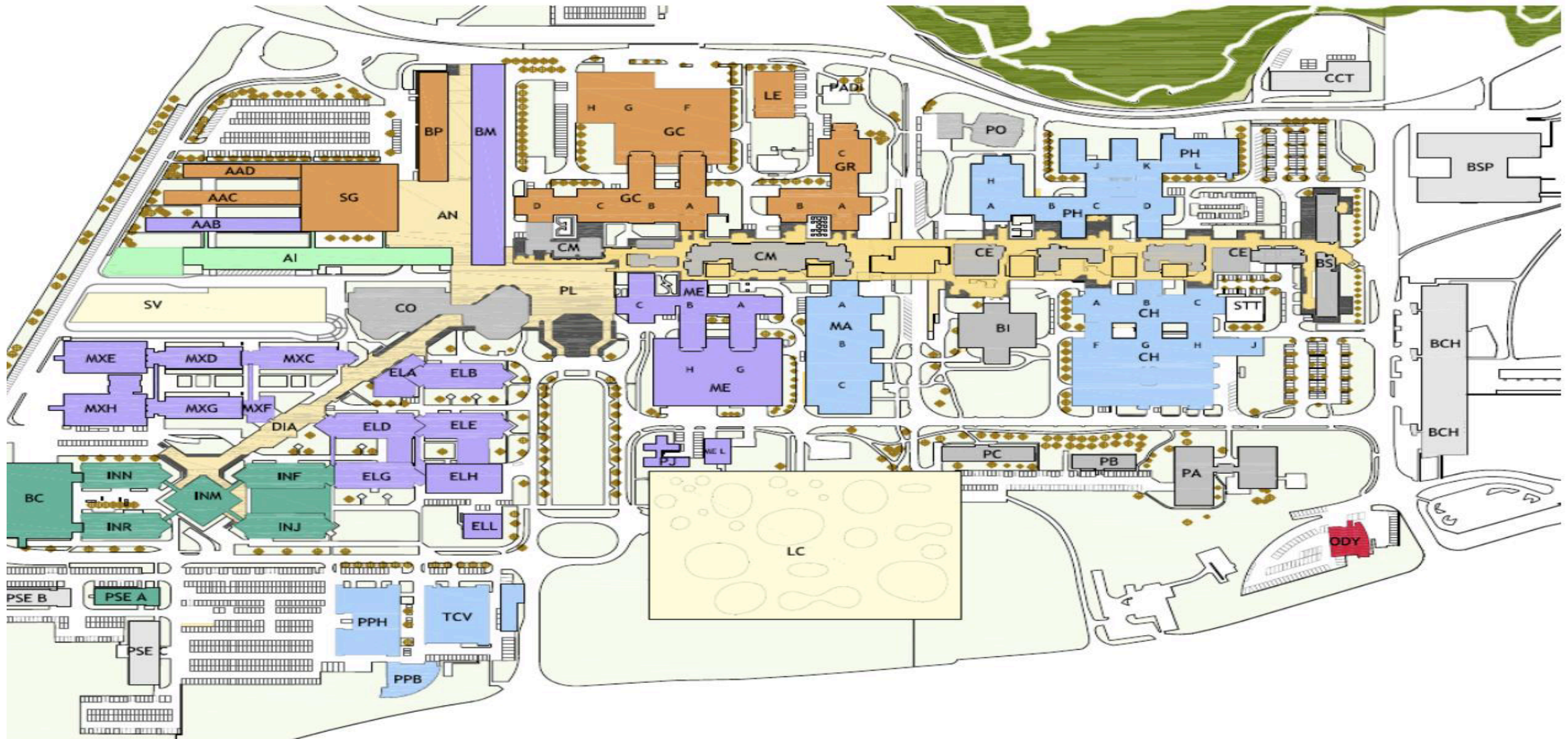


# Part 1 : defining the heating and cooling needs of a building

Prof François Marechal

## EPFL Buildings stock

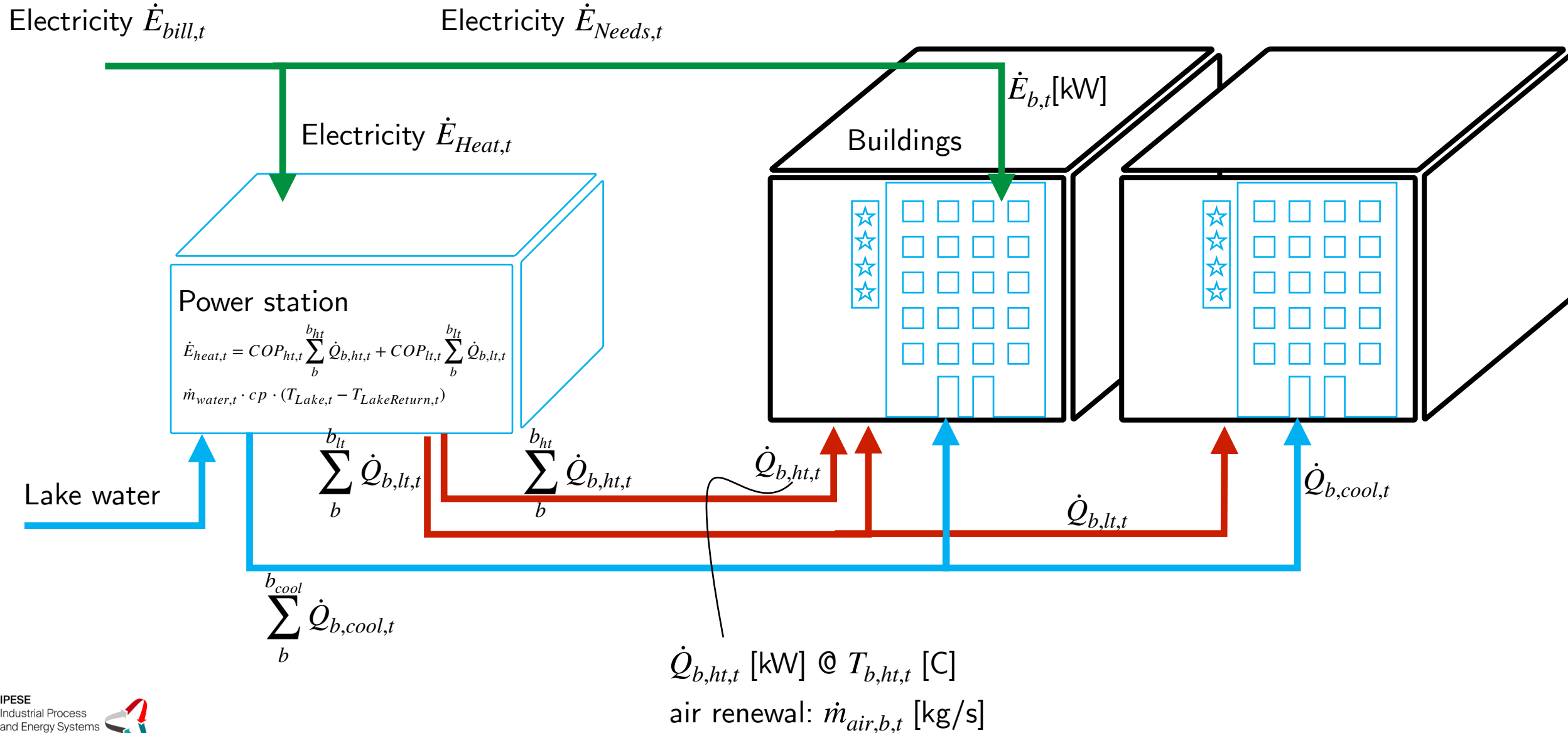


The goal is to design the energy system of an international university campus with the goal of minimising its environmental impact.

- **Task 1 : Defining the energy demand of a campus building**
  - What are the heat loads to be supplied to each building
  - Define the temperature levels of the demand
  - Define the energy bill
- **Task 2 : Model the building energy system and heat recovery options**
  - Define the building energy system flowsheet
  - Calculate the system configuration states
  - Estimate the related investment
- **Task 3 : Optimise the investment of heat recovery options for a building**
  - define the size of the investments on an objective function
  - model heat pumps and to choose the best working fluids and operating conditions of heat pumping cycles
  - Integrate the data center heat recovery
  - generate building's retrofit options
- **Task 4 : Propose and compare options for a more sustainable campus energy system**
  - integrate the buildings in the campus district heating and cooling system
  - define sustainability metrics for the decision support
  - Compare decentralised and centralised options with pro and cons for different options of the system design

- **1. Energy demand models: building modelling**
- **2. Methods for solving a set of equations**
- **3. Clustering : what are the most probable states to be realised by the energy system over its lifetime**
- **4. Flowsheets and energy systems models**
- **5. Key performance models of an energy system**
- **6. Techno-economic optimisation of an energy system**
- **7. Solving optimisation problems**
- **8. Constitutive equations and thermodynamic properties of flows in flowsheets**
- **9. Process units models**
- **10. FlowSheet simulation**
- **11. Data reconciliation and parameter identification**
- **12. Energy system modelling with Linear programming techniques**
- **13. Multi-objective optimization for energy system design**

# EPFL What are the needs ?



## ■ Analyse

- What we want ?
  - define variables ( $x_i$ ) : give a textual description
  - define physical units : e.g. [ $kJ_e/kJ_{th}$ ]
  - define order of magnitude of expected value of  $x_i$  :  $x_{i_{min}} \leq x_i \leq x_{i_{max}}$
- What we know : Write equations defining your knowledge !
  - write the knowledge as a set of equations  $f_k(x_i, \pi_{k,j}) = 0$
  - $\pi_{k,j}$  are parameters of equation k
- What we have : collect the data :
  - values of  $\pi_{k,j} \Rightarrow$  reference, [physical units], comments
  - add assumptions :  $f_a(x_i, \pi_{a,j}) = 0$  so that  $\#k + \#a = \#i$

## ■ Generate

- Find numerical value of  $x_i$  by solving the set of equations :  $f_e(x_i, \pi_{e,j}) = 0$ , with  $x_{i_{min}} \leq x_i \leq x_{i_{max}}$  and  $f_e = \{f_k, f_a\}$ 
  - define the solving method
  - define the convergence criteria

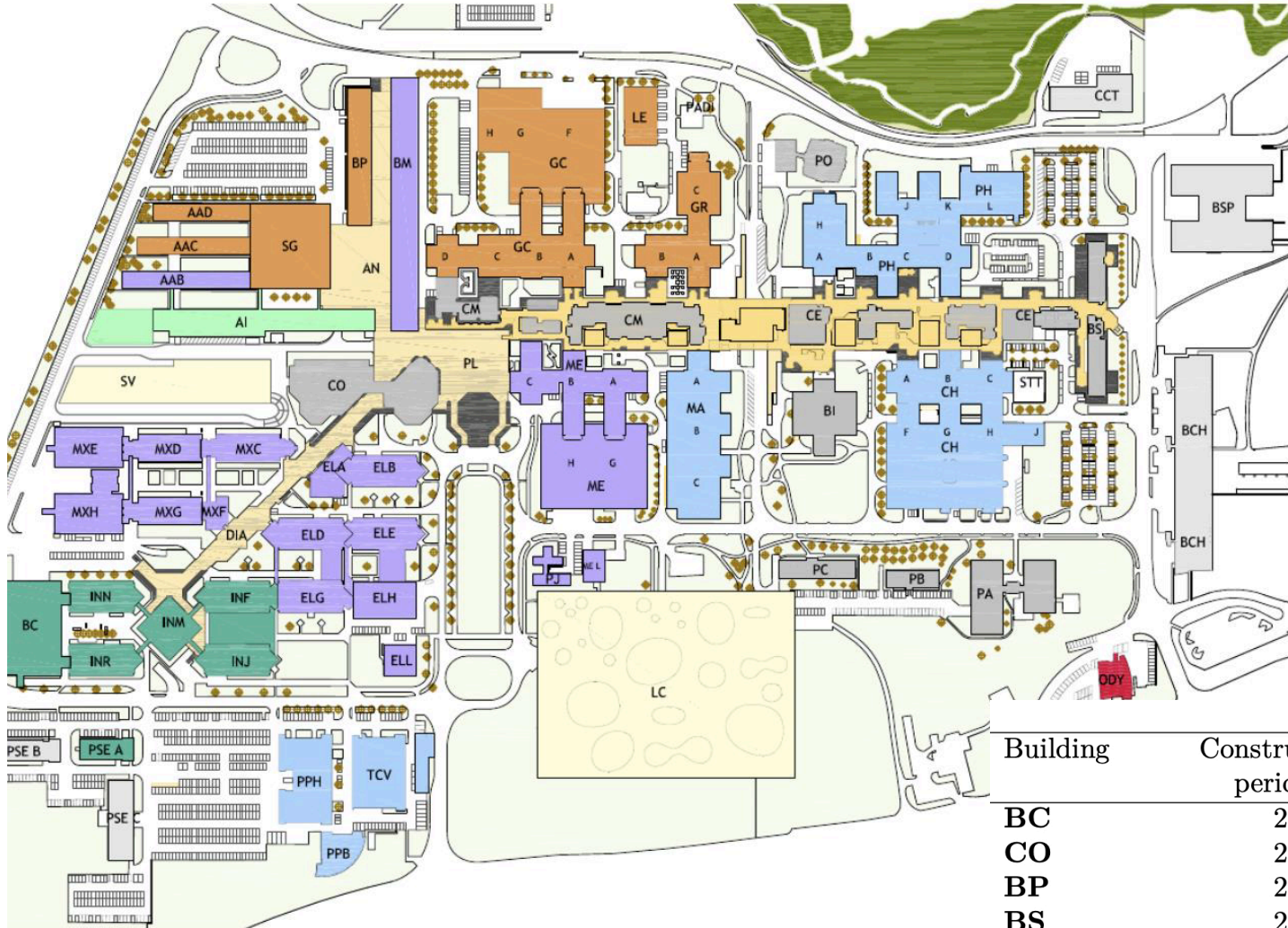
## ■ Interpret

- Verify that the value of  $x_i$  is meaningful for the application

## ■ Report

- Report the values (plots, tables, validity check)

## Buildings stock



Heating needs are defined by :

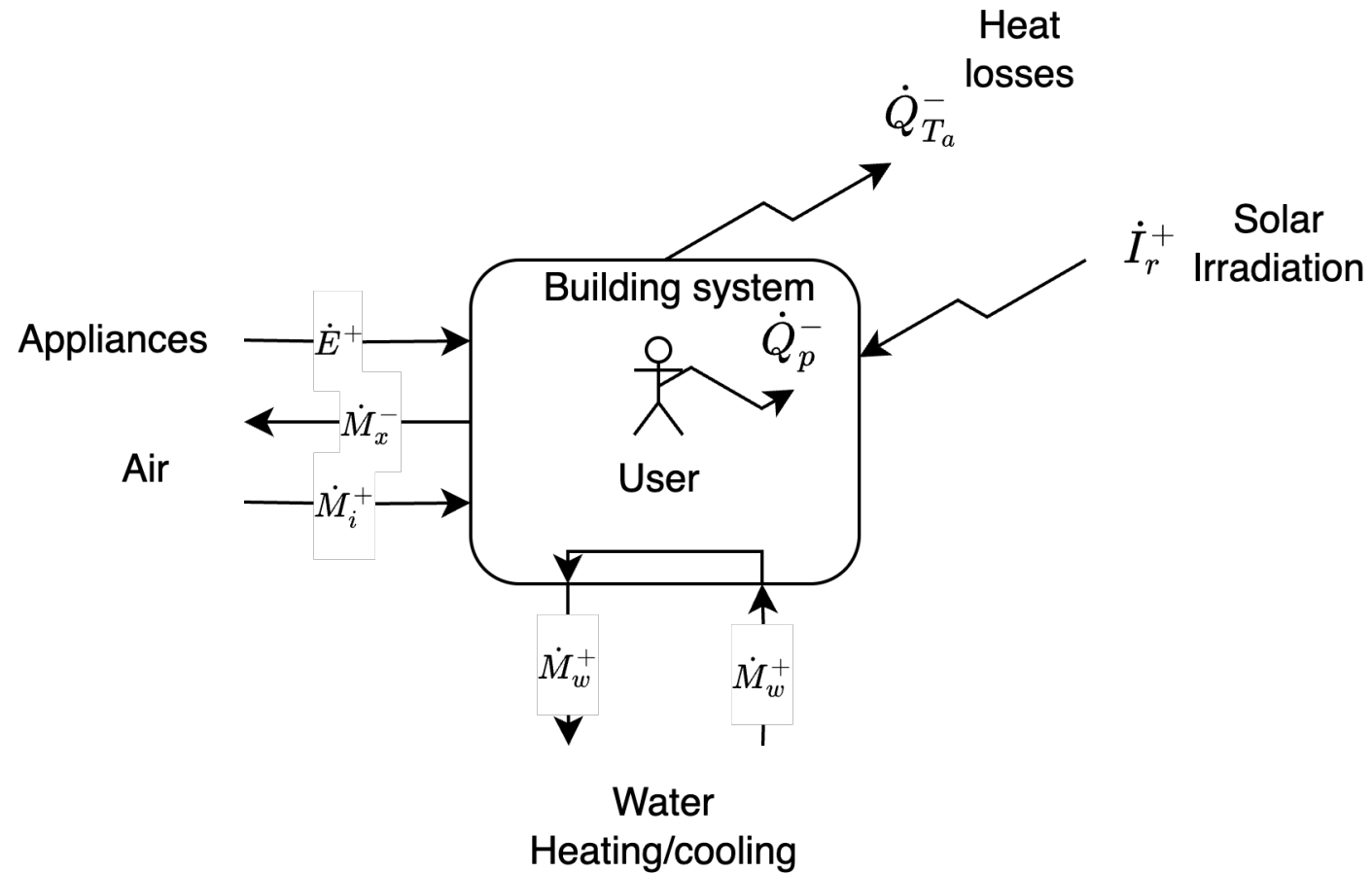
- $\dot{Q}_{b,t} \quad \forall b \in \{1..n_b\}$  [kW]  
heat required by building b at time t of the year
- $T_{b,t}^{supply} \quad \forall b \in \{1..n_b\}$  [°C]  
Minimum temperature of the heat supply of building b at time t of the year

Available :

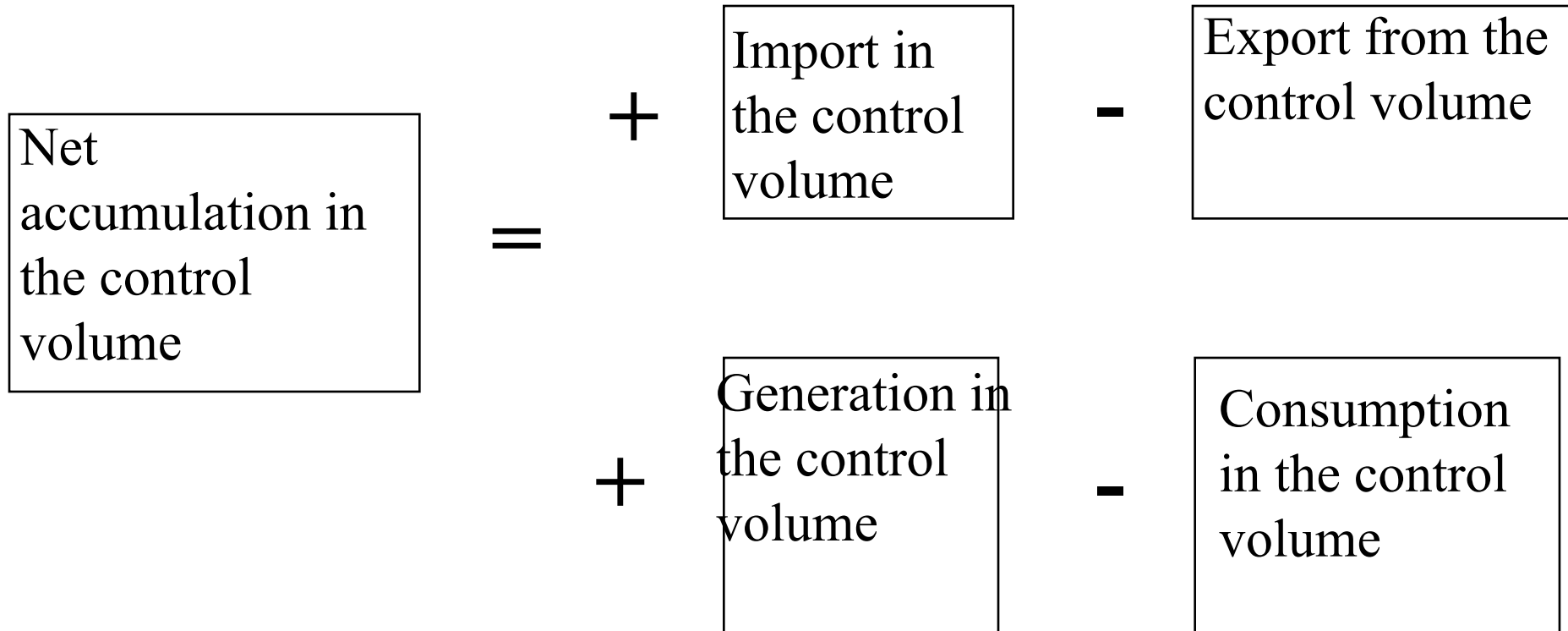
Table 1.1: EPFL Buildings

Building	Construction period <sup>a</sup>	Heated surface $A_{th}$ [m <sup>2</sup> ]	Annual heat demand $Q_{th}$ [kWh]	Annual electricity demand $Q_{el}$ [kWh]
BC	2	17480	418,491	1,603,596
CO	2	11901	477,008	943,653
BP	2	10442	457,861	691,031
BS	2	10267	509,183	350,860
TCV	2	6095	318,209	2,067,675

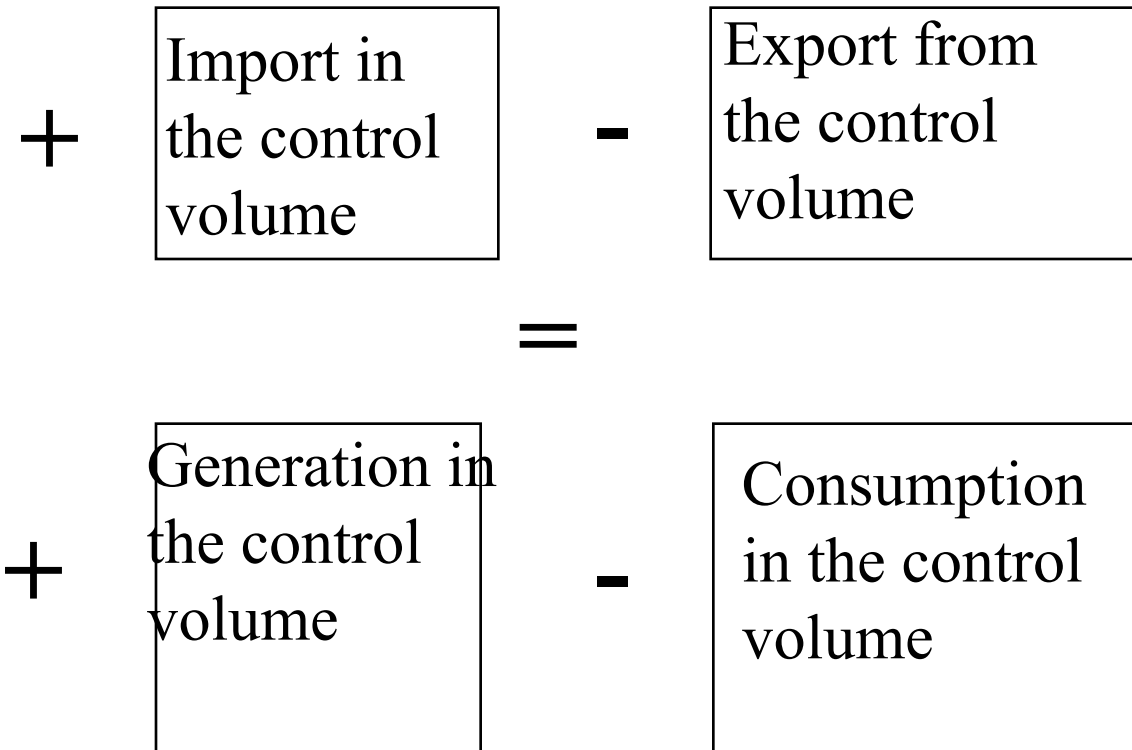




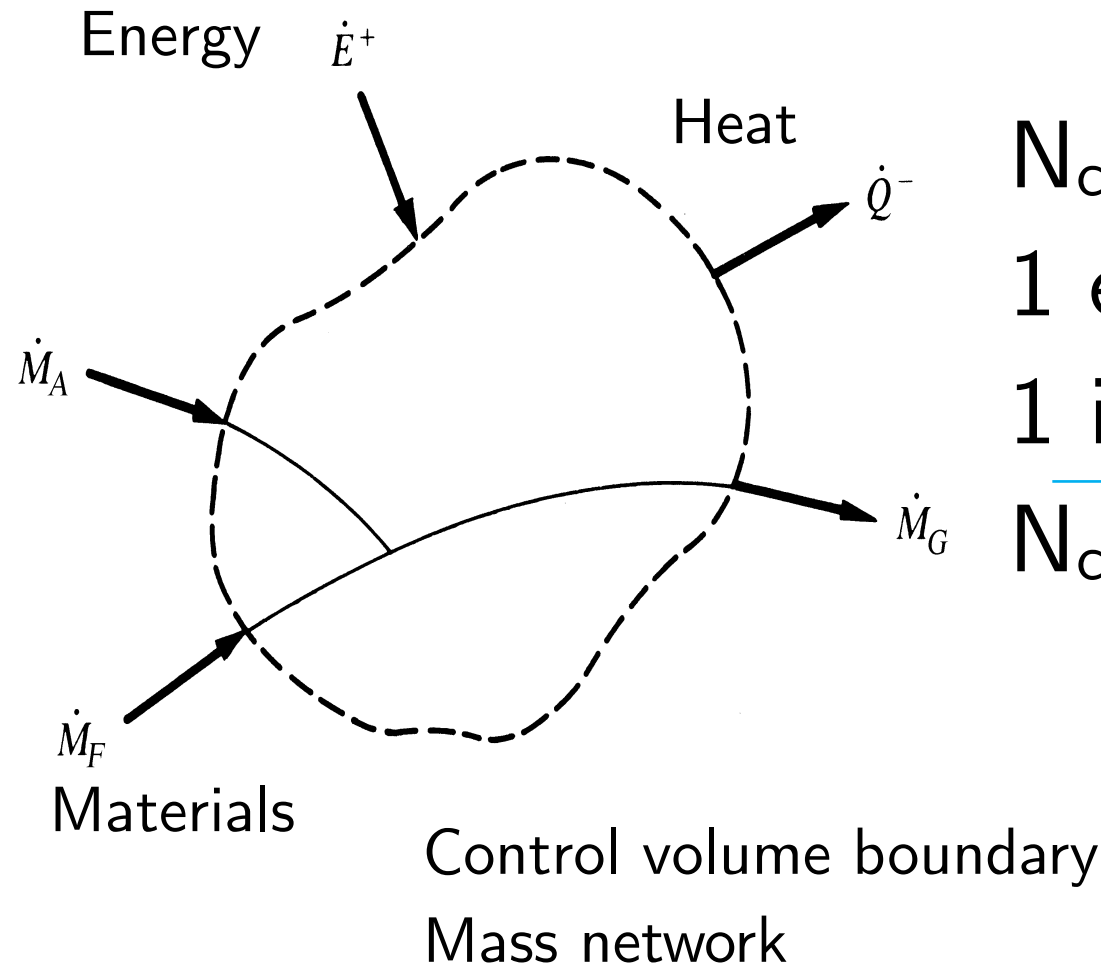
$$\mathbf{Accumulation = in - out + Generation - Consumption}$$



***no Accumulation = 0 = in - out + Generation - Consumption***



**For a given control volume with 1 network with  $N_c$  substances without chemical reactions**



$N_c$  mass balances per network\*

1 energy balance

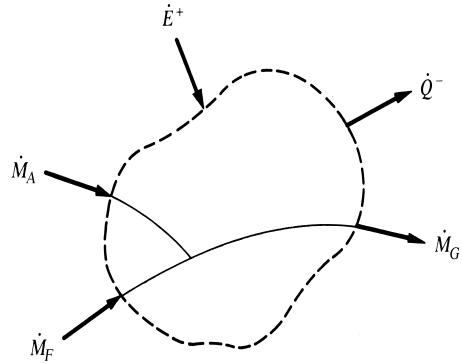
1 impulsion balance (P)

$N_c + 2$  balance equations

\*when chemical reactions occur the material balance is the atomic balance

Network or pipes : interconnected flows with mass exchange

## For a given control volume with 1 network with $N_c$ substances



Material balance

$$\sum_f \dot{m}_{c,f}^+ = \frac{dM_c}{dt} = 0 \quad \forall c$$

Accumulation

Energy balance

$$\sum_f \dot{m}_f^+ \cdot h(T_f, P_f, x_f) + \sum_Q \dot{Q}^+ + \sum_E \dot{E}^+ = \frac{dQ}{dt} = 0$$

Accumulation

Subscript + means positive when entering

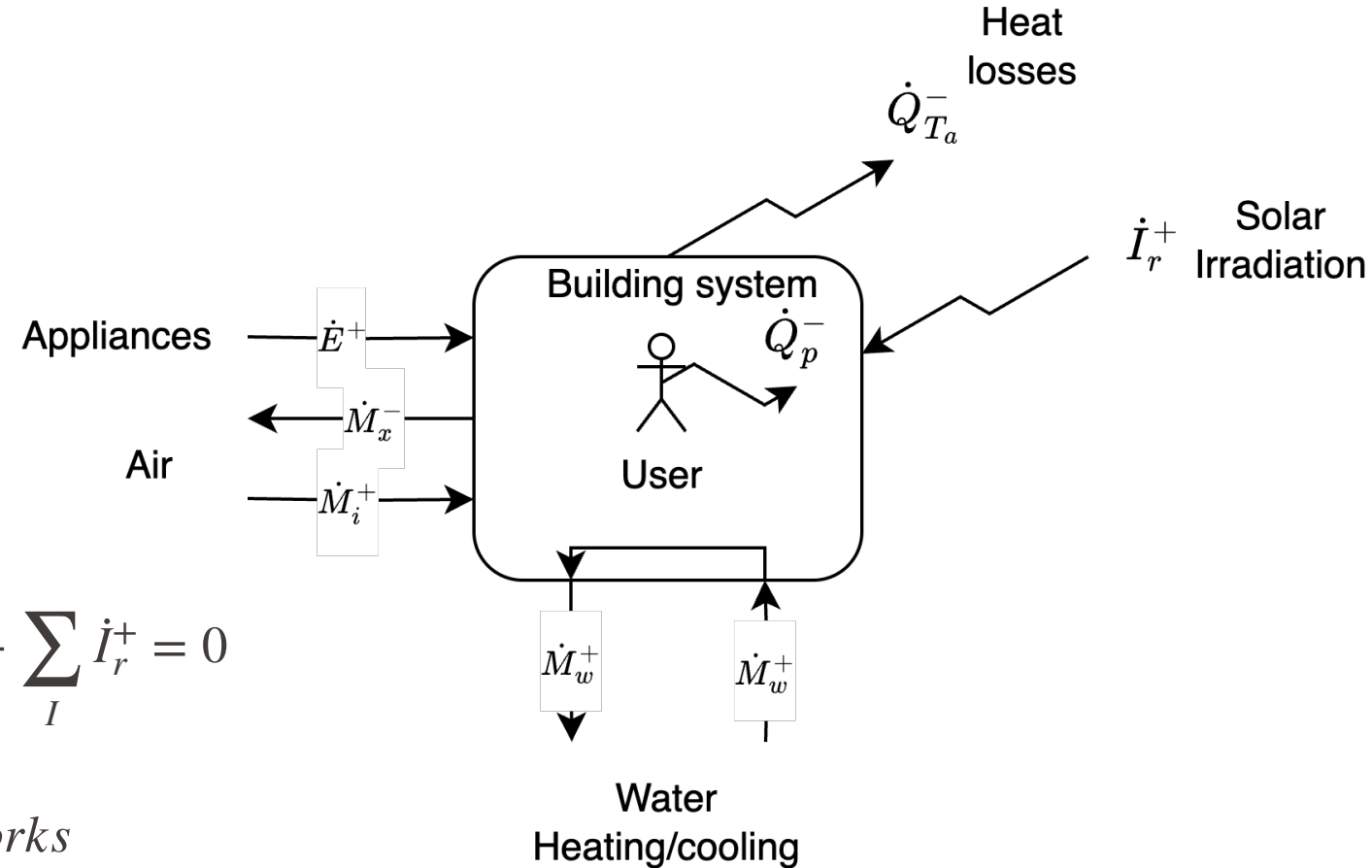
$h(T_f, P_f, x_f)$  enthalpy of flow  $f$  with temperature  $T_f$ , Pressure  $P_f$  and composition  $x_f$

Non linear equations !

- Each flow  $x$  is characterized by
  - Mass flow: e.g.  $\dot{M}_x^-$
  - Thermodynamic state:  $T_x, P_x, n_x$
  - State variables :  $s_x$  e.g.  $h(T_x, P_x, n_x)$
- Transfers are modeled by
  - $\dot{Q}_k^+ = f(\pi_k, \dot{M}_x^+, s_x)$
- Energy balance :

$$\sum_f \dot{M}_f^+ \cdot h(T_f, P_f, x_f) + \sum_Q \dot{Q}^+ + \sum_E \dot{E}^+ + \sum_I \dot{I}_r^+ = 0$$

- Mass balance :  $\sum_f \dot{M}_{n,f}^+ = 0 \quad \forall n \in networks$



- We would like to know what is the heat load and the corresponding temperature of the heat supply for each state that the building will see in the future :

$\dot{Q}_b^+$ : Heating/cooling load to supply to building  $b$  at time  $t$  of its life time to maintain the comfort temperature when the people are in the building

$$\dot{Q}_b^+ [kW] = \dot{M}_{w_b}^+ \cdot (h_w(T_s, P_s) - h_w(T_r, P_r))$$

with  $\dot{M}_{w_b}^+$ : flow of water heating of build b

$h_w(T_s, P_s)$ : Enthalpy of water at  $T_s, P_s$

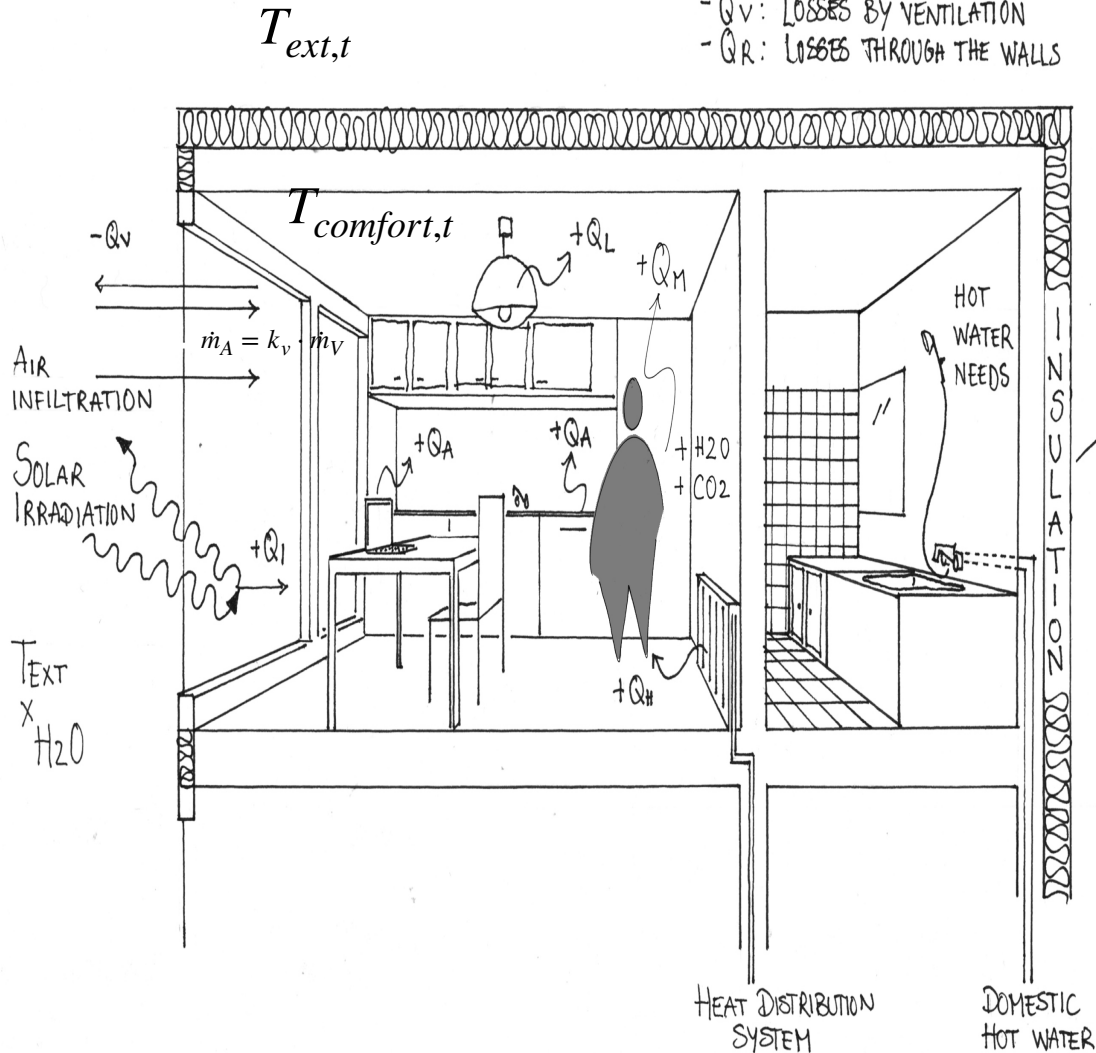
$$h_w(T_s, P_s) = \int_{T_0}^{T_s} c p_w(T) \cdot dT \approx \tilde{c} p_w (T_s - T_0)$$

$T_s$  : the Supply Temperature of the heat distribution system to the building b at time t

$T_r$  : the Return Temperature of the heat distribution system to the building b at time t

$T_0$ : reference temperature for the calculation of enthalpies

- + Q<sub>A</sub> : GAIN BY APPLIANCES
- + Q<sub>H</sub> : HEAT TO COMPENSATE LOSSES
- + Q<sub>L</sub> : GAIN BY LIGHTING SYSTEM
- + Q<sub>M</sub> : GAIN BY HUMAN
- + Q<sub>I</sub> : GAIN BY IRRADIATION
- Q<sub>V</sub> : LOSSES BY VENTILATION
- Q<sub>R</sub> : LOSSES THROUGH THE WALLS



Our knowledge :

The model of the building envelop heat balance

$$\dot{Q}_{A,t} [kW] = \dot{E}_{A,t}$$

$$\dot{Q}_{L,t} [kW] = \dot{E}_{L,t}$$

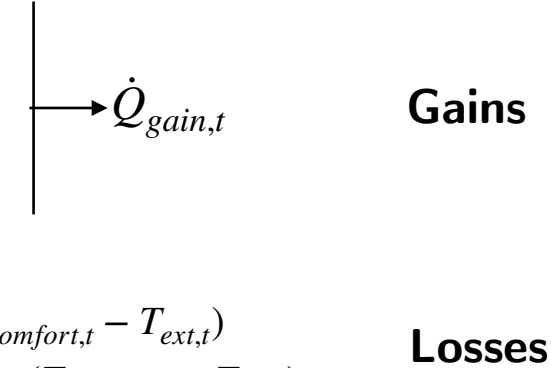
$$\dot{Q}_{M,t} [kW] = \dot{q}_{cap} \cdot \sum_{cap} cap_t$$

$$\dot{Q}_{I,t} [kW] = Irr_t \cdot k_{sun}$$

$$\dot{Q}_{V,t} [kW] = \dot{m}_v \cdot cp_{air} \cdot (T_{comfort,t} - T_{ext,t})$$

$$\dot{Q}_{R,t} [kW] = \sum_{wall} k_{wall} \cdot S_{wall} \cdot (T_{comfort,t} - T_{ext,t})$$

$$\dot{Q}_{V,t} + \dot{Q}_{R,t} = k_{th} (T_{comfort,t} - T_{ext,t})$$

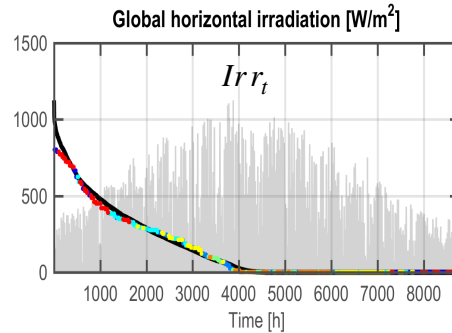
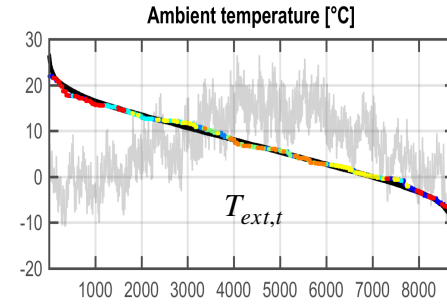
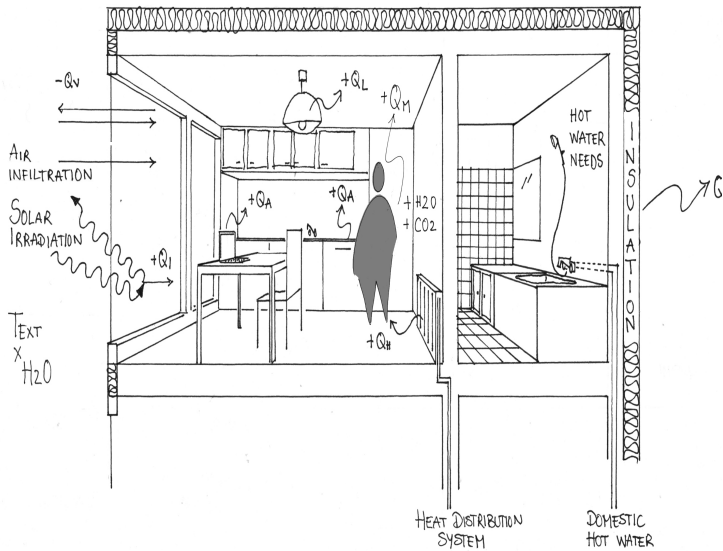


Energy balance :

what is the heat load to maintain the comfort ?

$$\dot{Q}_{H,t} [kW] = max(0, \dot{Q}_{V,t} + \dot{Q}_{R,t} - (\dot{Q}_{A,t} + \dot{Q}_{L,t} + \dot{Q}_{M,t} + \dot{Q}_{I,t}))$$

- +QA : GAIN BY APPLIANCES
- +QH : HEAT TO COMPENSATE LOSSES
- +QL : GAIN BY LIGHTING SYSTEM
- +QM : GAIN BY HUMAN
- +QI : GAIN BY IRRADIATION
- QV : LOSSES BY VENTILATION
- QR : LOSSES THROUGH THE WALLS



## Heat gains :

Appliances :  $\dot{Q}_{A,b,t} = \dot{E}_{A,b,t}$

Lighting :  $\dot{Q}_{L,b,t} = \dot{E}_{L,b,t}$

People :  $\dot{Q}_{M,b,t} = \dot{q}_{cap_b} \cdot \sum_{cap_b} cap_b$

Solar Irradiation :  $\dot{Q}_{I,b,t} = Irr_t \cdot k_{sun_b}$

## Losses

### Ventilation

$$\dot{Q}_{V,b,t} = \dot{m}_{V_b} \cdot cp_{air} \cdot (T_{comfort,b,t} - T_{ext,t})$$

### Heat transfer through the walls

$$\dot{Q}_{R,b,t} = \sum_{wall_b} k_{wall_b} \cdot S_{wall_b} \cdot (T_{comfort,b,t} - T_{ext,t})$$

## Balance : Heat to supply

$$\dot{Q}_{H,t} = \dot{Q}_{b,t} = \max(0, \dot{Q}_{V,b,t} + \dot{Q}_{R,b,t} - (\dot{Q}_{A,b,t} + \dot{Q}_{L,b,t} + \dot{Q}_{M,b,t} + \dot{Q}_{I,b,t}))$$

## Heat supply [kW] function :

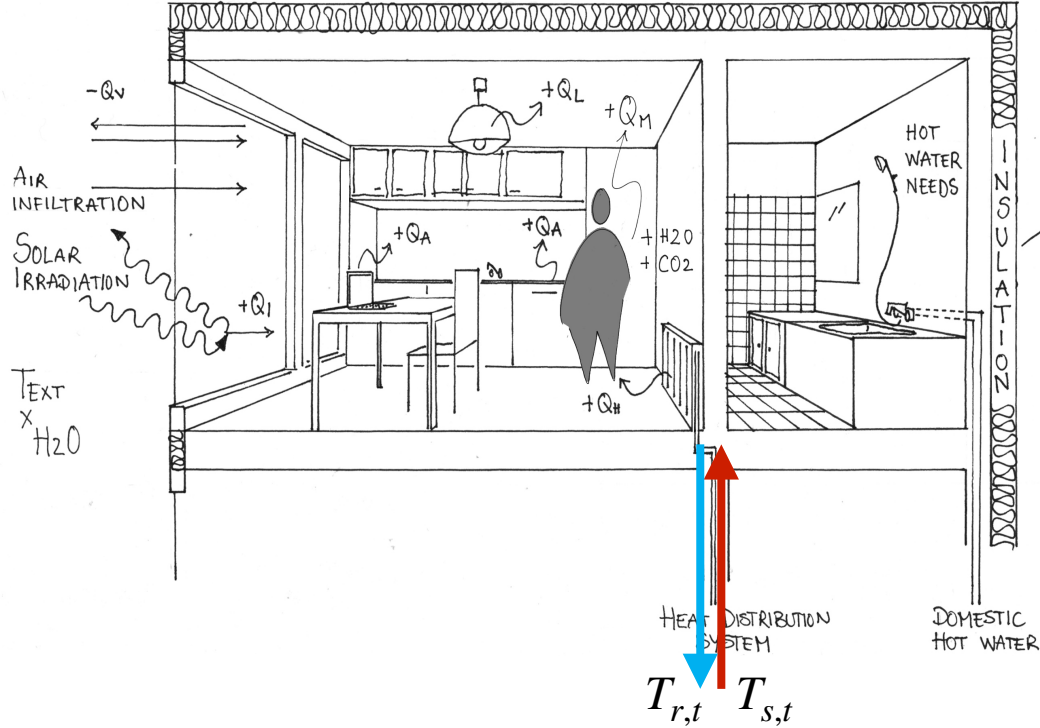
$$\dot{Q}_b(t) = \max(0, k_{th_b} \cdot (T_{comfort,b,t} - T_{ext,t}) - k_{sun_b} \cdot Irr_t - \dot{Q}_{gain,b,t})$$

## Heat energy [MJ/period] :

$$Q_b(t_0, t_{end}) = \int_{t_0}^{t_{end}} \dot{Q}_{b,t} \cdot dt = \int_{t_0}^{t_{end}} \max(0, k_{th_b} \cdot (T_{comfort,b,t} - T_{ext,t}) - k_{sun_b} \cdot Irr_t - \dot{Q}_{gain,b,t}) \cdot dt$$

- $Need_{k,t} = f(\pi_k, x_{k,i,t})$ 
  - $\pi_k$  : parameters characterising the need k
    - Assumptions & knowledge
      - Physical/Chemical phenomena
      - Typical values from engineering practice
    - Observations => parameter fitting
  - $x_{i,k,t}$  : variables defining the environment applying to the need k in the future
    - Observations
    - Statistics
    - Models : e.g. future temperatures, future use of the building

- + Q<sub>A</sub> : GAIN BY APPLIANCES
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Temperatures of the heat distribution (hd) system:  
supply  $T_{s,t}$  and return  $T_{r,t}$  can be calculated

$$\dot{Q}_{b,t} = \dot{m}_{hd_b,t} \cdot c_{p_{hd_b}} \cdot (T_{s_b,t} - T_{r_b,t}) \quad [1]$$

$$T_{r_b,t} = T_{s_b,t} - \frac{\dot{Q}_{b,t}}{\dot{m}_{hd_b,t} \cdot c_{p_{hd_b}}} \quad [2]$$

$T_{s_b,t}$  is calculated by solving heat transfer equation

$$\dot{Q}_{b,t} = UA_{hd_b} \frac{(T_{s_b,t} - T_{r_b,t})}{\ln(T_{s_b,t} - T_{comfort_{b,t}}) - \ln(T_{r_b,t} - T_{comfort_{b,t}})} \quad [3]^*$$

with  $UA_{hd_b}$  calculated from the design conditions @  $T_{ext} = -10 \text{ }^\circ\text{C}$

$$UA_{hd_b} = \dot{Q}_{b,design} \cdot \frac{\ln(T_{s_b,design} - T_{comfort_{b,design}}) - \ln(T_{r_b,design} - T_{comfort_{b,design}})}{(T_{s_b,design} - T_{r_b,design})}$$

For each building and each time will obtain the minimum supply and return temperatures of the building.

\* use [1] and [2] in [3] to have an explicit formula of  $T_{s_b,t}$  as a function of  $\dot{Q}_{b,t}$ ,  $\dot{m}_{hd_b,t} \cdot c_{p_{hd_b}}$  and  $UA_{hd_b}$

$$Q_b(t_0, t_{end}) = \int_{t_0}^{t_{end}} \dot{Q}_{b,t} \cdot dt = \int_{t_0}^{t_{end}} \max(0, \mathbf{k}_{th_b} \cdot (T_{comfort_{b,t}} - T_{ext,t}) - \mathbf{k}_{sun_b} \cdot Irr_t - \dot{Q}_{gain_{b,t}}) \cdot dt$$

$\mathbf{k}_{th_b}$  : thermal heat loss coefficient of the building b envelop

includes air renewable and convection losses via walls, windows roof and basement.

$\mathbf{k}_{sun_b}$  : solar gains coefficient of building b envelop

includes orientation and windows

Calculate  $k_{sun_b}$  and  $k_{th_b}$  if

$$Q_b^1 = Q_b(\text{January, December})$$

and

$$Q_b^2 = Q_b(\text{February, March})$$

$$Q_b(\text{January, December})(\mathbf{k}_{sun_b}, \mathbf{k}_{th_b}) - Q_b^1 = 0$$

$$Q_b(\text{February, March})(\mathbf{k}_{sun_b}, \mathbf{k}_{th_b}) - Q_b^2 = 0$$

2 equations and 2 unknowns :  $\mathbf{k}_{sun_b}, \mathbf{k}_{th_b}$

Activate your knowledge :

Solve a set of equations

$$F(X, \pi) = 0$$