

the number of stars formed in the mass interval  $(m, m + dm)$   $\phi(m)\psi(t)dm dt$

$\psi(t)$  Star formation rate (SFR) - total mass of stars per unit time

$\phi(m)$  Initial mass function (IMF) - number of stars formed @ mass  $m$

$\int_0^{\text{inf}} m\phi(m)dm = 1$  The IMF is normalized

$\phi(m) \propto m^{1+x}$  Power law ;  $x \equiv$  slope of the IMF

$$\frac{dM}{dt} = f$$

change in mass of the system,  $f \equiv$  gas inflow  
or accretion rate

$$\frac{dM_s}{dt} = \psi - E$$

$E$  total ejection rate from stars of all  
ages and mass

$$\frac{dM_g}{dt} = -\psi + E + f$$

$$M = M_s + M_g$$

Total mass distributed in gas and stars.

$$\mu = \frac{M_g}{M} \quad \text{gas fraction}$$

$$M_s = (1 - \mu)M$$

$m \equiv$  initial mass

$\tau_m$   $m$  mass star lifetime       $w_m$   $m$  mass star remnant.

$$E(t) = \int_{m_t}^{\infty} (m - w_m) \underbrace{\psi(t - \tau_m)}_{\text{time of birth of } m \text{ mass stars}} \phi(m) dm \quad \equiv \text{Ejection rate}$$

turn-off mass

$$\frac{Z M_g}{dt} = -Z\psi + \underbrace{E_Z}_{\text{re-cycled + newly synthesized}} + Z_f f$$

evolution of mass of metals  
in the gas.  $Z$  can be any element  
(Ca, Mg, Fe ...)

$$\int_{m_t}^{\infty} \underbrace{mp_{zm}} \psi(t - \tau_m) \phi(m) dm$$

mass fraction of a star of mass  $m$   
converted to metals and ejected

rate of ejection of new metals

$$E_Z(t) = \int_{m_t}^{\infty} \left[ \underbrace{(m - w_m - mp_{zm})}_{\text{unprocessed material}} Z(t - \tau_m) + mp_{zm} \right] \psi(t - \tau_m) \phi(m) dm$$

Total ejection of old and new metals

$$Z_s M_s + Z M_g = \int_0^t \int_{m_t}^{\infty} mp_{zm} \psi(t' - \tau_m) \phi(m) dt' dm$$

mean metal mass

stars in gas

conservation equation

$$R = \int_{m_t}^{\infty} (m - w_m) \phi(m) dm$$

$$y = \frac{1}{1-R} \int_{m_t}^{\infty} m p_{zm} \phi(m) dm$$

Returned mass fraction

yield = mass of new metals ejected when unit mass of matter is locked into stars.