

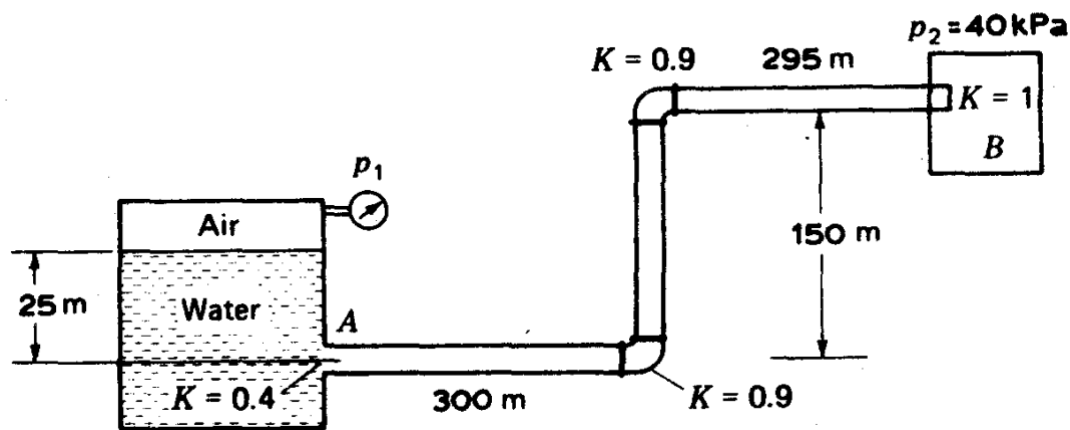
ChE 204 – Introduction to Transport Phenomena

Mid-term Exam

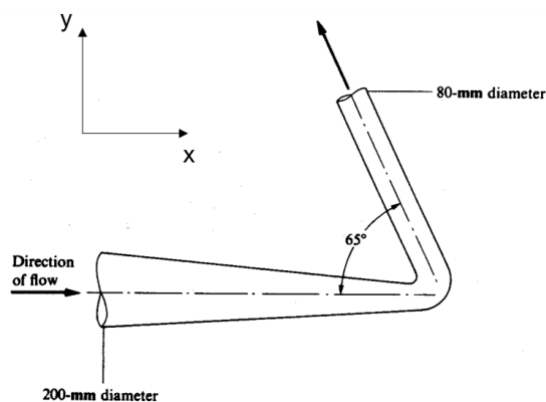
Question 1:

The system below carries water ($\rho = 1000 \text{ kg/m}^3$; $g = 9.8 \text{ m/s}^2$; $\mu = 8.9 \times 10^{-4} \text{ Pa}\cdot\text{s}$) at a volumetric rate of $0.1 \text{ m}^3/\text{s}$. If the pipe is stainless steel and has a diameter of 150mm, calculate the pressure P_1 in the following cases:

- neglecting losses
- including losses
- if water was finally discharged to the atmosphere in B (exclude losses)



Question 2:



The pipe bend on the left is in a horizontal plane. Water ($\rho = 1000 \text{ kg/m}^3$; $g = 9.8 \text{ m/s}^2$) enters the bend with a velocity of 3.5 m/s and a pressure of 280 kPa . Neglecting any energy losses in the bend, find the force required to hold the bend in place.

Question 3:

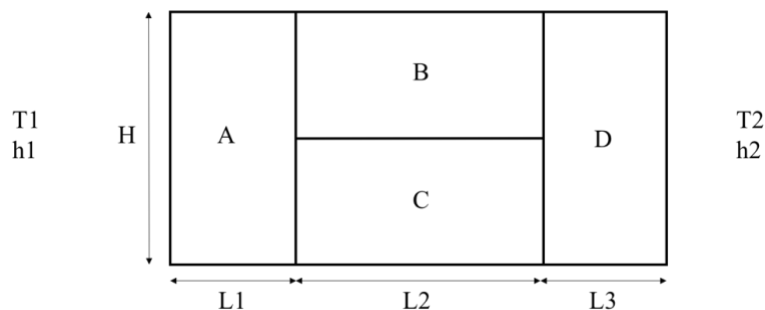
In a textile manufacturing plant, the waste dyeing water ($C_{p,h} = 4295 \text{ J/kg} \cdot ^\circ\text{C}$) at 75°C is to be used to preheat fresh water ($C_{p,c} = 4180 \text{ J/kg} \cdot ^\circ\text{C}$) at 15°C at the same flow rate of 2 kg/s in a double-pipe parallel flow heat exchanger. The overall heat transfer coefficient is $625 \text{ W/m}^2 \cdot ^\circ\text{C}$ and that the rate of heat transfer is 35 kW .

- Calculate the outlet temperatures of each fluid stream
- Calculate the heat transfer area
- Knowing that $h_h = 1350 \text{ W/m}^2 \cdot ^\circ\text{C}$, $h_c = 1500 \text{ W/m}^2 \cdot ^\circ\text{C}$ and the thickness of the inner tube wall is 0.1 m , find the thermal conductivity of the inner tube wall.

Question 4:

Consider the composite wall illustrated below for high $H = 3 \text{ m}$, thickness 1 m , $H_B = H_C = 1.5 \text{ m}$, $L_1 = L_3 = 0.05 \text{ m}$, $L_2 = 0.1 \text{ m}$, $k_A = k_D = 50 \text{ W/mK}$, $k_B = 10 \text{ W/mK}$ and $k_C = 1 \text{ W/mK}$.

- Sketch the thermal resistance circuit.
- Under conditions for which $T_1 = 200^\circ\text{C}$, $h_1 = 50 \text{ W/m}^2\text{K}$, $T_2 = 25^\circ\text{C}$ and $h_2 = 10 \text{ W/m}^2\text{K}$, what is the rate of heat transfer through the wall ?
- What are the interface temperatures ?



Introduction to Transport Phenomena: Solutions to mid-term exam

Question 1

$$\text{pipe area} = \pi \times r^2$$

$$A = \pi \times 0. \frac{15^2}{4} = 0.0176 \text{ m}^2$$

$$\text{velocity} = Q \times \frac{1}{A}$$

$$\text{velocity} = 0.1 \times \frac{1}{0.0176} = 5.68 \frac{\text{m}}{\text{s}}$$

a) Applying Bernoulli between point 1 and point 2

$$P_1 + \rho \cdot g \cdot h_1 + \frac{1}{2} \cdot \rho \cdot v_1^2 = P_2 + \rho \cdot g \cdot h_2 + \frac{1}{2} \cdot \rho \cdot v_2^2$$

$$P_1 + \rho \cdot g \cdot 25 = 40 \times 10^3 + \rho \cdot g \cdot 150 + \frac{1}{2} \cdot \rho \cdot 5.68^2$$

$$P_1 = 1.28 \text{ MPa}$$

- b) Now we must consider losses, so calculating the Reynolds number, relative roughness and the fanning friction factor

$$R_e = \rho \times v \times \frac{D}{\mu}$$

$$R_e = 1000 \times 5.68 \times 0. \frac{15}{8.9 \times 10^{-4}} = 10^6$$

$$\frac{\varepsilon}{D} = 0. \frac{015}{150} = 10^{-4}$$

Checking the corresponding value on the moody chart for the fanning friction factor,

$$f_f = 0.0035$$

$$P_1 + \rho \cdot g \cdot h_1 + \frac{1}{2} \cdot \rho \cdot v_1^2 = P_2 + \rho \cdot g \cdot h_2 + \frac{1}{2} \cdot \rho \cdot v_2^2 + \frac{1}{2} \cdot \rho \cdot v_2^2 \left(\frac{4f_f}{D} \cdot \left(\sum L_i \right) + \sum K_j \right)$$

1 pts

$$P_1 + \rho \cdot g \cdot 25 = \rho \cdot g \cdot 150 + \frac{1}{2} \cdot \rho \cdot 5.68^2 + 40 \times 10^3 + \frac{1}{2} \cdot \rho \cdot 5.68^2 \left(4 \times \frac{f_f}{0.15} (300 + 150 + 295) \right) + (0.4 + 0.9 + 0.9 + 1)$$

$$P_1 = 2.35 \text{ MPa}$$

- c) Essentially same as part 1, just P_2 changes to atmospheric pressure

$$P_1 + \rho \cdot g \cdot h_1 + \frac{1}{2} \cdot \rho \cdot v_1^2 = P_2 + \rho \cdot g \cdot h_2 + \frac{1}{2} \cdot \rho \cdot v_2^2$$

$$P_1 + \rho \cdot g \cdot 25 = 100 \times 10^3 + \rho \cdot g \cdot 150 + \frac{1}{2} \cdot \rho \cdot 5.68^2$$

$$P_1 = 1.34 \text{ MPa}$$

Question 2

$$v_1 = 3.5 \frac{m}{s}$$

$$P_1 = 280 \text{ kPa}$$

In order to determine the anchoring force, we need to resolve the forces along x and y directions.

$$\Sigma F_{reaction} + \Sigma F_{pressure} + \Sigma F_{friction} = \Sigma F_{surface}$$

$$\Sigma F_{friction} = 0$$

$$\Sigma F_{reaction} + (-P_1 A_1 \hat{n}_1) + (-P_2 A_2 \hat{n}_2) = \int_{A_1} \rho v_1 (v_1 \cdot \hat{n}_1) dA_1 + \int_{A_2} \rho v_2 (v_2 \cdot \hat{n}_2) dA_2$$

We need to calculate P_2 and v_2 .

Because of the continuity equation: $A_1 v_1 = A_2 v_2$

$$3.5 \times 0.2^2 = v_2 \times 0.08^2$$

$$v_2 = 21.875 \text{ m/s}$$

Regarding P_2 , we apply Bernoulli's principle:

$$\begin{array}{ccc} 0 & & 0 \\ \nearrow & & \nearrow \\ P_1 + \frac{1}{2} \rho \cdot v_1^2 + \rho \cdot g \cdot h_1 & = & P_2 + \frac{1}{2} \rho \cdot v_2^2 + \rho \cdot g \cdot h_2 \end{array}$$

$$280000 + 0.5 \times 1000 \times 3.5^2 = P_2 + 0.5 \times 1000 \times 21.875^2$$

$$P_2 = 46.86 \text{ kPa}$$

Resolving the forces along the +x direction:

$$\Sigma F_{reaction,x} - P_1 A_1 (-1) - P_2 A_2 (-1) \cos 65^\circ = -\rho v_1^2 A_1 - \rho v_2^2 A_2 \cos 65^\circ$$

$$\Sigma F_{reaction,x} = -P_1 A_1 - P_2 A_2 \cos 65^\circ - \rho v_1^2 A_1 - \rho v_2^2 A_2 \cos 65^\circ$$

$$= -A_1(P_1 + \rho v_1^2) - A_2 \cos 65^\circ (P_2 + \rho v_2^2)$$

$$= -3.14(0.1)^2(280000 + 1000 \times 3.5^2) - 3.14(0.04)^2 \times 0.42 \times (46860 + 1000 \times 21.875^2)$$

$$= -10200.04 \text{ N} = -10.2 \text{ kN}$$

Resolving the forces along the +y direction:

$$\Sigma F_{\text{reaction},y} + 0 - P_2 A_2 (+1) \sin 65^\circ = 0 + \rho v_2^2 A_2 \sin 65^\circ$$

$$\Sigma F_{\text{reaction},y} = A_2 \sin 65^\circ (P_2 + \rho v_2^2)$$

$$= 3.14 \times (0.04)^2 \times 0.9(46860 + 1000 \times 21.875^2)$$

$$= 2375.53 \text{ N} = 2.375 \text{ kN}$$

$$F_{\text{net}} = \sqrt{(F_{\text{reaction},x}^2 + F_{\text{reaction},y}^2)} = ((-10200.04)^2 + (2375.53)^2)^{1/2}$$

$$= 10473 \text{ N} = 10.473 \text{ kN}$$

Question 3:

$$a) \dot{Q} = 35000W = \dot{m}c_{p,h}(T_{h,i} - T_{h,o})$$

$$35000 = 2 * 4295 * (75 - T_{h,o})$$

$$T_{h,o} = 75 - \left(\frac{35000}{2 * 4295}\right)$$

$$T_{h,o} = 75 - 4.07 = 70.93^{\circ}\text{C}$$

$$\text{Similarly, } \dot{Q} = 35000W = \dot{m}c_{p,c}(T_{c,o} - T_{c,i})$$

$$35000 = 2 * 4295 * (T_{c,o} - T_{c,i})$$

$$T_{c,o} = 15 + \left(\frac{35000}{2 * 4295}\right)$$

$$T_{c,o} = 15 + 4.07 = 19.07^{\circ}\text{C}$$

b) Parallel flow recognition

$$\Delta T_{LMTD} = \frac{(T_{h,i} - T_{c,i}) - (T_{h,o} - T_{c,o})}{\ln \left(\frac{T_{h,i} - T_{c,i}}{T_{h,o} - T_{c,o}}\right)} = \frac{(75-15) - (71-19)}{\ln \left(\frac{75-15}{71-19}\right)} = 57.1^{\circ}\text{C}$$

$$Area = \frac{\dot{Q}}{U \Delta T_{LMTD}} = \frac{35000}{625 * 57.1} = 0.98m^2$$

c)

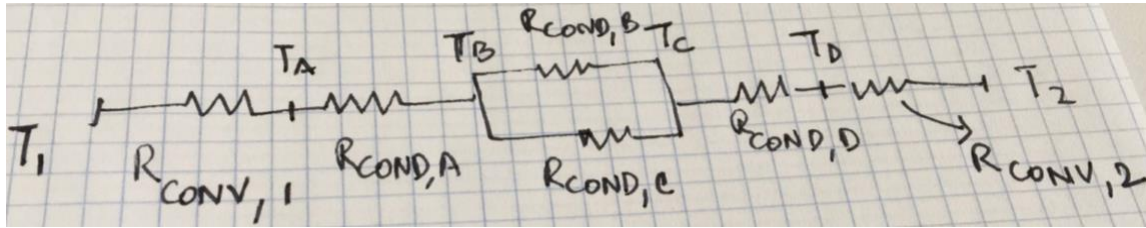
$$\frac{1}{U} = \frac{1}{h_h} + \frac{0.1}{k} + \frac{1}{h_c}$$

$$\frac{1}{625} = \frac{1}{1350} + \frac{0.1}{k} + \frac{1}{1500}$$

So, we get **k=500Wm⁻¹°C**

Question 4:

a)



b)

$$R_{tot} = \frac{1}{h_1 A_1} + \frac{L_A}{k_A A_A} + \frac{1}{\frac{k_B A_B}{L_B} + \frac{k_C A_C}{L_C}} + \frac{L_D}{k_D A_D} + \frac{1}{h_2 A_2}$$

$$R_{tot} = \frac{1}{50 * 3} + \frac{0.05}{50 * 3} + \frac{1}{\frac{10 * 1.5}{0.1} + \frac{1 * 1.5}{0.1}} + \frac{0.05}{50 * 3} + \frac{1}{10 * 3}$$

$$R_{tot} = 0.0067 + 0.0003 + 0.0060 + 0.0003 + 0.0333 = 0.0466^\circ\text{CW}^{-1}$$

$$\dot{Q} = \frac{\Delta T}{R_{tot}} = \frac{200 - 25}{0.0466} = \mathbf{3755.4 \text{ W}}$$

c)

For the interface temperatures,

$$\dot{Q} = h_1 A_1 (T_1 - T_A)$$

$$\text{So, } T_A = T_1 - \frac{\dot{Q}}{h_1 A_1} = 200 - \frac{3755.4}{50 * 3} = \mathbf{174.96^\circ\text{C}}$$

$$\text{Similarly, } \dot{Q} = h_2 A_2 (T_D - T_2)$$

$$\text{So, } T_D = T_2 + \frac{\dot{Q}}{h_2 A_2} = 25 + \frac{3755.4}{10 * 3} = \mathbf{150.18^\circ\text{C}}$$

$$T_B = T_A - \frac{\dot{Q}}{\frac{k_A A_A}{L_A}}$$

$$T_B = 174.96 - R_{COND,A} \dot{Q} = 174.96 - 0.0003 * 3755.4 = \mathbf{173.8}$$

Similarly,

$$T_C = T_D + R_{COND,D} \dot{Q} = 150.18 + 0.0003 * 3755.4 = \mathbf{151.3^\circ\text{C}}$$