

EPFL

# MICRO-435 Quantum and Nanocomputing

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MT - SCF LOOP  
& EE BESD MT SIMULATOR

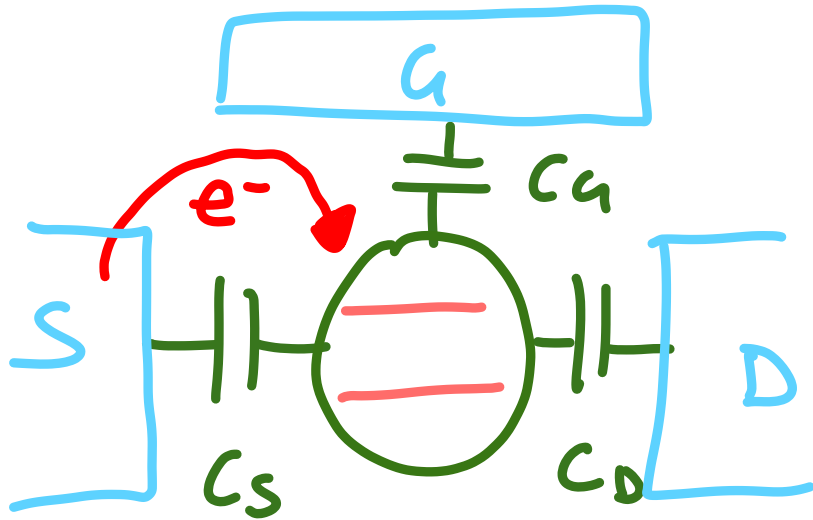
# OBJECTIVES

a) SCF LOOP

b) SIMPLE  
CIRCUITS BASED ON RT

a) SCF LOOP

# CAPACITIVE MODEL OF QDOT



$$C_{ES} = C_S + C_D + C_G + C_{BG}$$

$$U_{\text{DOT}} = -q V_{DS} \frac{C_D}{C_{ES}} - q V_{GS} \cdot \frac{C_G}{C_{ES}} + \frac{q^2}{E_S} \cdot (N - N_0)$$

CHARGING EFFECT

ACTUAL N: OF  $e^-$  IN THE DOT

$N_0$  No. of  $e^-$  @ Eq.

$$U_{VDS} = -q \frac{C_D}{C_{ES}} V_{DS}$$

$$U_{VGS} = -q \frac{C_G}{C_{ES}} V_{GS}$$

$$U_{C.E.} = \frac{q^2}{C_{ES}} \cdot \Delta N$$

$$\Delta N = N - N_0 \leftarrow \begin{matrix} \text{No el. } \odot \\ \text{EQ.} \end{matrix}$$

$V_{GS} > 0$   $U$  SHIFTS LOWER ENERGY

$V_{GS} < 0$   $U$  SHIFTS HIGHER ENERGY

+  $V_{BG}$  IF PRESENT!

$U_{SCF}$  SELF CONSISTING FIELD

$$U_{SCF} = U_0 (N - N_0)$$

$\uparrow$   $\uparrow$   $\uparrow$   
 $U_0$   $N$   $N_0$   $N$   $el.$   $@$   $EQ,$   
 actual  $N$  of  $el.$  involved  
 in calculation

$$N = \int_{-\infty}^{+\infty} D(\bar{E} - U_{SCF}) \cdot \frac{d_1 d_2}{d_1 + d_2} [f(\bar{E} - \bar{E}_{FS}) - f(\bar{E} - \bar{E}_{FD})]$$

$\underbrace{\hspace{10em}}$   
 DOS of SHIFTED EN.



HOW CAN WE FIND  
THE ACTUAL  $N$   
FOR A CERTAIN  
CONDITION?



# SCF LOOP(i)

START.

$T(E)$

$D(E)$

⓪

EQUILIBRIUM

$V_{DS}$   
SEVERAL  
STEPS  
 $i$

$$\begin{aligned} \epsilon_i &\leftarrow \epsilon_{i-1} - U_{SCFi-1} \\ N_i &\leftarrow D_{os} \leftarrow \epsilon_i \\ U_{SCFi} &\leftarrow N_i \end{aligned}$$

$V_i \in V_{DS}$   
RANGE

NO

$$U_{SCFi} - U_{SCFi-1} <$$

CONVERGENCE  
TERM

YES

$$T(\epsilon_i), I_{DSi}$$

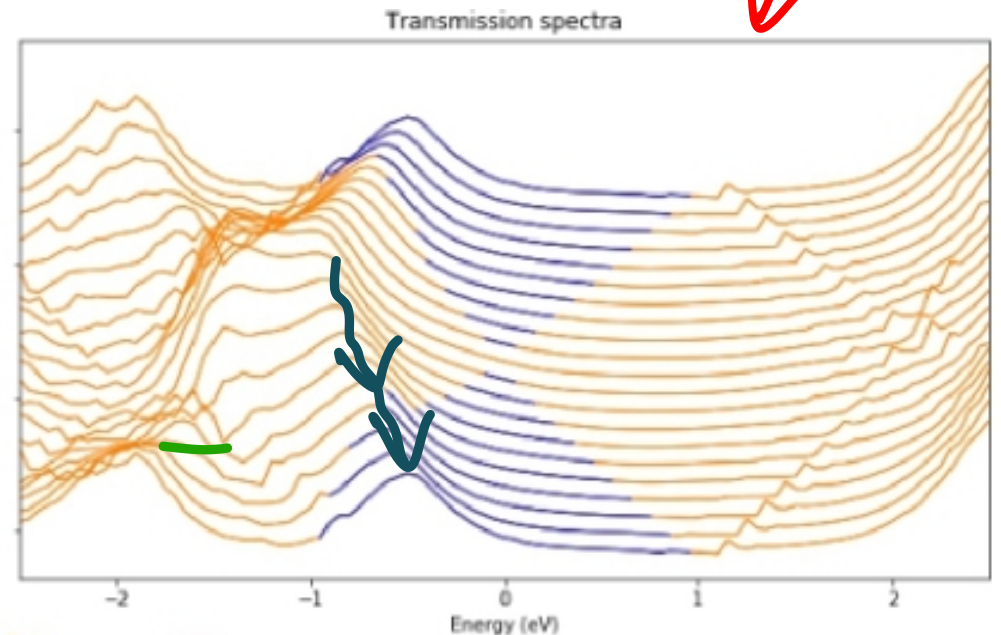
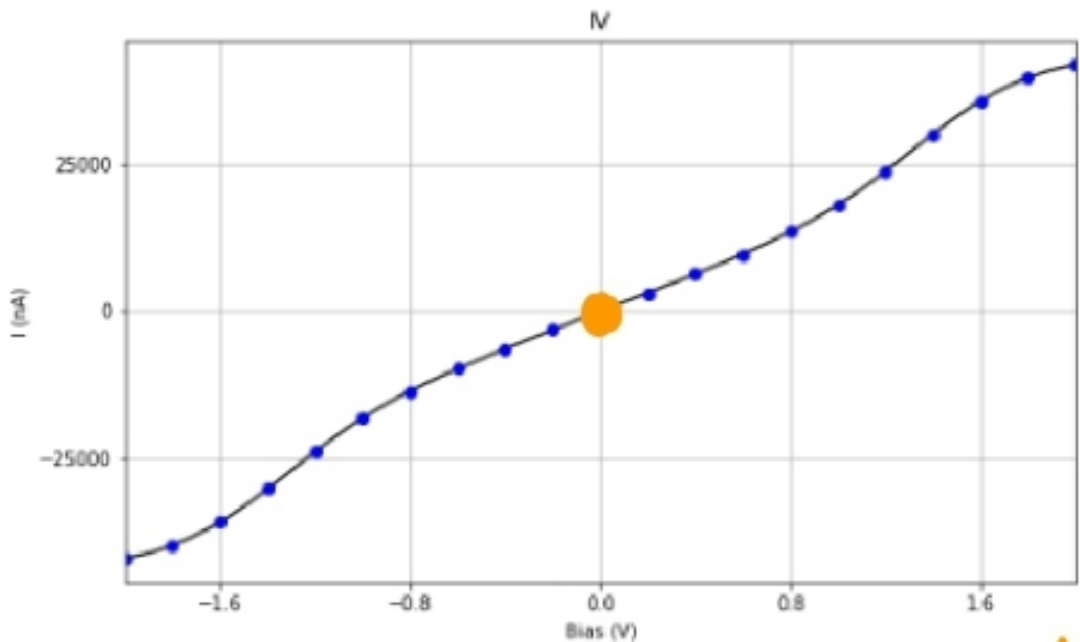
← for each  $V_{DS}$

PROBLEM!  $N \leftarrow D \leftarrow$  PEAKS!

00  
00

HOW DOS CHANGES  
w.r.t.  $\odot$  EQUILIBRIUM

HOW TO EVALUATE?



# PROBLEM!

$N \leftarrow D \leftarrow$  PEAKS!

100%

HOW DOES CHANGES  
W.R.T.  $\odot$  EQUILIBRIUM

HOW TO EVALUATE?

QUANTUM-ATK



AB INITIO  
SIMULATION



- PRECISE
- CPU CONSUMING

EEBESD



HOW PEAKS  
CHANGE WHEN  
 $V_{DS}$  ( $V_{GS}$ ) CHANGE

BASED ON } AB INITIO  
OR EXP.

EEBESD - SOLVES SCF LOOP

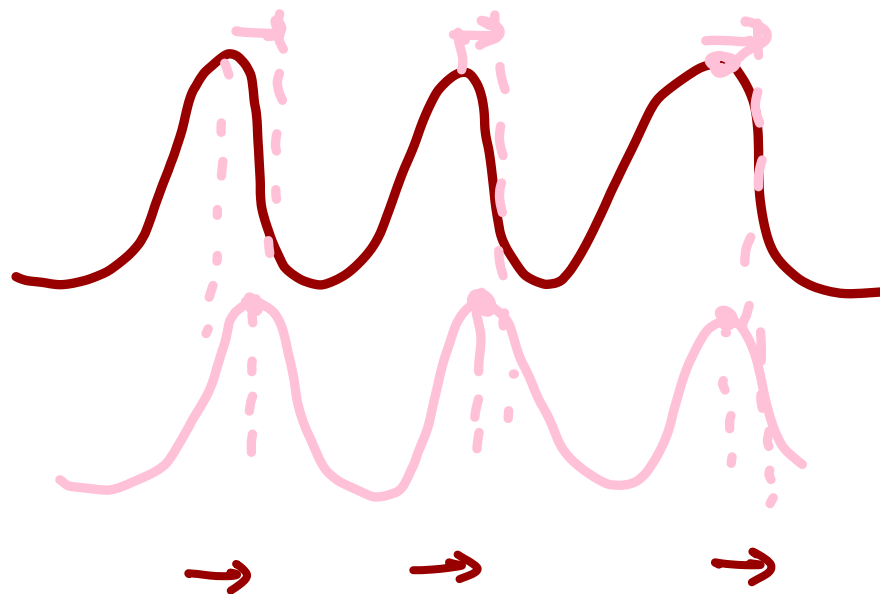
- ESTIMATES DOS

ASSUMPTIONS

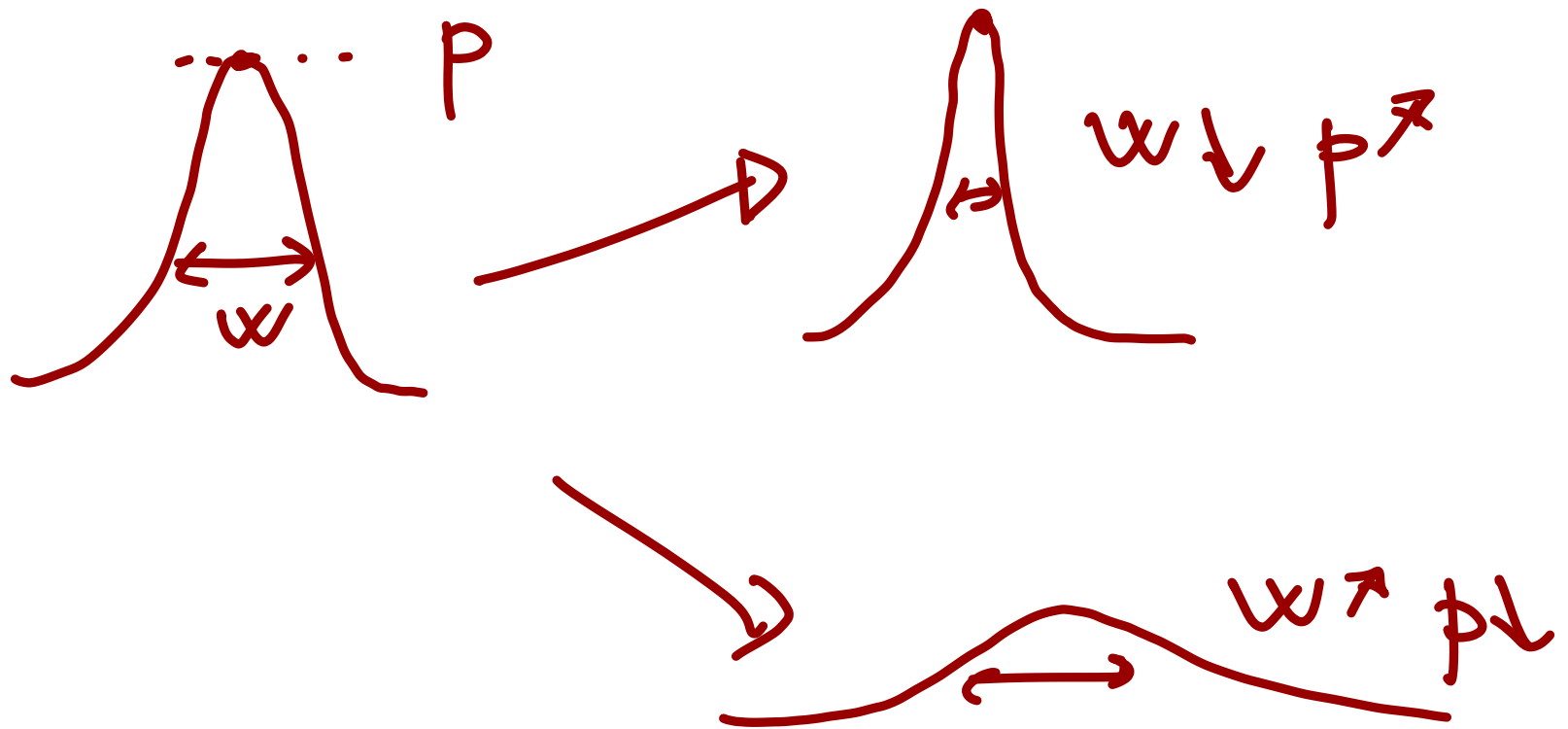
- BASED ON A BUNCH OF PRELIMINARY AB-INITIO SIM

① WHEN  $V_{DS}$  APPLIED PEAKS SHIFT

RIGIDLY



②



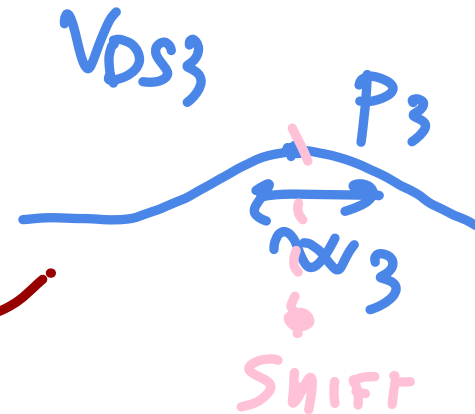
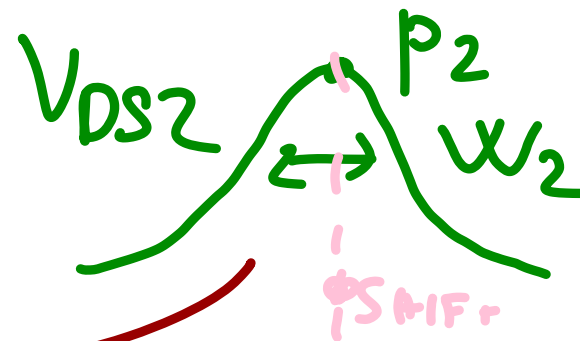
THERE MIGHT BE A PEAK VARIATION....

TALLER - SLINNER

SHORTER - FATTER

# To model (1) & (2)

AB INITIO SIM



ELABORATE

$$k_1 + \alpha k_2 + \alpha^2 k_3$$

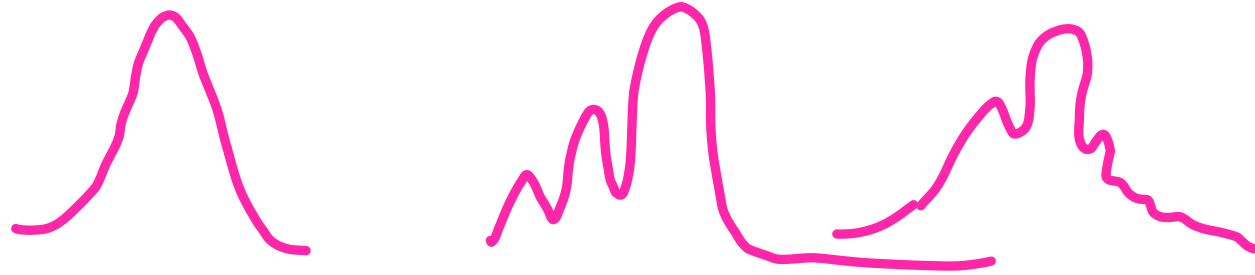
DESCRIBES EVOLUTION  
PEAKS VDS

VALID FOR  
1 MOLECULE

OTHER THINGS NOT  
CONSIDERED FOR NOW

③

PEAKS CHANGE SHAPE



DIFFICULT

④

RESONANCE



# EEBESD ORGANIZATION

- INITIAL EVAL  $\textcircled{B}$  EQ
- EXTRACTED PARAMS FROM AB INITIO (ESTIMATE DOS  $k_1 k_2 k_3$ )

$\nabla V_G$   $\leftarrow$   $\alpha$  COUPLING FACTOR

$\nabla V_{DS}$

$\hookrightarrow$  EVALUATE  $\textcircled{E}$ ,  
IN SCFL

$\delta_1 \delta_2$

ESTIMATE DOS

$V_{SCF}$

$T(\bar{E}, V_{DS}, V_G)$

$I(V_G, V_{DS})$

EEB30

USED IN EXERCISES

- FOR SOME MOLECULES
- FOR SEVERAL  $V_{DS}, V_{GS}$
- FOR CASES OF PARAMETERS  $\alpha, \beta_1, \beta_2$

MATLAB BASED

# CRISTALLIZATION

2) SCF LOOP

3) SIMPLE  
CIRCUITS BASED ON RT

↳ NEXT LECTURE