
ME-446 Liquid-Gas Interfacial Heat and Mass Transfer

Homework 8

Presentation by Group 8 on Thursday 13th November

Problem 1: Maxima of number of isolated bubbles

In *International Journal of Heat and Mass Transfer* 182 (2022) 121904, Zhang et al gave an expression for the number of isolated bubbles on a surface:

$$N_{iso} = \sum_{N=1}^{\infty} \frac{N_0^N}{(N-1)!} e^{-\left(N_0 + \frac{\pi N D_b^2}{A}\right)}$$

where N_0 is the expectation value of the number of active nucleation sites on the surface, A is the surface area, and D_b is the diameter when departing from the surface. Assume the critical heat flux (CHF) is reached when $\frac{\partial N_{iso}}{\partial T} = 0$ and N_0 is the only parameter on the right-hand side that is a function of temperature T .

A) Prove that the following is true at CHF,

$$n_0 \pi D_b^2 = 1$$

where n_0 is the expected active nucleation site density at CHF or $n_0 = N_0/A$ at CHF.

B) Show that at CHF,

$$N_{iso} = \frac{N_0}{e}$$

Problem 2: Kandlikar Model

Kandlikar expression for the critical heat flux of pool boiling at an upward-facing horizontal heated large surface is given by:

$$q_c'' = h_{fg} \rho_g^{\frac{1}{2}} \left(\frac{1 + \cos \beta}{16} \right) \left[\frac{2}{\pi} + \frac{\pi}{4} (1 + \cos \beta) \right]^{\frac{1}{2}} [\sigma g (\rho_l - \rho_v)]^{\frac{1}{4}}$$

Plot the CHF prediction for contact angles β between 5° and 50° using water properties at atmospheric pressure.

Problem 3: Bubble coalescence

Consider two bubbles, both with radius r , initially isolated, with contact angle $= 0^\circ$. If they merge into a bigger spherical bubble while conserving the volume (also with contact angle $= 0^\circ$). Calculate the surface energy change of the system, assuming the liquid-bubble interface has a surface tension of γ .

Problem 4: Monte-Carlo simulation of spatial distribution of nucleation sites

Write a Monte Carlo code to simulate the spatial distribution of nucleation sites.

1. Define a $1 \text{ cm} \times 1 \text{ cm}$ plate.
 2. Randomly select 100 points on this plate as active nucleation sites.
- A) Plot the histogram for the probability density distribution of the nearest-neighbor distance among active nucleation sites.
- B) What functional form do you expect for this distribution? How well does the expected form align with your simulation data, and why?
- C) Repeat the same analysis for a cylindrical surface with radius 0.5 cm and height 1 cm instead of the flat plate. Answer the same questions (a) and (b) for this configuration.