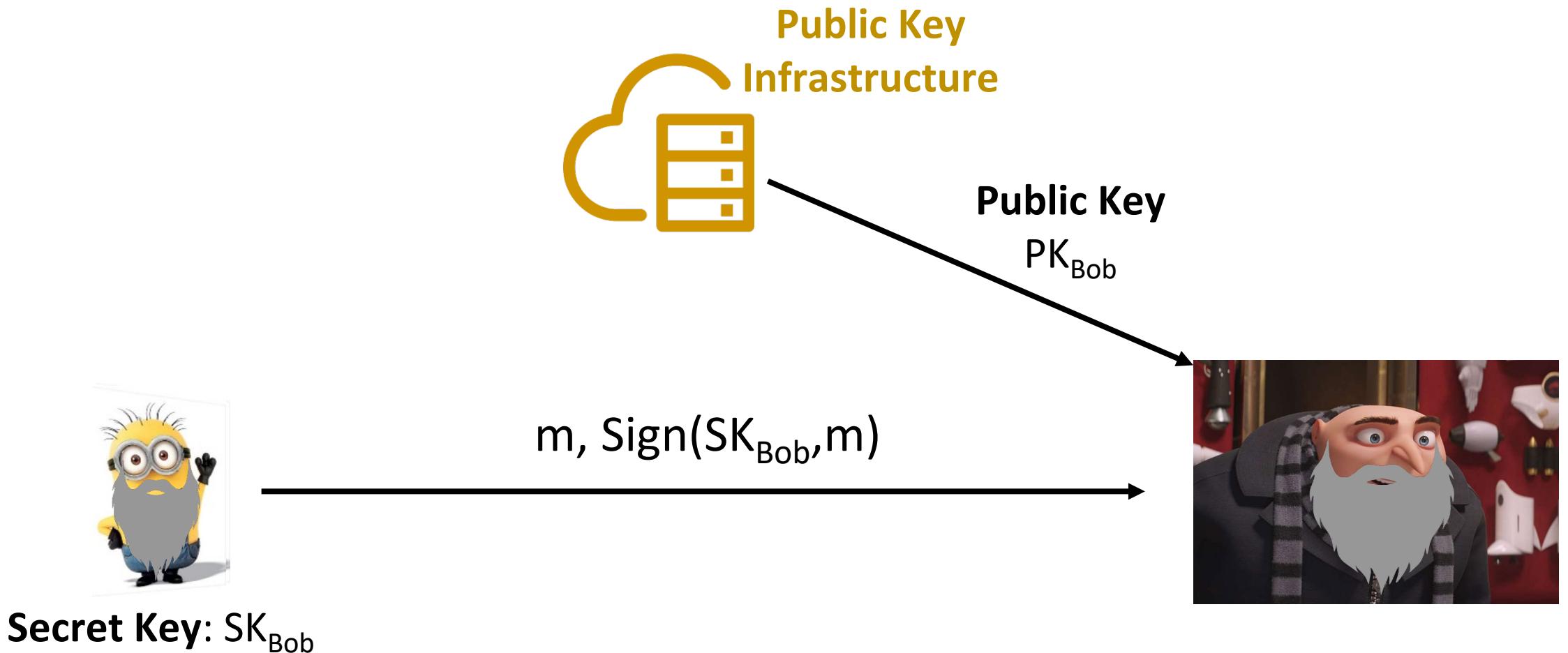
Sign hash of messages

Hybrid encryption
(only encrypt small symmetric key)

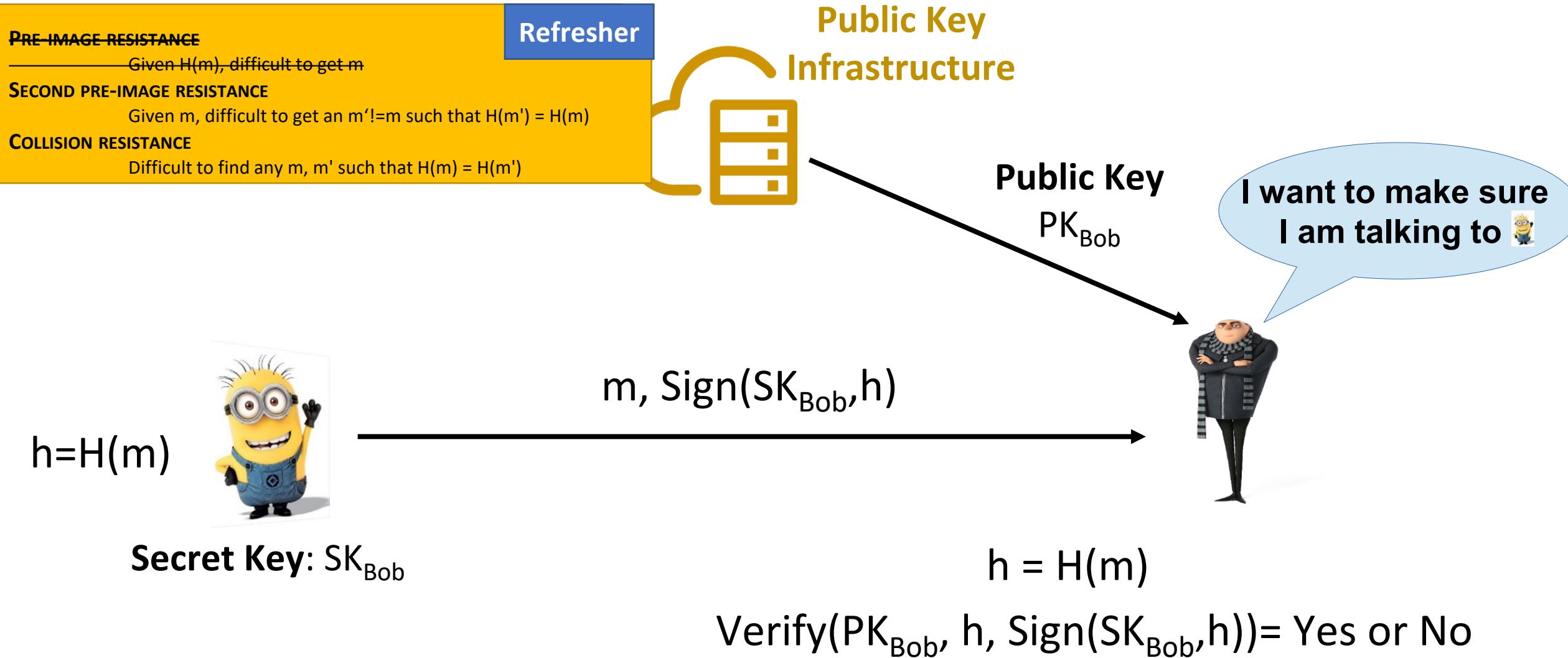
Digital signatures on hash functions



Digital signatures on hash functions



Digital signatures on hash functions



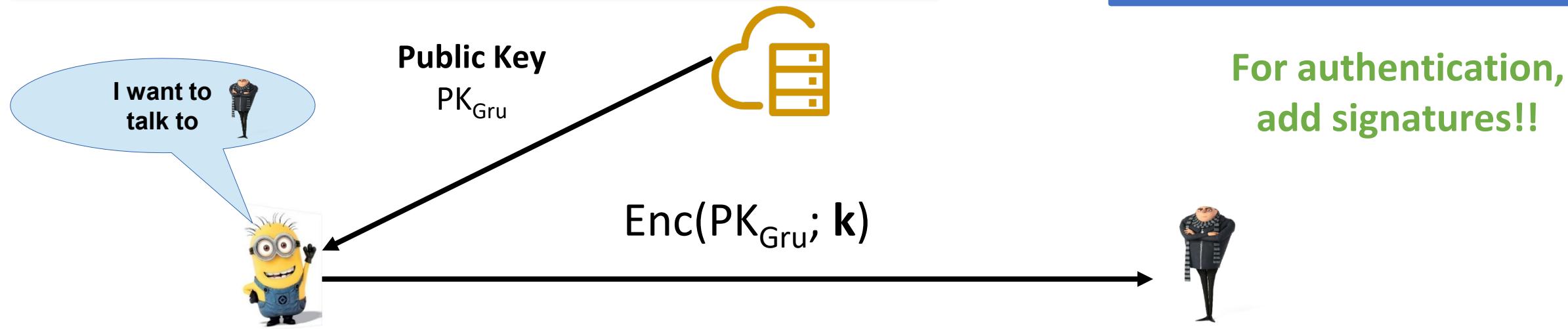
Hybrid encryption

Asymmetric encryption **is slow**, but symmetric **is fast!**

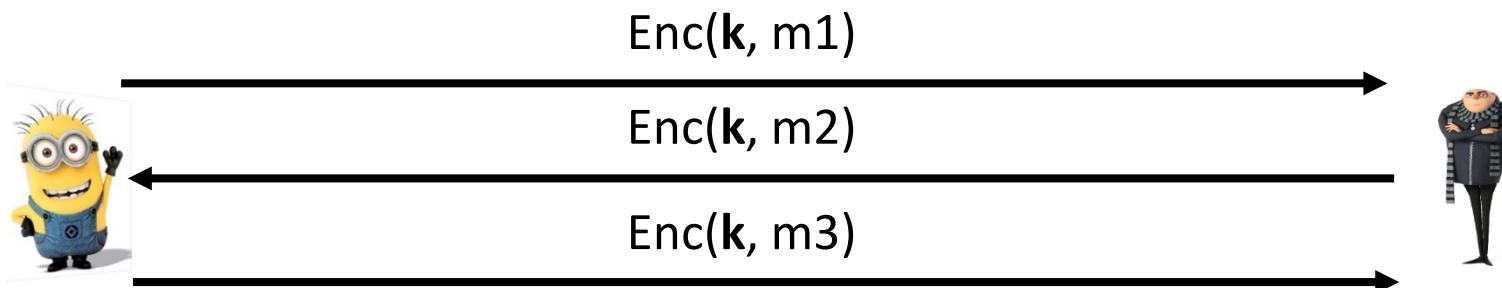
Step 1: establish a shared symmetric key k using “key transport”

Don't design
your own 

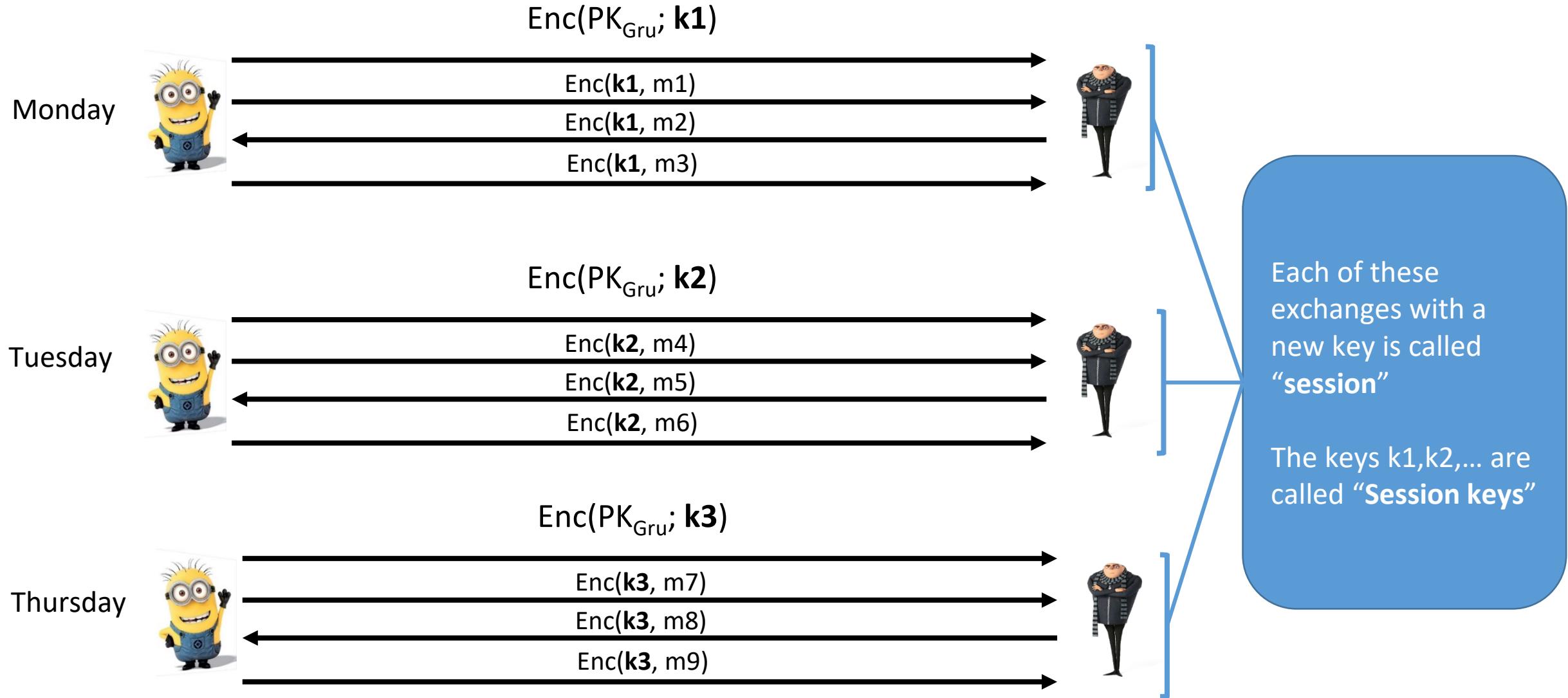
NOT SO SIMPLE!
e.g. ISO 9798-3
TLS



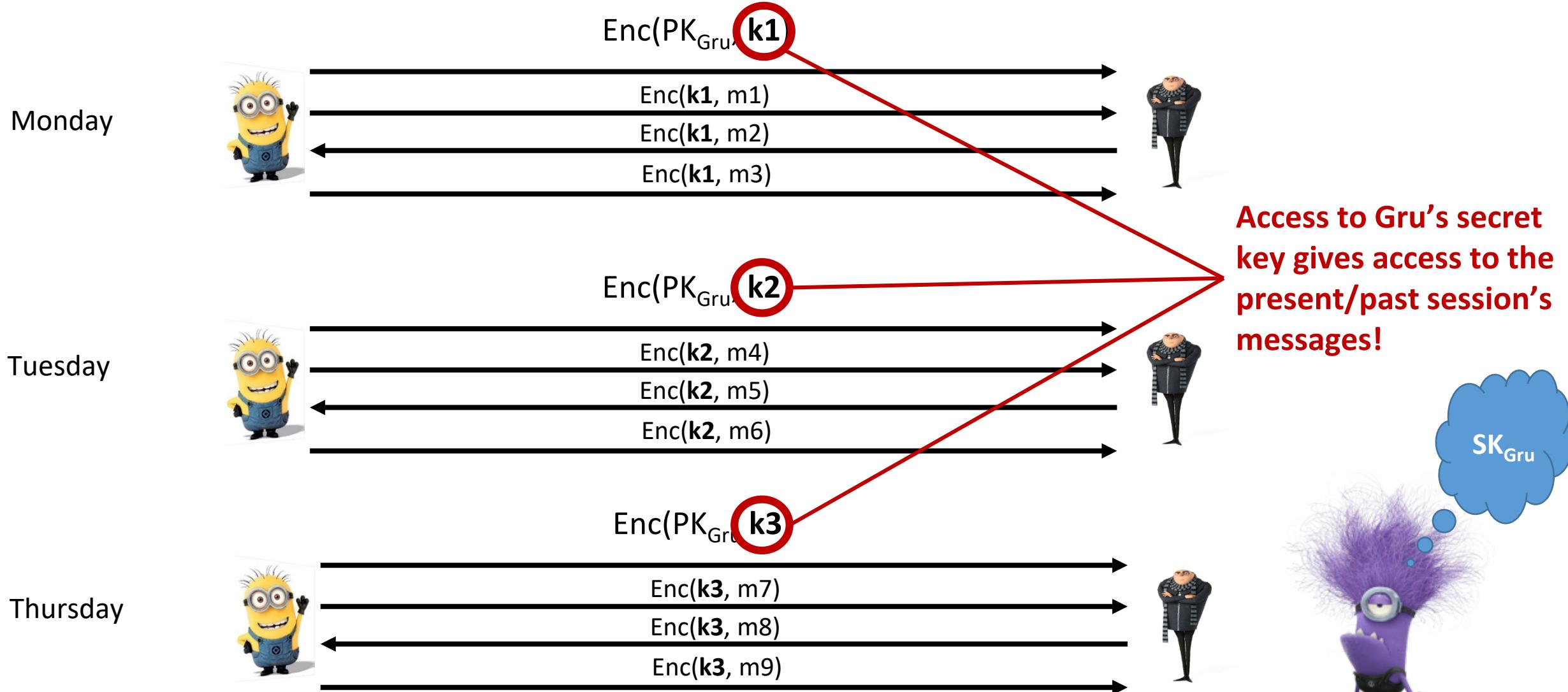
Step 2: use the shared symmetric key k to encrypt the rest of the communication



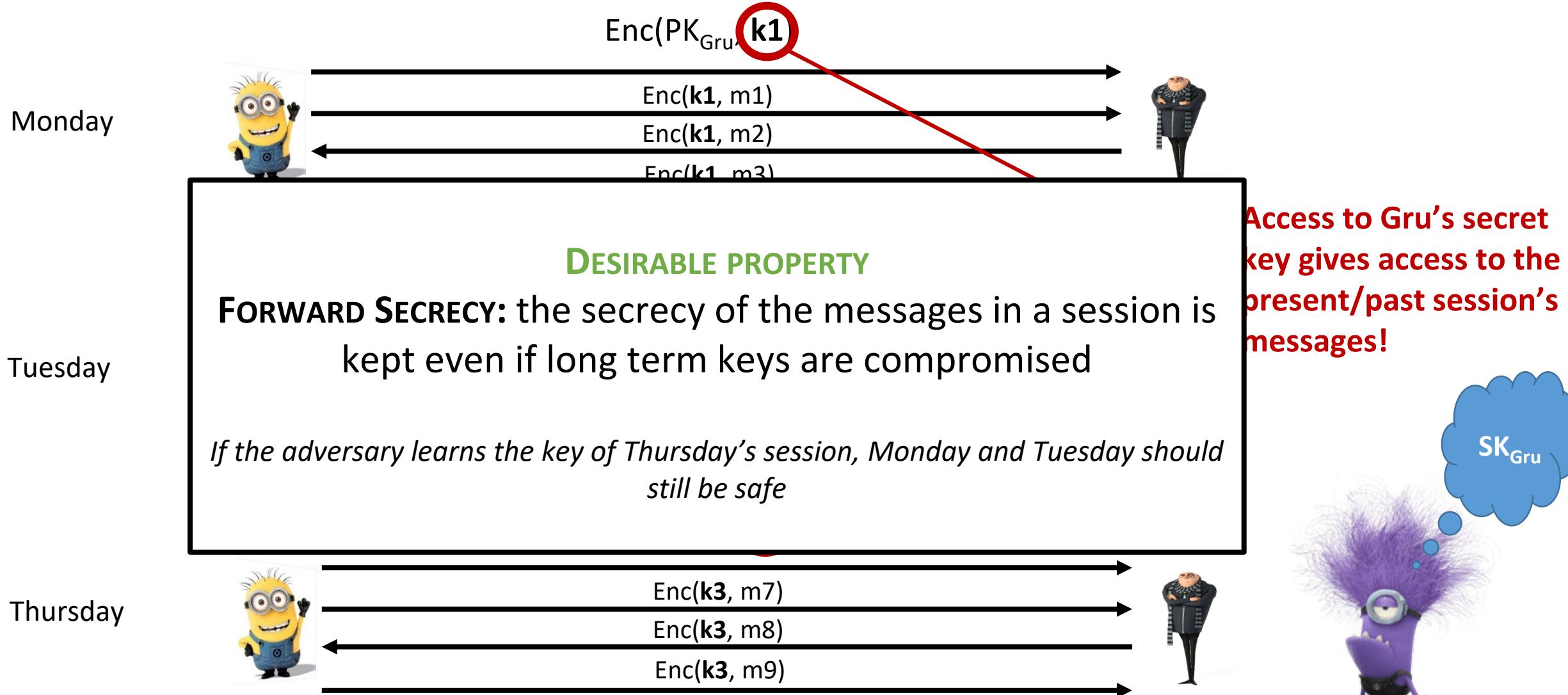
This process is repeated every time Bob wants to talk to Gru



What happens if the adversary gets access to Gru's asymmetric key on Thursday?



What happens if the adversary gets access to Gru's asymmetric key on Thursday?



Key agreement for forward secrecy – The Math

Arithmetic modulo a number: clock arithmetic

$$6 \pmod{12} = 6 \pmod{12}$$

$$12 \pmod{12} = 0 \pmod{12}$$

$$14 \pmod{12} = 2 \pmod{12}$$

Arithmetic modulo a large prime p (>1024 bits)

Addition and multiplication $(\pmod p)$ can be computed

Exponentiation can be computed [Given $(a, x) \rightarrow a^x \pmod p$?]

Discrete logarithms are **HARD!** [Given $(a, a^x \pmod p) \rightarrow x$?]

Basic Diffie-Hellman key exchange

Every time Bob wants to talk to Gru...

Shared **public** parameters p, g

Because of the discrete logarithm hardness, an adversary observing these values cannot recover x and y , therefore cannot compute k



Secret Key: x (random!)
 $(P_a)^x = g^{xy} \pmod{p}$

P_b
 P_a



Secret Key: y (random!)
 $(P_b)^y = g^{xy} \pmod{p}$

Shared secret!!
 $k = g^{xy} \pmod{p}$
To encrypt messages for the session

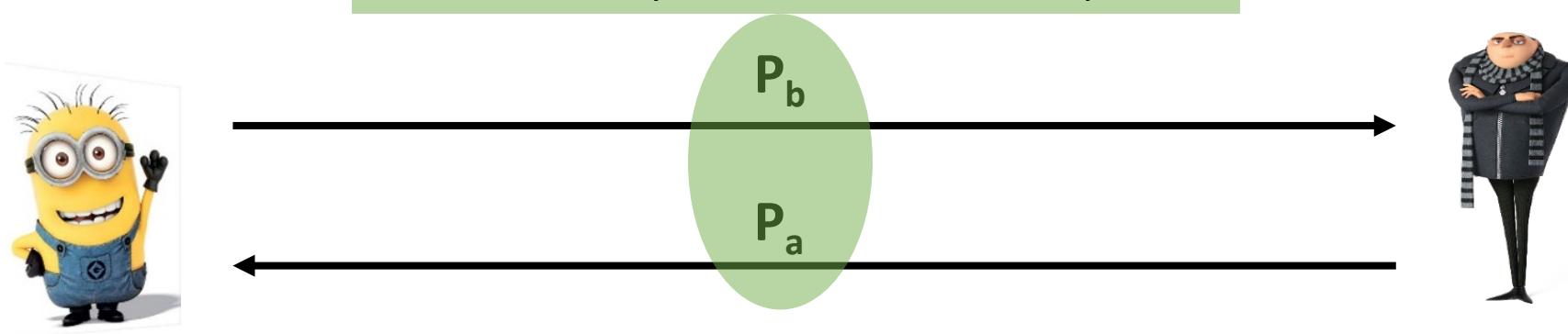
Basic Diffie-Hellman

Every time

After the session has ended, delete the secrets x and y.
The key can never be recovered.
Forward secrecy is achieved!!

Shared **public** parameters p , g

Because of the discrete logarithm hardness, an adversary observing these values cannot recover x and y, therefore cannot compute k



Secret Key: x (random!)
 $(P_a)^x = g^{xy} \pmod p$

Shared secret!!
 $k = g^{xy} \pmod p$

To encrypt messages for the session

Secret Key: y (random!)
 $(P_b)^y = g^{xy} \pmod p$

Summary of the crypto lectures

Symmetric cryptography

- Confidentiality: Stream ciphers, Block ciphers (modes of operation!)
- Integrity / Authentication: Message Authentication Codes (MACs)

Asymmetric cryptography

- Confidentiality: Encryption
- Integrity / Authentication: Digital signatures

Hybrid encryption
best both worlds!

Hash functions

- Three security properties
- Support Digital Signatures + other functions

Forward secrecy
Diffie Hellman

Why a MAC should not be constructed as $\text{Hash}(k||m)$



TAs & Carmela: Why are they designing their own crypto?!?!?
Why is this designing Crypto? You go from Hash to MAC.

COM-208 Computer networks!!

“Computer Networking: A Top-Down Approach”: $\text{MAC} = \text{Hash}(k||\text{I am Alice})$

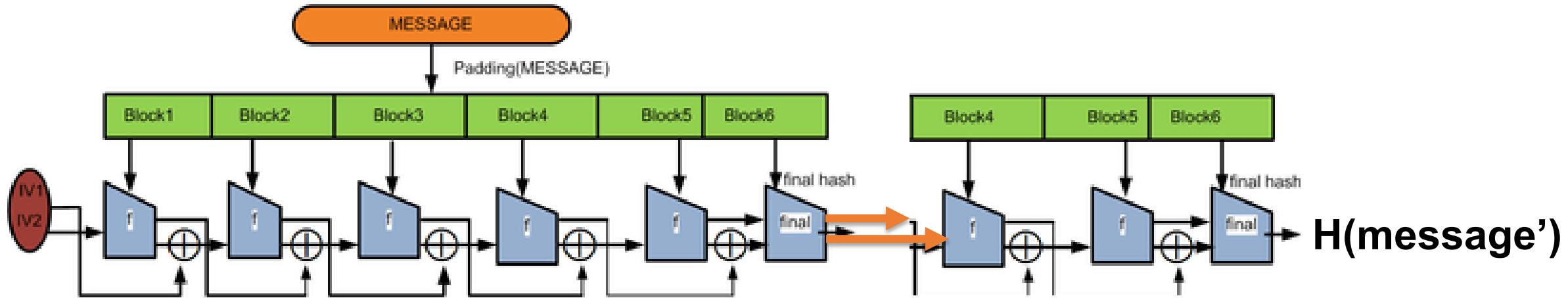


Is it wrong?!?!?!
Short answer: Not always
So when is it wrong?

Not exam material!!

Why a MAC should not be constructed as Hash($k||m$)

Many Hash functions (MD5, SHA1, SHA256) are built using **the Merkle-Damgard paradigm**



Hash length extension attacks! (given $H(m)$ obtain $H(m||stuff)$)

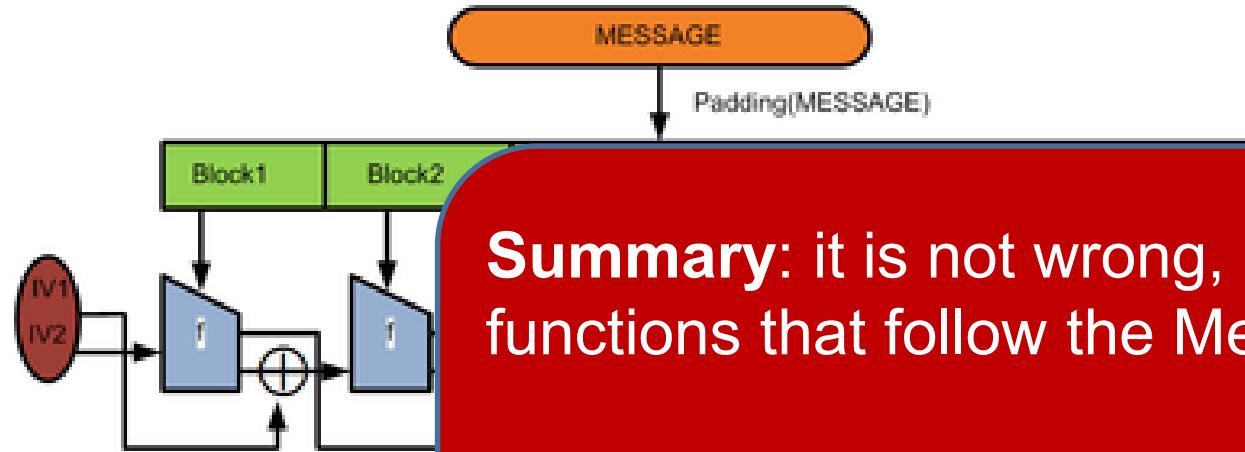
Example: $H(k||\text{this is Alice}) \rightarrow H(k||\text{this is Alice, First of her name, Queen of the Andals and the First Men})$

**MAC= $H(k||Alice)$ does not guarantee integrity
for Merkle-Damgard hash functions**

Not exam
material!!

Why a MAC should not be constructed as $\text{Hash}(k||m)$

Many Hash functions (MD5, SHA1, SHA256) are built using **the Merkle-Damgard paradigm**



Summary: it is not wrong, but there are **many** hash functions that follow the Merkle-Damgard paradigm.

Safe choice: don't do this.

If you want an HMAC, use a standardized one
e.g. <https://datatracker.ietf.org/doc/html/rfc2104>

Example: $H(k||\text{this is a test} || \text{stuff})$

MAC= $H(k||\text{Alice})$ does not guarantee integrity for Merkle-Damgard hash functions

Not exam material!!