

## **7. Applications of absorption and fluorescence spectroscopies in photomedicine**

### **7.1 Molecular Energy Levels**

- A. Different energy levels**
- B. Electronic (and vibrational) energy levels**
- C. Population of energy levels**

# Energy Levels

## A. Different energy levels

$$E_{\text{molecule}} = E_{\text{translation}} + E_{\text{electron spin}} + E_{\text{nuclear spin}} + E_{\text{rotation}} + E_{\text{vibration}} + E_{\text{electronic}}$$

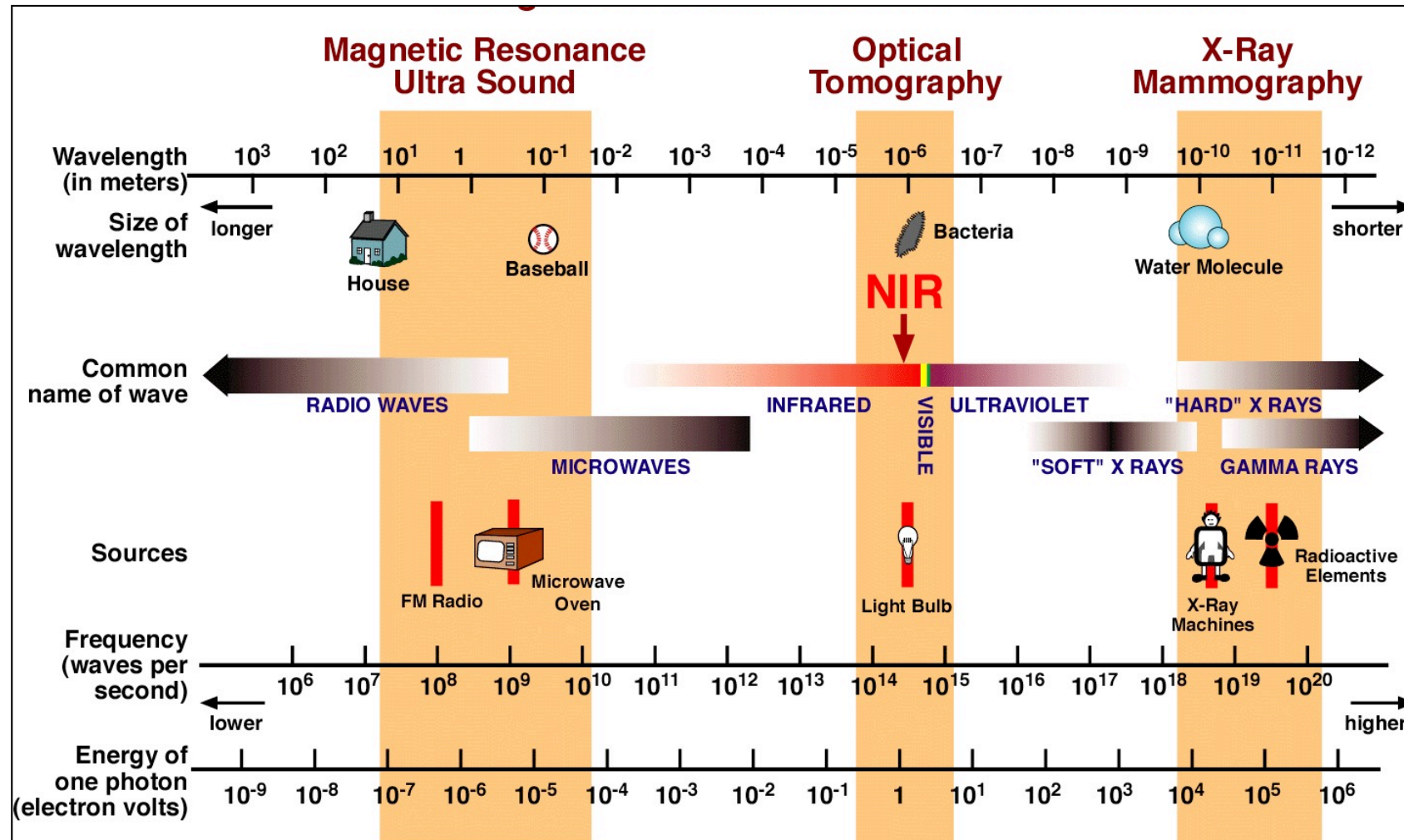
- Translational energy: motion of the molecule's center of mass through space
- Spin energy: nuclear and electron spin
- Rotational energy: rotation of the molecule about its center of mass
- Vibrational energy: vibration of the molecule's constituent atoms
- Electronic energy: mutual interactions of the molecules electrons and nuclei

The energy associated with each of these levels is quantized.  
They are associated to orbitals

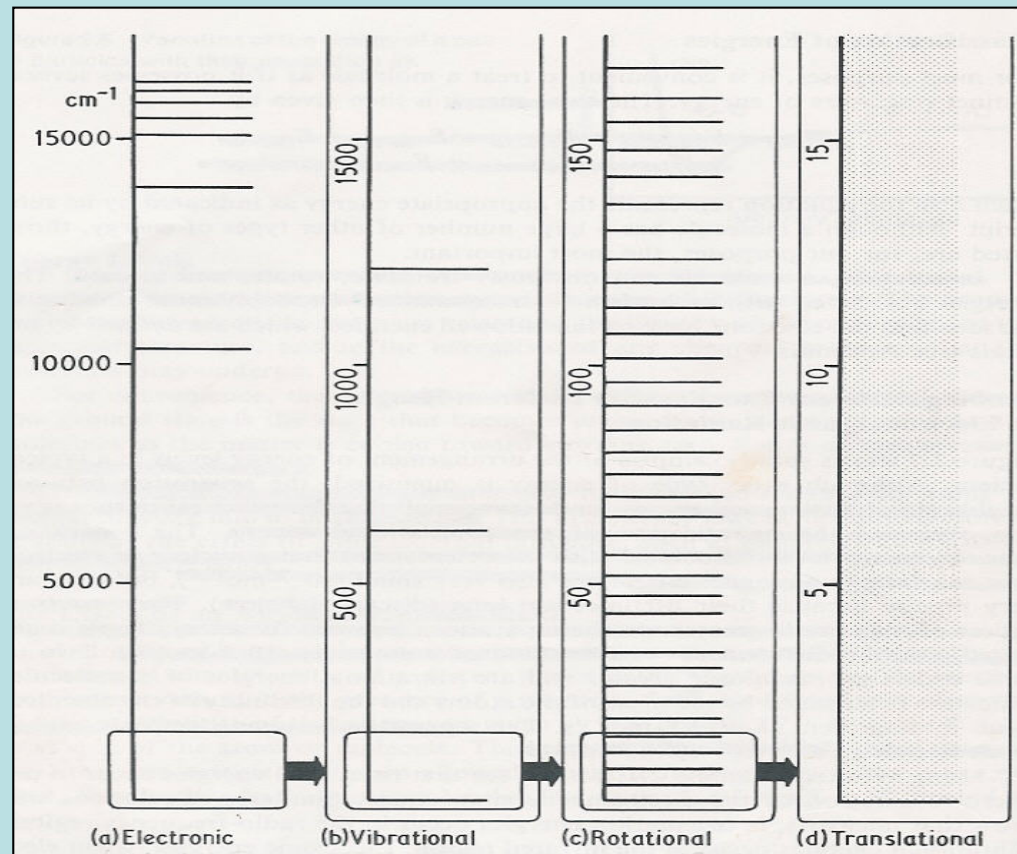
# Energy Levels

Energy	Energy Level Separation [J]
Translation	Very small
Spin	$10^{-25}$
Rotation	$10^{-22}$
Vibration	$10^{-20}$
Electronic	$10^{-19}$

# Energy Levels



# Energy Levels

 $\text{cm}^{-1}$ 

**Common spectroscopists unit, wavenumber =  $1 / \text{wavelength}$ , so proportional to frequency and energy**

# Energy Levels

## B. Electronic energy levels

(The most important energy levels in photomedicine)

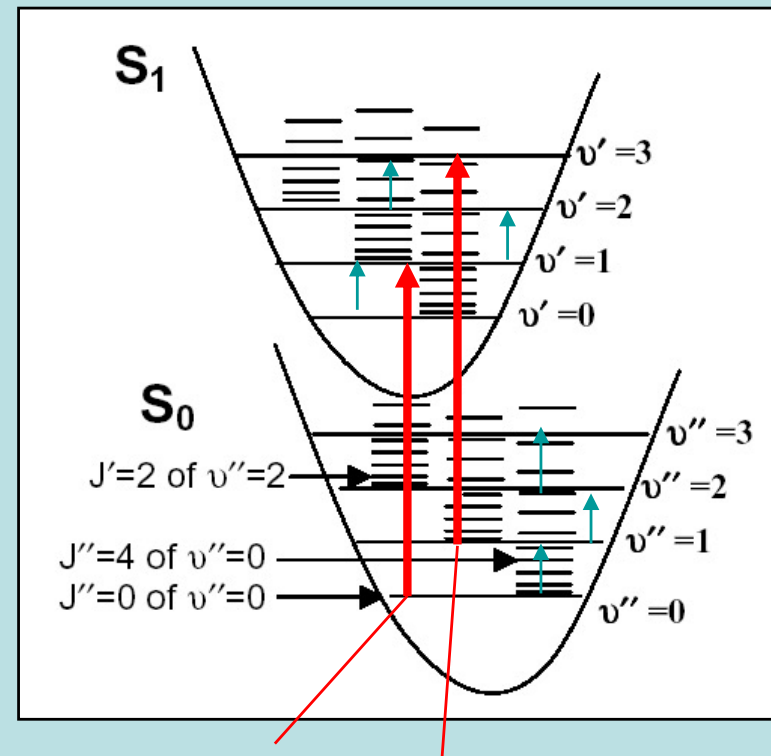
- In particular, UV-VIS absorption / fluorescence spectroscopy involves electronic energy transitions
- 
- Electronic energy levels of molecules are described by molecular orbitals
  - When an electron undergoes an electronic transition, it is transferred from one molecular orbital to another

# Infrared Absorption Spectroscopy

## Infrared absorption

IR radiation does not have enough energy to induce electronic transitions as seen with UV. Absorption of IR is restricted to compounds with small energy differences in the possible vibrational and rotational states.

<http://www.shu.ac.uk/schools/sci/chem/tutorials/molspec/irspec1.htm>

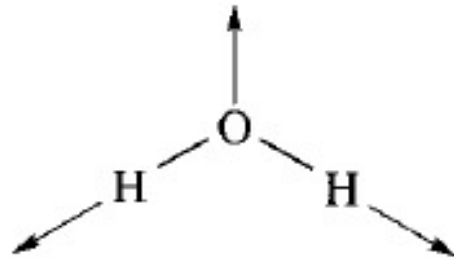


Electronic transition

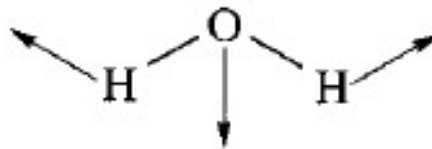
# Vibrational States of a Molecule

## More general cases

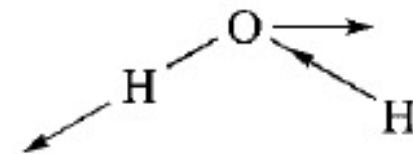
Normal modes of vibration of a water molecule:



Symmetric Stretch  
 $\nu_1 = 3652 \text{ cm}^{-1}$



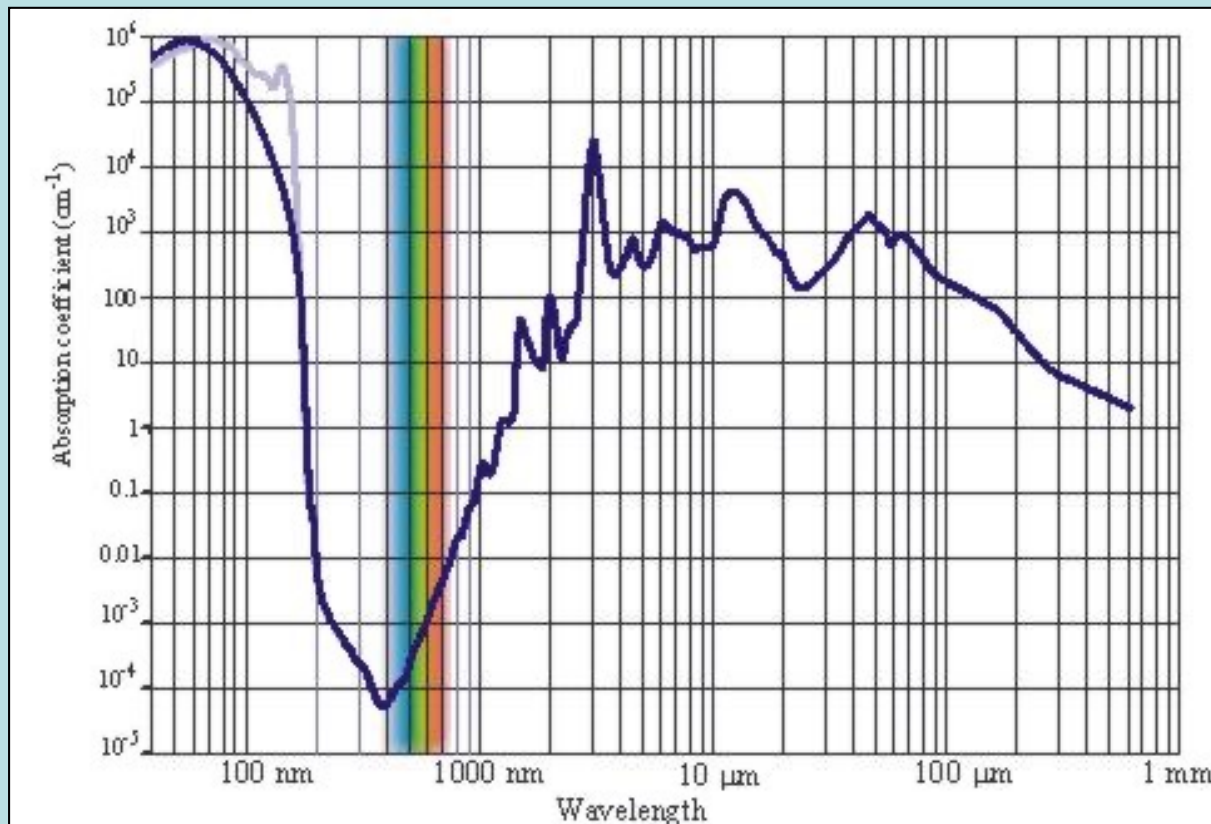
Symmetric Bend  
 $\nu_2 = 1595 \text{ cm}^{-1}$



Unsymymmetric Stretch  
 $\nu_3 = 3756 \text{ cm}^{-1}$

# Infrared Absorption Spectroscopy

**Water (major chromophore in biological samples) absorption**



Water absorption spectrum - note absorption peaks at 1.45, 1.94, 2.94, 4.5 and 6 microns !

# Water absorption in the visible



# Absorption imaging in the visible and IR



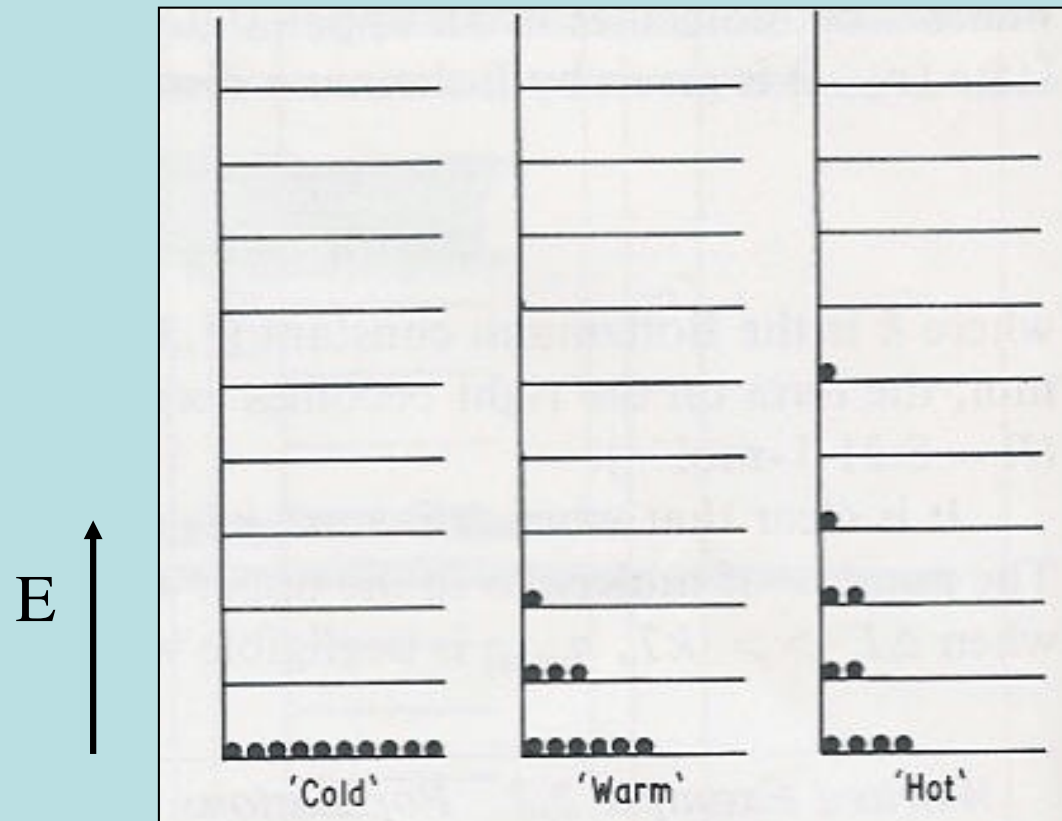
# Energy Levels

## C. Population of energy levels

- At any finite temperature ( $T$ ), molecules will be distributed among available  $E$  levels due to thermal agitation
- The exact distribution among energy levels will depend upon the temperature and separation between energy levels

# Energy Levels

## Population of energy levels



# Energy Levels

## Population of energy levels

- At any finite temperature (T), the molecules in an upper state ( $n_{\text{upper}}$ ) relative to the number in a lower state ( $n_{\text{lower}}$ ) is given by the Boltzmann's distribution:

$$\frac{n_{\text{upper}}}{n_{\text{lower}}} = \exp\left(-\frac{\Delta E}{kT}\right)$$

$k=1.38 \times 10^{-23} \text{ JK}^{-1}$  (Boltzmann's constant)

$\Delta E$  = separation in energy level (HOMO–LUMO gap)

# Energy Levels

$$\frac{n_{upper}}{n_{lower}} = \exp\left(-\frac{\Delta E}{kT}\right)$$

$k = 1.38 \cdot 10^{-23} \text{ JK}^{-1}$  (Boltzmann's constant)

$\Delta E$  = separation in energy level (HOMO–LUMO gap)

If  $\Delta E = 1 \text{ eV}$  (energy difference between electronic states)

at physiological temperature:  $n_{upper}/n_{lower} = \exp(-40) = 1.6 \cdot 10^{-17}$

If  $\Delta E = 0.1 \text{ eV}$  (energy difference between vibrational states)

at physiological temperature:  $n_{upper}/n_{lower} = \exp(-4) = 0.02$

If  $\Delta E = 0.001 \text{ eV}$  (energy difference between rotational states)

at physiological temperature:  $n_{upper}/n_{lower} = \exp(-0.04) = 0.96$