

# Hydropower

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# Outline

- Introduction
  - Hydro today and future potential
  - Types of power stations
  
- Physics of hydro
  - Key equations: energy balance
  - Buckingham  $\pi$  theorem: similarity
  
- Hydraulic turbines
  - Hydraulic turbines: Pelton, Francis, Kaplan
  - New developments: microturbines
  
- Hydro & energy systems
  - Integration in the energy system
  
- Take home message

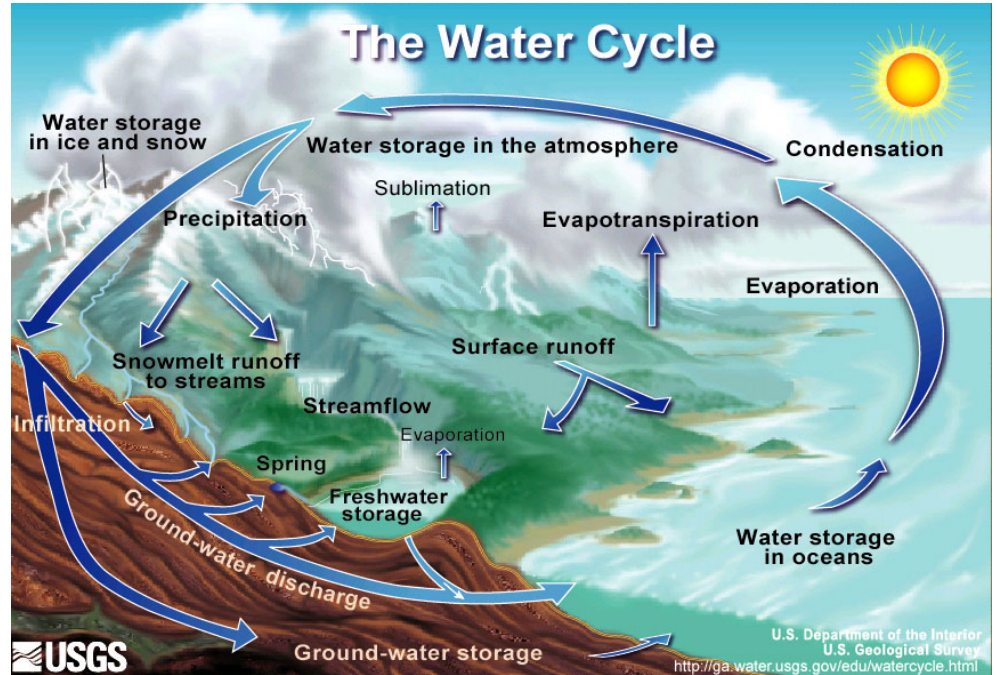


# Introduction

# EPFL What is hydropower?

- Water covers 71% of the Earth surface, mostly (>95%) concentrated in oceans. → the water cycle is driven by the sun.

- Used since early history:
  - Water wheels for irrigation
  - Water mills
  - Barbegal (Arles, F), 260 AD:
    - 10km long aqueduct
    - 18m head
    - 53 kW for flour production

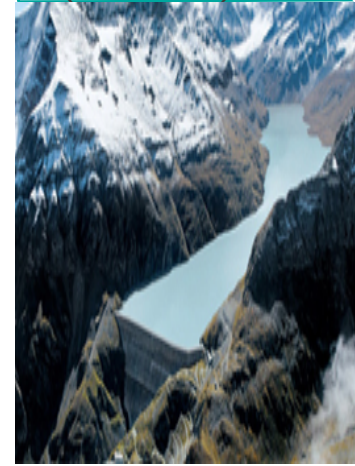


# EPFL Types of hydro power plants

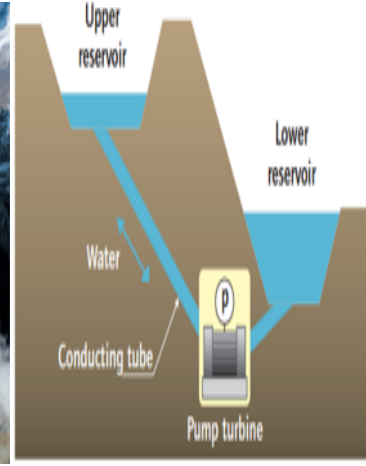
Hydro run-of-river



Hydro dam  
(storage)



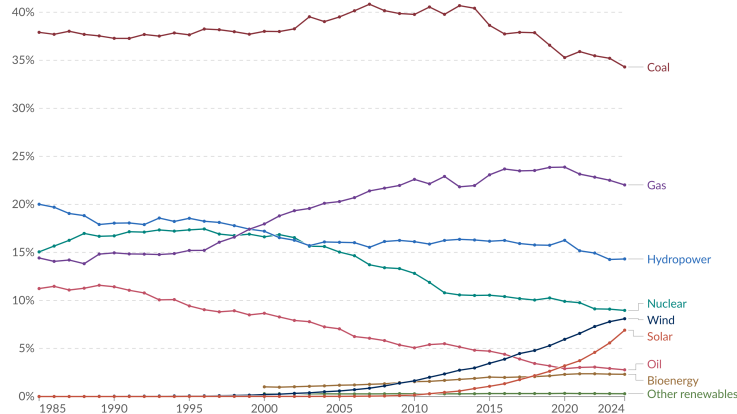
Pumped  
storage



# EPFL Hydro Power in the energy mix?

- World final energy consumption: 123800 TWh/y (2023)
- World electricity production: 28066 TWhe/y (2023)
- Hydro electricity production: 4210 TWhe/y (2023) (14.5%)
- IEA technical potential: 15000 TWhe/y
- Most developed and mature renewable technology

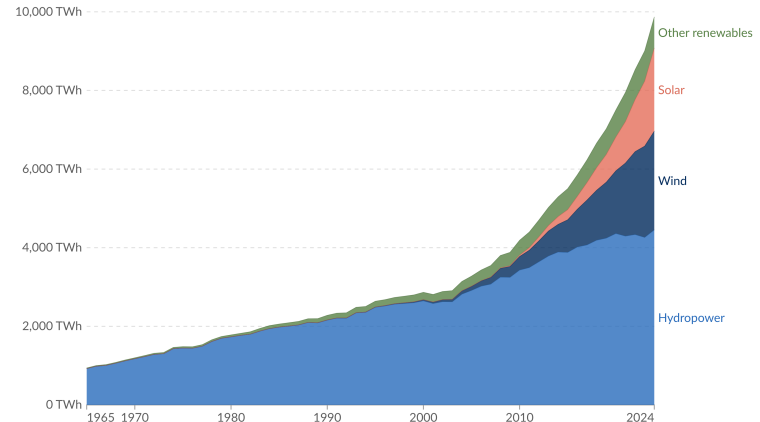
### Share of electricity production by source, World



Data source: Ember (2025); Energy Institute - Statistical Review of World Energy (2025)  
Note: "Other renewables" include geothermal, wave, and tidal.

OurWorldinData.org/energy | CC BY

### Renewable electricity generation, World



Data source: Energy Institute - Statistical Review of World Energy (2025)

OurWorldinData.org/renewable-energy | CC BY

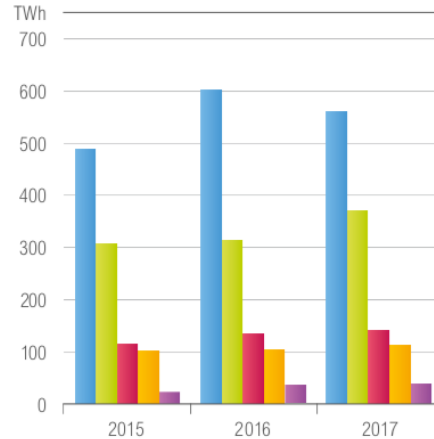
Note: "Other renewables" refers to renewable sources including geothermal, biomass, waste, wave and tidal. Traditional biomass is not included.

# EPFL Hydro today : Europe

- Hydro capacity relatively stable
- ENTSO-E hydro electricity: 600 TWh/y (2023) → 15.3%
- ENTSO-E hydro capacity: 230 GW (2023) → 18.4%

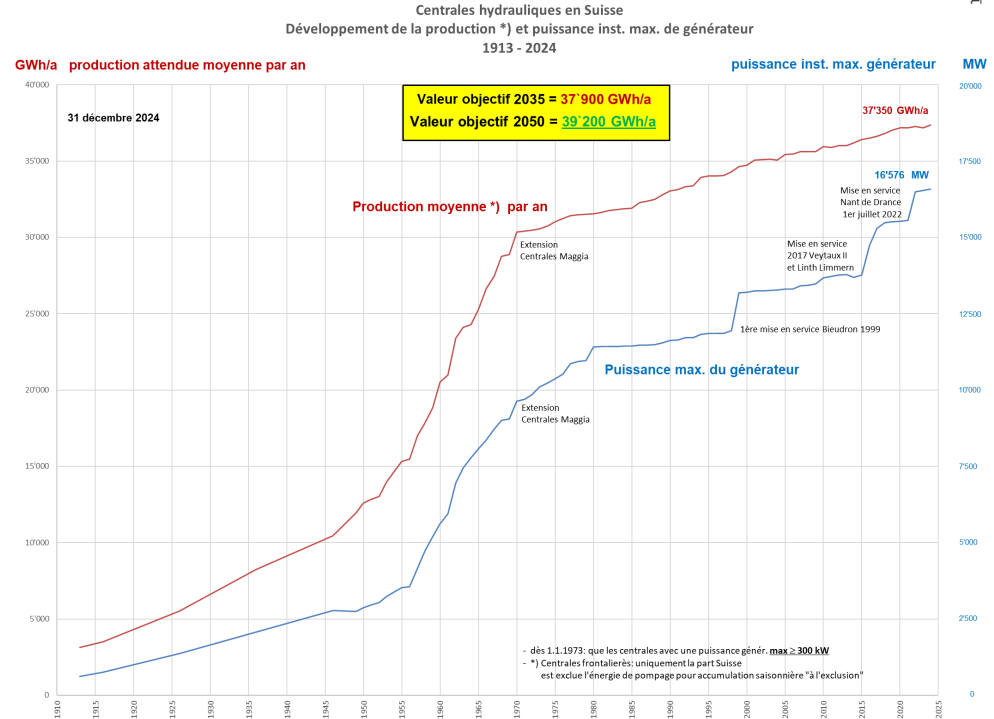
ENTSO-E renewable generation<sup>1</sup>

	year	TWh	%
<b>Renewable net generation</b>	2015	1042.4	
	2016	1200.0	
	<b>2017</b>	<b>1228.1</b>	
of which hydro	2015	489.2	47
	2016	604.6	50
	<b>2017</b>	<b>562.8</b>	<b>46</b>
of which wind	2015	310.6	30
	2016	316.1	26
	<b>2017</b>	<b>370.8</b>	<b>30</b>
of which biomass	2015	116.2	11
	2016	136.1	11
	<b>2017</b>	<b>141.1</b>	<b>11</b>
of which solar	2015	102.0	10
	2016	105.0	9
	<b>2017</b>	<b>114.3</b>	<b>9</b>
of which other renewable	2015	24.5	2
	2016	38.3	3
	<b>2017</b>	<b>39.3</b>	<b>3</b>



# EPFL Hydro today : CH

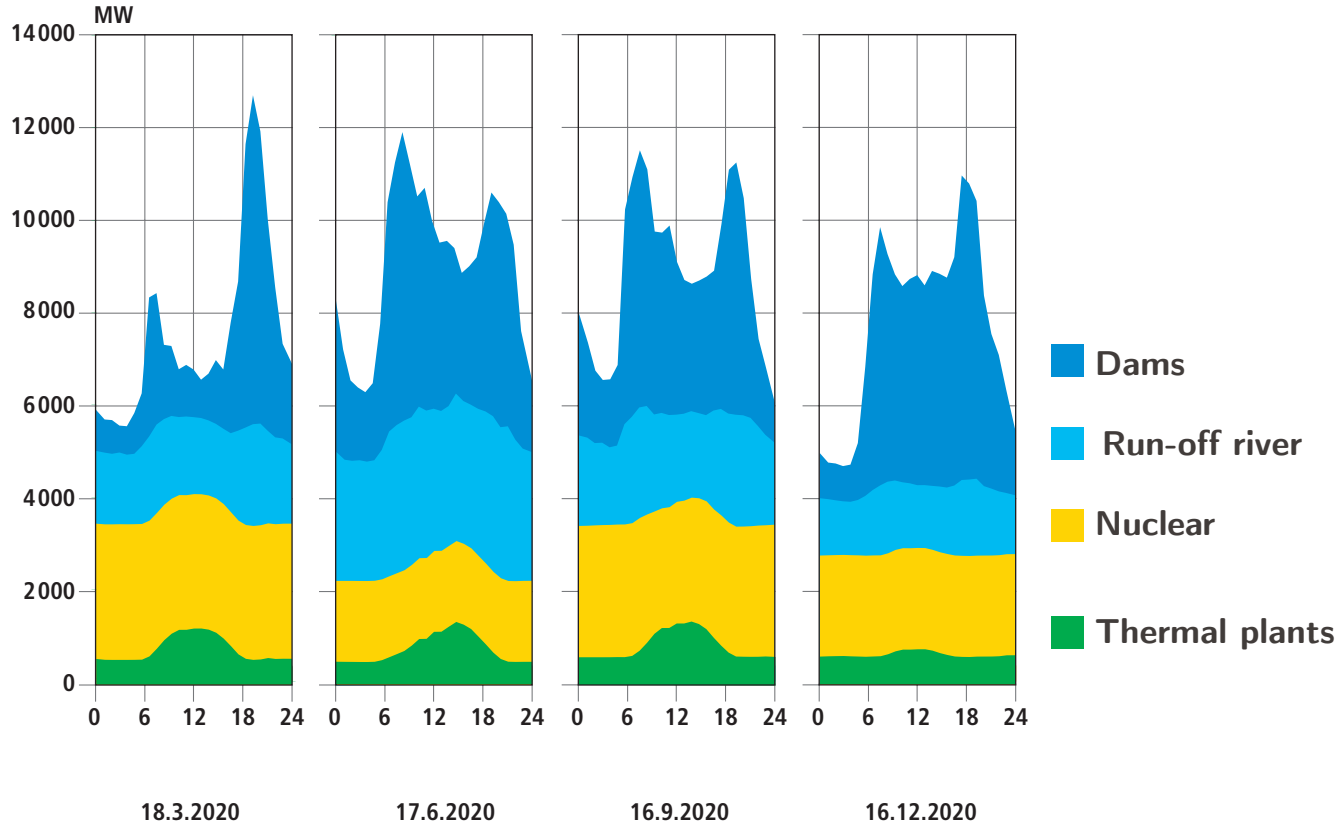
- Swiss electricity hydro production: 35 TWh<sub>e</sub>/y
  - ~60% of Swiss gross electricity production
- Of which hydro: (2024)
  - Dams (47.5%): 16.6 TWh/y
  - Rivers (48.4%): 17 TWh/y
  - Pumped Hydro(4.1%): 1.4 TWh/y



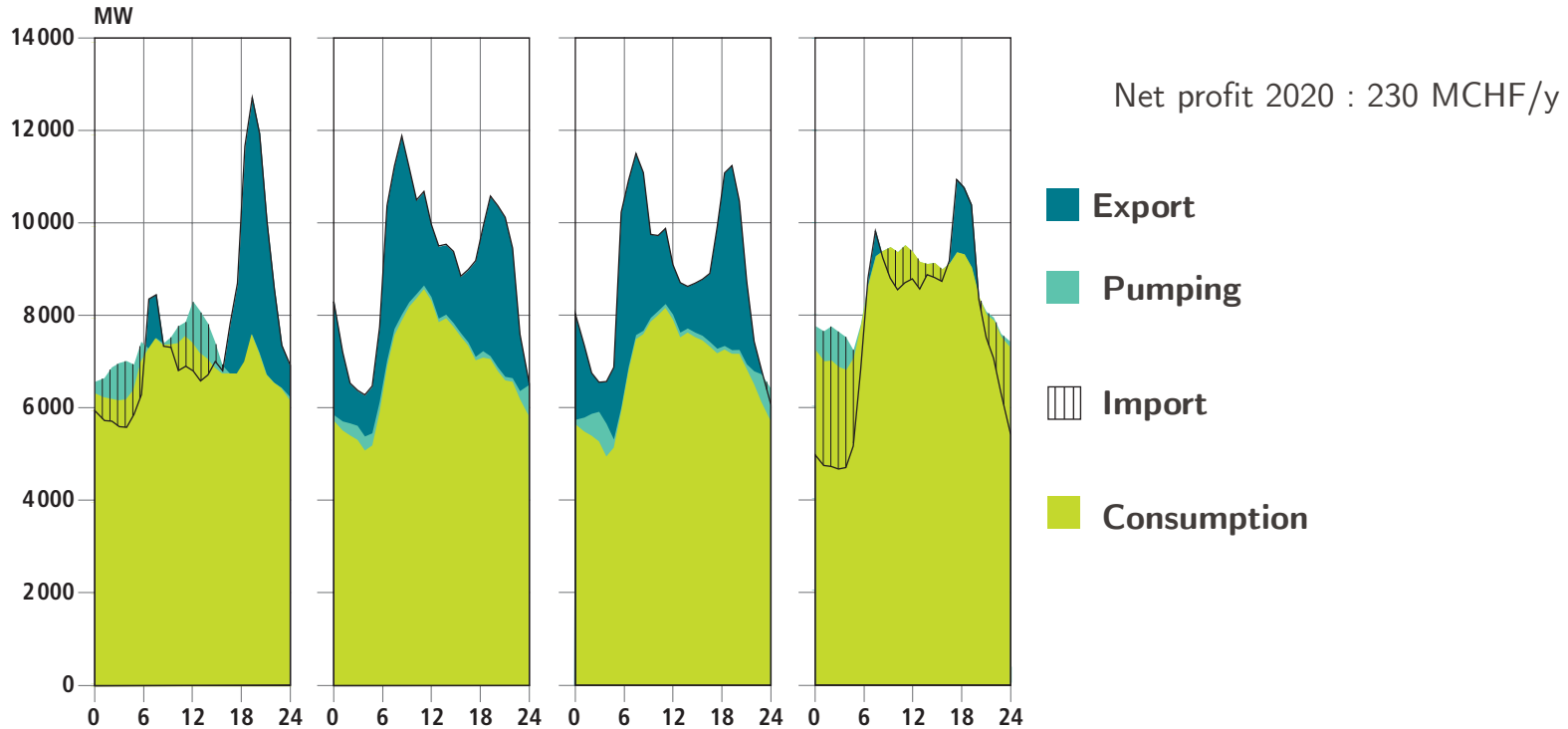
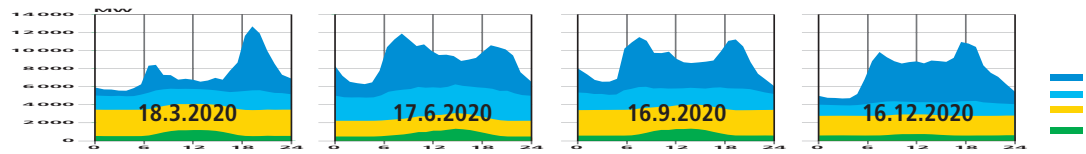
Environ 48,4 % sont générés par des centrales au fil de l'eau, 47,5 % par des centrales à accumulation, et 4,1 % par des centrales à pompage-turbine.

# EPFL Role of Hydro Power in the electricity in CH : following the demand

Fig. 17 Belastungsverlauf am 3. Mittwoch des Monats: Erzeugung (oben), Verbrauch (unten)  
Diagramme de la puissance/charge le 3<sup>e</sup> mercredi du mois: production (en haut), conso



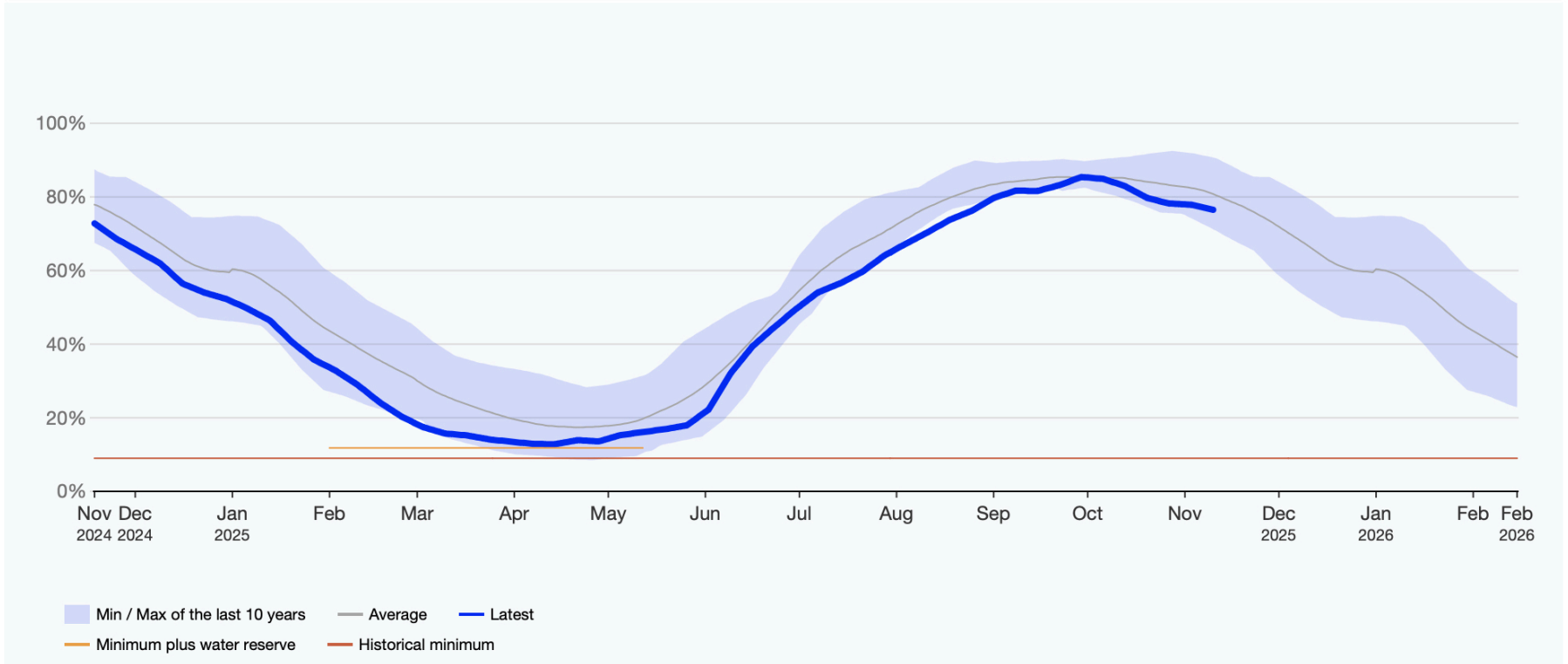
# EPFL Role of Hydro Power in the electricity in CH : following the market



<https://energiedashboard.admin.ch/strom/fuellstaende-speicherseen>

# hydropower reserve

Weekly updates - Status Nov 10, 2025



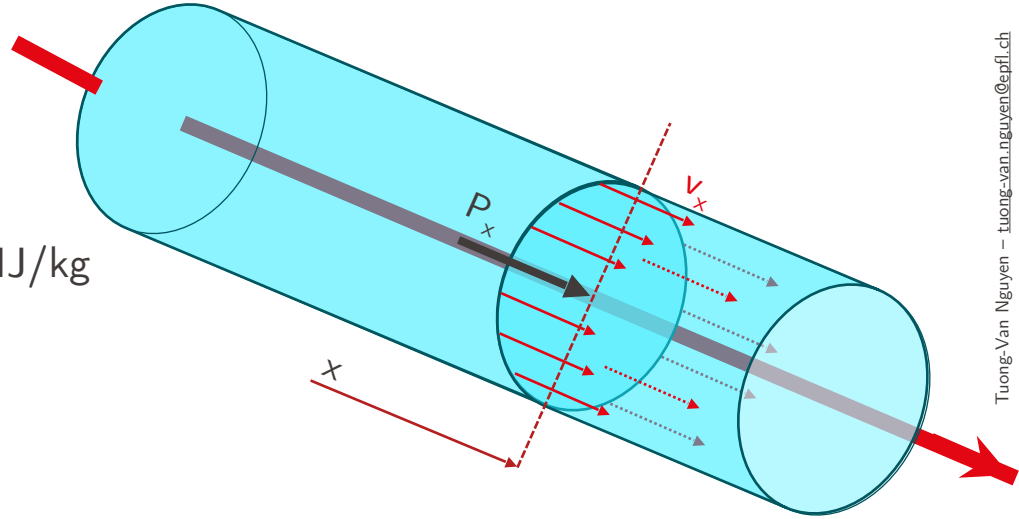


# Physics of hydro

# Physics of hydro

## Key equations

- Low energy density resource:
  - Water @ 100m height: 0.001 MJ/kg
  - Natural gas: 45-50 MJ/kg



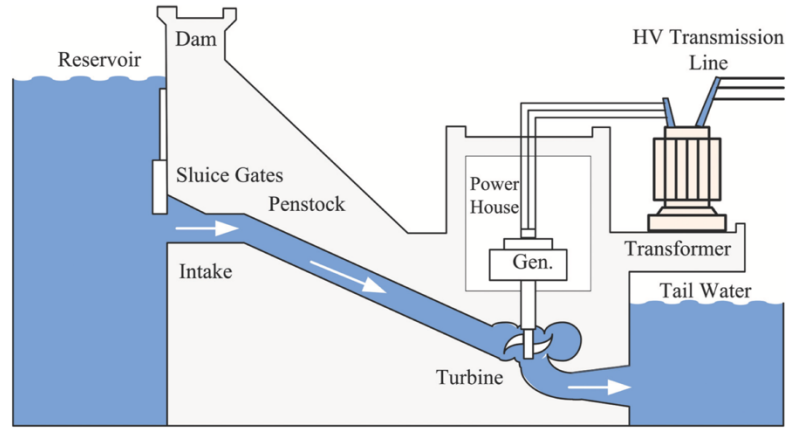
- Basic equations for a water flow:

- Bernoulli at  $x \rightarrow$  specific enthalpy [J/kg] 
$$gH_x = gz_x + \frac{P_x}{\rho} + \frac{v_x^2}{2}$$
- Discharge (flow rate) [m<sup>3</sup>/s]: 
$$Q = \int_A \vec{v} \cdot \vec{n} dA = v_x A$$
- Power [W]: 
$$\dot{E} = \rho v_x A g H_x$$

# Physics of hydro

## Energy balance

- Schematics of a power station:
  - $z_U$ : level of the upper reservoir [m]
  - $z_L$ : level of the lower reservoir [m]
  - 1: entry of the turbine
  - 2: exit of the turbine



1. High energy side (head water):

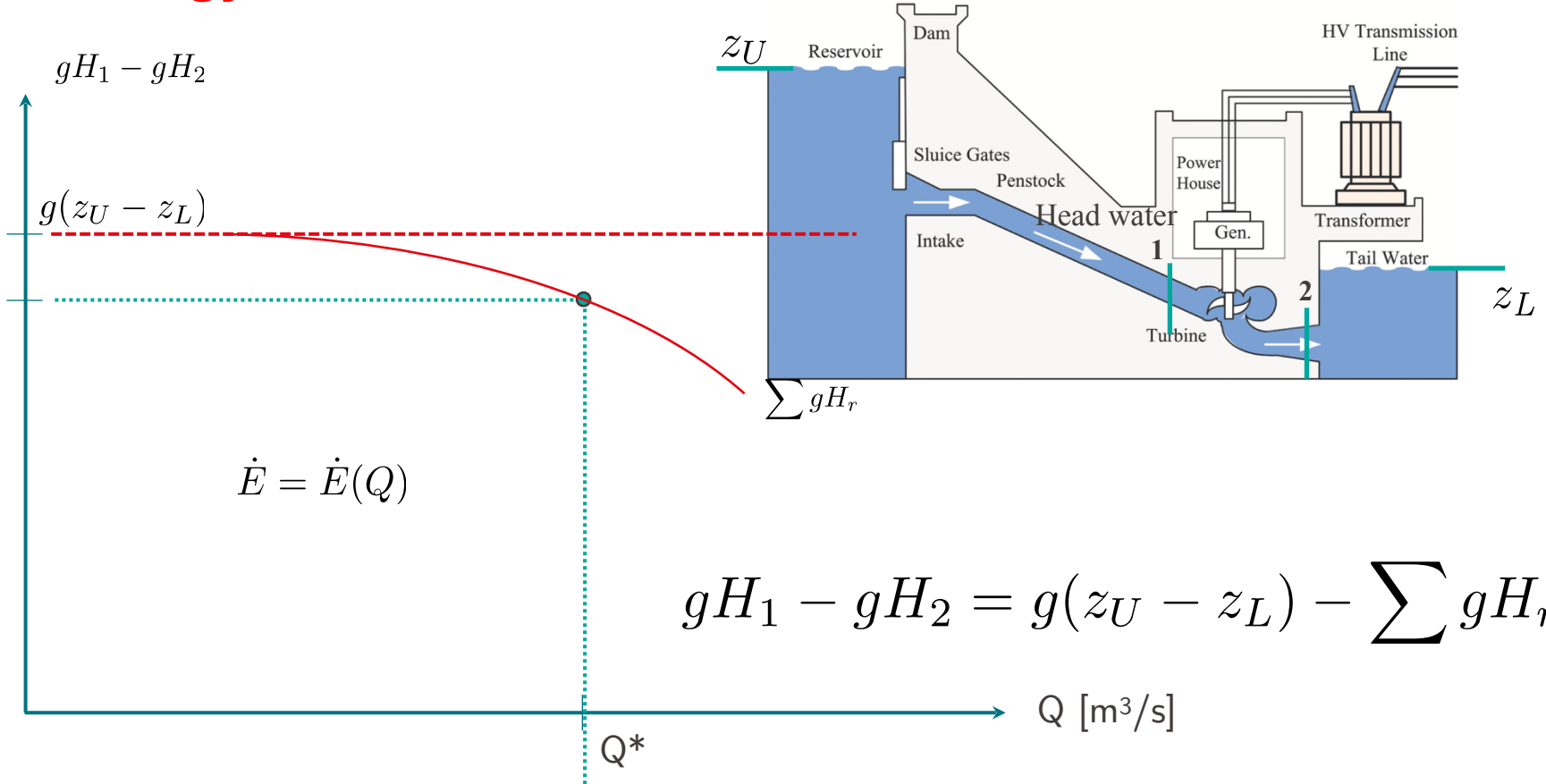
$$gH_U = \frac{P_{atm}}{\rho} + gz_U + 0 = gH_1 + \sum_{\text{Head side}} gH_r$$

2. Low energy side (tail water):

$$gH_L = \frac{P_{atm}}{\rho} + gz_L + 0 = gH_2 + \sum_{\text{Tail side}} gH_r$$

# EPFL Physics of hydro

## Energy balance



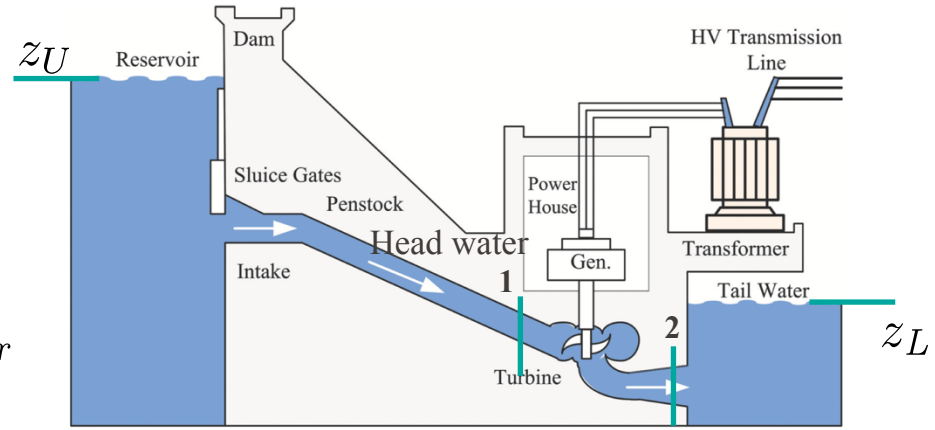
# EPFL Physics of hydro

## Energy balance

- At the turbine:

$$\begin{aligned}
 e_{12} &= gH_1 - gH_2 = g(z_U - z_L) - \sum gH_r \\
 &= \underbrace{\left( \cancel{gz_1} + \frac{P_1}{\rho} \right)}_{e_p \text{ potential}} - \underbrace{\left( \cancel{gz_2} + \frac{P_2}{\rho} \right)}_{e_k \text{ kinetic}} + \frac{1}{2}(v_1^2 - v_2^2) - e_{loss}
 \end{aligned}$$

- Degree of reaction:  $\tau_r = \frac{e_p}{e_{12}}$



# Physics of hydro

## Buckingham theorem

- “if there is a physically meaningful equation involving a certain number  $n$  of physical variables, then the original equation can be rewritten in terms of a set of  $p = n - k$  **dimensionless** parameters  $\pi_1, \pi_2, \dots, \pi_p$  constructed from the original variables [ $k = \#$  independent dimensions.]”
  - e.g. for  $t$  (time),  $d$  (distance),  $v$  (speed):  $n = 3$ ;  $k = 2$  ([m], [s]);  $p = 1 \rightarrow \pi = t*v/d$ .
- Dimensionless quantities are fundamental in engineering as they allow studying systems in lower scales  $\rightarrow$  **similarity**
- The **specific speed** is a dimensionless quantity which summarizes the essential characteristics of a water turbine:

$$v = \frac{\omega Q^{\frac{1}{2}}}{\pi^{\frac{1}{2}} (2e)^{\frac{3}{4}}}$$

Angular speed [rad/s]  $\leftarrow$

Discharge [m<sup>3</sup>/s]  $\nearrow$

Specific energy available at the turbine [J/kg]  $\rightarrow$  depends on the head [m]

# EPFL Physics of hydro

■ ME-409 ENERGY CONVERSION AND RENEWABLE ENERGY




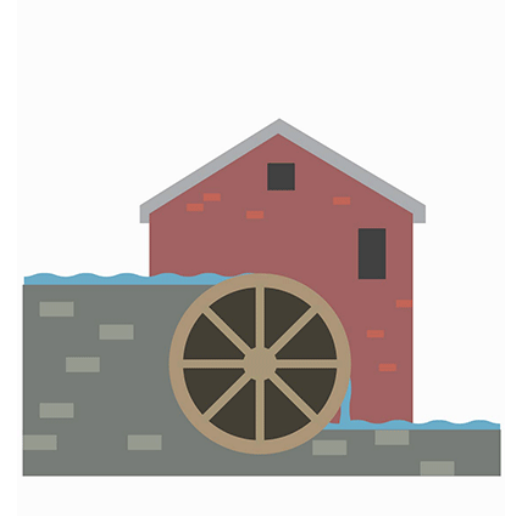


# Hydraulic turbines

# Hydraulic turbines

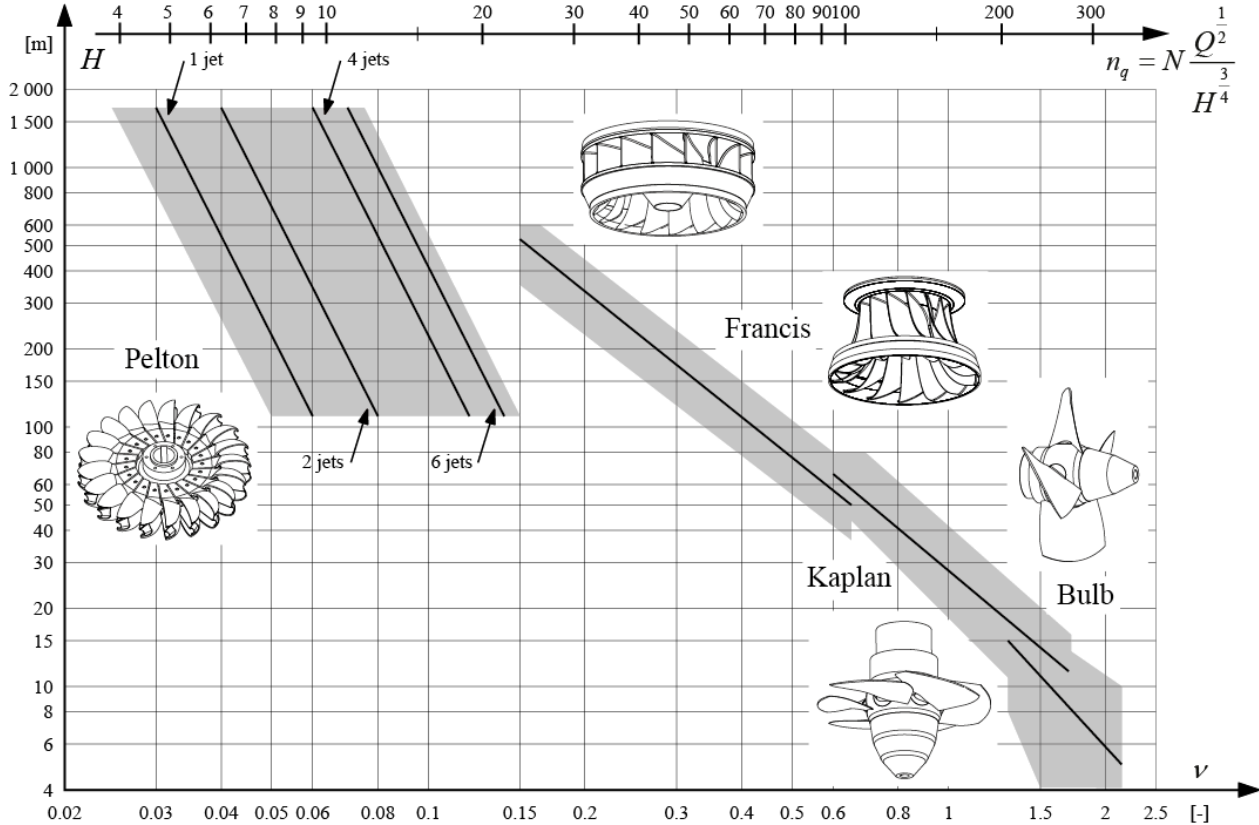
## Classification

$$e_{12} = \underbrace{\left(\frac{P_1}{\rho} - \frac{P_2}{\rho}\right)}_{\text{displacement}} + \underbrace{\frac{1}{2}(v_1^2 - v_2^2)}_{\text{impulse}} + \underbrace{g(z_1 - z_2)}_{\text{water wheels}} - e_{loss}$$




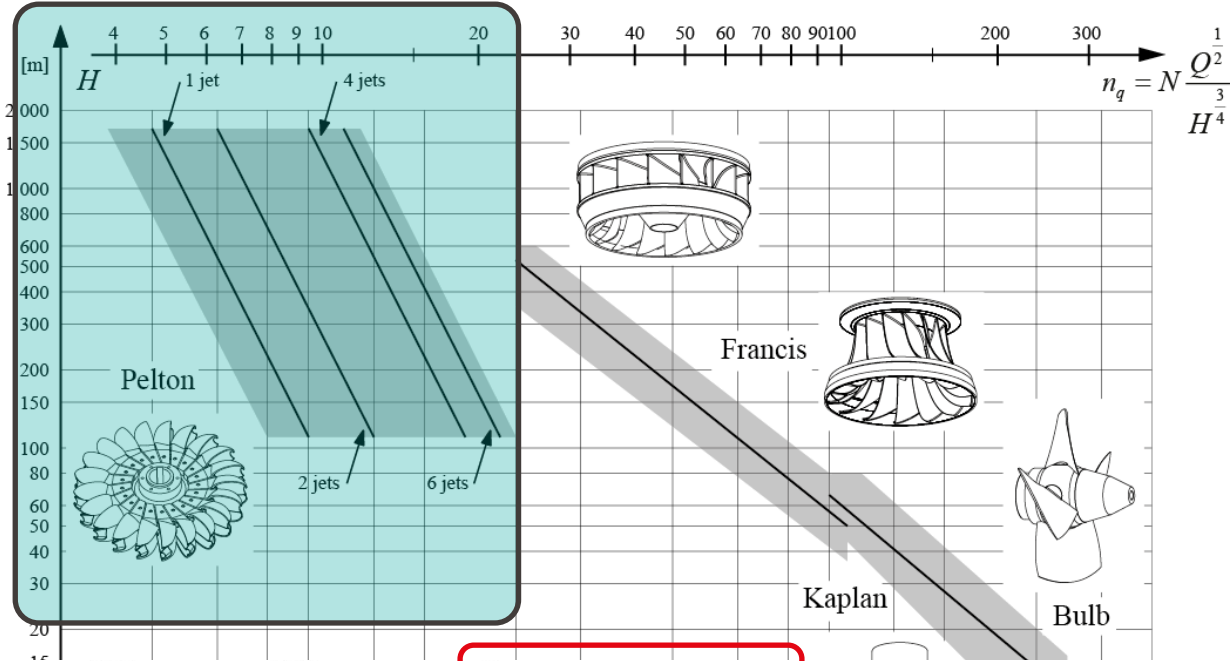
# Hydraulic turbines

## Classification



# Hydraulic turbines

## Classification Pelton turbines

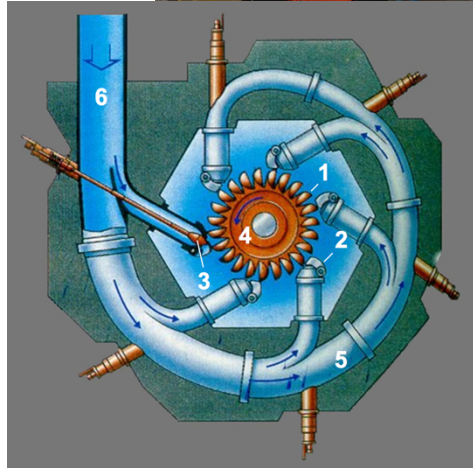


$$e_{12} = \left( \frac{P_1}{\rho} - \frac{P_2}{\rho} \right) + \frac{1}{2} (v_1^2 - v_2^2) + g(z_1 - z_2) - e_{loss}$$

# Hydraulic turbine

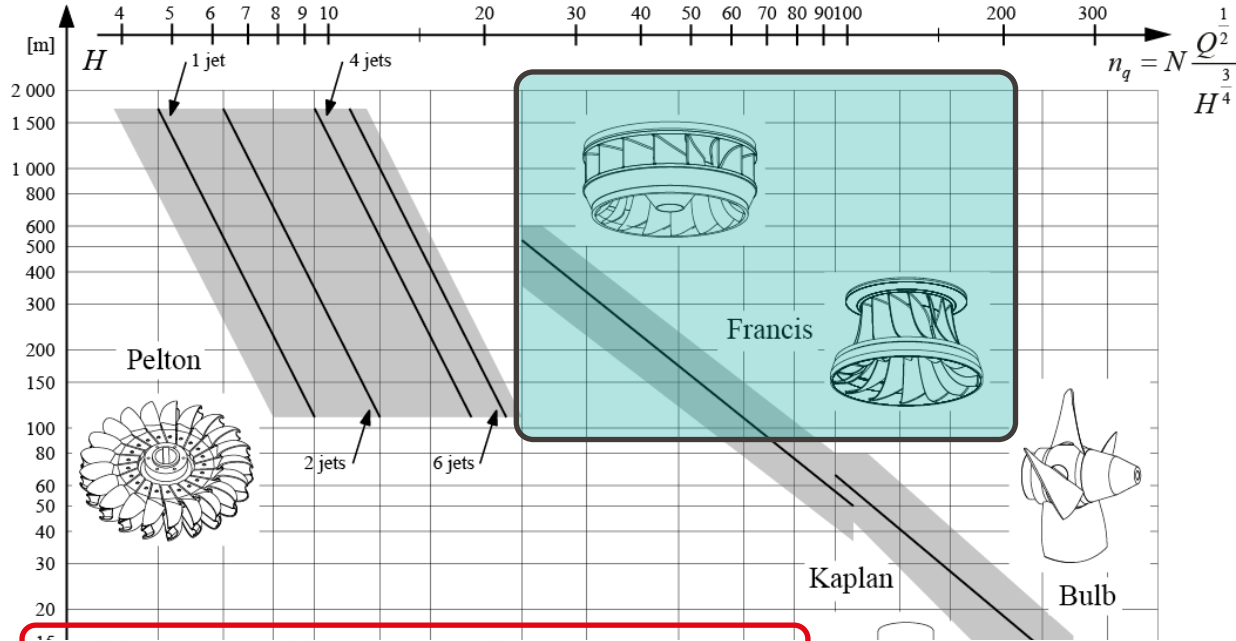
## Pelton

- High head, low discharge
- Impulse/action turbine (only speed)
- Head: 300-2000m
- Power up to  $\sim 400 \text{ MW}_e$
- Efficiency up to 92%



# Hydraulic turbines

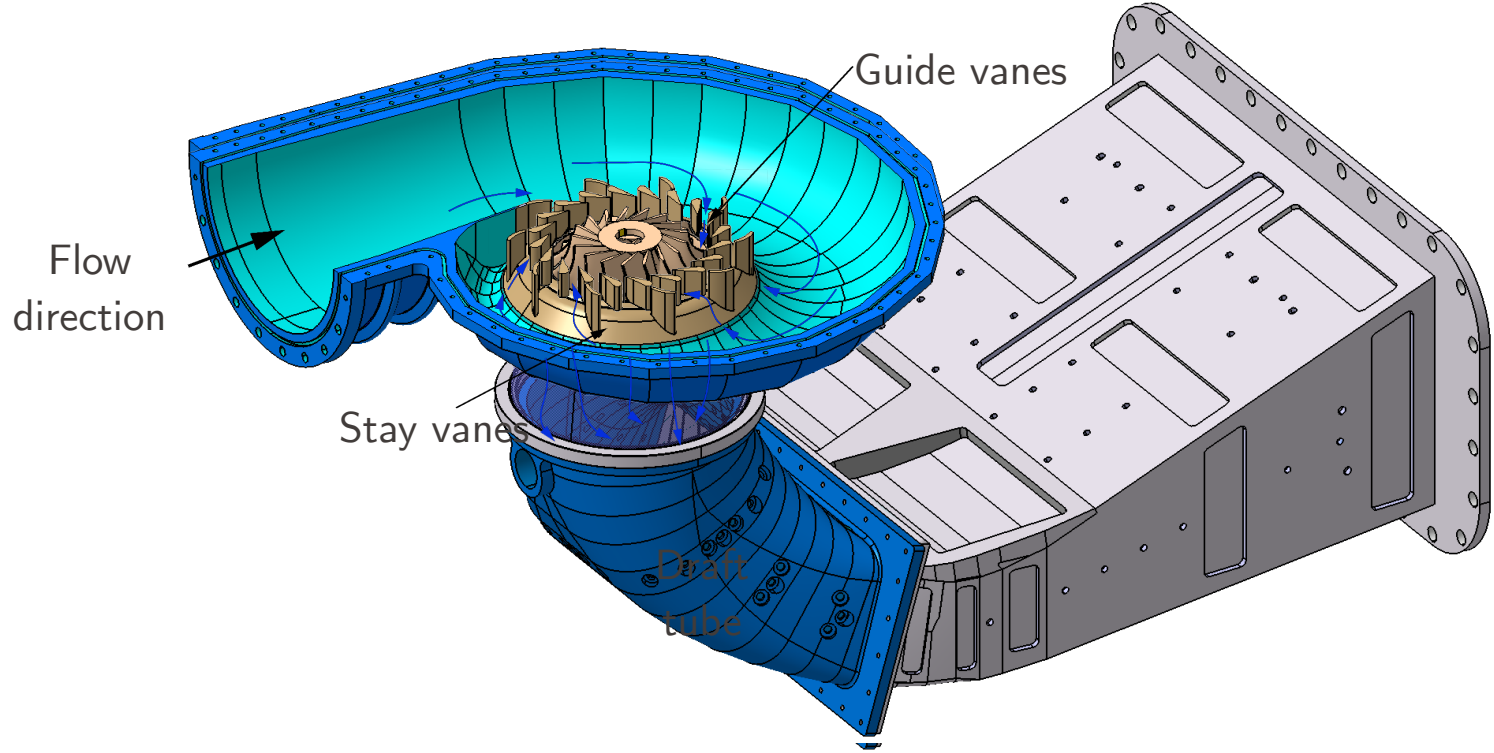
## Classification : Francis turbines



$$e_{12} = \left( \frac{P_1}{\rho} - \frac{P_2}{\rho} \right) + \frac{1}{2} (v_1^2 - v_2^2) + g(z_1 - z_2) - e_{loss}$$

# Hydraulic turbines

## Francis



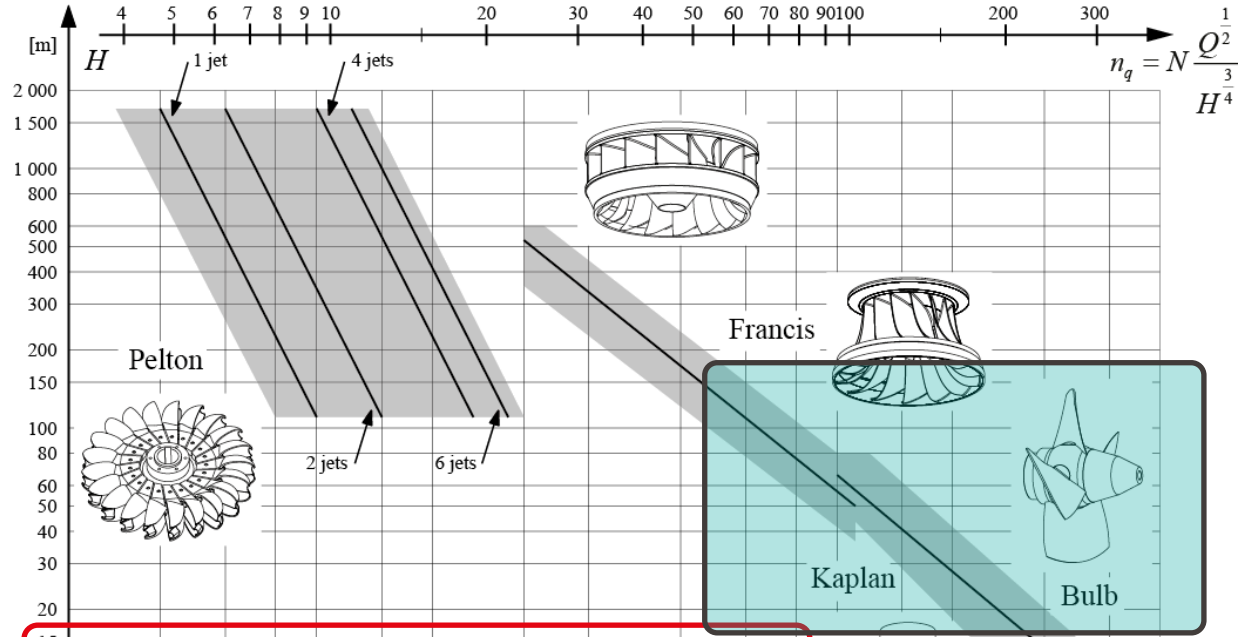
# Hydraulic turbines

## Francis

- Most used and versatile turbine:  
~60% of capacity worldwide
- Reaction turbine
- Medium heads: 40-600m
- Wheel diameters: 0.6-8m
- High efficiency: 96-97%
- Three Gorges dam (China):  
Biggest power plant worldwide  
Total capacity: 22.5 GW<sub>e</sub>
- Itaipu (Brazil):  
20\*700 MW = 14 GW  
103.1 TWh/y (record 2016)



## Classification Kaplan and Bulb turbines



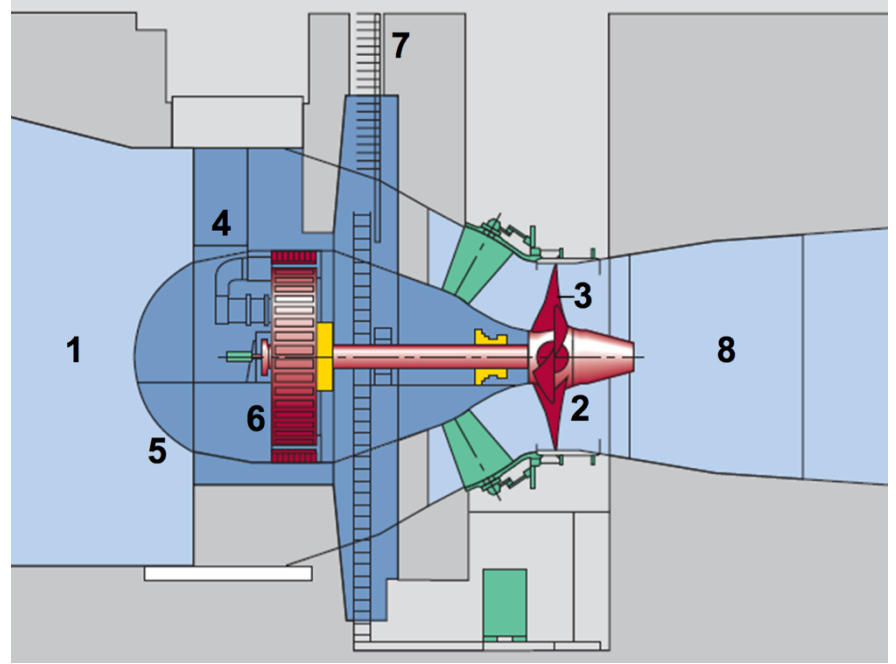
$$e_{12} = \left( \frac{P_1}{\rho} - \frac{P_2}{\rho} \right) + \frac{1}{2} (v_1^2 - v_2^2) + g(z_1 - z_2) - e_{loss}$$



# EPFL Hydraulic turbines

## Bulb turbines

- 1930s: evolution of the Kaplan turbine
- Axial flow → higher efficiencies
- Compact design
- Lower costs



# Efficiency of turbine

$$\dot{E} = \dot{m} \cdot w_{12} \cdot \eta_T \cdot \eta_{gen} \cdot \eta_{gear} \cdot \eta_{transfo}$$

$\eta_T = 92\%$  Mechanical efficiency of the turbine

$\eta_{gear} = 98\%$  Efficiency of the gear box

$\eta_{gen} = 97\%$  Efficiency of the generator

$\eta_{transfo} = 98\%$  Efficiency of the transformer

$\eta_{total} = 86\%$  Overall efficiency to grid

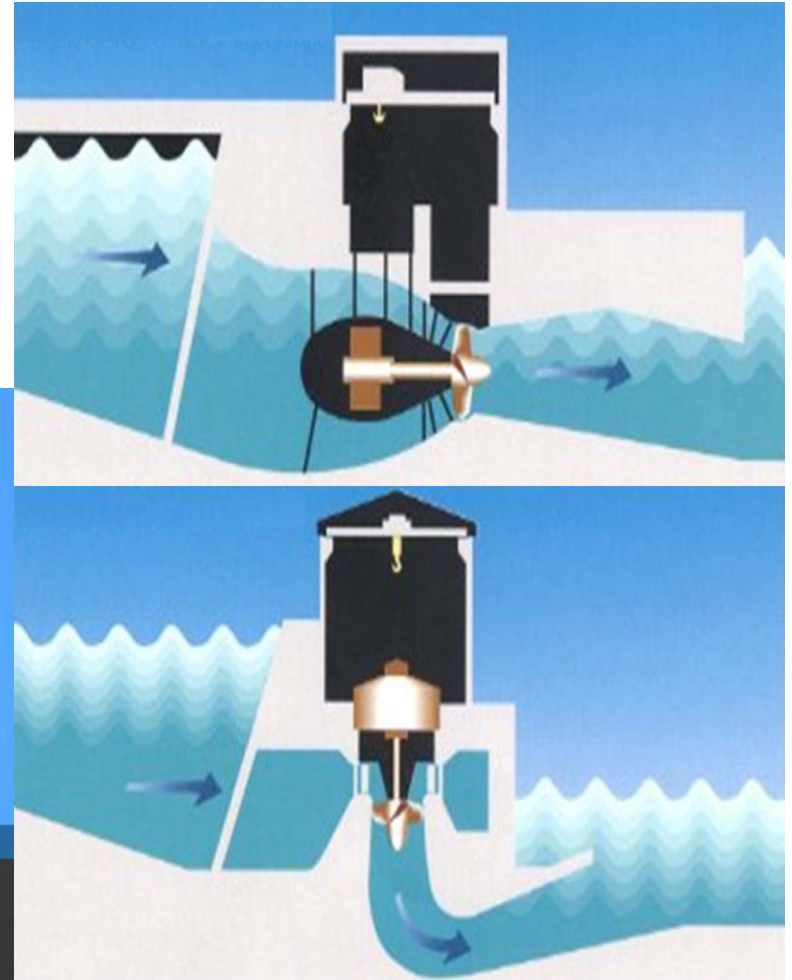
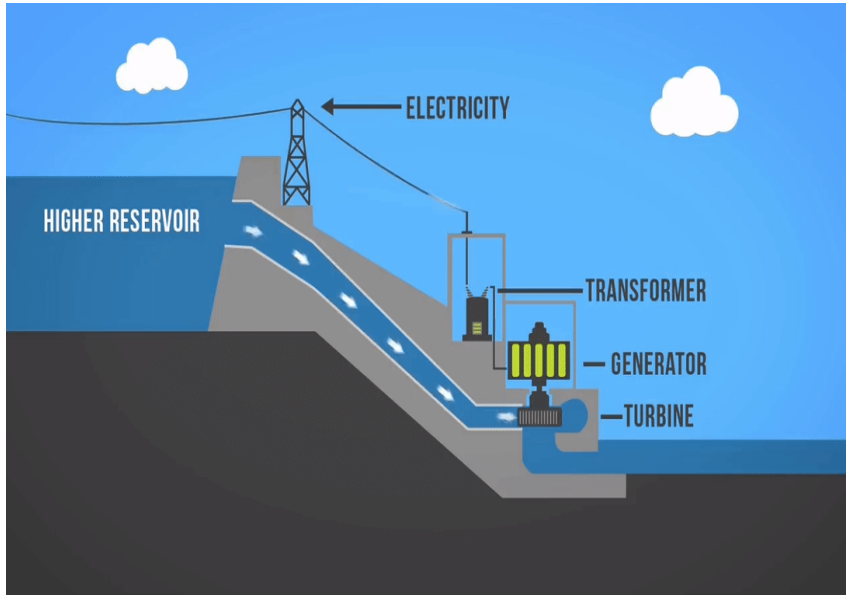


# Hydro and energy systems

# Hydro and energy systems

## Hydroelectric schemes

- Storage and run-of-river power plants



# Hydro and energy systems

## Costs

- Costs are quite project specific: 1050-7650 USD/kW<sub>e</sub> for large projects
- LCOE @  $c_p = 50\%$ : 28-90 USD/MWh<sub>e</sub> → very competitive!

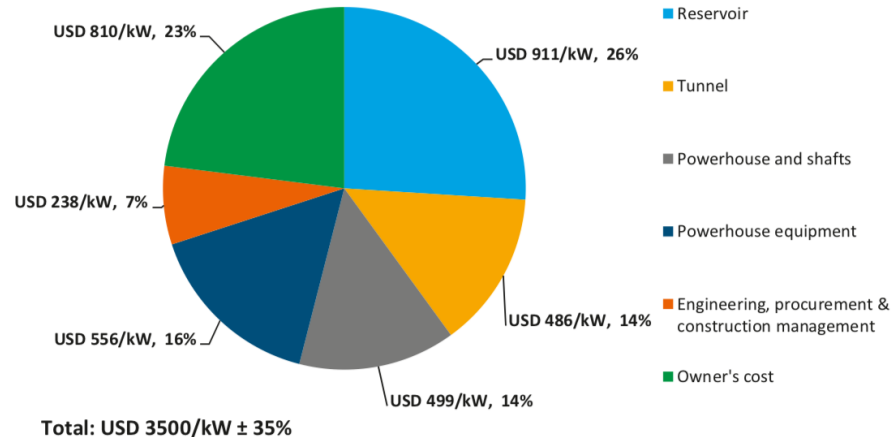
LCOE (USD/MWh)	Weighted average capital cost or discount rate			
		8%	10%	12%
Load factor	25%	90	110	133
	50%	41	51	61
	75%	28	34	41

LCOE assuming 1500 USD/kW, O&M 2.5% of  $c_{inv}$ , 5y construction, 50y lifetime

# Hydro and energy systems

## Costs

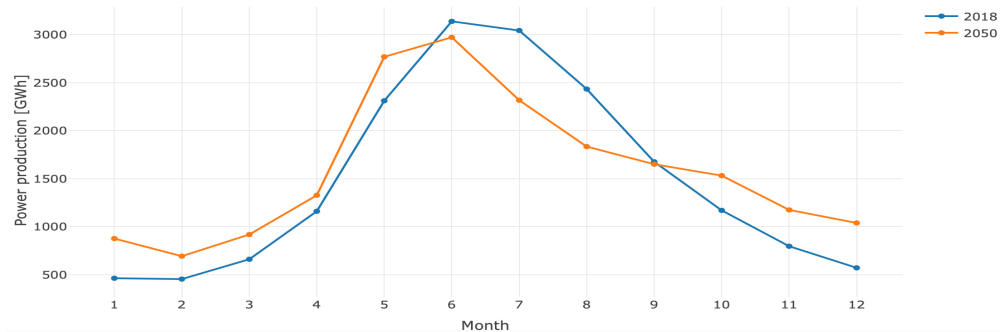
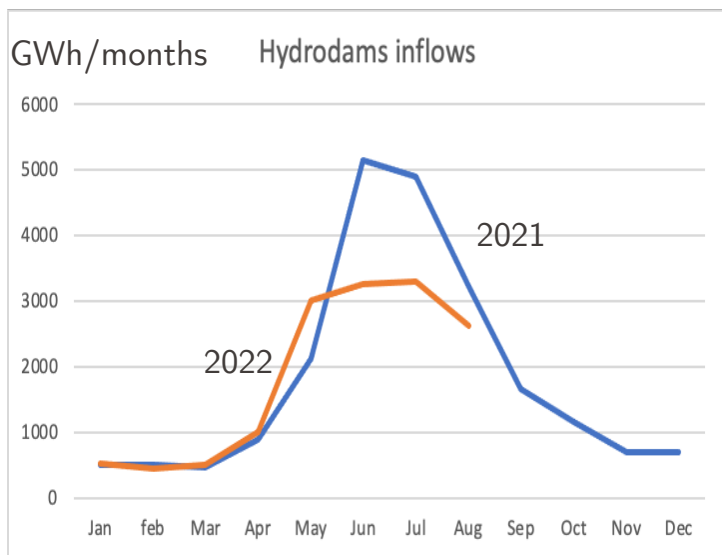
- Costs are quite project specific: 1050-7650 USD/kW<sub>e</sub> for large projects
- LCOE @ c<sub>p</sub> = 50%: 28-90 USD/MWh<sub>e</sub> → very competitive!



# EPFL Impact of climate change/meteo

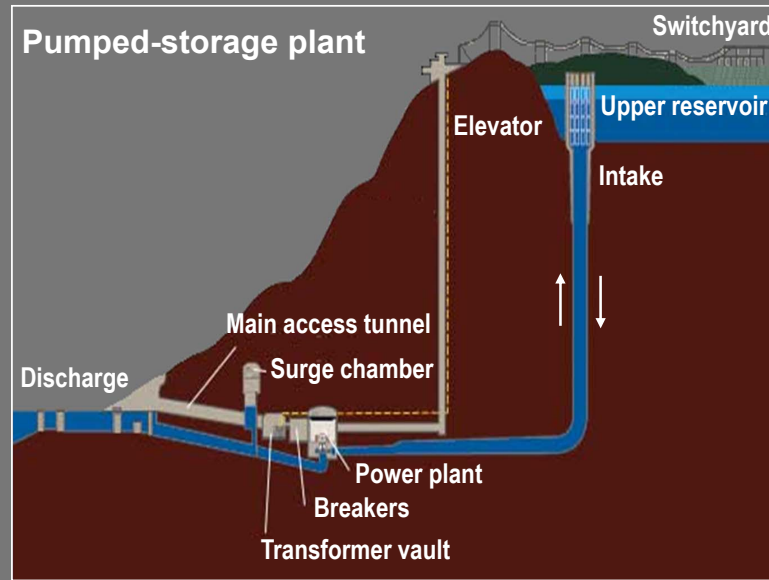
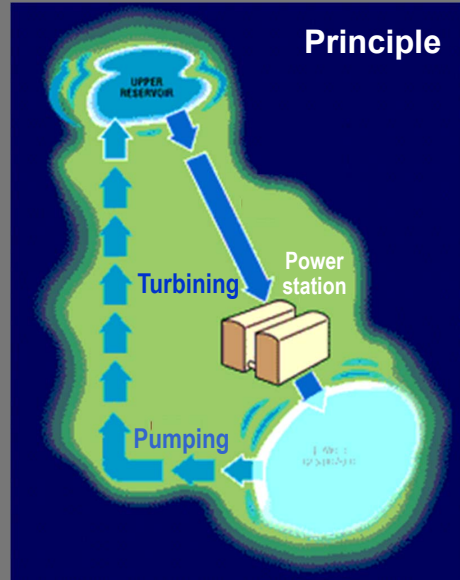
- Glaciers are losing 1 GT/year (2%) of ice (transformed in power)
- Temperatures will influence storage in snow and precipitation

Inflow of water in dams Switzerland [GWh/month]



## Hydro-electric schemes

### Pumped storage

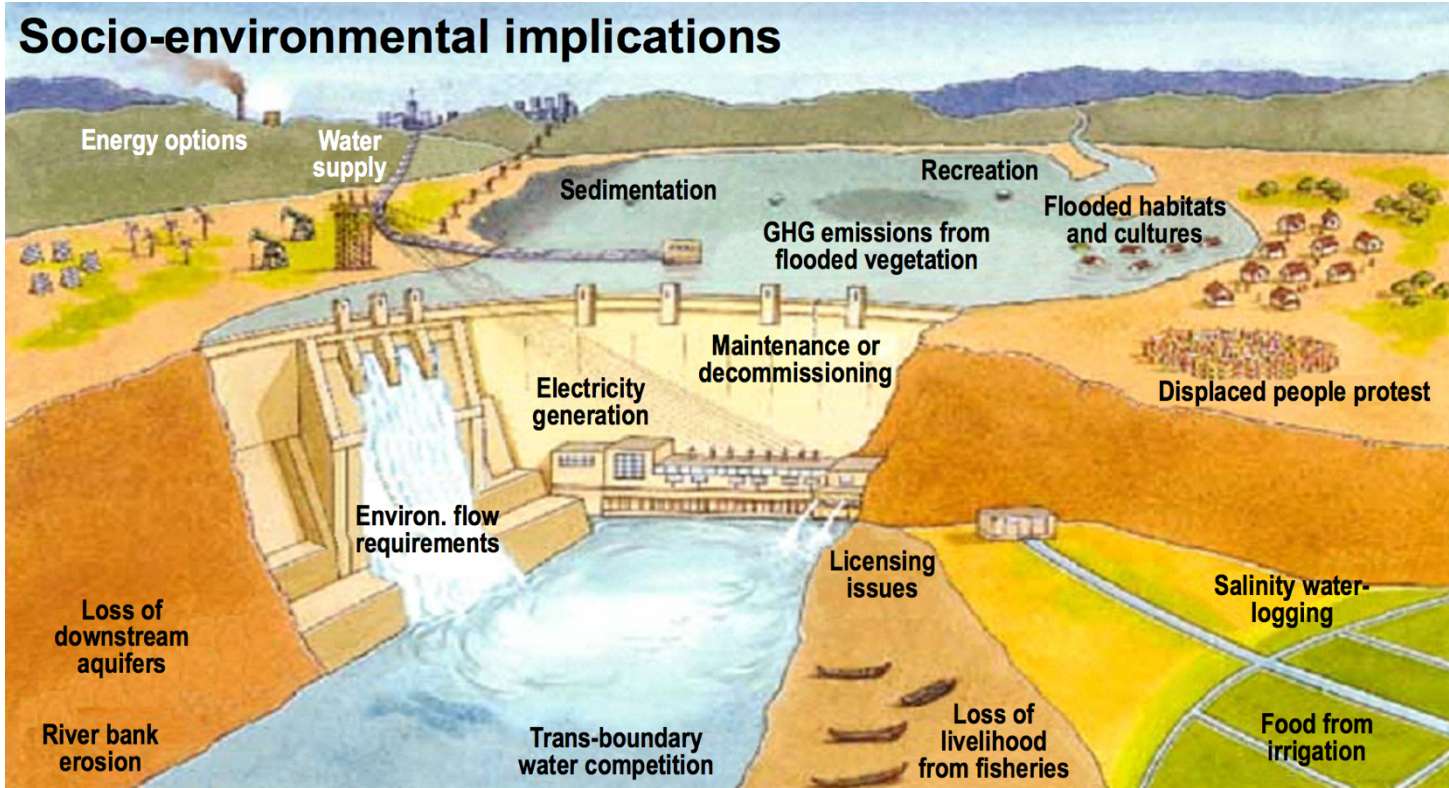


$$\eta_{RoundTrip} = \frac{E^{out}}{E^{in}}$$

Round trip efficiency = 80%

# Hydro and energy systems

## Impacts



# EPFL Hydro dams : land occupation & people displacement

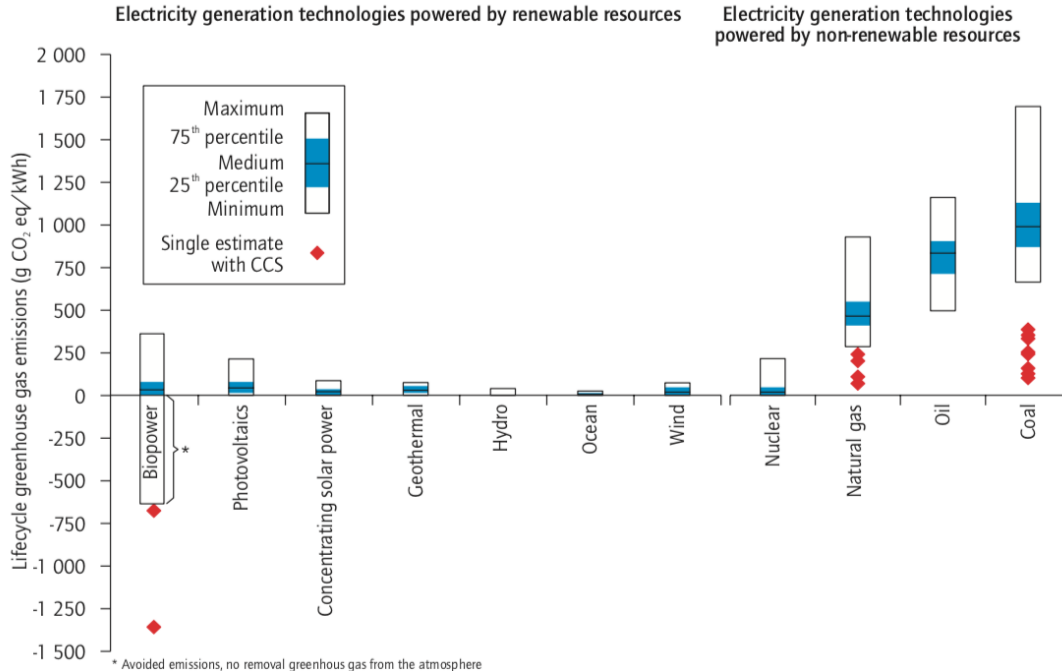
- China : about 15 to 20 Million people relocated

- Land occupation source wikipedia

Name	Country	Dam	Outflow	Surface area		Ref	Image
				km <sup>2</sup>	mi <sup>2</sup>		
Lake Victoria <sup>[n 1]</sup>	 Kenya Tanzania Uganda	Owen Falls Dam	White Nile	66,400	25,600	[1]	
Irkutsk Reservoir– Lake Baikal <sup>[n 2]</sup>	 Russia	Irkutsk Dam	Angara River	32,000	12,000	[2]	
Lake Winnipeg <sup>[n 3]</sup>	 Canada	Jenpeg Dam	Nelson River	24,420	9,430	[3]	
Lake Volta	 Ghana	Akosombo Dam	Volta River	8,500	3,300	[4]	
Smallwood Reservoir	 Canada	Multiple	Churchill River	6,527	2,520	[5]	
Reindeer Lake <sup>[n 4]</sup>	 Canada	Whitesand Dam	Reindeer River	6,500	2,500	[6]	
Kuybyshev Reservoir	 Russia	Zhiguli Dam	Volga River	6,450	2,490		
Lake Kariba	 Zambia Zimbabwe	Kariba Dam	Zambezi River	5,580	2,150	[7]	
Bukhtarma Reservoir <sup>[n 5]</sup>	 Kazakhstan	Bukhtarma Dam	Irtys River	5,490	2,120	[8]	
Bratsk Reservoir	 Russia	Bratsk Dam	Angara River	5,470	2,110	[9]	



Figure 13: Estimates of lifecycle GHG emissions in electricity generation (excluding land-use changes)



Count of estimates	222 (+4)	124	42	8	28	10	126	125	83 (+7)	24	169 (+12)
Count of references	52 (+0)	26	13	6	11	5	49	32	36 (+4)	10	50 (+10)

# Hydro and energy systems

## Impacts : fatalities

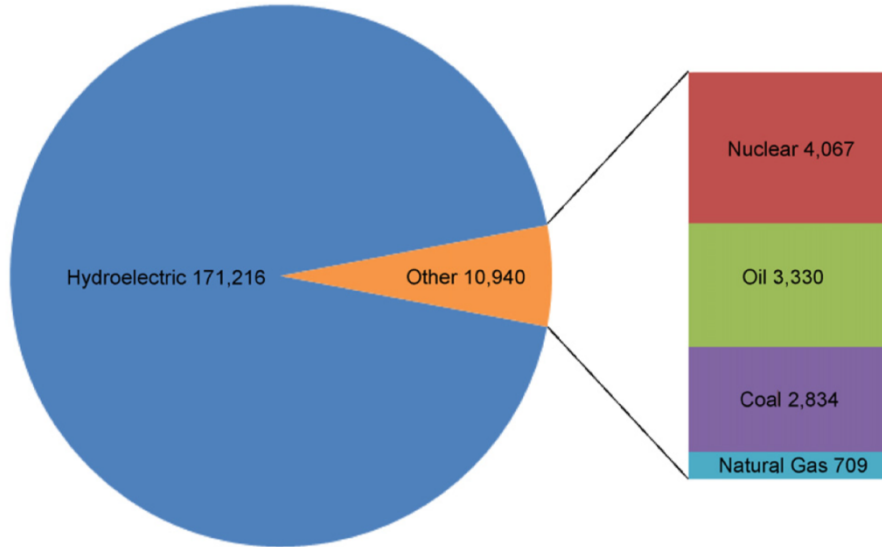


Fig. 1. Energy accident fatalities by source, 1907–2007.

Energy Source	[deaths/ PWh]
Coal – global average	100000
Coal – China	170000
Coal – U.S.	10000
Oil	36000
Natural Gas	4000
Biofuel/Biomass	24000
Solar (rooftop)	440
Wind	150
Hydro – global average	1400
Hydro – U.S.	5
Nuclear – global average	90
Nuclear – U.S.	0.1



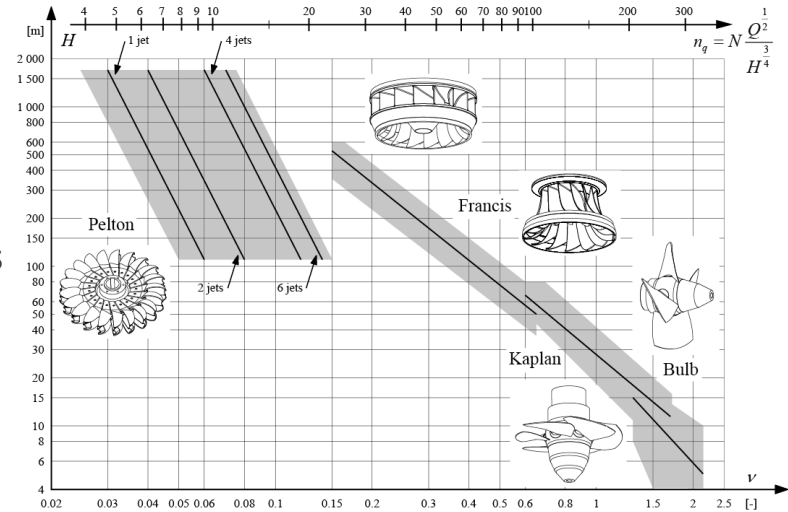
# Take-home message

# Take-home message

- In general
  - Hydro most developed renewable
  - Key resource in CH
  - Run-of-river & storage power plants
- Physics
  - Specific energy depends on **head** [m]
  - Total power depends on head & **discharge**
  - **Specific speed  $v$**  to characterize turbines
- Hydraulic turbines
  - **Pelton**: high head, low discharge
  - **Francis** (60%): medium head/discharge
  - **Kaplan/Bulb**: low head, high discharge
- Energy system integration
  - Competitive for cost/GHG

$$gH_1 - gH_2 = g(z_U - z_L) - \sum gH_r$$

$$v = \frac{\omega Q^{\frac{1}{2}}}{\pi^{\frac{1}{2}} (2e)^{\frac{3}{4}}} \quad \dot{E} = \rho v_x A g H_x$$



# Questions?

Prof. François  
Maréchal