



5

Bottom-up approach

Growth

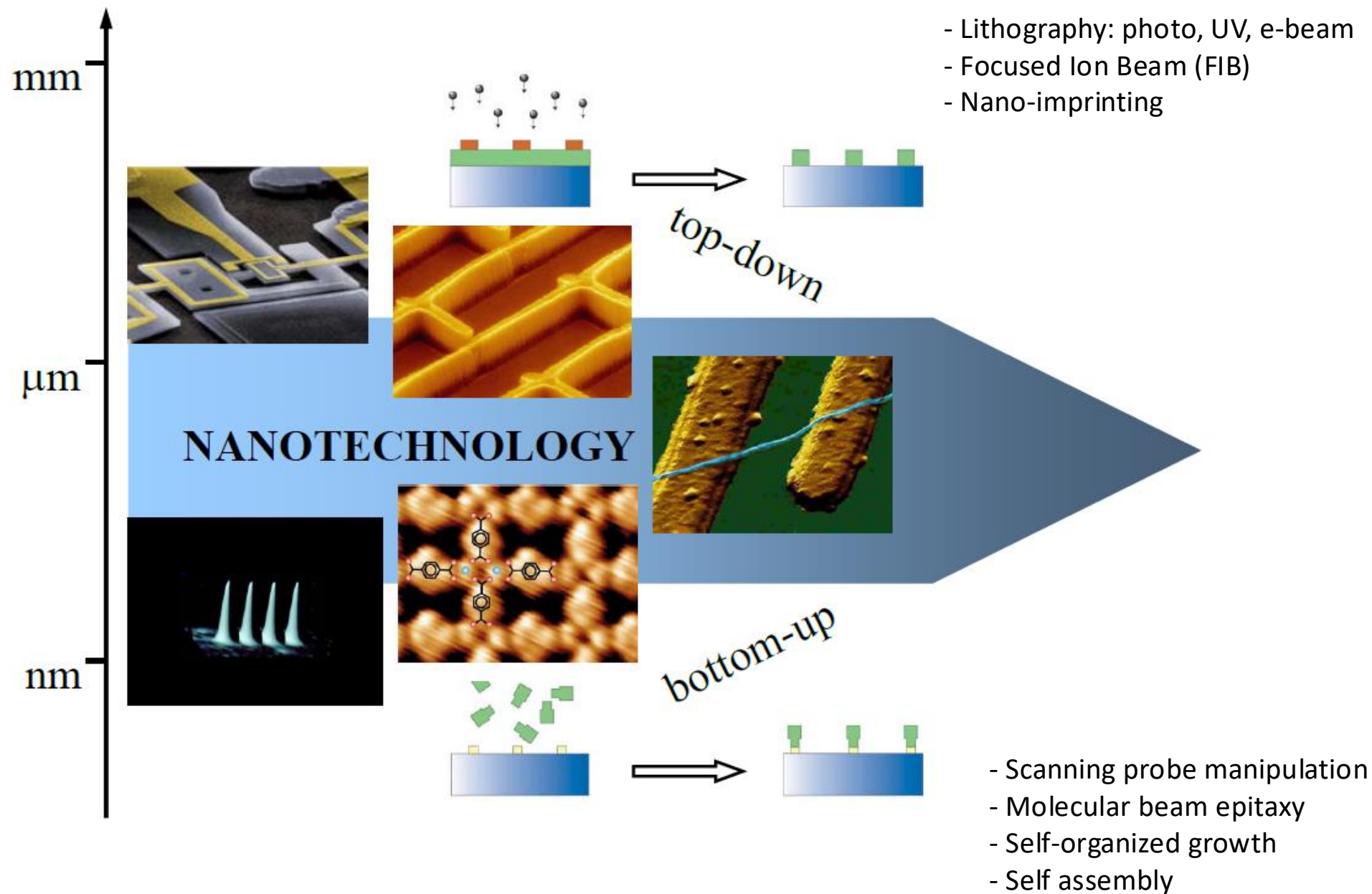


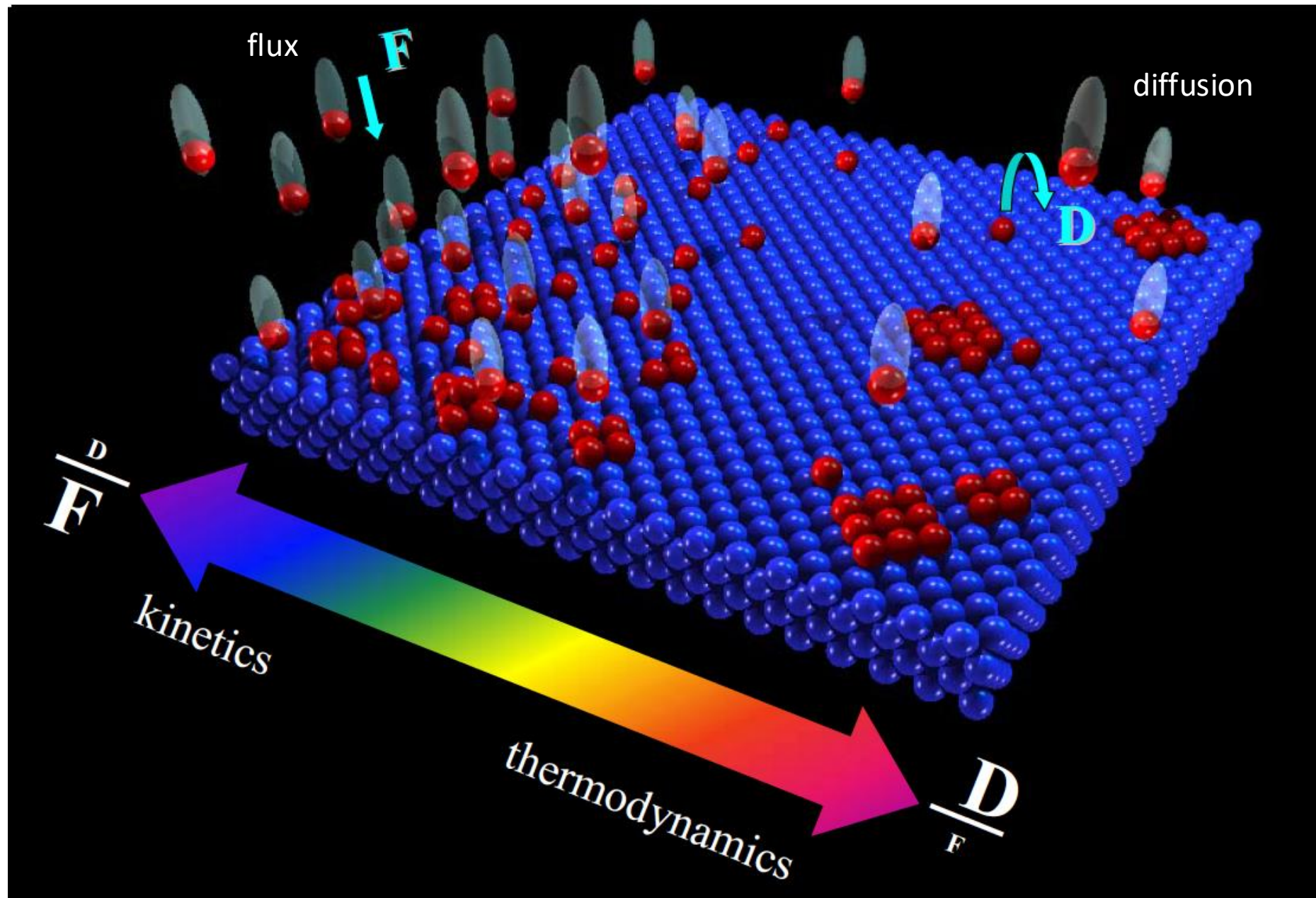
Introduction to Surface and Thin Film Processes  
J. A. Venables  
Cambridge University Press

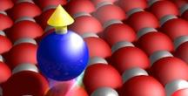
Epitaxial Growth of Thin Films  
H. Brune  
in: *Surface and Interface Science: Solid-Solid Interfaces and Thin Films*  
© 2014 Wiley-VCH Verlag GmbH & Co. KGaA



# How to make the nanostructures: two approaches







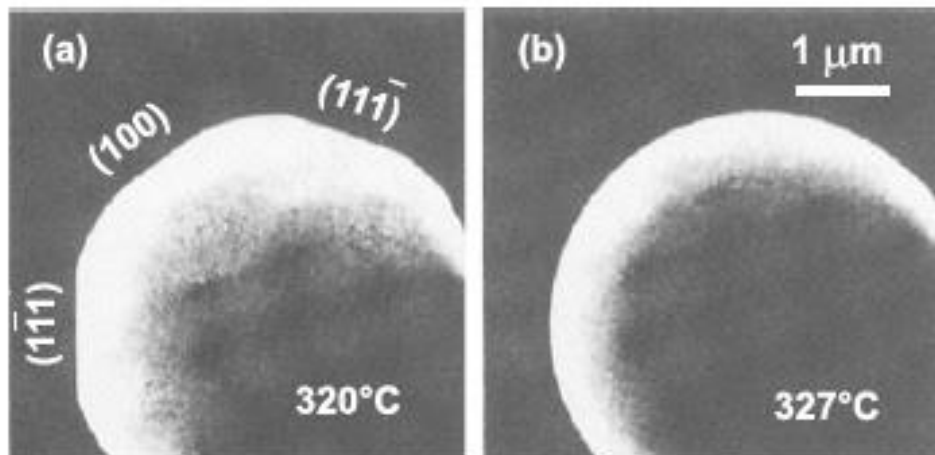
From bulk, creation of a surface (atoms that are not fully coordinated, i.e., there are broken bonds) → additional energy term  $\gamma$ : surface energy per unit surface (surface tension)

$\gamma > 0$  and energy =  $\gamma A$ , with  $A$  the area of the additional surface, at constant volume

Shape of a solid at equilibrium minimizes the surface energy

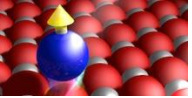
in liquids  $\gamma$  is isotropic → spherical shape (smallest surface area)

in solids  $\gamma$  is different for the different surface orientations of a crystal:  $\gamma(\vec{n})$



SEM photographs of the equilibrium shape of Pb crystals in the [011] azimuth; in b) Pb is liquid

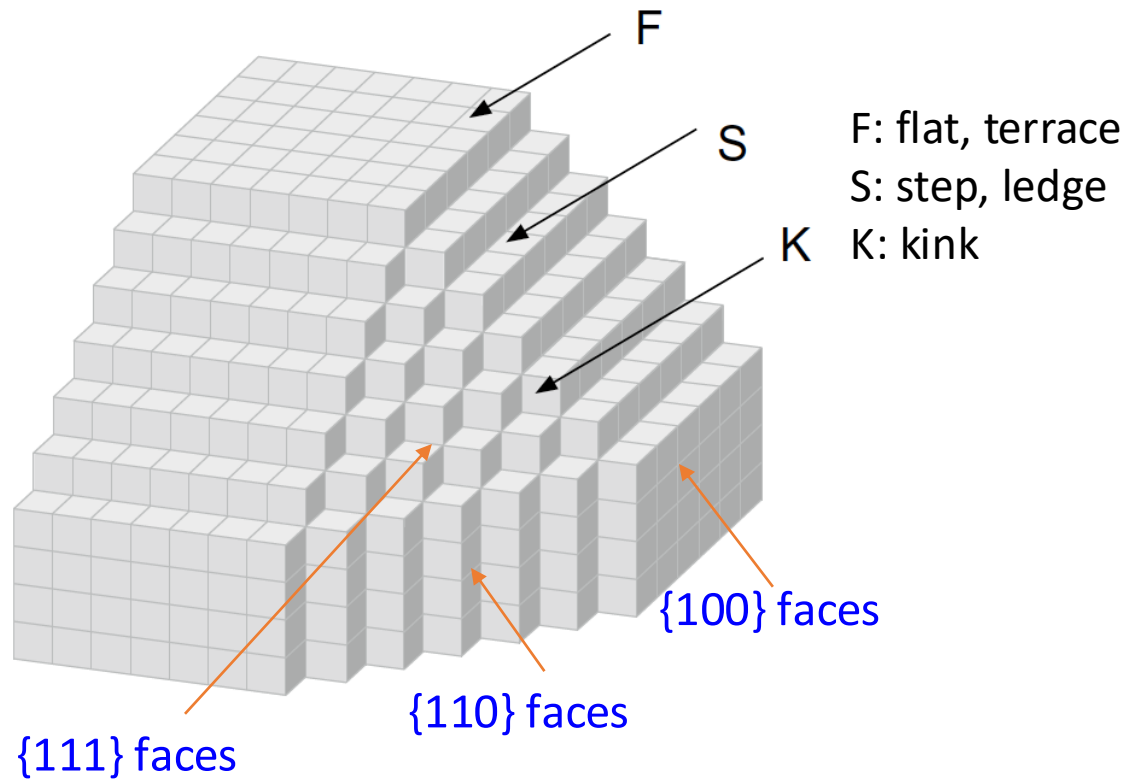
J.J. Métois & J.C. Heyraud, **31**, 73 (1989)



different crystal orientation → different surface energy

simplest model: Kossel crystal (simple cubic - sc)

evaluate the number of broken bonds per unit surface depending on the surface orientation



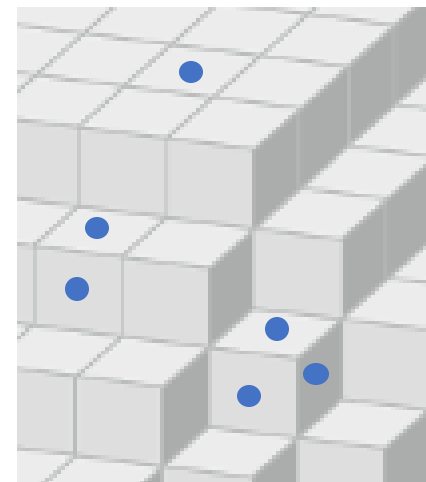
considering only the nearest neighbors (NN)

bulk: 6 NN → 6 bonds per atom

terrace: 5 NN → 5 bonds per atom, 1 broken bond

step: 4 NN → 4 bonds per atom, 2 broken bonds

kink: 3 NN → 3 bonds per atom, 3 broken bonds  
(half-crystal site)





## Exercises 5.1 – 5.3

Considering the number of broken bonds per unit surface, for singular (low-Miller index) surfaces:

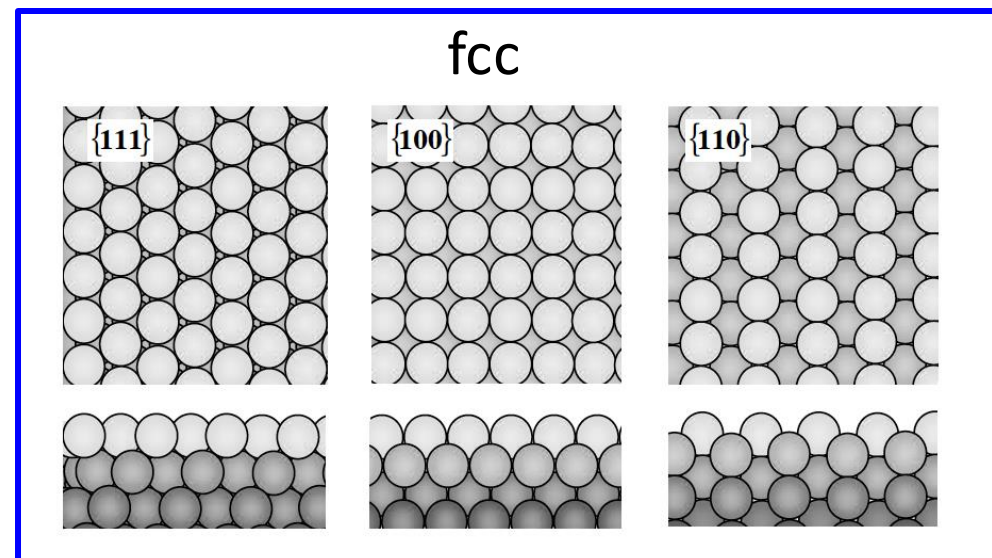
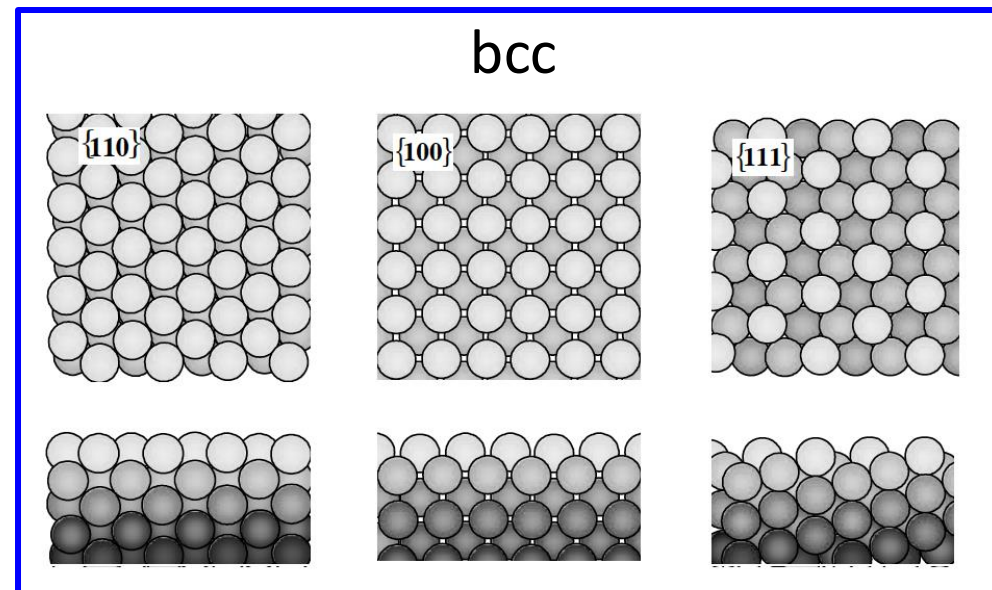
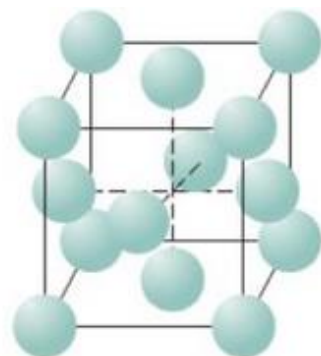
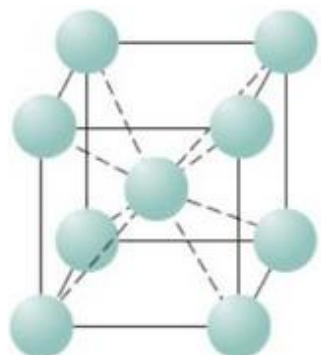
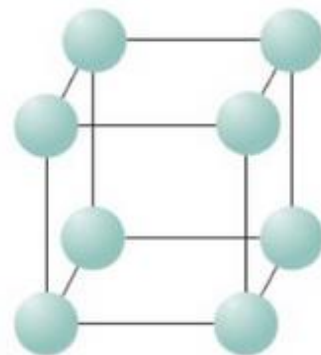
sc:  $\gamma_{100} < \gamma_{110} < \gamma_{111}$

bcc:  $\gamma_{110} < \gamma_{100} < \gamma_{111}$

fcc:  $\gamma_{111} < \gamma_{100} < \gamma_{110}$

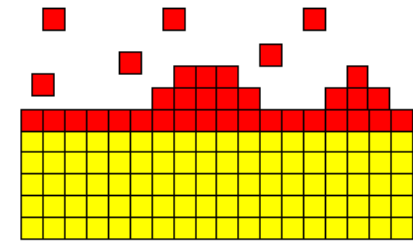
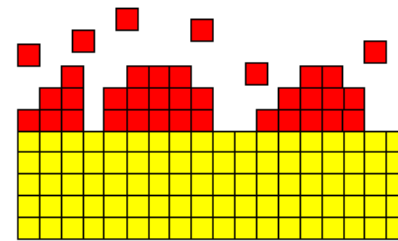
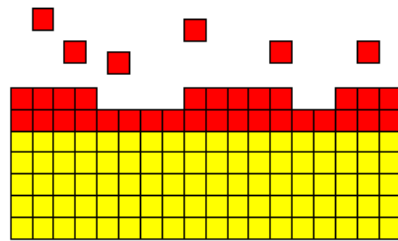
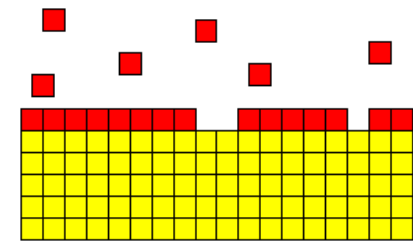
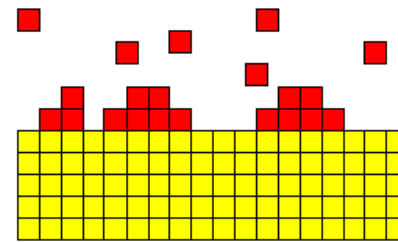
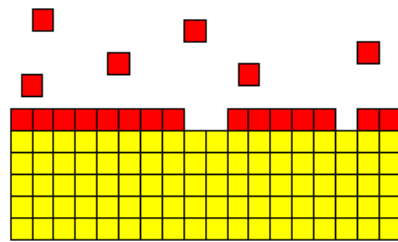
**in general, the more compact the surface, the lower the surface energy**

conventional unit cell





## Growth of A on B



$\gamma_A$ : surface energy of A  
(interface with vacuum)

$\gamma_B$ : surface energy of B  
(interface with vacuum)

$\gamma_{AB}$ :  
A-B interface energy  
(hybridization,  
lattice mismatch,...)

layer - by - layer growth  
(Frank - van der Merve)

$$\gamma_A < \gamma_B + \gamma_{AB}$$

island growth  
(Volmer - Weber)

$$\gamma_A > \gamma_B + \gamma_{AB}$$

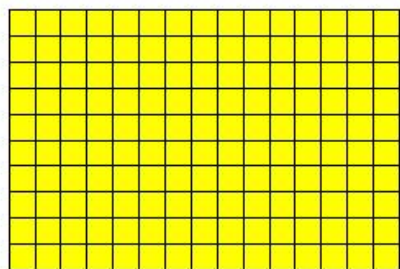
layer - by - layer  
+ island growth  
(Stranski - Krastanov)

$\gamma_A > \gamma_B + \gamma_{AB}$   
 $\gamma_{AB}$  increases with coverage  
(due to strain)  $\rightarrow$  change from  
2D to 3D

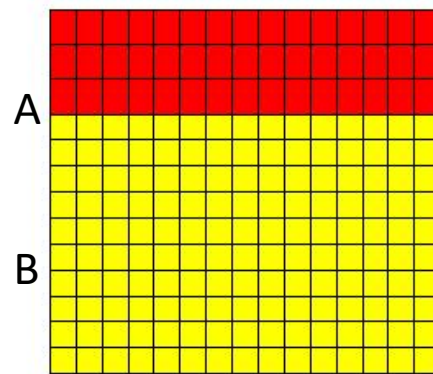


# Stranki-Krastanov growth of semiconductor quantum dots

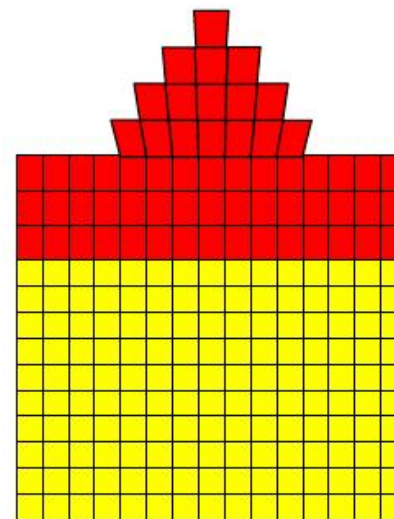
lattice constants:  $a_A > a_B$



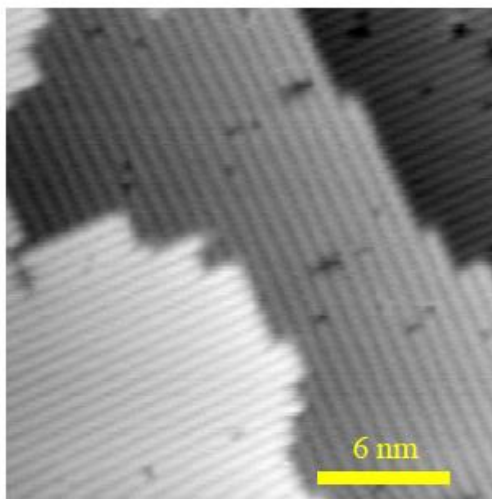
substrate



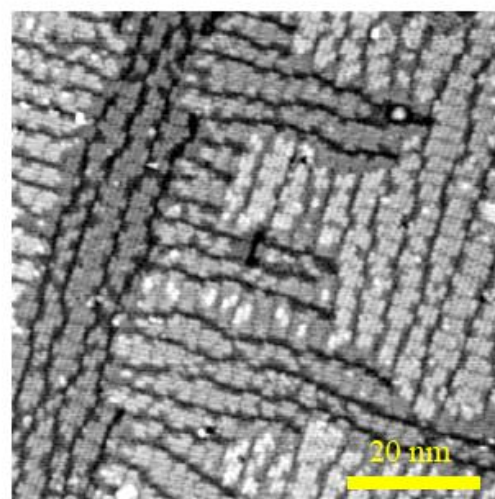
wetting layer



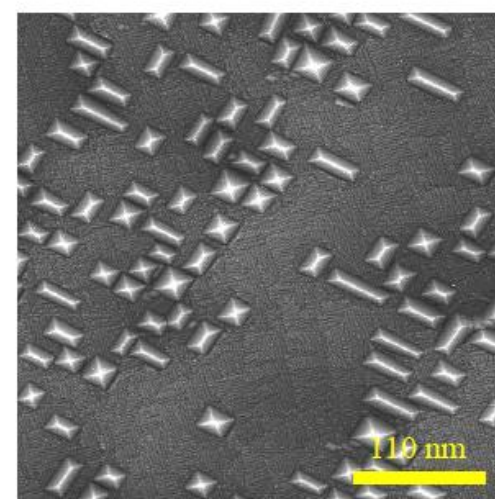
islands



Si(001)

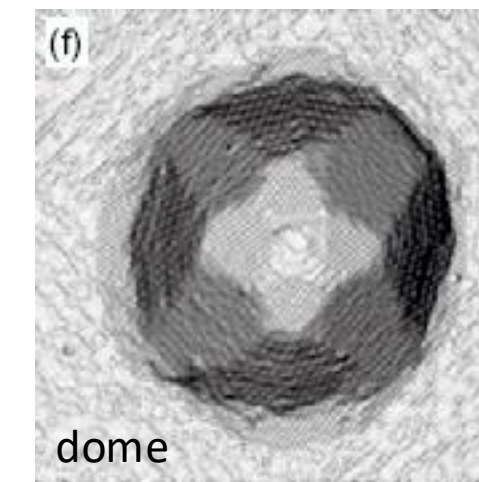
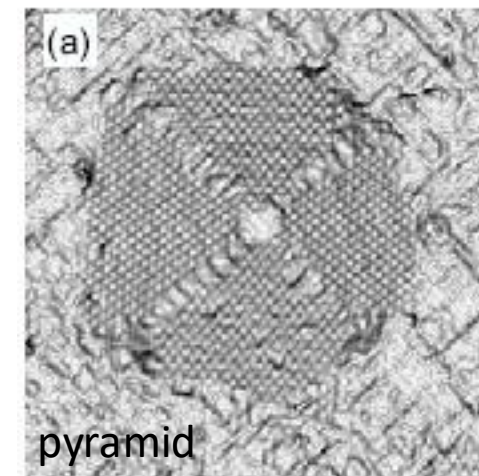


3ML Ge on Si(001)



6ML Ge on Si(001)

growth parameters

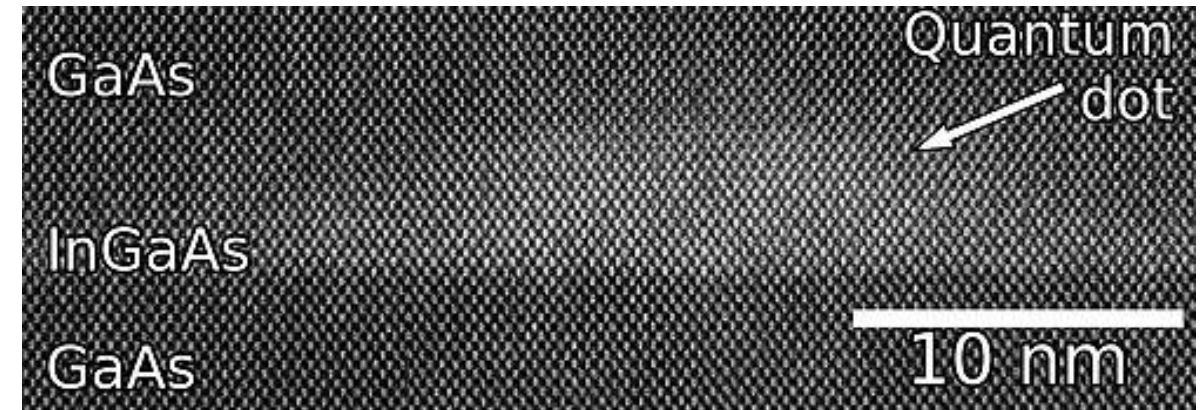
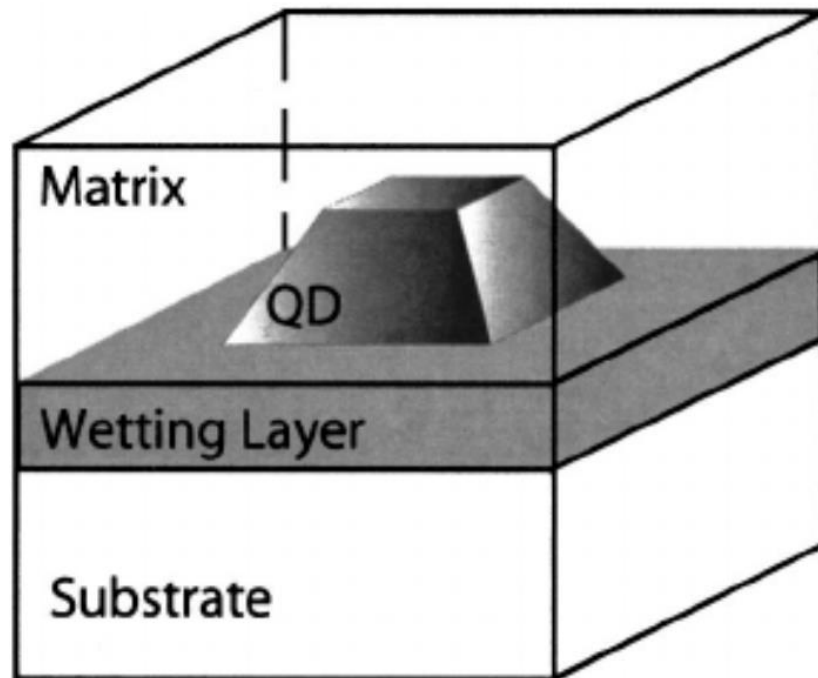




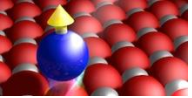
The islands can be subsequently buried

Potential applications:

- single-photon sources (quantum cryptography)
- quantum computation



TEM image

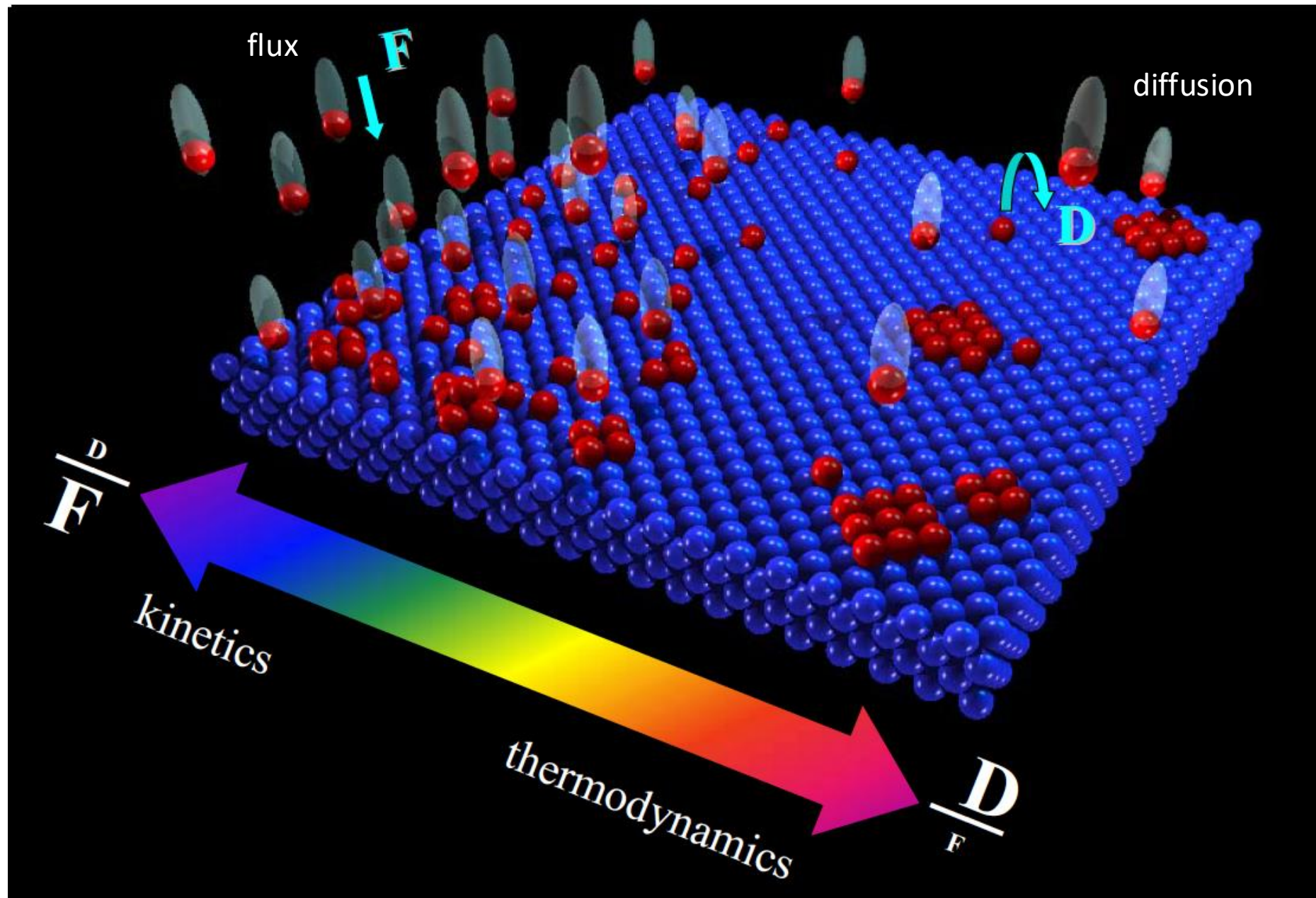


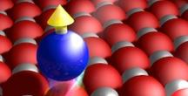
Solid-state electronic devices rely on the growth of sequences of many ultrathin epitaxial layers with atomically sharp interfaces and thickness control down to the monolayer level.

Examples:

- Alternating layers of large- and small-band-gap semiconductors are grown to tailor the electronic properties by quantum confinement of charge carriers in the small-band-gap regions (quantum well structures).  
Applications: ultrafast transistors, sensors, semiconductor lasers
- Sequences of ferromagnetic layers separated by nonmagnetic spacers; metallic or insulating spacer layers.  
Applications: spin valves, magnetic hard-disk read heads, magnetic-random access memories
- ...

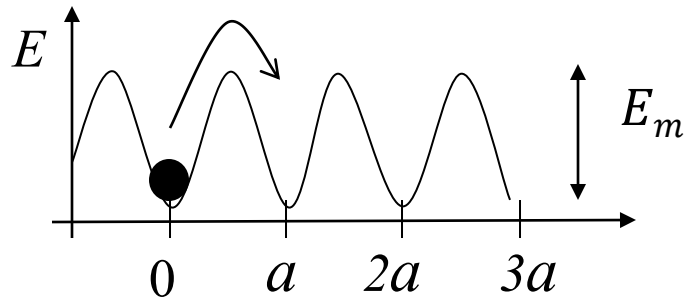
The growth of perfectly flat 2D layers of materials A/B, and subsequently B/A, is a stringent requirement for device functionality.





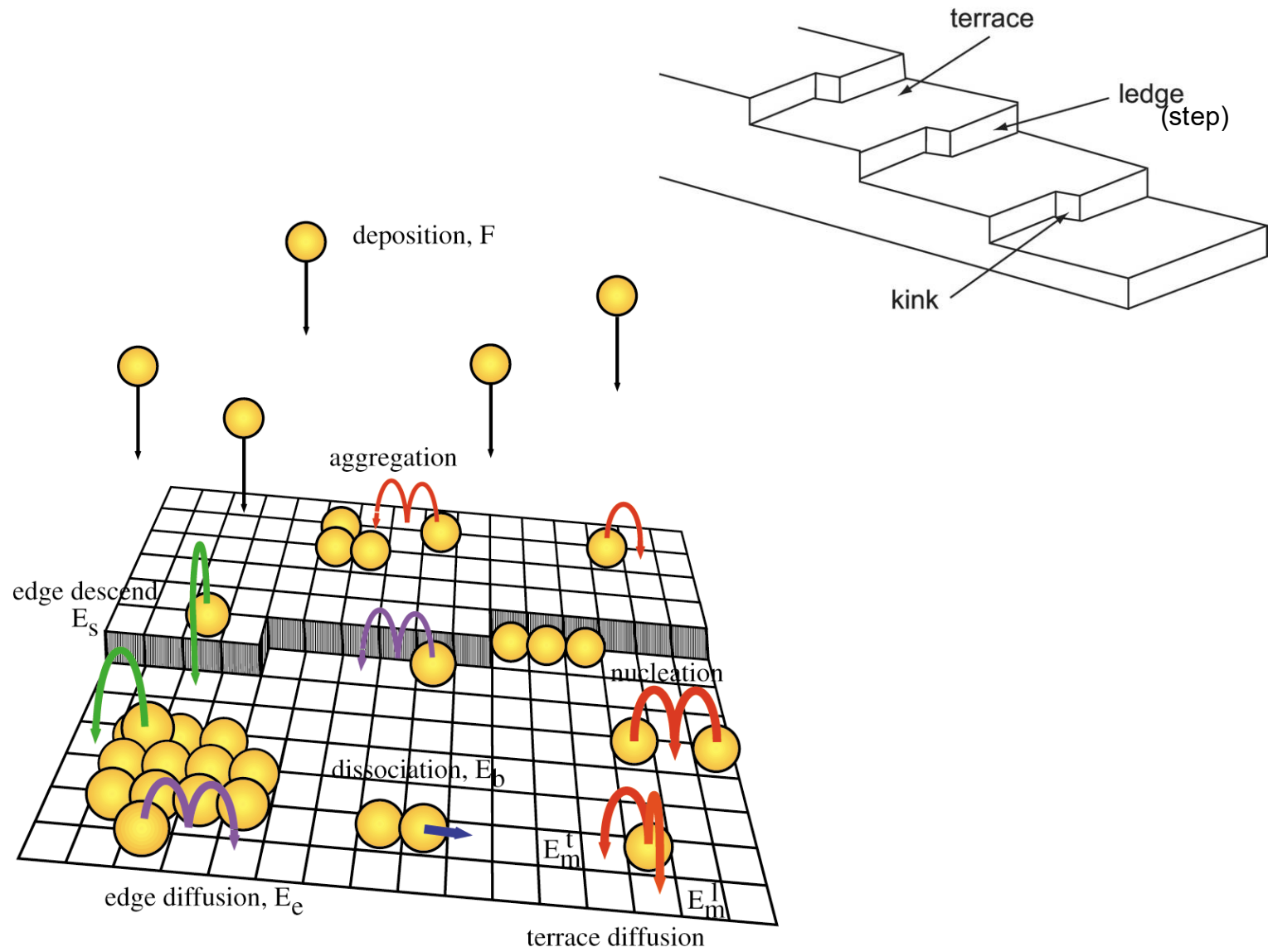
single crystal surfaces: a 2D laboratory

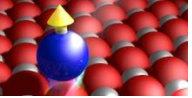
each process  $i$  has an energy barrier  $E_i$  and a rate  $n$



diffusion process, random walk  
 $a$  lattice constant,  $t$  time  
 number of jumps =  $\nu t$   
 mean squared displacement:

$$\langle \Delta r^2 \rangle = \nu a^2 t$$





## We aim at controlling:

- mean size
- size distribution
- density
- shape
- composition

## Control parameters are:

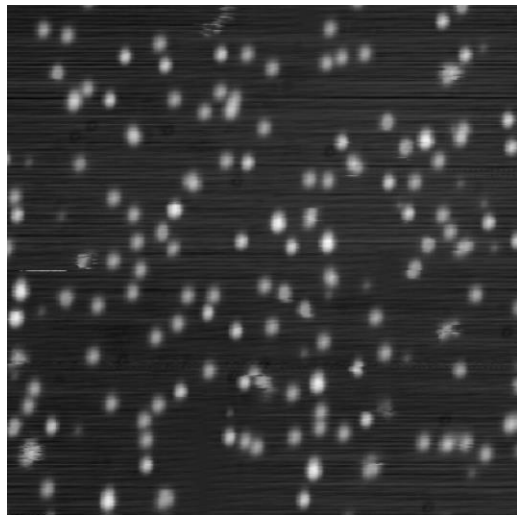
- substrate temperature  $T$
- deposition flux  $F$
- coverage  $\Theta$
- substrate/overlayer material (strain, mixing, etc.)
- substrate symmetry or patterning



- thermally-activated diffusion is frozen
- $\nu = \nu_0 \exp(-E_1/k_B T) \rightarrow 0$
- the coverage determines the mean island size  $n$
- broad size distribution

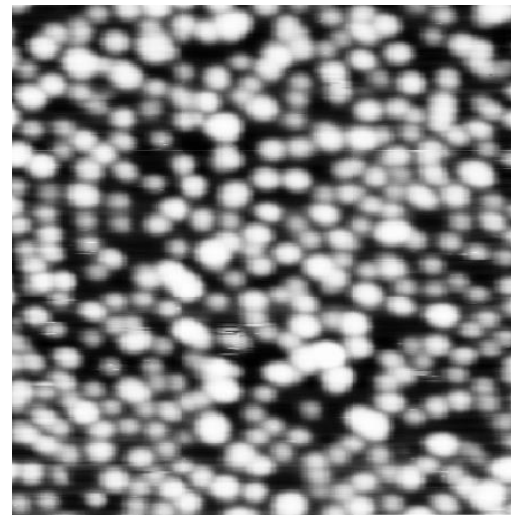
## Co/Pt(111)

0.03 ML,  $T = 50$  K  
 $n = 1.2$



50 Å

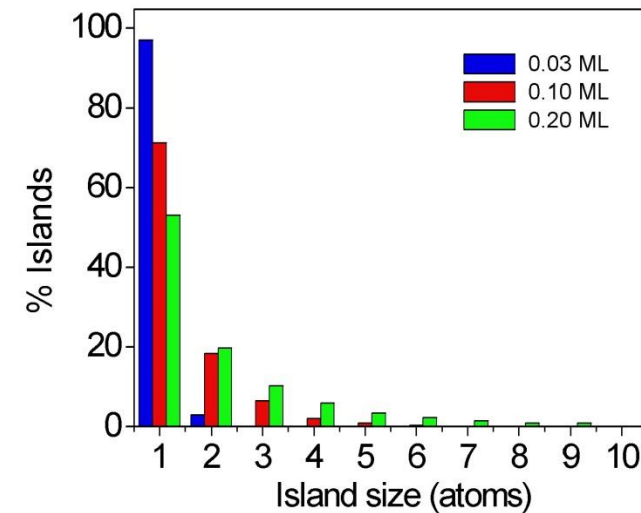
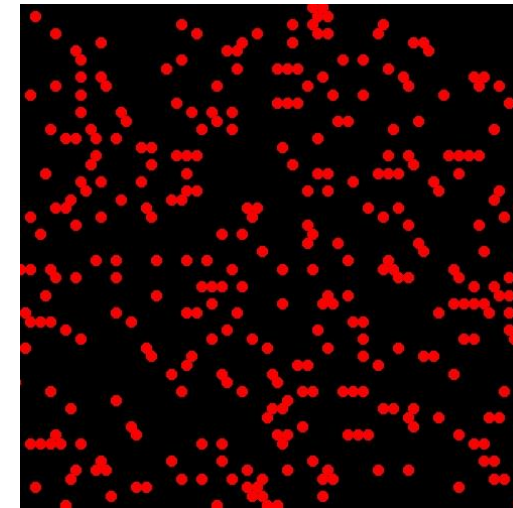
0.10 ML,  $T = 50$  K  
 $n = 2.9$

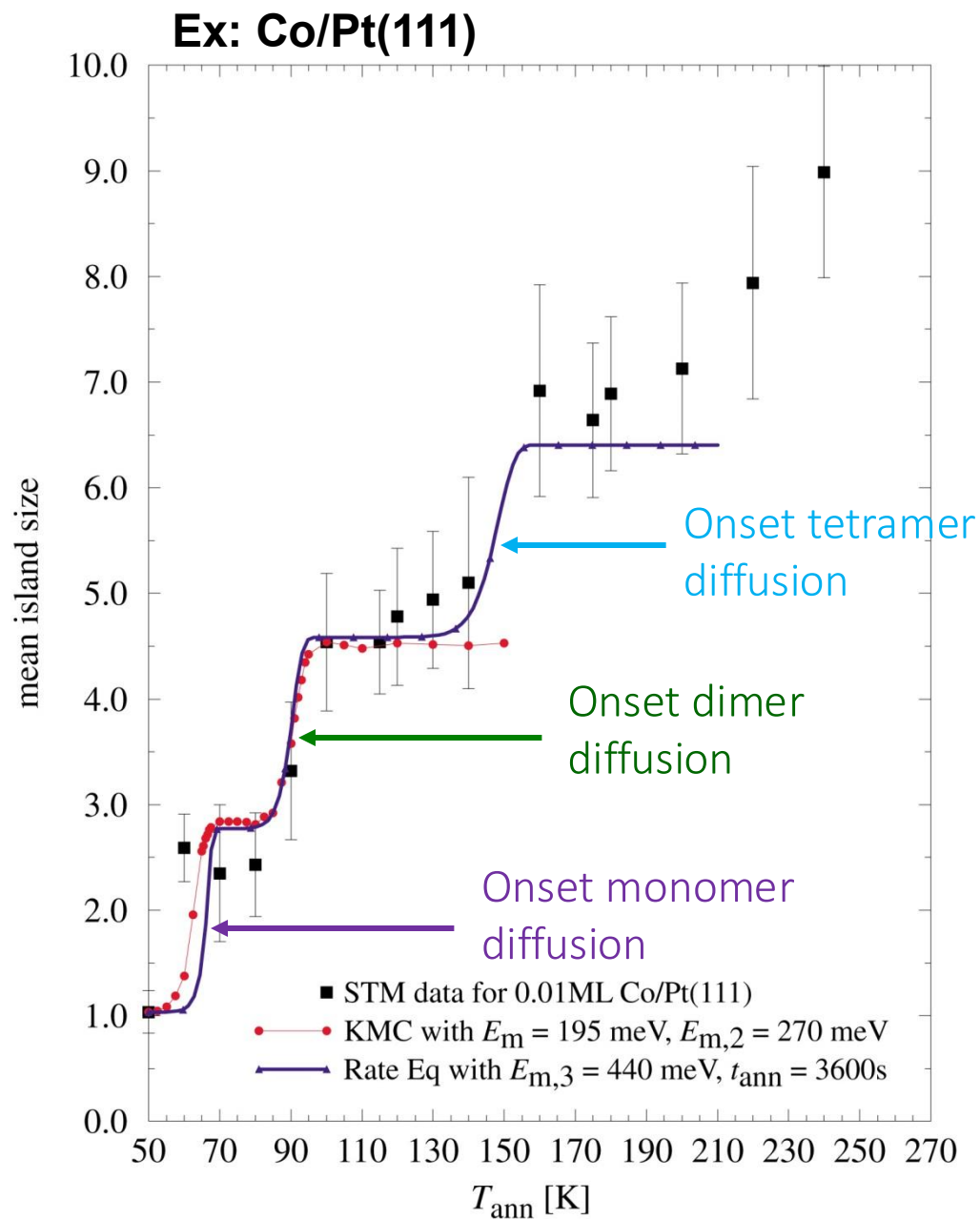


50 Å

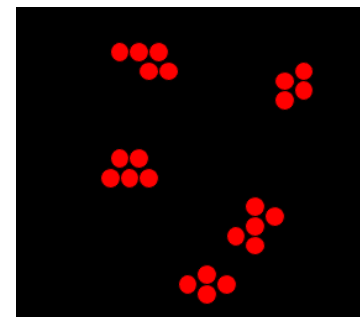
$n = \text{mean island size} = \text{coverage} / \text{island density}$

Kinetic Monte Carlo  
simulation

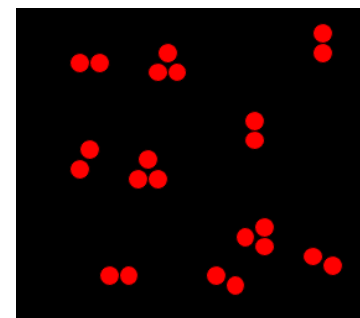




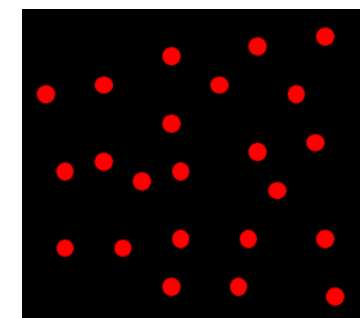
By increasing  $T$ , sequential activation of cluster diffusion results in size selection:



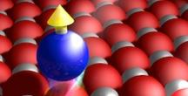
$100 \text{ K} < T < 130 \text{ K}$ :  
tetramers and pentamers



$60 \text{ K} < T < 90 \text{ K}$ :  
dimers and trimers



$T < 60 \text{ K}$ : monomers



Assumption: adatom can diffuse with a rate  $D$   
 but  
 dimer is stable, i.e. when two atoms meet, they cannot detach  
 Critical size  $i = 1$

Time evolution of average values of  $n_1$  and  $n_x$

$n_1$  adatom density

**Dimer creation**

**Growth flux**

**Adatom-island attachment**

$$\frac{dn_1}{dt} = F - 2\sigma_1 D n_1^2 - \sigma_x D n_1 n_x - k_x F (Ft - n_1) - 2k_1 F n_1$$

$$\frac{dn_x}{dt} = \sigma_1 D n_1^2 + k_1 F n_1$$

**Direct impinging on an island**

**Direct impinging on an adatom**

$$D = D_0 \exp(-E_1/k_B T)$$

Rate equations give the formation rate for adatoms and stable islands



## Exercise 5.4

$$n_x = \eta(\theta, i) \left(\frac{D}{F}\right)^{-\chi} \exp\left(\frac{E_i^c}{(i+2)k_B T}\right)$$

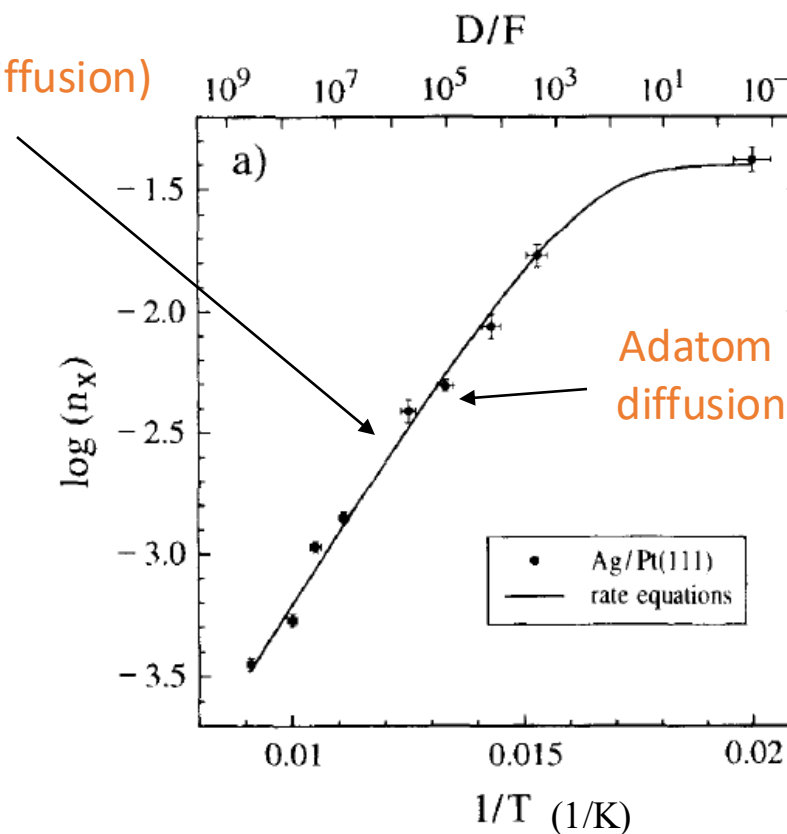
$$D = D_0 \exp\left(-\frac{E_1}{k_B T}\right) \quad \chi = \frac{i}{i+2}$$

$E_i^c$  is the dissociation energy of the island with critical size =  $i$

$$i = 1 \rightarrow E_i^c = 0 \rightarrow n_x = \eta(\theta, 1) \left(\frac{D}{F}\right)^{-1/3} = \eta(\theta, 1) \left(\frac{D_0}{F}\right)^{-1/3} \exp\left(\frac{E_1}{3k_B T}\right)$$

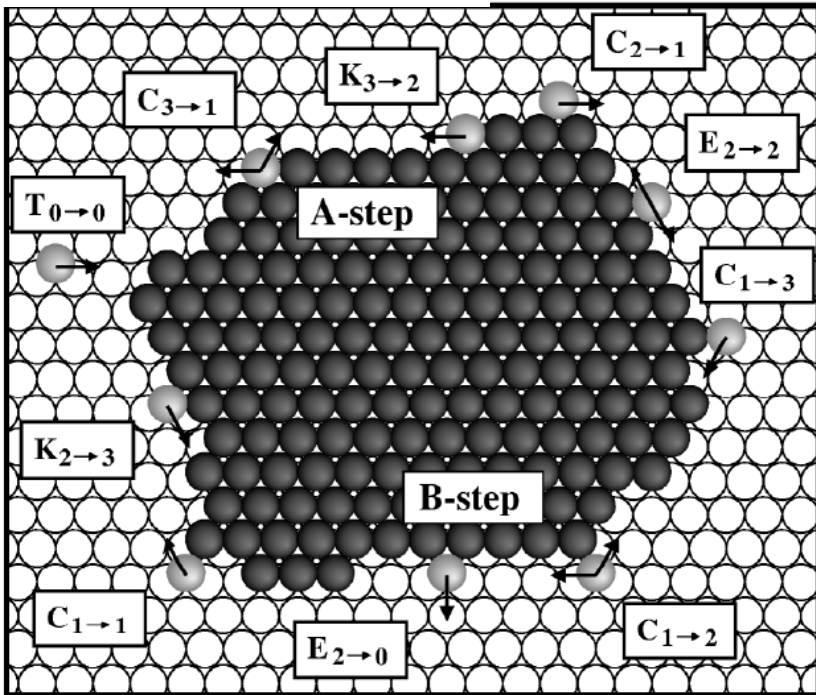
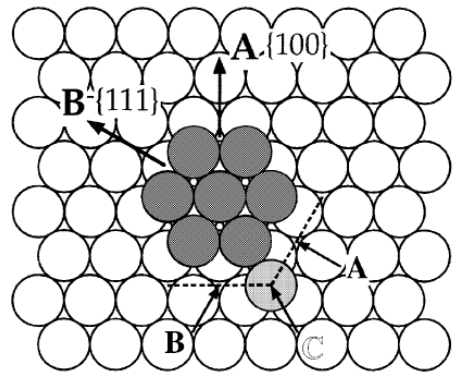
The slope gives  $E_1$   
(energy barrier for adatom (monomer) diffusion)

Arrhenius plot of saturation island densities (coverage = 0.2 ML) for the regime where dimers are stable nuclei

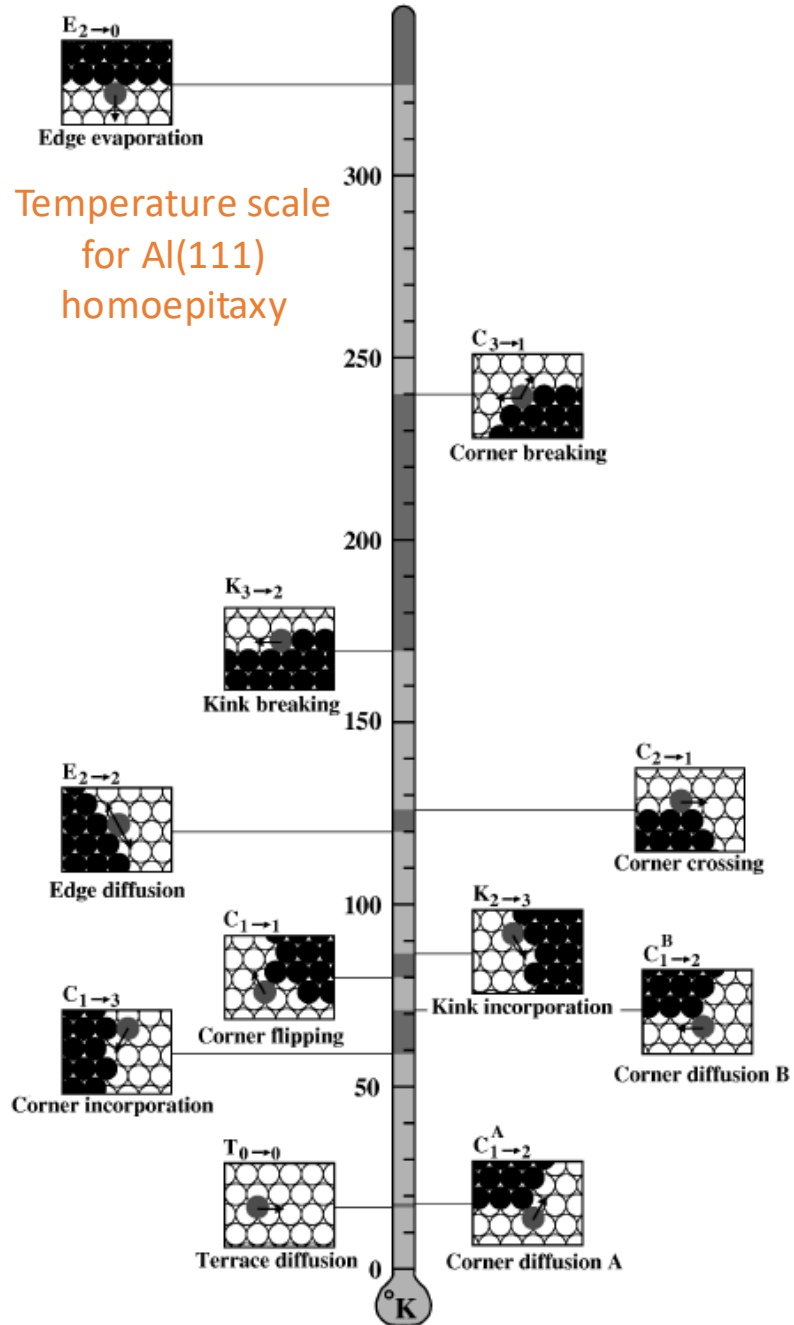




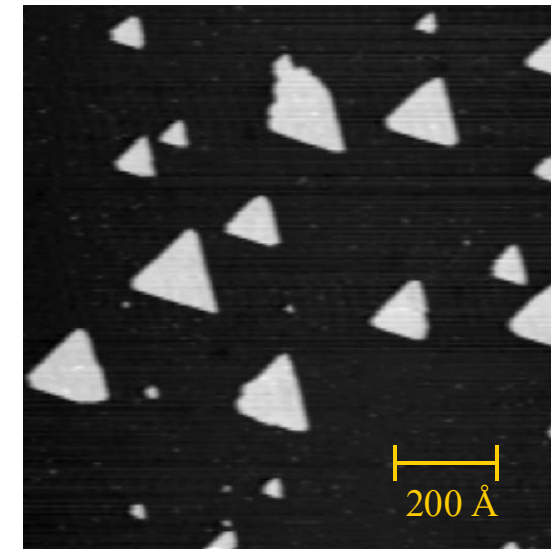
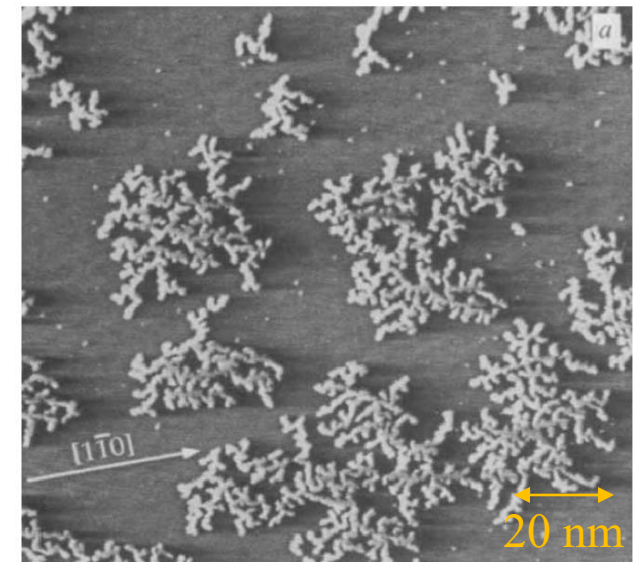
# Island shape: diffusion along the edges



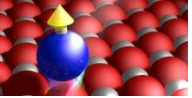
H. Brune *et al.* Nature **369**, 469 (1994);  
 S. Ovesson *et al.* Phys. Rev. Lett. **83**, 2608 (1999);  
 A. Bogicevic *et al.* Phys. Rev. Lett. **81**, 637 (1998)



Ag/Pt(111) T=110K  
 Adatom stick at the island edge and stop



Co/Pt(111) T=270K  
 Activated adatom edge diffusion



Diffusion rate depends on the supporting substrate and on the deposited species

Fe

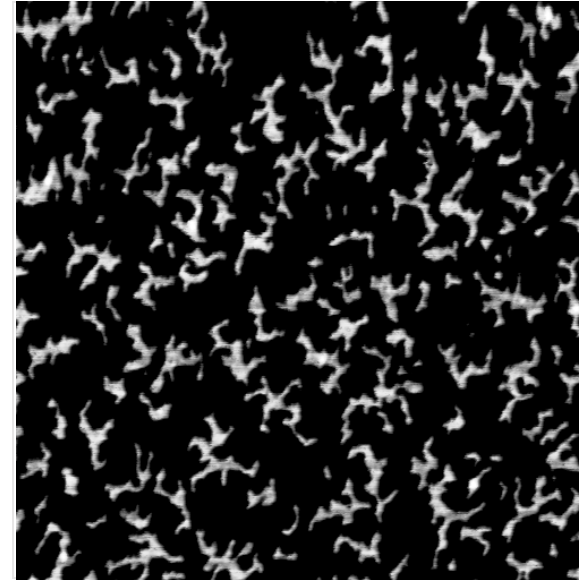
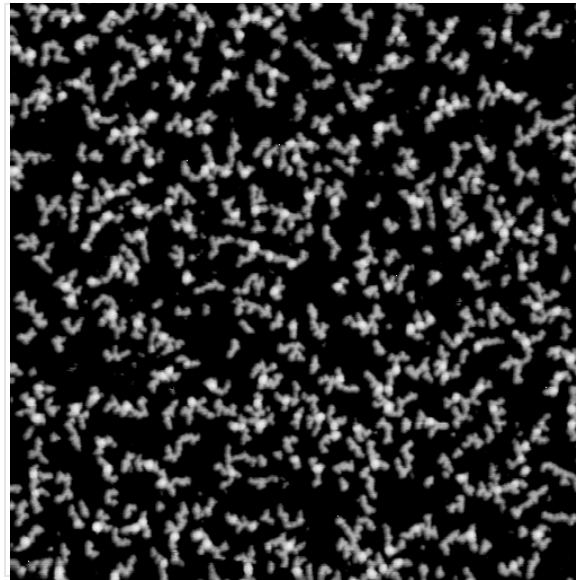


$$v = v_0 \exp(-E_{Fe}/k_B T)$$

Co



$$v = v_0 \exp(-E_{Co}/k_B T)$$



$T_{dep} = 140 \text{ K}$   
 $\Theta = 0.25 \text{ ML}$

Substrate: Pt(111)

Island size = 90 atoms/isl

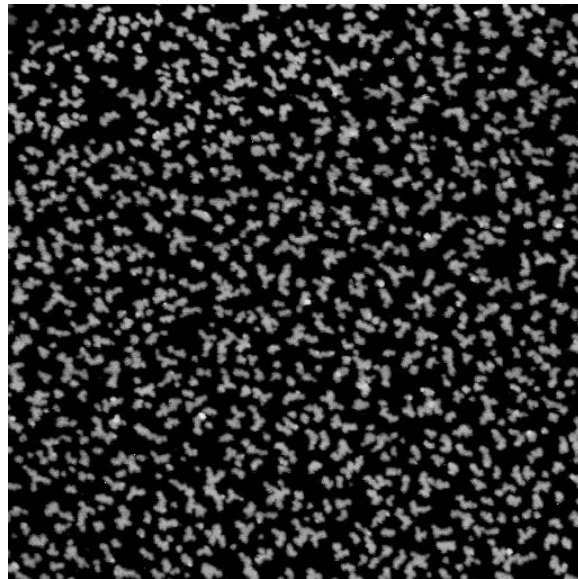
$$E_{Fe} > E_{Co}$$

Island size = 390 atoms/isl

How to form alloy clusters? How to form lattices?  
With the help of patterned substrates and/or templates



# Epitaxial growth of two-dimensional alloys

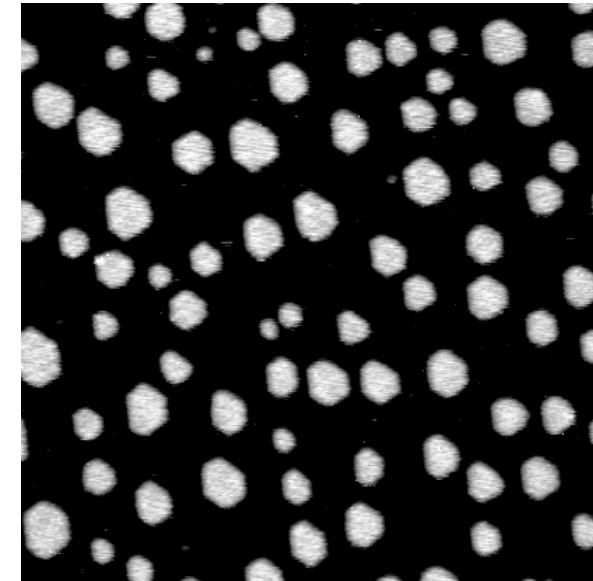


10 nm

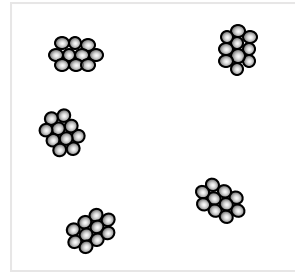
Pt  
 $T_{\text{dep}} = 200\text{K}$   
 $\Theta = 0.2\text{ ML}$



Annealing  
to 800 K

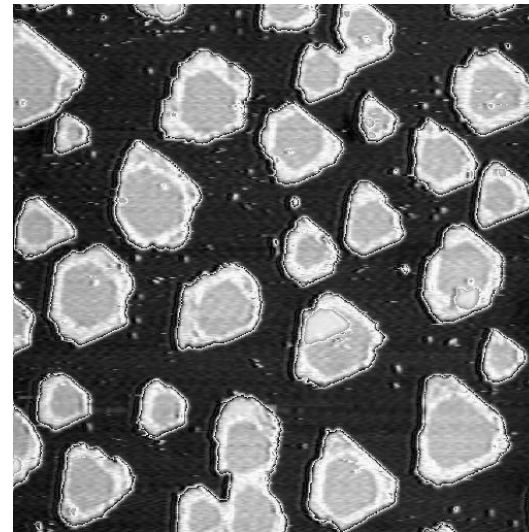
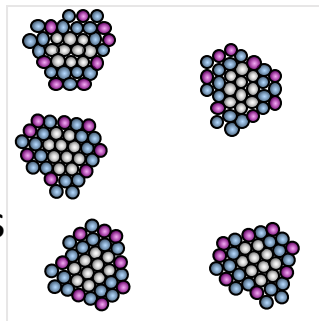


10 nm



Pre-defined  
nucleation  
sites (seeds)  
to define the  
island density

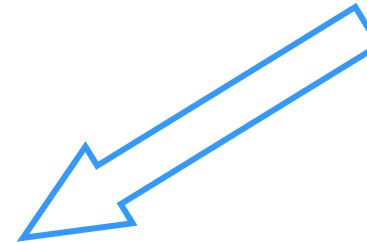
Growth of the  
alloyed  
nanostructures

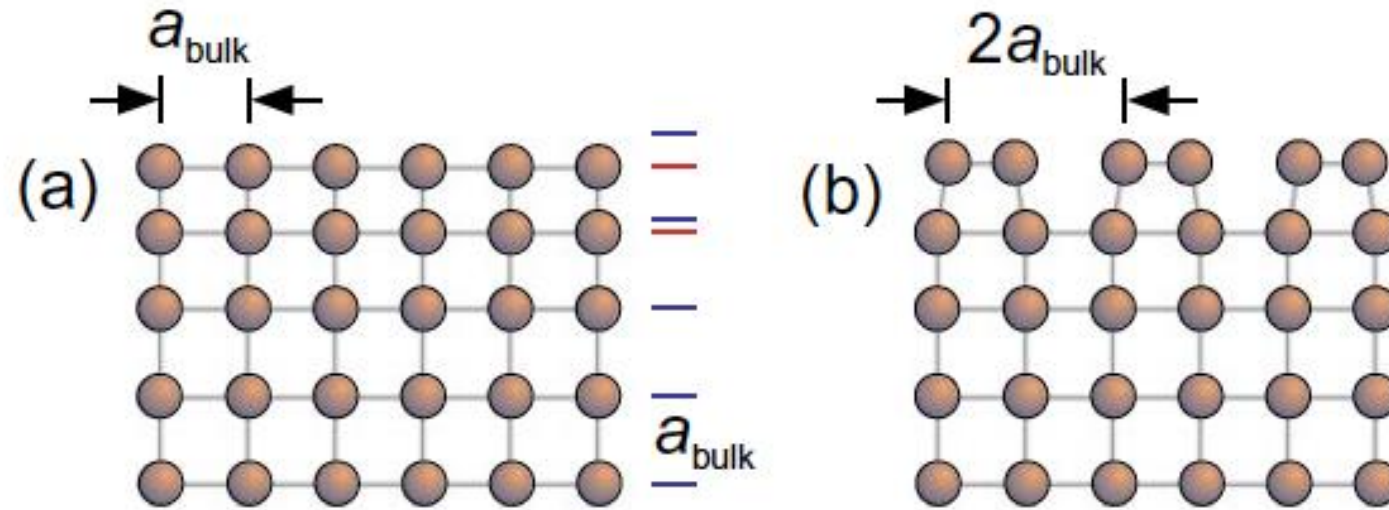
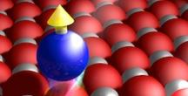


30 nm

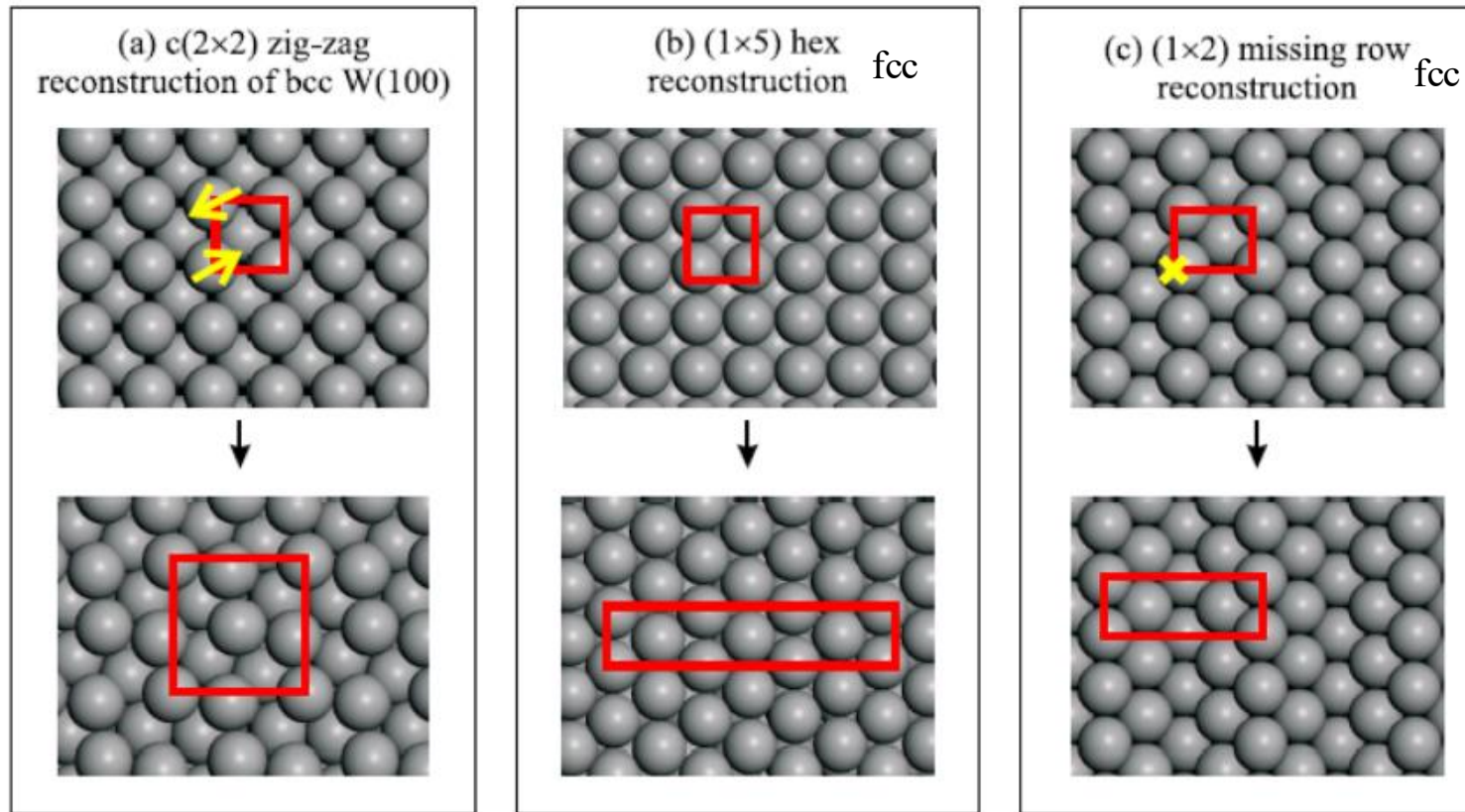
$\text{Co}_x\text{Fe}_{1-x}$  decoration

$T_{\text{dep}} = 250\text{K}$   
 $\Theta = 0.2\text{ ML}$



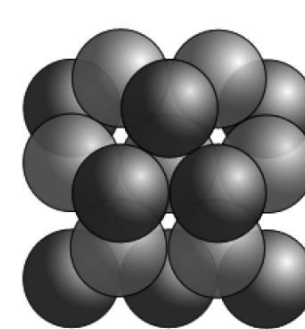
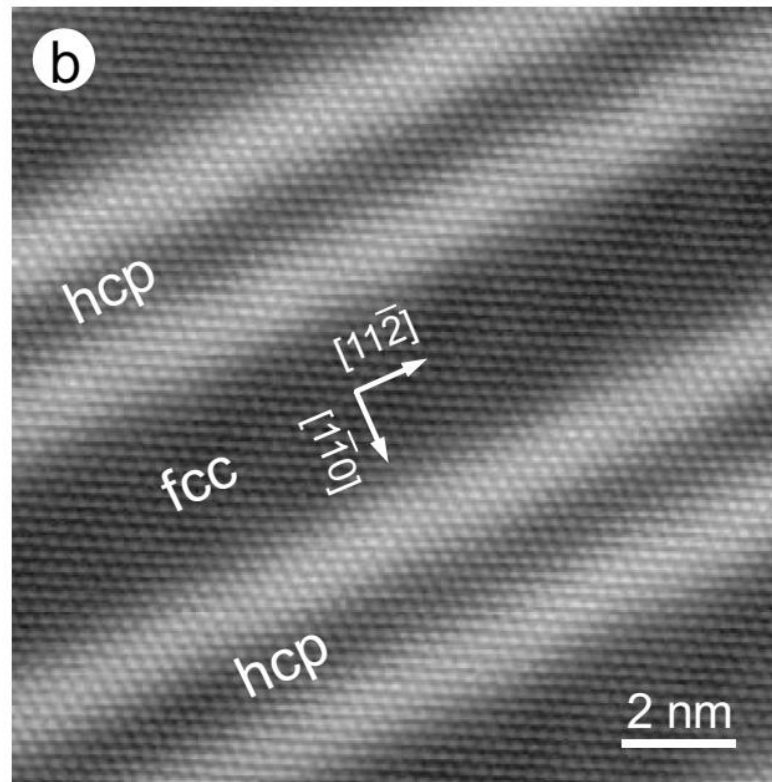
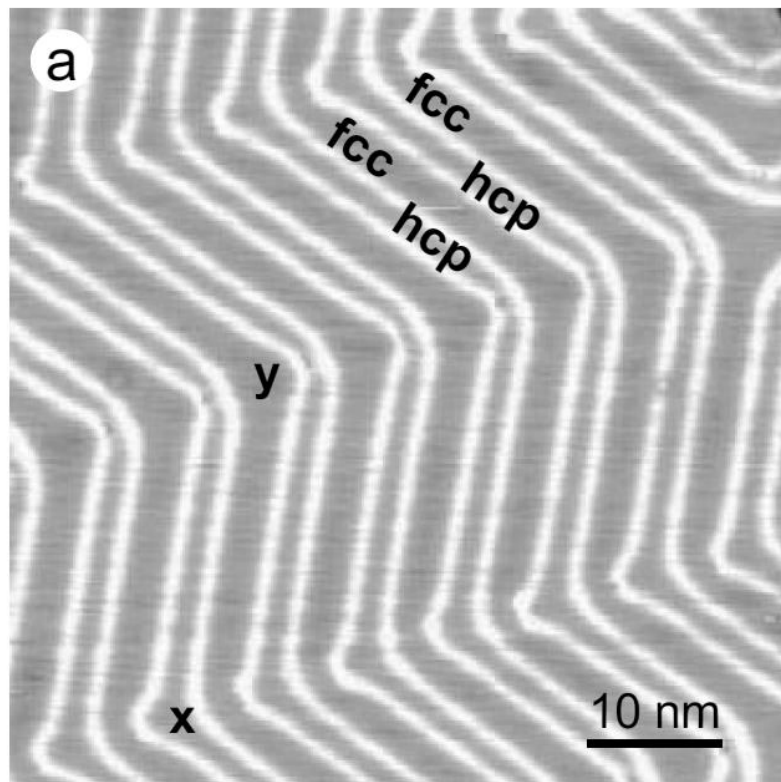


rearrangements of surface ( and near surface ) atoms driven by the energetics of the system

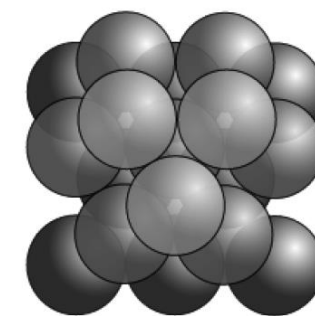


**Figure 5.5.** - Illustration of three bulk truncated surfaces and typical types of reconstruction that they undergo. (a) depicts the  $(1 \times 1)$  to  $c(2 \times 2)$  reconstruction of bcc W(100). The arrows indicate the direction in which the top layer W atoms move upon reconstruction. (b) displays an example of the “hex” reconstruction that the late 5d (fcc) transition metals undergo. The specific example is the  $(1 \times 1)$  to  $(1 \times 5)$  reconstruction of fcc Ir(100). (c) displays the  $(1 \times 1)$  to  $(1 \times 2)$  “missing row” reconstruction that occurs on the (110) surfaces of the late 5d (fcc) transition metals. The rows of atoms removed by the reconstruction are indicated by the  $\times$  at the edge of the unit cell.

Michele Romeo,  
PhD Thesis 2015, University  
of Trieste

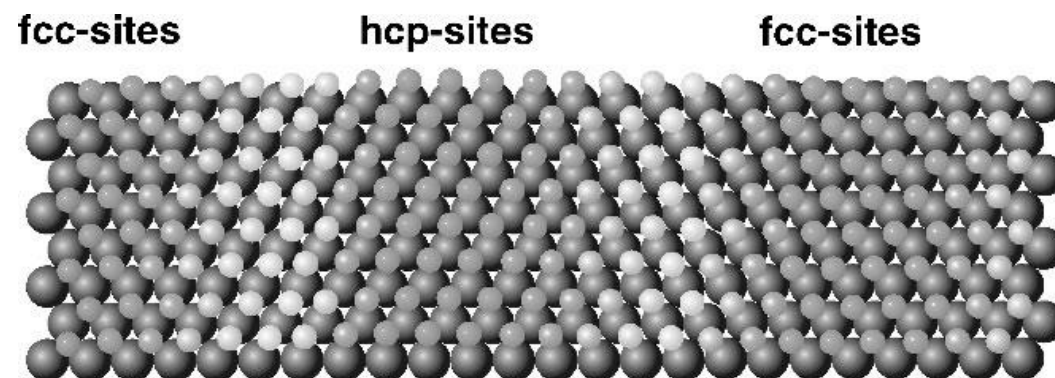


hcp: ABA



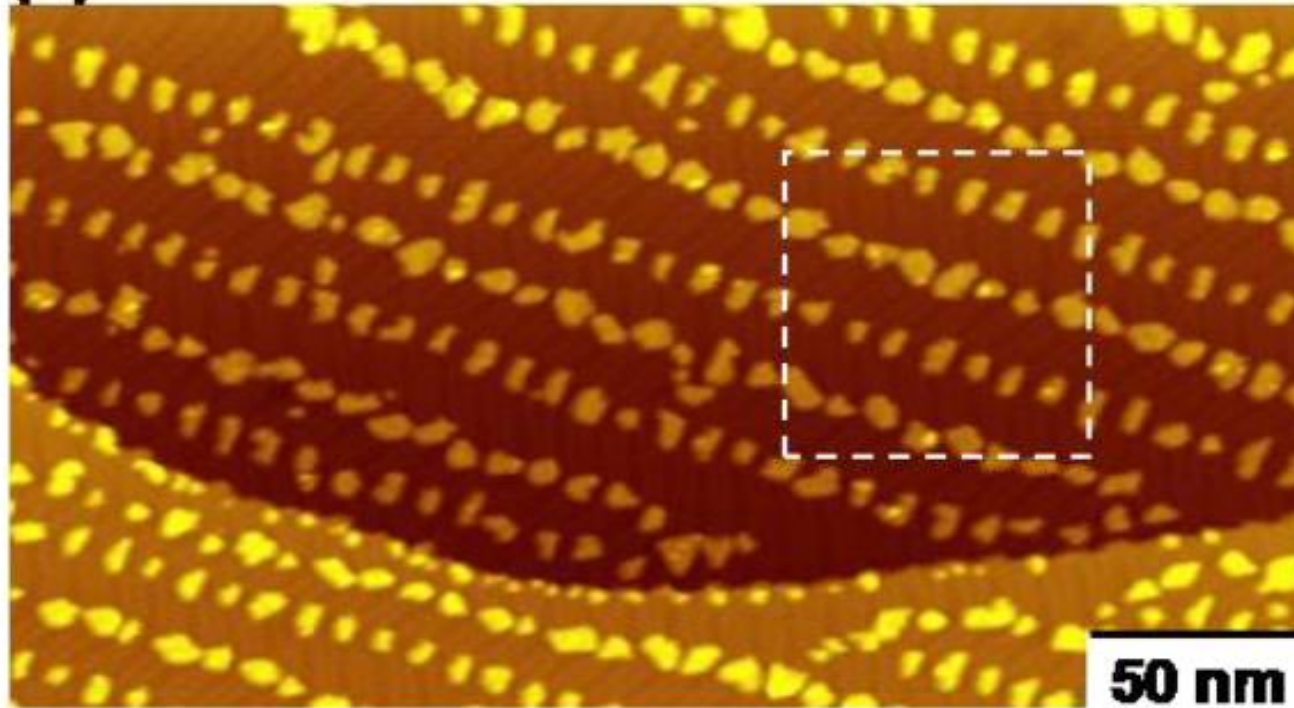
fcc: ABC

Figure 3.1: STM image showing the herringbone reconstructed Au(111) surface. a) Alternating fcc and hcp stacking domains, as well as x- and y-type elbows are visible. b) Atomically resolved STM image, revealing the slightly distorted hexagonal arrangement of the surface atoms together with the domain walls separating fcc and hcp stacking. The interatomic distances along  $[11\bar{2}]$  and  $[1\bar{1}0]$  are  $2.88 \text{ \AA}$  and  $\approx 2.75 \text{ \AA}$ , respectively. (Tunneling parameters: a)  $V = -0.7 \text{ V}$ ,  $I = 0.2 \text{ nA}$ ; b)  $V = -0.02 \text{ V}$ ,  $I = 1.3 \text{ nA}$ )

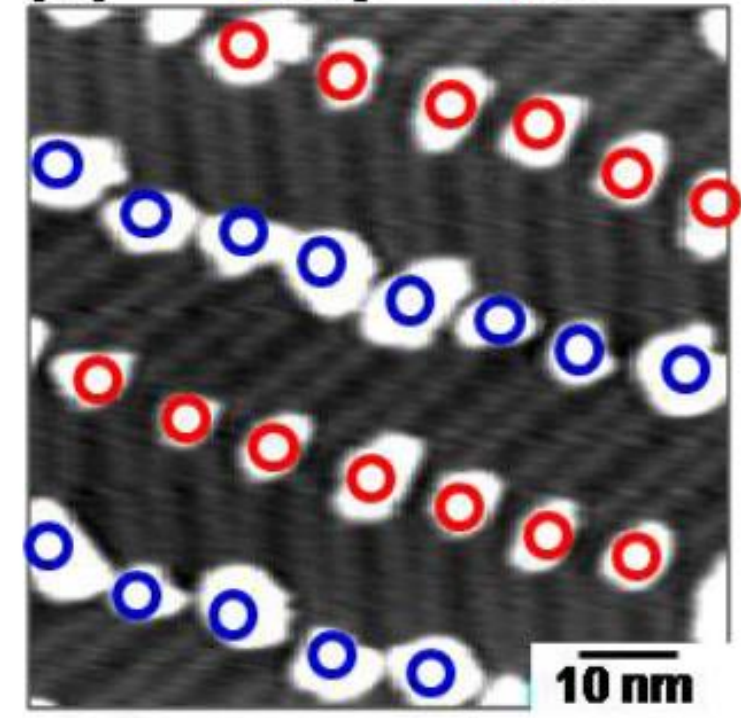




**(a) 250 K - 0.18 ML**



**(b) ○ hcp ○ fcc**

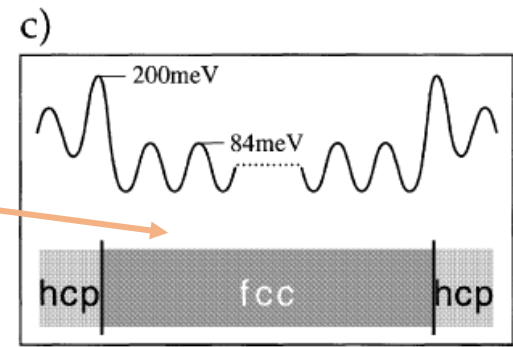
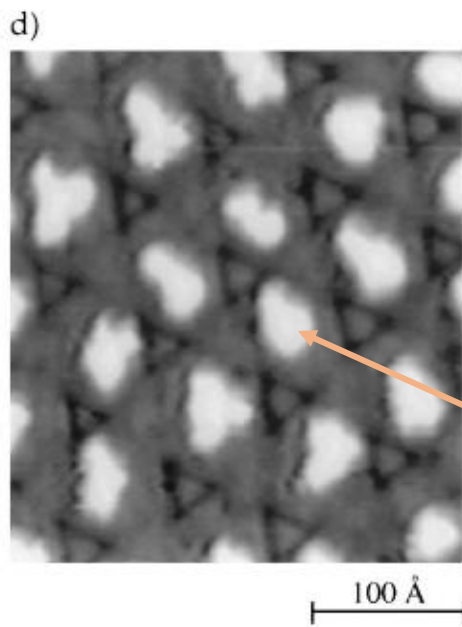
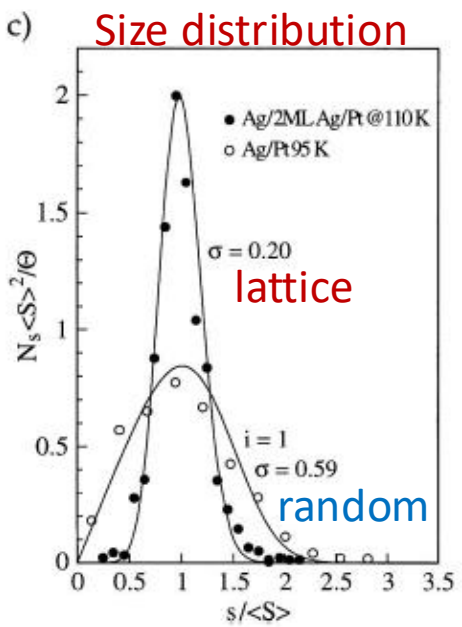
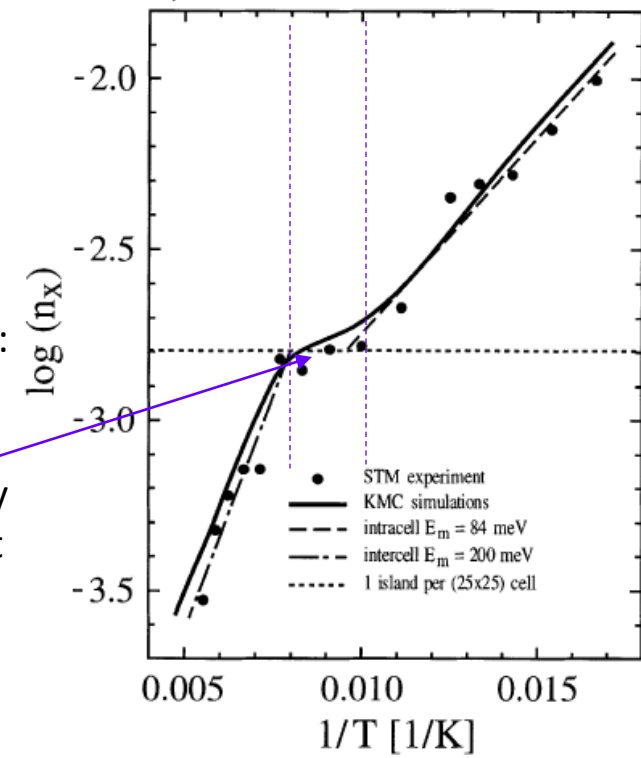
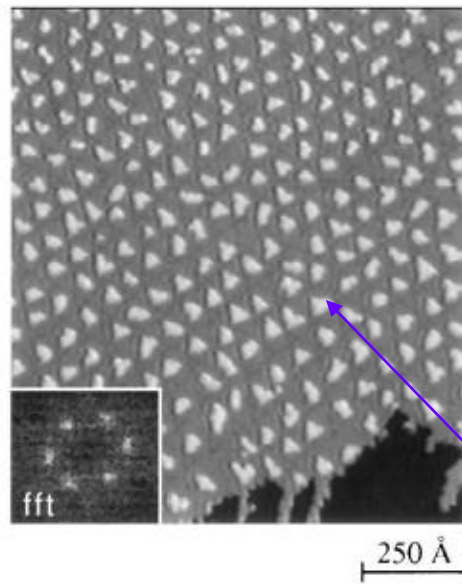
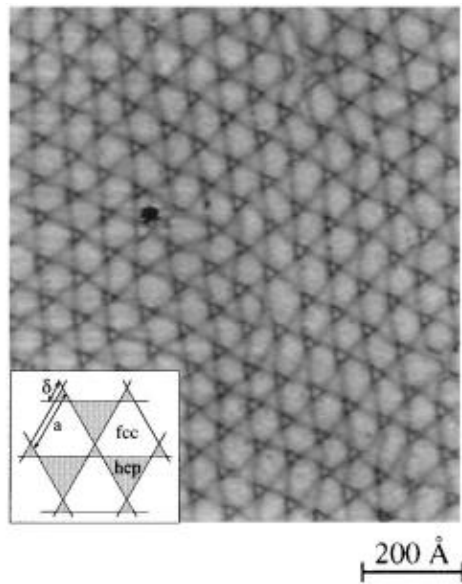
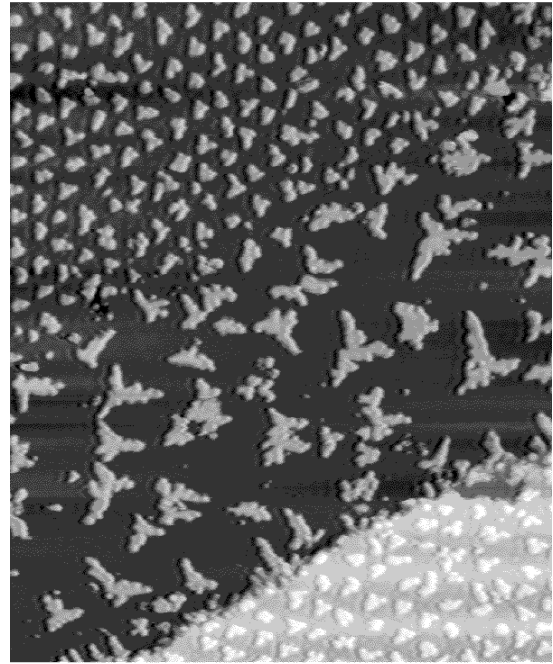


0.18 ML Fe deposited at 250 K  
islands nucleate at the elbows of the reconstruction



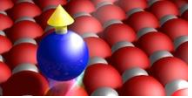
# Self assembled nanostructure arrays on patterned substrate

Nucleation of an Ag island superlattice ( $T_{dep} = 110$  K) on the dislocation network formed by 2 ML of Ag on Pt(111)



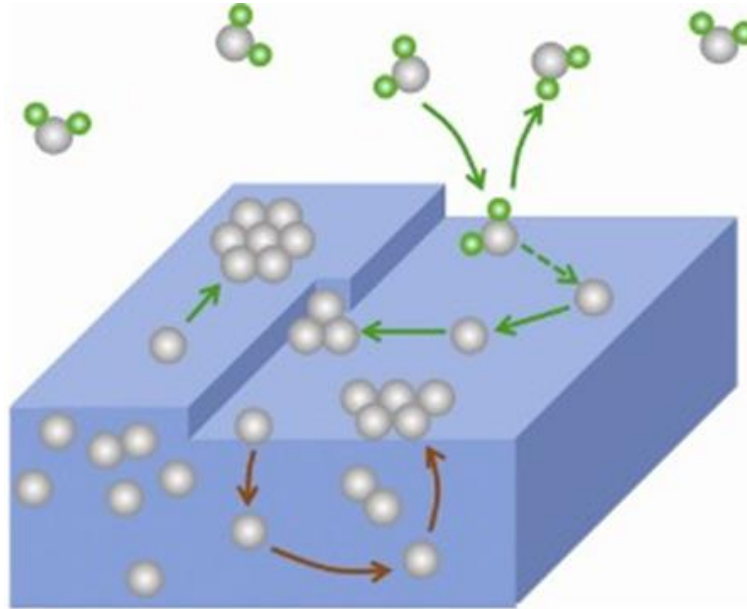
Almost monodispersed size distribution thanks to the template effect of the dislocation network

Atoms are confined in the fcc stacking areas



## Graphene growth by CVD (chemical vapor deposition)

hydrocarbon flux



- Hydrogen
- Carbon

Hydrocarbon molecules dissociate on the hot surface: H atoms leave the surface while C atoms organize in the honeycomb lattice of graphene

Ex of hydrocarbons:

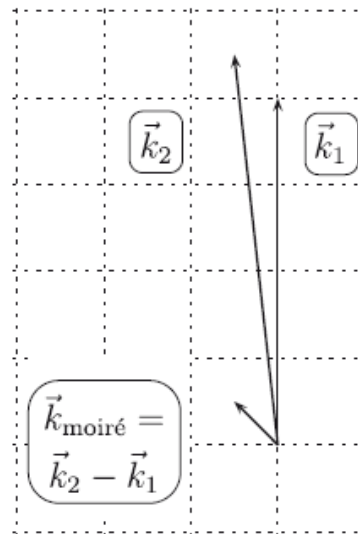
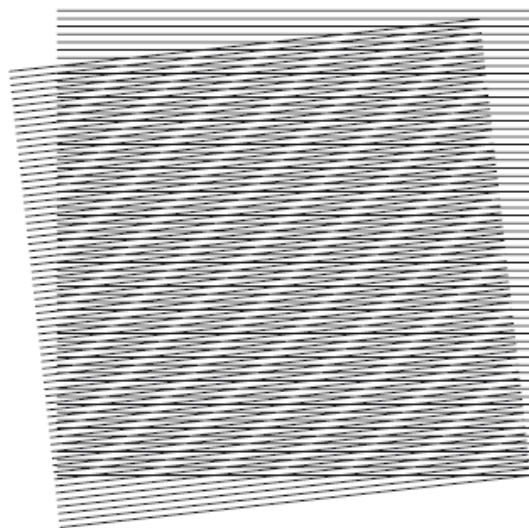
$\text{CH}_2$	Methylene
$\text{C}_2\text{H}_4$	Ethylene

Note: C atoms dissolved in the bulk segregate to the sample surface and can contribute to form graphene

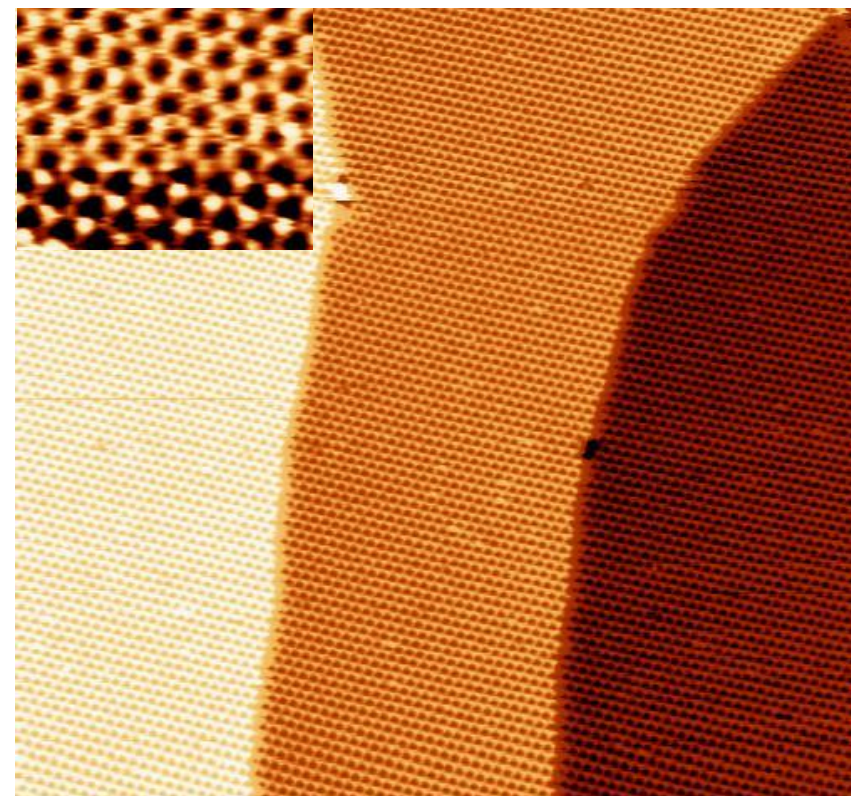
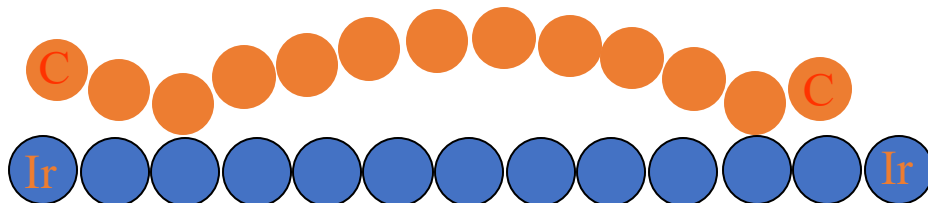


# Moiré pattern due to graphene-Ir(111) lattice mismatch

A moiré is a superposition of two lattices generating a third one.



$a_{Ir} = 0.27 \text{ nm}$   
 $a_C = 0.245 \text{ nm}$



180 x 200 nm<sup>2</sup>

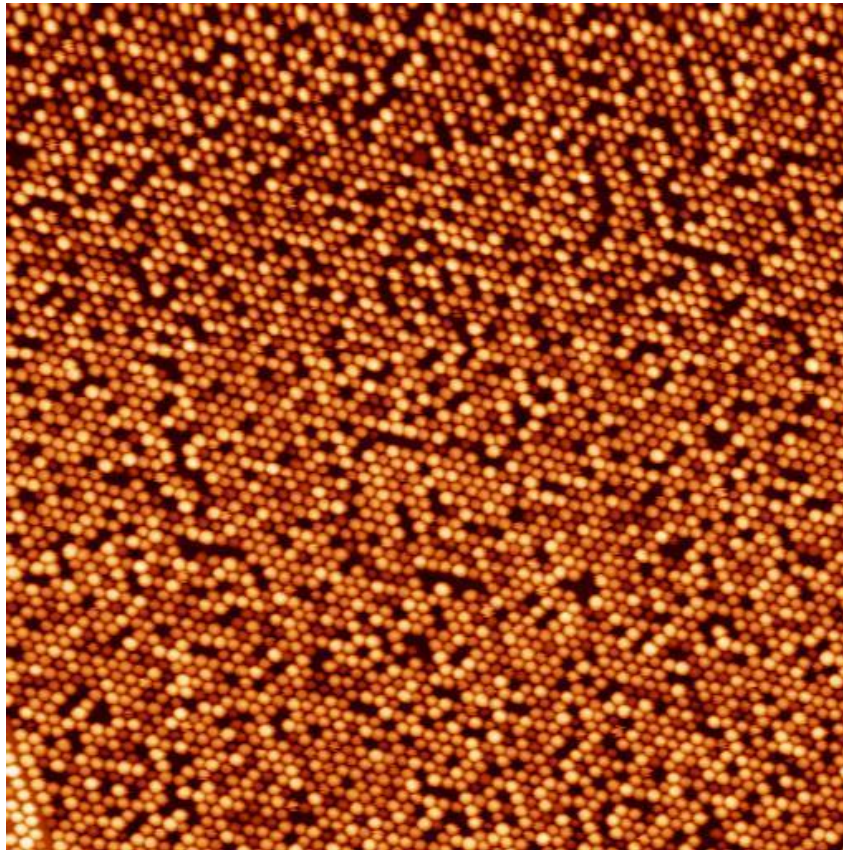
Supercell with (10x10) C atoms  
on (9x9) Ir substrate atoms



# Core-shell nanostructure arrays on graphene/Ir(111)

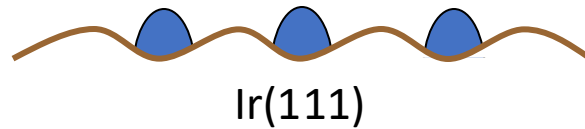
**Ir** island

Ir deposition:  $T = 375$  K



150 x 150 nm<sup>2</sup>

graphene

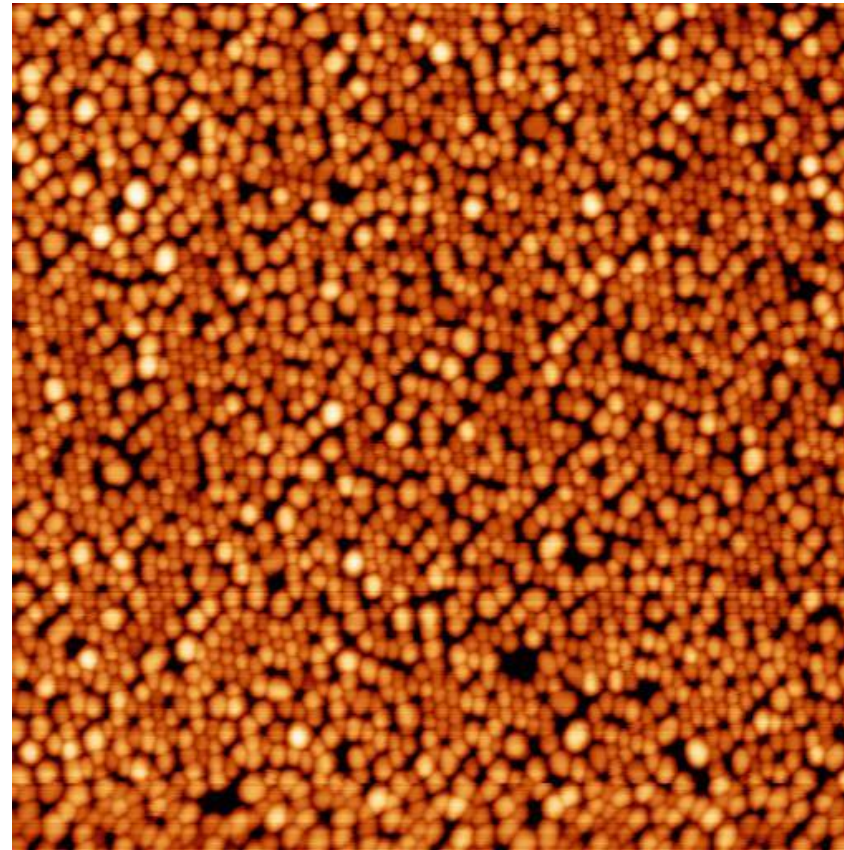


Ir(111)

**Ir-core Co-shell** islands

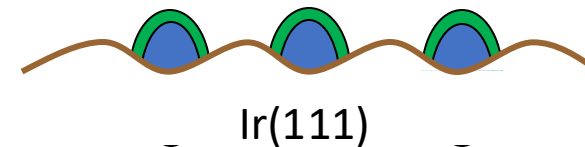
Ir deposition:  $T = 375$  K

Co deposition: 1 ML,  $T = 300$  K



150 x 150 nm<sup>2</sup>

**Ir-core  
Co-shell**



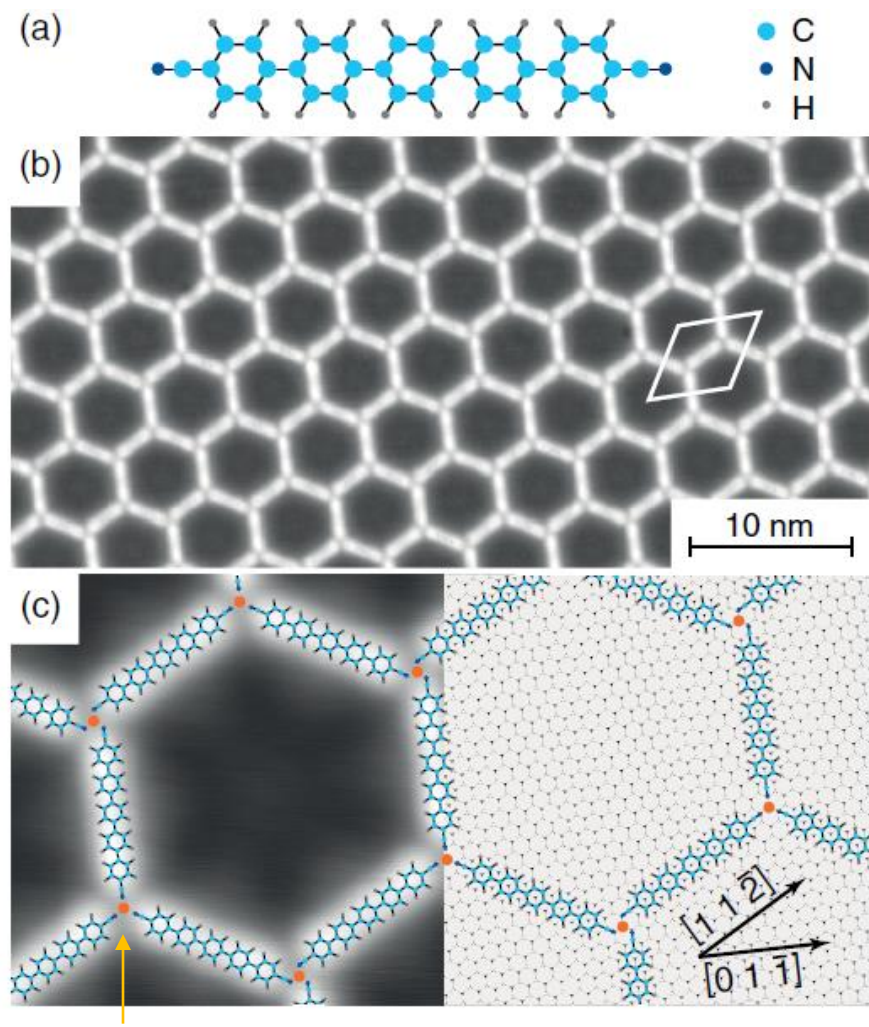
Ir(111)



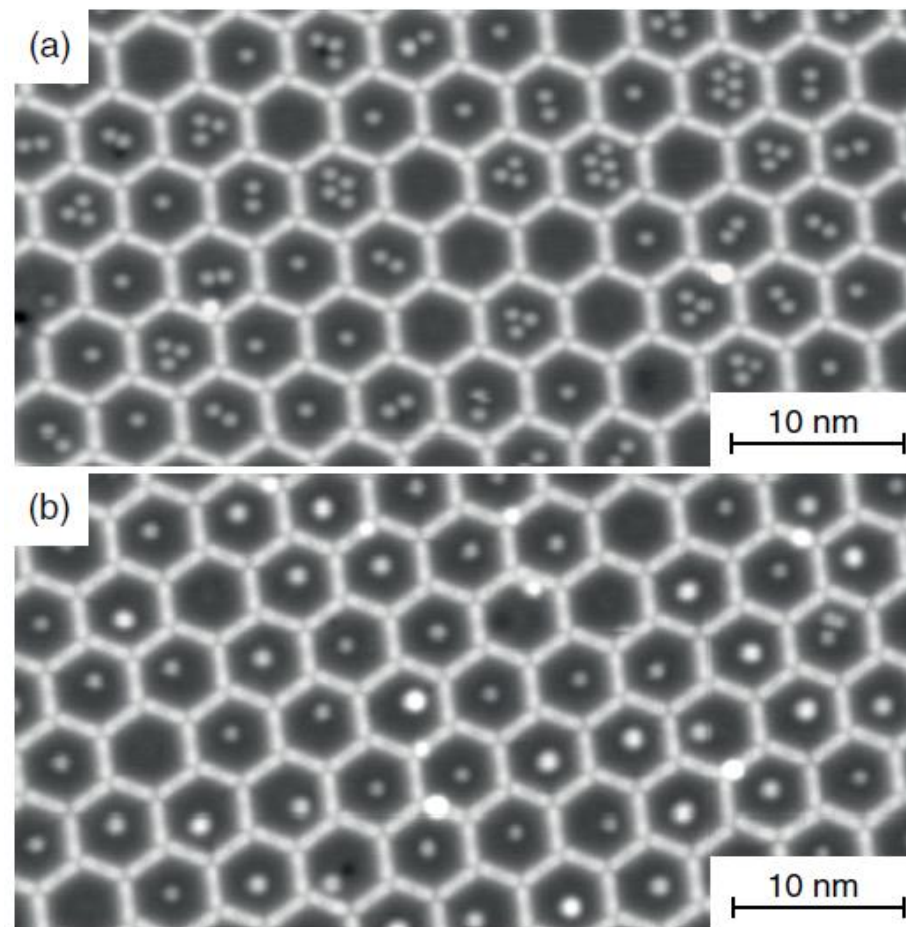
## Exercise 5.5

Metal organic quantum box network on Cu(111)

a) Fe deposition at  $T = 10K$



Cu atoms



b) cluster formation after annealing to  $T_{ann} = 18K$

