

Course

# Denoising of Microscopy Images



# Noise in Bioimage

## Pushing the limits of imaging

- Low-light condition, low excitation
- High spatial resolution
- Long sequence: bleaching

## Degrading in multiple dimension

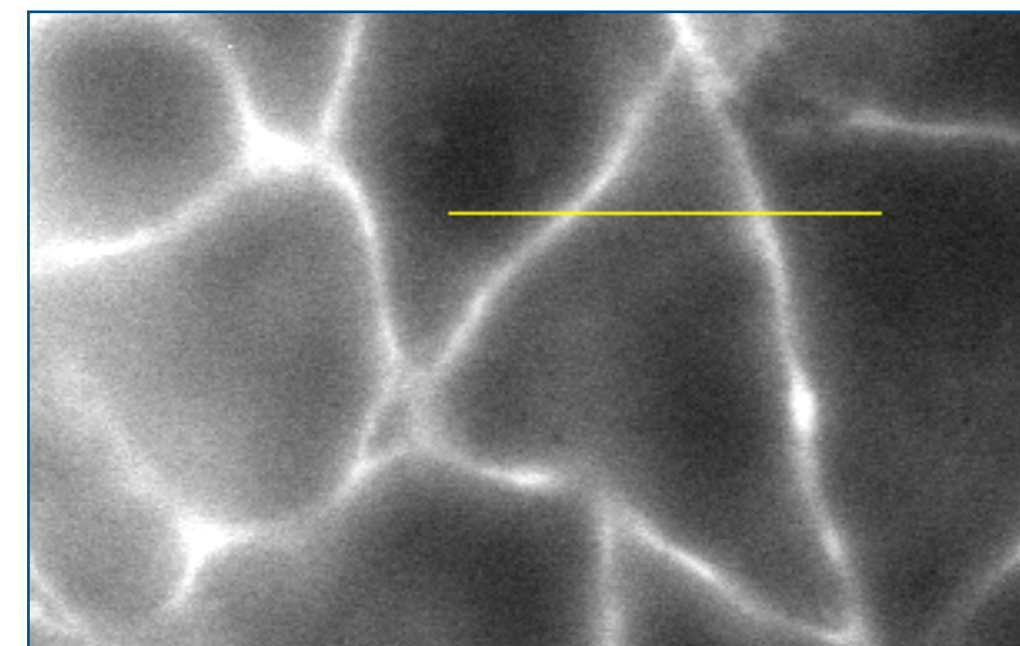
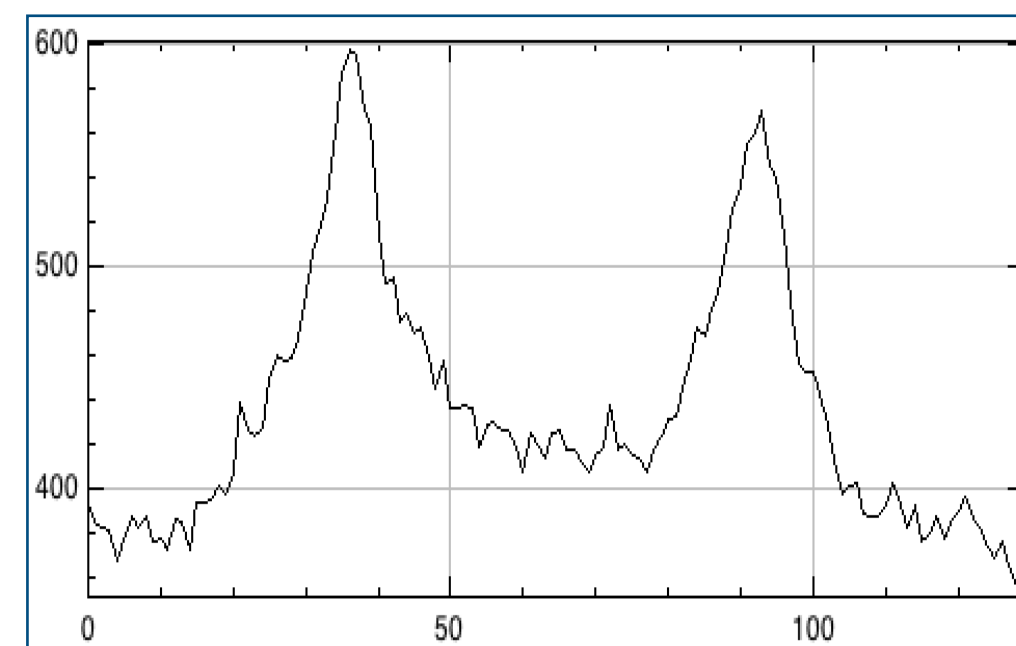
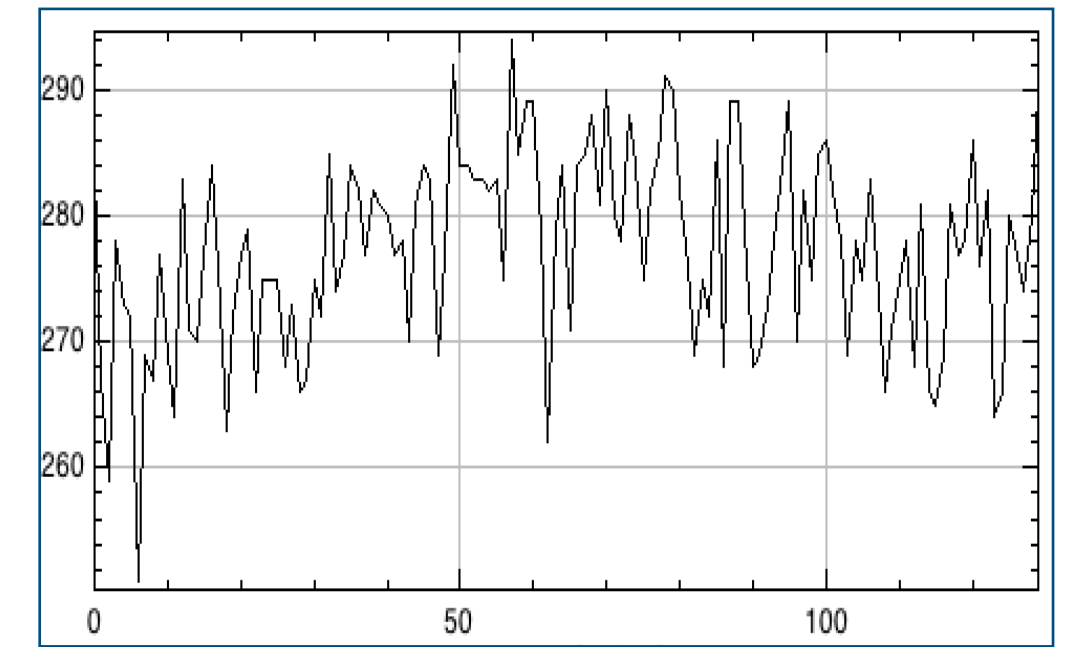
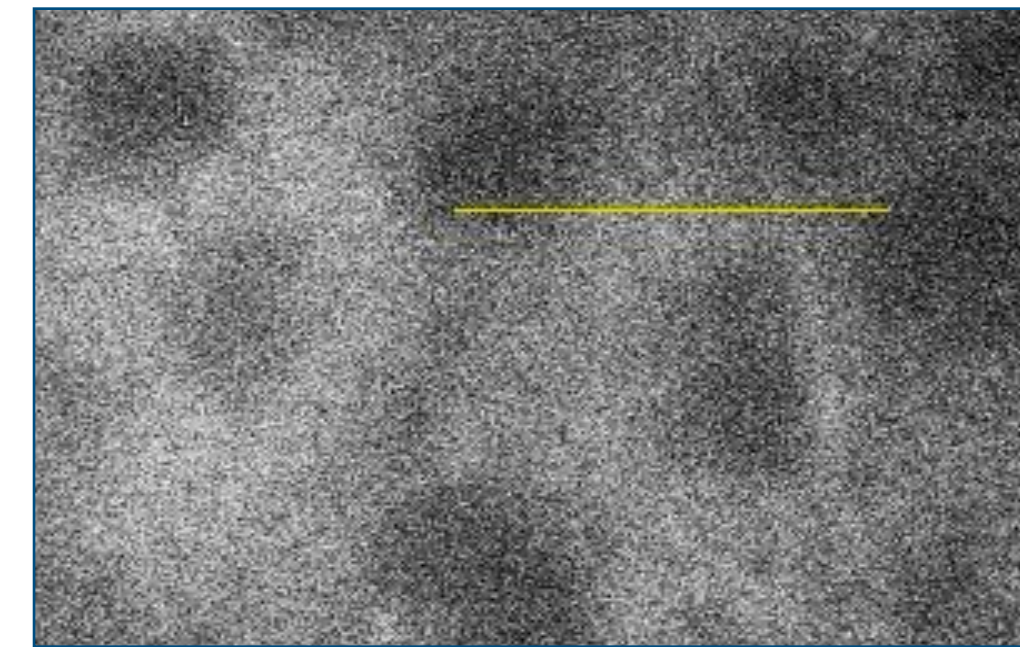
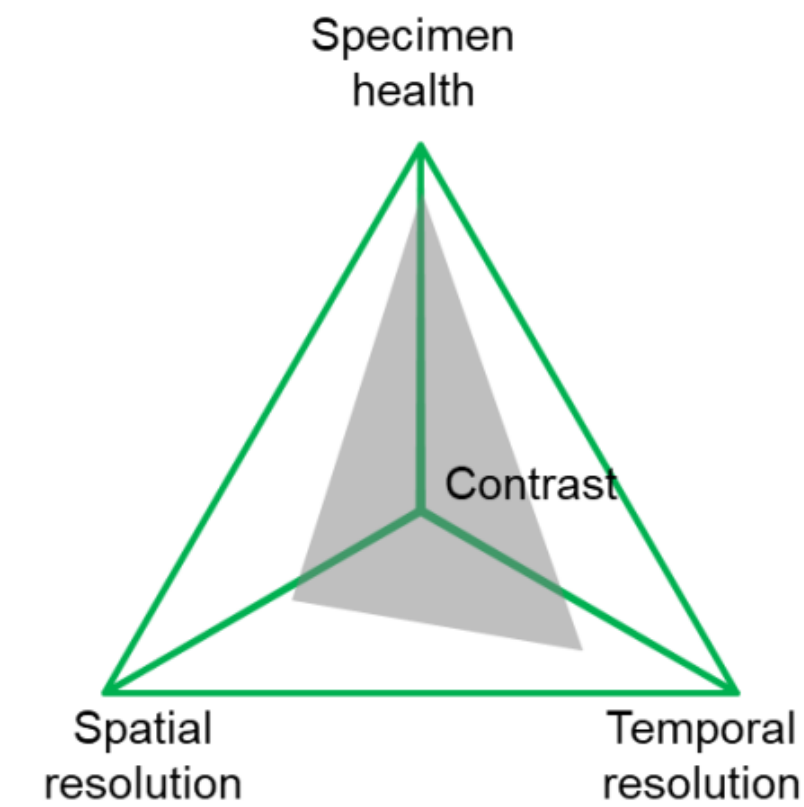
- Time: short exposure times
- Channel: bleed-through
- Depth: Scattering, less excitation

## Source of noise

- ▶ From the acquisition device
- ▶ From the camera/detector
- ▶ From the structure
- ▶ From the background

### Noise in microscopy

- ▶ Shot noise
- ▶ Dark current
- ▶ Read-out noise
- ▶ Spurious charge
- ▶ Thermal noise
- ▶ Quantization noise
- ▶ Dead pixels
- ▶ Stuck pixels
- ▶ Blocking JPEG

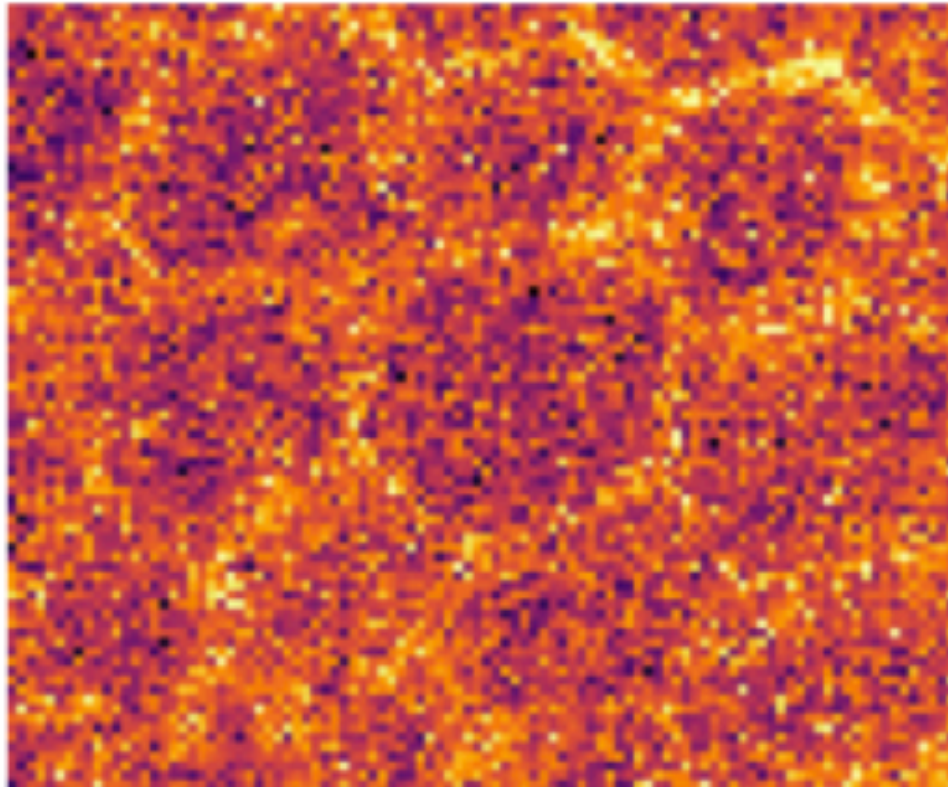


*Human are good to guess structures in noisy image*



# Noise Structure

## Pixelwise Noise



$$y[k] = x[k] + n[k]$$

### Signal prior

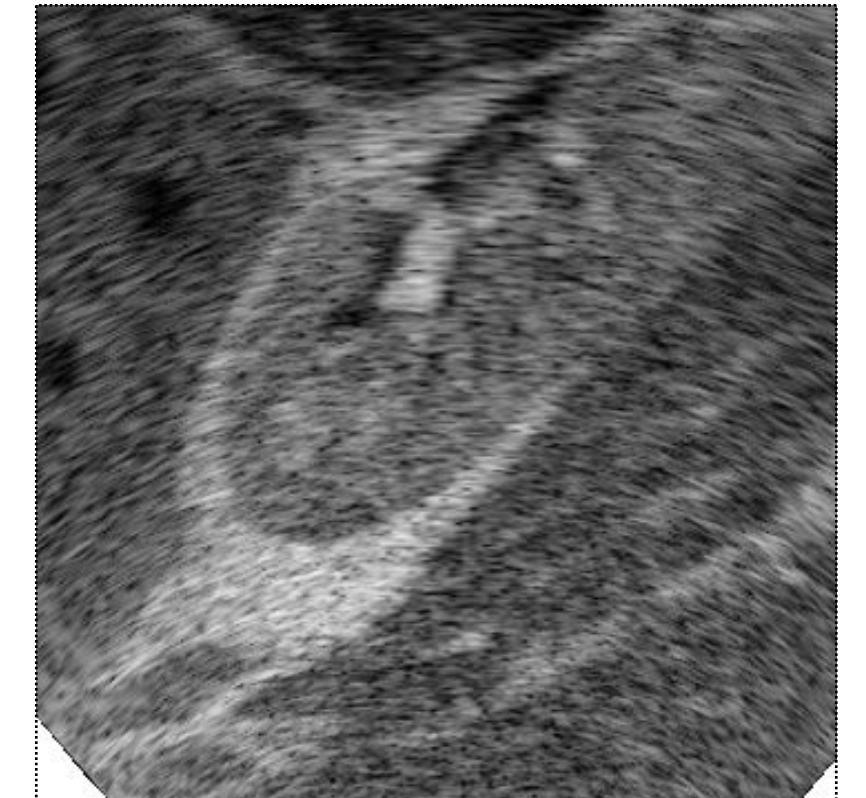
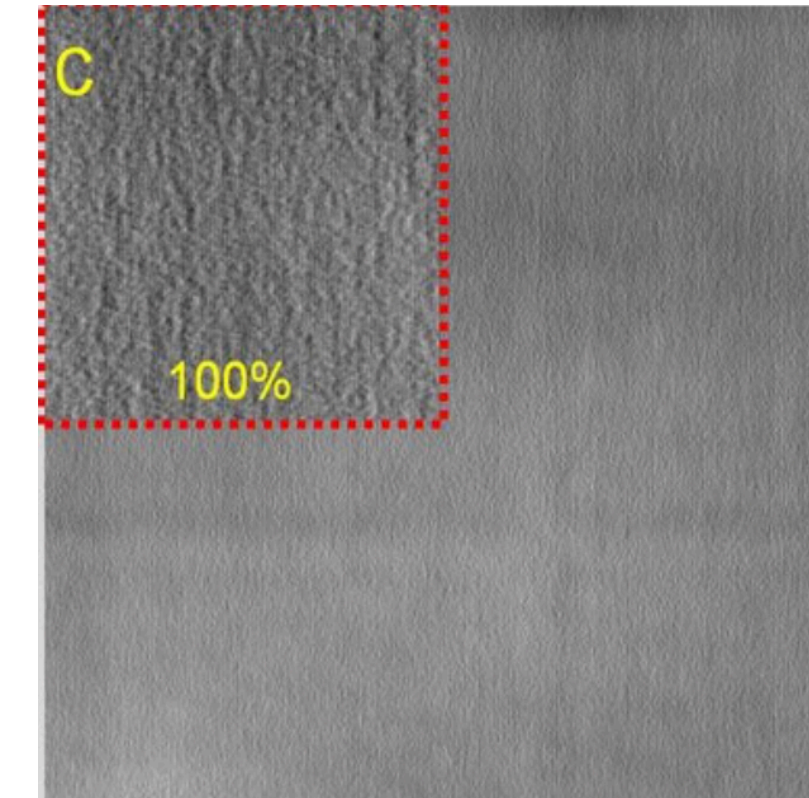
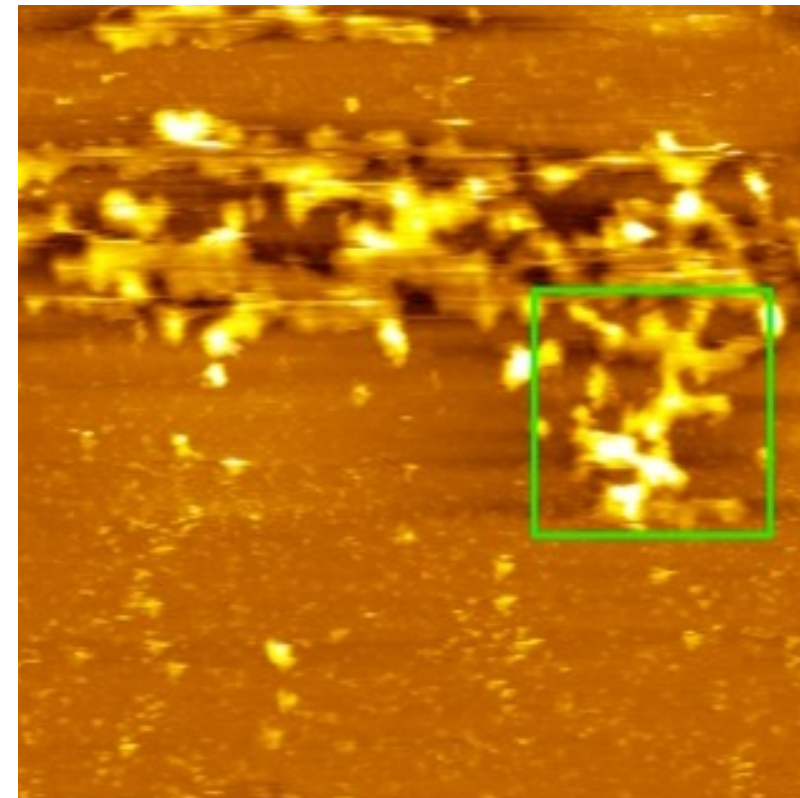
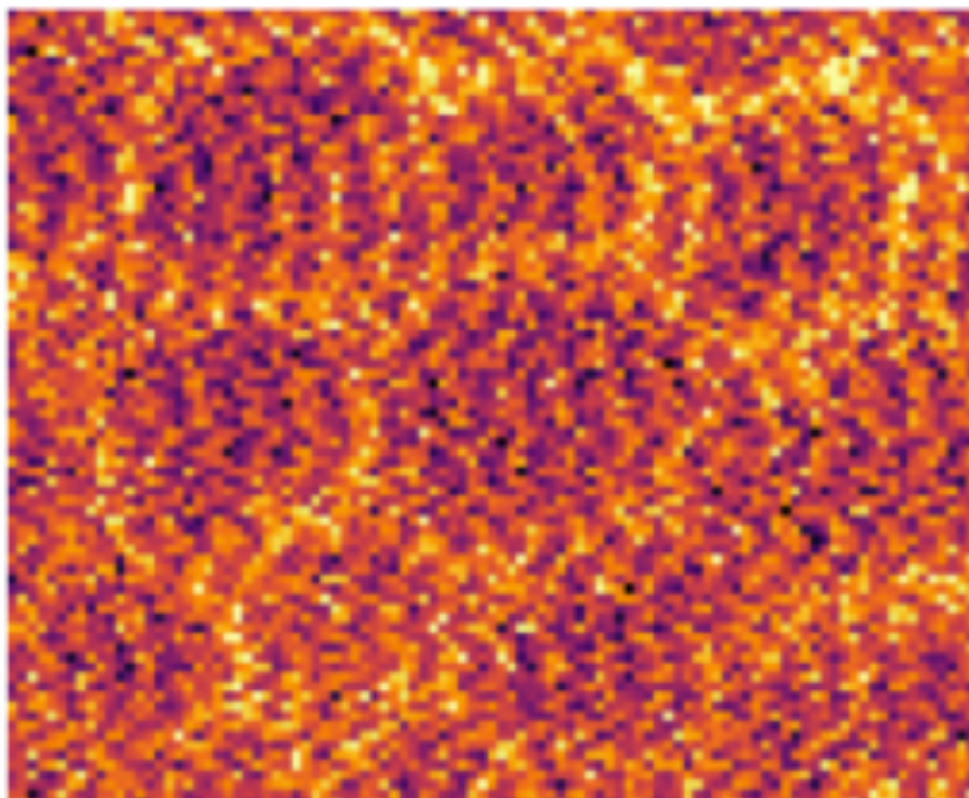
Correlation among pixels  
Self-similarity  
Patterns  
Sparsity  
Low frequency

+

### Noise model

Random variables  
No spatial structure  
Independent realizations  
Statistical distribution  
High frequency

## Structural Noise







# Noise Quantity

## Signal-to-Noise Ratio **SNR**

$$SNR = \frac{\text{mean}}{\text{stdev}}$$

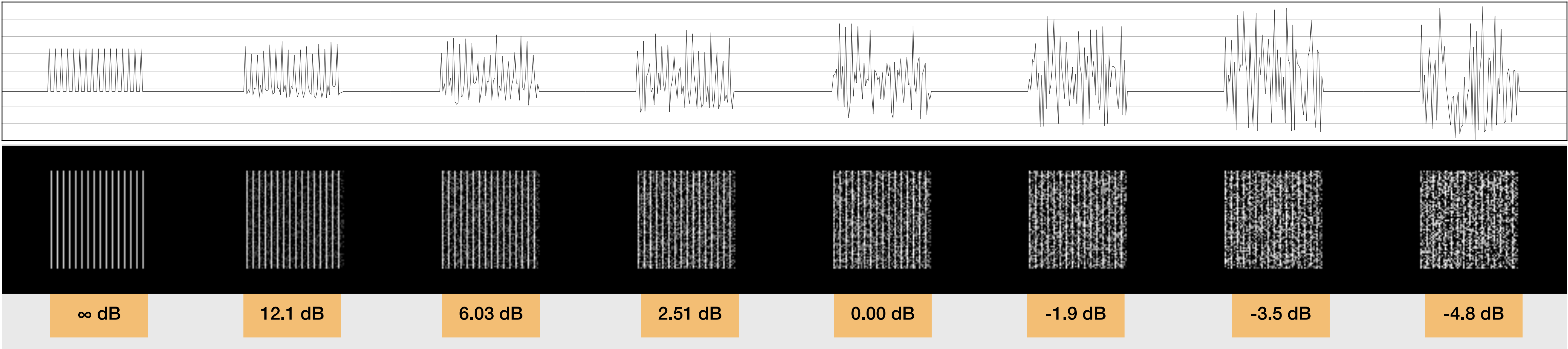
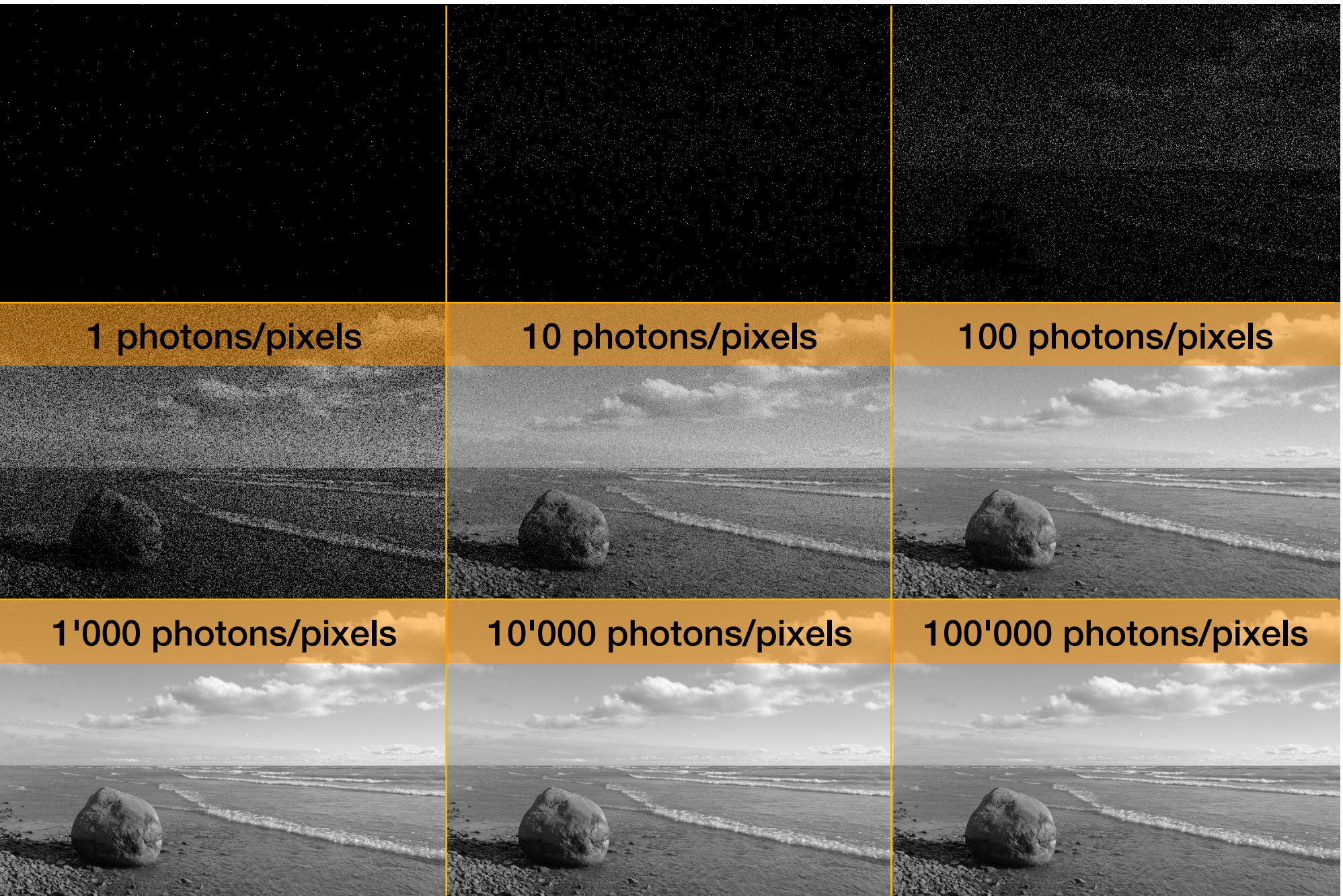
$$SNR_{dB} = 10 \log_{10}(SNR)$$

## Peak Signal-to-Noise Ratio **PSNR**

$$PSNR = \frac{\text{dynamic range}}{\text{stdev}}$$

## Contrast-to-Noise Ratio **CNR**

$$CNR = \frac{\mu_{sig} - \mu_{bg}}{\sigma}$$

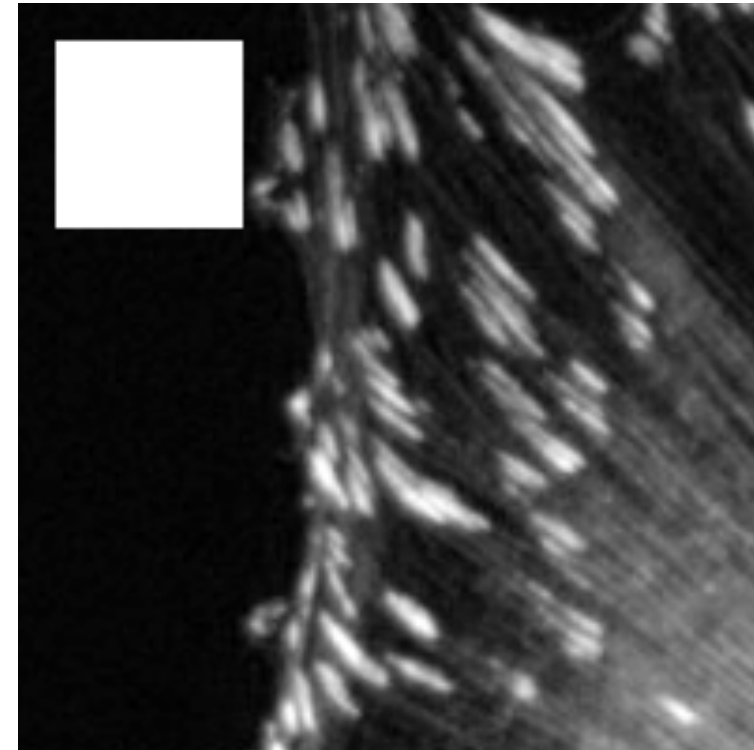






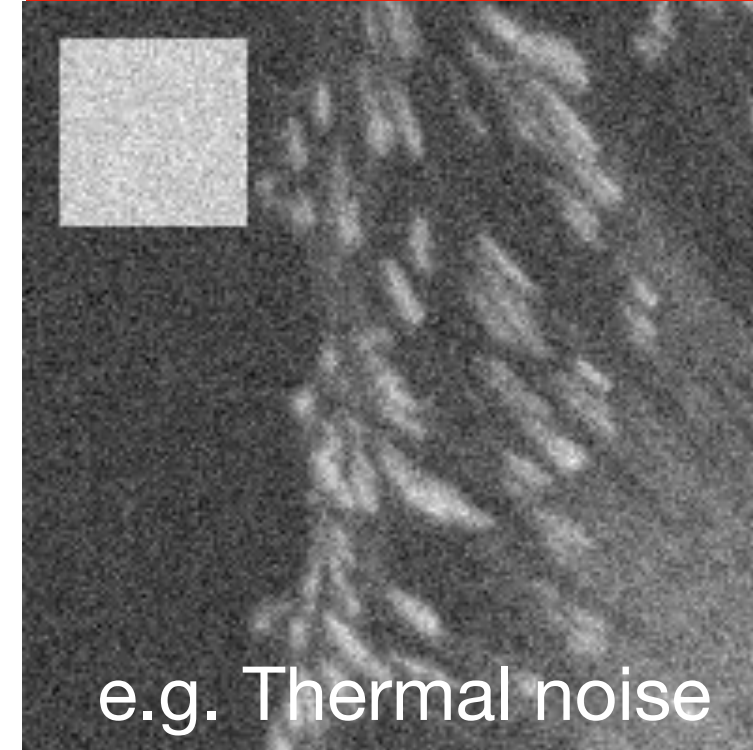
# Noise Distribution Models

Test image  
Noiseless

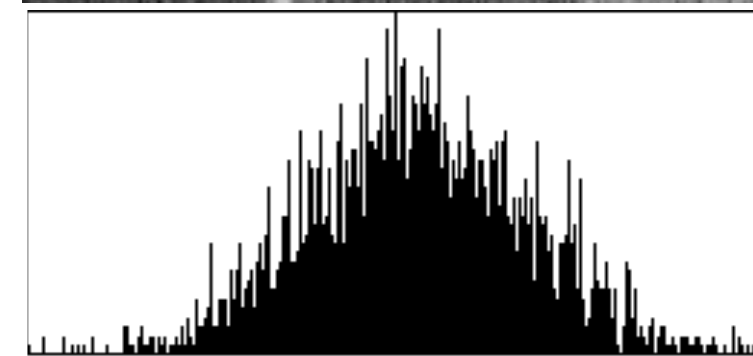


Source: CIL38985

Gaussian

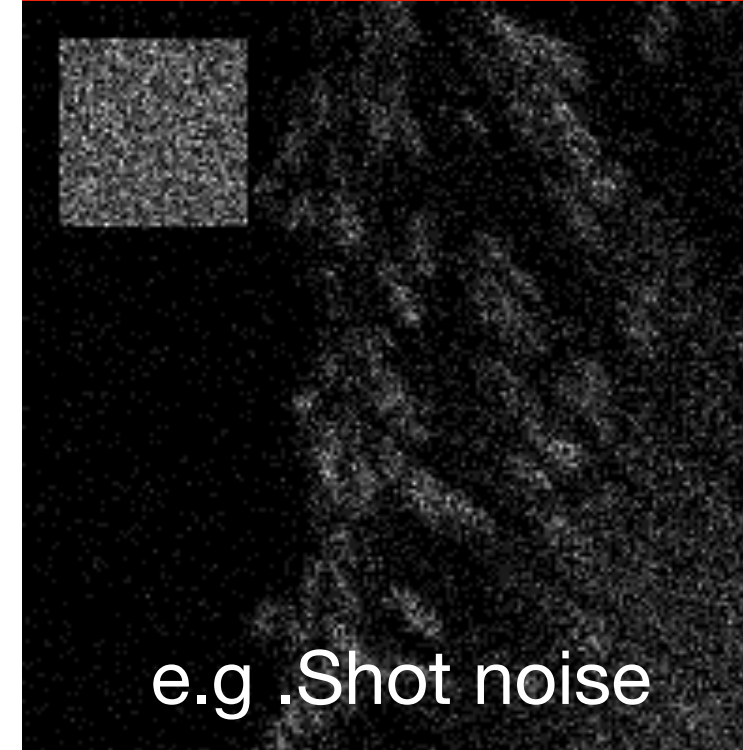


e.g. Thermal noise

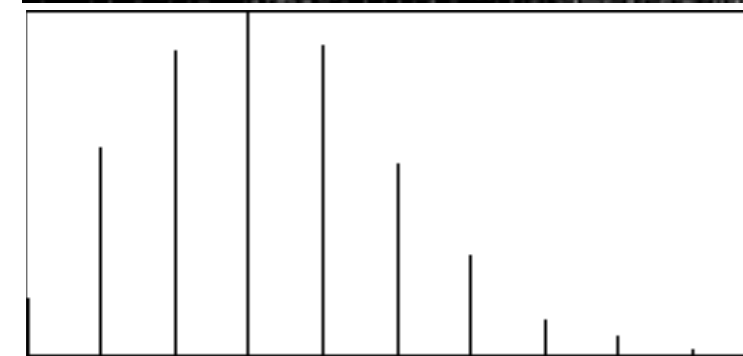


mean  $\mu$   
standard deviation  $\sigma$

Poisson

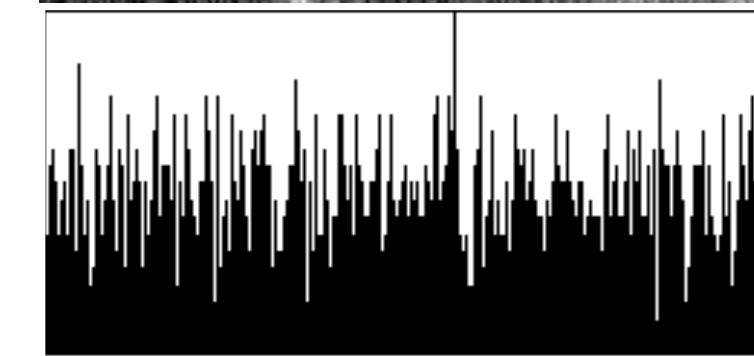
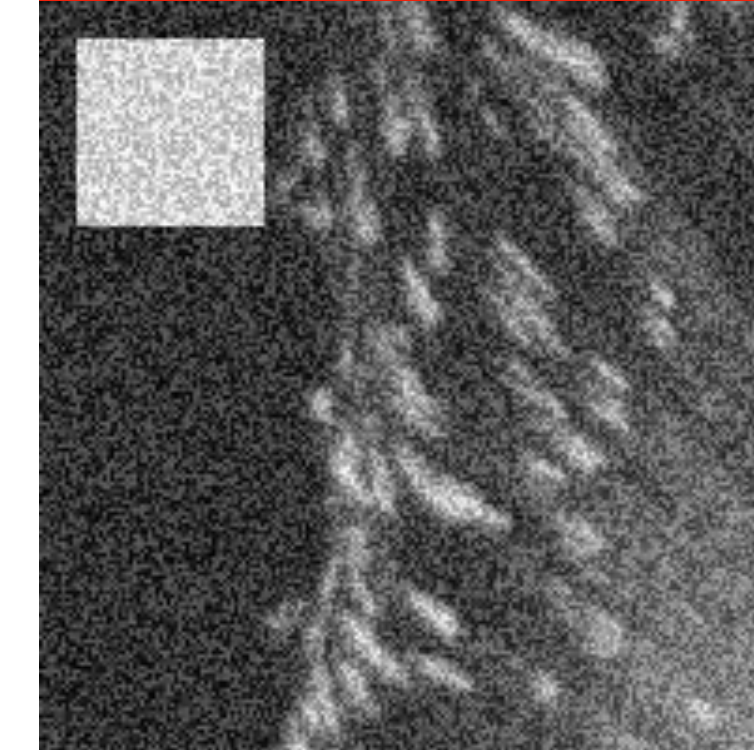


e.g. Shot noise



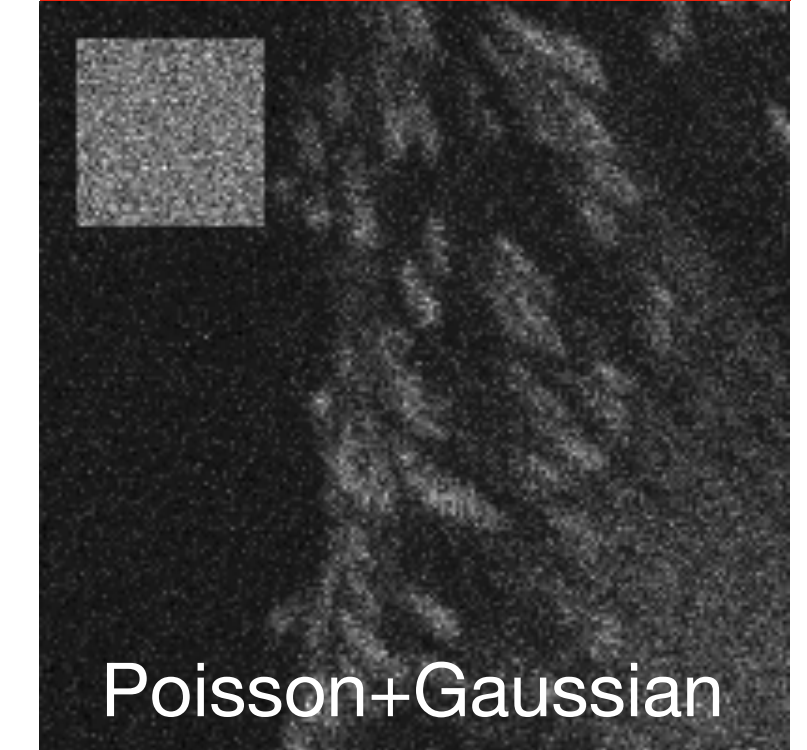
mean  $\mu = \lambda$   
variance  $\sigma^2 = \lambda$

Uniform

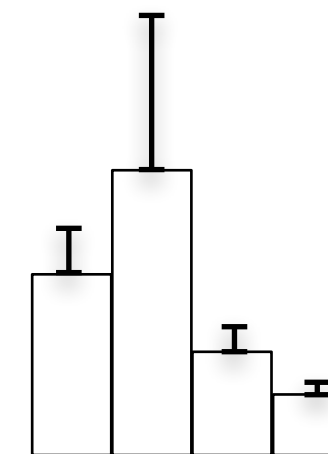
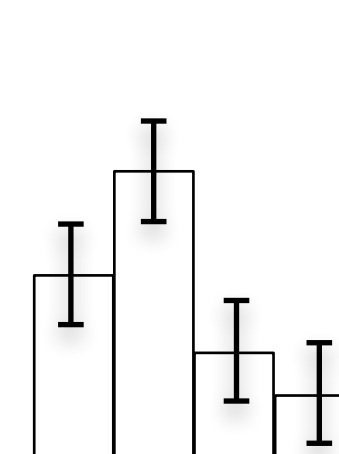
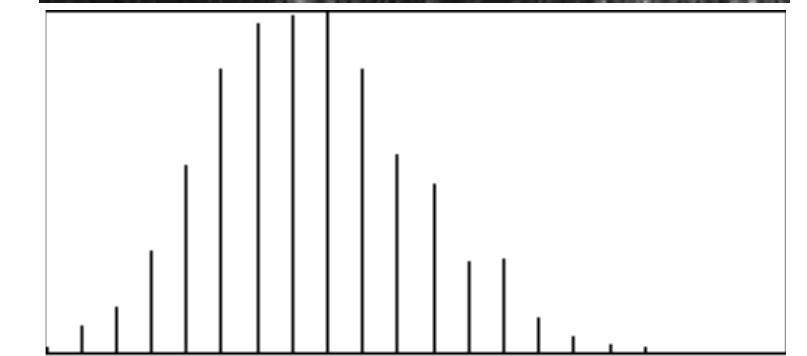


[min, max]  
mean  $\mu = (\text{max} + \text{min}) / 2$

Mixed P. G.



Poisson+Gaussian



## Mixed Poisson-Gaussian

- Realistic model in fluorescence
- Poisson (shot and dark noise)
- Gaussian (readout noise)

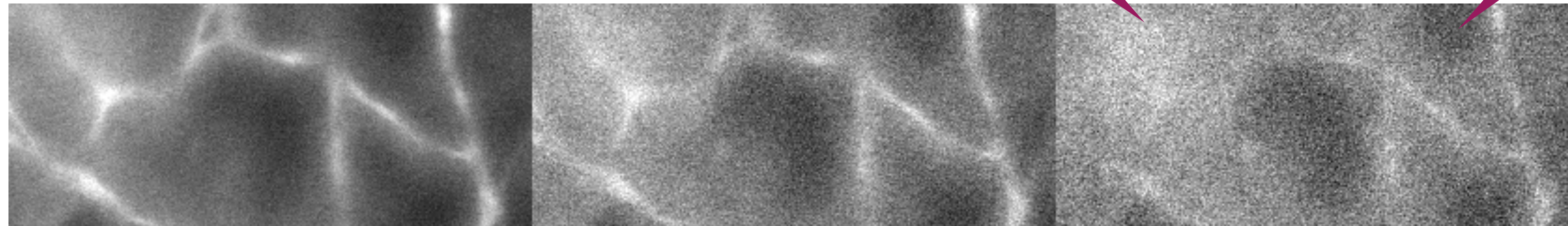




# Basic Methods

## Noisy data

Frames at 3 time-points.  
Signal is decreasing  
(bleaching)



Source: D. Wüstner, University of Odense, Denmark

## Gaussian Filter

### Low-pass filter

Spatial blurring  
Reduction of high  
frequency noise



Gaussian Filter of ImageJ, sigma=2

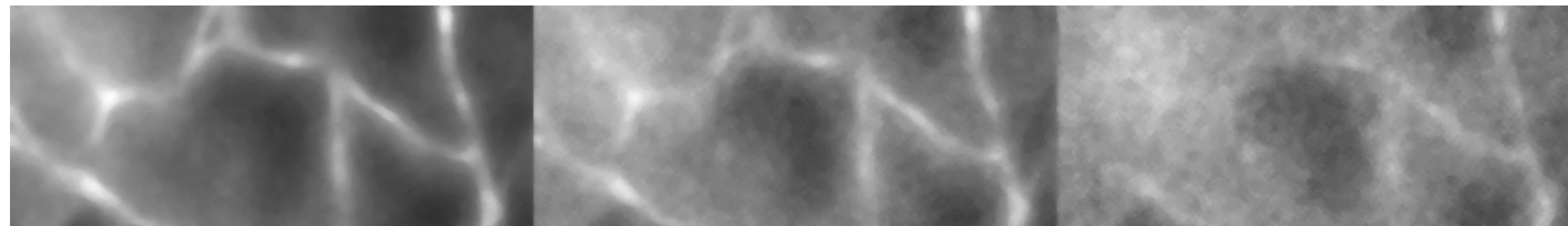


Smoothing  
Kill the HF signal  
? imaging setup

## Median Filter

### Speckle noise

Preserve edges  
Reduce shot noise  
Cartoon effect



Median Filter of ImageJ, radius=3



No fine tuning  
Heuristic control

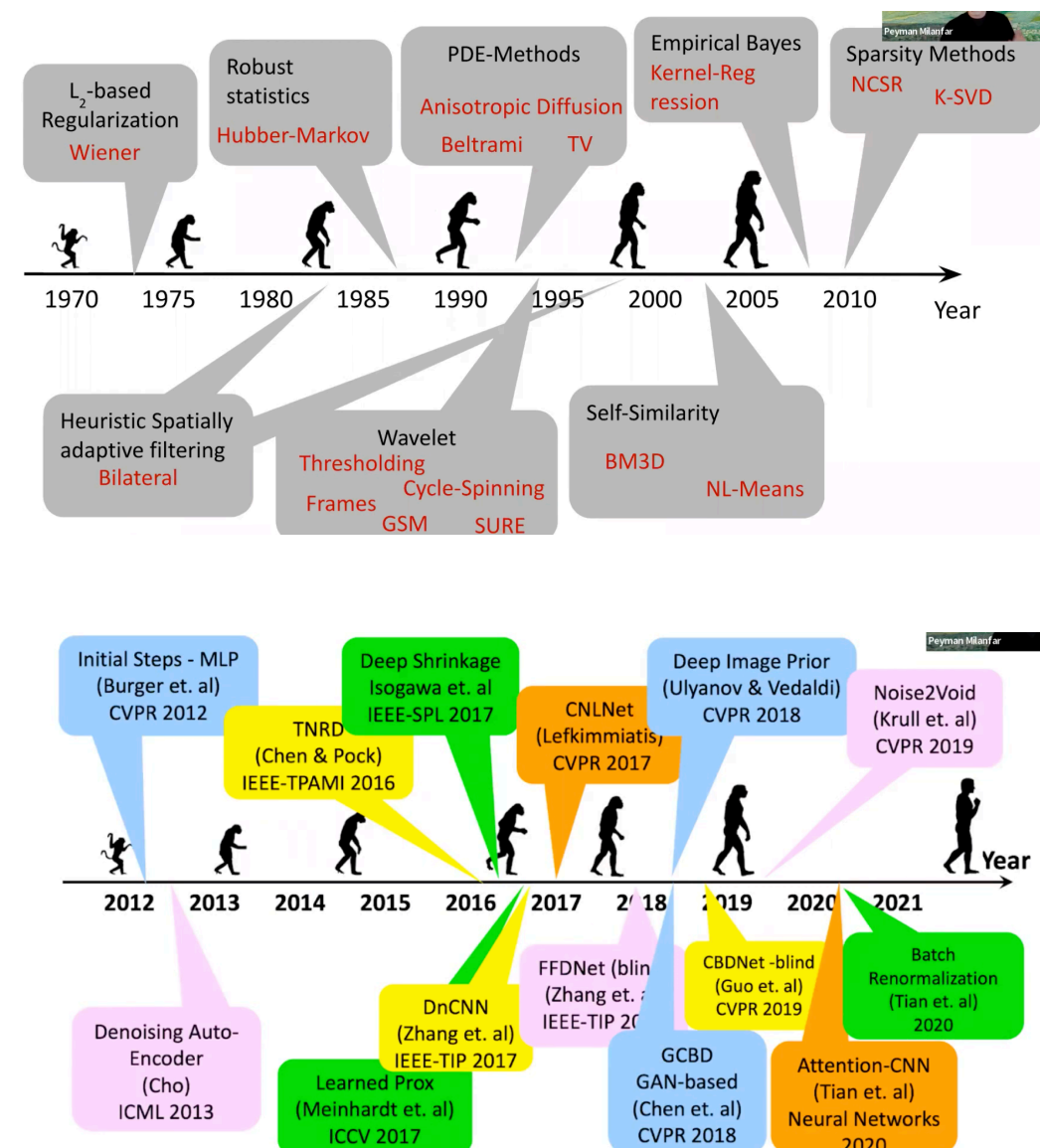


# 👁 Methods for Image Denoising

## Goal: Image simplification

- ✓ Preprocess before image segmentation
- ✓ Enhance the structure of interest
- ✓ Take advantages of the multidimensional data

## Video tutorial of Peyman Milanfar



## Remove high frequency

- Digital linear filtering (Gaussian)

## Edge-preserving smoothing

- Non-linear filtering (Median)
- Anisotropic diffusion [Perona-Malik, 1990]
- Bilateral filter [Tomasi, 1998]
- Mean-shift [Comaniciu, 2002]

## Sparsity prior

- Total variation [Rudin-Osher-Fatemi, 1992]
- Wavelet shrinkage [Donoho 1998]
- PureLET [Luisier 2010]

## Self-similarity prior

- Non-local mean [Buades, 2005]
- Block matching [Dabov 2006]

## Supervised Learning

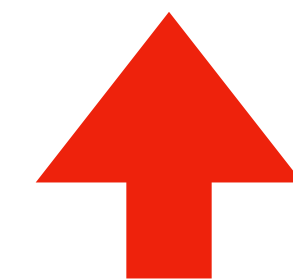
- DnCNN [Zhang 2017]
- CARE [Weigert 2018]

## Self-Supervised Learning

- Noise2Noise [Lehtinen 2018]
- Deep Image Prior [Ulyanov 2018]
- Noise2Void [Krull 2019]

## Other strategies of learning

- PnP Denosing [Ulugbek 2022]
- Diffusion Generative Model [Song 2020]



**Deep-learning approaches**

Meinzel et al, Denoising of microscopy images : a review of the state-of-the-art, *IEEE* 2018.

Laine et al., Imaging in focus : An introduction to denoising bioimages in the era of deep learning, 2021.





# "Classic" Image Simplification



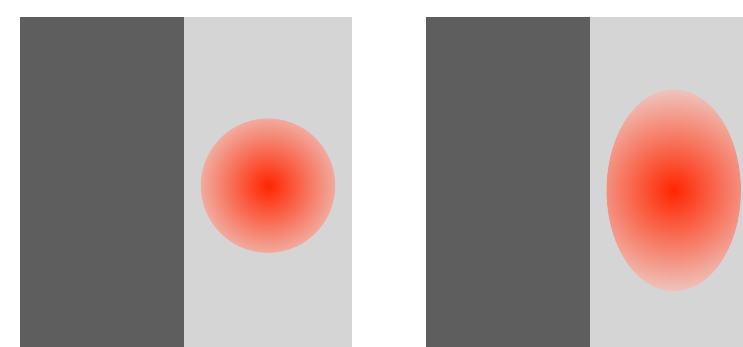
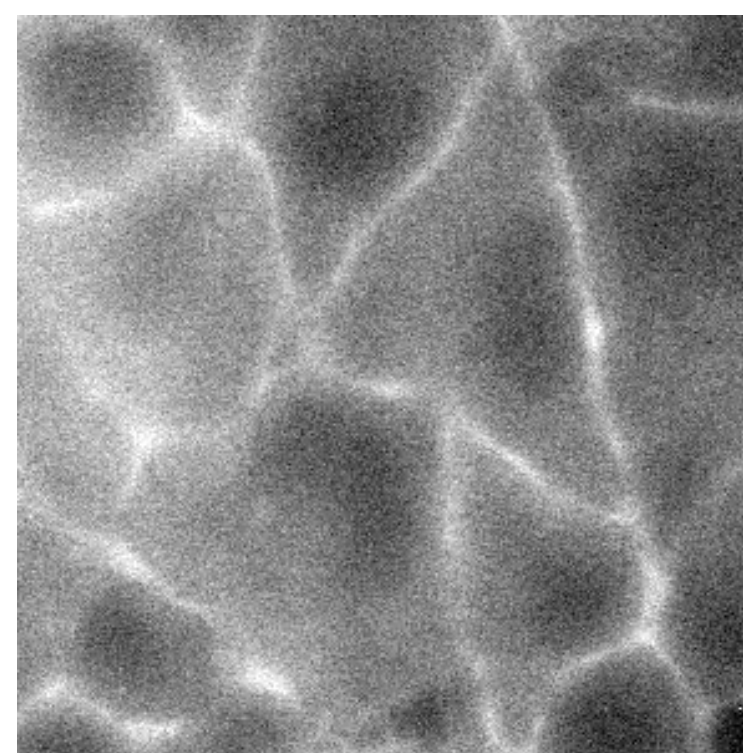
ImageJ plugin

## Anisotropic Diffusion

[Perona-Malik, 1990]

Iterative diffusion  
Many parameters

$$\frac{\partial f}{\partial t} = \text{div}(c(\|\nabla f\|) \nabla f)$$



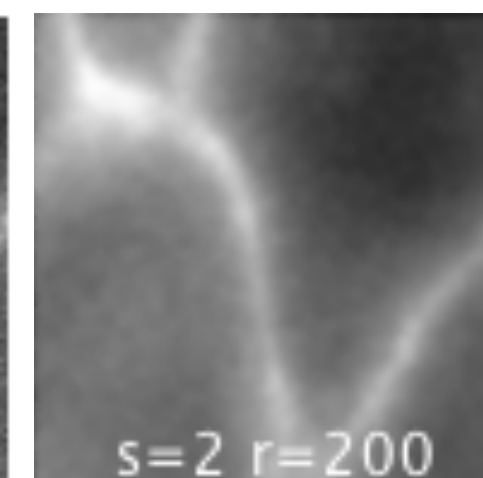
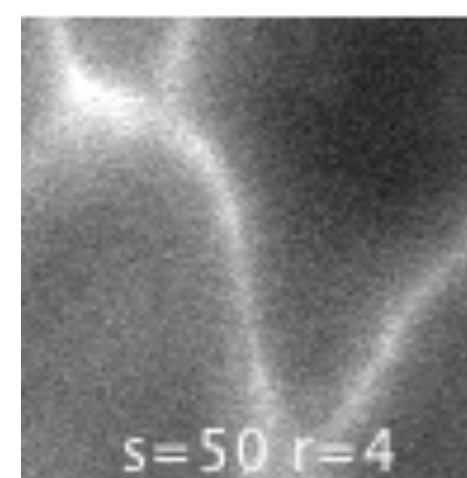
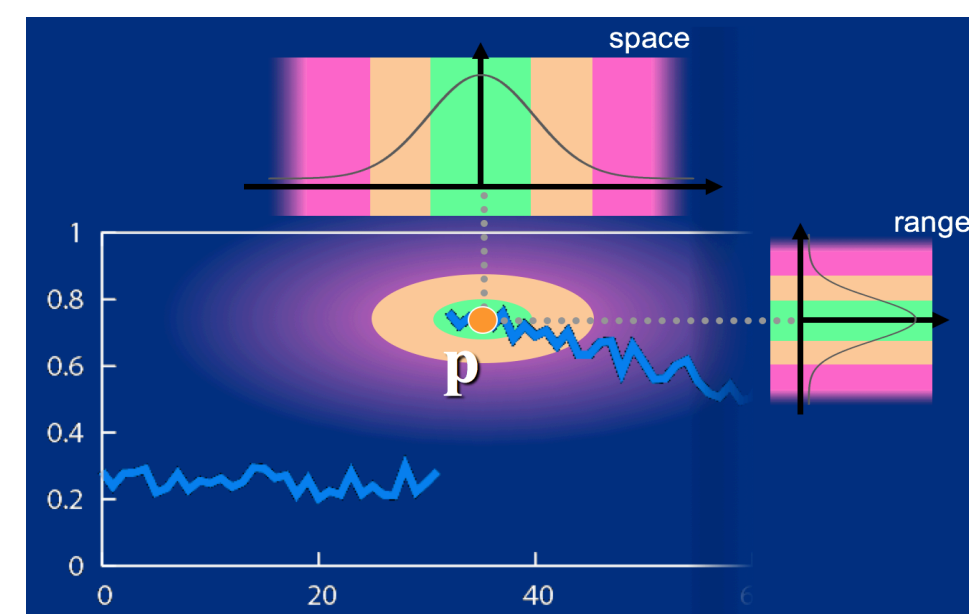
To preserve edges

## Bilateral Filter

[Tomasi, 1998]

Local adaptive blur  
Preserve edges

$$h(\mathbf{x}) = \frac{1}{W} \int_{\mathbf{k} \in \Omega} f(\mathbf{k}) w(\mathbf{x} - \mathbf{k}) \phi(f(\mathbf{x}) - f(\mathbf{k})) d\mathbf{k}$$

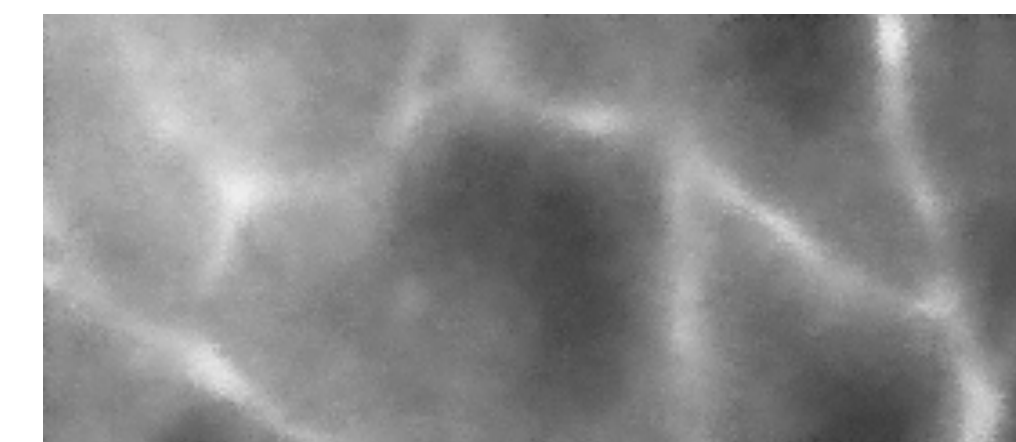
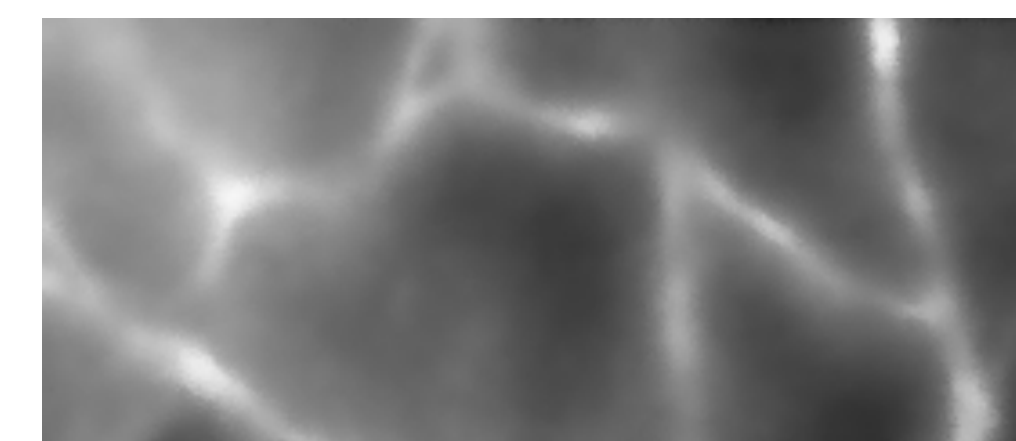


## Mean-Shift

[Comaniciu, 2002]

Data clustering algorithm  
Cartoon effect, extensible in nD

- For every pixel
1. Calculate the center of mass on local window:  $\mathbf{x}$  and  $\mathbf{u}$
  2. Shift to  $\mathbf{x}$
  3. Repeat step 1 until convergence





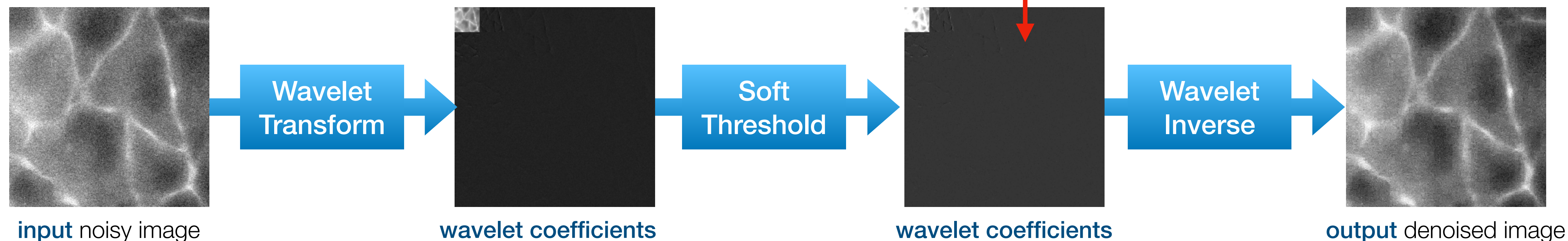


# Wavelet Shrinkage

## In the wavelet domain

[Donoho, 1998]

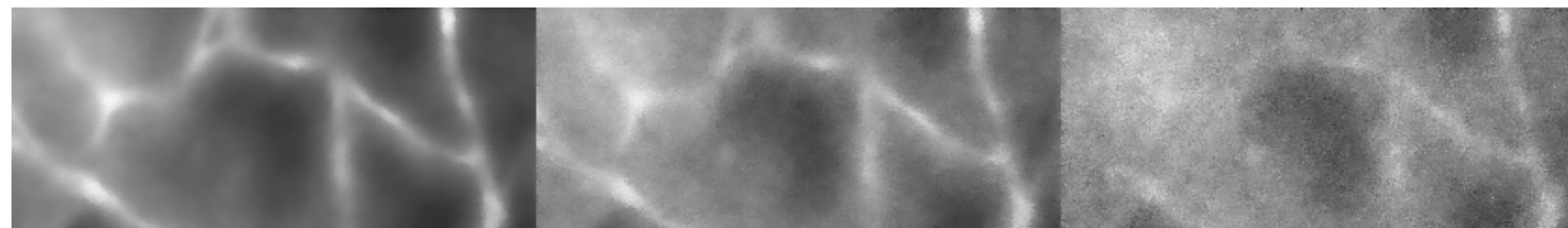
- Decorrelation ability
- Sparse representation
- Multiscale



## PureDenoise

[Luisier, 2010]

Linear expansion of threshold  
using a unbiased criteria



PureDenoise, plugin of ImageJ, EPFL



# Self-Similarity-Based Denoising

## Non-local mean

[Buades-Coll-Morel, 2005]

### Assumptions

- Images have repetitive textures
- Images have self-similarity

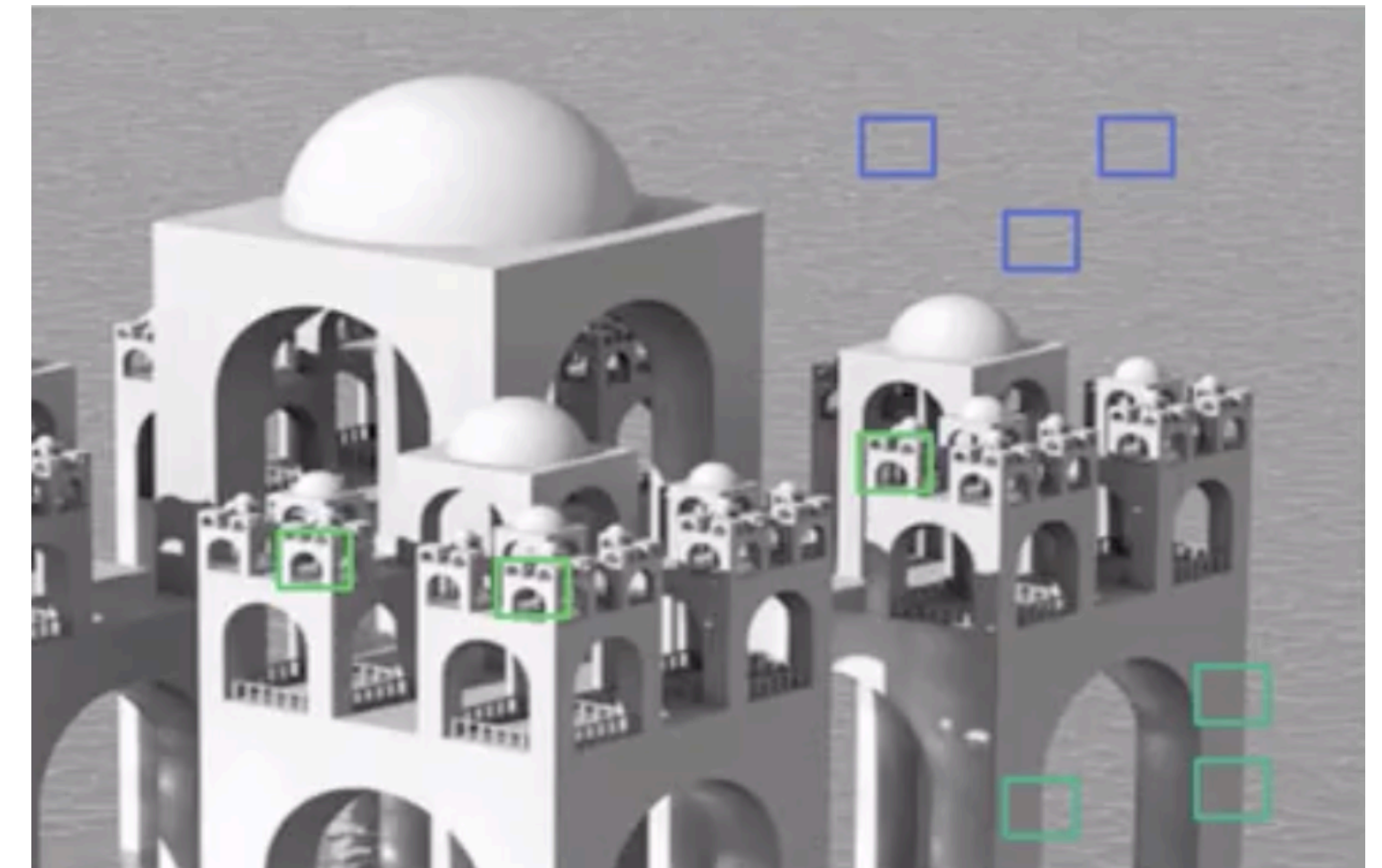
### Algorithms

- No averaging around the pixel
- For over all the image find the similar pixel and then average

$$\begin{aligned}p_1 &= p_0 + n_1 \\p_2 &= p_0 + n_2 \\&\dots \\p_n &= p_0 + n_n\end{aligned}$$



**ij-nlm**  
**CANDLE-J**



## BM3D

[Dabov, 2006]

- Block-Matching 3D
- Wavelet threshold
- Combine patches

State-of-the-art in image  
denoising  
only in Matlab!

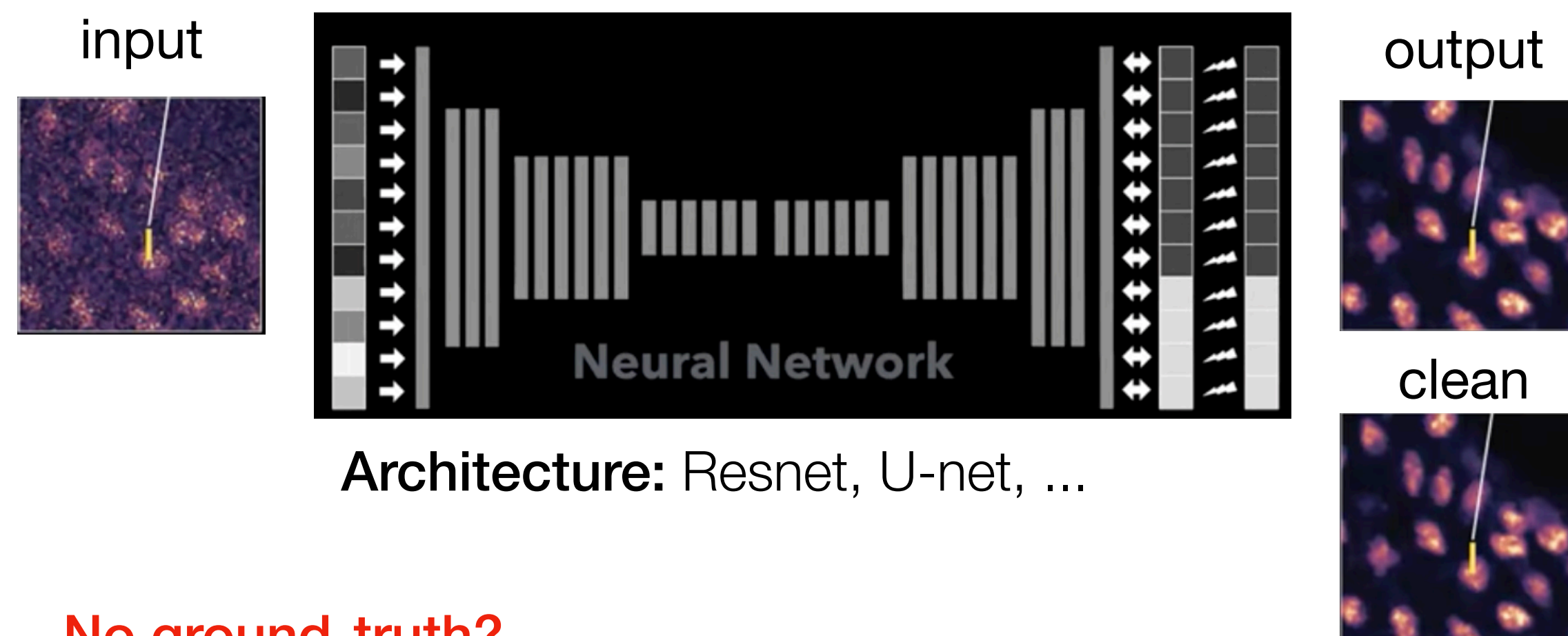




# Supervised Learning

noisy image   TRAINING  ground-truth 

noisy image   PREDICT  clean image 



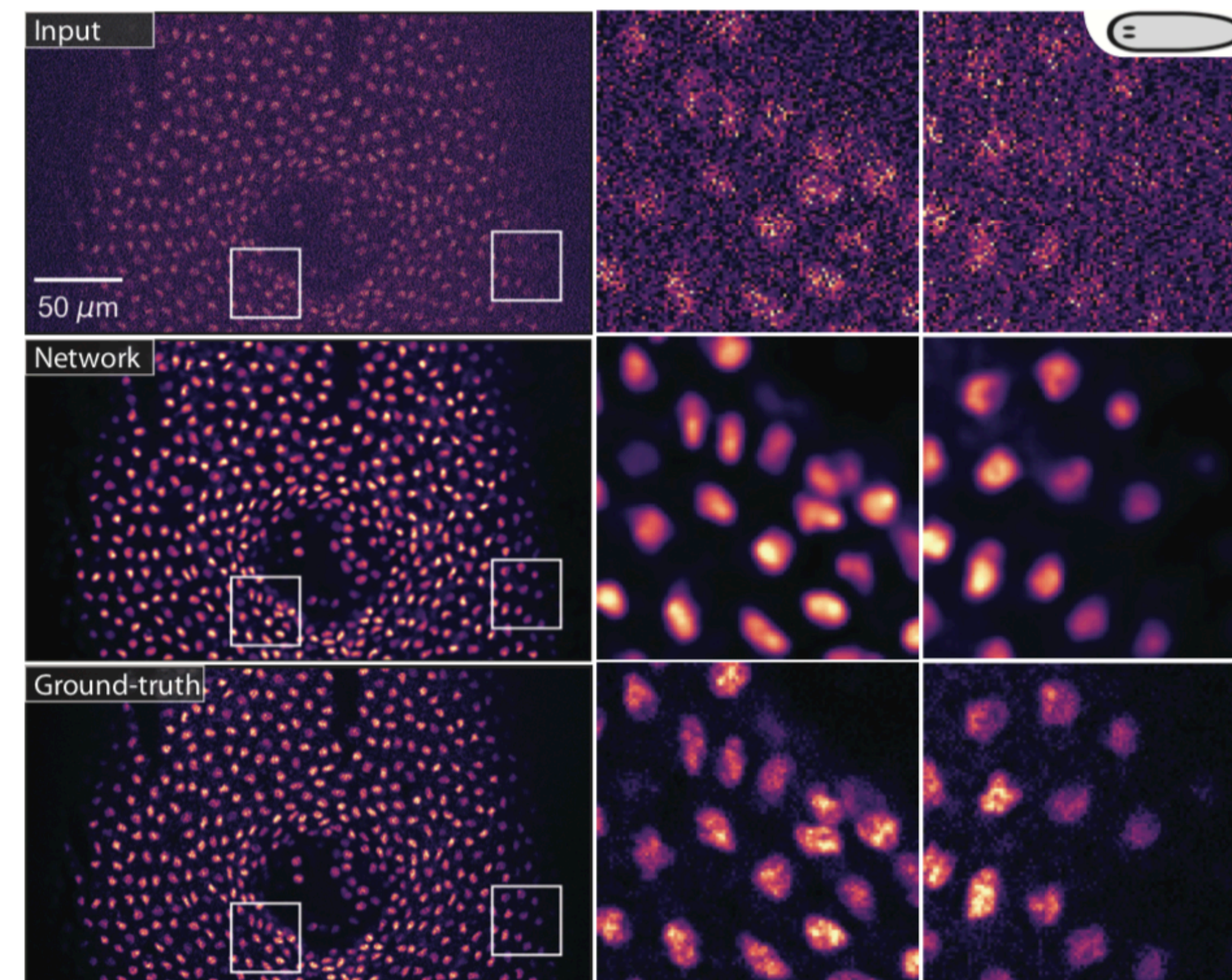
No ground-truth?

## Simulation

- Add various noise quantity
- Add various noise type

## Real data (microscope)

- Higher illumination
- Slow down the acquisition



CARE

Weigert, Nature Methods, 2018

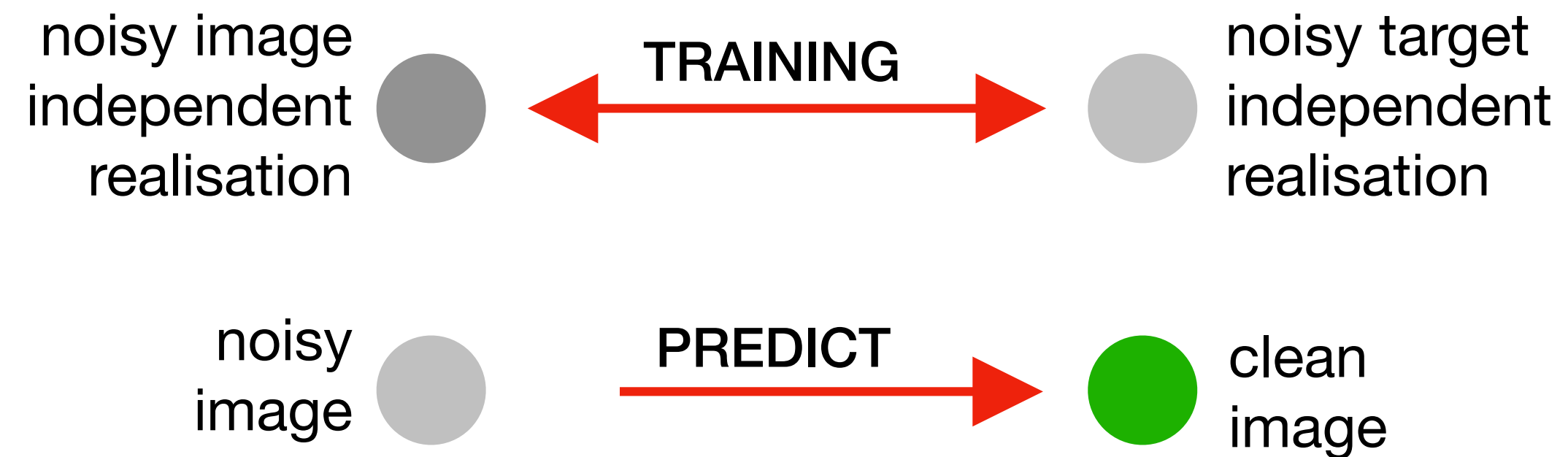
Video tutorial of Joran Deschamps, Denoising microscopy images with self supervised deep learning Nature Methods, Aneris Eurobioimaging, 2023



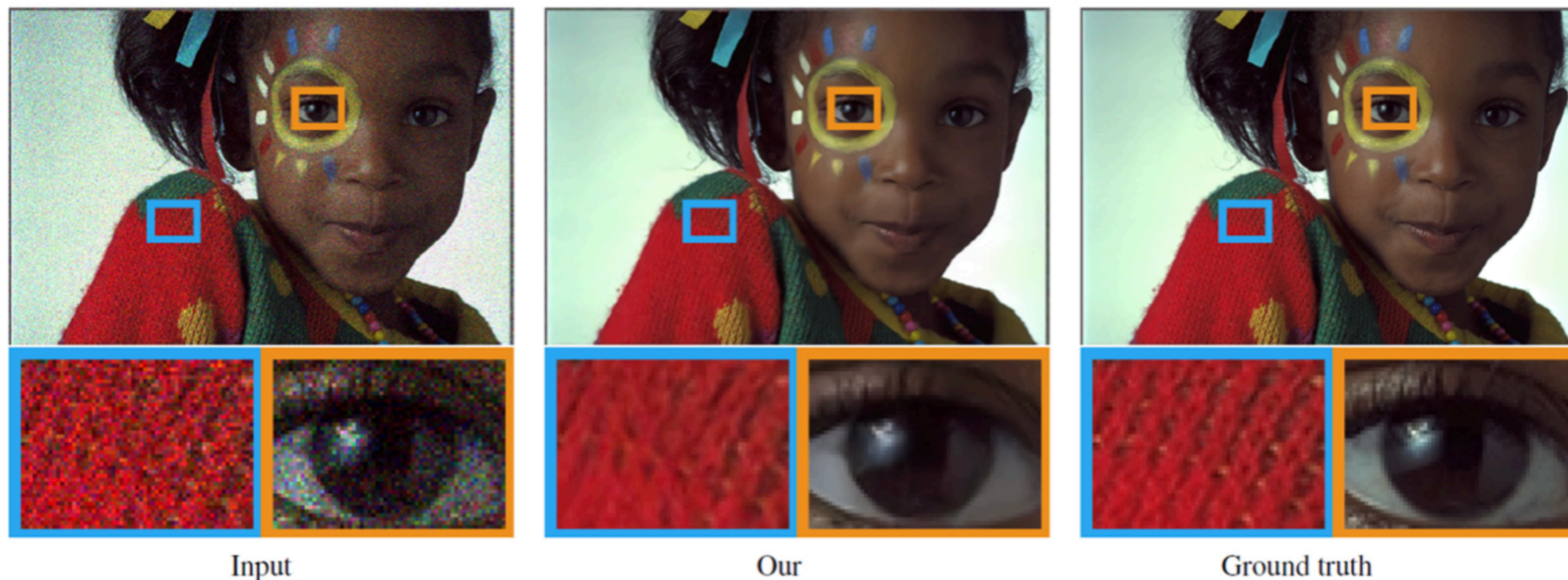
# Self-Supervised Learning

noise2noise

[Lehtinen, arXiv 2018] Learn bad images into good images by only looking at bad images



"if we were to acquire multiple images with the same signal, but different realizations of noise and average them, the result would approach the true signal"



NVidia web site

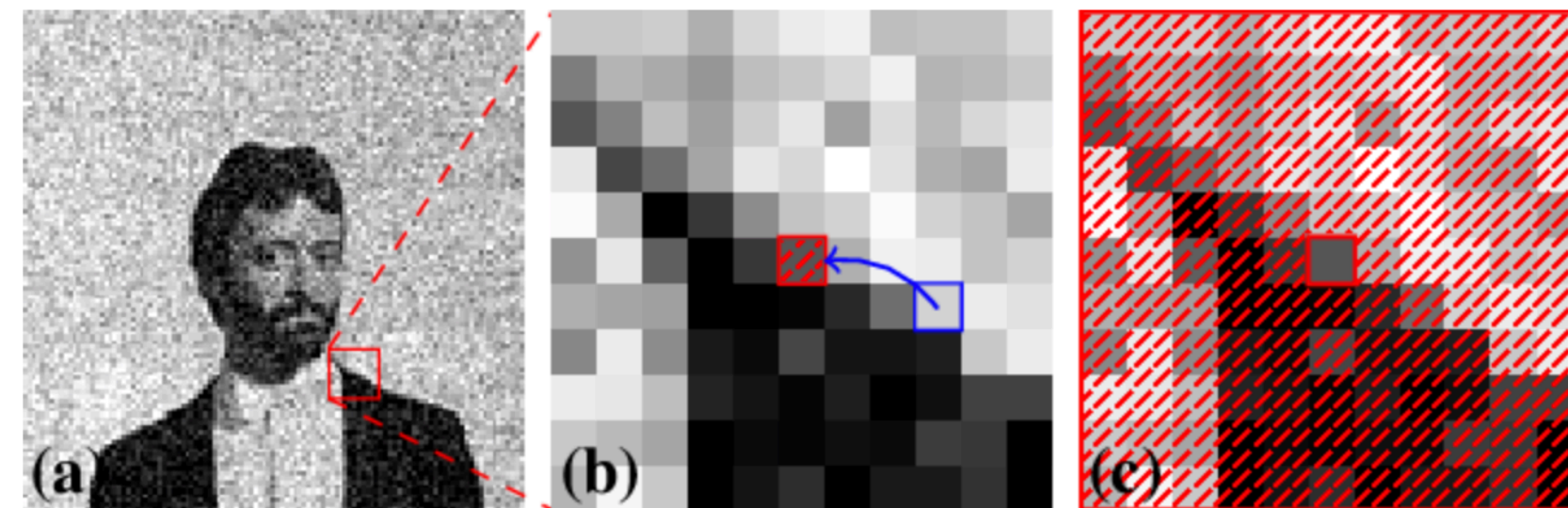
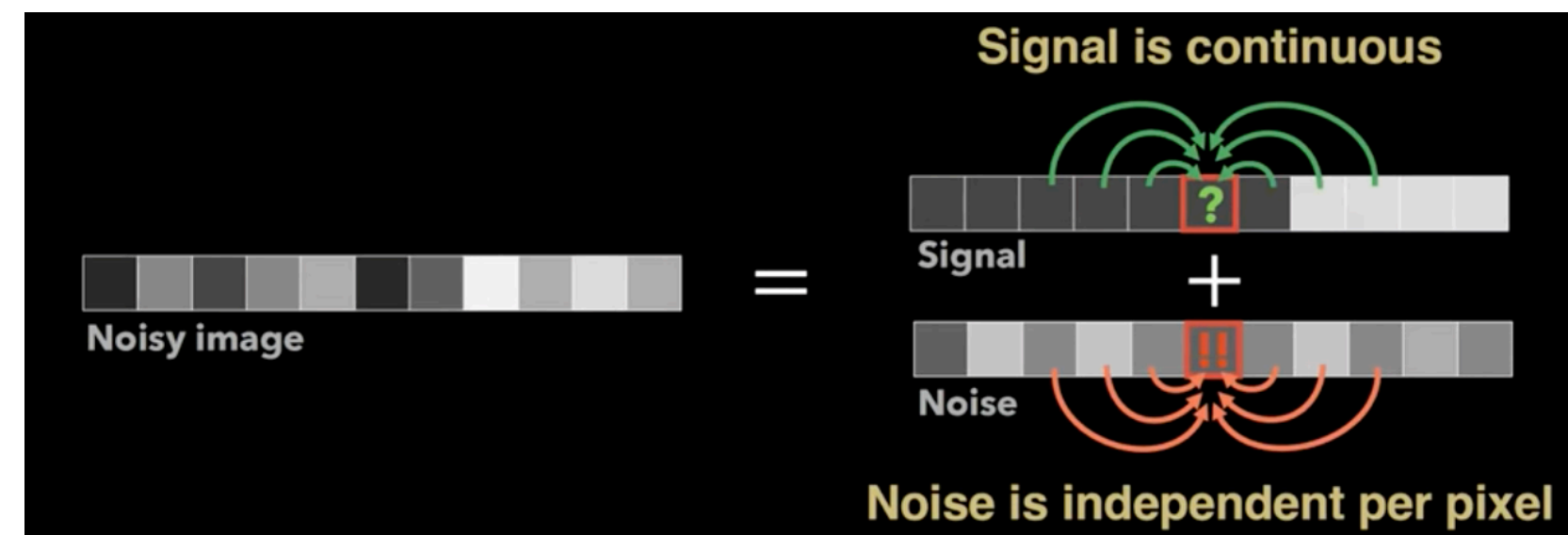
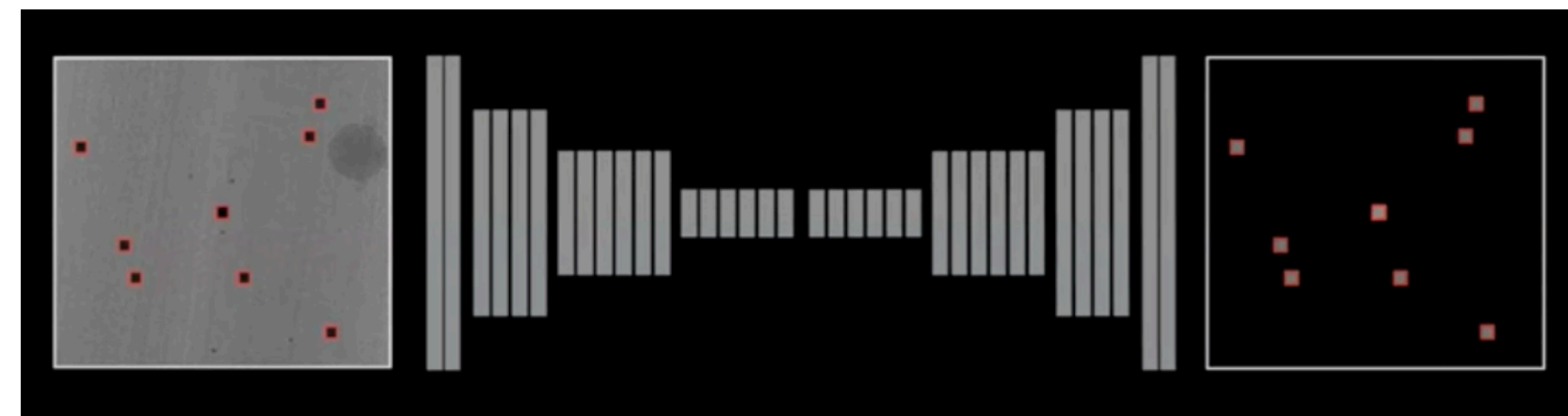




# Self-Supervised Learning

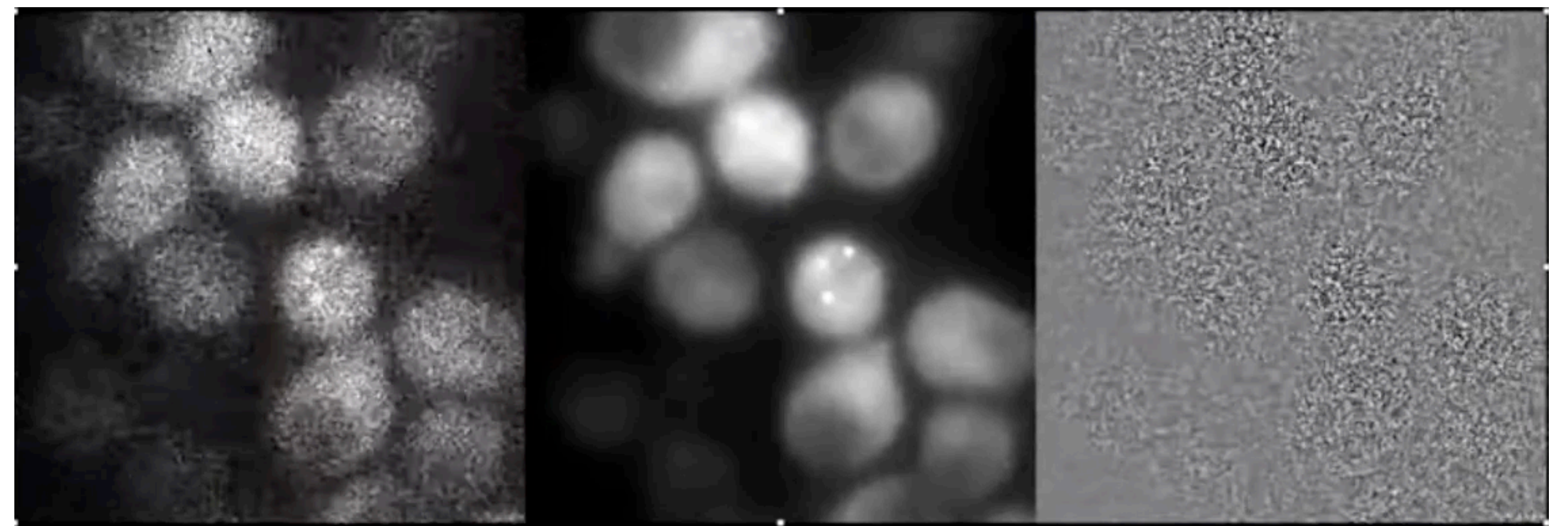
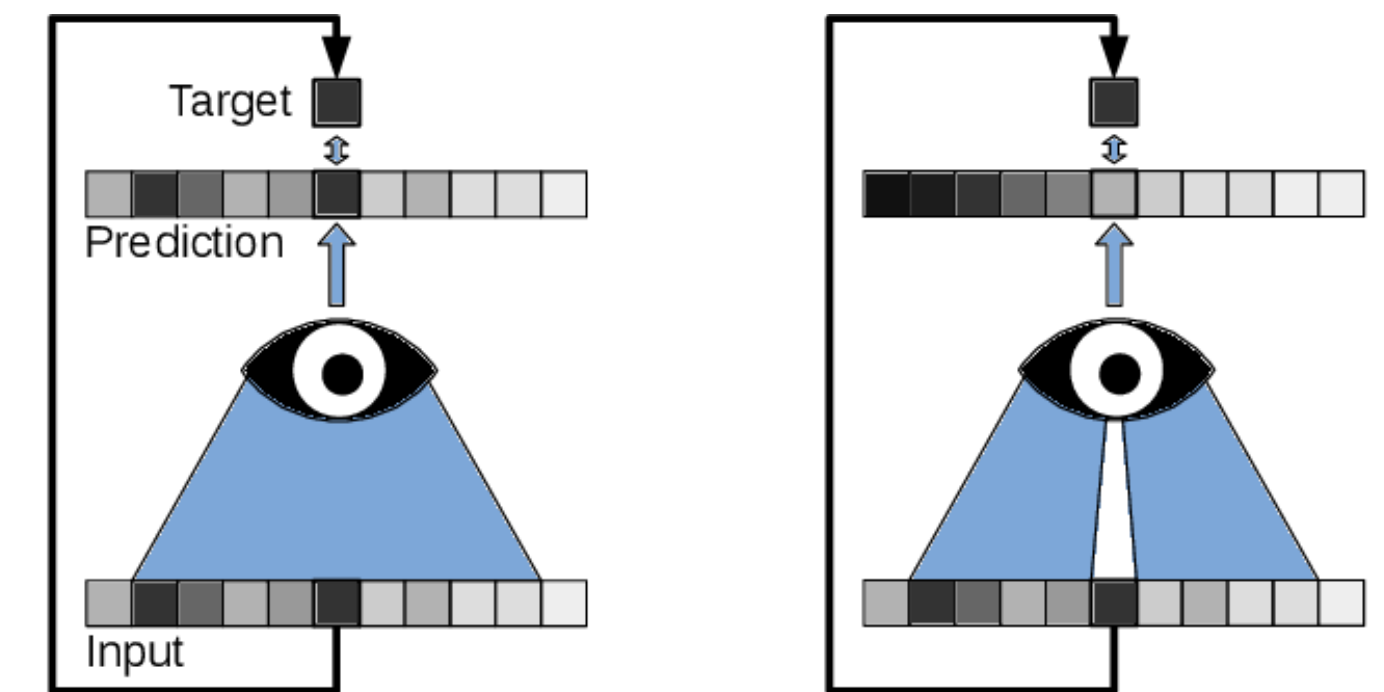
noise2void

[Krull, IEEE 2019]

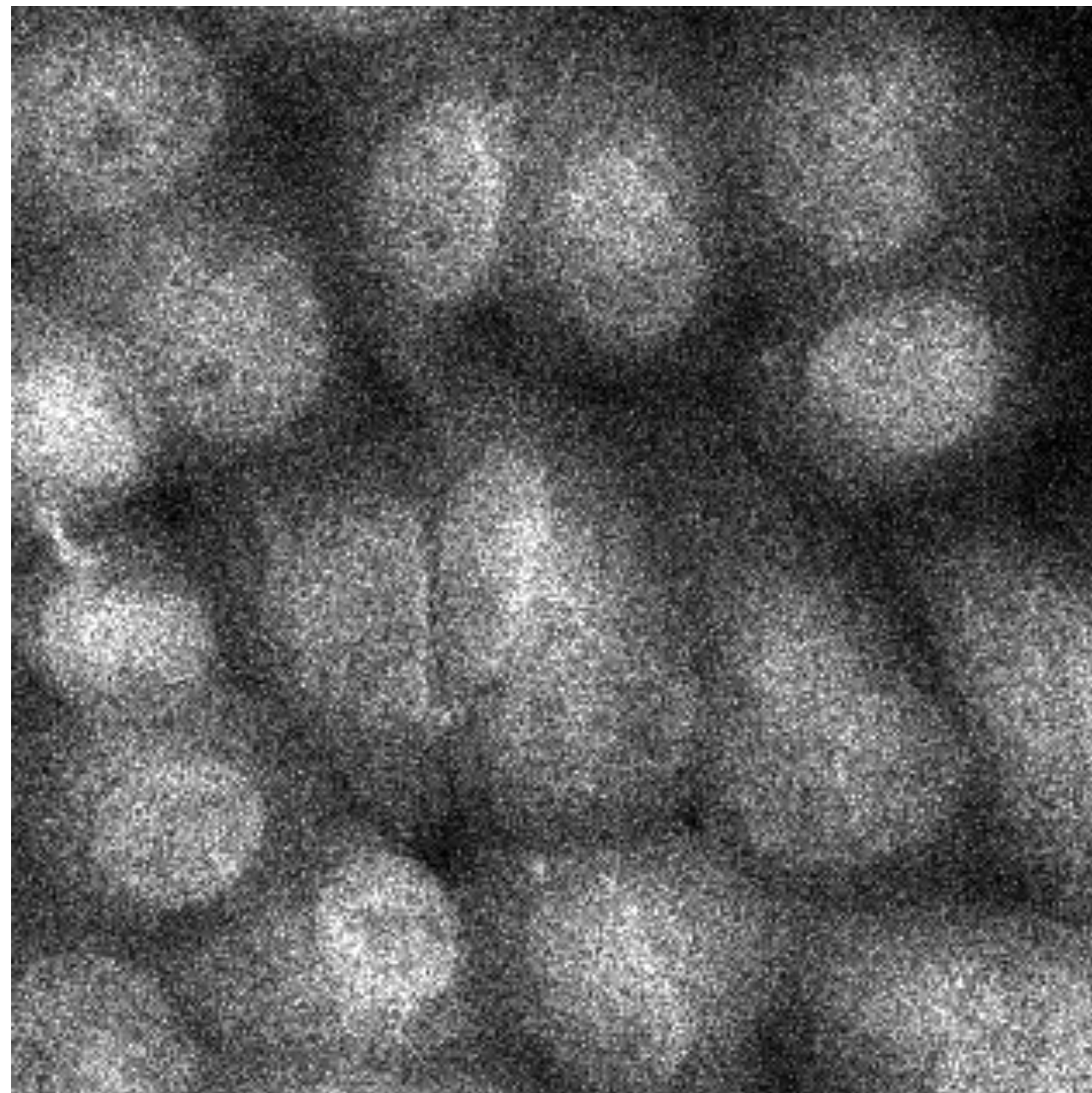


## noise2void

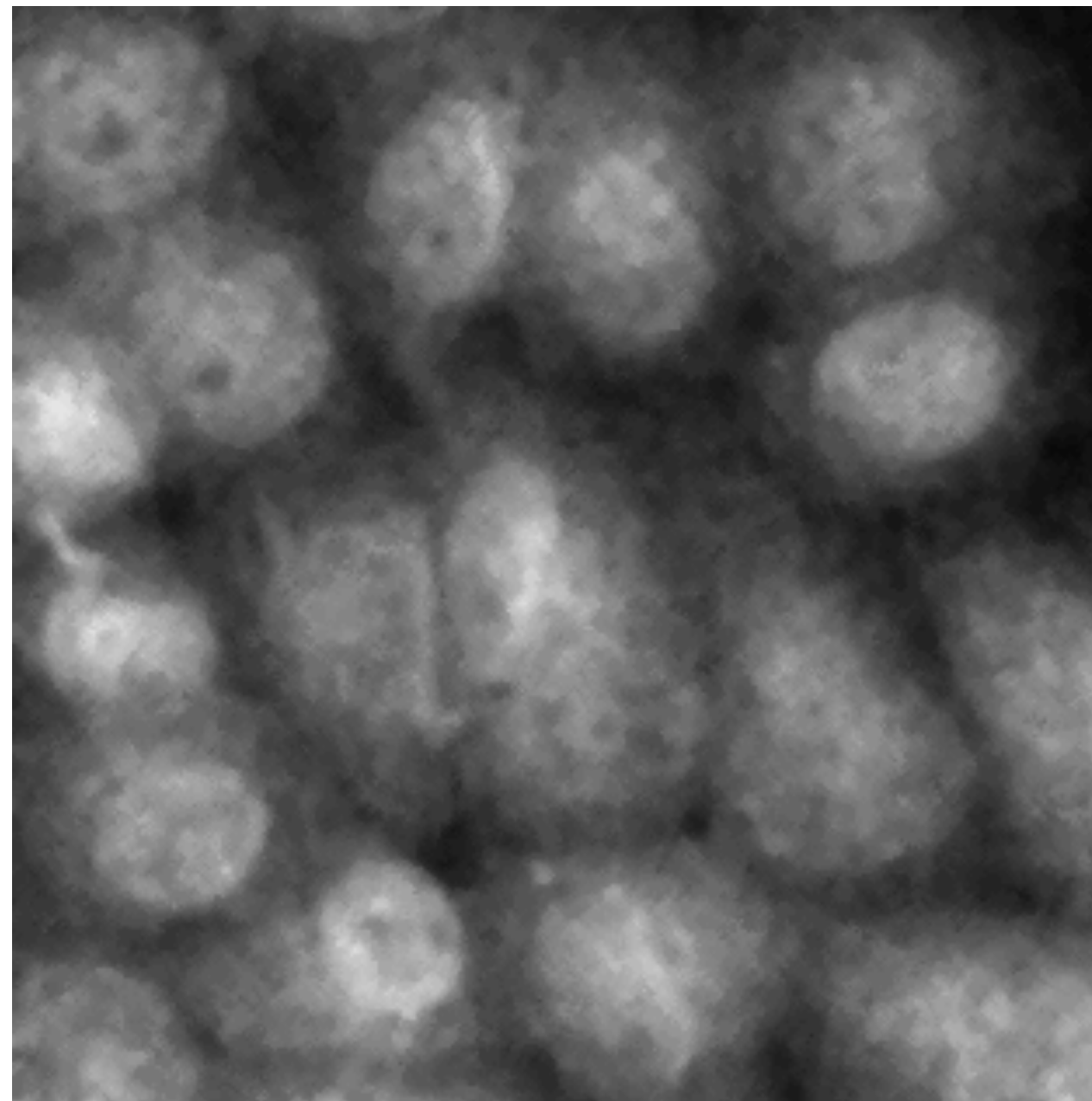
- Fiji plugins
- Napari plugins
- Training on GPU
- Prediction on CPU



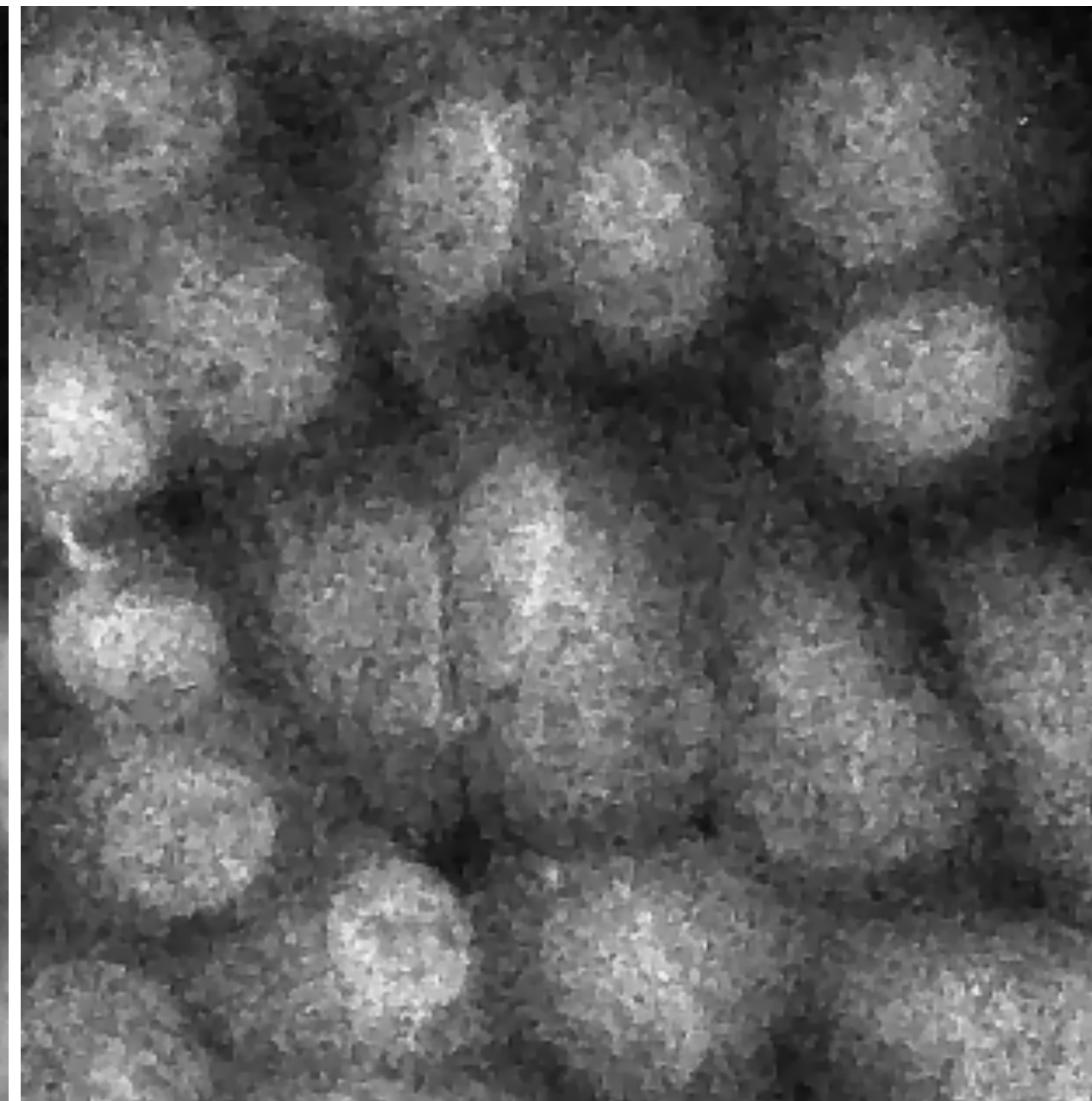




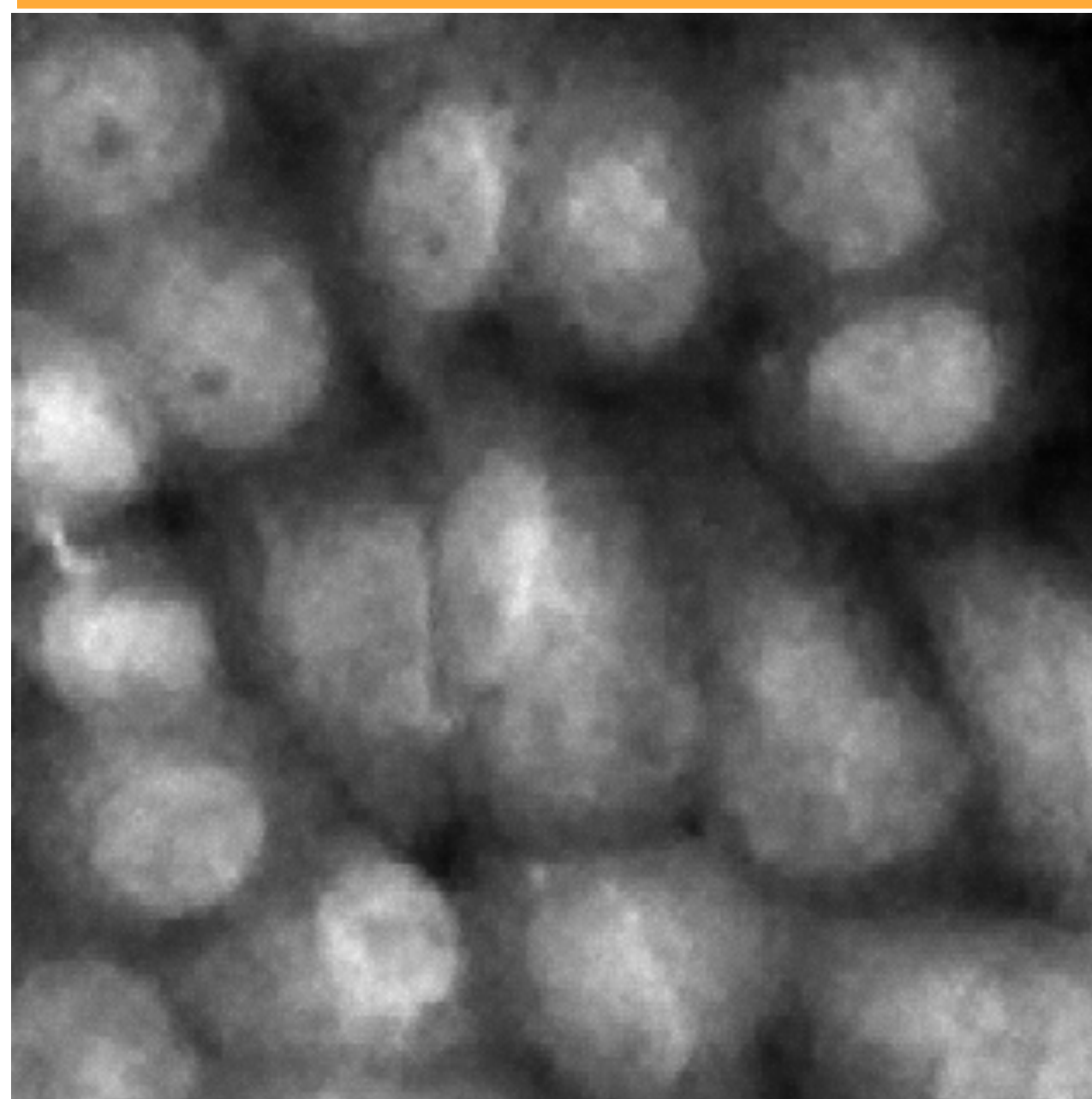
Input



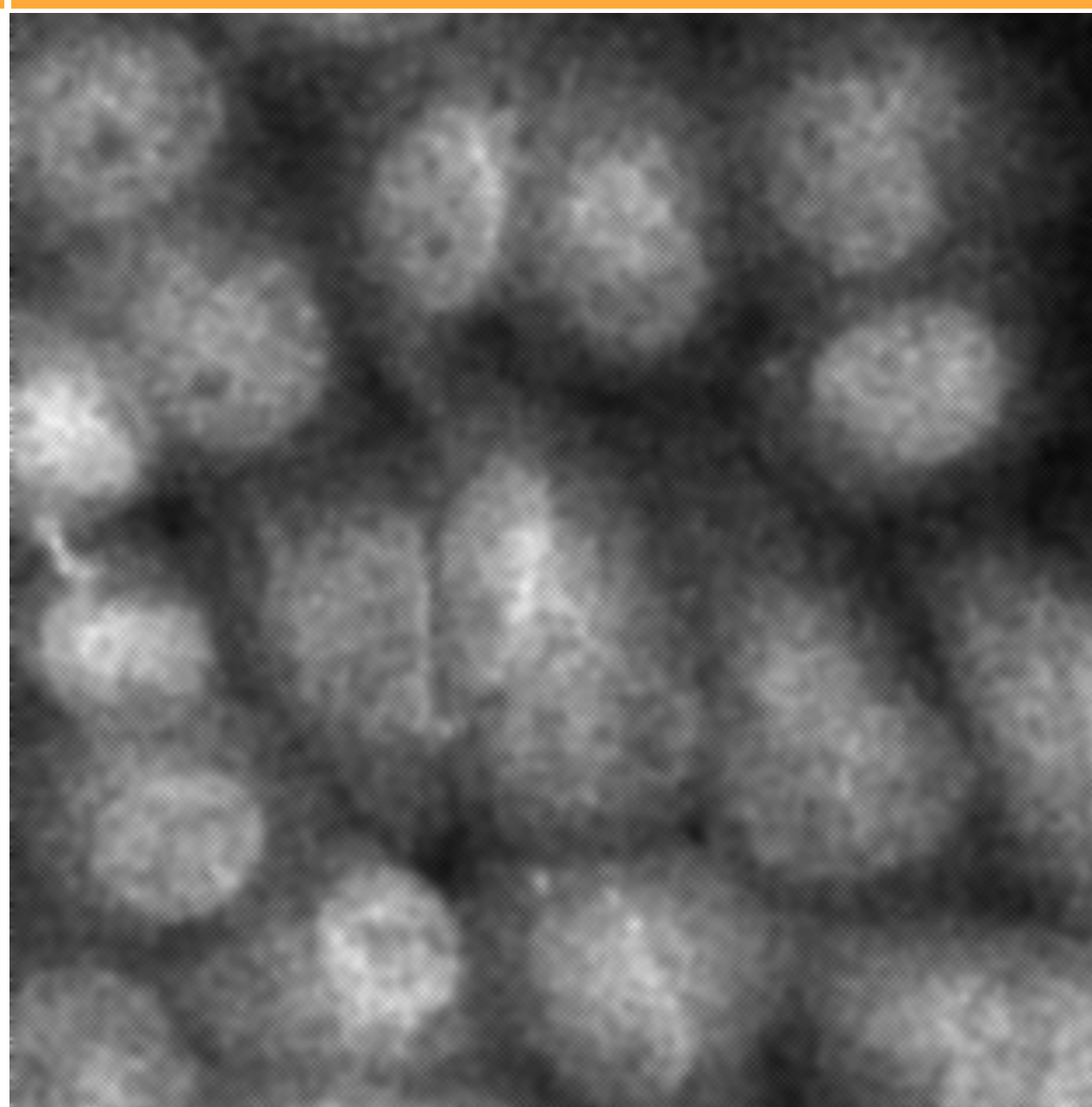
Median filter



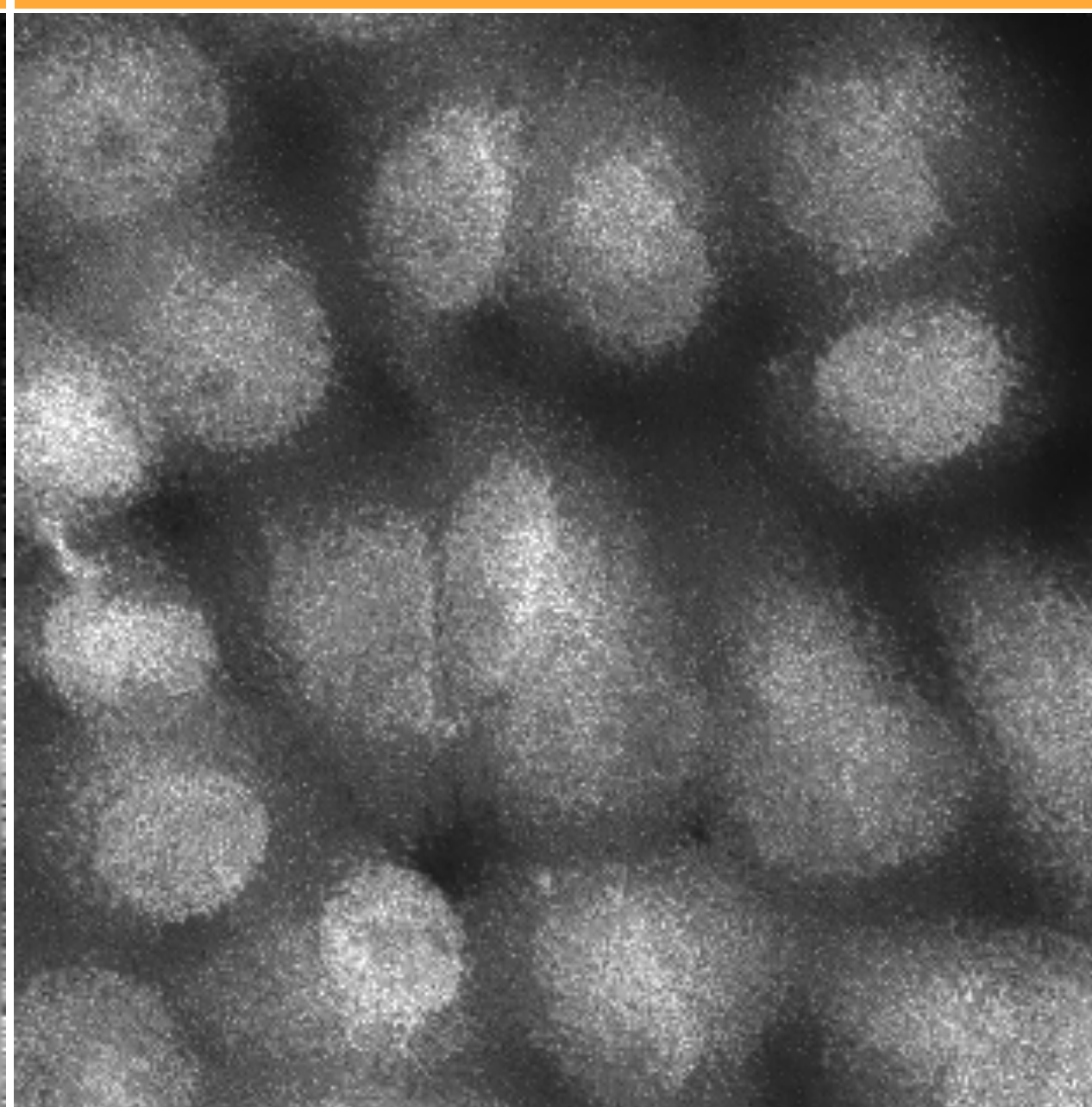
Anisotropic diffusion



PureDenoise auto

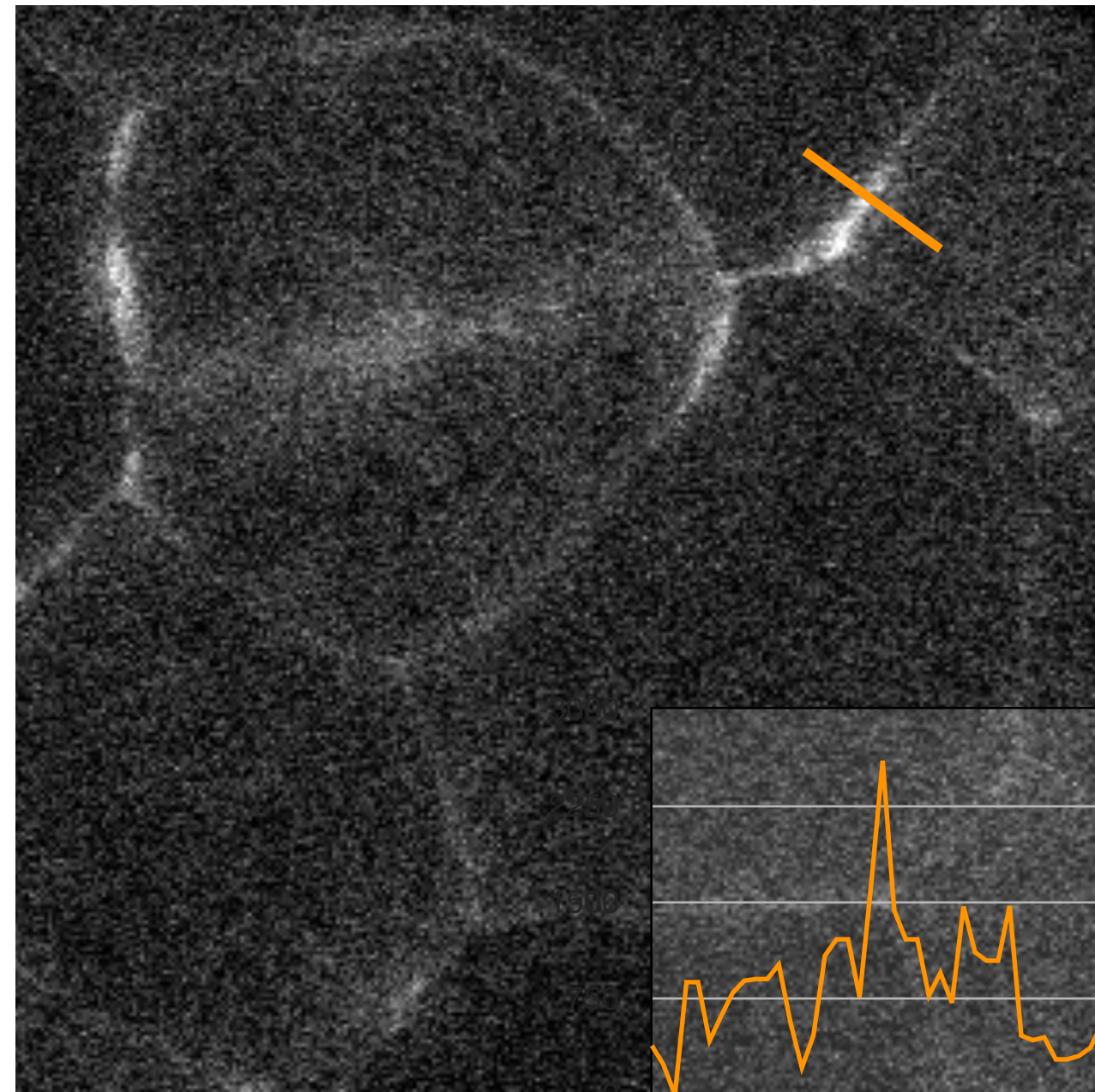


Total Variation auto

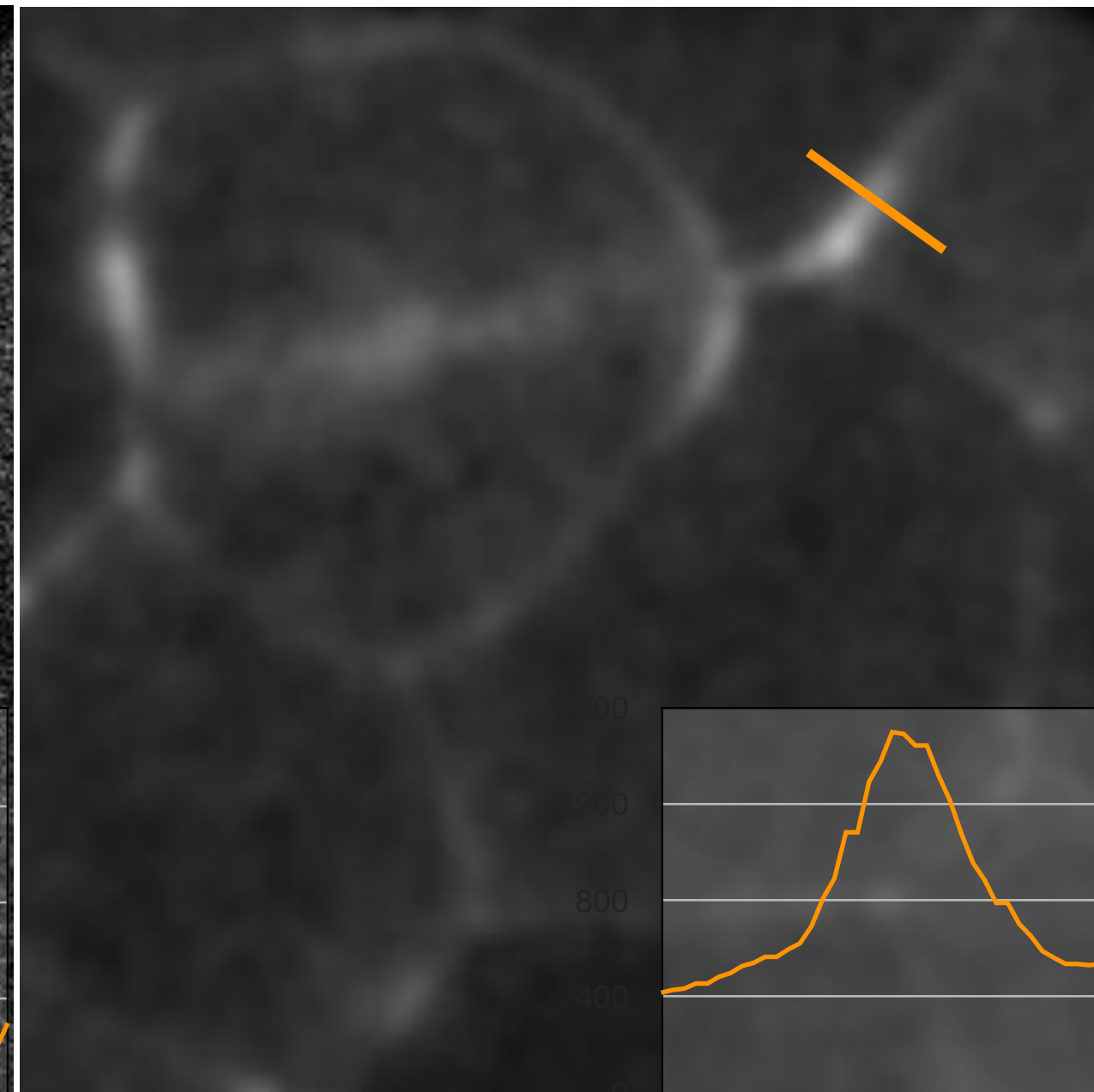


Non-local mean auto

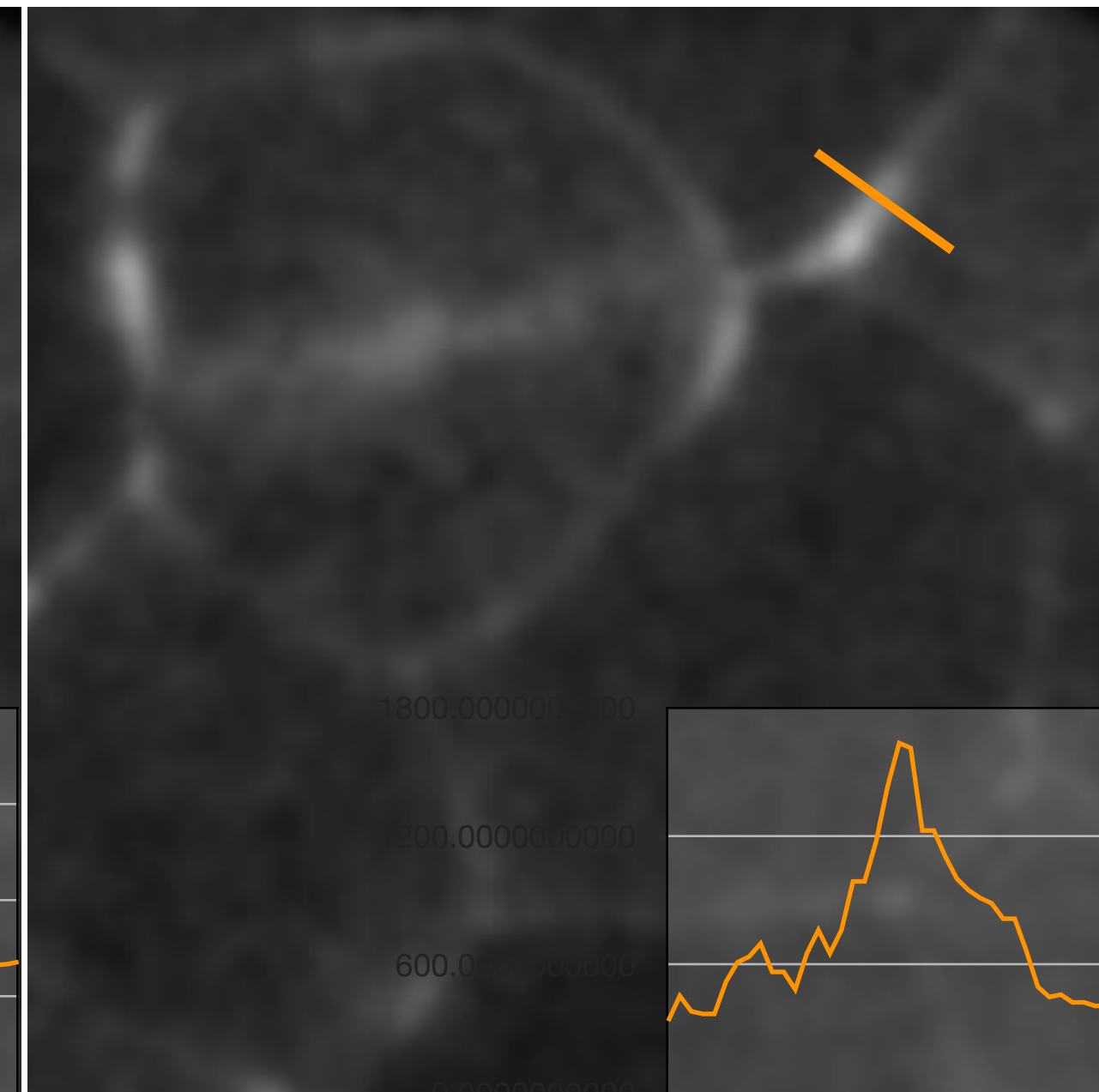




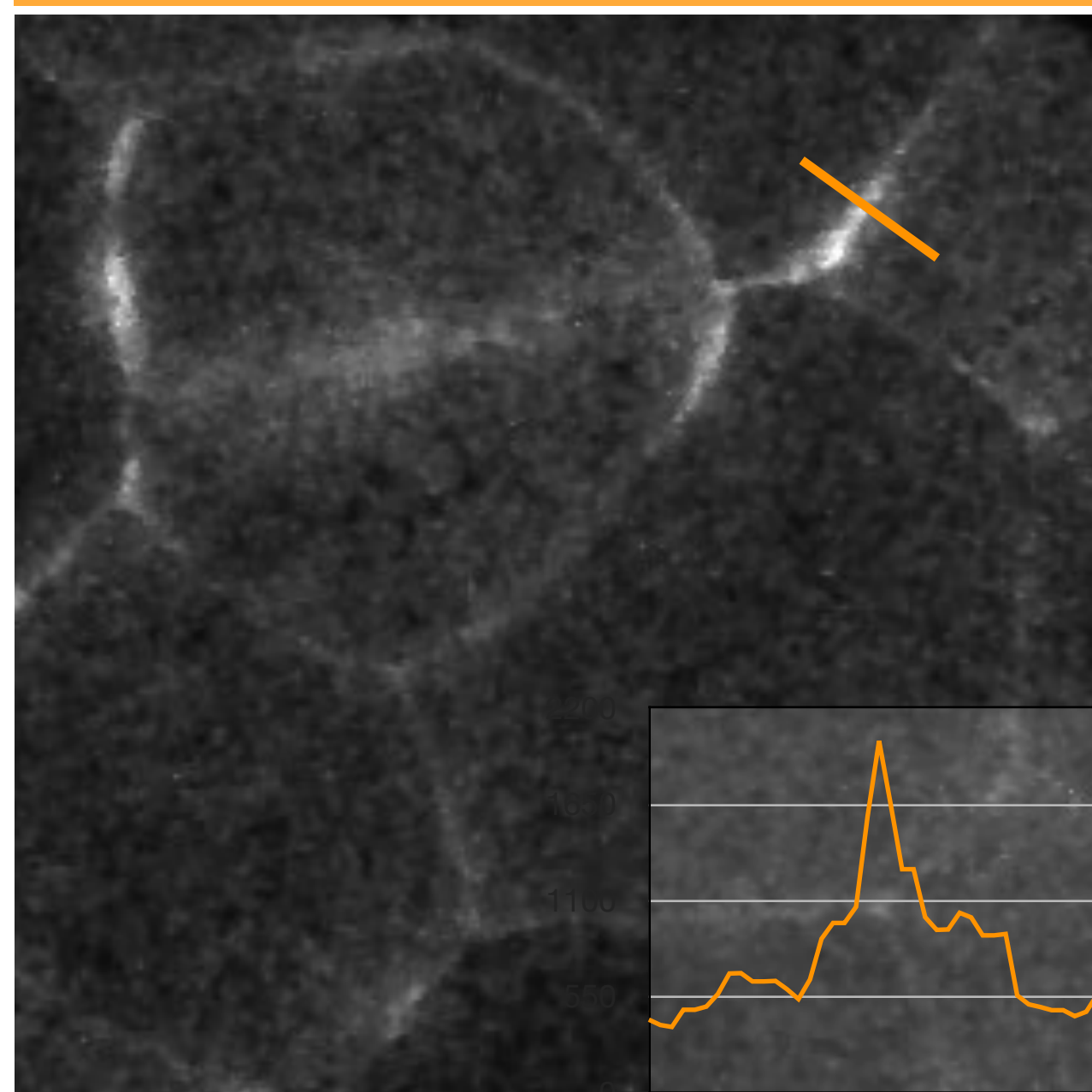
Input



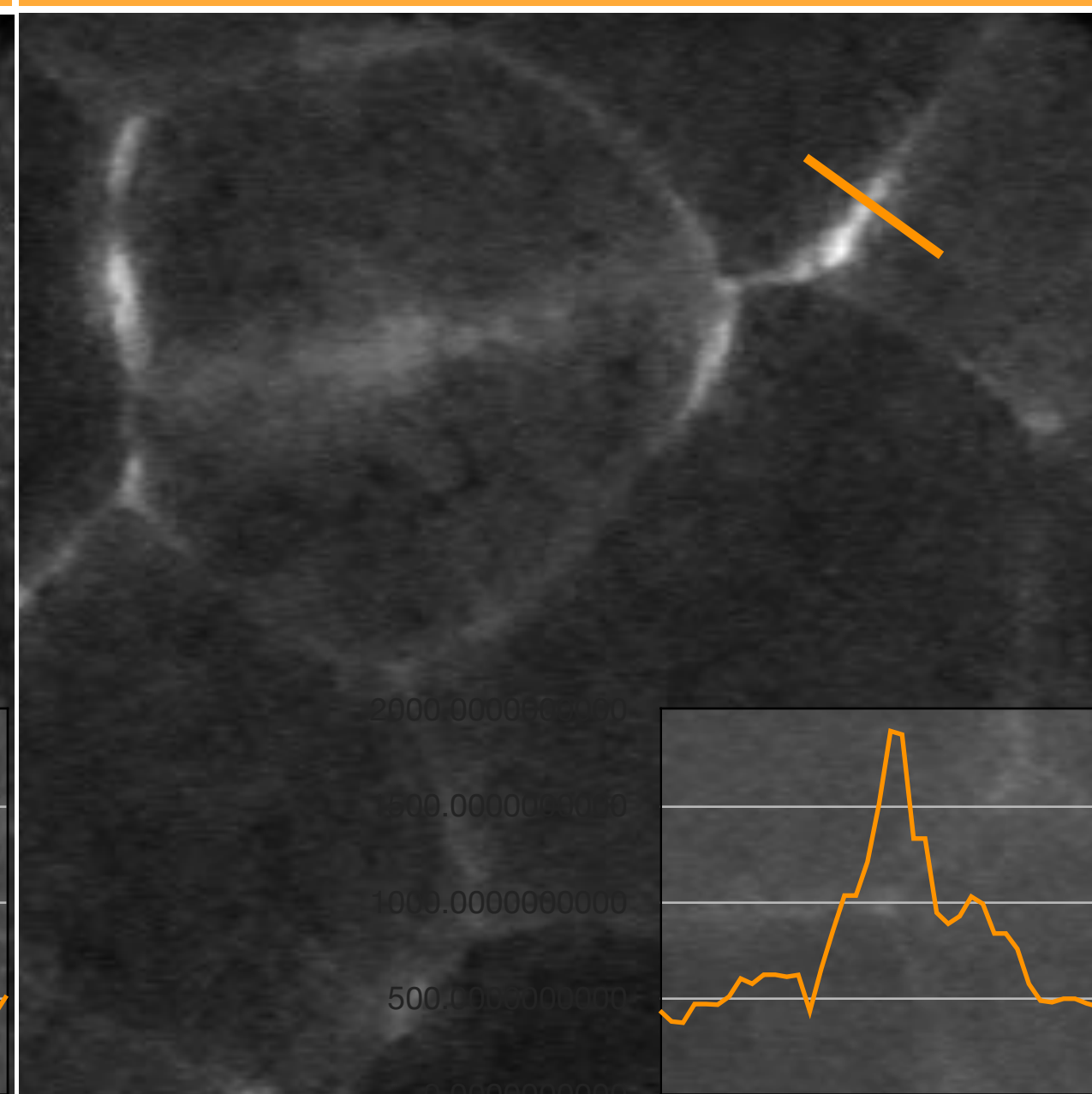
Gaussian filter



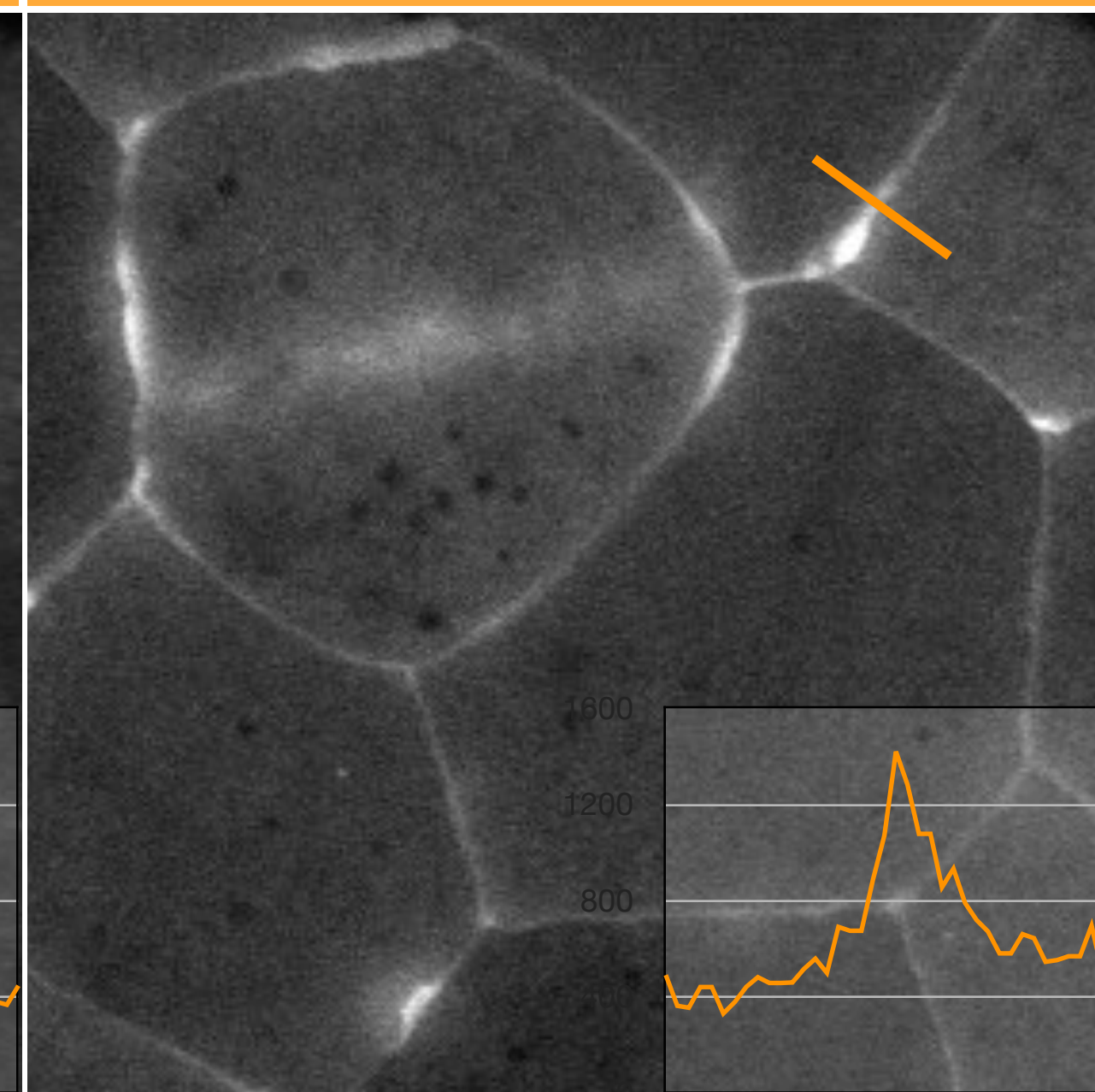
Median filter



Total Variation



PureDenoise



Average on 15 frames





# Take-Home Messages

## Which method to choose?

- Characterization of the noise (frequency)
- Prior of the structure (**self similarity** is relevant in bioimage)
- Selection of parameters (between noise and structure, automatic)

- ✓ **Acquisition** is the key to avoid corrupted image
- ✓ Denoising is useful for **image simplification** (scattering, autofluo)
- ✓ **Joint** denoising and segmentation performs better (e.g. active contour)
- ✓ **Quantification** is generally affected by denoising

## Acquisition

- Exposure time
- Denoising by averaging frames

