

EPFL



MICRO-435 Quantum and Nanocomputing

Edoardo Charbon
Mariagrazia Graziano

MIT BEHAVIOR & CHARACTERISTICS
PART 4

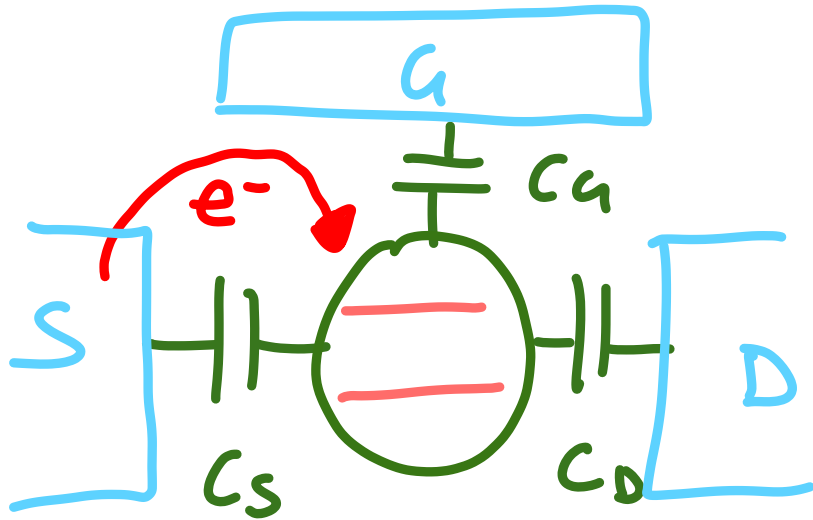
OBJECTIVES

a) SCF LOOP

b) SIMPLE
CIRCUITS BASED ON RT

a) SCF LOOP

CAPACITIVE MODEL OF QDOT



$$C_{ES} = C_S + C_D + C_G + C_{BG}$$

$$U_{\text{DOT}} = -q V_{DS} \frac{C_D}{C_{ES}} - q V_{GS} \cdot \frac{C_G}{C_{ES}} + \frac{q^2}{E_S} \cdot (N - N_0)$$

CHARGING EFFECT

ACTUAL N: OF e^- IN THE DOT

N_0 No. of e^- @ Eq.

$$U_{VDS} = -q \frac{C_D}{C_{ES}} V_{DS}$$

$$U_{VGS} = -q \frac{C_G}{C_{ES}} V_{GS}$$

$$U_{C.E.} = \frac{q^2}{C_{ES}} \cdot \Delta N$$

$$\Delta N = N - N_0 \leftarrow \begin{matrix} \text{No el. } \odot \\ \text{EQ.} \end{matrix}$$

$V_{GS} > 0$ U SHIFTS LOWER ENERGY

$V_{GS} < 0$ U SHIFTS HIGHER ENERGY

+ V_{BG} IF PRESENT!

U_{SCF} SELF CONSISTING FIELD

$$U_{SCF} = U_0 (N - N_0)$$

\uparrow \uparrow \uparrow
 U_0 N N_0 $N. el. @ EQ,$
 actual N of el. involved
 in calculation

$$N = \int_{-\infty}^{+\infty} D(E - U_{SCF}) \cdot \frac{d_1 d_2}{d_1 + d_2} [f(E - E_{FS}) - f(E - E_{FD})]$$

$\underbrace{\hspace{10em}}$
 DOS of SHIFTED EN.



HOW CAN WE FIND
THE ACTUAL N
FOR A CERTAIN
CONDITION?



SCF LOOP(i)

START.

$T(E)$

$D(E)$

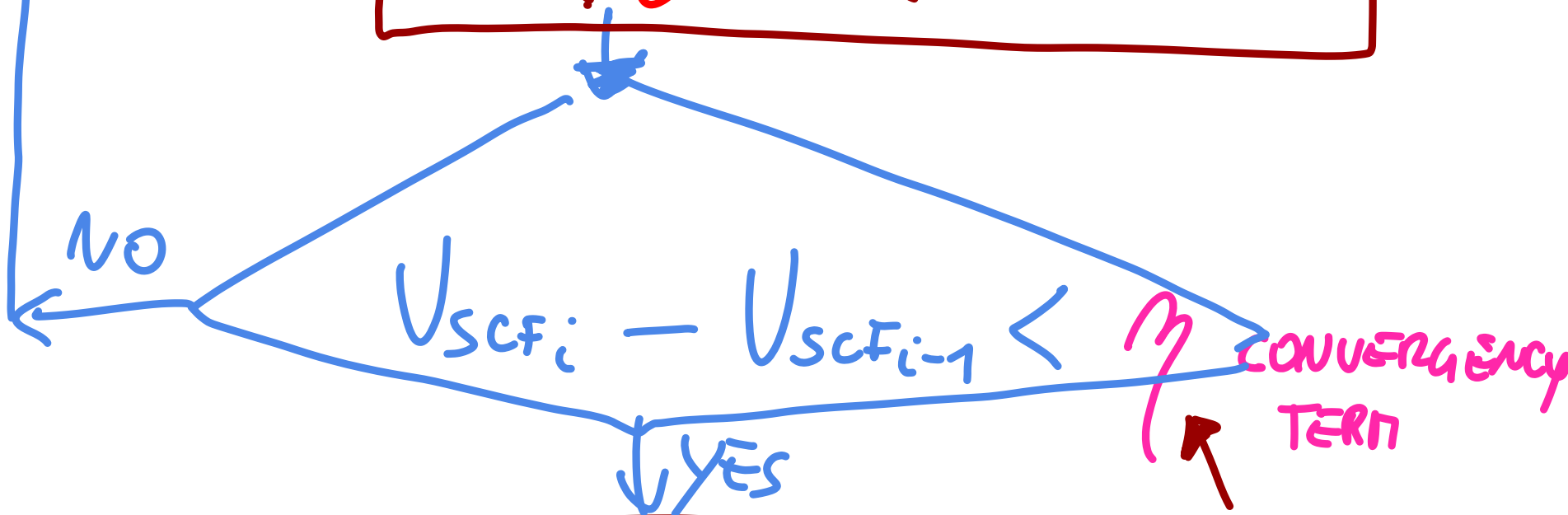
⊙

EQUILIBRIUM

V_{DS}
SEVERAL
STEPS
 i

$$\begin{aligned} \epsilon_i &\leftarrow \epsilon_{i-1} - U_{SCF i-1} \\ N_i &\leftarrow D_{OS} \leftarrow \epsilon_i \\ U_{SCF i} &\leftarrow N_i \end{aligned}$$

$V_i \in V_{DS}$
RANGE



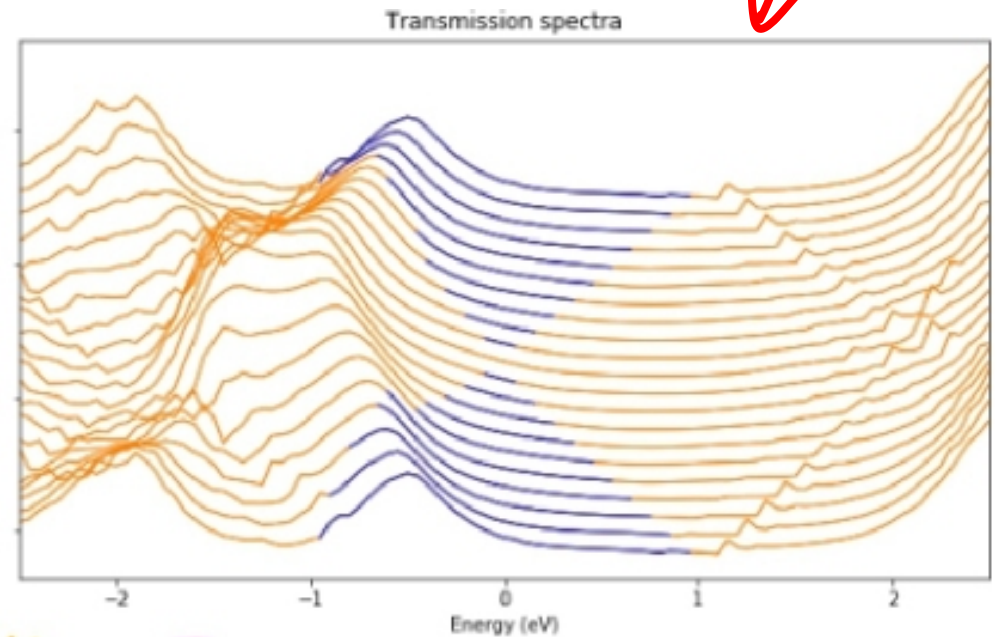
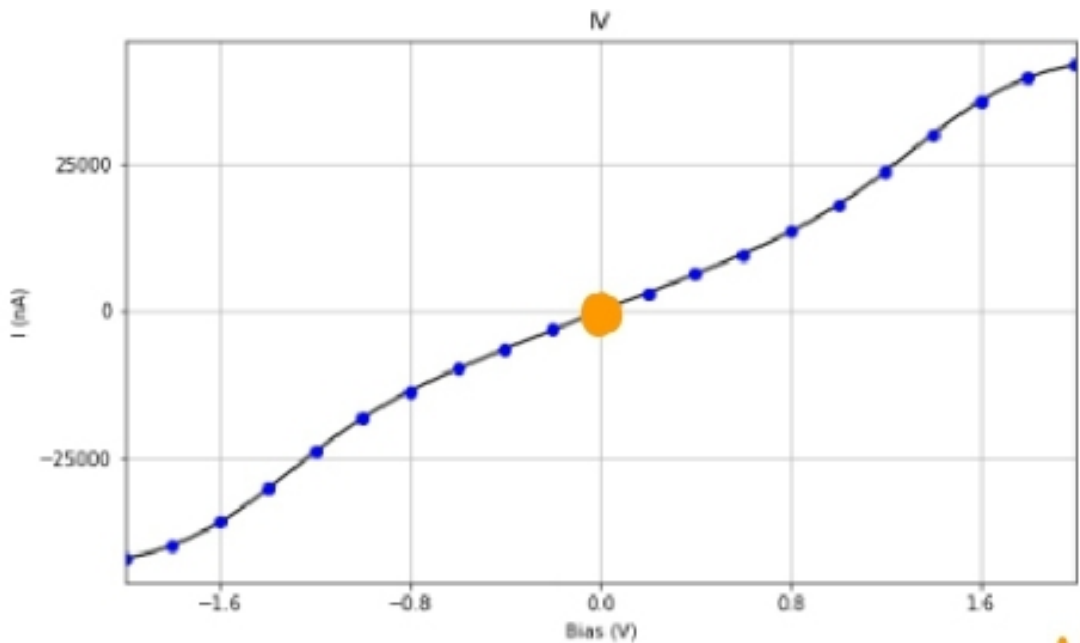
$$T(\epsilon_i), I_{DS i}$$

PROBLEM! $N \leftarrow D \leftarrow$ PEAKS!

00
00

HOW DOS CHANGES
w.r.t. \odot EQUILIBRIUM

HOW TO EVALUATE?



PROBLEM!

$N \leftarrow D \leftarrow$ PEAKS!

100%

HOW DOES CHANGES
W.R.T. \odot EQUILIBRIUM

HOW TO EVALUATE?

QUANTUM-ATK



AB INITIO
SIMULATION



- PRECISE
- CPU CONSUMING

EEBESD



HOW PEAKS
CHANGE WHEN
 V_{DS} (V_{GS}) CHANGE

BASED ON } AB INITIO
OR EXP.

EEBESD - SOLVES SCF LOOP

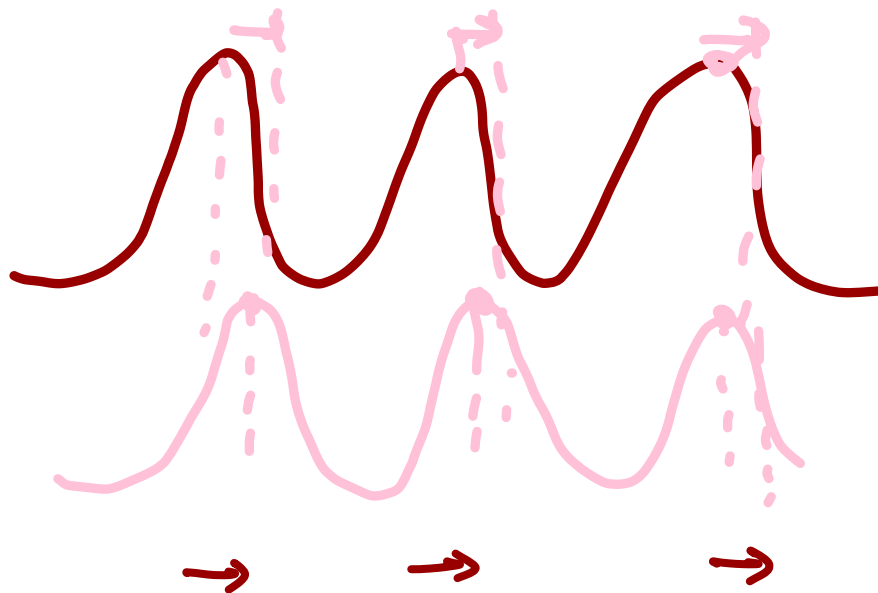
- ESTIMATES DOS

ASSUMPTIONS

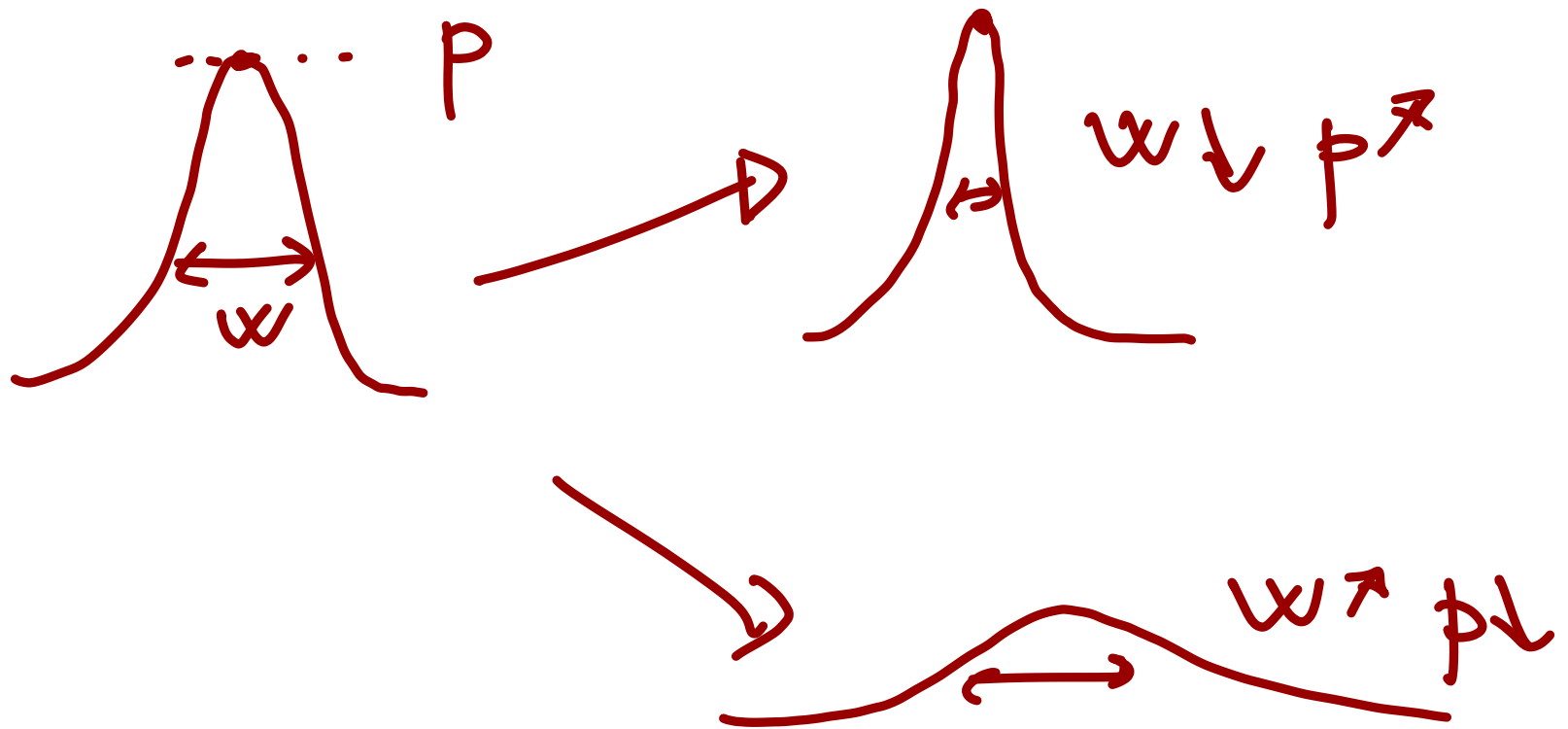
- BASED ON A BUNCH OF PRELIMINARY AB-INITIO SIM

① WHEN V_{DS} APPLIED PEAKS SHIFT

RIGIDLY



②



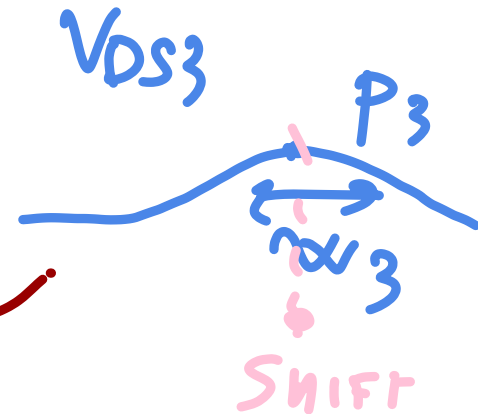
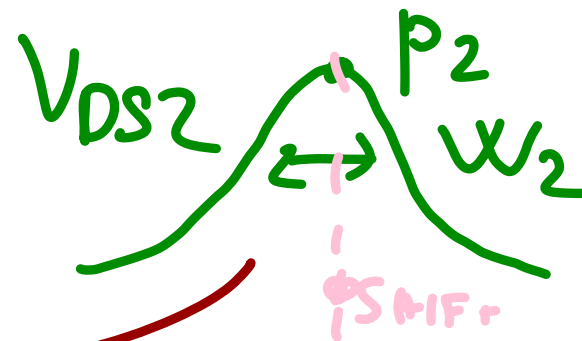
THERE MIGHT BE A PEAK VARIATION....

TALLER - SLINNER

SHORTER - FATTER

To model (1) & (2)

AB INITIO SIM



ELABORATE

$$k_1 + \alpha k_2 + \alpha^2 k_3$$

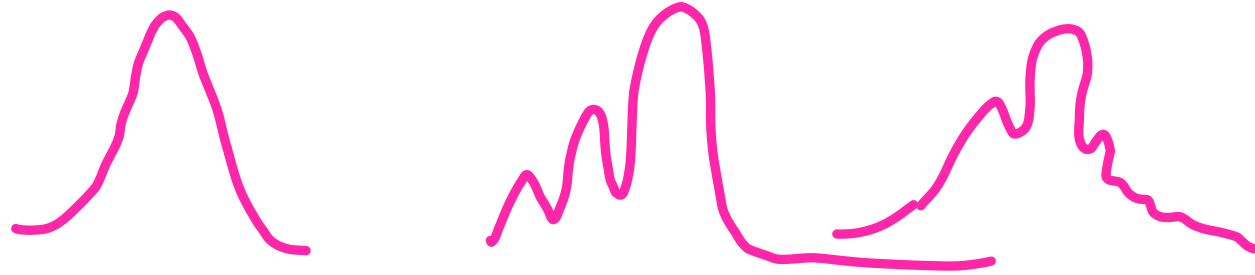
DESCRIBES EVOLUTION
PEAKS VDS

VALID FOR
1 MOLECULE

OTHER THINGS NOT
CONSIDERED FOR NOW

③

PEAKS CHANGE SHAPE



DIFFICULT

④

RESONANCE



EEBESD ORGANIZATION

- INITIAL EVAL \textcircled{B} EQ
- EXTRACTED PARAMS FROM AB INITIO (ESTIMATE DOS $k_1 k_2 k_3$)

∇V_G \leftarrow α COUPLING FACTOR

∇V_{DS}

\hookrightarrow EVALUATE \textcircled{E} ,
IN SCFL

$\delta_1 \delta_2$

ESTIMATE DOS

V_{SCF}

$T(\bar{E}, V_{DS}, V_G)$ $I(V_G, V_{DS})$

EEB30

USED IN EXERCISES

- FOR SOME MOLECULES
- FOR SEVERAL V_{DS}, V_{GS}
- FOR CASES OF PARAMETERS
 α, β_1, β_2

MATLAB BASED

CRISTALLIZATION

2) SCF LOOP

3) SIMPLE
CIRCUITS BASED ON RT

↳ NEXT LECTURE