

Chapter 4: Discovery learning

How do people learn ?

- by exploration, trial and error
- by incremental mastery
- by verbal elaboration

Learning Fractions: Comparing 2 methods

GOMATHS.ch Le site d'entraînement au calcul mental et autres techniques de calcul.

Accueil | Nouvel | Contact | Info | Soutien | Nouveautés | Calculatrice | Suggestions

Les 4 opérations - l'addition

Adapte la difficulté à ton niveau. Choisis le thème de ta fraction. Tu es élève ou enseignant ? Si enseignant, affiche les corrigés sur une feuille de travail.

Essaie également les autres outils sur la même thème (multiplication, division, soustraction).

- Liste de fractions personnalisées
- La table de l'addition avec l'outil addition
- Les opérations de l'addition sur un CPM (à adapter)

Ordre de grandeur: 100 - 1000 (nombre entier) (nombre décimal)

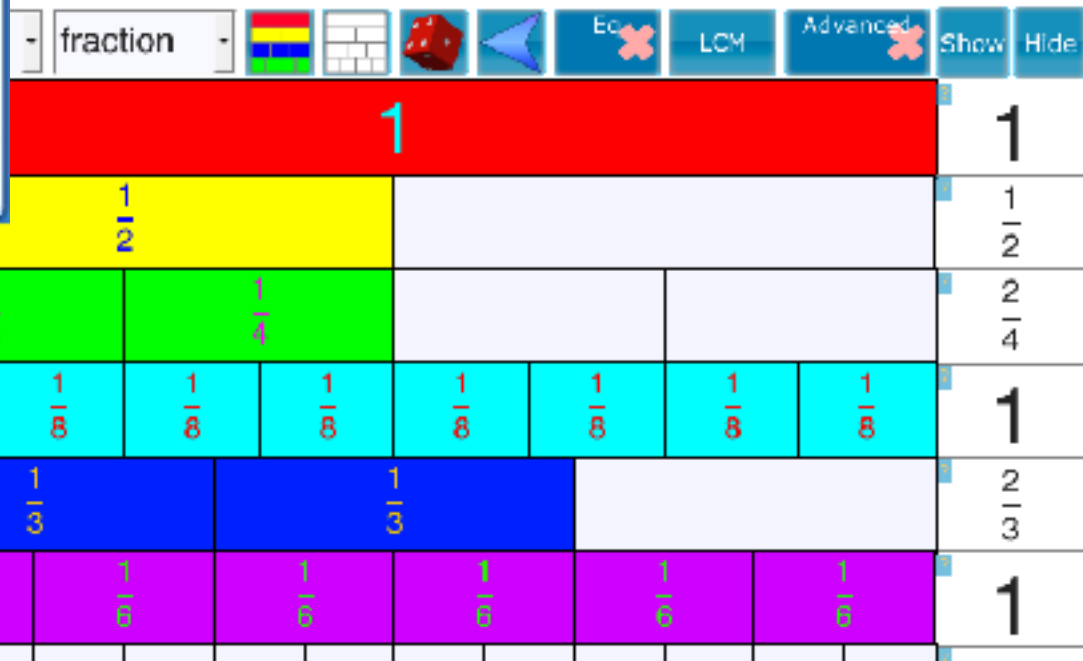
Commencer | Voir la réponse

le calcul

réponse

✓ ✗

insérer une liste de fractions ou 10 additions en colonne



https://gomaths.edu-vd.ch/cf_mix.php

<https://www.visnos.com/demos/fraction-wall>

gomaths.ch

Créer un profil ou télécharger nos logiciels gratuits

Accueil | Accueil | Nos logiciels | Nos logiciels | Nos logiciels | Nos logiciels

Simplification de fractions

Insérer un nombre au numérateur et un nombre au dénominateur. Réduire la fraction à son plus petit dénominateur possible. Donner une valeur à la fraction. Donner une valeur à la simplification.

Numérateur: / Dénominateur: [Simplifier]

[OK] [Annuler]

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mixed	-	fraction					Eq	LCM	Advanced	Show	Hide	
1											1	
1/2											1/2	
1/4		1/4									2/4	
1/8	1/8	1/8	1/8	1/8	1/8	1/8	1/8	1/8	1/8		1	
1/3				1/3								2/3
1/6	1/6	1/6	1/6	1/6	1/6	1/6	1/6	1/6	1/6		1	



LEGO SYSTEM

1

2

3

4

5





Curriculum ?

Lesson A

A **splountz** is a triangle with 3 smaller shapes placed on different sides, one in the same color as the triangle and the two others in a different color.

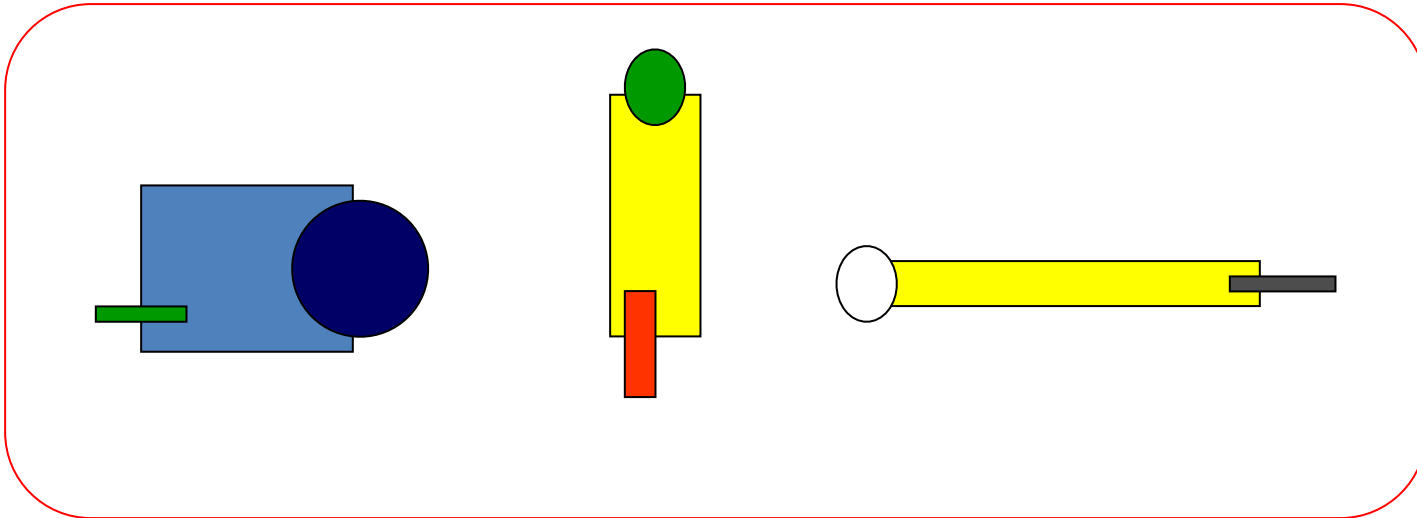


Is this a Splountz ?

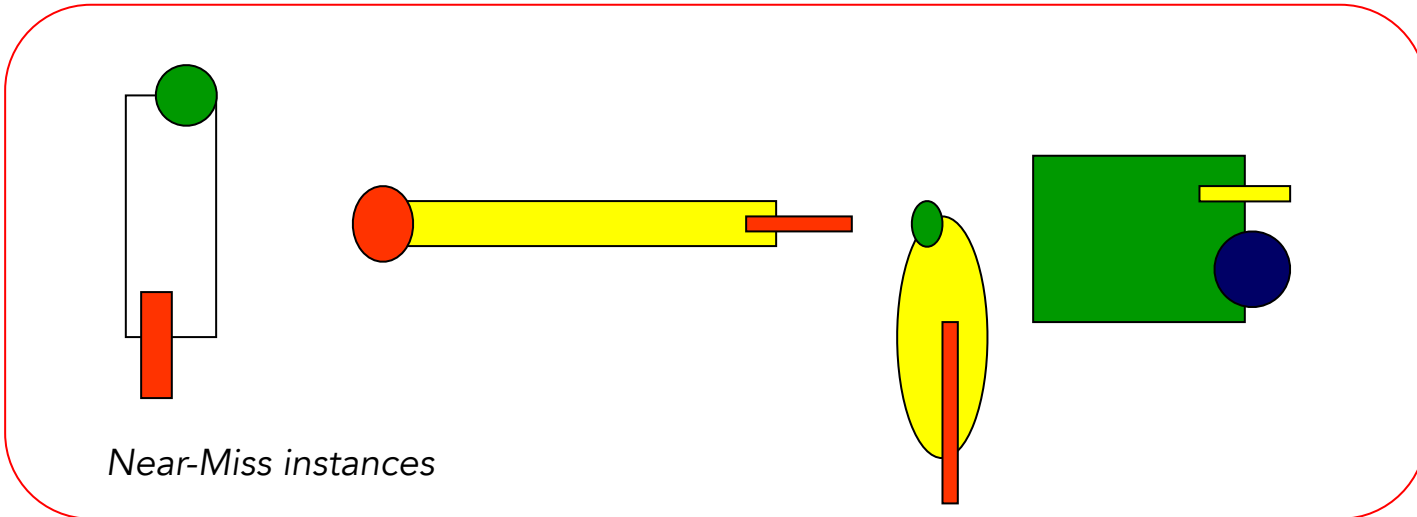
- Yes
- No

Lesson B

WHAS IS A SPUC ?



Positive instances



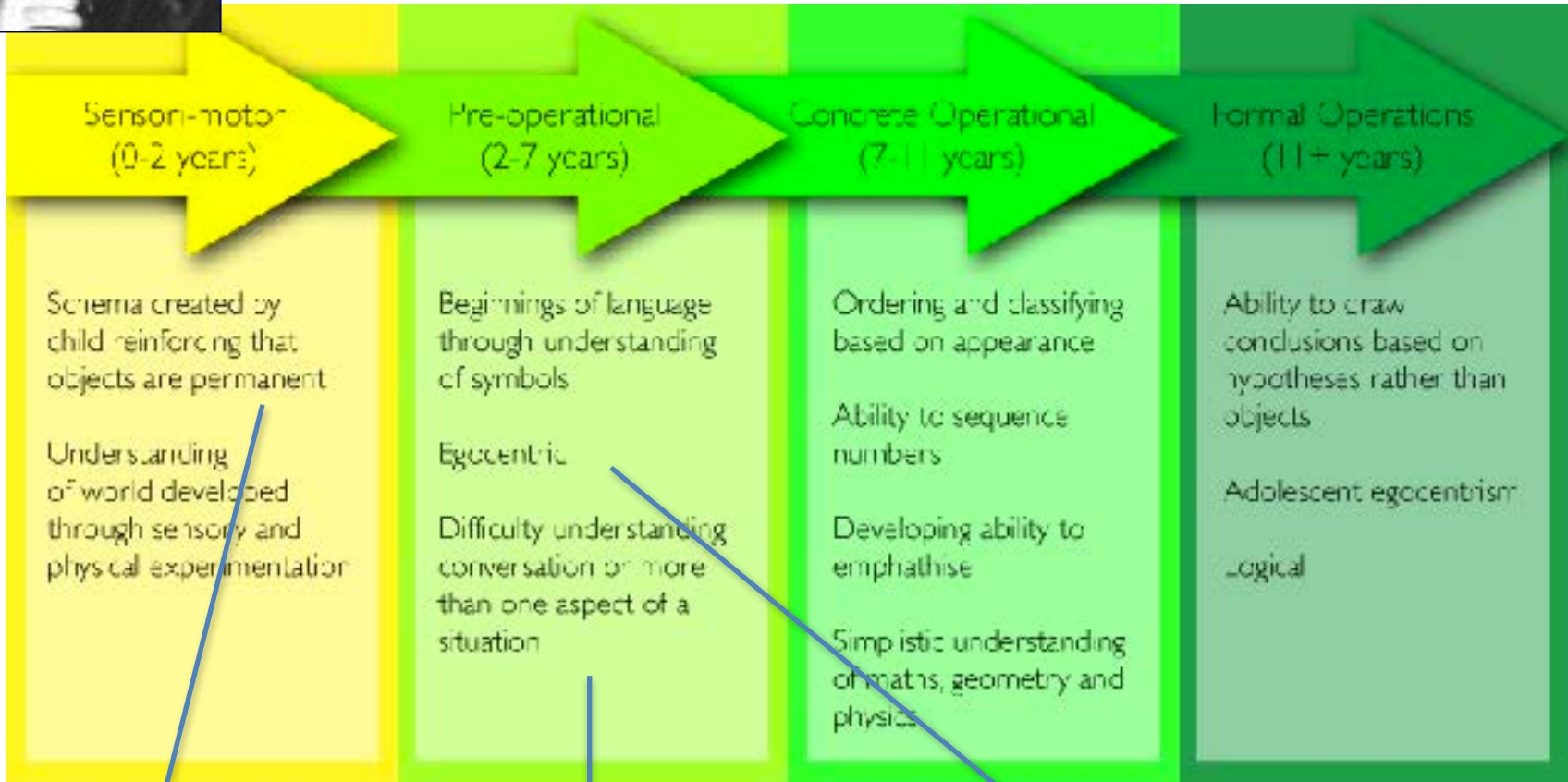
Near-Miss instances

Negative instances

Stages of cognitive development

Constructivism

Jean Piaget



<https://www.papermasters.com/intellectual-growth.html>

Permanence of object

Conservation Task

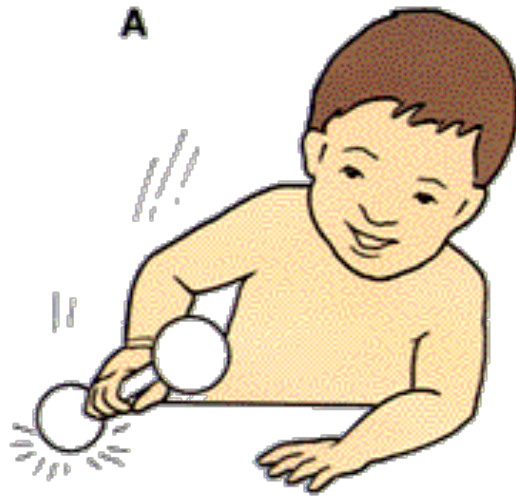
Pyramid Task

Assimilation and Accommodation

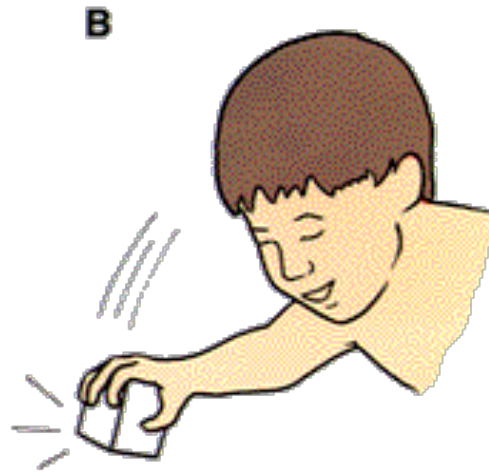
How can this girl use her “dog” schema when encountering a cat?



- She can **assimilate** the experience into her schema by referring to the cat as a “dog”
- or
- she can **accommodate** her animal schema by separating the cat, and even different types of dogs, into separate schemas.



Banging is a favorite **scheme** used by babies to explore their world . . .



. . . And **assimilation** occurs when they incorporate new objects into the scheme.

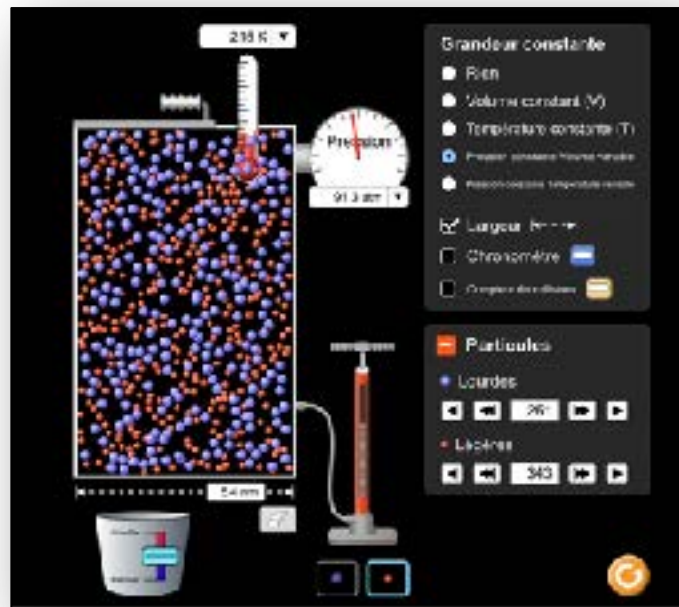


Accomodation occurs when the new object doesn't fit the existing scheme.

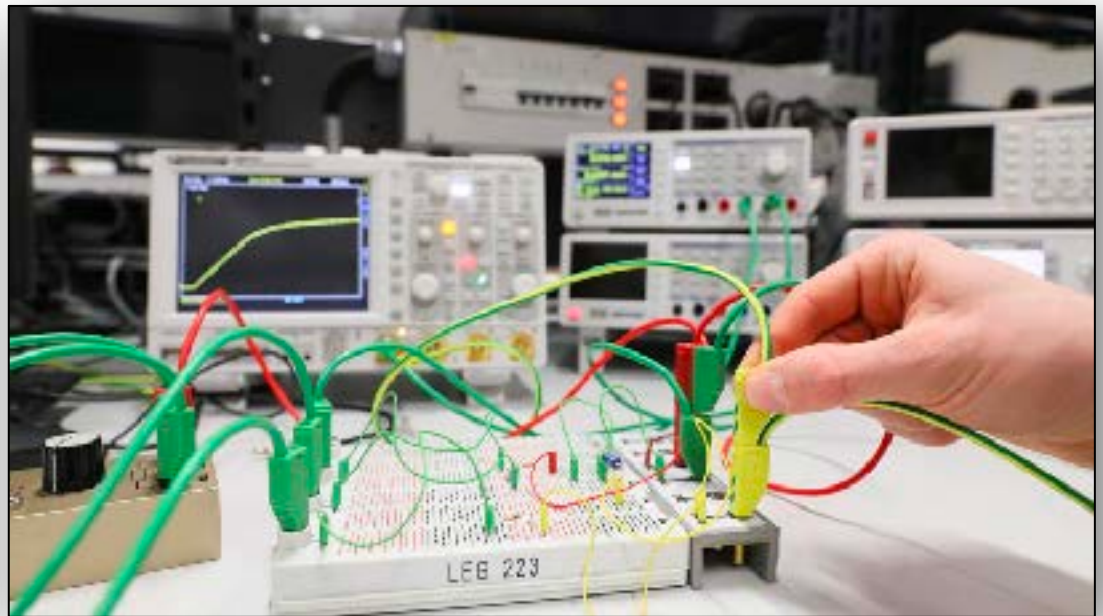
Piaget (1952) defined a schema as 'a cohesive, repeatable action sequence possessing component actions that are tightly interconnected and governed by a core meaning'. Basically, a schema is the building block of intelligent behavior

Cognitive Conflict as key learning mechanism

- Learning from experience
- Learning by doing
- Discovery learning

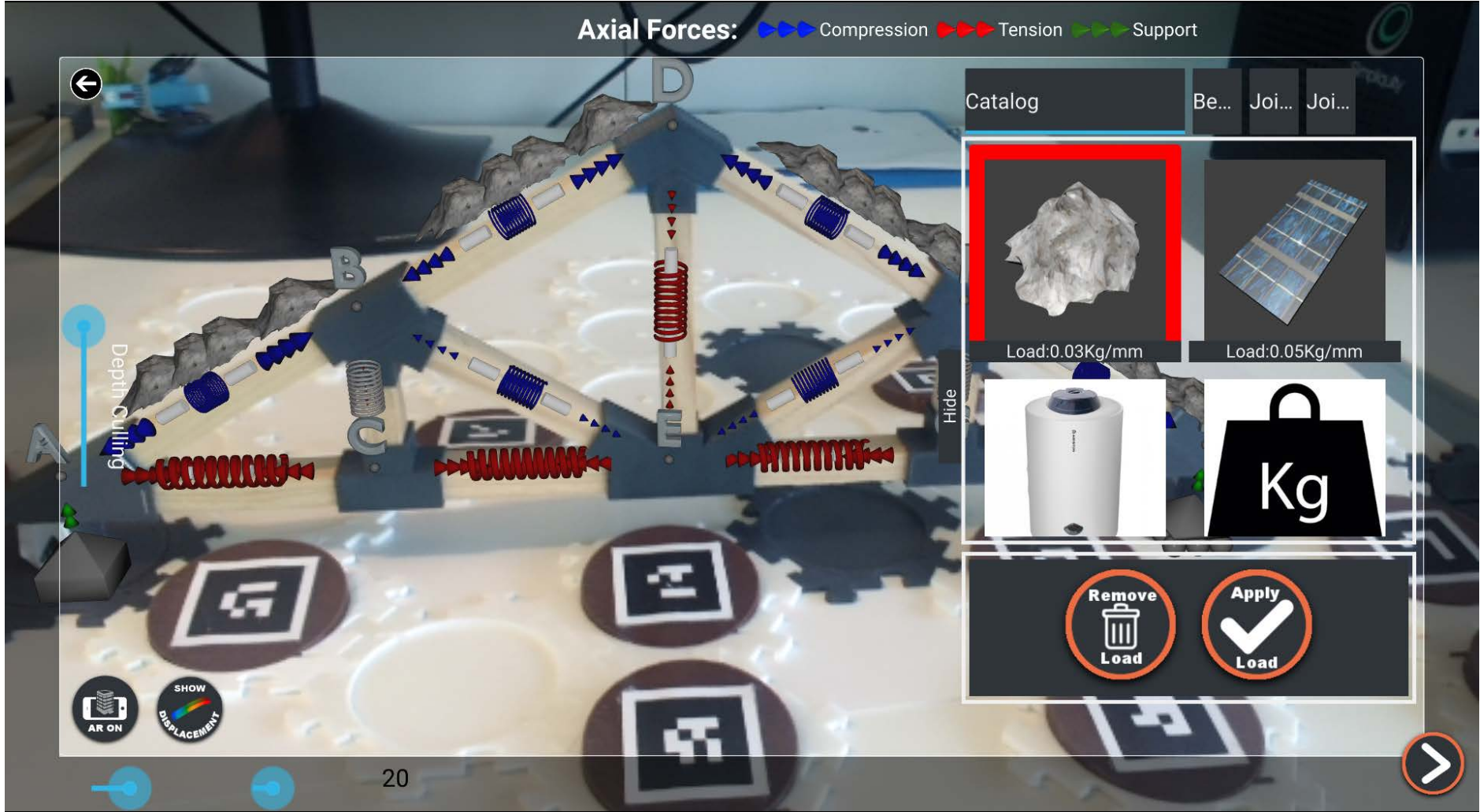


https://phet.colorado.edu/sims/html/gases-intro/latest/gases-intro_all.html?locale=fr



Discovery learning lab (The SPOT)

Learning by (guided) Discovery ?



Discovery intuitive static principles (for carpenters) ?



exploration

Learning by Discovery



Semi-Constructivism

There is a time for telling

No Over-expectation !

“Productive Failure”

Who's the most consistent striker?

Year	Mike Arwen	Dave Backhand	Ivan Right
1988	14	13	13
1989	9	9	18
1990	14	16	15
1991	10	14	10
1992	15	10	16
1993	11	11	10
1994	15	13	17
1995	11	14	10
1996	16	15	12
1997	12	19	14
1998	16	14	19
1999	12	12	14
2000	17	15	18
2001	13	14	9
2002	17	17	10

Comparing regularity

Mike Arwen : Mean = $\frac{280}{20}$
 = 14 goals / year
 Mode = 14

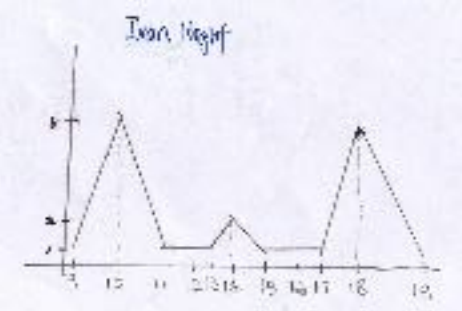
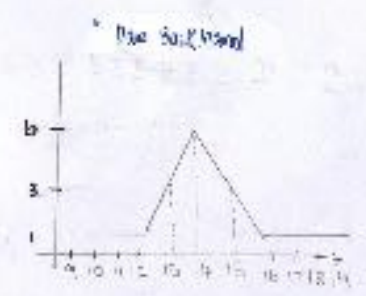
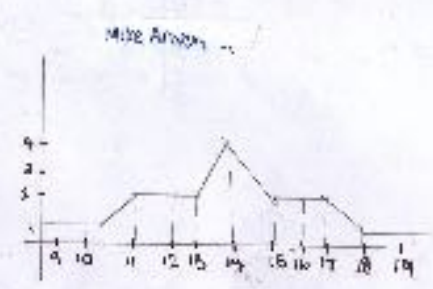
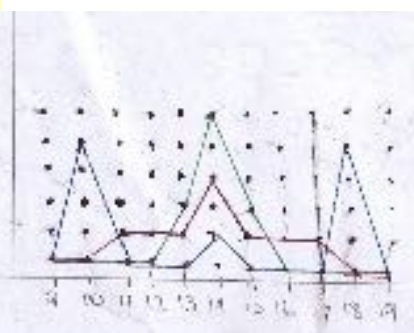
9	10	11	12	13	14	15	16	17	18	19
1	1	2	2	2	4	2	2	2	1	1

Dave Backhand : Mean = $\frac{280}{20}$
 = 14 goals / year
 Mode = 14

1	1	1	1	3	6	3	1	1	1	1
---	---	---	---	---	---	---	---	---	---	---

Ivan Right : Mean = $\frac{280}{20}$
 = 14 goals / year
 Mode = 18 and 10

1	5	1	1	1	2	1	1	1	5	1
---	---	---	---	---	---	---	---	---	---	---



9 10 11 11 12 12 13 13 14 14 14 14 15 15 16 16 17 17 18 19

From Question paper: Average = $\frac{280}{20}$

Mike has 8 years < average

4 years = average

8 years > average

Dave has 7 years < average

6 years = average

7 years > average

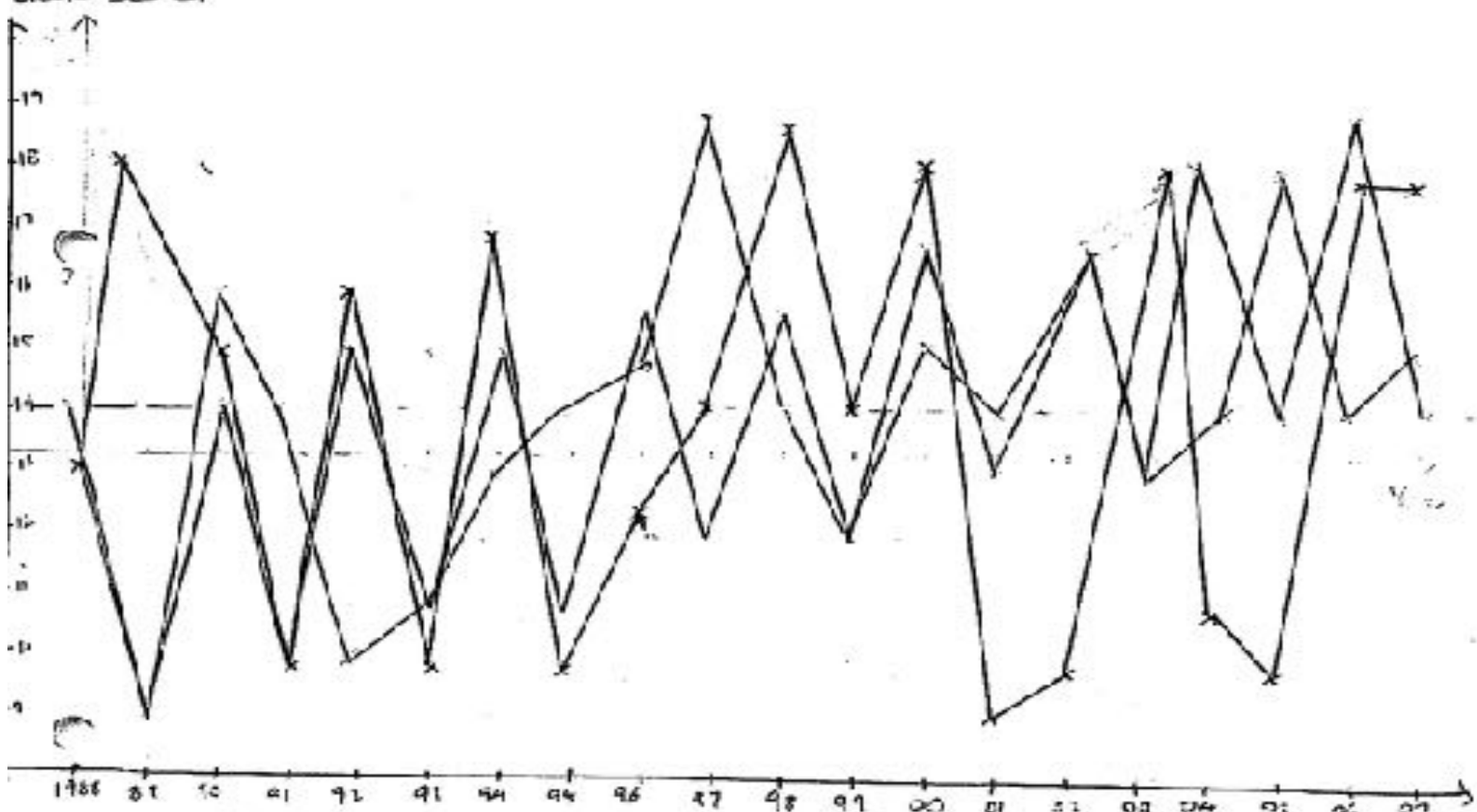
Ivan has 9 years < average

2 years = average

9 years > average

**Frequency of years
above, below, and at
average**

Consistency = years at the
mean / years away from the
mean



- Mike Arsen
- ... Dave Backlund
- - - Ivan Pight

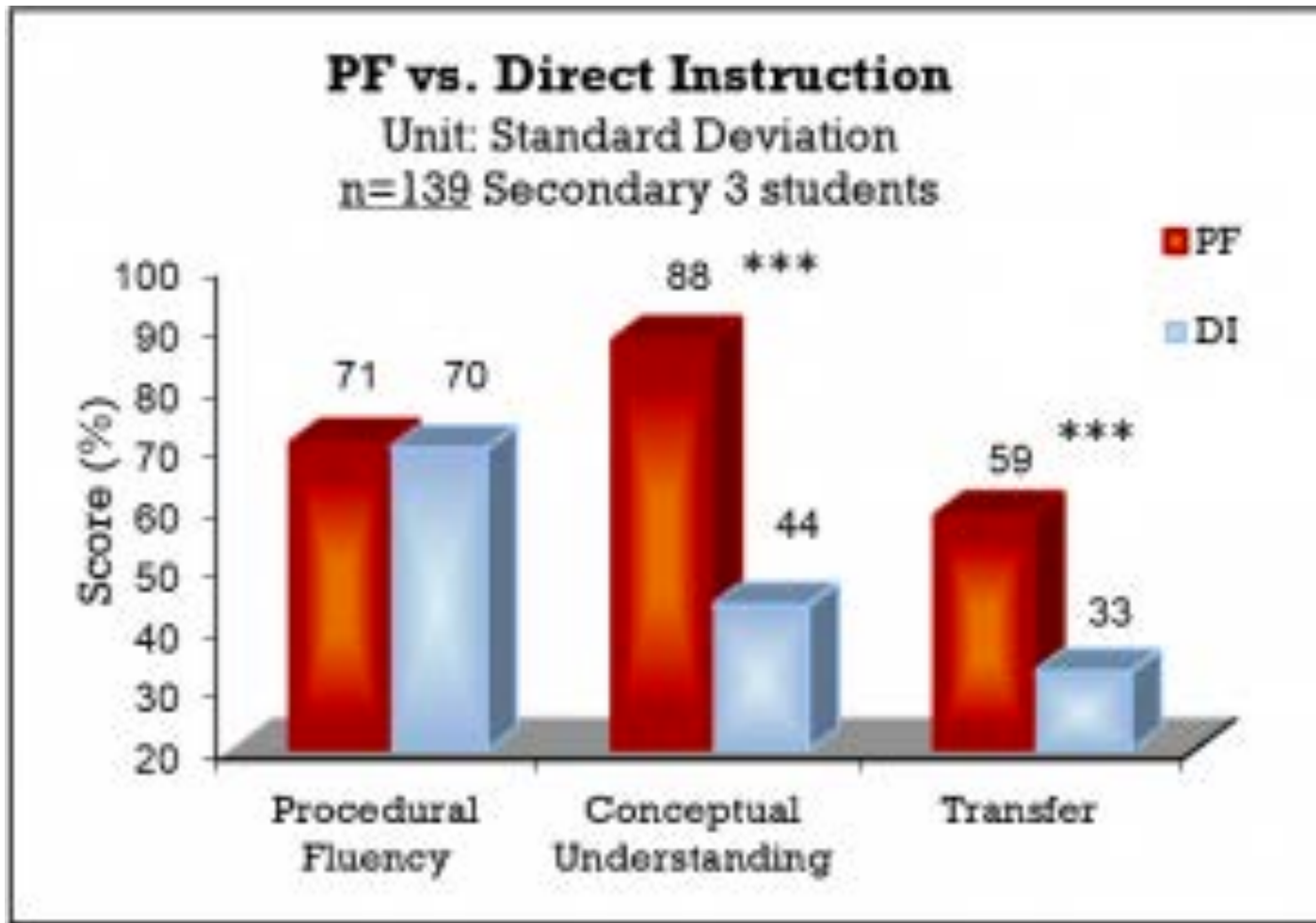
Idea 3 Measure Graph Length

$$\begin{aligned}
 MA & \sqrt{2} + \sqrt{2} = 83.26 \\
 DB & \sqrt{2} + \sqrt{2} = 56.4 \\
 IR & \sqrt{2} + \sqrt{2} = 94.54
 \end{aligned}$$

∴ Dave Backlund is the most consistent player as he has the shortest 'stretch-and-act' graph, staying consistently near 10.

Azad
Aitken

3



Constructivism \neq Teacherless

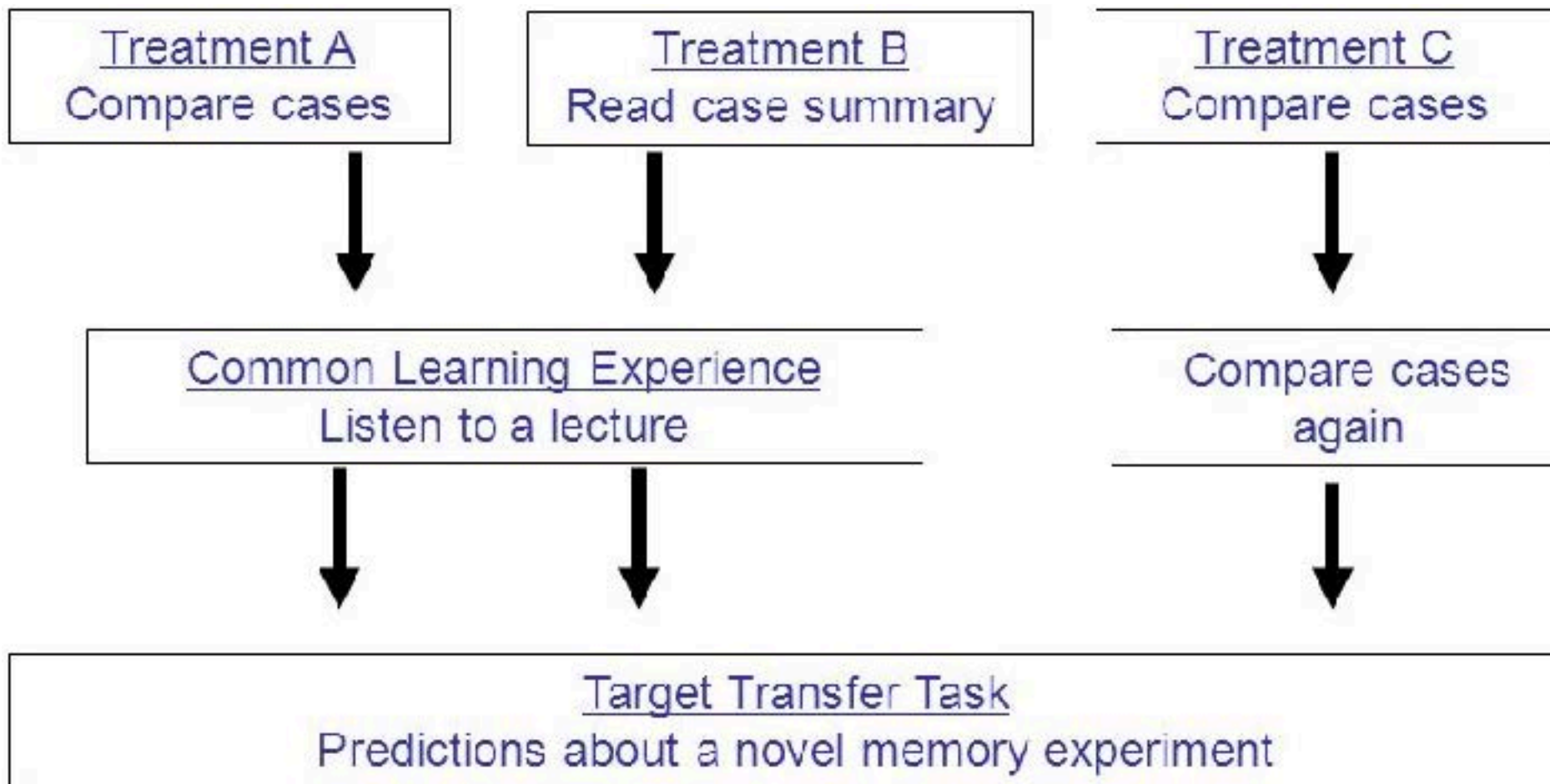
There is a time for telling



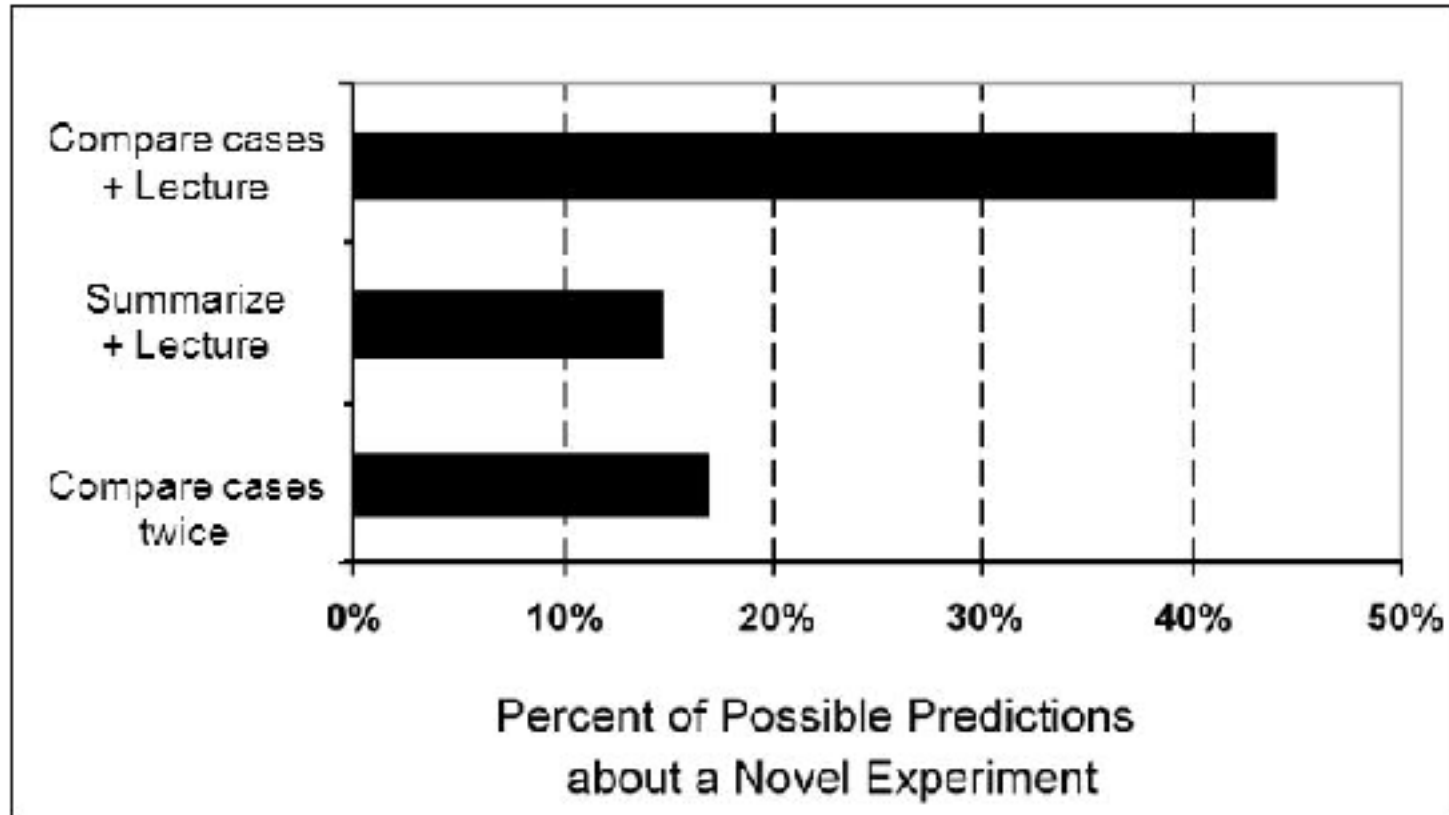
Exploration

Consolidation

« Contrasting Cases »



« Contrasting Cases »



There is a time for telling



How to guide learners ?

[Don't imitate Monthly Python](#)

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Exploration

Consolidation

1. Carefully design the data set
2. Comparisons, playing with differences
3. Conflict: trapping predictions
4. Advance organizers (metaphors,...)
5. Pushing reflection

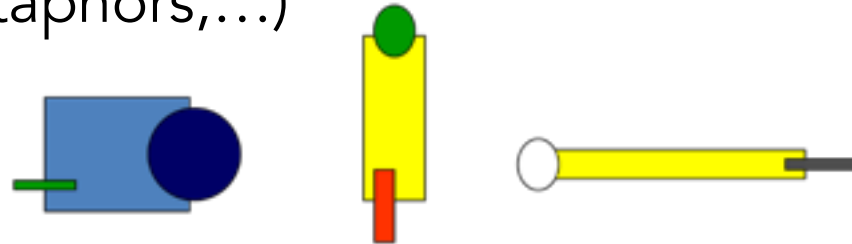


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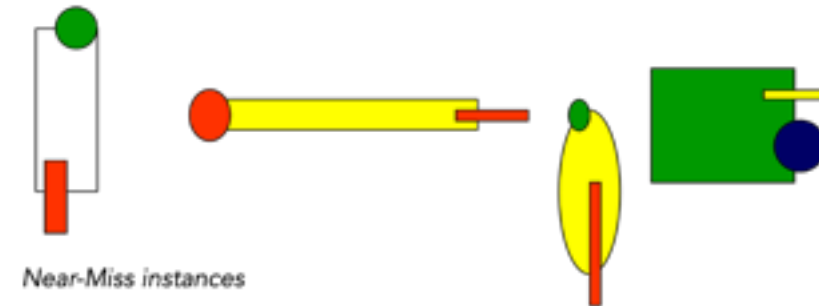
Exploration

Consolidation

1. Carefully design the data set
- 2. Comparisons, playing with differences**
3. Conflict: trapping predictions
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Positive instances



Near-Miss instances

Negative instances

Gloria and Tim were asked to solve $5(x + 3) = 20$.

Gloria's "distribute first" way

Tim's "divide first" way

First I distributed.

Then I subtracted on both sides.

I divided by 5.

Here is my answer

?

$$5(x + 3) = 20$$

$$5x + 15 = 20$$

$$5x + 15 = 20$$

$$-15 \quad -15$$

$$\frac{5x}{5} = \frac{5}{5}$$

$$x = 1$$



$$5(x + 3) = 20$$

$$\frac{5(x + 3)}{5} = \frac{20}{5}$$

$$x + 3 = 4$$

$$-3 \quad -3$$

$$x = 1$$



?

First I divided by 5.

Then I subtracted from both sides.


Here is my answer.

How did Gloria and Tim find the solution to the equation?

Which method is better? What are some important differences between Gloria's "distribute first" method and Tim's "divide first" method?

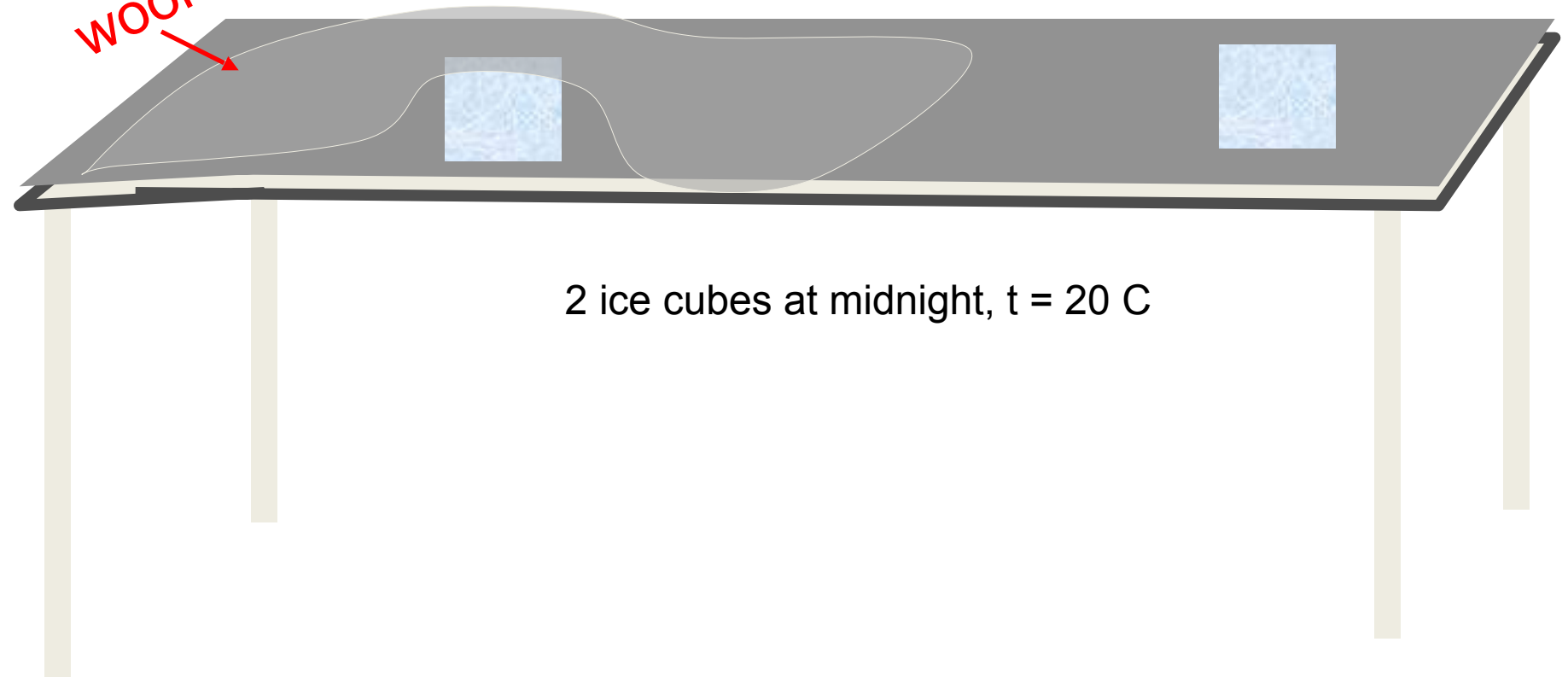
Exploration

Consolidation

- 
1. Carefully design the data set
 2. Comparisons, playing with differences
 - 3. Conflict: trapping predictions**
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Trapping misconceptions

wool



2 ice cubes at midnight, $t = 20\text{ C}$

Which ice cube will melt faster ?

Exploration


Consolidation

1. Carefully design the data set
2. Comparisons, playing with differences
3. Conflict: trapping predictions
- 4. Advance organizers (metaphors,...)**
5. Pushing reflection



Exploration

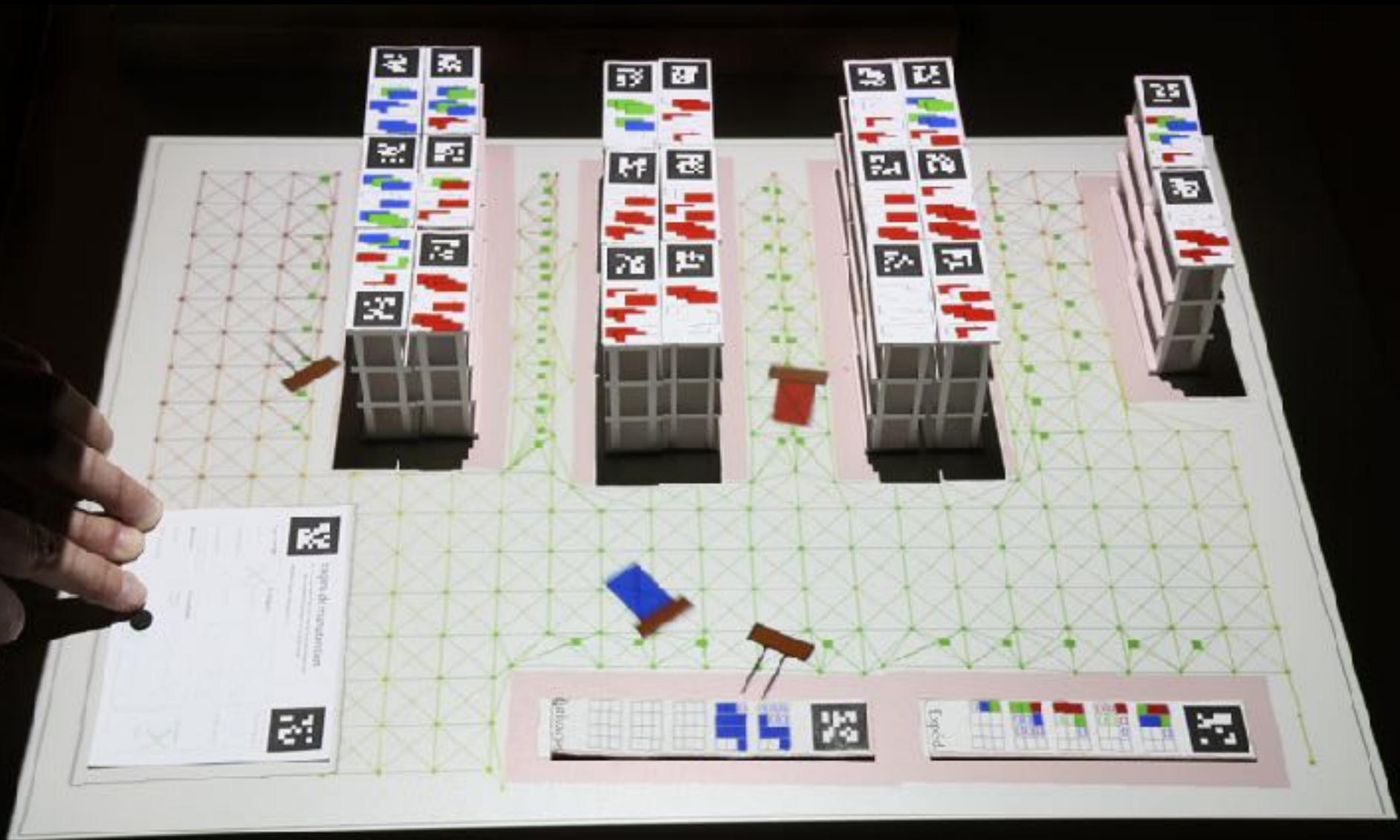
Consolidation

- 
1. Carefully design the data set
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Apprentissage



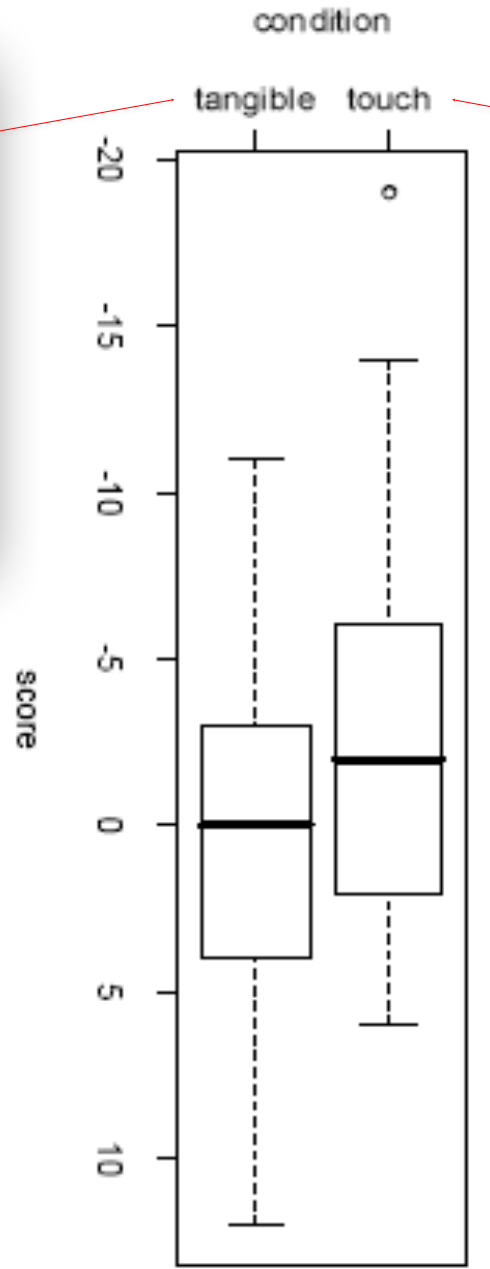


The TinkerLamp



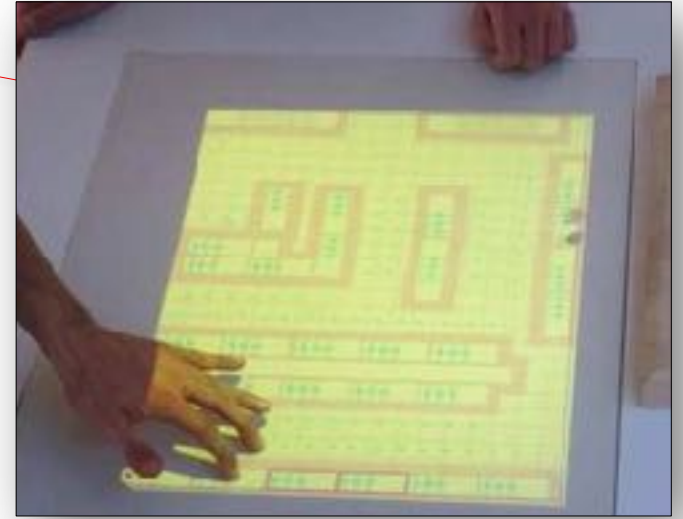
The logo for Simpliquity features a stylized circular icon on the left, composed of two concentric rings in shades of green and grey. To the right of the icon, the word "Simpliquity" is written in a clean, grey, sans-serif typeface.

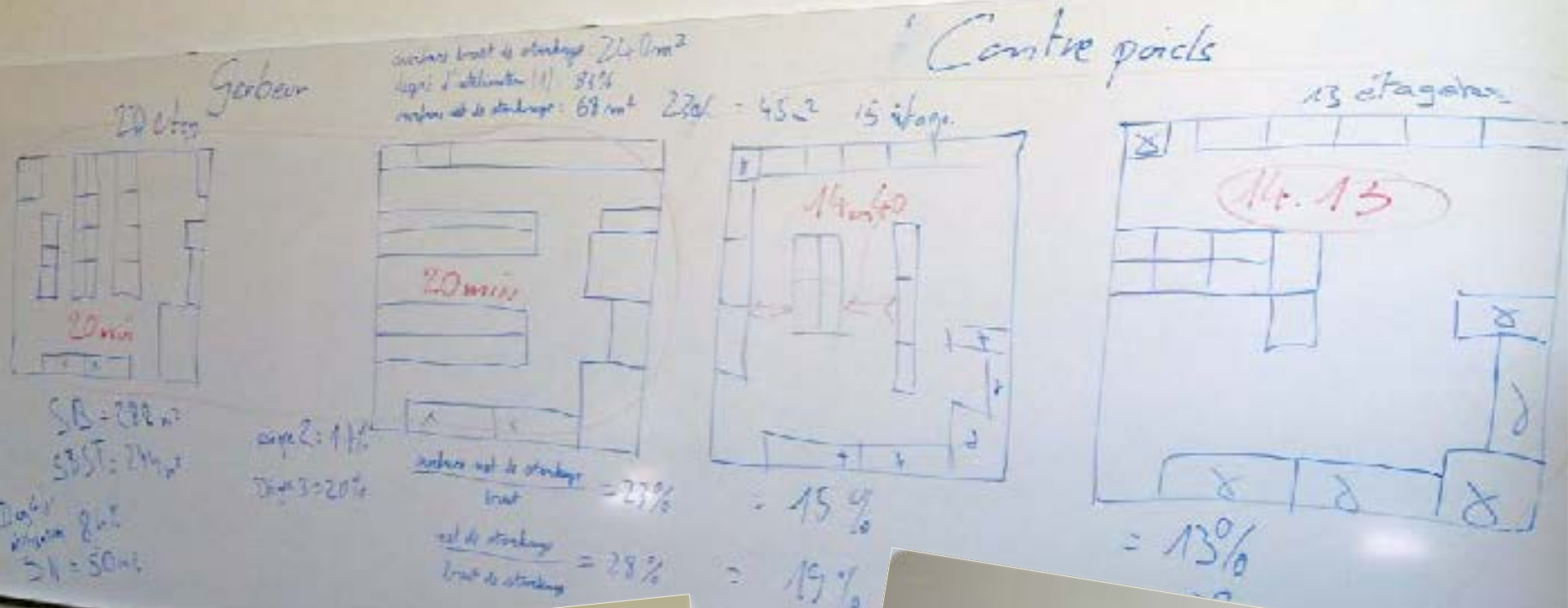
Simpliquity



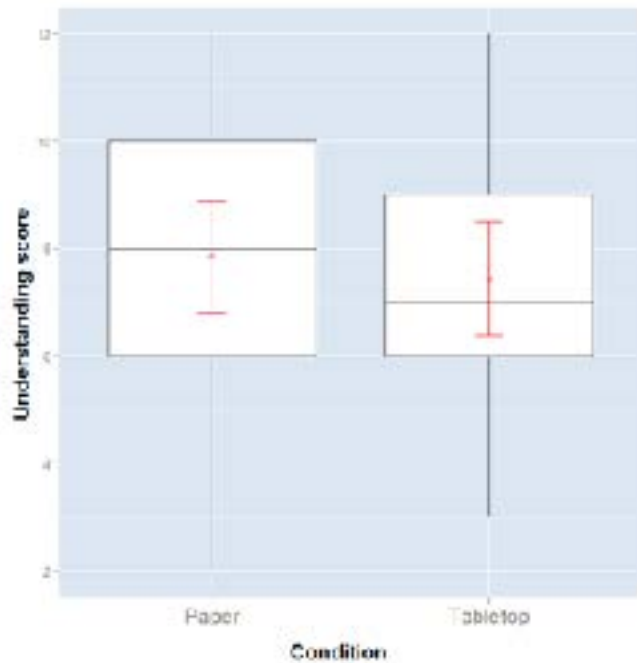
$F(1,37) = 6.68, p < .05$

Learning gain



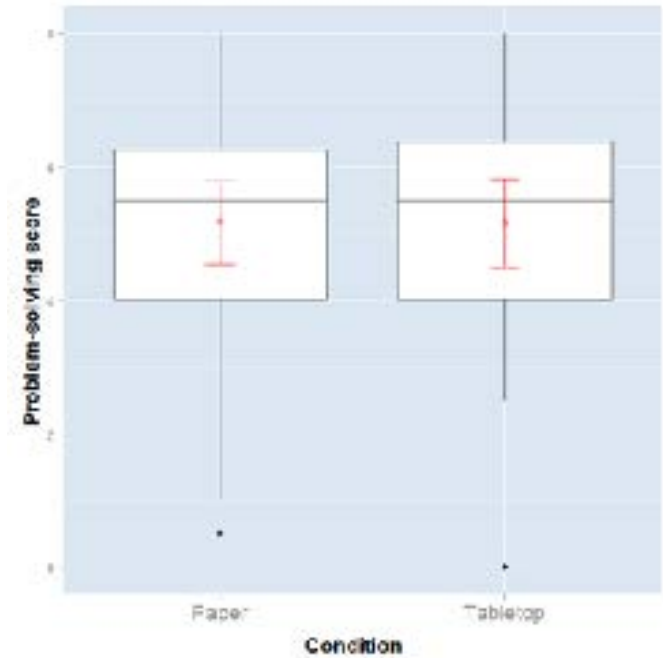


No sign. effect in
understanding



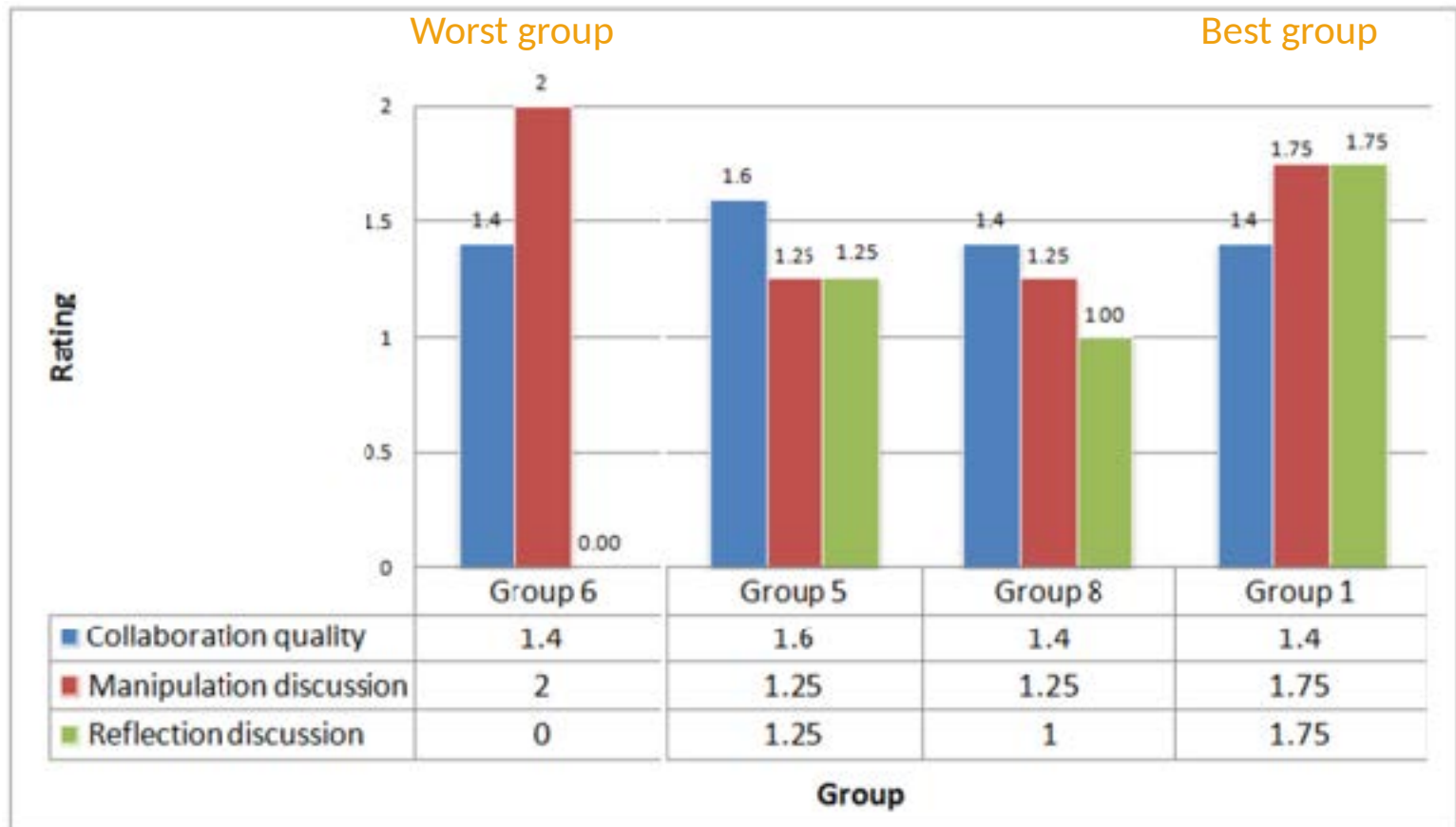
mean = 7.84 vs. mean = 7.43
 $F(1,14) = .25; p > .05$

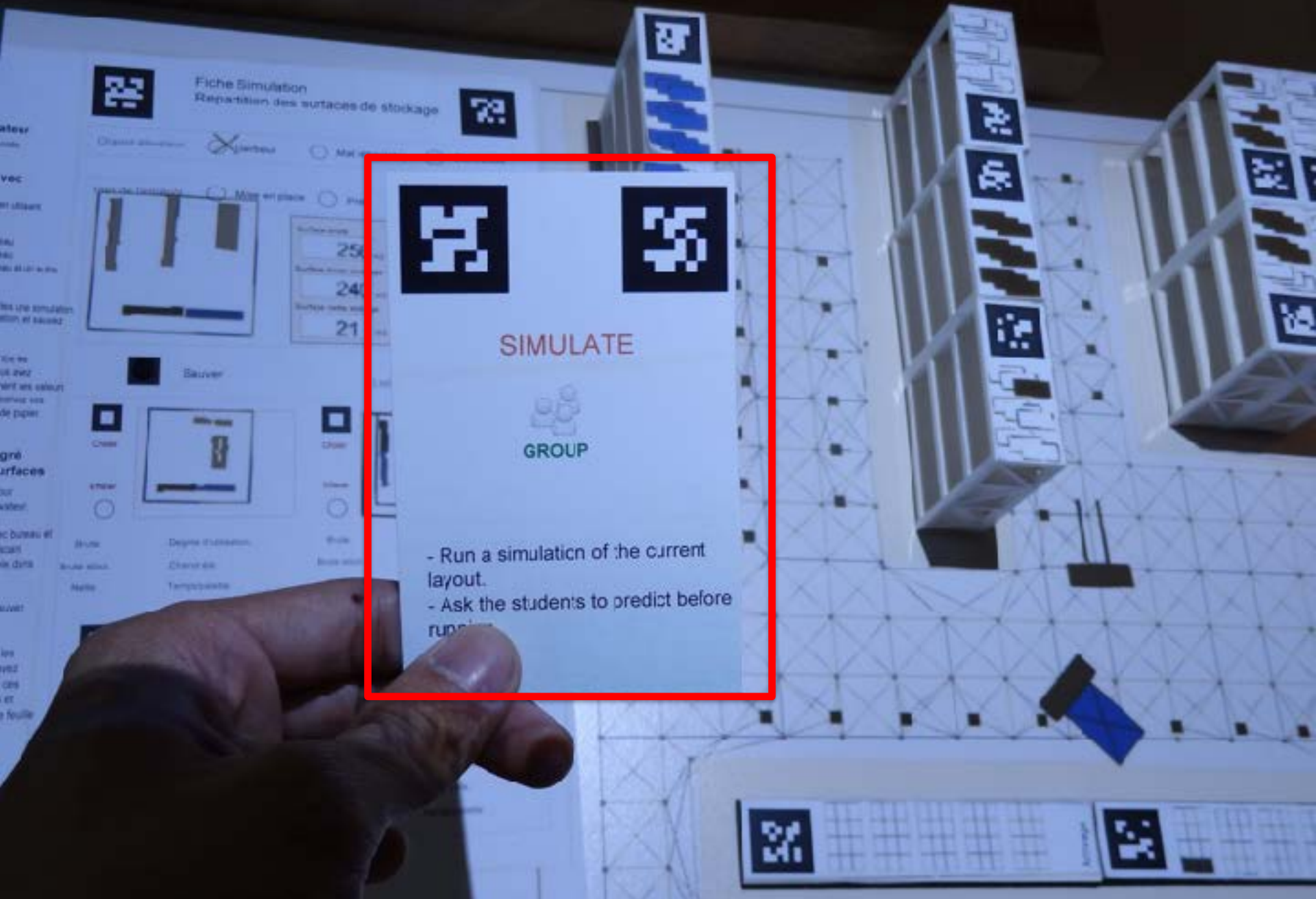
No sign. effect in
problem-solving



mean = 5.16 vs. mean = 5.15
 $F(1,14) = .06, p > .05$

"Tentation de manipulation"





Fiche Simulation
Repartition des surfaces de stockage



SIMULATE



- Run a simulation of the current layout.
- Ask the students to predict before running...

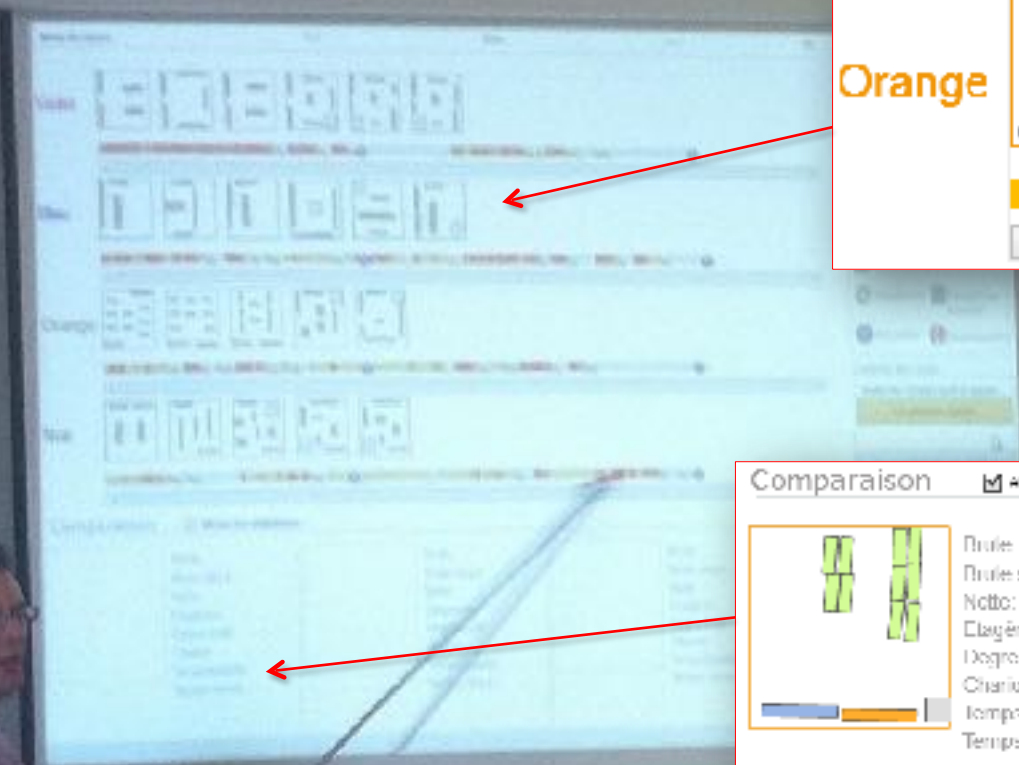


PAUSE CLASS

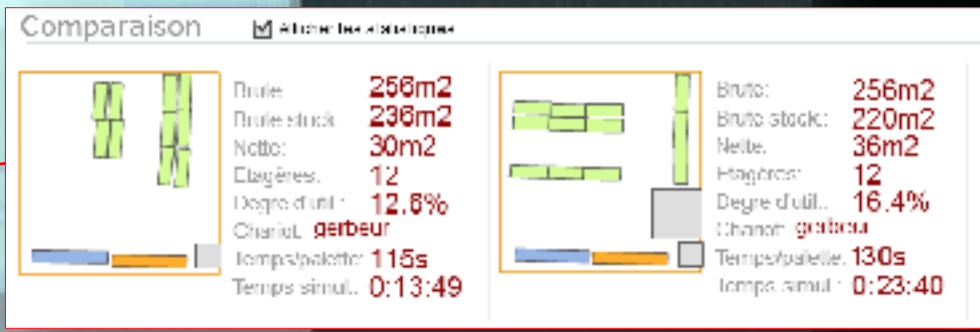


CLASS

- Pause all the actions (simulation, building model, etc.) in the whole class

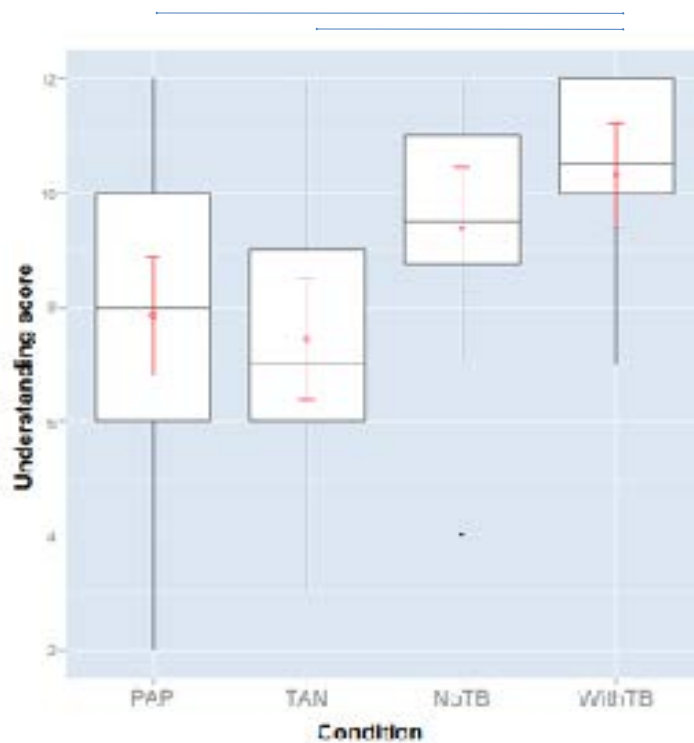


Orange

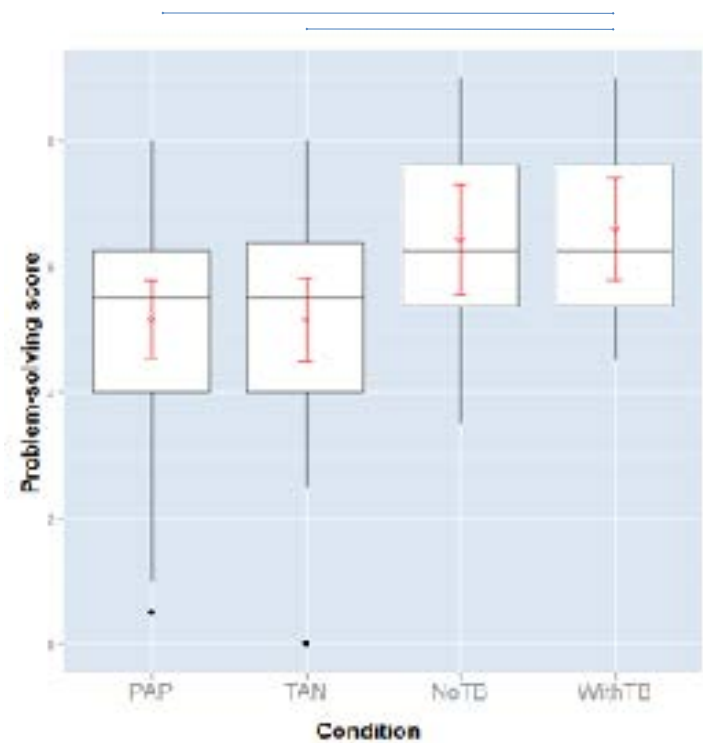


Post-test

Sign. effect in understanding



Sign. effect in problem-solving



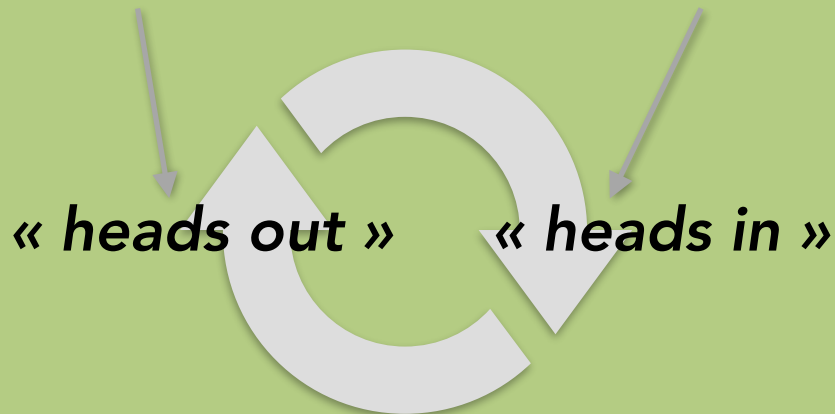
Measures	Warehouse study's conditions		Evaluation of TinkerLamp 2.0 conditions	
	Paper/pen	TinkerLamp 1.0	TinkerLamp 2.0 With TinkerBoard	TinkerLamp 2.0 No TinkerBoard
<i>Understanding score</i>	7.94(2.05)	7.43(2.02)	9.39(2.03)	10.31(1.70)
<i>Problem-solving score</i>	5.16(1.70)	5.15(1.78)	6.44(1.65)	6.59(1.53)

Exploration

Consolidation

1. Carefully design the data set
2. Comparisons, playing with differences
3. Conflict: trapping predictions
4. Advance organizers (metaphors,...)
5. **Pushing reflection**

Reflection turns experience into knowledge



How do people learn? →

Which technology for learning?

Jean Piaget

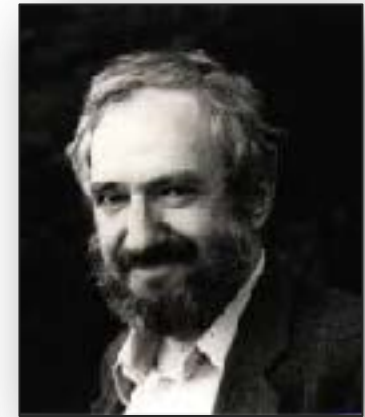


Scheme



Object to
think with

To implement a complex
program, I can decompose it
into sub-problems



Seymour Papert

Function/method in
programming language

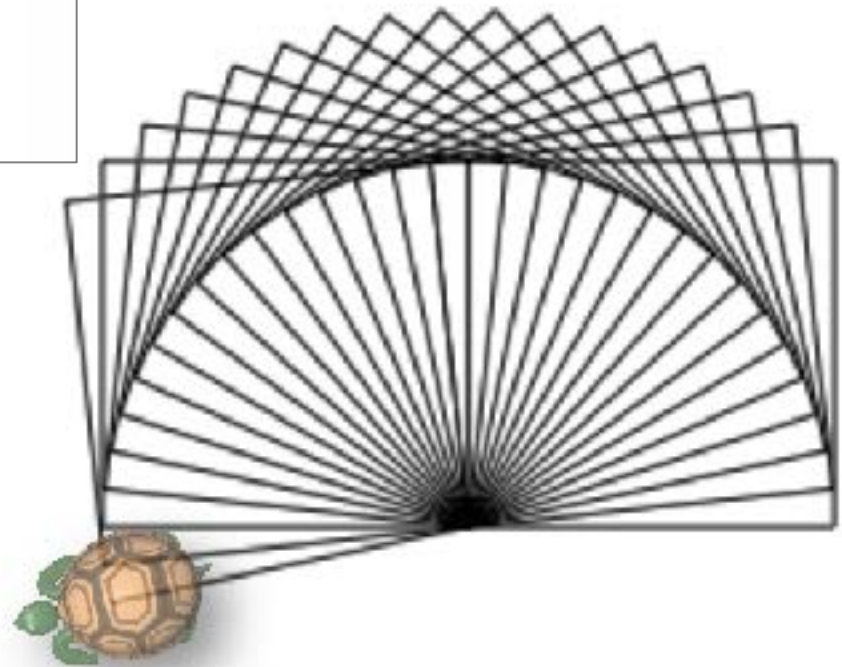
If I cannot reach object A, I
can take object B that
connects my hand to A

« MICROWORLD »

```
ExoLogO
define "carre [[size]
[repeat 4 [forward :size wait 0.1 right 90]]

define "fleur [[size]
[clean repeat 60 [carre :size left 6]]

fleur 100
```

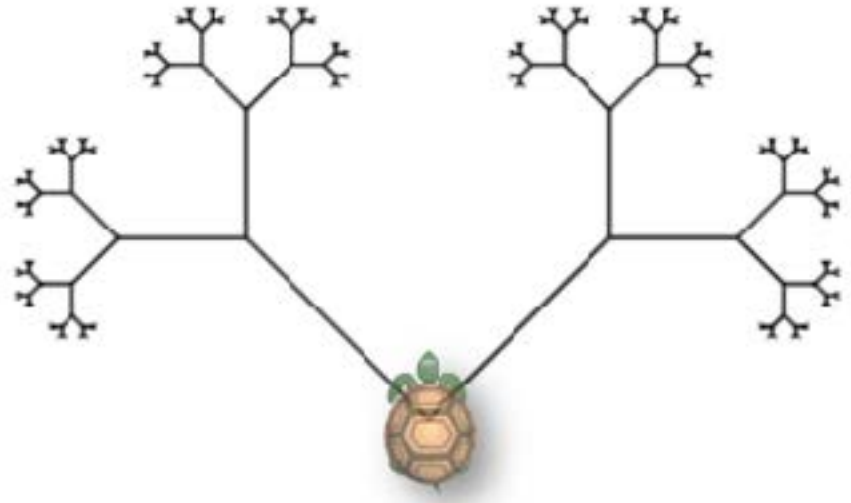


<http://www.alancsmith.co.uk/logo/>

```

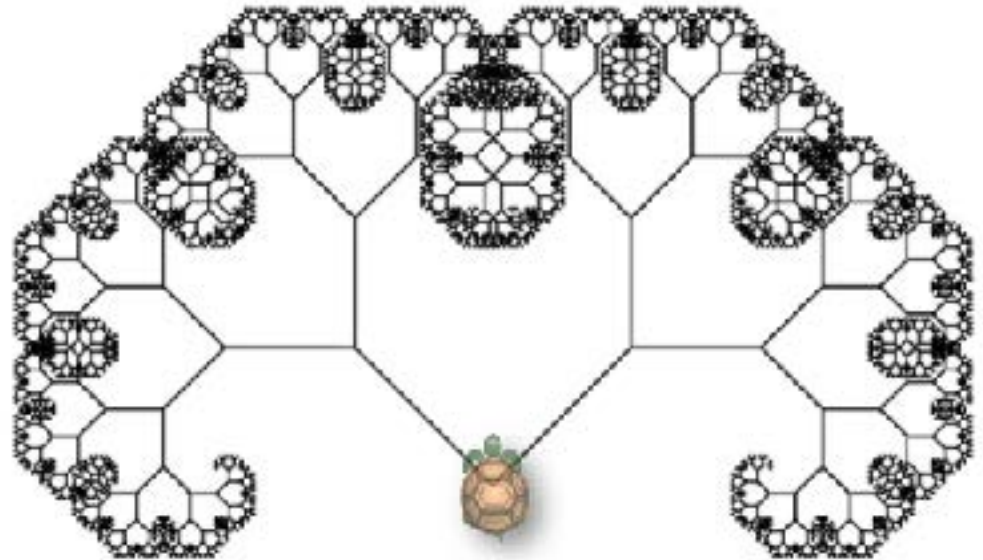
define "Zum" [[length divider]
  [if :length < 1
    [stop]
    [ left 45
      forward :length
      zum :length/:divider :divider
      back :length
      right 90
      forward :length
      zum :length/:divider :divider
      back :length
      left 45
    ]
  ]
]

```



zum 100 2

zum 100 1.5

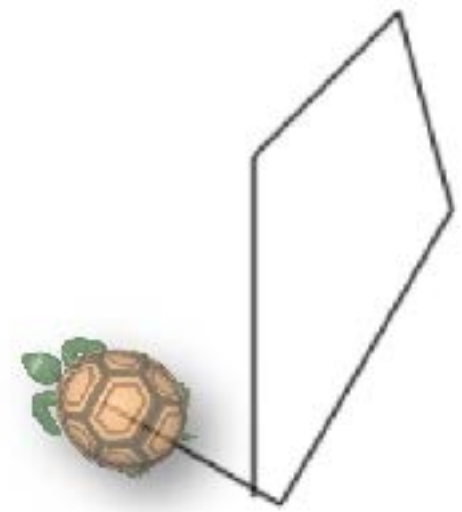


Cognitive Conflict as key learning mechanism

(1) I want to get this



(2) I got that



```
define "house1 [[ ]  
  [forward 100  
    right 45  
    forward 60  
    right 120  
    forward 60  
    right 45  
    forward 100  
    right 90  
    forward 60  
  ]]
```



(3) The problem is here

METACOGNITION

Cognitive Conflict as key learning mechanism

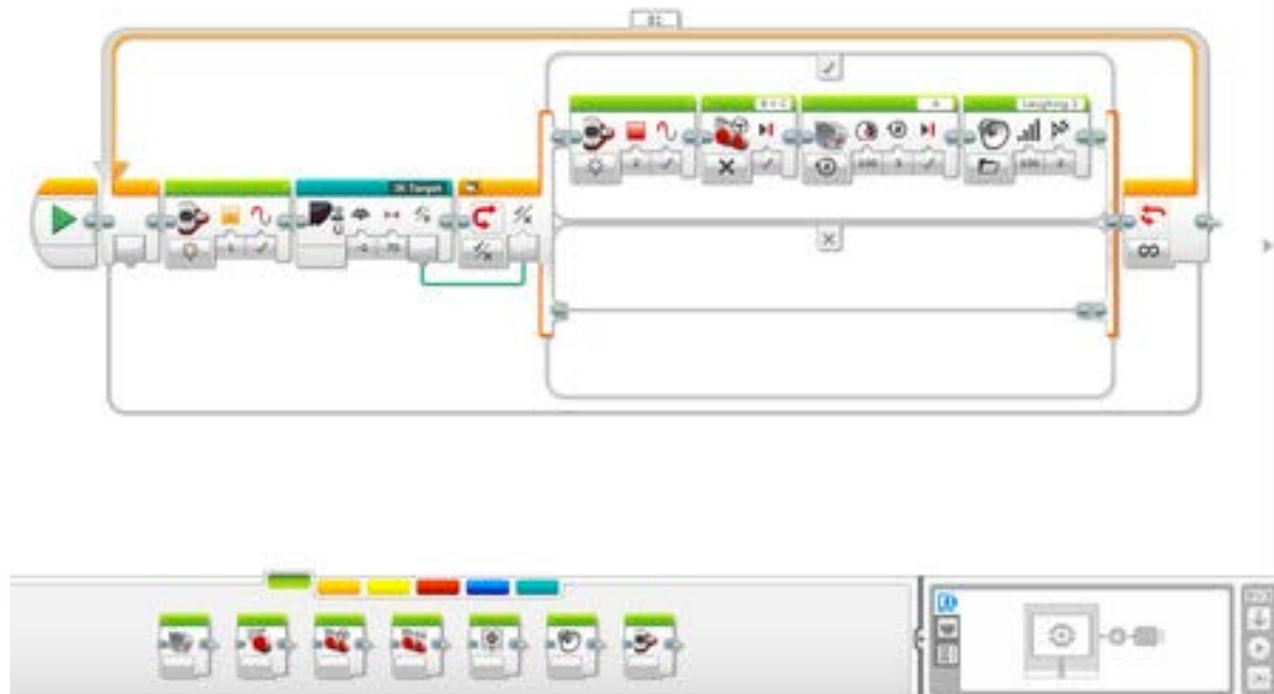
- Learning from experience
- Learning by doing
- Learning from failure
- Discovery learning

Conditions:

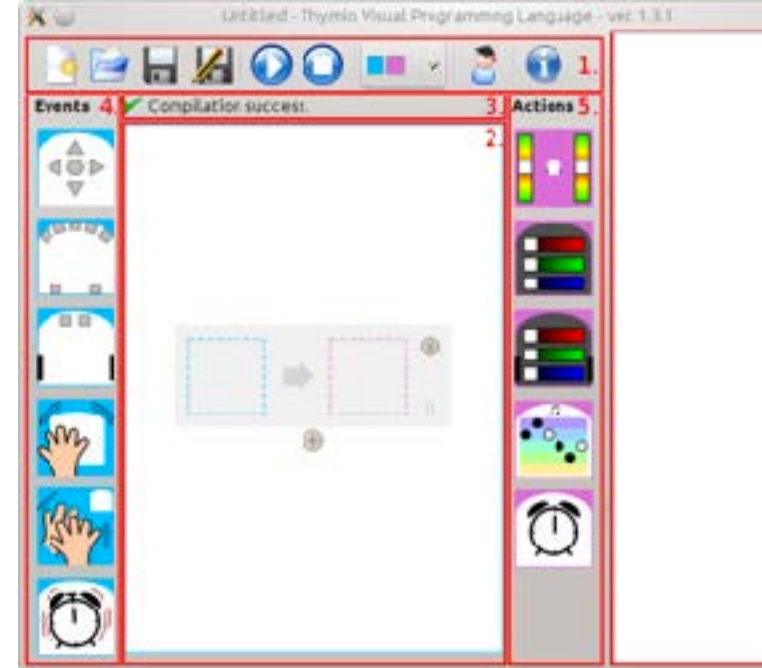
1. The conflict is detected
2. The learner finds how to solve it

Role of the environment (sequence of projects / teacher / peer)

constructivism → **constructionnism**



THYMIO



<https://aseba.wikidot.com/fr:thymiovgl>

<https://www.youtube.com/watch?v=8RiEDT8bsOs>



constructivism →
constructionism

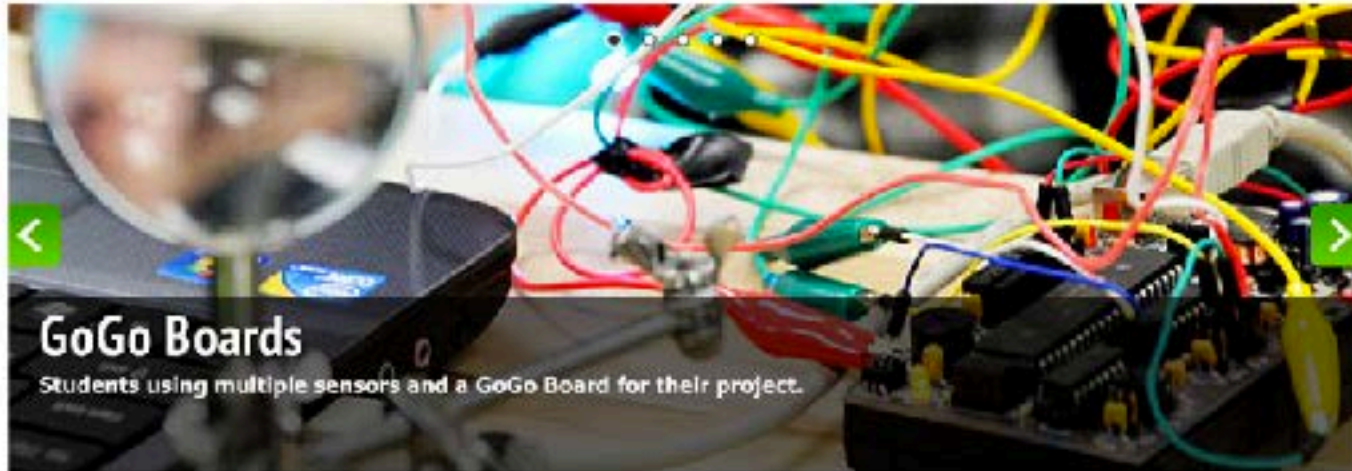
<http://guerrillamakerspace.squarespace.com/space-4/>



Digital Fabrication
and Hands-on Learning in Education

<http://fablabatschool.org/>

[About](#) [Blogs](#) [Photos](#) [Projects](#) [Resources](#)



GoGo Boards

Students using multiple sensors and a GoGo Board for their project.

FabLab@School

A growing network of educational digital fabrication labs that put cutting-edge technology for design and construction - such as 3D printers and laser cutters - into the hands of middle and high school students.

WORKSHOP @ IDC 2013

A half-day workshop on Digital Fabrication and Making in Education will take place on Monday afternoon, June 24th, 2013.

This is a satellite event of the 12th International Conference on Interaction Design and Children - IDC 2013.

Projects

Check out past student projects!



Resources

Find useful link, activities, and tutorials here!



FabLabs@School
Around the World

- [CASTILLEJA SCHOOL](#)
- [RUSSIA](#)
- [STANFORD](#)
- [THAILAND](#)
- [How to Get a FabLab@School](#)



<http://www.3ders.org/articles/20120701-fayetteville-free-library-launched-3d-printing-fab-lab.html>

From constructivism to **constructionnism**



Seymour Papert, MIT



« *Radical* » *branch*

The scandal of education is that every time you teach something, you deprive a [student] of the pleasure and benefit of discovery.

I think schools generally do an effective and terribly damaging job of teaching children to be infantile, dependent, intellectually dishonest, passive and disrespectful to their own developmental capacities.

Every maker of video games knows something that the makers of curriculum don't seem to understand. You'll never see a video game being advertised as being easy. Kids who do not like school will tell you it's not because it's too hard.

Constructivism

Microworlds

Radical

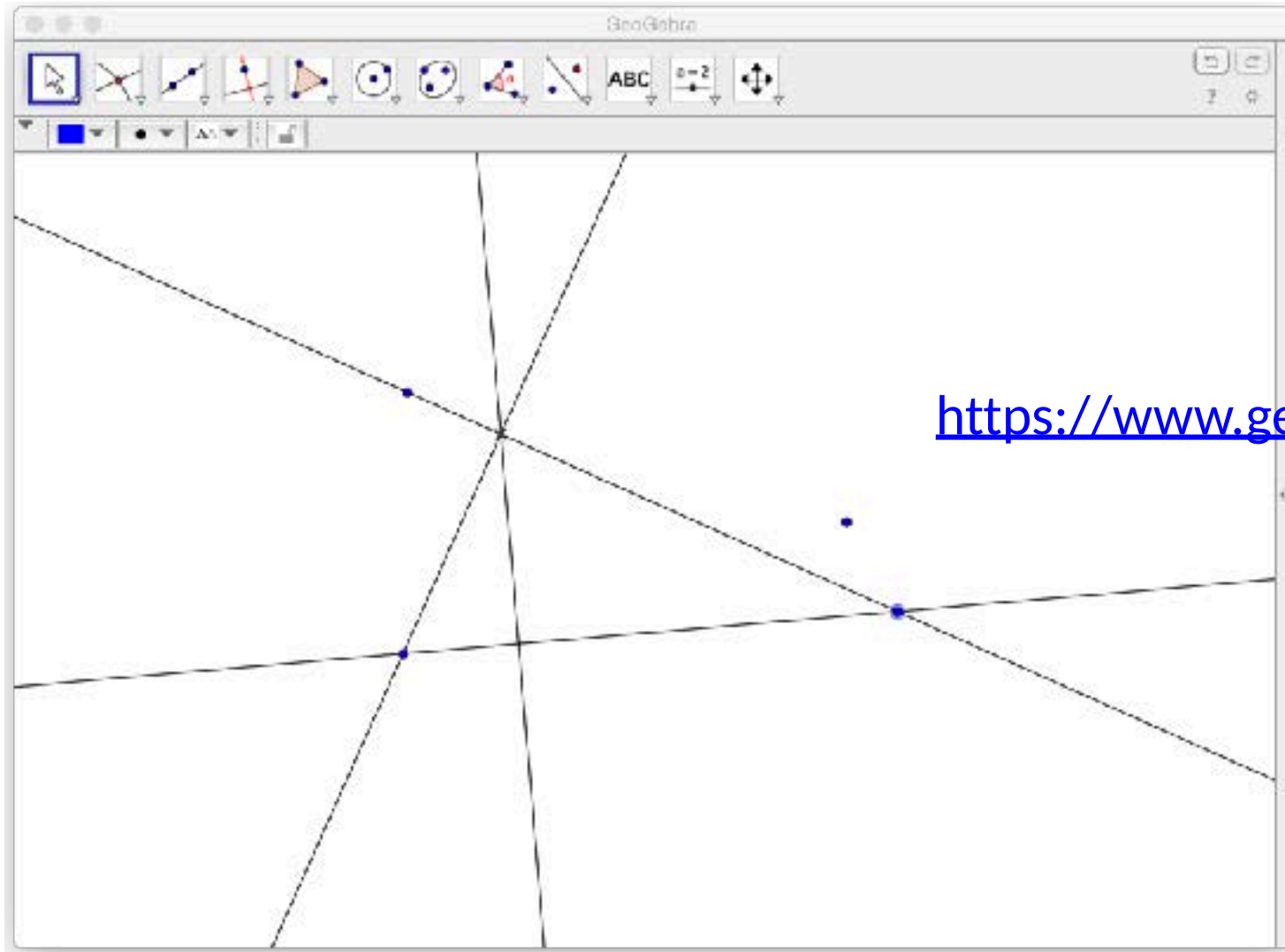
Quest for effectiveness

Constructionism

Guided Discovery

- *Content-rich microworlds*
- *Simulations*
- *Modelling*

Quest for effectiveness: Adding Contents

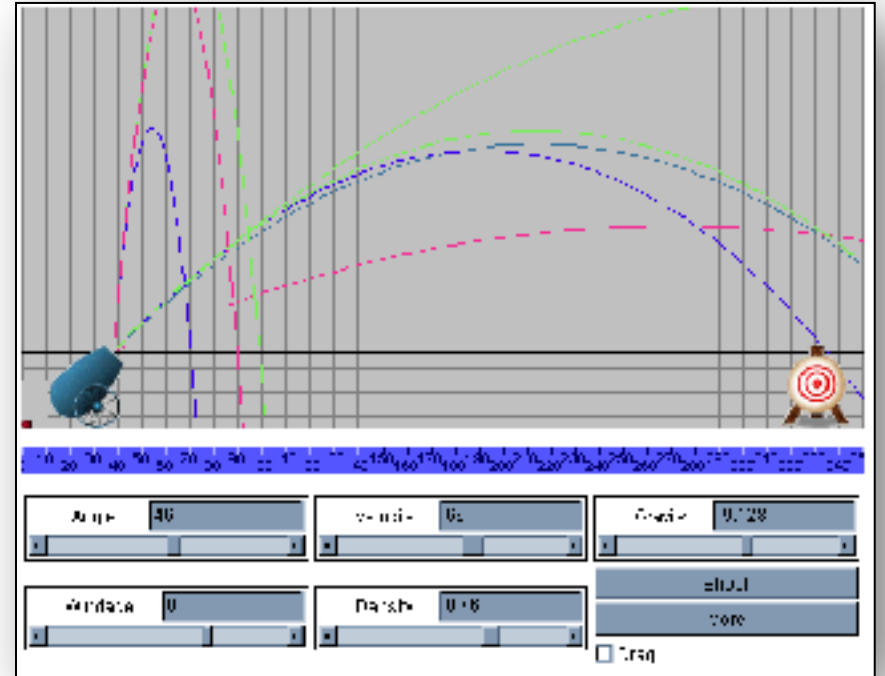


<https://www.geogebra.org/>

Learning from Simulations



Acquire Skills



Discover underlying model

NET LOGO

view updates
 on ticks
 Settings...

normal speed

setup

basic sliders:

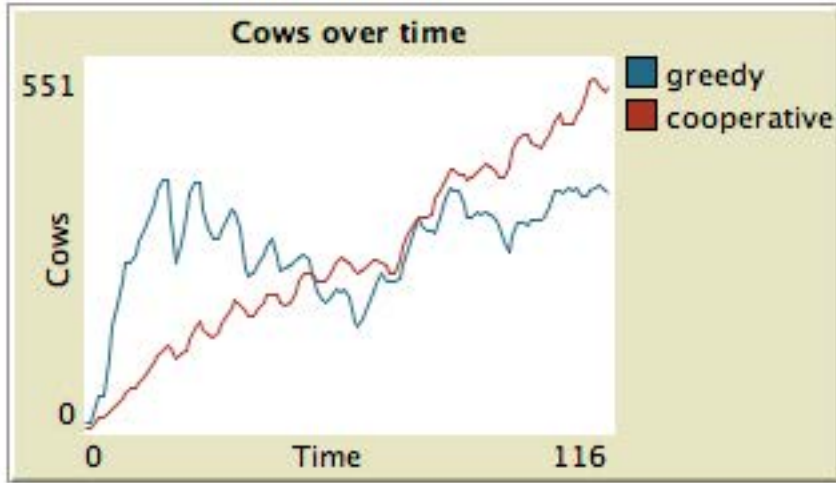
go

initial-cows 20 stride-length 0.08

cooperative-probability 0.50 metabolism 6

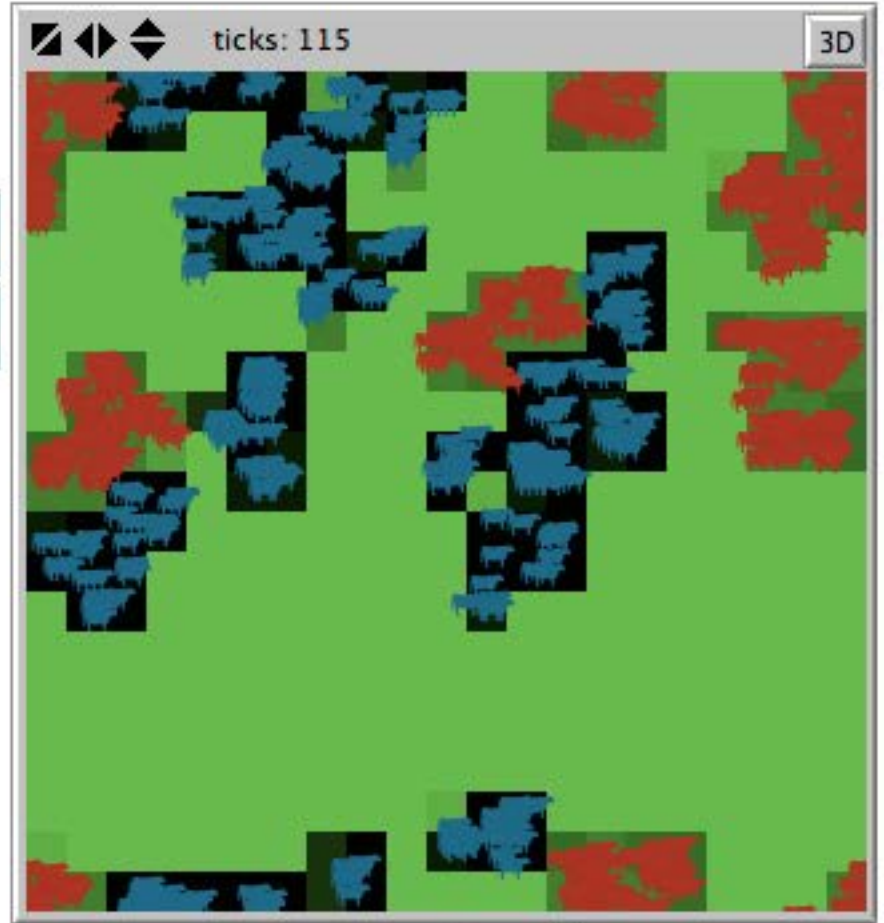
reproduction-cost 54

reproduction-threshold 102



greedy cows
353

cooperative cows
508



advanced sliders:

grass-energy 51

high-growth-chance 77 max-grass-height 10

low-growth-chance 30 low-high-threshold 5

Learning from Simulations

More [examples](#)

An Overview paper

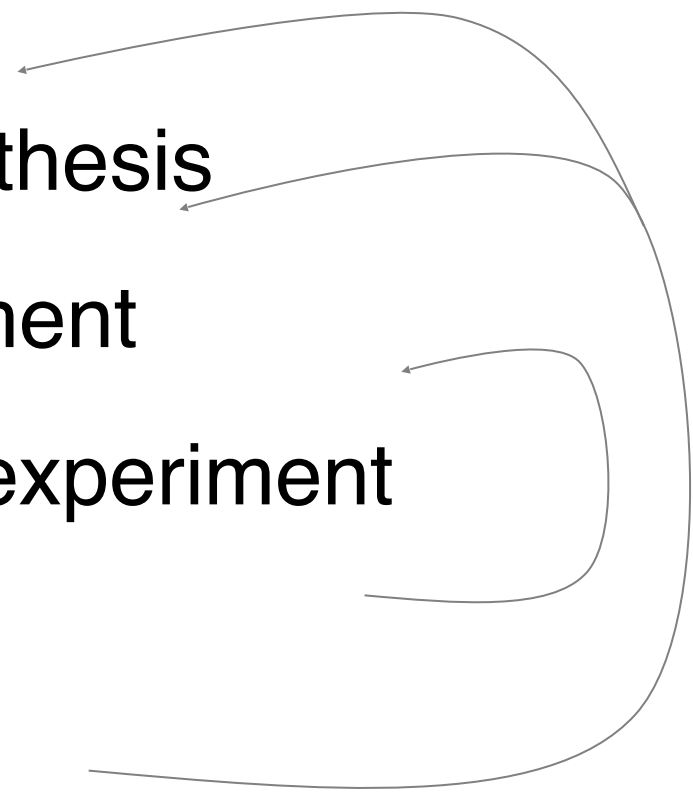
Inquiry learning

“Inquiry-based learning involves learners

- asking **questions** about the natural or material world,
- collecting **data** to answer those questions,
- making **discoveries** and
- **testing** those discoveries rigorously”

de Jong, 2006

Hypothetico-deductive reasoning

1. (Raise a question)
 2. Generate an hypothesis
 3. Design an experiment
 4. Run/simulate the experiment
 5. Interpret results
- 
- The diagram illustrates the iterative nature of the hypothetico-deductive process. It features five numbered steps. Curved arrows indicate feedback loops: one from step 2 back to step 1, one from step 3 back to step 2, one from step 4 back to step 3, and a larger one from step 5 back to step 1. This shows that at any stage, a researcher can return to a previous step if the current path is not fruitful.

But...

1. Question
 2. Hypothesis
 3. Design
 4. Run
 5. Interpret
- No clear hypothesis is formulated or badly formulated (42%), i.e. no relationship between variables
 - Design unconvincing experiments, students vary several parameters at at time
 - Confirmation bias: to design experience that confirm the hypothesis
 - 35% to 63% errors in data interpretation and graphics readings
-

And...

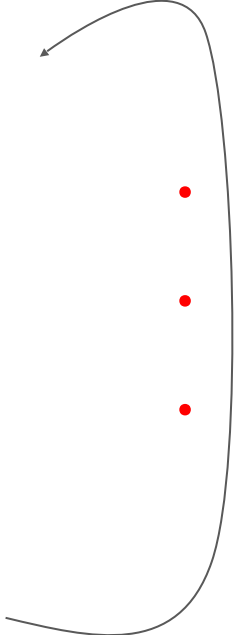
1. Question

2. Hypothesis

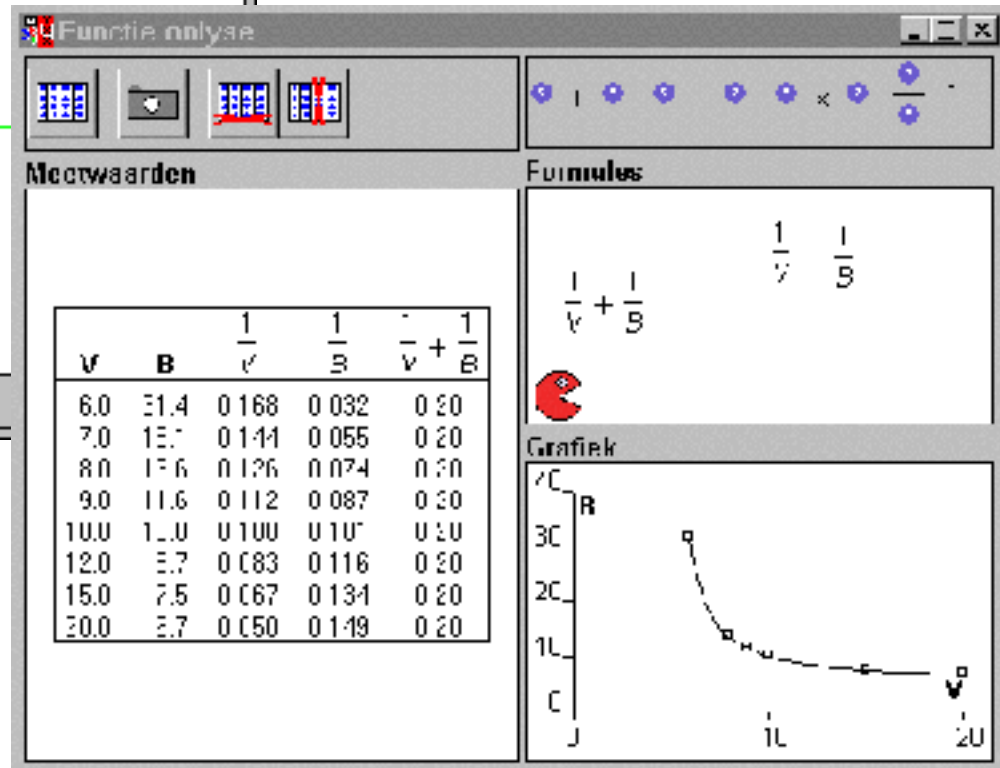
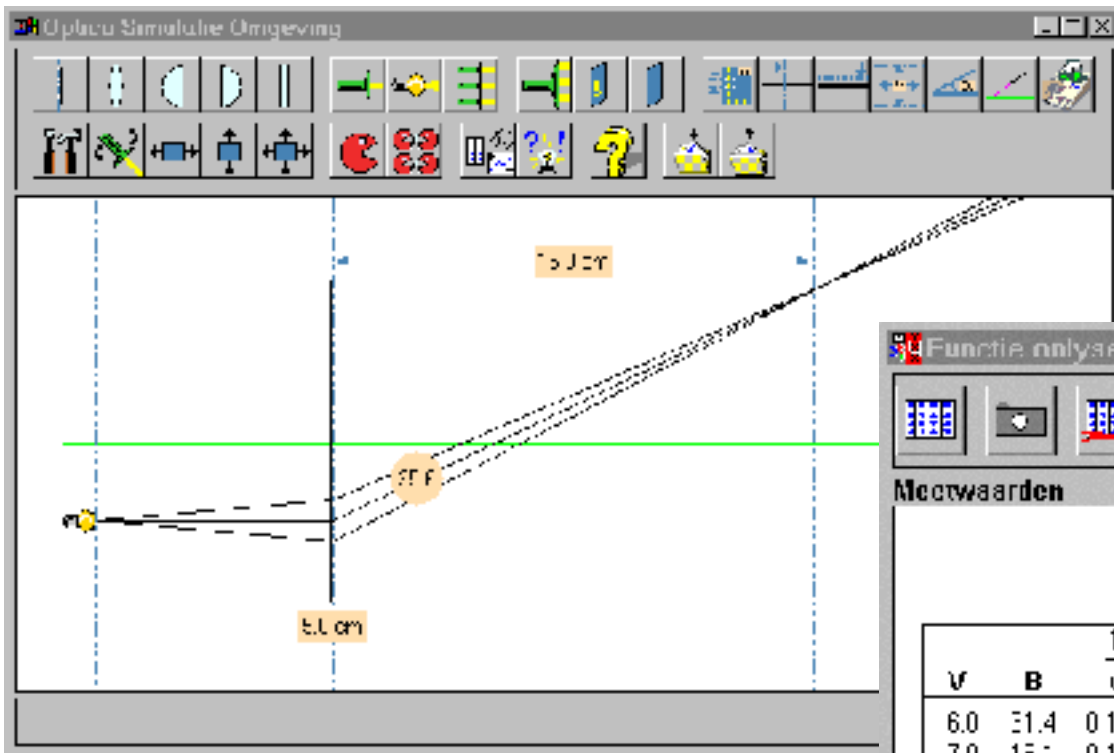
3. Design

4. Run

5. Interpret

- 
- Change several parameters
 - Keep hypothesis despite negative evidence
 - Reject hypothesis despite positive evidence

Example of **tools** to overcome these pitfalls



Tool to express hypotheses

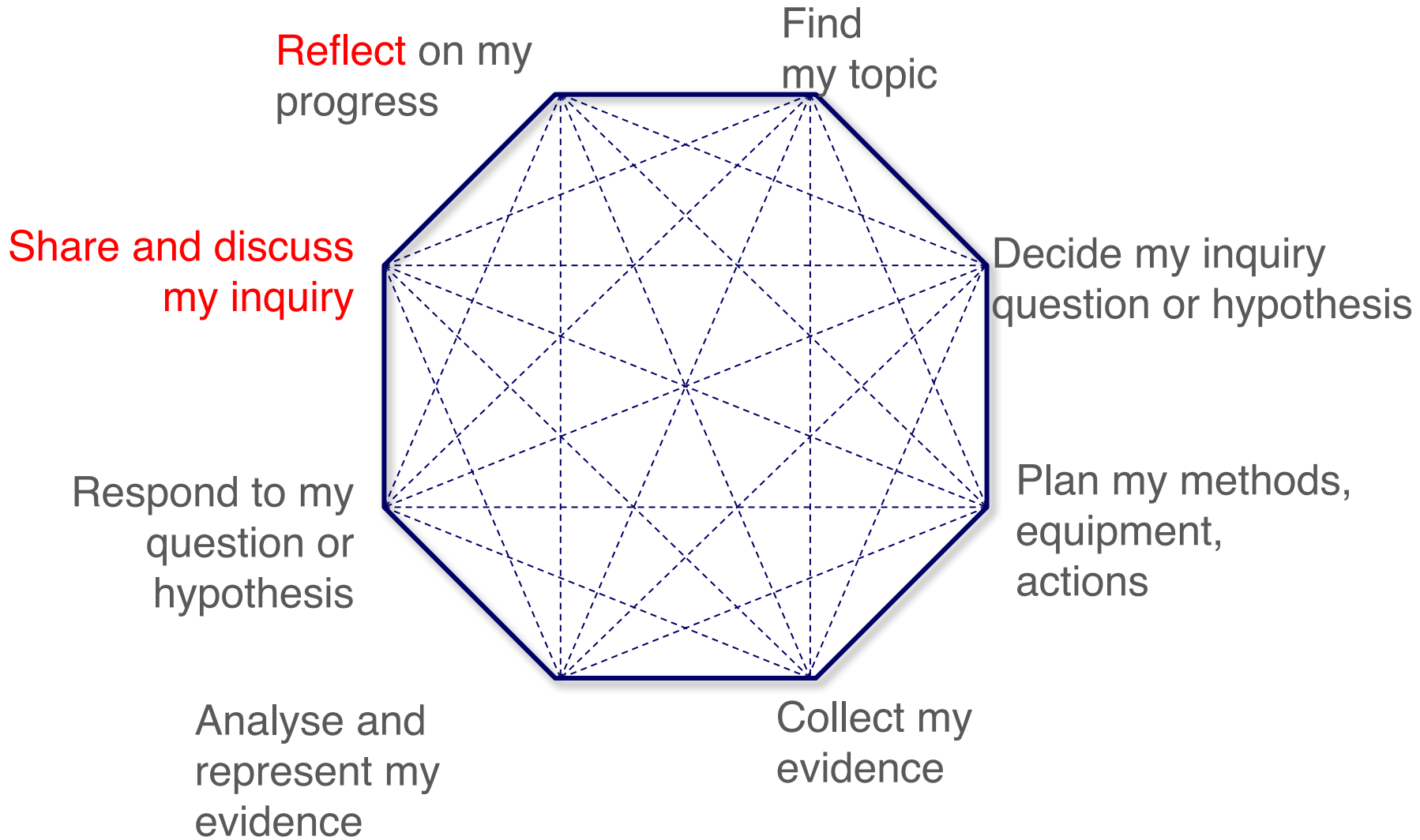
Example of **scenario** to overcome these pitfalls

- ① Ask students to write their hypothesis
- ② Find student with conflicting hypothesis
- ③ Ask them to find out with the simulation which hypothesis is right

The effects of any learning technology
depends upon the quality of
classroom **orchestration**

Cycle of engagement and reflection

by Mike Sharples, Open Universty



Inquiry is a more open process than simulations

A lesson is not inquiry based if:

- Students know what results they are supposed to get
- The questions and steps are pre-determined for them
- The teacher is working harder than the students

2 **Healthy Eating** Version ID: 0CTAQmaf@GUT 135a2905-638504660373

My progress: 1 - 2 **5**

Healthy Eating

An investigation of healthy diet and nutrients.

My inquiries > Healthy Eating > Collect my evidence > Food diary for 20.09.2010 (Breakfast) >

Food diary for 20.09.2010 (Breakfast)

4 **3**

Submitted by Amelia Student on Mon, 09/09/2010 - 11:34

1 **Navigation**

- Find my topic
- Decide my inquiry question or hypothesis
- Plan my methods, equipment & actions
- Collect my evidence
 - My data
- Analyze and represent my evidence
- Respond to my question or hypothesis
- Share and discuss my inquiry
- Reflect on my progress

Breakfast		Lunch	
			
Breakfast		Dinner	
Food	Portion Size	Food	Portion Size
Bread - Brown	3 slice(s)	Bread - Brown	3 slice(s)
Meat - Red	1 portion	Meat - Red	1 portion
Pulses (beans, lentils)	1 portion	Pulses (beans, lentils)	1 portion
Egg	2 portion	Egg	2 portion
		Meat - White	1 portion
		Vegetables	1 portion
Snack			
Food	Portion Size		
Veget	1 portion		

Sensors
3 cm Wave Signal Strength
AC Millivolt
Accelerometer 2 axis
Accelerometer 3 axis
Altimeter
Anemometer
Carbon Dioxide
Carbon Dioxide Replacement Cell
Carbon Monoxide
Carbon Monoxide Replacement Cell
Charge Sensor
Conductivity
Current ±1 A
Current ±1 mA
Current ±10 A
Current +100 mA
Distance IR
Distance Ultrasonic Basin
Electrosmog advanced
Electrosmog Basic
Flow Advanced
Flow Meter
Force Dual Range
Frequency
Humidity
IR Irradiance
Joulemeter
Light (Advanced)
Light (General Purpose)
Magnetic Field with 100mT Probe
Magnetic Probe 30 mT
Nitrogen Dioxide
Oxygen Atmospheric
Oxygen Atmospheric Cell
Oxygen Probe - Dissolved
pH Interface
pH Probe Sensor - advanced
pH Probe Sensor - basic
Pressure (Absolute 0 - 700 Kpa)
Pressure (Absolute 0 - 200 KPa)

Sharples, M., Collins, T., FeilssM., Gaved, M., Mulholland, P., Paxton, M., & Wright, M. (2011) A Laboratory of Knowledge-Making for Personal Inquiry Learning. Artificial Intelligence in Education.



ScienceScope

Linking ICT With Science Education

Constructivism

Microworlds

Radical

Quest for effectiveness

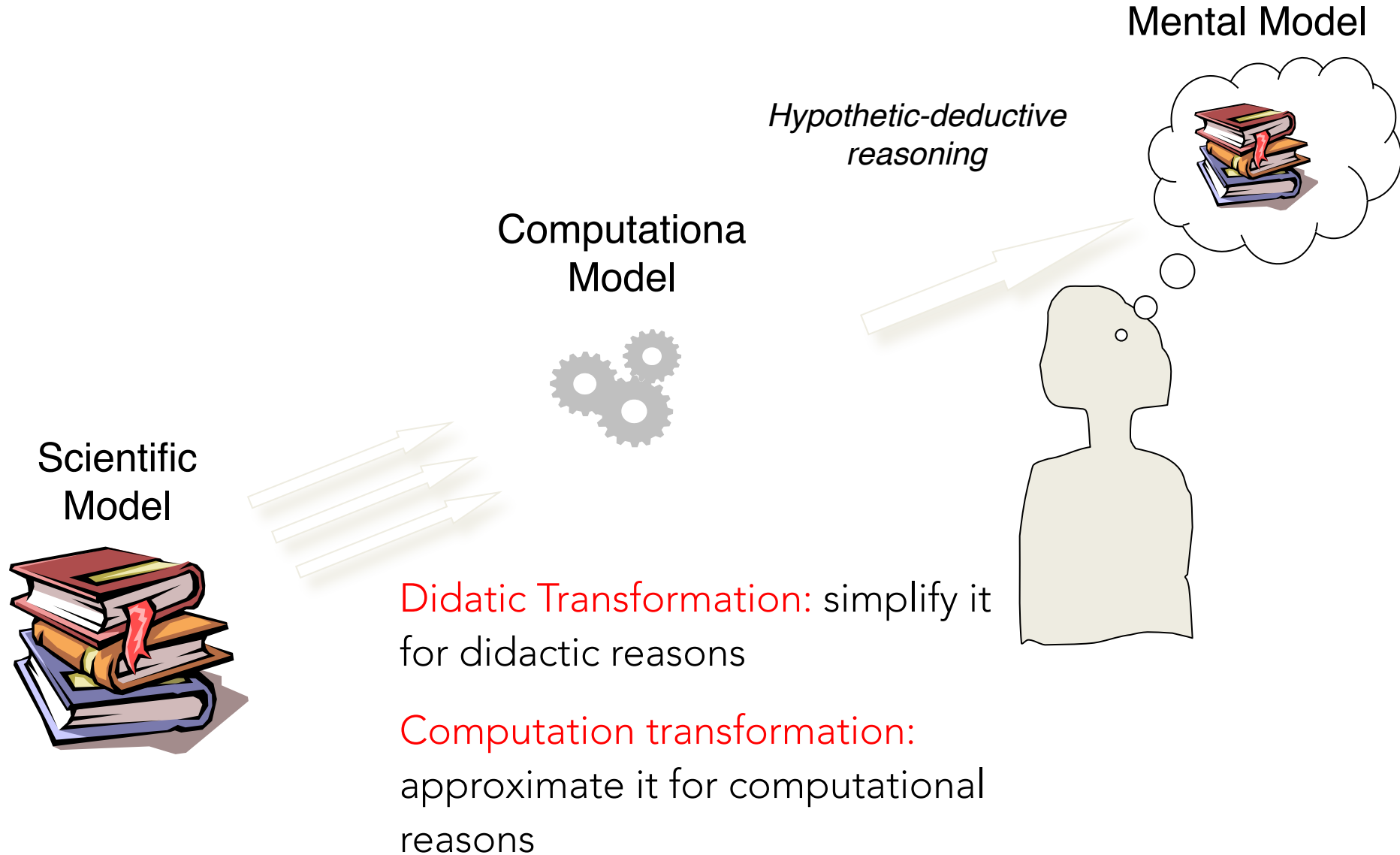
Constructionism

Guided Discovery

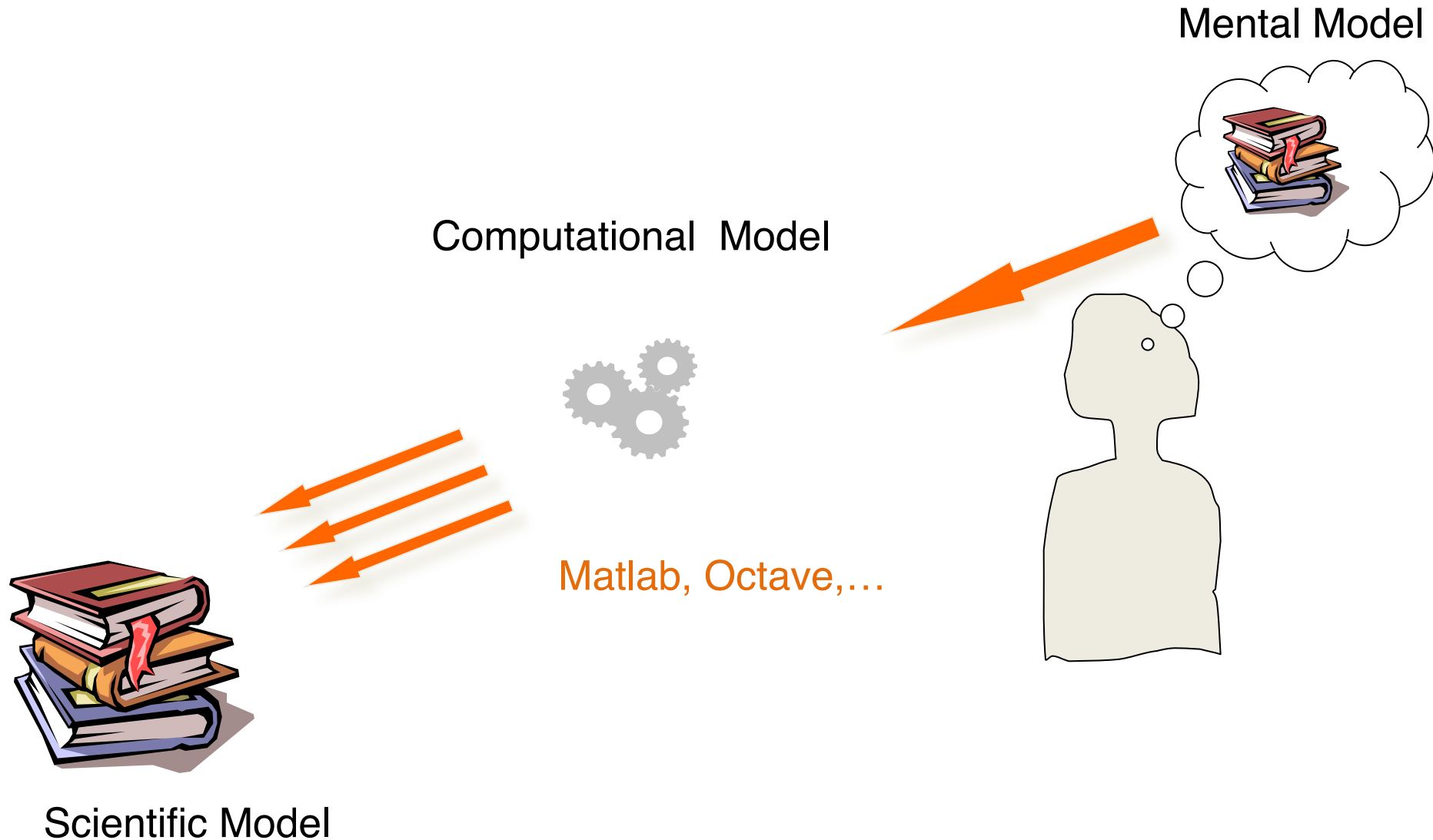
Inquiry-based learning

Learning by modelling

Learning from simulations



Learning from modelling



SCYLab: adam in Design a CO2-friendly house

Suzanne Michael

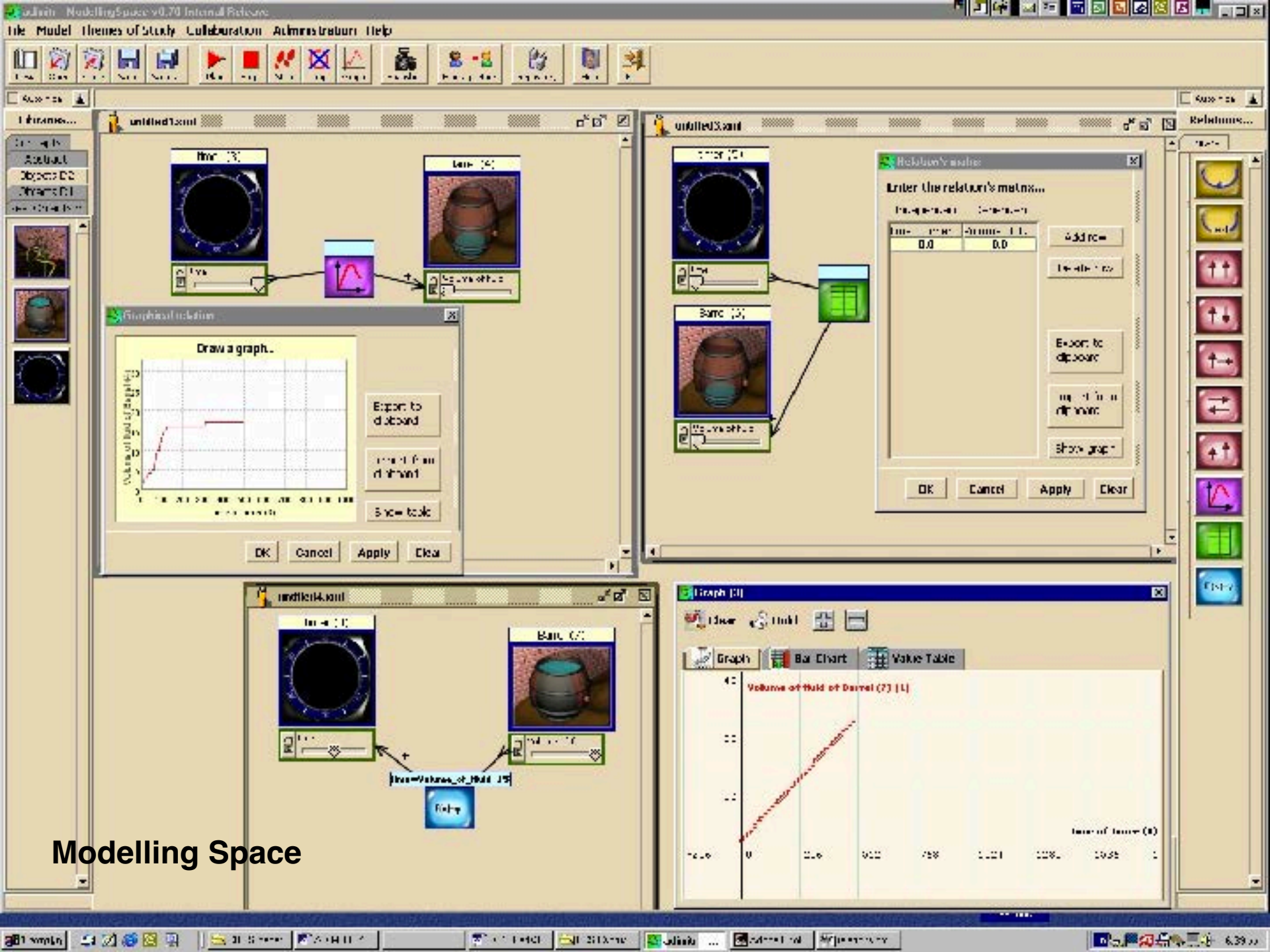
Concept map

Save Save as

Background Foreground Fill Shadow

interesting
me: thanks
suzanne: What's your current progress on it?
me: I have changed some parts, wanna see it?
suzanne: Sure!
me: Let's me start a shared session...
suzanne: I'm in :)
suzanne: Okay, let me see...
suzanne: I think that the geometry of the house is also quite important
me: Oh, yes, good point!

Figure 2: A SCY concept map with drawers attached. Available peers are above and a SCYchat is active to the right

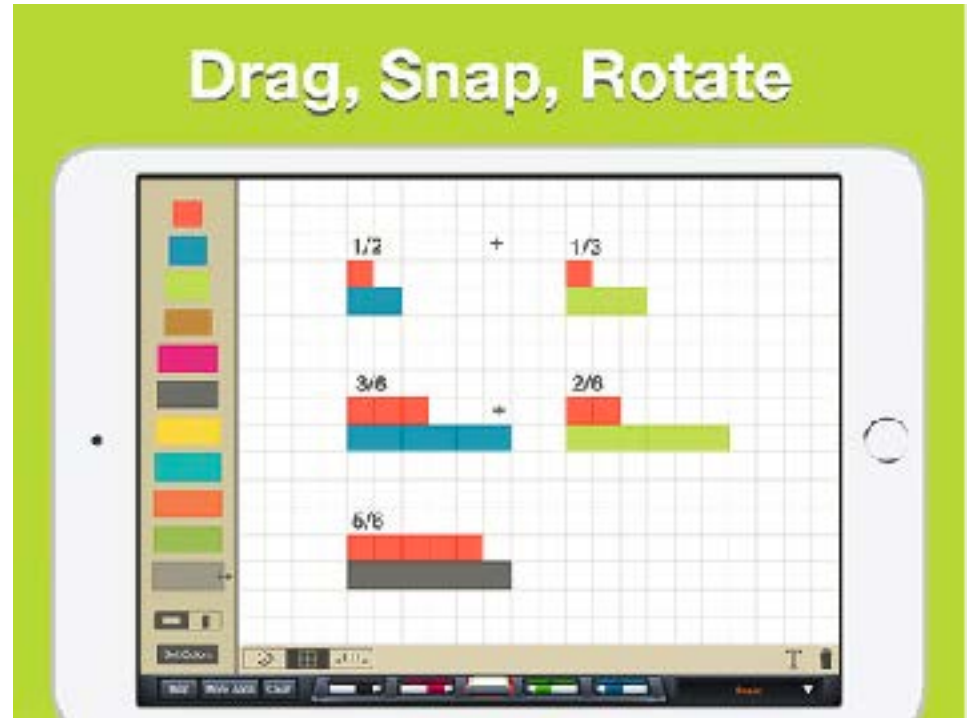


Modelling Space

Manipulating real or virtual objects ?



Cuisenaire Rods



iPad Version

<https://itunes.apple.com/gb/app/number-rods/id536204074?mt=8>

The real-virtual debate: offer both!

The image displays a control system simulation software interface. The main window shows a plot of three signals (green, red, yellow) over time from 0.0s to 4.0s. The y-axis ranges from -12 to 12. The green signal is a step function that jumps from -5 to 5 at approximately 3.3s. The red and yellow signals are smooth curves that converge towards the step function. To the right of the plot is a small inset image of a physical servo motor. Below the plot are various control parameters: K_p (1.0), T_i (0.5), T_d (0.5), U_0 (0.0), and f_c (35.0). There are also checkboxes for ARW and P-éd. Below these are sliders for Ampl. (ϵ), Offset (J), Fréq. (0.1 Hz), and Excitation (echelon). At the bottom, there are dropdown menus for Boucle fermée and Position, a Cascade checkbox, and a PUSH! button. The bottom right corner shows a scale $h: 0.02$ [sec.] and language flags for French and English.

<http://emersion.epfl.ch/mechatronics/index.html>

For you project, look for reusable exploration/simulation/problem solving activities



Summary:

1. People don't learn by being taught but by **adapting their knowledge structures** through interaction with artefacts. Educational philosophy: from telling students what to do to letting them **invent** things
2. In practice, this approach does not work very well without external **support** and requires talented teachers. Learning from simulation requires **inquiry skills**. Training these transversal skills are key goals of any education
3. Evolution of pedagogical methods from building mental schemes to building **concrete** objects. Digital artefacts offer rich interactions but digital education is not limited to virtual object. **Tangible** interfaces and augmented reality open it to physical manipulation.