

# **Randomness and information in biological data**

## **BIO-369**

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**EPFL**

Lecture 3

Do you expect thermal fluctuations to be:

- A. Negligible at our scale and at the cellular scale
- B. Important at our scale and at the cellular scale
- C. Important at our scale but negligible at the cellular scale
- D. Negligible at our scale but important at the cellular scale
- E. It depends

To answer, please:

- Connect to <http://tppoll.eu>
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- Select your answer

# Outline of the course

## I Randomness in biological processes and biological data

### 1 Randomness and random variables

1.1 Coins and dice: discrete random variables

1.2 Medical testing and conditional probabilities

1.3 Luria-Delbrück experiment: Poisson distribution vs. jackpot distribution

### 2 Importance of thermal fluctuations at the cellular scale

2.1 Thermal fluctuations and associated energy scale

2.2 Strength of various chemical bonds

2.3 Flexibility of biopolymers and biomembranes

### 3 Random walks

3.1 Population genetics

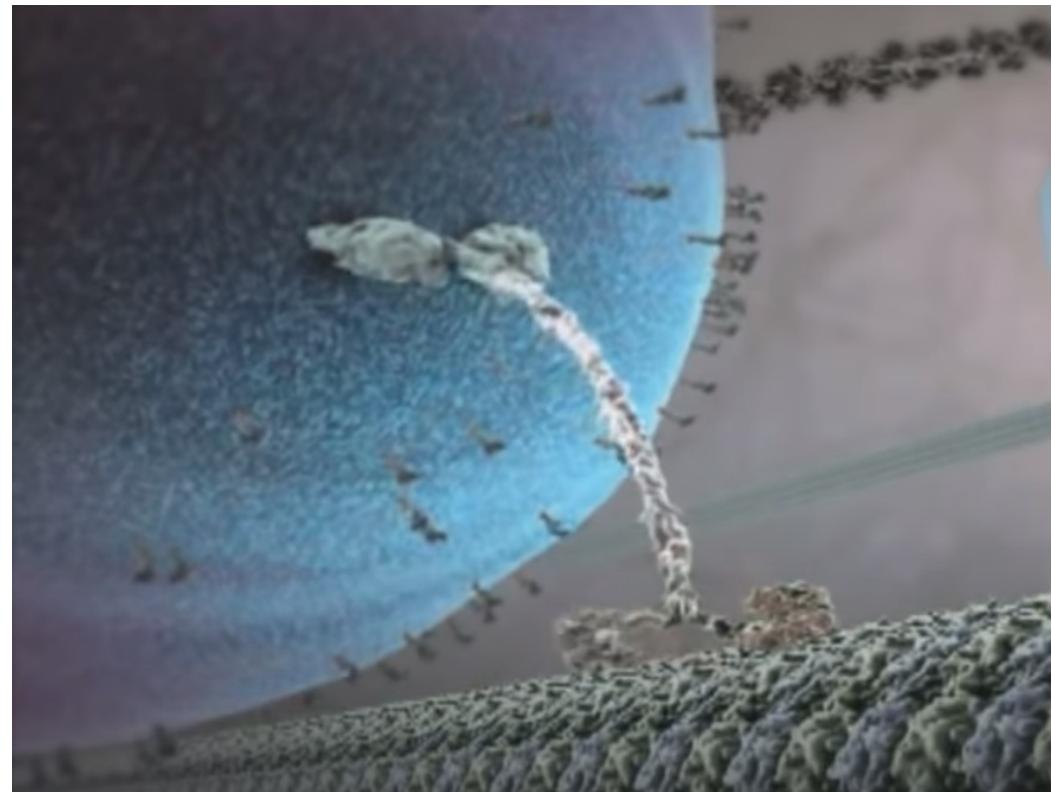
3.2 Protein abundances in single cells

3.3 Importance of random walks in biological systems

# Motivation

- Thermal fluctuations are important at the cellular scale: kinesin walking on a microtubule

- Kinesin = motor protein, found in eukaryotic cells
- Kinesins move along microtubule filaments *in one direction* ( $- \rightarrow +$ )
- Motion powered by the hydrolysis of ATP
- Involved in mitosis (spindle), meiosis and transport of cellular cargo, e.g. in axons
- Speed  $\sim$ 40 nm/s

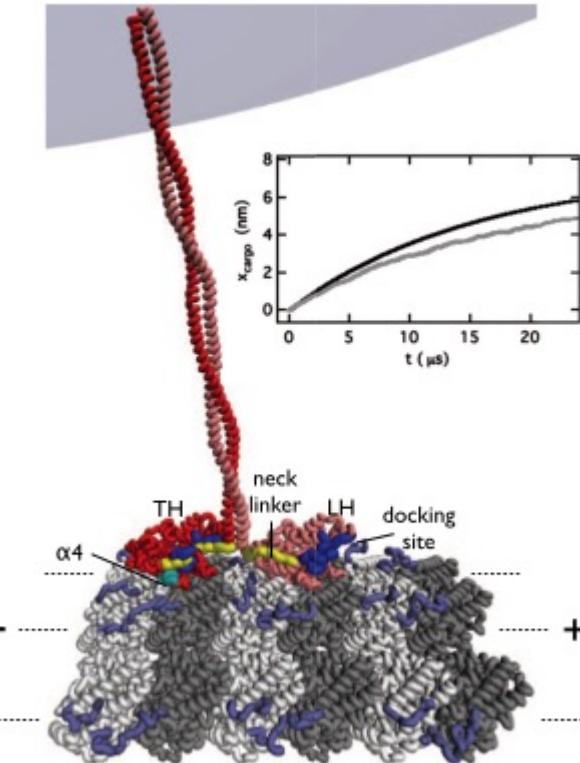


- Animation

<https://www.youtube.com/watch?v=wJyUtbn0O5Y> 1:14-1:25 (Harvard)

# Motivation

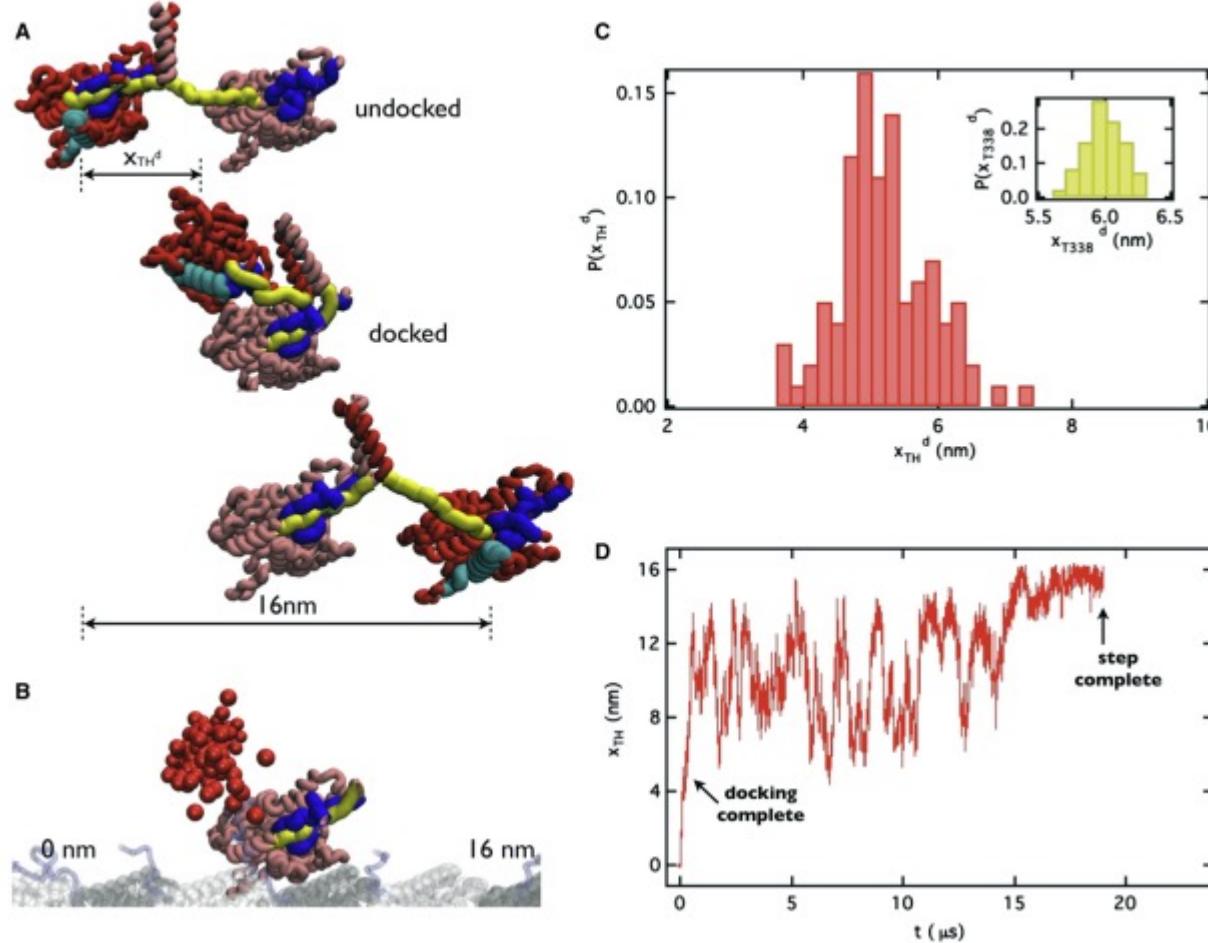
- Thermal fluctuations are important at the cellular scale: kinesin walking on a microtubule
  - Brownian dynamics simulation (Zhang & Thirumalai 2012)



<https://www.youtube.com/watch?v=JckOUrI3aes>

# Motivation

- Thermal fluctuations are important at the cellular scale: kinesin walking on a microtubule
  - Brownian dynamics simulation (Zhang & Thirumalai 2012)



Histograms, based on 99 trajectories, of the TH (trailing head) movement

Time-dependent changes in the center of mass of the TH as a function of  $t$  for a sample trajectory

What is the unit of the Boltzmann constant  $k_B$ ?

- 0% A. Joule (energy unit)
- 0% B. Kelvin
- 0% C. Joule / Kelvin
- 0% D. Joule . Kelvin
- 0% E. Something else

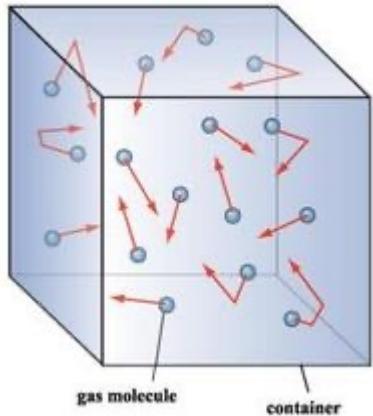
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# Thermal fluctuations in a gas

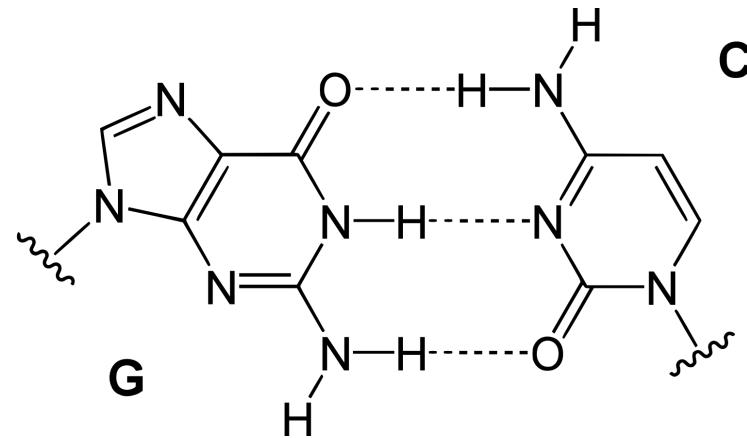
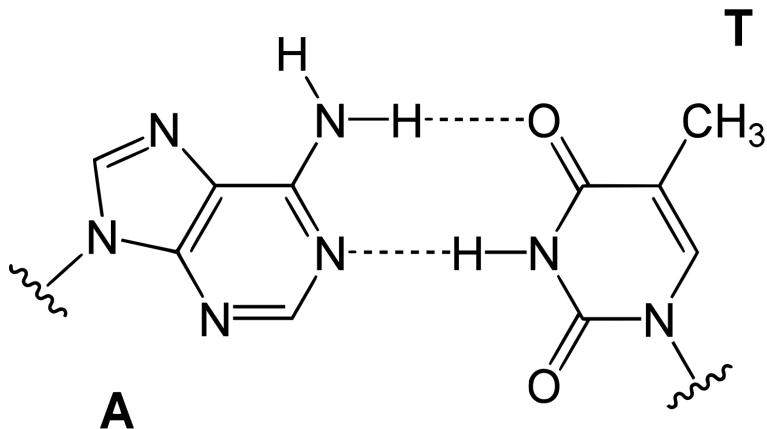
- Random motion (microscopic) → pressure (macroscopic)

- Gas molecules hit the walls of the box



# Hydrogen bonds

- Watson-Crick base pairs in DNA



Do you expect the bond between two DNA bases to be:

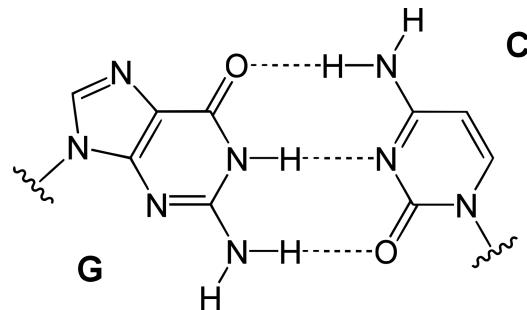
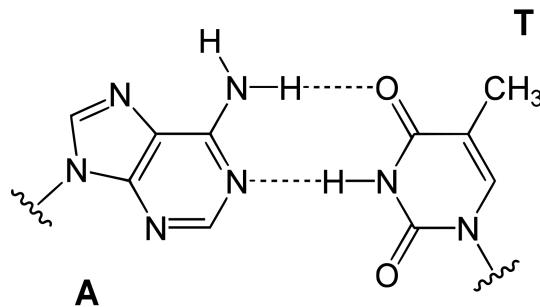
- A. Quite robust to thermal fluctuations
- B. Not so robust to thermal fluctuations
- C. Completely destroyed by thermal fluctuations

To answer, please:

- Connect to <http://tppoll.eu>
- Enter the session ID **bio369**
- Select your answer

What base pair is more robust?

- A. A-T
- B. C-G
- C. It is the same



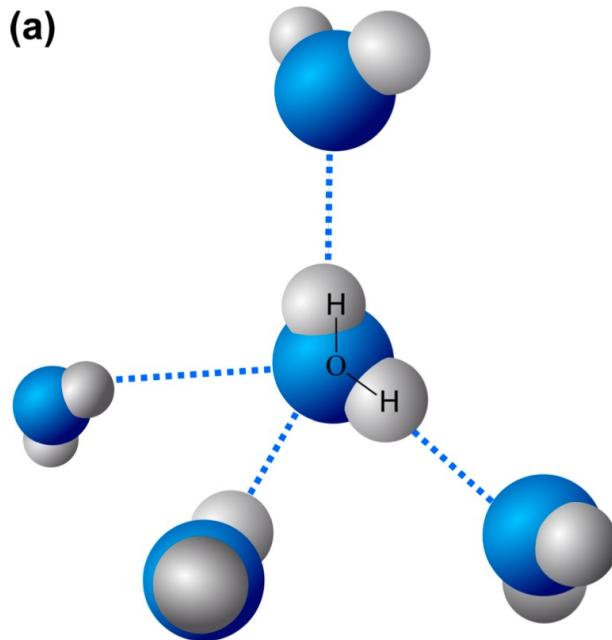
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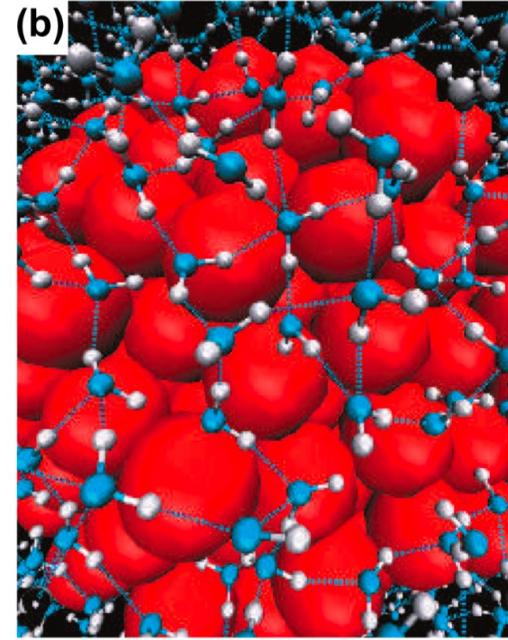
# Hydrophobic interactions

- Reorganization of dynamic hydrogen bonds between water molecules

(a)



(b)



(a): In bulk water, each water molecule is able to participate in up to four hydrogen bonds

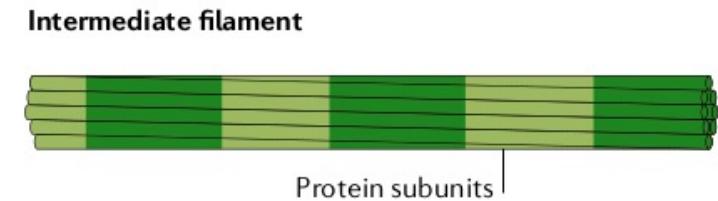
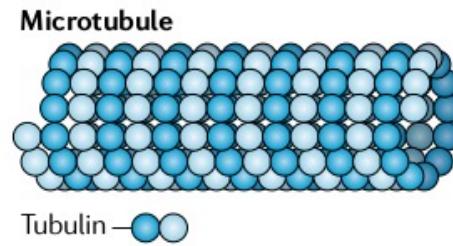
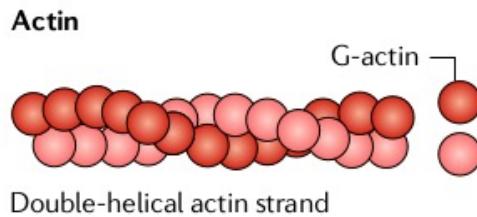
(b): Configurations of water molecules near a hydrophobic cluster (red) in a molecular dynamics simulation

# Motivation

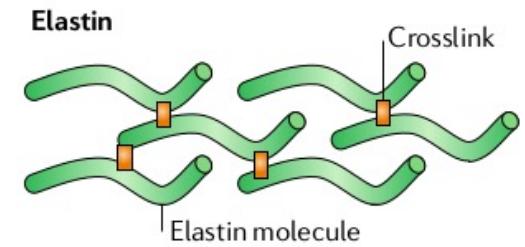
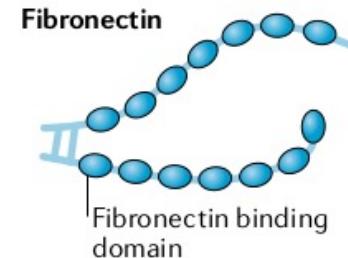
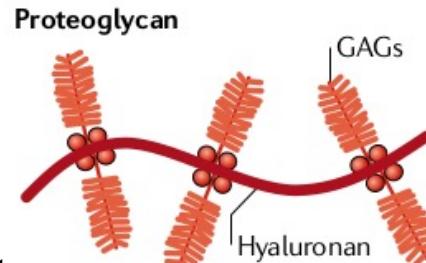
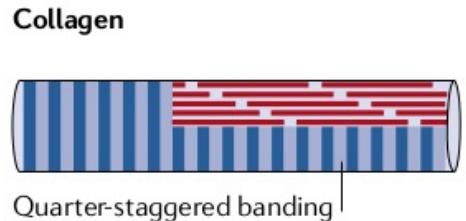
- Importance of biopolymers and biopolymer networks in and around cells

Cells and tissues are mechanically supported by biopolymer networks

- Cytoskeleton



- Extracellular matrix

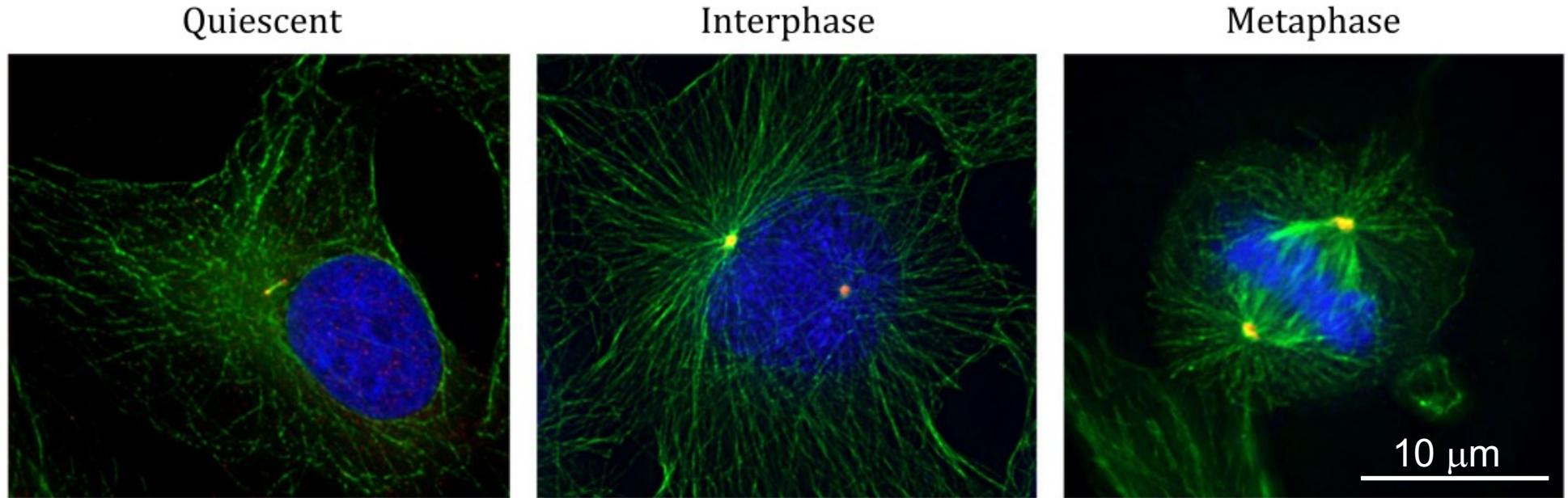


Collagen = most abundant protein in mammals

# Motivation

- Importance of biopolymers and biopolymer networks in and around cells

Microtubules are rigid and able to reorganize

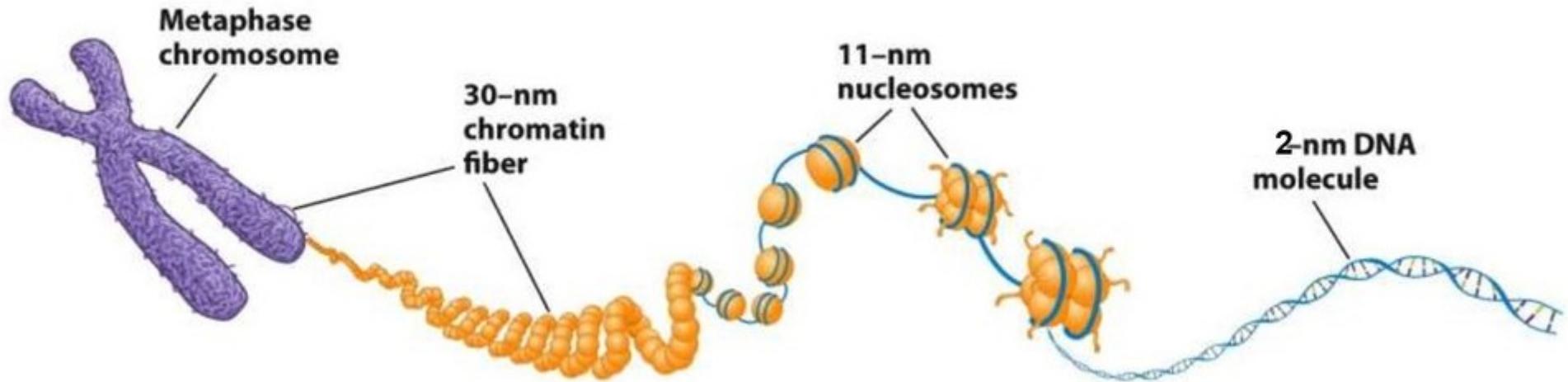


Green: microtubules / Blue: DNA

Fu and Zhang 2019

# Motivation

- Biopolymers are also the support of genetic information



DNA is quite flexible, and it compacts in eukaryotic cells

Remark: single proteins are also very important biopolymers, but we won't discuss them in this section (except those that form cytoskeletal protein) due to their particular 3D folding

Do you expect the persistence length of a microtubule to be:

- A. Larger than that of DNA
- B. Smaller than that of DNA
- C. The same
- D. It depends on the conditions

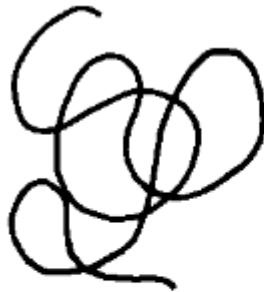
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# Flexibility of biopolymers

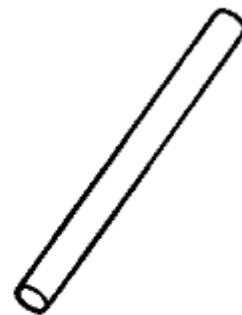
## ■ Persistence length

(a): total length  $\gg$  persistence length



(a)

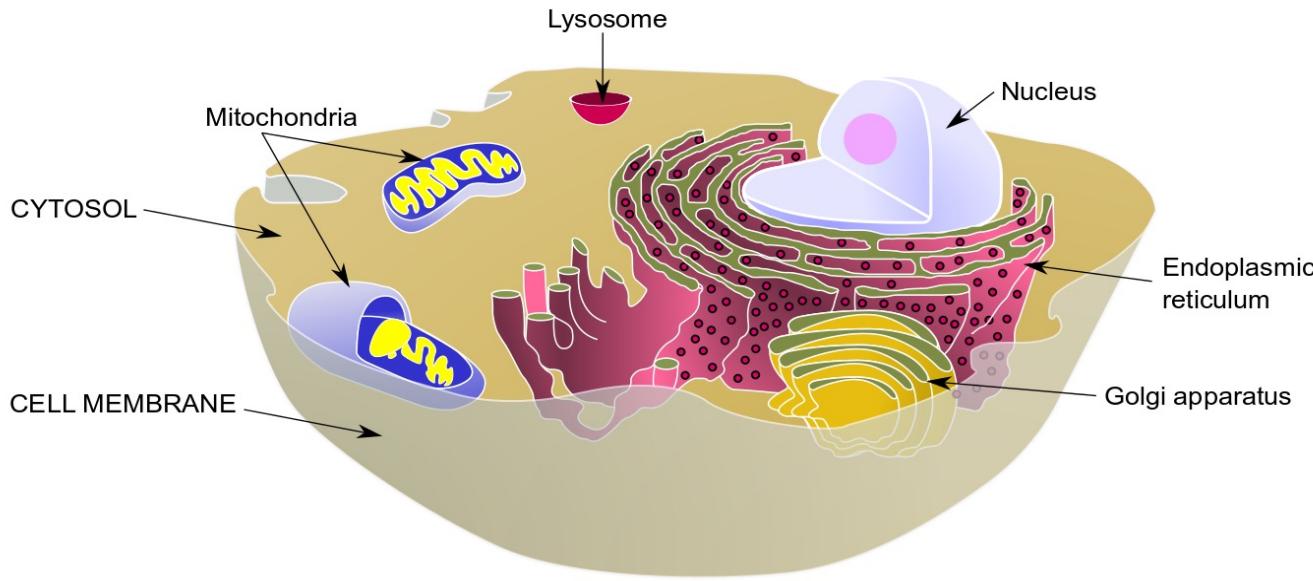
(b) total length  $\ll$  persistence length



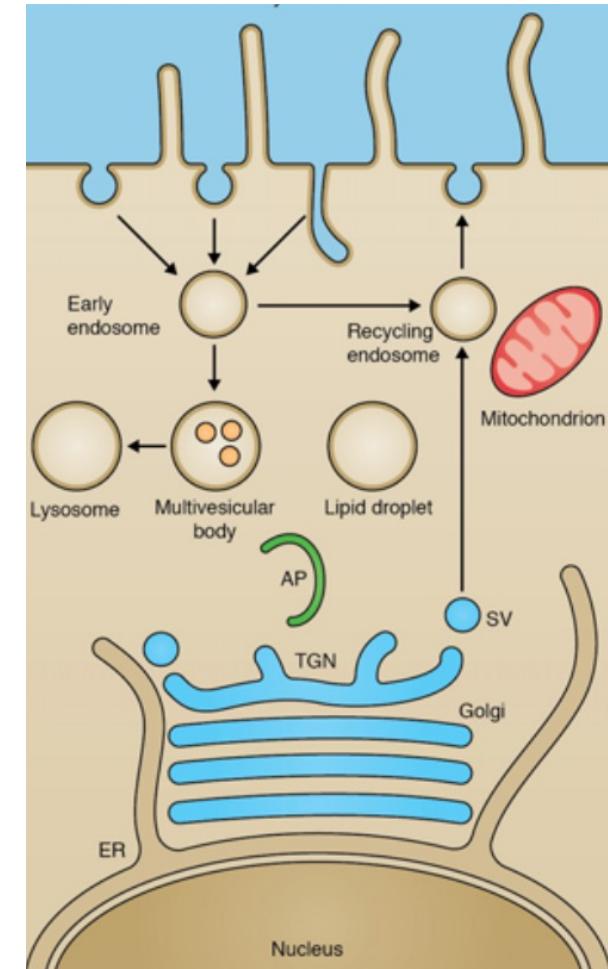
(b)

# Motivation

- Biomembranes are curved and constantly change shape



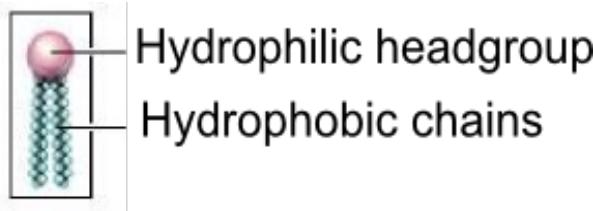
Membrane thickness: a few nm  
Cell size: 1 – 100  $\mu\text{m}$



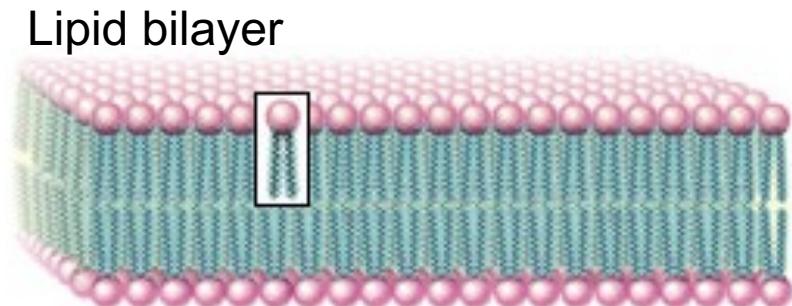
# Biomembrane properties

## ■ Basic structure

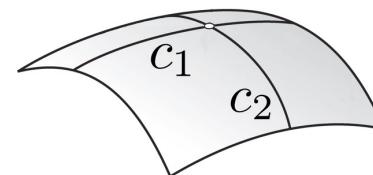
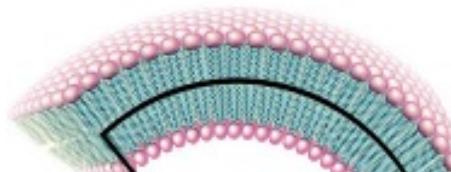
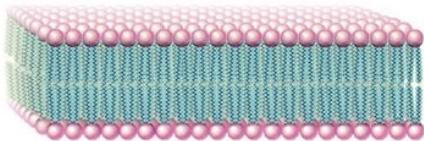
Lipid molecule: amphiphilic



Self-assembly  
in water



## ■ Elasticity: bending



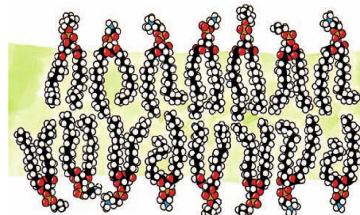
$$R_1 \rightarrow c_1 = \frac{1}{R_1}$$

Curvature energy:

$$H = \int_A dA \frac{\kappa}{2} (c_1 + c_2)^2$$

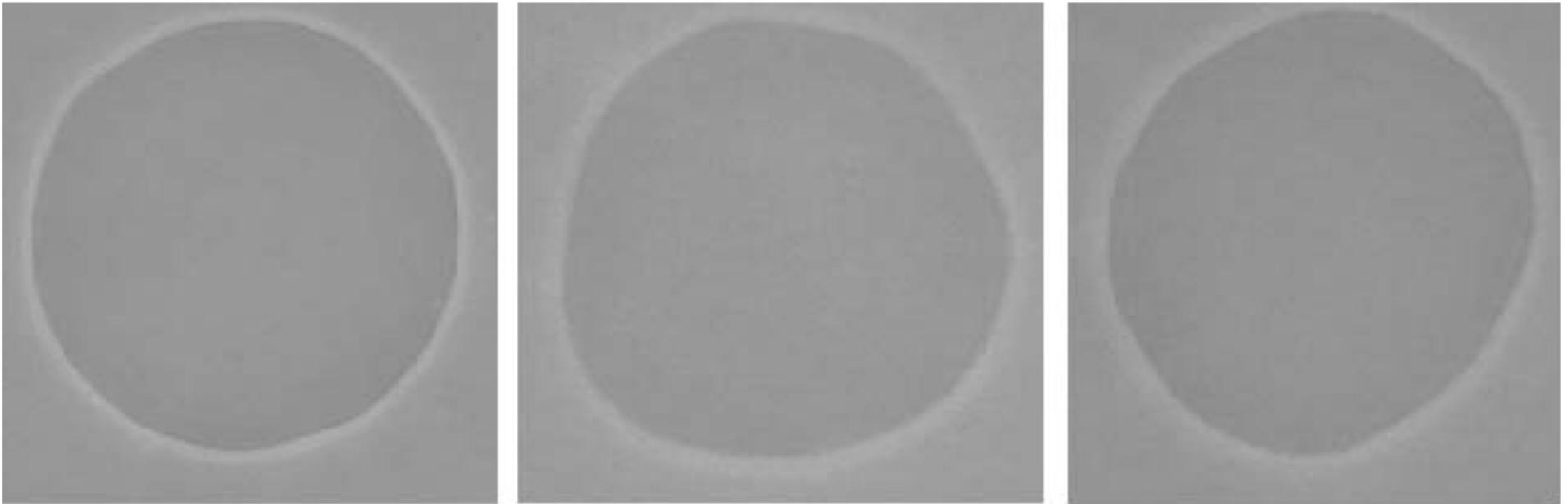
Helfrich (1973)

## ■ Fluidity



Each monolayer is a 2D fluid

## Flexibility of biomembranes



Snapshots of a giant unilamellar vesicle (i.e., a closed bilayer of lipids in water) of diameter 50  $\mu\text{m}$  observed under the microscope at different times

# Conclusion

- Thermal fluctuations have a strong impact at the microscopic scale, esp. at the cellular scale
- Importance of comparing the energy scales involved in important cell biology processes to the energy scale  $k_B T$  of thermal fluctuations (Boltzmann distribution)
- Many cell biology processes, including DNA base pairing, protein-protein interactions, biopolymer and biomembrane deformations, involve energies larger than  $k_B T$ , but not by a lot, typically of order  $10$  to  $20$   $k_B T$  → stable to thermal fluctuations but readily deformable
- In particular, can be deformed by active processes involving ATP consumption:  
Hydrolysis of ATP to ADP releases an energy of  $30$  kJ/mol, thus for the hydrolysis of one molecule of ATP:

$$\Delta E_{\text{ATP}} \approx 12 k_B T$$

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