

# Wind energy

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Lausanne – 18/11/2024

# Outline

- Introduction
  - What is wind energy?
  - Wind energy today and future potential
  - The resource
- Physics of wind energy
  - Physics of wind energy: key equations
  - Betz limit
  - Forces: lift and drag
- Wind Turbines & energy systems
  - Types of wind turbines
  - Integration in the energy system
- Take home message



# Introduction

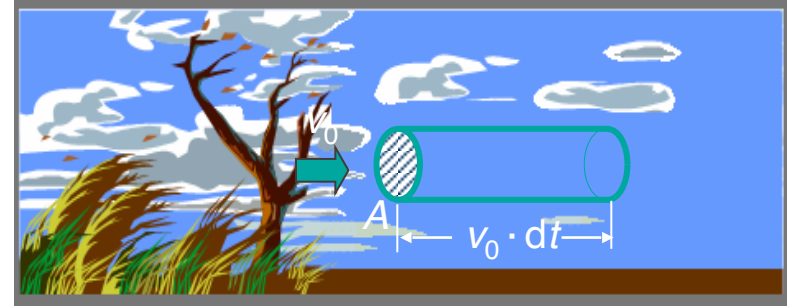
# EPFL What is wind energy?

- Wind can be defined as “air in motion”:
  1. Differences in pressure (pressure gradient force), caused by uneven solar heating on the earth surface
  2. Rotation of the Earth: Coriolis force
  3. Friction close to the Earth surface

- Kinetic energy, power, force
  - Air passing through control volume  $V$  in  $dt$ :
  - Mass flow through an area  $A$ :
  - Kinetic energy contained in the moving air:

- Power: 
$$\dot{E}_{k,air} = \frac{dE_{k,air}}{dt} = \frac{1}{2}\rho Av_0^3$$

- Force (drag): 
$$F_{air} = \frac{\dot{E}_{k,air}}{v_0} = \frac{1}{2}\rho Av_0^2$$



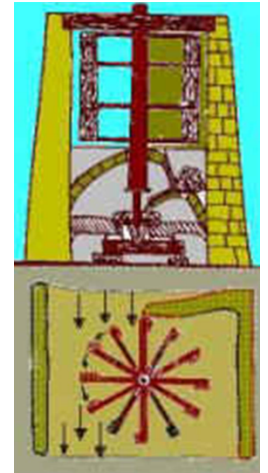
$$E_{k,air} = \frac{1}{2}m_{air}v_0^2 = \frac{1}{2}\rho Av_0^3 dt$$

# EPFL Harvesting wind energy?

- Historically, wind has been used for:
  - ~3000BC: sailboats (Babylonians, Egyptians)
  - ~2000BC: pumping water
  - ~1000AD: milling (Europe)
  - Mechanical work



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# EPFL Harvesting wind energy?

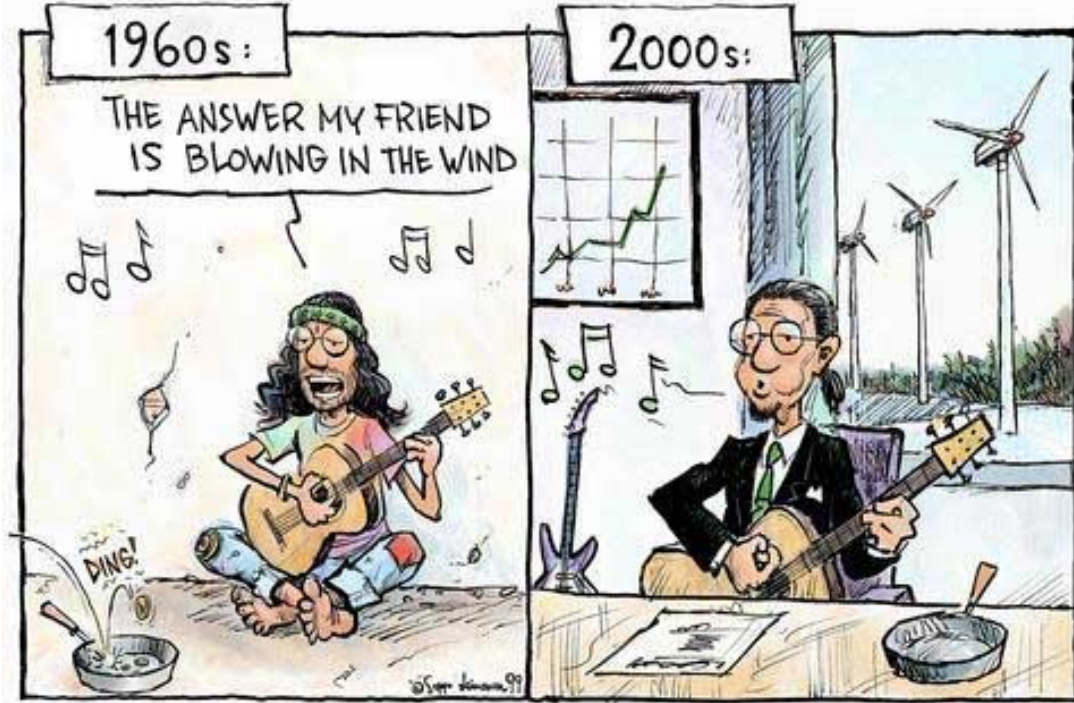


Why wind farms — Search Google

Google Suggestions

- Why wind farms
- why wind farms are bad
- why wind farms are good
- why wind farms are important
- why wind farms are a good idea

# EPFL Harvesting wind energy?

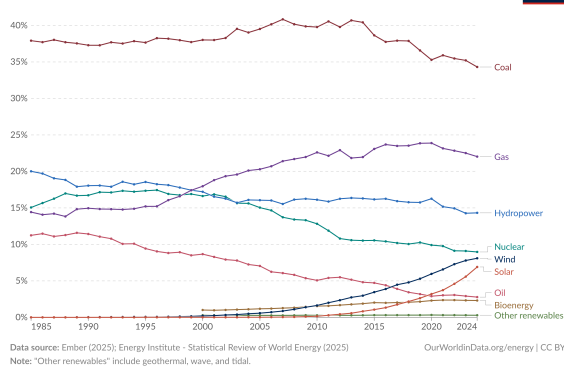


www.seppo.net

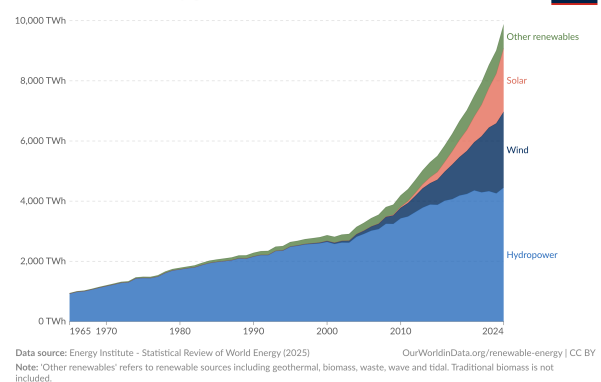
# EPFL Wind energy today

- World Wind capacity installed (2023): 1021 GW
- Wind production 2311 TWh/y (2023) : capacity factor = 25%)
  - 7.8% of world electricity supply
- IIASA, practical potential (onshore): 20'000-100'000 TWh/y
- IEA: 18% of world electricity supply in 2050
- Potential depends on wind speed...

Share of electricity production by source, World



Renewable electricity generation, World

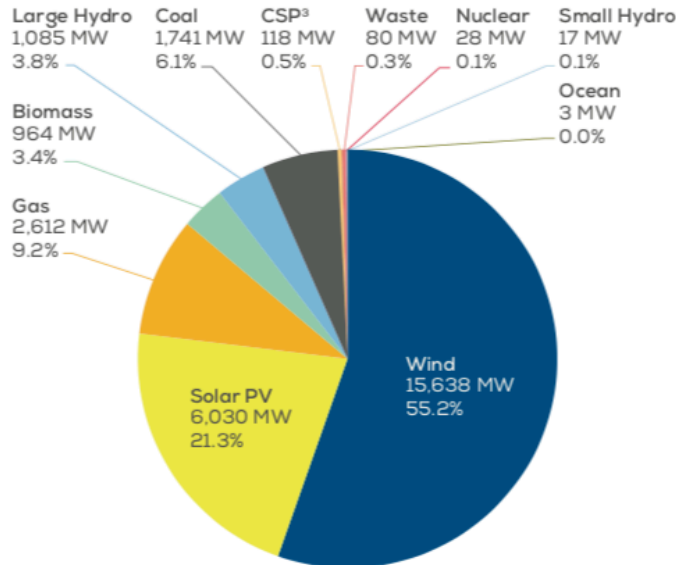


# EPFL Wind energy in Europe

- Total wind capacity in EU: 220 GW<sub>e</sub> (2020), of which 25 GW<sub>e</sub> offshore
- +14 GW<sub>e</sub> /year installed in 2010-2020
- 16% of electricity demand

FIGURE 3

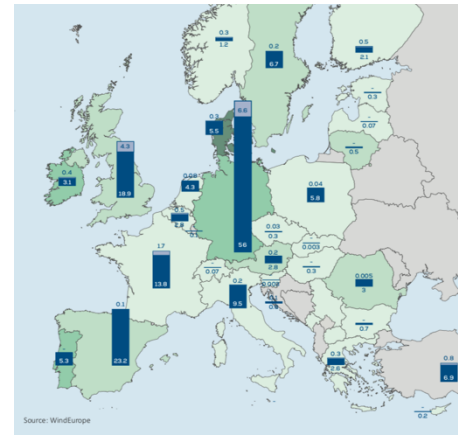
Share of new installed capacity. Total 28,316 MW



48% 38% 27% 27% 25% 22% 20%



Highest wind energy shares

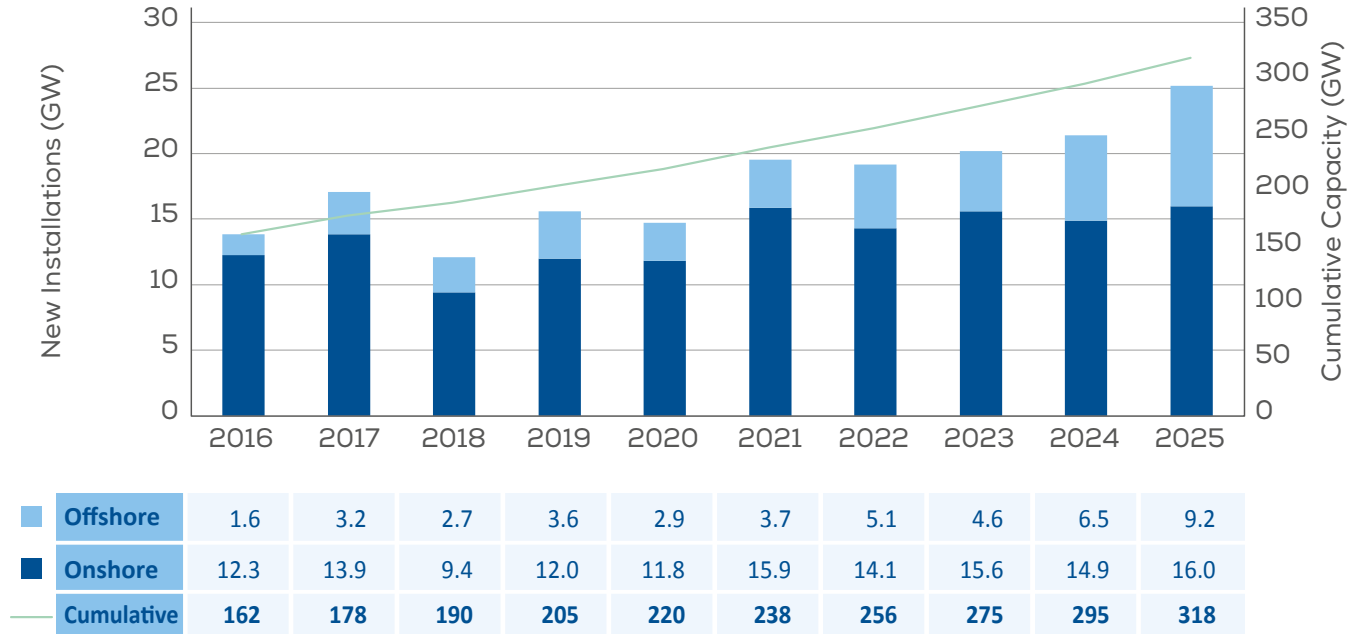


<http://windeurope.org>

# EPFL Wind energy Europe 2021-2025

FIGURE 13

New and total (cumulative) installations in Europe - WindEurope's Realistic Expectations Scenario



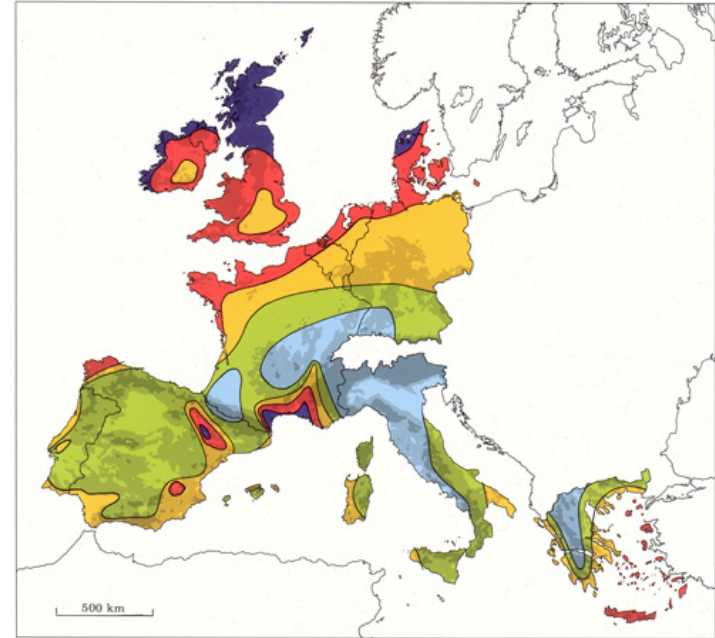
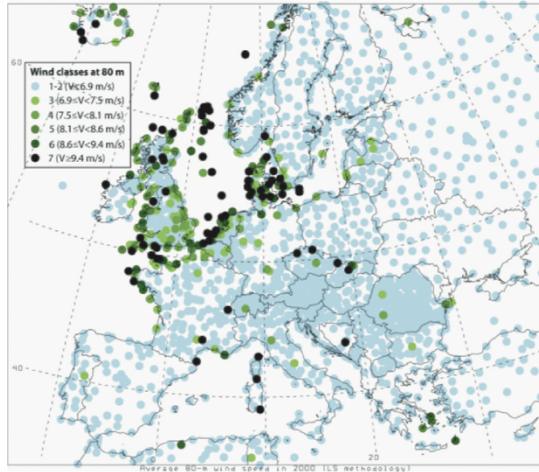
Onshore : 72% of new installations

- Swiss final energy consumption: 207 TWh/y (2020)
- Swiss electricity consumption: 55.5 TWh<sub>e</sub>/y (2020)
- Wind electricity production: 0.17 TWh<sub>e</sub>/y (2020)
  - Only 41 turbines (86.5 MW<sub>e</sub>) installed in CH
  - Target 2050 : 4.3 TWhe/y (2050)
    - ~ 850 Turbines (2400 MWe)



$$\dot{E}_{k,air} = \frac{dE_{k,air}}{dt} = \frac{1}{2} \rho A v_0^3$$

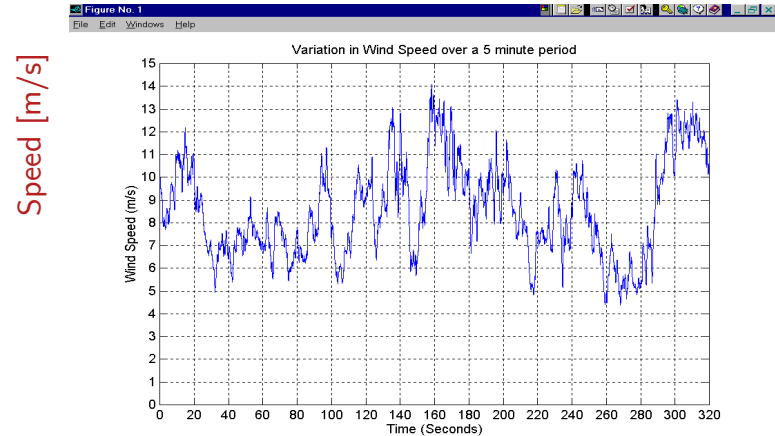
- The main factor is the wind speed!



Wind resources <sup>1</sup> at 50 metres above ground level for five different topographic conditions									
Sheltered terrain <sup>2</sup>		Open plain <sup>3</sup>		At a sea coast <sup>4</sup>		Open sea <sup>5</sup>		Hills and ridges <sup>6</sup>	
m s <sup>-1</sup>	Wm <sup>-2</sup>	m s <sup>-1</sup>	Wm <sup>-2</sup>	m s <sup>-1</sup>	Wm <sup>-2</sup>	m s <sup>-1</sup>	Wm <sup>-2</sup>	m s <sup>-1</sup>	Wm <sup>-2</sup>
> 6.0	> 250	> 7.5	> 500	> 8.5	> 700	> 9.0	> 800	> 11.5	> 1800
5.0-6.0	150-250	6.5-7.5	300-500	7.0-8.5	400-700	8.0-9.0	600-800	10.0-11.5	1200-1800
4.5-5.0	100-150	5.5-6.5	200-300	6.0-7.0	250-400	7.0-8.0	400-600	8.5-10.0	700-1200
3.5-4.5	50-100	4.5-5.5	100-200	5.0-6.0	150-250	5.5-7.0	200-400	7.0- 8.5	400- 700
< 3.5	< 50	< 4.5	< 100	< 5.0	< 150	< 5.5	< 200	< 7.0	< 400

Source: Risø DTU National Laboratory, Denmark

- To be able to predict the performance of a wind turbine at a particular site the developer must know the characteristics (**speed** and **direction**) of the resource at the location in question
- Speed variation and time scales:
  1. Yearly
  2. Seasonal
  3. Synoptic (= a passing weather system)
  4. Day
  5. Seconds (turbulence)
- Influences on:
  - Electricity production forecast (1&2)
  - Wind turbine design (all)



# EPFL Introduction

## The resource

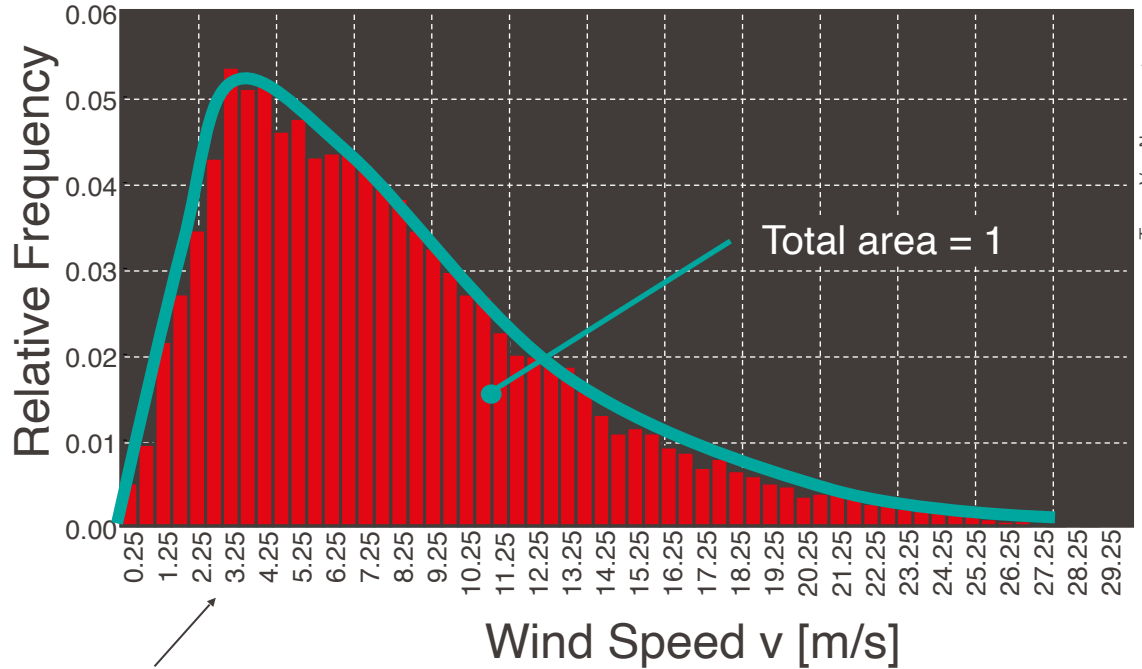
- Wind speed distribution at a given site:

- Weibull** probability density function:

$$f(v) = \left(\frac{k}{c}\right) \cdot \left(\frac{v}{c}\right)^{k-1} \cdot \exp\left[-\left(\frac{v}{c}\right)^k\right]$$

k: shape parameter

c: scale parameter



# Introduction

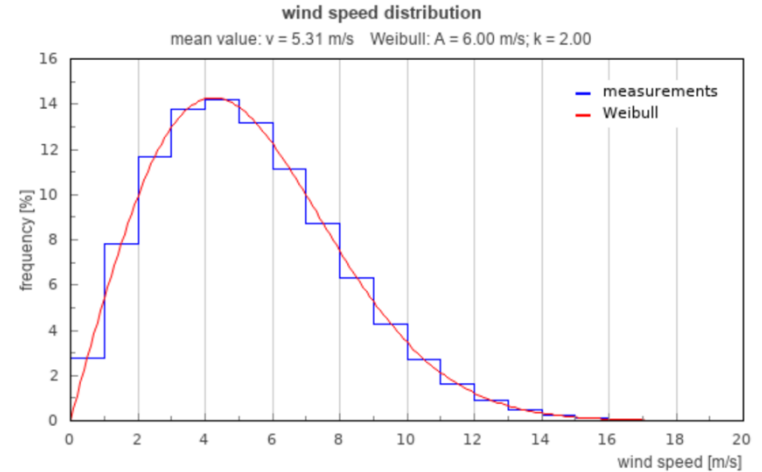
## The resource

- Data base of the Probability distribution function parameters:

<https://wind-data.ch/tools/weibull.php?lng=en>

Class	Frequency in %
0 - 1 m/s	2.75
1 - 2 m/s	7.80
2 - 3 m/s	11.64
3 - 4 m/s	13.79
4 - 5 m/s	14.20
5 - 6 m/s	13.15
6 - 7 m/s	11.14
7 - 8 m/s	8.72
8 - 9 m/s	6.34
9 - 10 m/s	4.30
10 - 11 m/s	2.73
11 - 12 m/s	1.62
12 - 13 m/s	0.91
13 - 14 m/s	0.48
14 - 15 m/s	0.24
15 - 16 m/s	0.11
16 - 17 m/s	0.05
17 - 18 m/s	0.02
18 - 19 m/s	0.01
19 - 20 m/s	0.00
<b>Sum</b>	<b>100.00</b>

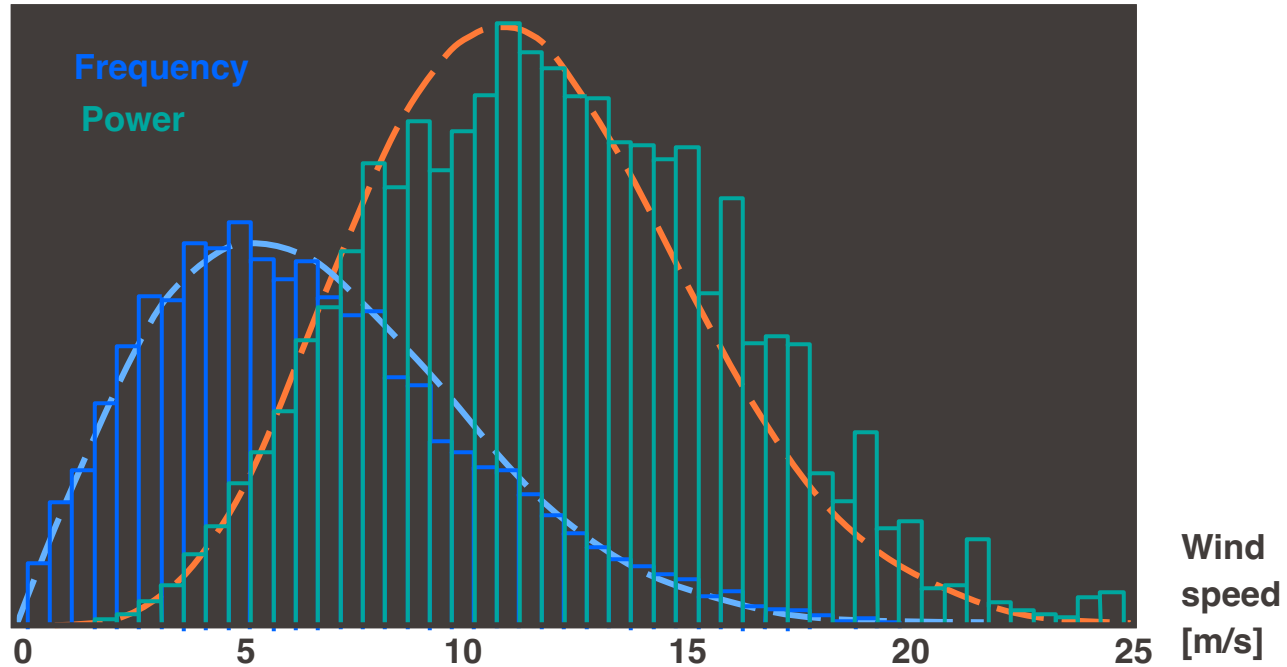
Result



# EPFL Introduction

## The resource

- Remember that the power is proportional to  $v^3$ :





# Physics of wind energy

# EPFL Physics of wind energy

- Additional elements we need:

- Mass conservation
- Bernoulli's principle

- Kinetic energy, power, force

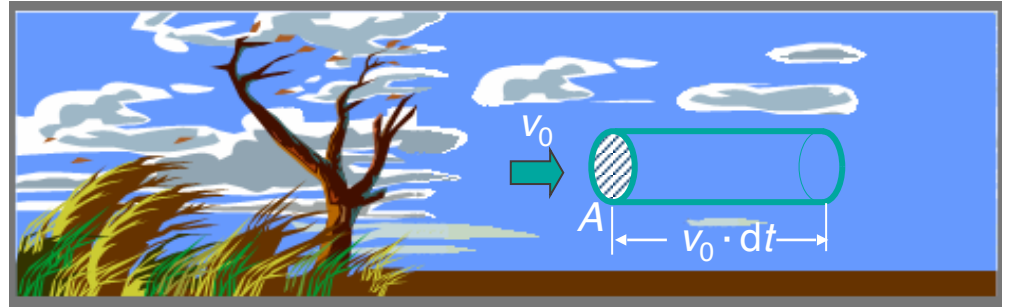
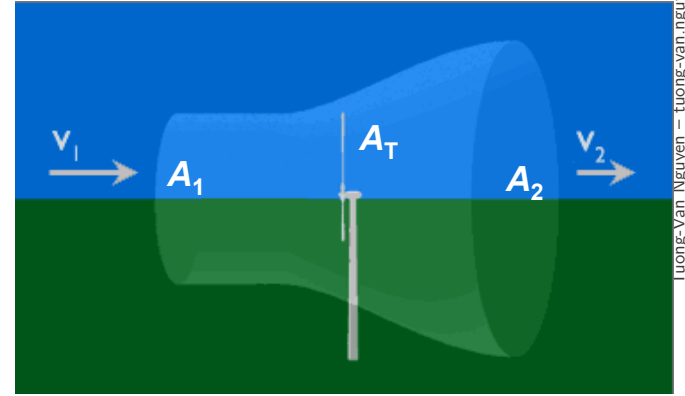
- Air passing through control volume  $V$  in  $dt$ :  $m_{air} = \rho V = \rho A v_0 dt$
- Mass flow through  $A$ :  $\dot{m}_{air} = \rho A v_0$
- Kinetic energy contained in the air:

$$E_{k,air} = \frac{1}{2} m_{air} v_0^2 = \frac{1}{2} \rho A v_0^3 dt$$

- Power:

$$\dot{E}_{k,air} = \frac{dE_{k,air}}{dt} = \frac{1}{2} \rho A v_0^3$$

- Force (drag):  $F_{air} = \frac{\dot{E}_{k,air}}{v_0} = \frac{1}{2} \rho A v_0^2$



# EPFL Physics of wind energy

- Let's consider the “**control volume**”  $V$ : If the surface  $A_T$  is swept by the blades of an horizontal-axis wind turbine of diameter  $D$ , the disturbed air flux affects a volume (control volume) having a cross-section **significantly larger** than  $A_T$

- Force** acting on the turbine ( $v_0 =$  “free” wind speed; recalling that

$$\cancel{F \cdot dt} = m dv = \rho \cdot A_T \cdot v_T \cdot \cancel{dt} (v_1 - v_2) = \rho \cdot A_T \cdot v_T \cdot \cancel{dt} (v_0 - v_2)$$

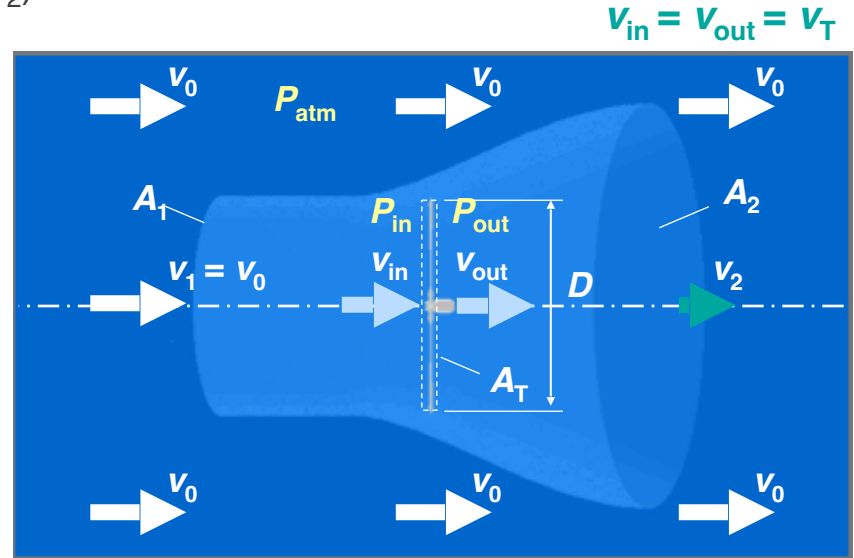
- We have also that:  $F = A_T \cdot (P_{in} - P_{out})$

$$\Rightarrow \boxed{A_T \cdot (P_{in} - P_{out}) = \rho \cdot A_T \cdot v_T \cdot (v_0 - v_2)} \quad (3)$$

- And from Bernoulli's principle:

$$\left\{ \begin{array}{l} \text{upstream: } P_{in} - P_{atm} = \rho \frac{v_0^2 - v_1^2}{2} \\ \text{downstream: } P_{atm} - P_{out} = \rho \frac{v_2^2 - v_0^2}{2} \end{array} \right. \quad \frac{1}{2} \cdot \rho \cdot v^2 + P = \text{cst}$$

$$\Rightarrow \boxed{P_{in} - P_{out} = \frac{1}{2} \rho (v_0^2 - v_2^2)} \quad (4)$$



# EPFL Physics of wind energy

- Let's consider the “**control volume**”  $V$ : If the surface  $A_T$  is swept by the blades of an horizontal-axis wind turbine of diameter  $D$ , the disturbed air flux affects a volume (control volume) having a cross-section **significantly larger** than  $A_T$
- Let's now look at the **kinetic energy**:

$$E_T = E_{kin,air}^{in} - E_{kin,air}^{out} = \frac{1}{2} m_{air} (v_0^2 - v_2^2) \quad (1)$$

$$\dot{E}_T = \frac{1}{2} \dot{m}_{air} (v_0^2 - v_2^2) = \frac{1}{2} \rho_{air} \underbrace{A_T v_T}_{=A_2 \cdot v_2 \text{ (mass conservation)}} (v_0^2 - v_2^2) \quad (2)$$

$$\dot{E}_T = \frac{1}{2} \rho_{air} A_T \frac{A_2}{A_T} v_2 (v_0^2 - v_2^2) \quad (\text{multiply by } v_0/v_0)$$

$$\dot{E}_T = \frac{1}{2} \rho_{air} A_T v_0^3 \frac{A_2}{A_T} \frac{v_2}{v_0} \left[ 1 - \left( \frac{v_2}{v_0} \right)^2 \right] \quad \boxed{\dot{E}_T = C_p \dot{E}_{Wind}} \quad (5)$$

Power in the wind

$C_p$ : Power coefficient

$$A_T \cdot (P_{in} - P_{out}) = \rho \cdot A_2 \cdot v_2 \cdot (v_0 - v_2) \quad (3)$$

$$P_{in} - P_{out} = \frac{1}{2} \rho (v_0^2 - v_2^2) \quad (4)$$

$v_{in} = v_{out} = v_T$

$$\frac{A_2}{A_T} = \frac{(1 + \frac{v_2}{v_0})}{2 \frac{v_2}{v_0}}$$

if  $x = \frac{v_2}{v_0}$  then  $C_p = \frac{(1+x)(1-x^2)}{2} K$

# Power coefficient : max for $x = v_2/v_0$

- Betz law gives us a **theoretical limit** for the efficiency (i.e. conversion of wind kinetic energy into mechanical power) – we can harness **59.3%** of the energy in the wind.

- Effective** (real) power coefficient:

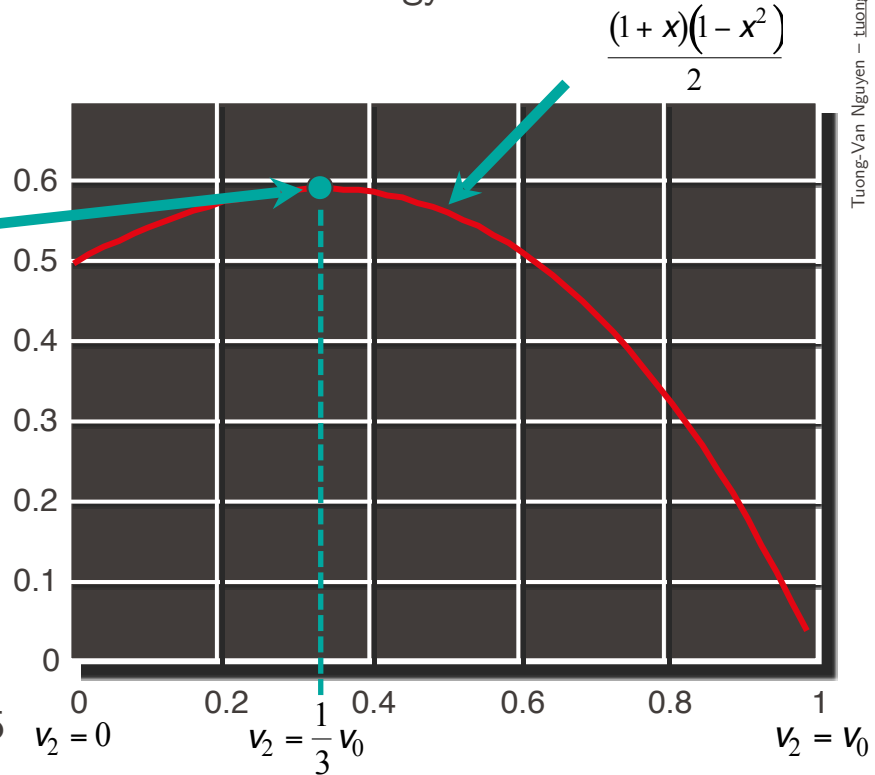
$$C_p = \frac{\dot{E}_T}{\dot{E}_W} = \frac{\dot{E}_T}{\frac{1}{2}\rho_{air}A_T v_0^3}$$

$$\max_x C_p(x) = \frac{(1+x)(1-x^2)}{2}$$

- Betz limit:  $16/27 = 0.5926\dots$

- $v_2 = v_0/3$
- $v_T = 2v_0/3$
- $A_2 = 3A_1$
- $A_T = 3A_1/2$

- Practical values in real applications: 0.35-0.5

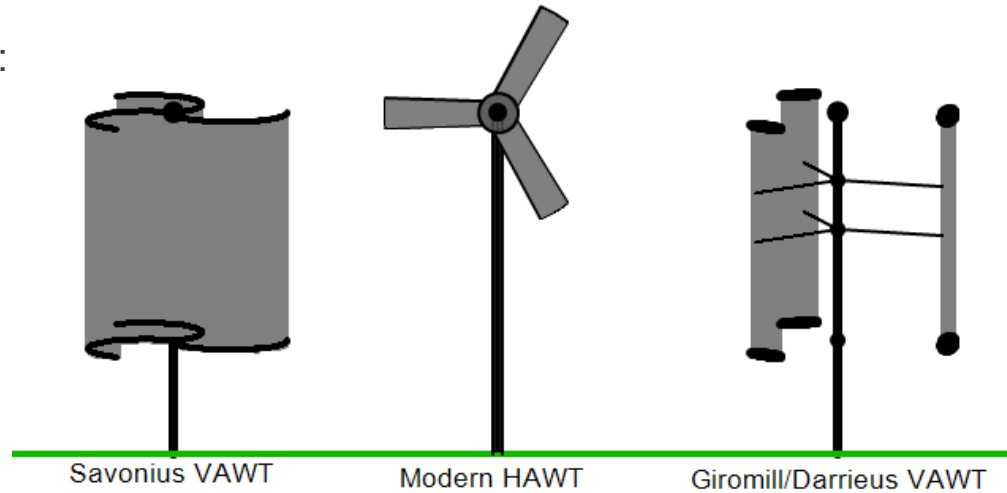




# Wind turbines & energy systems

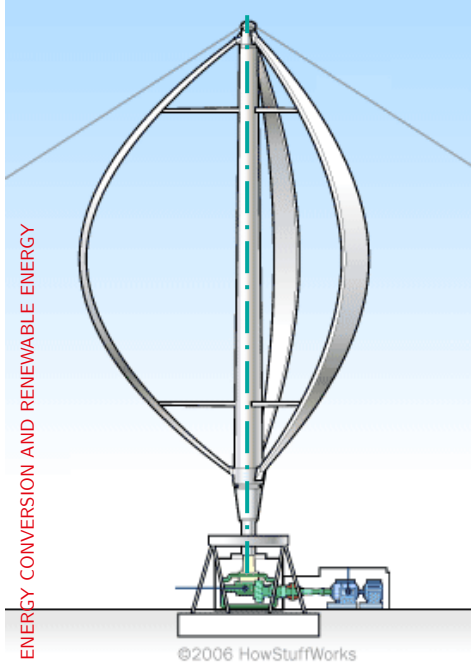
# EPFL Wind turbines

- Types of wind turbines
- Key components
- Design parameters (HAWT):
- Operating ranges
- Growing in size
- Wind farms

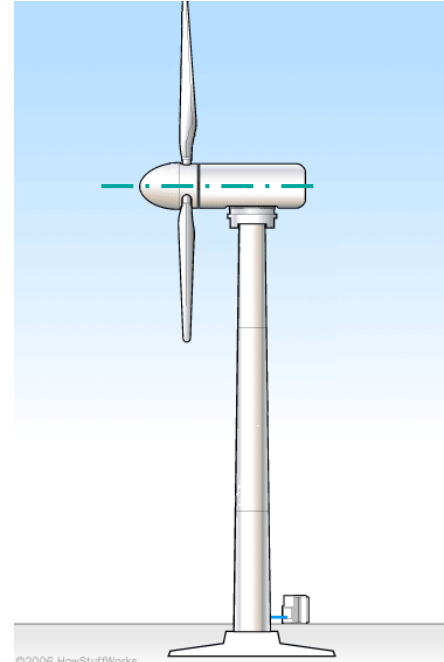


# EPFL Types of wind turbines

- Key classification: vertical vs. horizontal axis



**VAWT:** Vertical axis wind turbines. Can be drag (Savonius rotor) or lift based (Darrieus rotor)

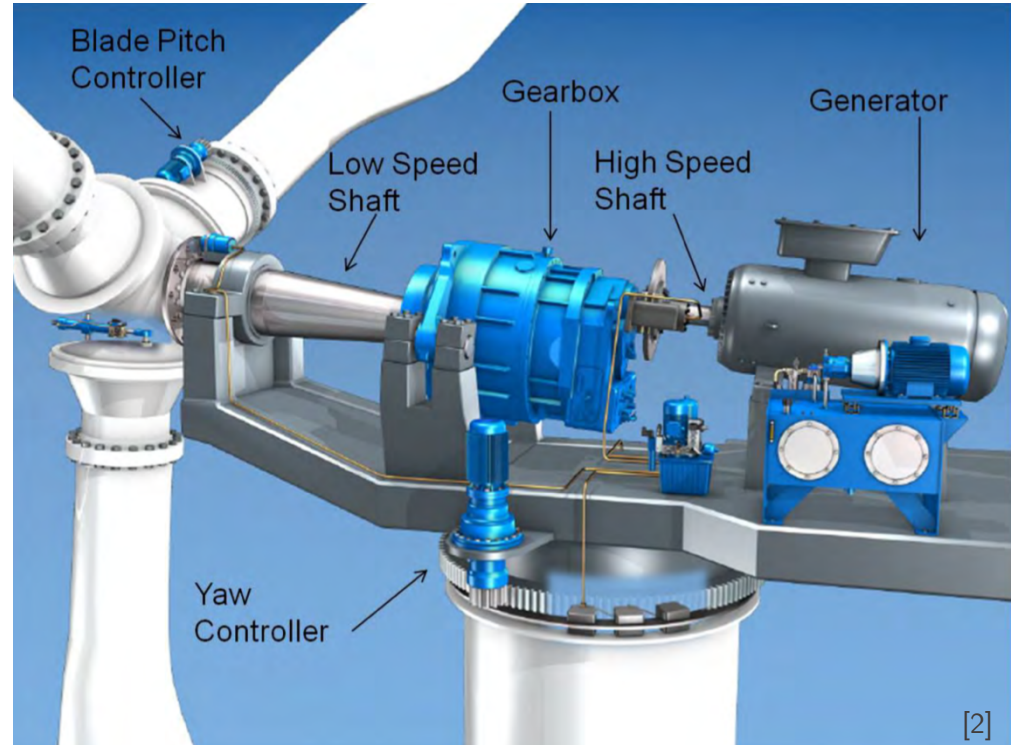


**HAWT:** Horizontal axis wind turbines. Most used and efficient configurations, normally with 1-3 blades.

# Key components

Key components of a horizontal axis wind turbine.

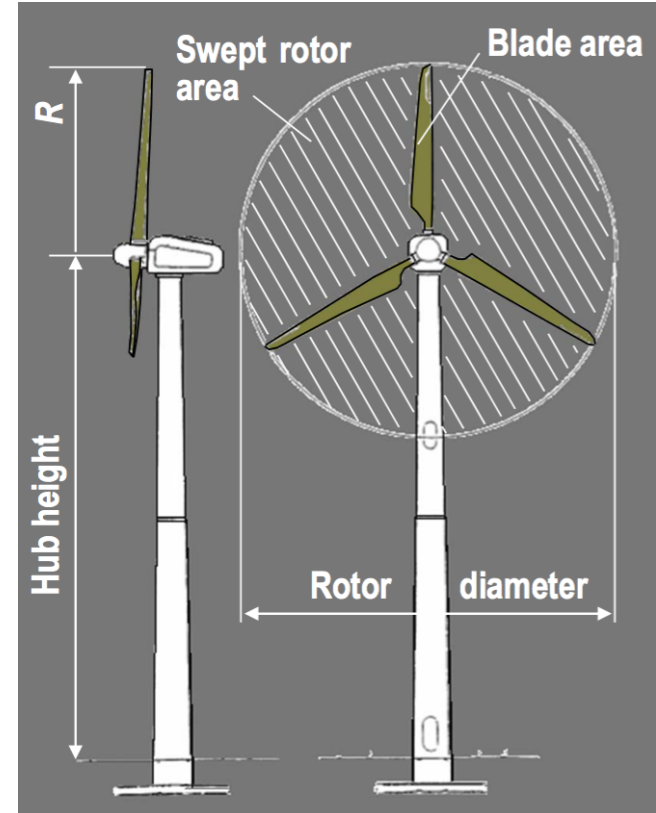
- The drivetrain consists of a **gearbox** connected to the rotor by a low-speed shaft
- The **generator** converts mechanical work to electricity..
- Mechanical **brakes** needed to completely stop the turbine



# Design parameters of HAWT

Key parameters of a HAWT:

- Number of blades
- Rated power
- Hub height (directly proportional to diameter)
- Swept area
- Solidity = blade area / swept area
  - High: **high** starting torque, **low** speed of rotation  $\omega$
  - Low: **low** starting torque, **high** speed of rotation  $\omega$



# Design parameters of HAWT

- **Number of blades:** it does not influence the power. In theory, the most efficient design comes with **infinite number of infinitely narrow blades**
- Real design criteria: aesthetics, structural, financial



1 blade



2 blades

- Same power
- Low torque
- High RPM
- More noise
- **Cheap**
- +6% efficiency vs 1-blade<sup>[2]</sup>



3 blades

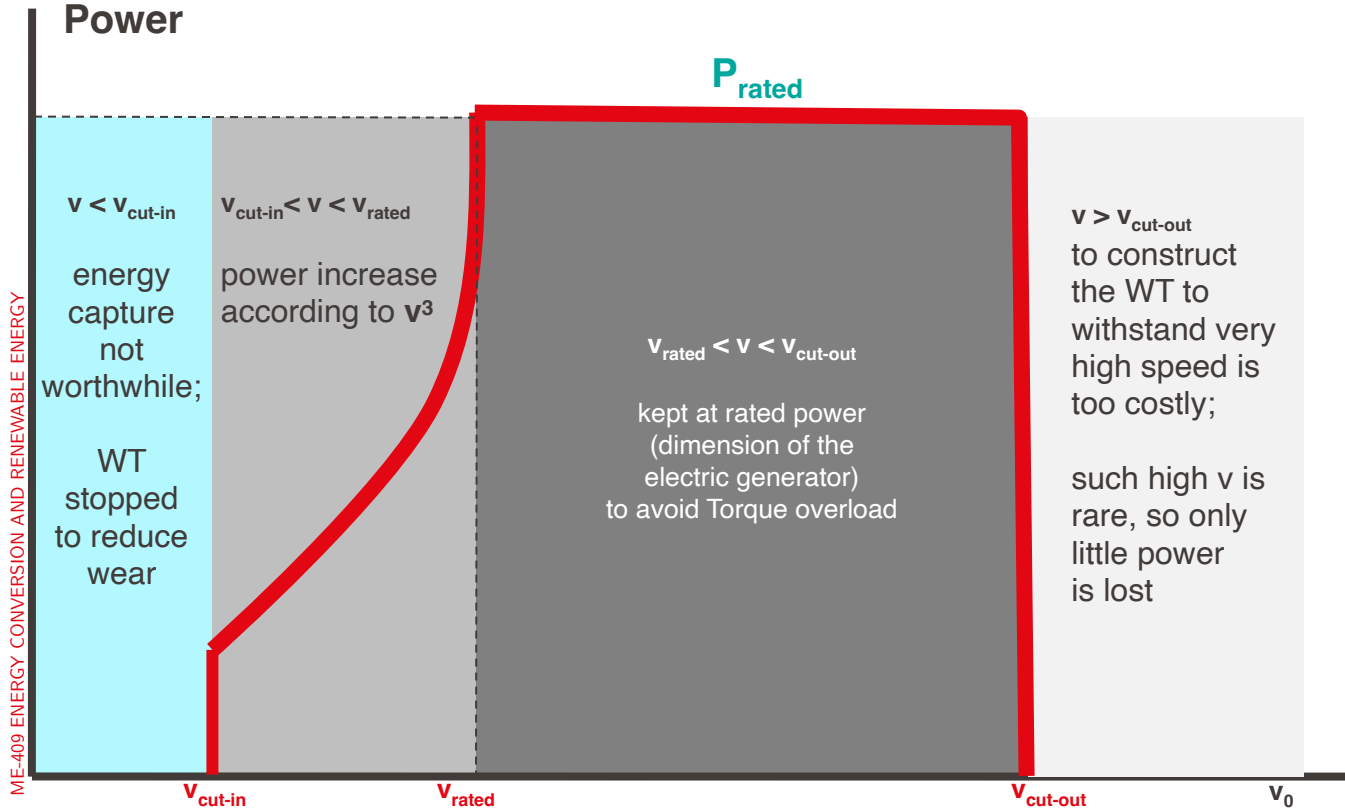
- Same power
- Higher torque
- Lower RPM
- Less noise
- +3% efficiency vs 2-blades<sup>[2]</sup>



Multiple blades

- Same power
- **High** torque
- Low RPM
- No noise
- Expensive rotor
- Negligible better efficiency<sup>[2]</sup>

# EPFL Operating ranges



Aerodynamic power limiting regulation by:

1. Variable pitch
2. Yaw
3. Stall

WT can be run at:

- **One fixed  $\omega$**
- **Two fixed  $\omega$**
- **Variable  $\omega$**

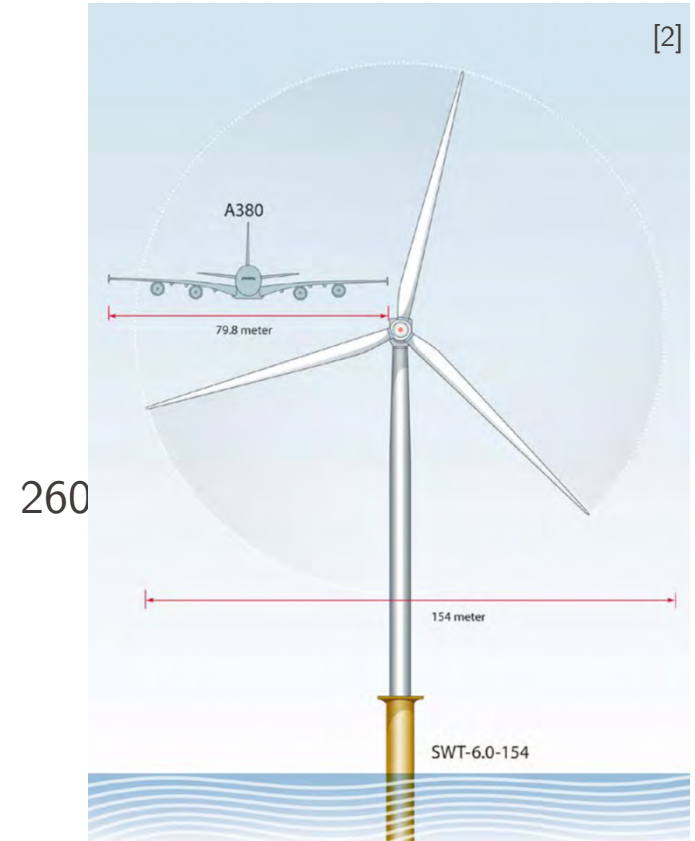
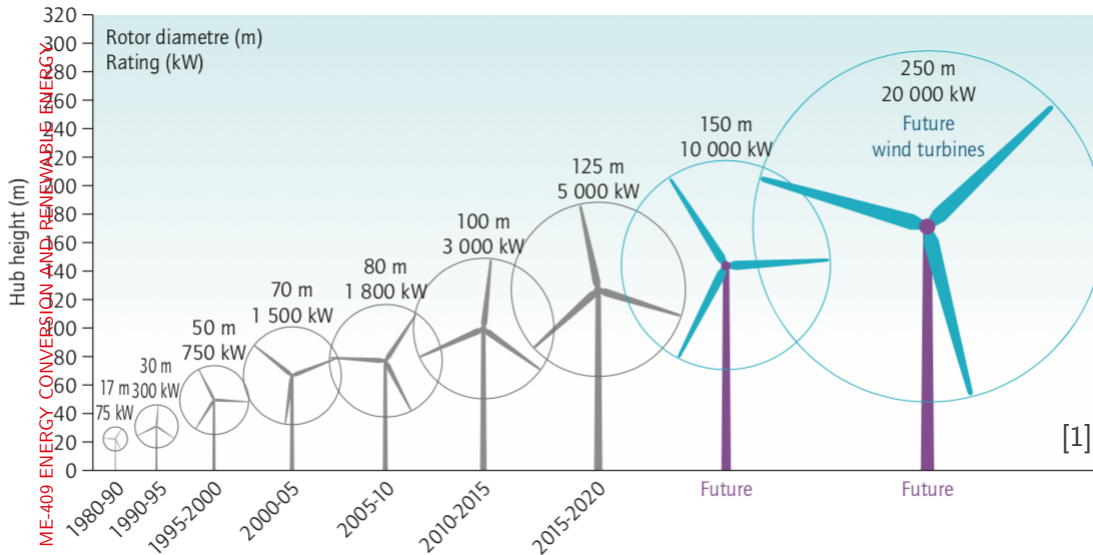
Variable speed:

- + 7% energy
- + less power fluctuations
- higher cost
- less reliability

# EPFL Growing in size

$$\dot{E}_{k,air} = \frac{dE_{k,air}}{dt} = \frac{1}{2} \rho A v_0^3$$

- The power is proportional to A  $\rightarrow$  D<sup>2</sup>



# EPFL Wind farms

- Wind turbines are commonly used in wind farms:
  - Usually 10-30 turbines
  - Spacing: 7-8\*Diagrams
  - 1 grid transformer for the whole site
  - Timing: construction (1y); operation (20y); decommissioning (0.5y)
- Horns Rev offshore wind farm (DK):
  - 80 turbines
  - 160 MW<sub>e</sub>
  - Offshore:
    - Higher capacity factors
    - Higher and more regular wind speed (120 m/s)
    - More noise (lower solidity)



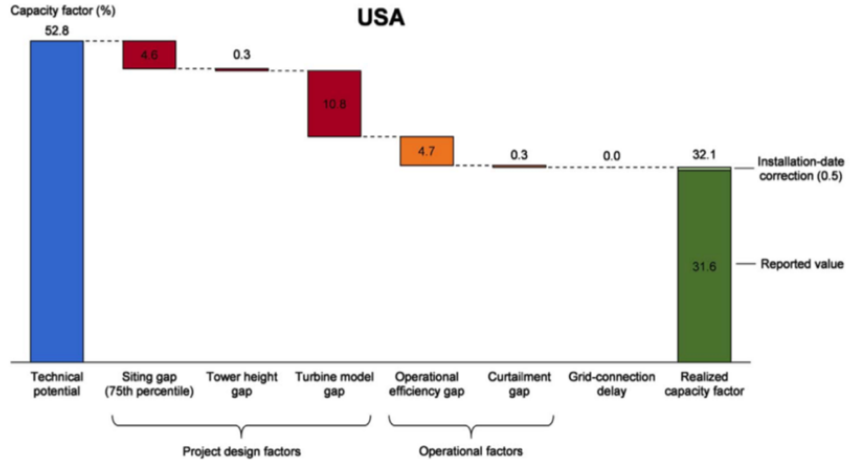
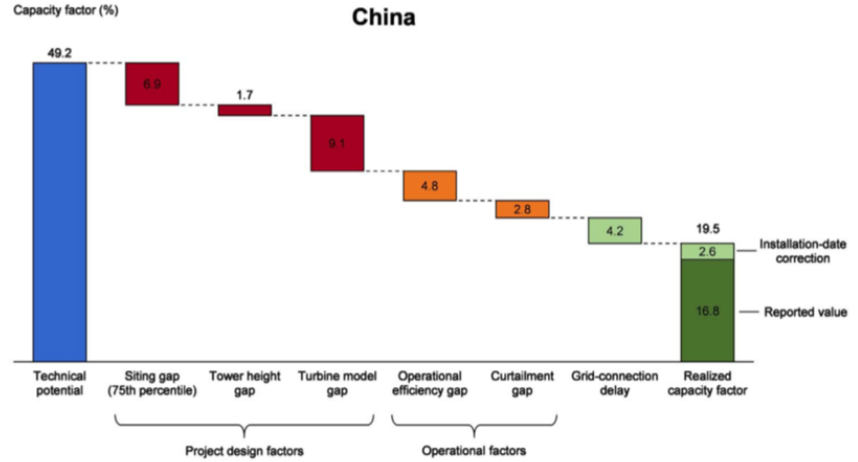
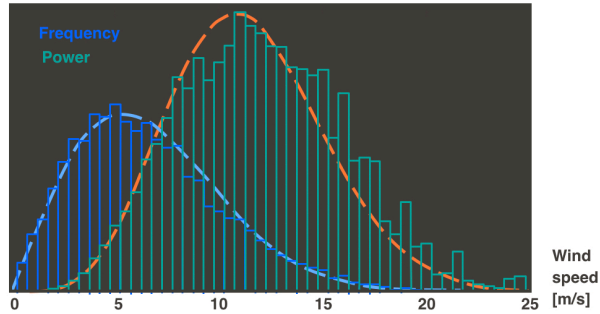
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# Capacity factor

$$CapacityFactor = \frac{\int_{year} \dot{E}(t) dt}{\dot{E}_{rated} \cdot 8760}$$

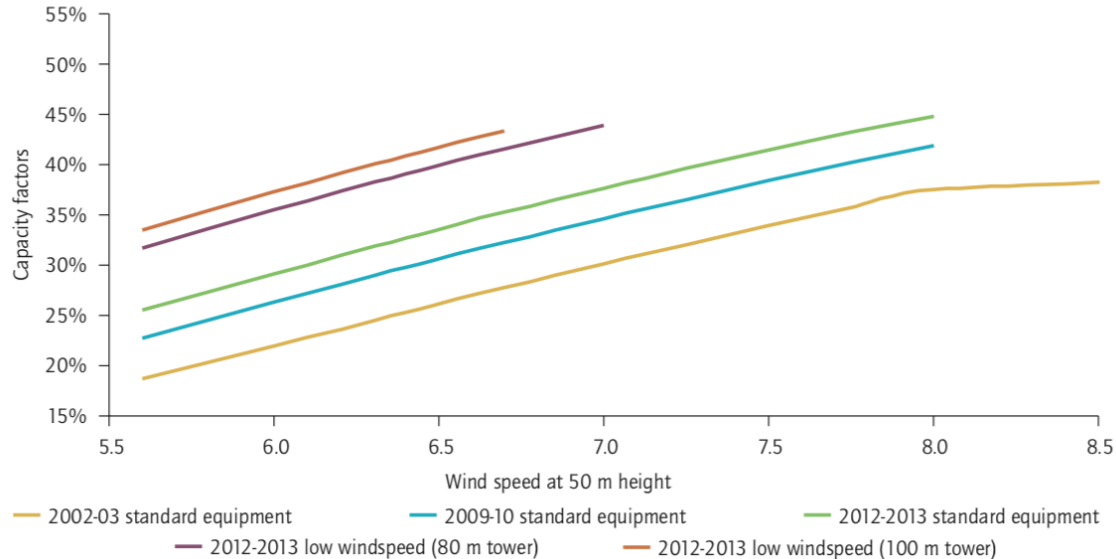
Location is critical (wind speed distribution)



# Capacity factors

- Capacity factor  $c_f$ , typical values:
  - Onshore: 26% (2013) → 31% (2050)
  - Offshore: 36% (2013) → 42% (2050)
  - In Switzerland: 19% (today) → 23% (future)

Figure 3: Capacity factors of selected turbine types



# Costs

- Cost is decreasing!
  - IEA projection for 2035: 1600 USD<sub>2012</sub>/KW<sub>e</sub>
  - 2017 data by Wind Europe:
    - 22.3 B€ announced investments
    - 11.5 GW<sub>e</sub>
 → 1939 €/kW<sub>e</sub>
  - LCOE in 2023: 35-80 €/MWh onshore, 70-120 €/MWh offshore

Figure 5.3 Total installed costs of onshore wind projects and global weighted average, 1983-2017

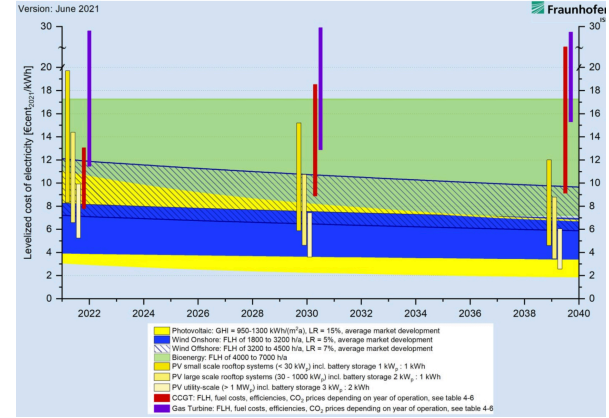
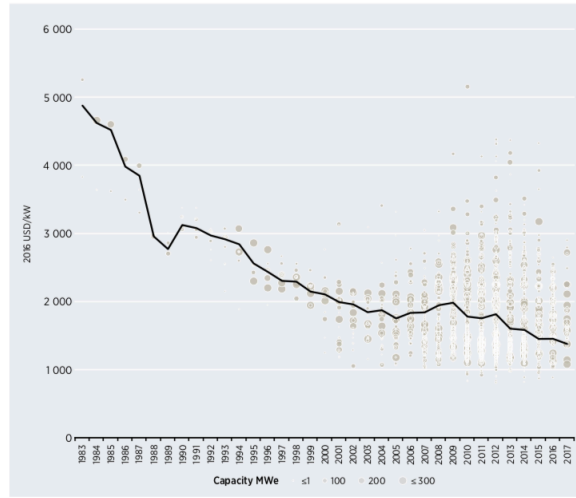
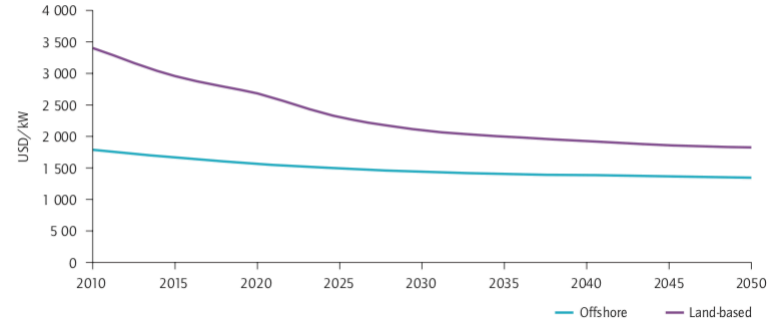
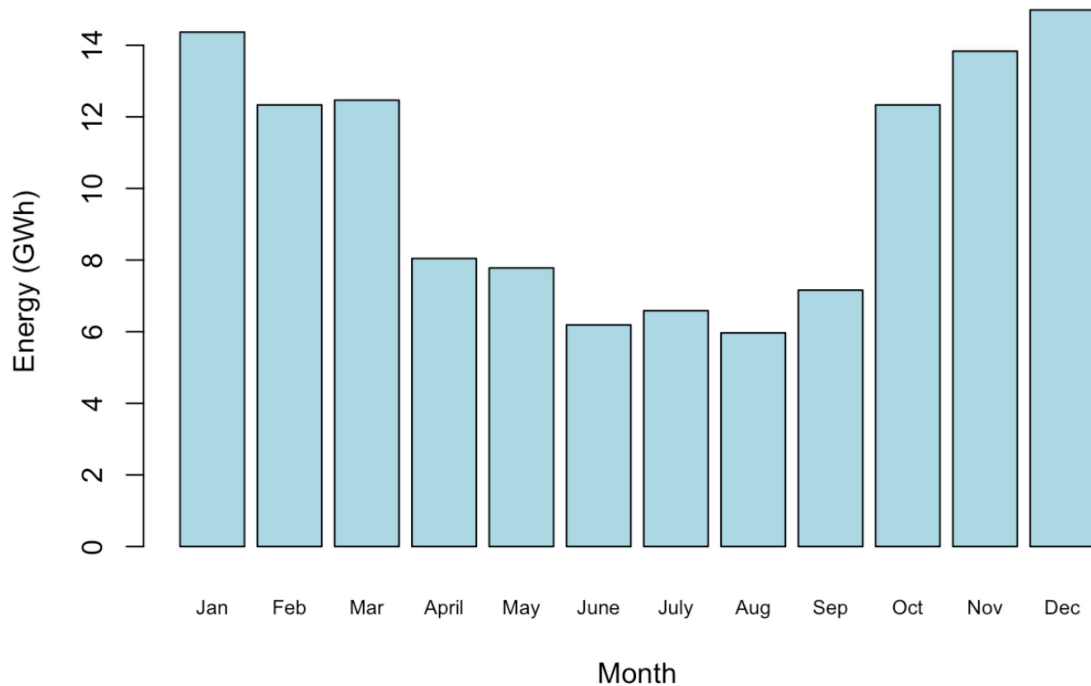


Figure 13: 2DS projections for investment costs of wind turbines



# Monthly profiles

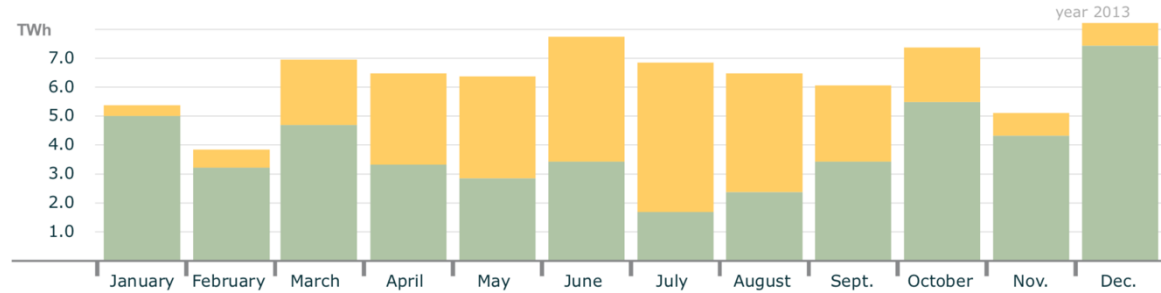


Monthly wind energy in Switzerland, 2018 [3]

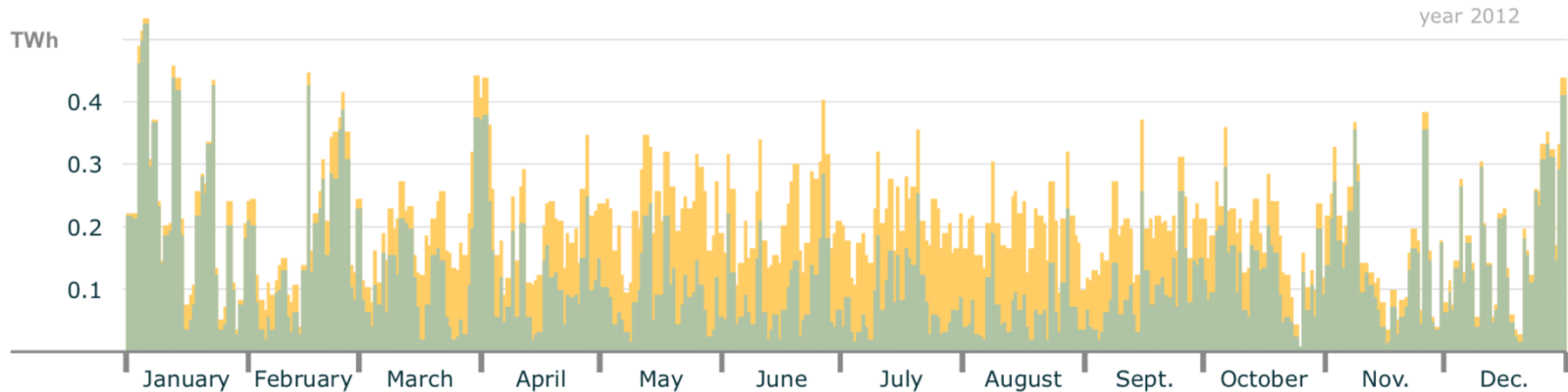
# Intermittency

- Different time scales:
  - Hourly
  - Daily
  - Weekly
  - Seasonal
- Can complement solar!

Monthly Production Solar and Wind



Daily production Solar and Wind



# EPFL Risks and impacts

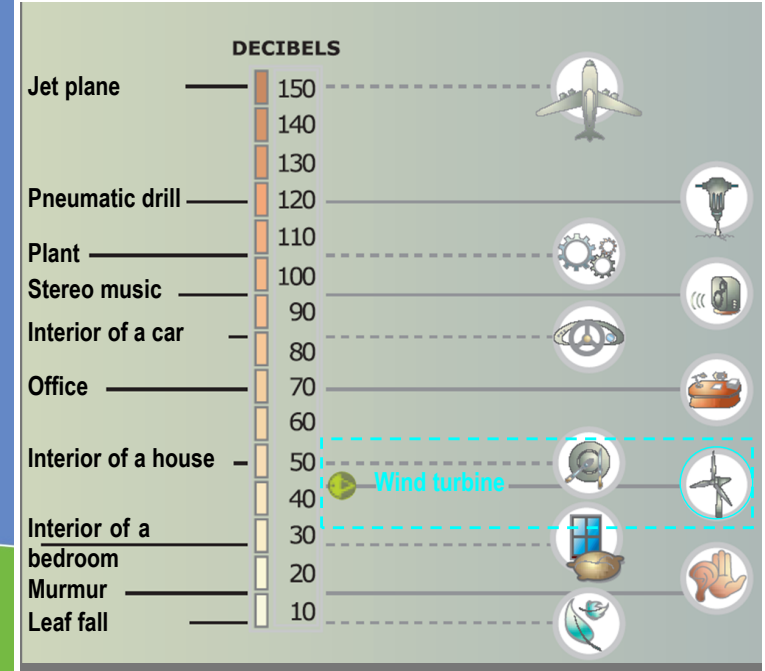
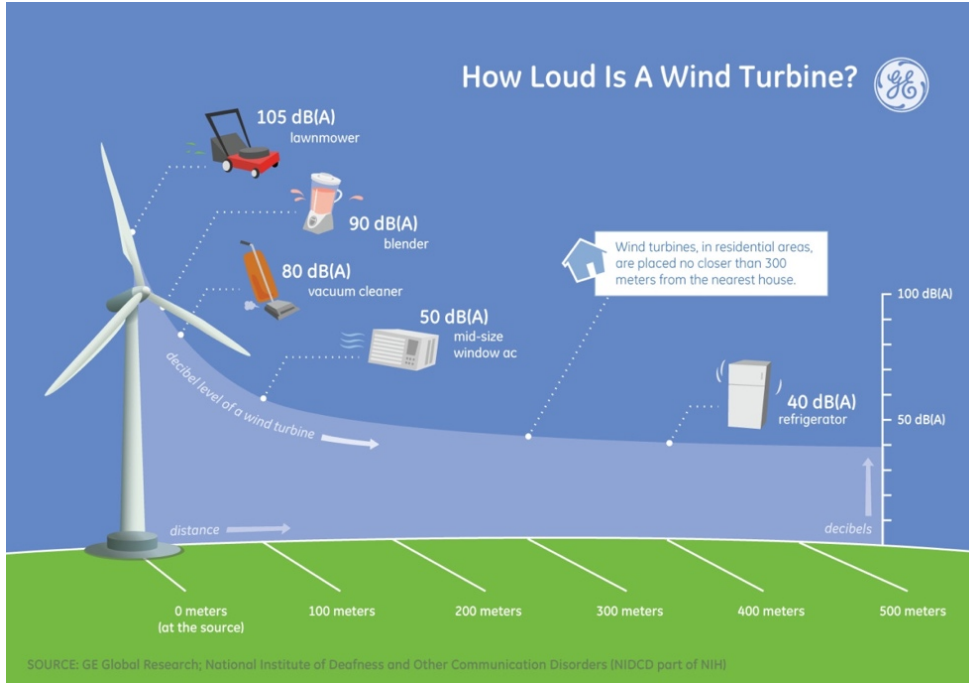
- Machinery maintenance accidents
- Blade failures
- Falling ice
- Paragliders and small aircraft crashing into support structures
- Turbine's brake fails → the turbine can spin freely until it disintegrates
- Turbine blades may fall off due to manufacturing flaws
- Lightning strikes → rotor blade damage and fires



*A turbine on fire after an oil leak*

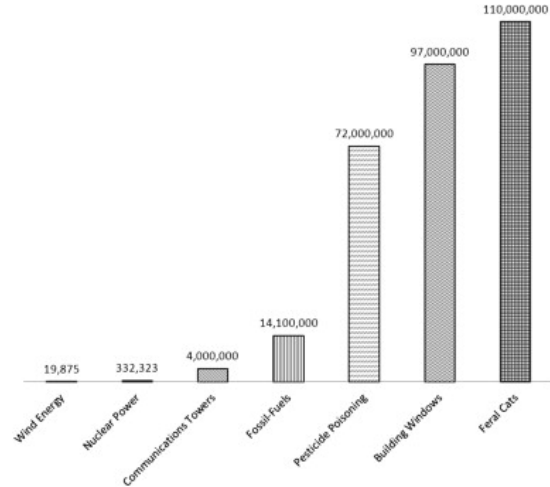
# EPFL Perceived risks : noise

- Other perceived problems are: visual impact, noise and killing birds



# Risks and impacts: Killing birds

- Other perceived problems are: visual impact, **noise** and **killing birds**



Annual avian deaths in 2009 in the US

Some controversy about

- Orders of magnitude are clear
- Relatively small danger for birds
- Climate change likely to be a more severe risk for birds



# Take-home message

# Take-home message

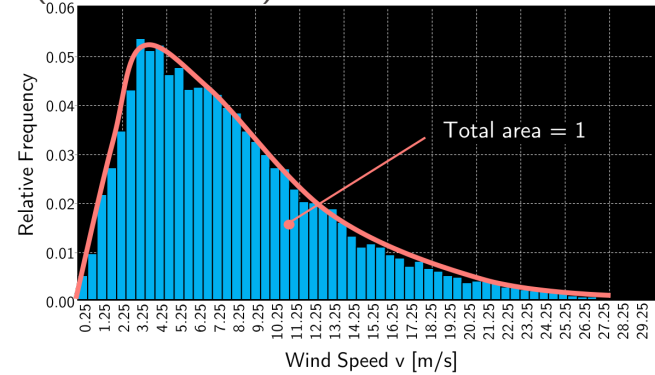
## ■ Key concepts

- Wind is growing fast → key player for climate change
- Resource: power goes with  $v^3$ , location dependent (Weibull PDF)
- Betz limit: theoretical limit is 59.3% efficiency
- Forces: maximise lift/drag

$$\dot{E}_{k,air} = \frac{dE_{k,air}}{dt} = \frac{1}{2}\rho A v_0^3$$

## ■ Wind Turbines

- Classified in vertical vs horizontal axes
- Growing in size
- Wind farms



$$\dot{E}_{T,max} = \frac{1}{2}\rho_{air}A_T v_0^3 \left[ \frac{16}{27} \right] = 0.593 \dot{E}_{Wind}$$

## ■ Wind in the energy system

- Costs are quickly reducing → wind is competitive!
- Capacity factors: 25-30% onshore, 35-40% offshore
- Wind can be a good complement of solar

$$CapacityFactor = \frac{\int_{year} \dot{E}(t)dt}{\dot{E}_{rated} \cdot 8760}$$



Questions?

Prof. François  
Maréchal