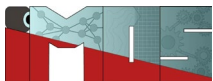


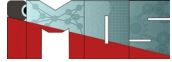


EPFL

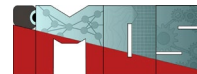


# Machine Learning for Predictive Maintenance Applications: Prognostics

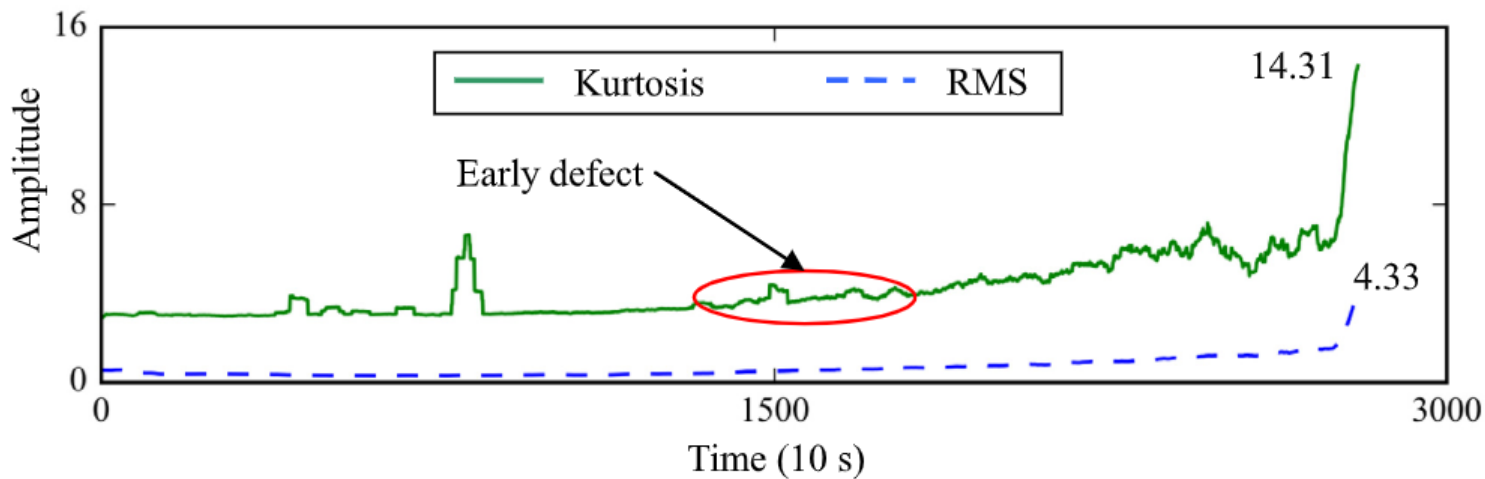
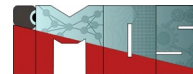
Prof. Dr. Olga Fink



# Condition / Health indicators

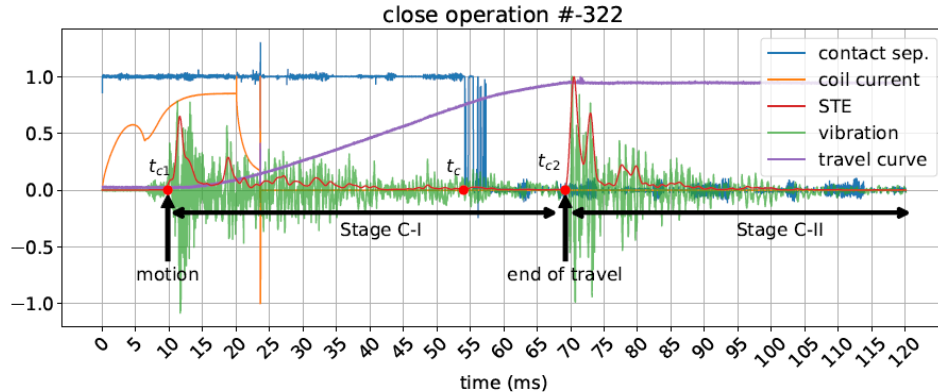
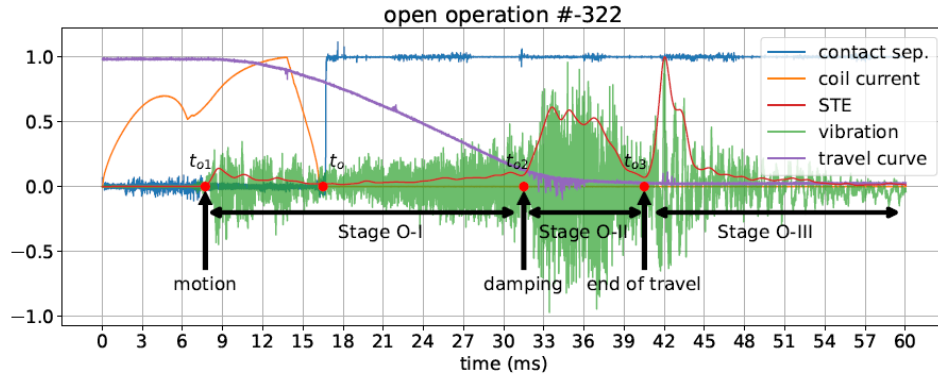
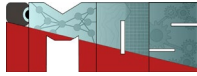


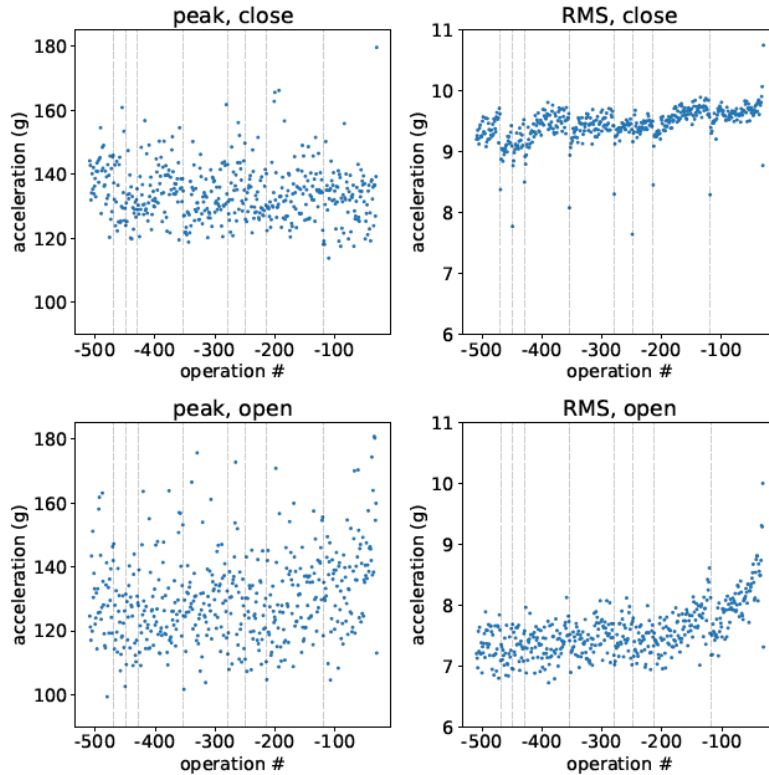
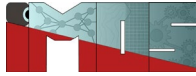
- A *condition indicator* is a feature of system data whose behavior changes in a predictable way as the system degrades or operates in different operational modes.
- A condition indicator can be any feature that is useful for distinguishing normal from faulty operation or for predicting remaining useful life.



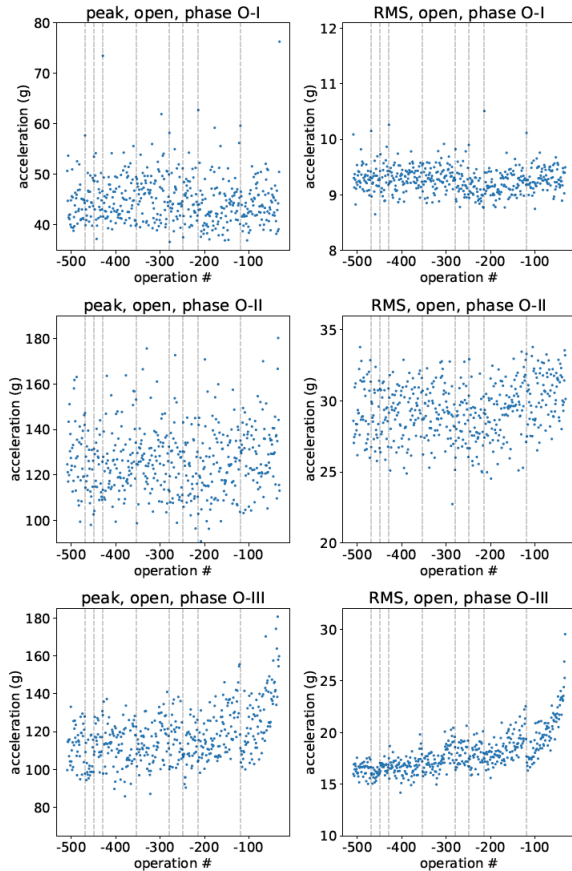
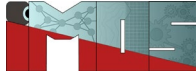
Source: Guo et. al 2017

# Example signals (normalised) collected during open and close operation of a circuit breaker

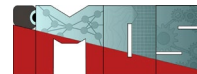




# Condition indicators of a circuit breaker

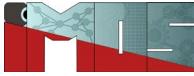


# Condition vs. Health Indicators

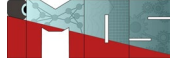


- Health indicators consist of the integration of **several condition indicators** into one value that provides the health status of the component to the end user.

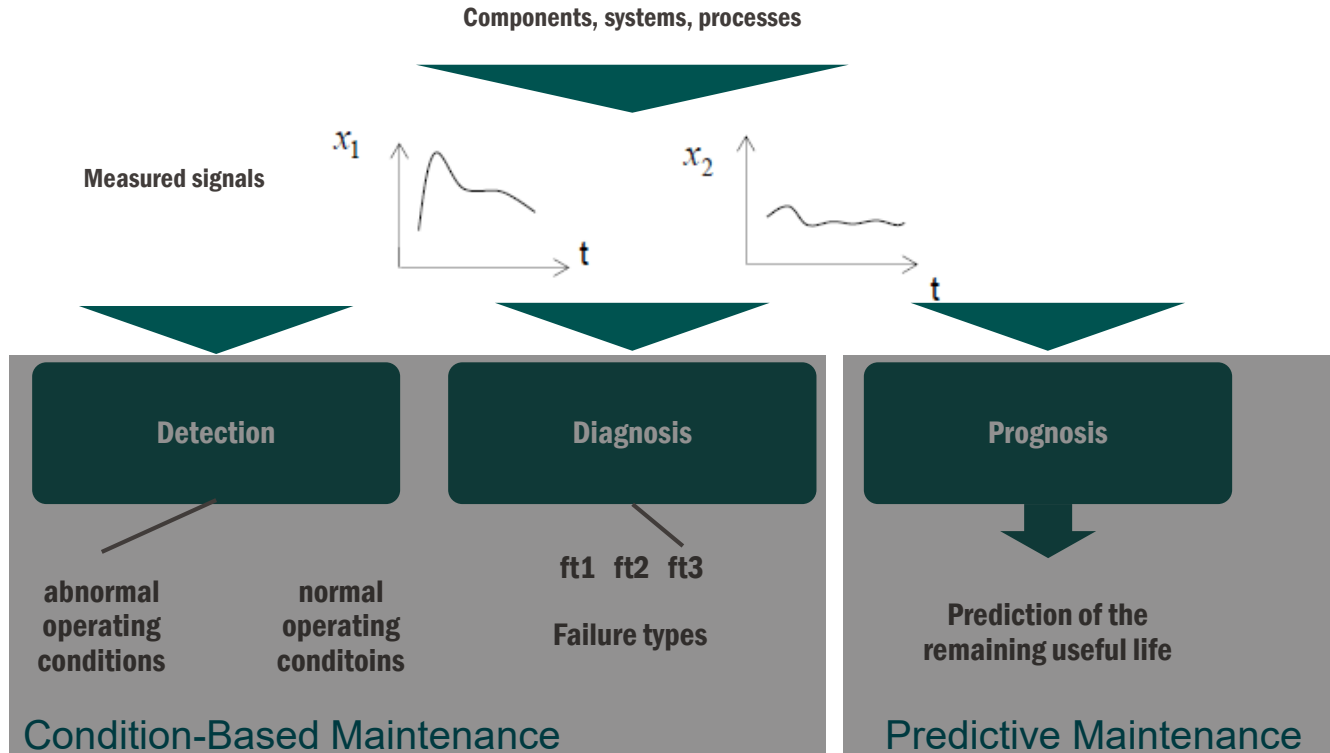
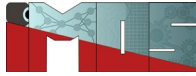
# Desired characteristics of health / condition indicators

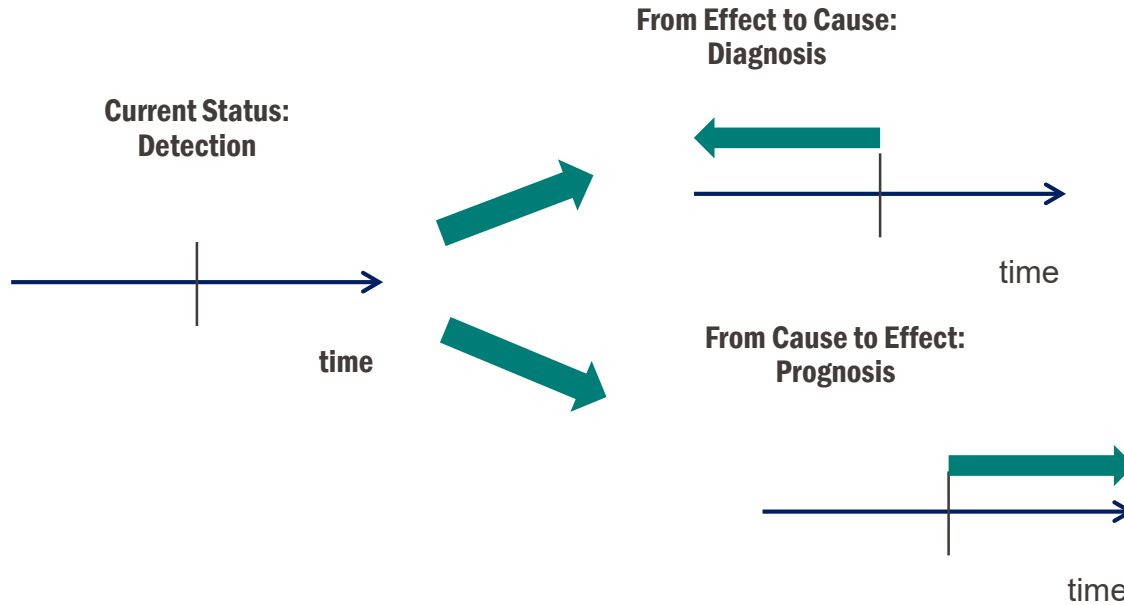
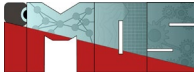


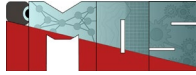
- Monotonicity
- Robustness
- Adaptability



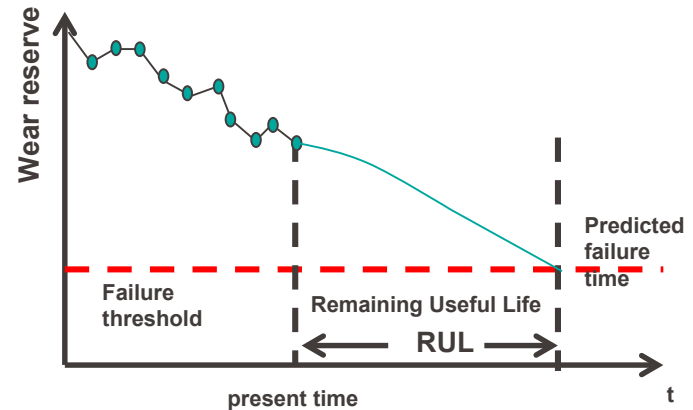
# Prognostics



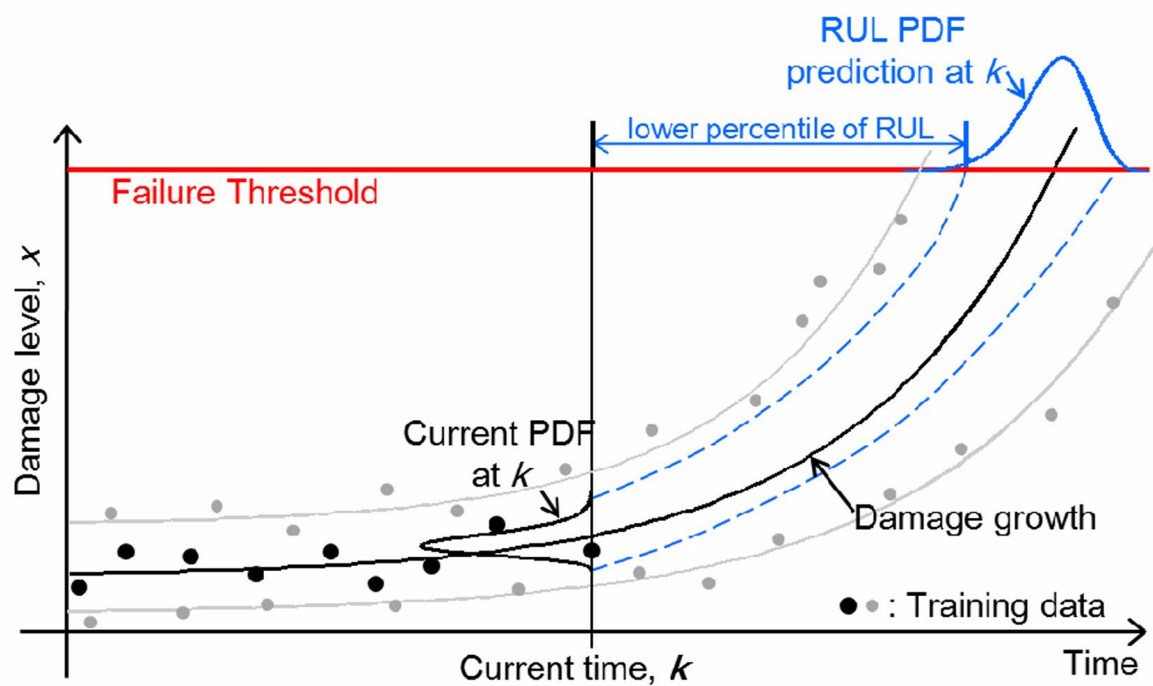
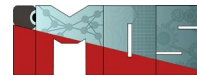




- Remaining Useful Life (RUL): the amount of time, in terms of operating hours, cycles, or other measures the component will continue to meet its design specification
- Time of Failure (ToF): the time a component is expected to fail (no longer meet its design specifications).
- Probability of Failure (PoF): the failure probability distribution of the component.
- End of Life (EoL) refers to a failure of the component as defined by its functional specifications

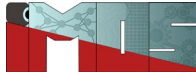


Source: Coble, 2016

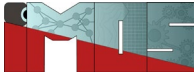


An, D., Choi, J. H., & Kim, N. H. (2018). Prediction of remaining useful life under different conditions using accelerated life testing data. *Journal of Mechanical Science and Technology*, 32, 2497-2507.

# Types of failures (End of Life)

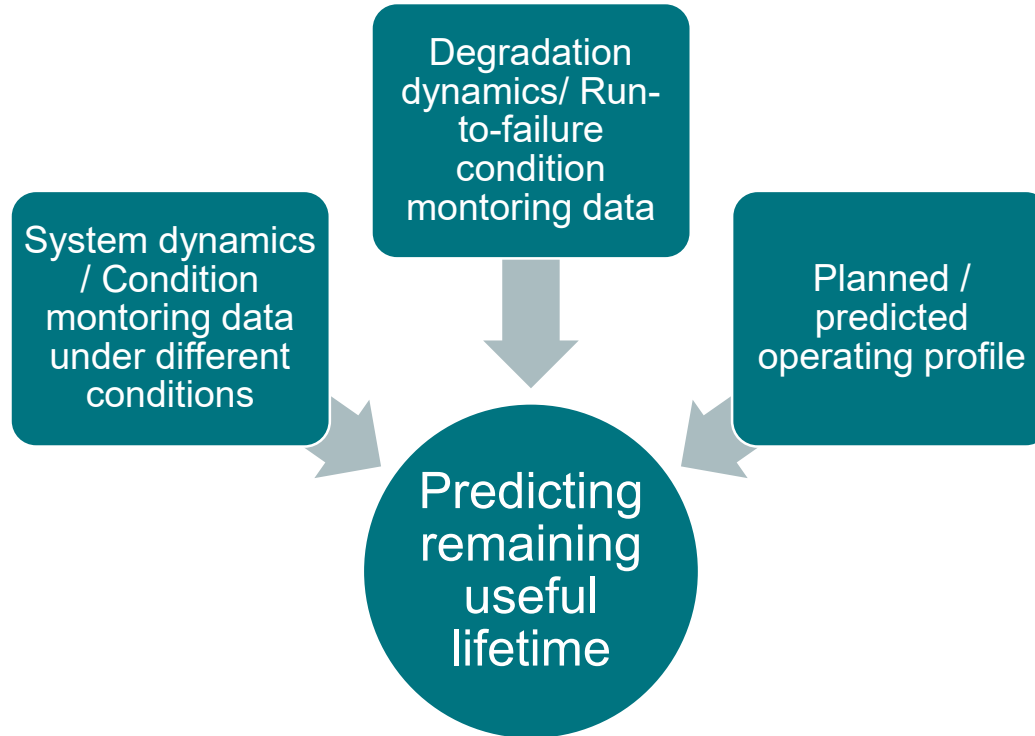
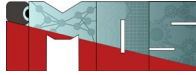


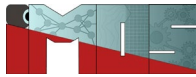
- Soft failures:
  - Soft failures refer to conditions where a system or component experiences performance degradation or intermittent issues without complete loss of functionality. These failures often manifest as a gradual decline in performance, reliability, or efficiency.
  - Intermittent Performance Issues: Systems may function sporadically, with performance fluctuating between optimal and suboptimal states.
  - Degradation Over Time: Gradual wear and tear lead to diminishing performance metrics.
  - Early Warning Signs: Often preceded by detectable anomalies or deviations in health indicators.
  - Non-Catastrophic: Do not cause immediate or severe damage but can lead to significant issues if unaddressed.
- Hard Failures
  - Hard failures occur when a system or component ceases to function entirely or experiences a catastrophic breakdown. These failures result in the immediate and complete loss of functionality, often requiring significant repairs or replacements.
  - Sudden and Complete Failure: Systems stop working abruptly without prior warning.
  - Catastrophic Impact: Can cause extensive damage to equipment, infrastructure, or even pose safety hazards.
  - High Severity: Often lead to significant operational disruptions and financial losses.
  - Immediate Action Required: Necessitate prompt intervention to restore functionality and prevent further damage.
- Other terms used in the context of system failures:
  - Warning
  - Alarm



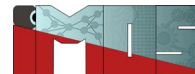
- *Predict progression of the system health state based on **current** and **future** operational and environmental conditions to estimate the time at which a system no longer fulfils its **function within desired specifications** (“Remaining Useful Life”)*

# Required ingredients for successful prediction of remaining useful lifetime (RUL)





- **Prognostics:** Predict the remaining useful life or time to failure of a failing component/system
- **Trending:** Trend or linearly project/regress a current measurement until it reaches a predefined threshold
- **Predictive Diagnostics:** Find precursors to failure



## End-of-Life predictions

Event predictions → RUL prediction

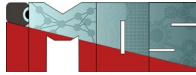
Decay /degradation prediction → trajectory prediction

No/little history data → mainly model-based

History data → data-driven methods can be applied

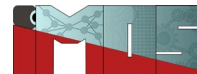
Nominal data only

Nominal and failure data



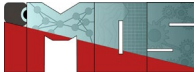
- Type I: Reliability Data-based
  - Use population based statistical model
  - These methods consider historical time to failure data which are used to model the failure distribution. They estimate the life of a typical component under nominal usage conditions.
  - Example: Weibull Analysis
  
- Type II: Stress-based
  - Use population based fault growth model – learned from accumulated knowledge
  - These methods also consider the environmental stresses (temperature, load, vibration, etc.) on the component. They estimate the life of an average component under specific usage conditions.
  - Example: Proportional Hazards Model
  
- Type III: Condition-based
  - Individual component based data-driven model
  - These methods also consider the measured or inferred component degradation. They estimate the life of a specific component under specific usage and degradation conditions.
  - Example: Cumulative Damage Model, Filtering and State Estimation

Source: Goebel, 2012



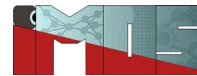
- Reliability analysis gives us information about the failure of a population of similar systems or components
- Prognostics extends this to a specific system or component
- When will it fail?
- What's the probability that it will fail in the next 5 minutes?
- What's the probability that we can complete the mission before something fails?

# Type III – Degradation-based Prediction

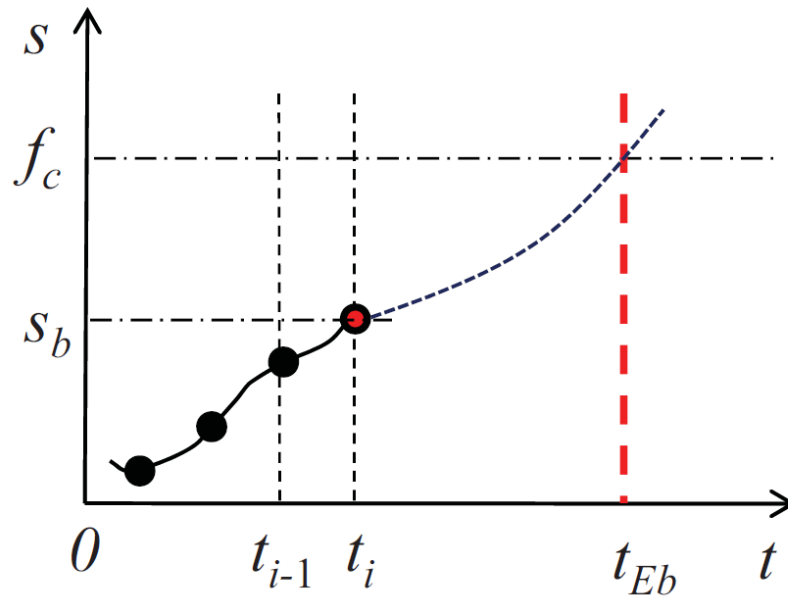
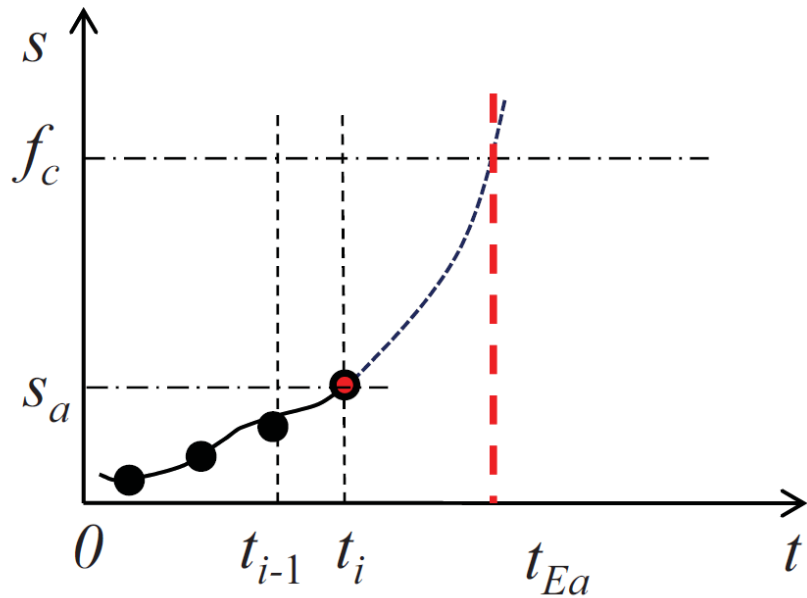
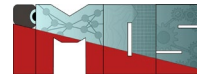


- Type III prognostics estimate the lifetime of the specific component in its specific operating environment
- Type III algorithms track the degradation (damage) as a function of time and predict when the total damage will exceed a predefined threshold that defines failure
- Damage is generally assumed to be cumulative (irreversible)

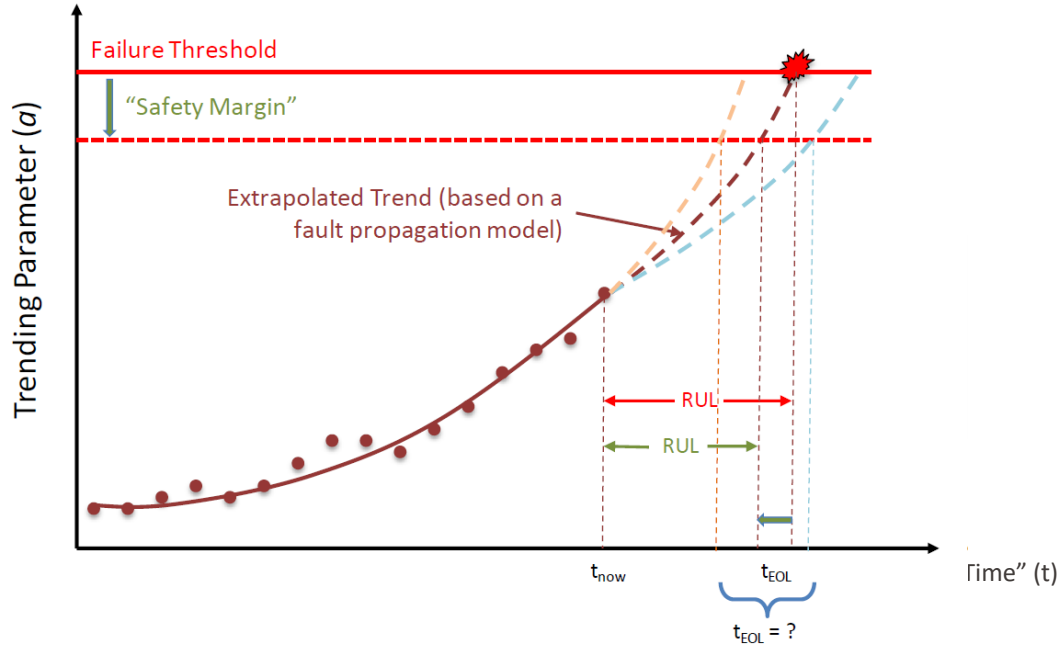
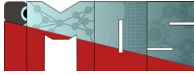
# Degradation-Based Prognostics

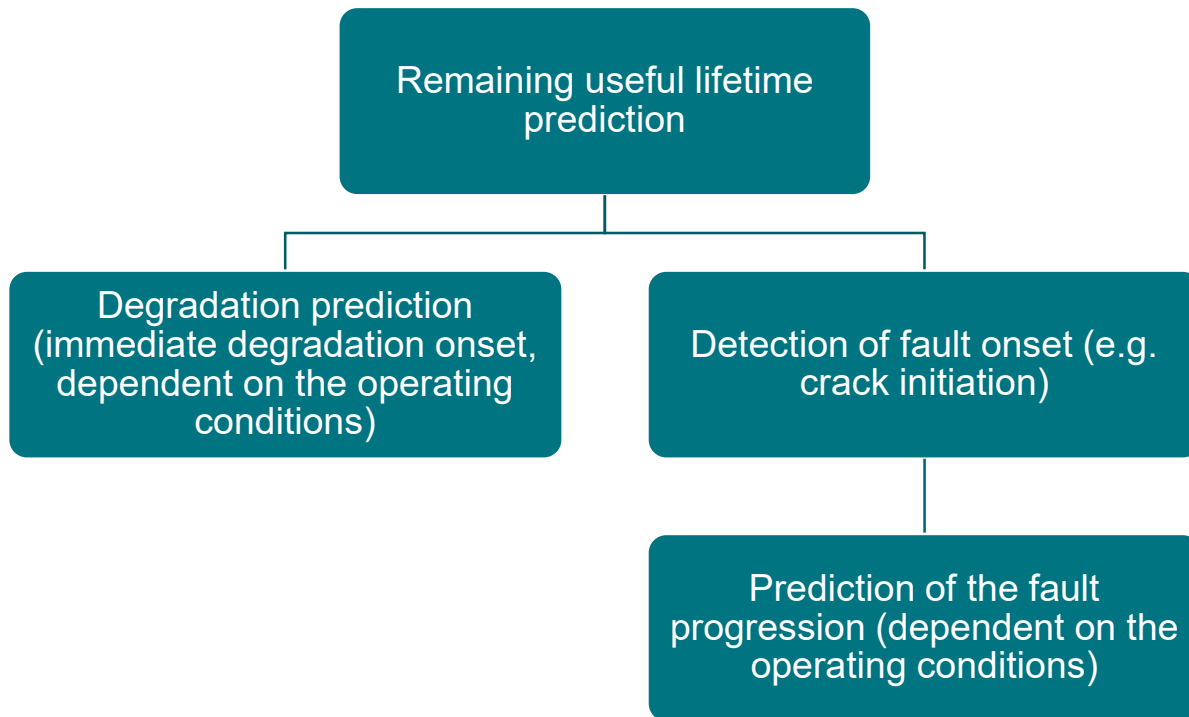
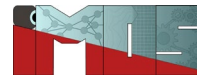


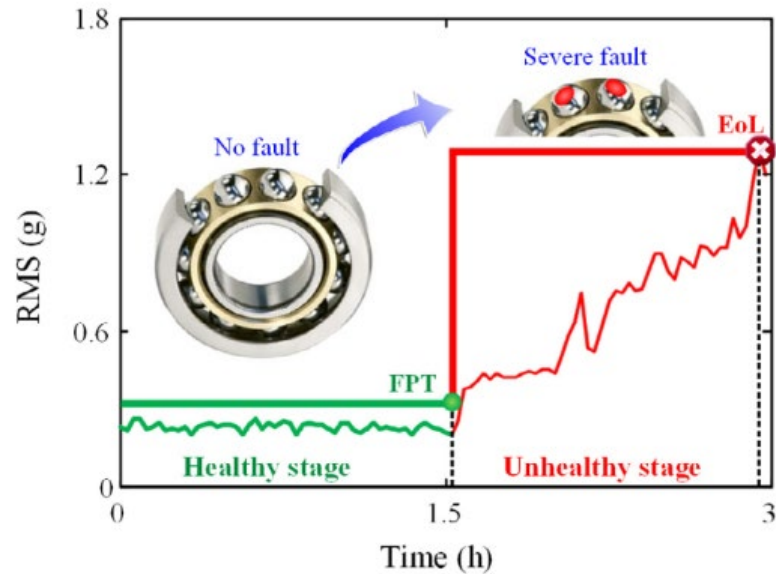
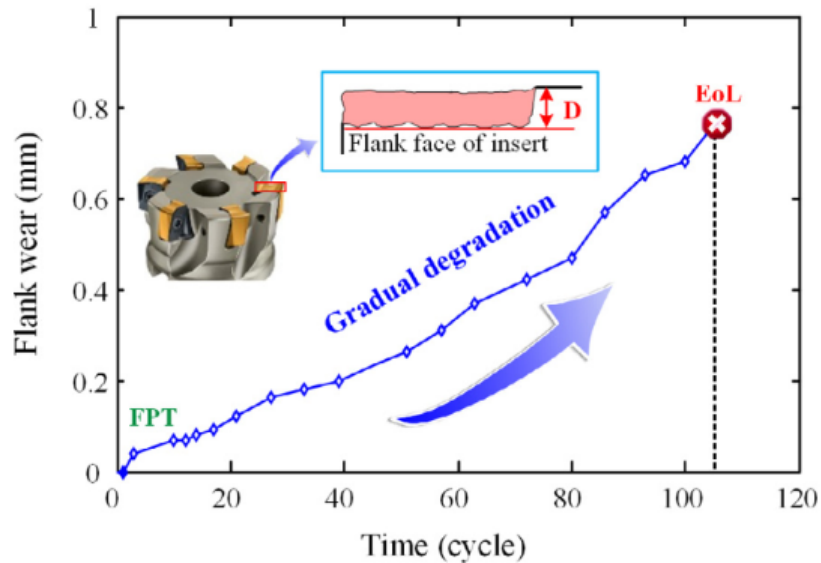
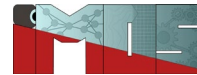
- A degradation measure is a scalar or vector quantity that numerically reflects the current ability of the system to perform its designated functions properly. It is a quantity that is correlated with the probability of failure at a given moment.
- A degradation path is a trajectory along which the degradation measure is evolving in time towards the critical level corresponding to a failure event.



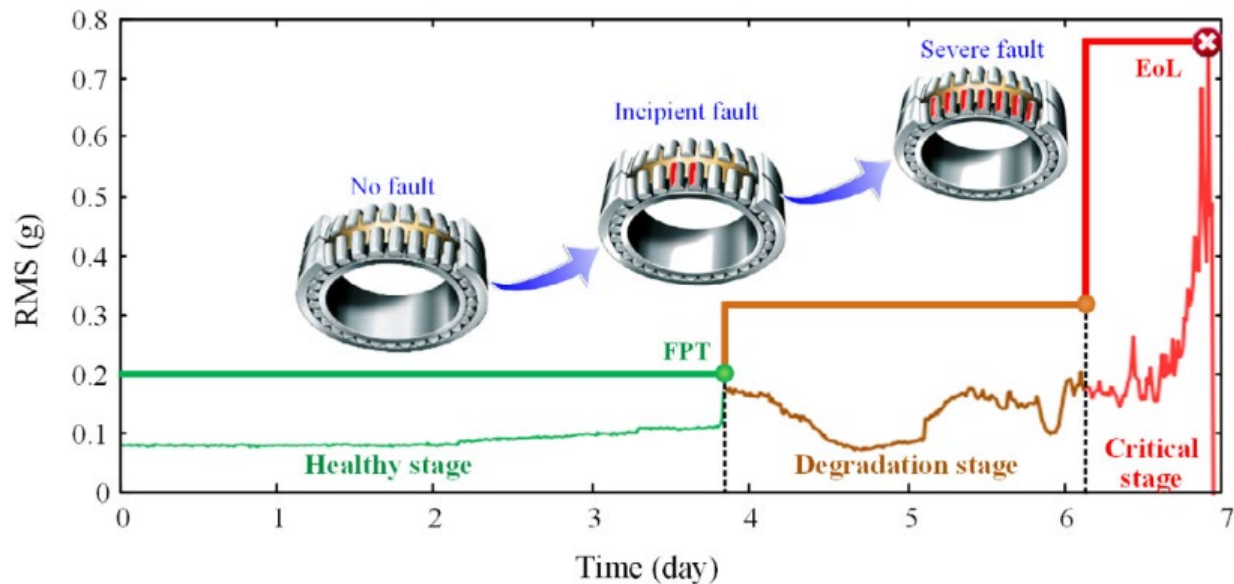
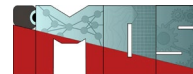
Wang, T., Trajectory Similarity Based Prediction for Remaining Useful Life Estimation, 2010

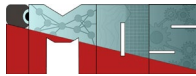






# Different degradation trajectories





## Prognostics Methods

Data-driven

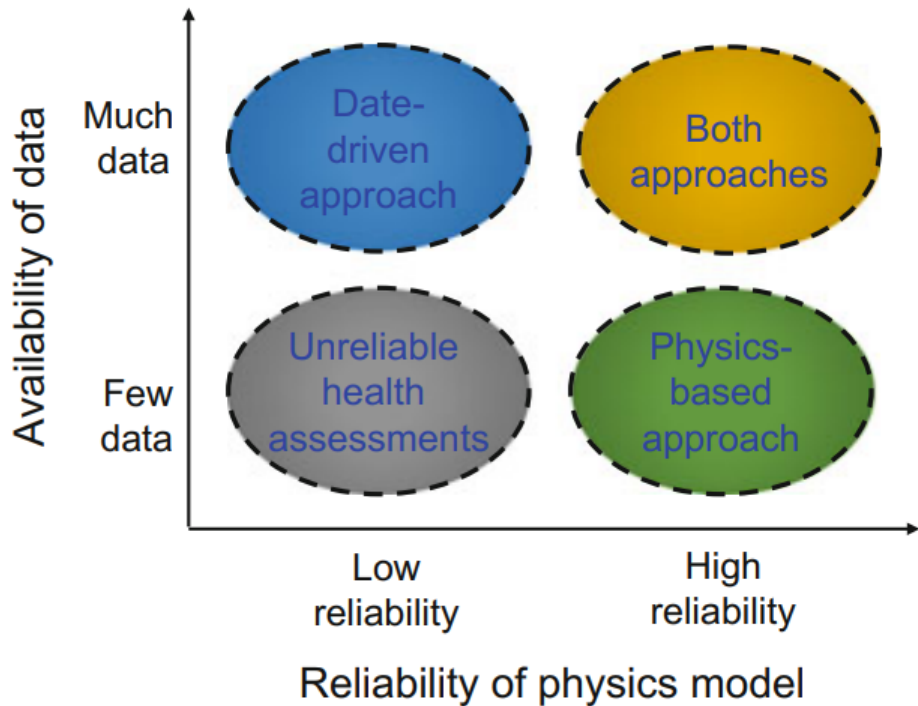
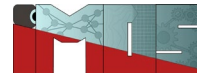
Statistical  
Approaches

Machine  
Learning

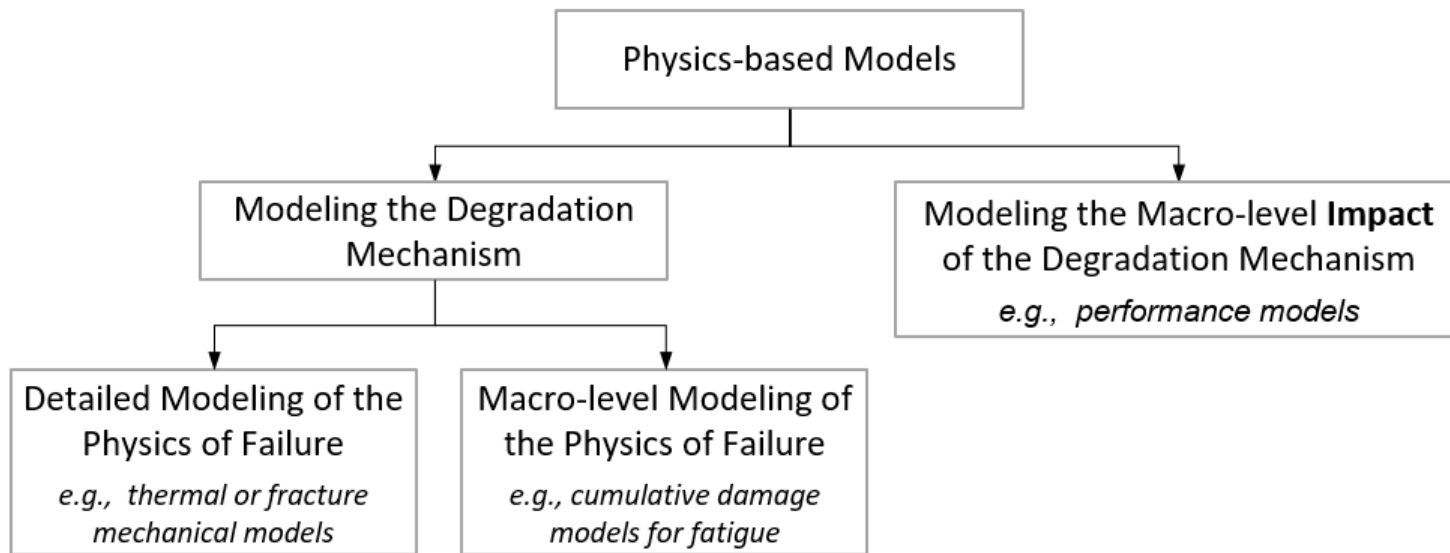
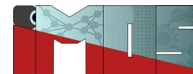
Physics-  
based  
(model-  
based)

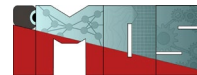
Hybrid  
approaches  
(physics-  
based +  
data-driven)

Knowledge-  
based



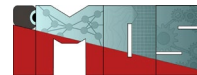
Source: Prognostics and Health Management of Engineering Systems



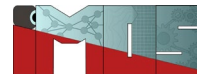


- Description of a system's underlying physics using suitable representation
- Some examples:
  - Model derived from "First Principles"
    - Encapsulate fundamental laws of physics
      - partial differential equations (PDEs)
      - Euler-Lagrange Equations
  - Empirical model chosen based on an understanding of the dynamics of a system
    - Lumped Parameter Model
    - Classical 1<sup>st</sup> (or higher) order response curves
  - Mappings of stressors onto damage accumulation
    - Finite Element Model
    - High-fidelity Simulation Model
- Something in the model correlates to the failure mode(s) of interest

# Steps for physics-based prognostics



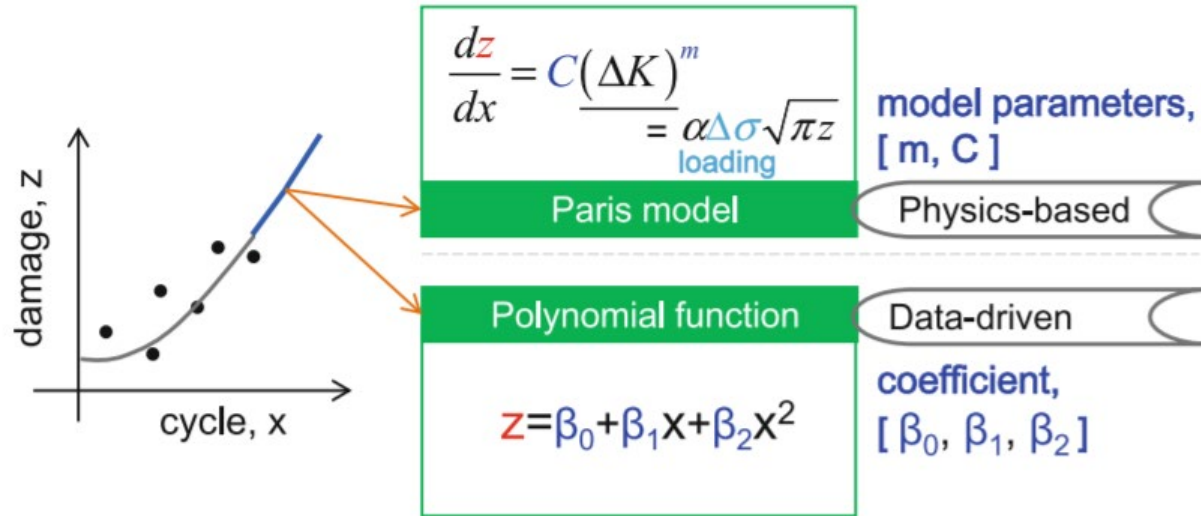
- Model underlying physics of a component/subsystem
- Model physics of damage propagation mechanisms
- Determine criteria for End-of-Life threshold
- Develop algorithms to propagate damage into future
- Deal with uncertainty



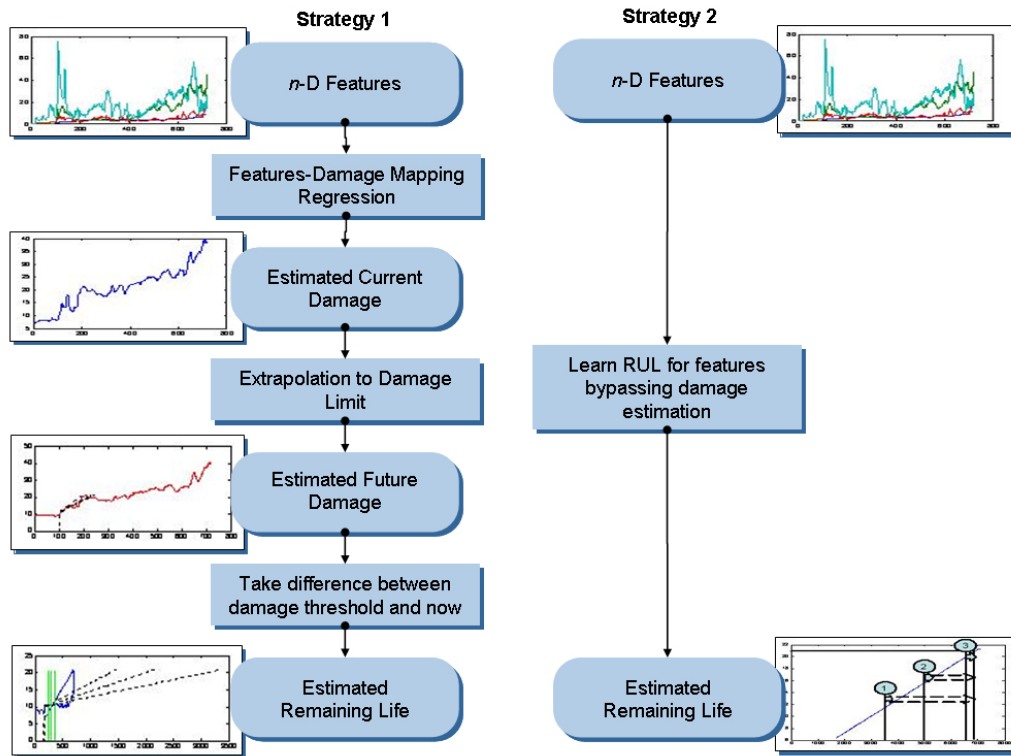
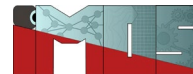
- Model is based solely on data collected from the system
- Some system knowledge may still be handy:
  - What the system 'is'
  - What the failure modes are
  - What sensor information is available
  - Which sensors may contain indicators of fault progression (and how those signals may 'grow')
- *General* steps:
  - Gather what information you can (if any)
  - Determine which sensors give good trends
  - Process the data to “clean it up” – try to get nice, monotonic trends
  - Determine threshold(s) either from experience (data) or requirements
  - Use the model to predict RUL
    - Regression / trending
    - Mapping (e.g., using a neural network)
    - Statistics

Source: Goebel, 2012

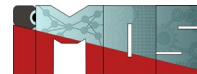
# Simple example of data-driven vs. physics-based (crack growth model)



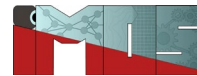
# Different approaches to data-driven RUL prediction



Source: NASA

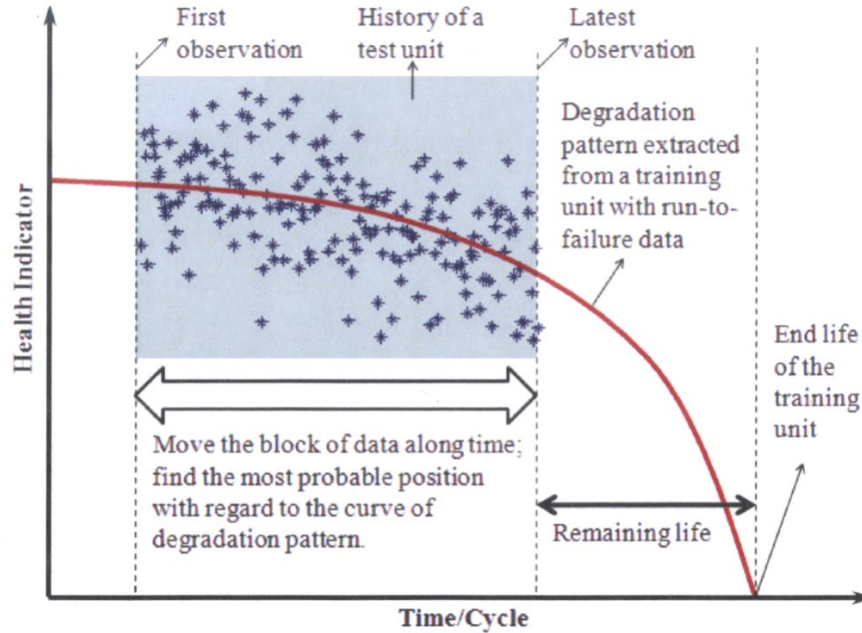
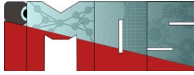


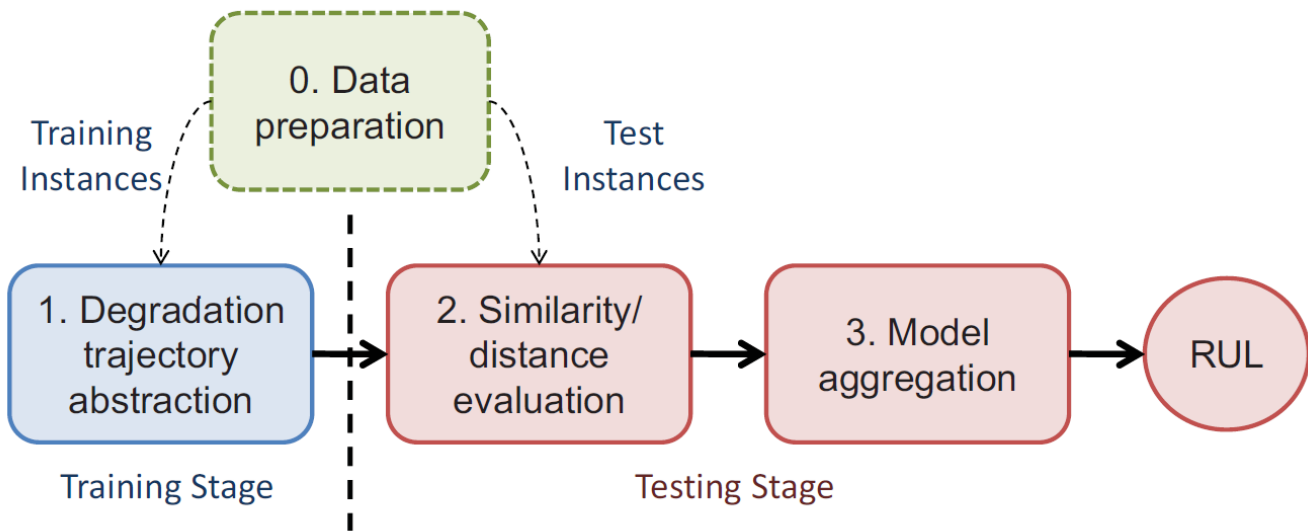
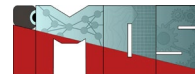
- Leverages the concept of comparing the current state of a system with historical data to estimate the remaining useful life.
- Underlying assumption is that systems with similar degradation patterns will exhibit similar RUL trajectories.
- Similarity-based approaches generally involve the following steps:
- Data Collection and Preprocessing:
  - Historical Data: Gather comprehensive historical operational and failure data.
  - Feature Extraction: Identify and extract relevant health indicators or features that represent the system's state.
  - Normalization: Standardize data to ensure consistency across different datasets.
- Similarity Measurement:
  - Distance Metrics: Utilize metrics such as Euclidean distance, Dynamic Time Warping (DTW), or Mahalanobis distance to quantify similarity between current and historical states.
  - Feature Space Comparison: Assess similarity in a multidimensional feature space where each dimension corresponds to a health indicator.
- RUL Estimation:
  - Weighted Averaging: Compute RUL based on the weighted average of RULs from the most similar historical instances.
  - Nearest Neighbors: Identify the 'k' most similar historical cases and use their RULs to predict the current RUL.



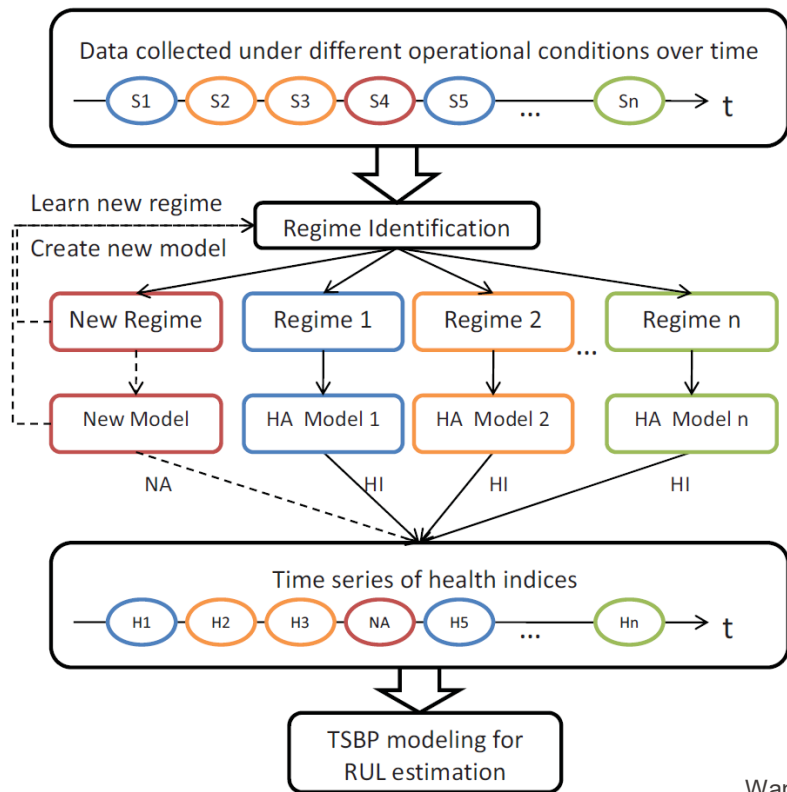
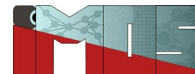
- **K-Nearest Neighbors (K-NN):**
  - Description: Identifies the 'k' most similar historical instances to the current state and averages their RULs.
  - Advantages: Simple to implement and interpret.
  - Limitations: Sensitive to the choice of 'k' and distance metrics; may not capture complex degradation patterns.
- **Pattern Matching and Template Matching:**
  - Description: Compares current degradation patterns with predefined templates representing typical failure modes.
  - Advantages: Can effectively recognize known failure patterns.
  - Limitations: Limited to detecting only those failure modes represented by templates; lacks flexibility for novel failures.
- **Cluster-Based Similarity:**
  - Description: Groups historical data into clusters and predicts RUL based on the cluster membership of the current state.
  - Advantages: Reduces computational complexity by limiting comparisons within relevant clusters.
  - Limitations: Requires effective clustering algorithms; may not handle overlapping or dynamic clusters well.

# Similarity based RUL prediction



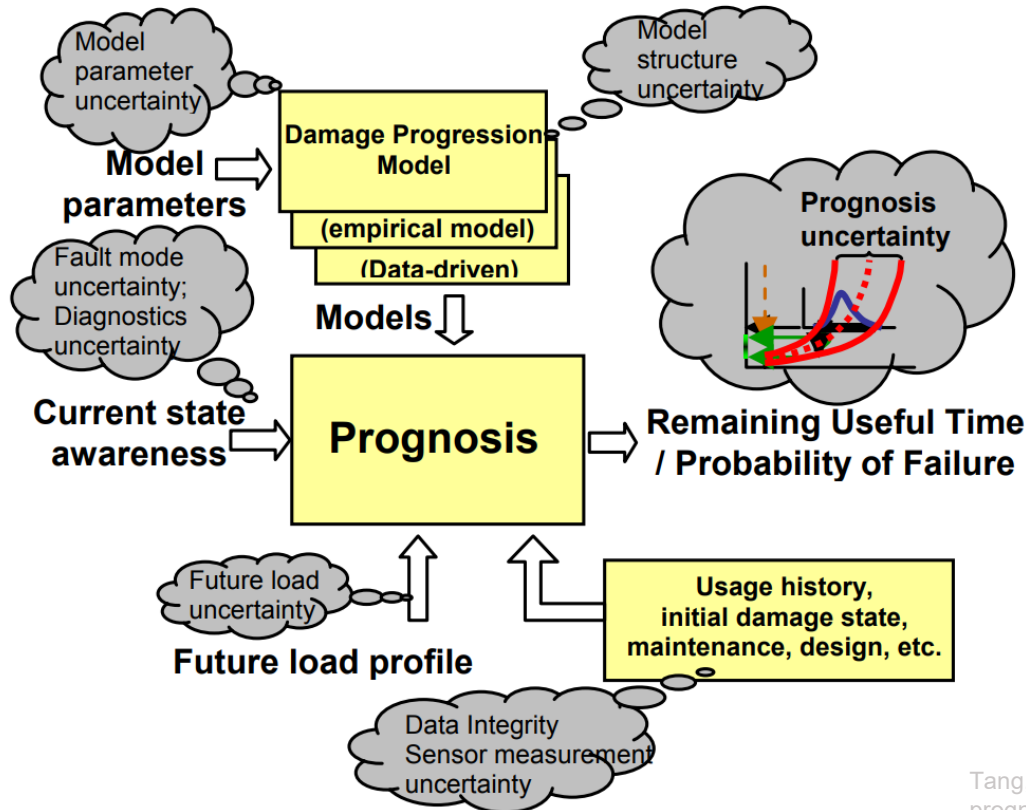
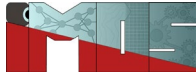


# Similarity based RUL predictions

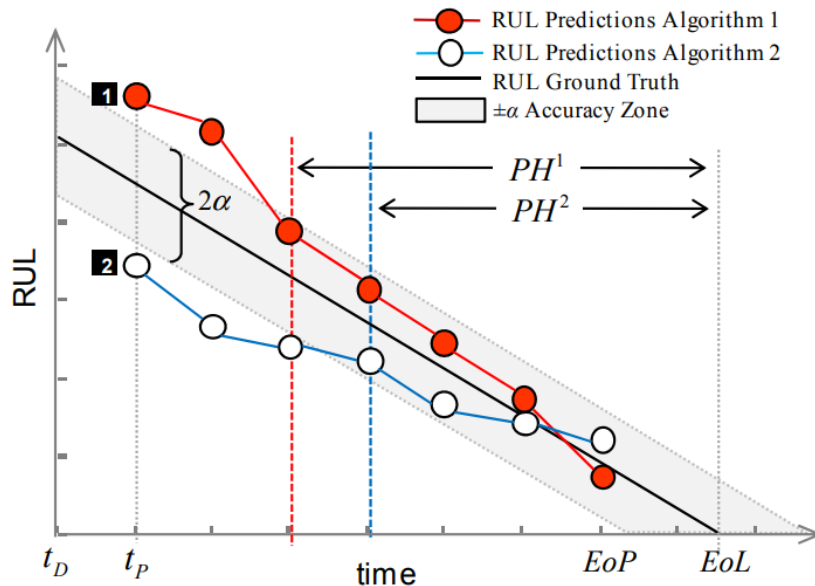
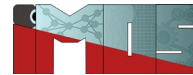


Wang, T., Trajectory Similarity Based Prediction for Remaining Useful Life Estimation, 2010

# Sources of uncertainty in prognostics



Tang, Liang, et al. "Methodologies for uncertainty management in prognostics." 2009 IEEE Aerospace conference. IEEE, 2009.



$$PH = EoL - i$$

where:

$$i = \min\{j \mid (j \in \ell) \wedge (r_* - EoL * \alpha) \leq r^j(j) \leq r_* + EoL * \alpha)\}$$

is the first time index when predictions satisfy  $\alpha$ -bounds

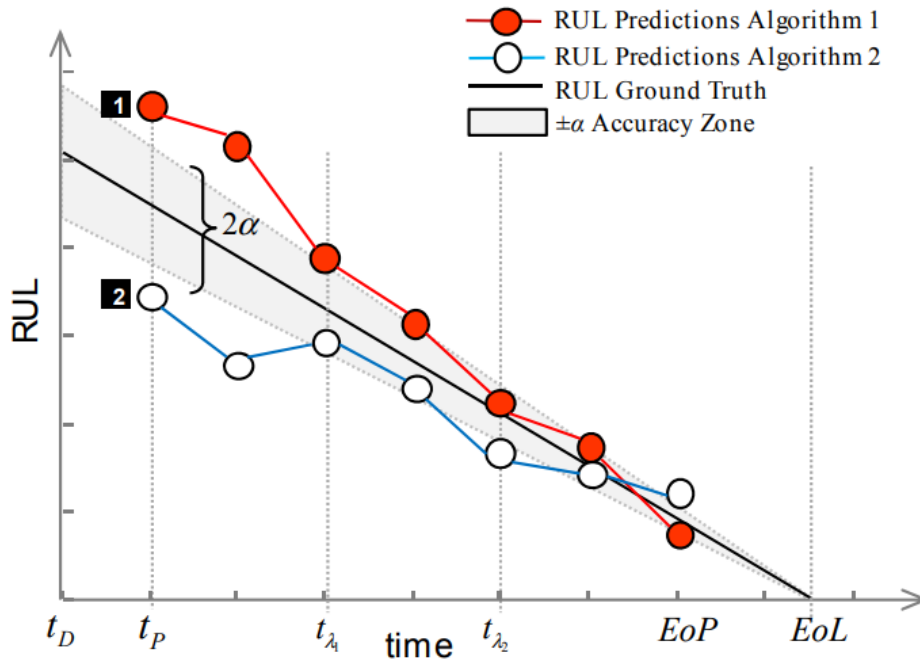
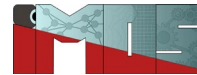
$\ell$  is the set of all time indexes when a prediction is made

$l$  is the index for  $l^{\text{th}}$  unit under test (UUT)

$r_*$  is the ground truth RUL

$r(j)$  is the predicted RUL at time  $j$

EoL is the ground truth End-of-Life (actual failure)

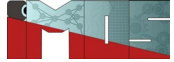


$$(1 - \alpha) \cdot r_*(t) \leq r^l(t_\lambda) \leq (1 + \alpha) \cdot r_*(t)$$

where:

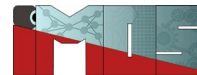
$\alpha$  is the accuracy modifier

$\lambda$  is a time window modifier such that  
 $t_\lambda = t_p + \lambda(EoL - t_p)$

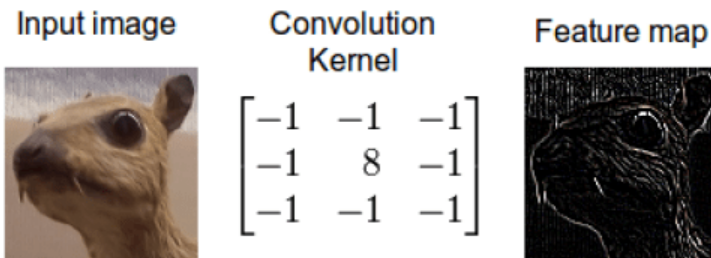


# Recap: Convolutional neural networks

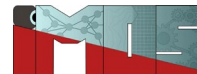
# General intuition behind using convolutional filters



- Image filters can enhance image attributes
- Convolutional neural networks are similar to conventional image filtering
- Filter kernels are learnt



Source: UIO, 2017



0	0	0	0	0	0	0
0	2	4	9	1	4	0
0	2	1	4	4	6	0
0	1	1	2	9	2	0
0	7	3	5	1	3	0
0	2	3	4	8	5	0
0	0	0	0	0	0	0

Image

x

1	2	3
-4	7	4
2	-5	1

Filter /  
Kernel

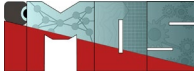
=

21	59	37	-19	2
30	51	66	20	43
-14	31	49	101	-19
59	15	53	-2	21
49	57	64	76	10

Feature

$$O = \frac{n - f + 2p}{s} + 1$$

Where O is the output height/length, n is input height / length, f is filter size, p is the padding, and s is the stride



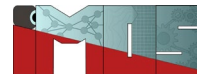
6	8	6	3	1	0
9	13	10	5	2	0
9	14	11	6	3	0
9	13	11	6	2	0
8	13	10	5	3	0
6	7	5	3	1	0

Feature map

13	10	2
14	11	3
13	10	3

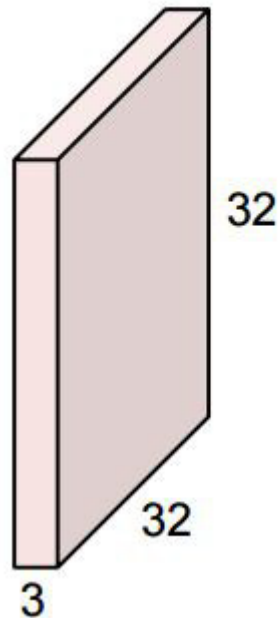
Max pooling

# Filters and channels (Standard method)

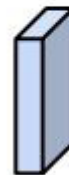


- An input image has a third dimension (say RGB)
- A filter/kernel always has the same third dimension

32x32x3 image

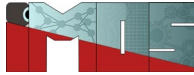


5x5x3

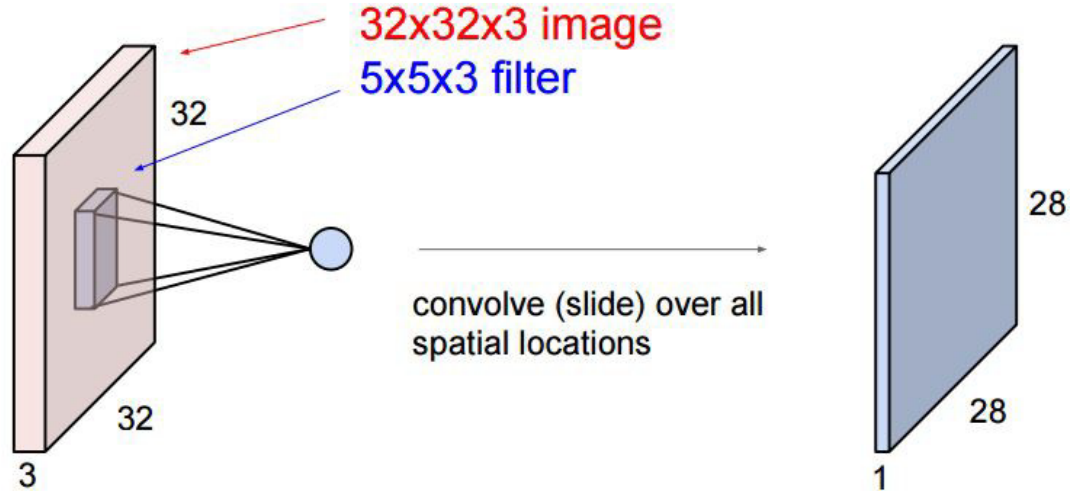


Source: UIO, 2017

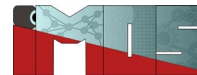
# EPFL Filters and channels



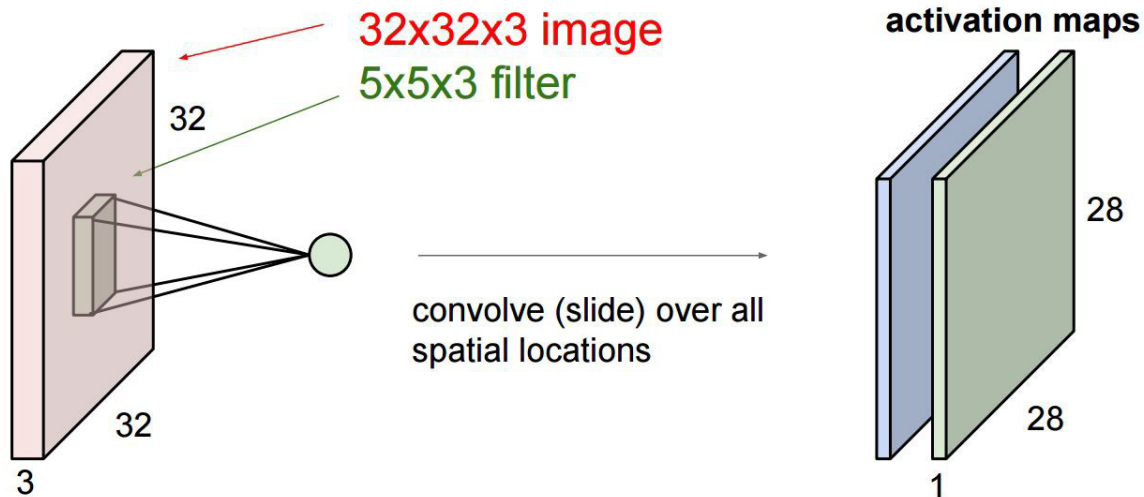
- Overlapping area is multiplied then summed (dot product)
- With sliding you get 28x28x1 output



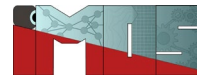
# Usually we use multiple filters per layer



- A new kernel/filter slides over the same image
- Create a new filtered image

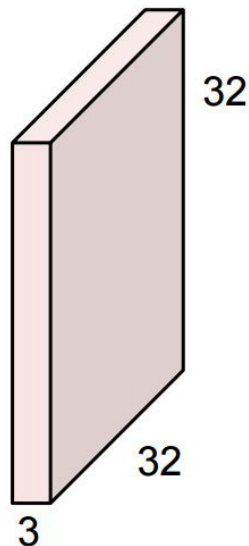


Source: UIO, 2017

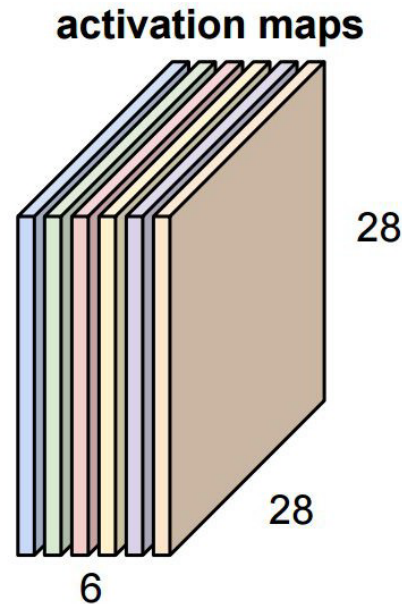


Many activation maps create a new “image”

If we filter the image 6 times, we get a new image with 6 channels.

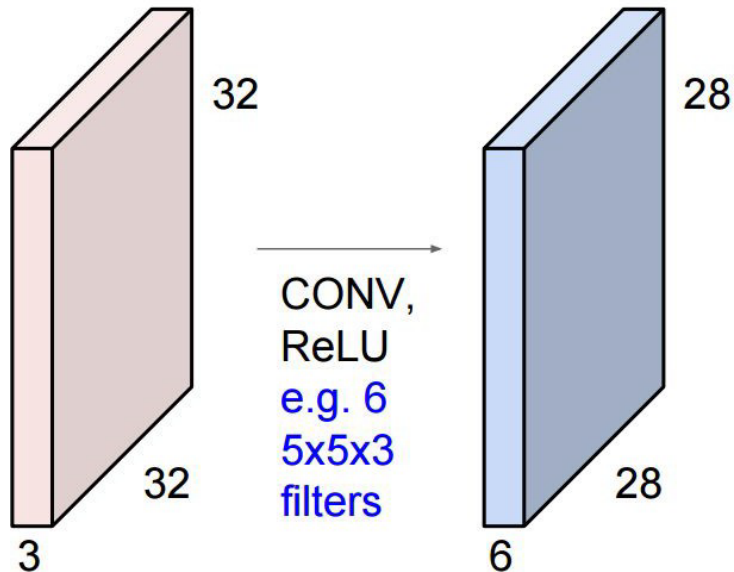
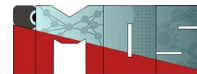


Convolution Layer

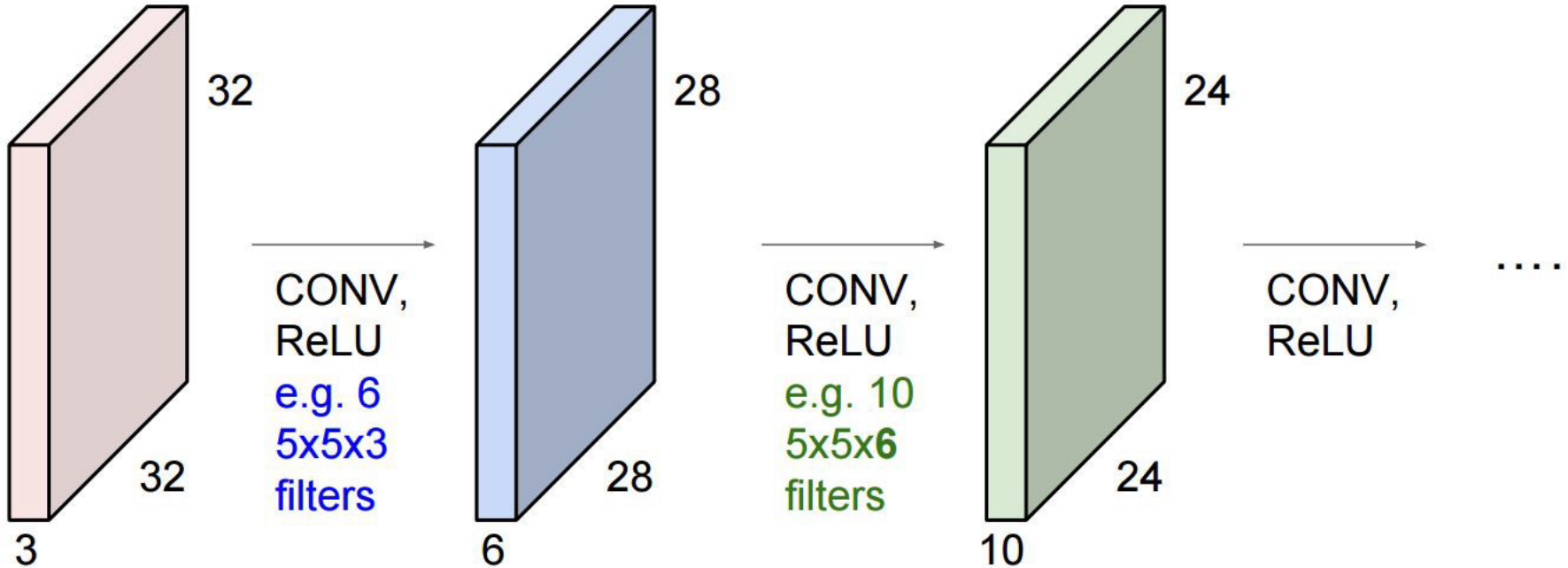
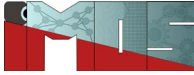


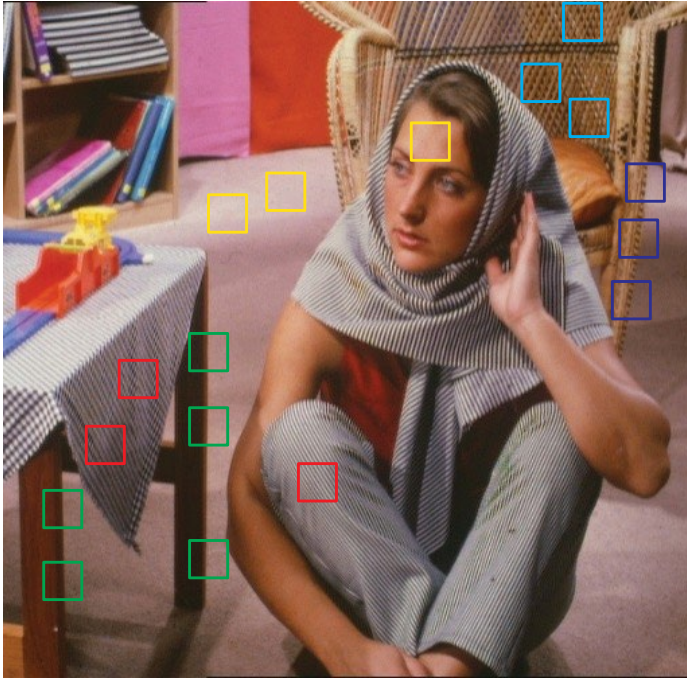
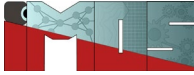
Source: UIO, 2017

# Convolutional neural network consist of multiple layers



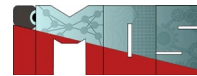
# EPFL Convolutional neural network consist of multiple layers





Data is self-similar across the domain

# Translation invariance (image classification tasks)

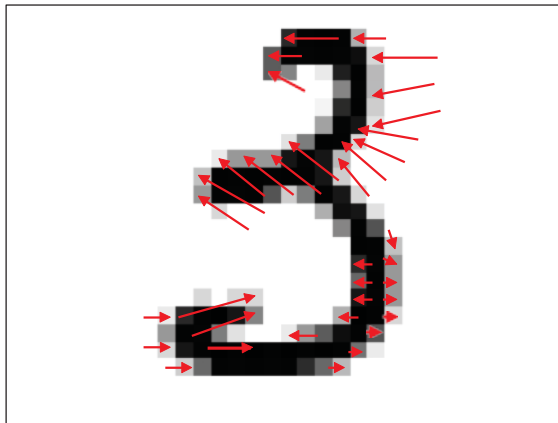
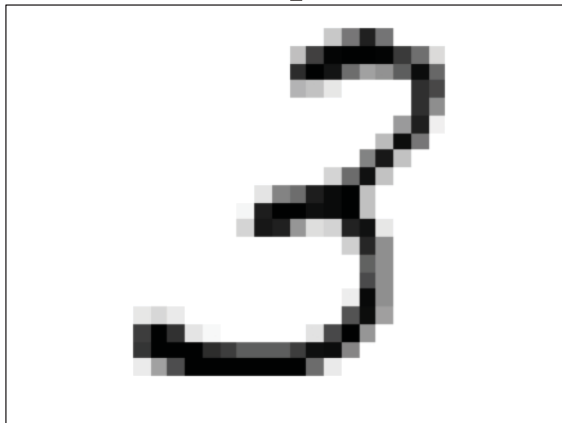
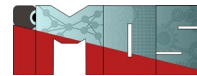


$$f(\mathcal{T}_{\mathbf{v}}x) = f(x) \quad \forall x, \mathbf{v}$$

where

- image is modeled as a function  $x \in L^2([0, 1]^2)$
- $\mathcal{T}_{\mathbf{v}}x(\mathbf{u}) = x(\mathbf{u} - \mathbf{v})$  is a **translation operator**
- $\mathbf{v} \in [0, 1]^2$  is a translation vector
- $f : L^2([0, 1]^2) \rightarrow \{1, \dots, L\}$  is a classification functional

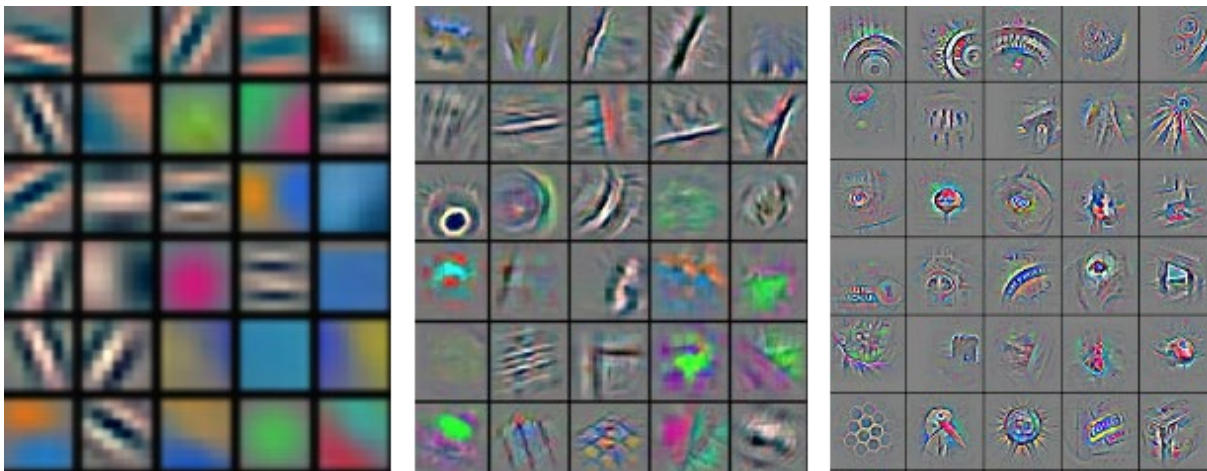
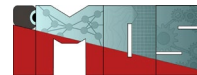
# EPFL Deformation invariance (image classification tasks)



$$|f(\mathcal{L}_\tau x) - f(x)| \approx \|\nabla \tau\| \quad \forall f, \tau$$

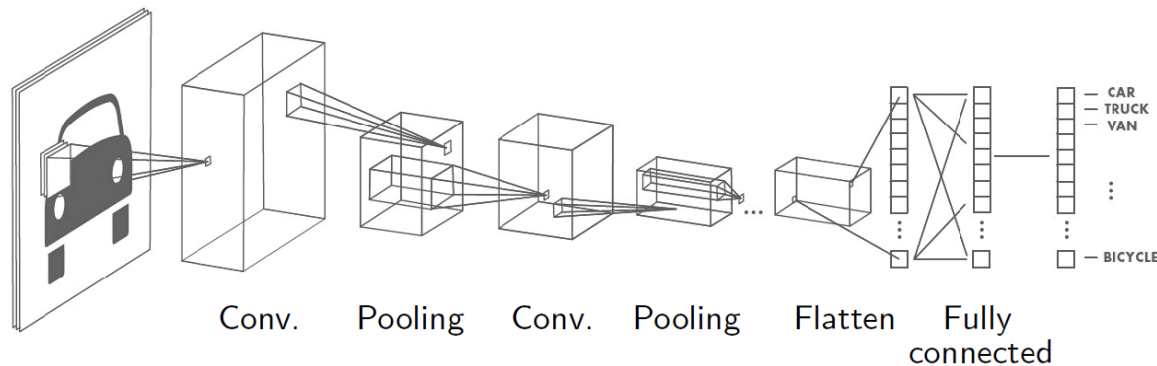
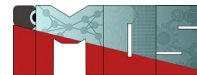
where

- image is modeled as a function  $x \in L^2([0, 1]^2)$
- $\mathcal{L}_\tau x(\mathbf{u}) = x(\mathbf{u} - \tau(\mathbf{u}))$  is a **warping operator**
- $\tau : [0, 1]^2 \rightarrow [0, 1]^2$  is a smooth **deformation field**
- $f : L^2([0, 1]^2) \rightarrow \{1, \dots, L\}$  is a classification functional



Typical features learned by a CNN becoming increasingly complex at deeper layers

Zeiler, Fergus 2013



Conv. layer

$$x_{\ell'}^{(l+1)}(\mathbf{u}) = \xi \left( \sum_{\ell=1}^{d^{(l)}} (w_{\ell'\ell}^{(l+1)} \star x_{\ell}^{(l)})(\mathbf{u}) \right)$$

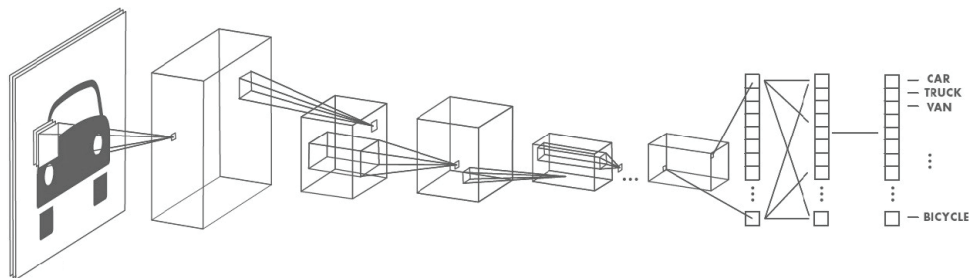
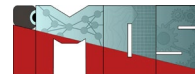
Activation, e.g.  $\xi(x) = \max\{x, 0\}$  rectified linear unit (ReLU)

Parameters filters  $W^{(1)}, \dots, W^{(L)}$

Pooling  $x_{\ell}^{(l+1)}(\mathbf{u}) = \|x_{\ell}^{(l)}(\mathbf{u}') : \mathbf{u}' \in \mathcal{N}(\mathbf{u})\|_p \quad p = 1, 2, \text{ or } \infty$

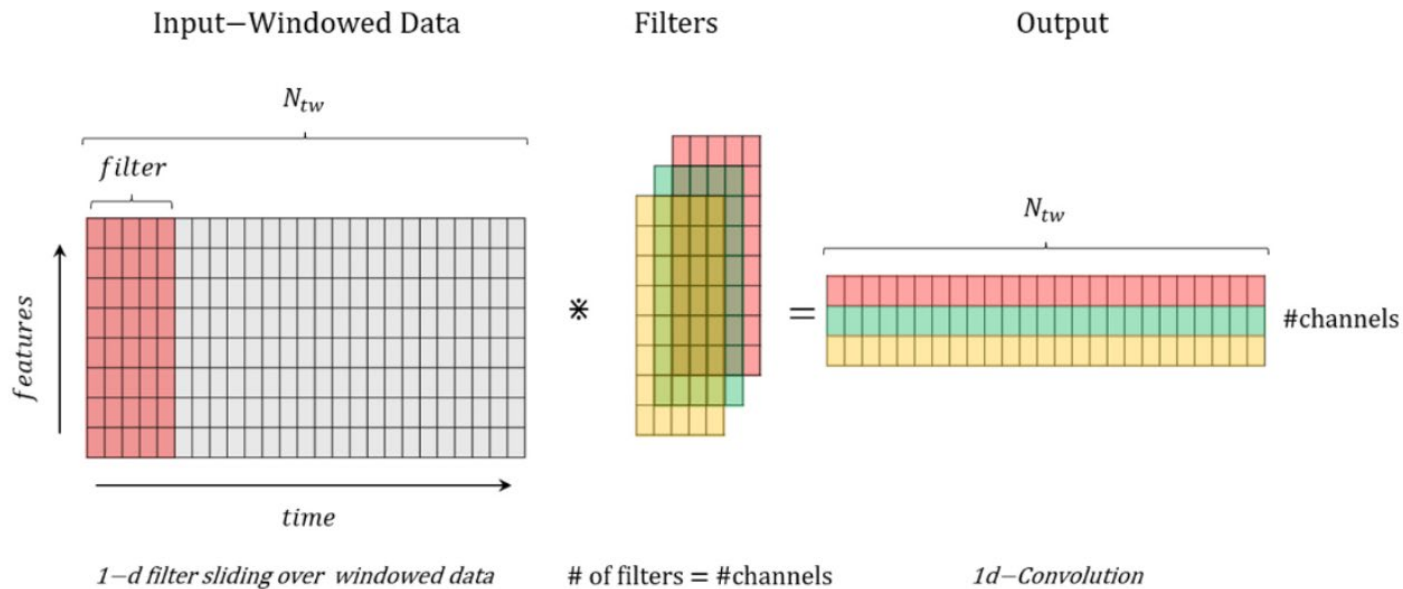
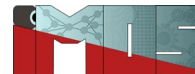
LeCun et al. 1989 (Image: Debarko De)

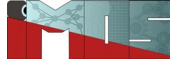
# Key properties of CNNs



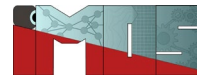
- ☺ Convolutional filters (**Translation invariance+Self-similarity**)
- ☺ Multiple layers (**Compositionality**)
- ☺ Filters localized in space (**Locality**)
- ☺  $\mathcal{O}(1)$  parameters per filter (independent of input image size  $n$ )
- ☺  $\mathcal{O}(n)$  complexity per layer (filtering done in the spatial domain)
- ☺  $\mathcal{O}(\log n)$  layers in classification tasks

LeCun et al. 1989





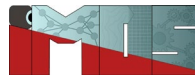
# Hyperparameter search



- **Definition:** Hyperparameter tuning involves adjusting the parameters of a machine learning model that are set prior to the start of the learning process. These parameters influence model training and can significantly affect performance.

## Why It's Important

- Hyperparameters control the learning process and directly impact the effectiveness and efficiency of the model.
- Proper tuning can prevent overfitting, underfitting, and can improve model accuracy.

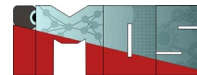


- In a general sense, tuning involves these components:
  - a learning algorithm  $A$ , parameterized by hyperparameters  $\lambda$
  - training and validation data  $\mathbf{X}^{(tr)}$ ,  $\mathbf{X}^{(vl)}$
  - a model  $\mathcal{M} = \mathcal{A}(\mathbf{X}^{(tr)} \mid \lambda)$
  - loss function  $\mathcal{L}$  to assess quality of  $\mathcal{M}$ , typically using  $\mathbf{X}^{(vl)}$ :

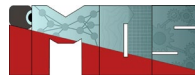
$$\mathcal{L}(\mathcal{M} \mid \mathbf{X}^{(te)})$$

- In optimization terms, we aim to find  $\lambda^*$  (assuming minimization):

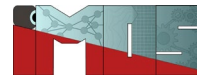
$$\lambda^* = \arg \min_{\lambda} \mathcal{L}(\mathcal{A}(\mathbf{X}^{(tr)} \mid \lambda) \mid \mathbf{X}^{(vl)}) = \arg \min_{\lambda} \underbrace{\mathcal{F}(\lambda \mid \mathcal{A}, \mathbf{X}^{(tr)}, \mathbf{X}^{(vl)}, \mathcal{L})}_{\text{objective function}}$$



- Most often done using a combination of grid and manual search:
  - grid search suffers from the curse of dimensionality
  - manual tuning leads to poor reproducibility

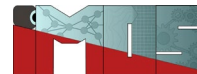


- We need to define the hyperparameters we want to optimize:
  - Architecture (#layers, #kernels, stride, kernel size)
  - Learning rate, optimizer (momentum)
  - Regularizations (weight decay rate, dropout probability)
  - Batchnorm / no batchnorm
  - Number of epochs: The number of times the learning algorithm will work through the entire training dataset.
  - Batch size: The number of training examples utilized in one iteration.
- Our diagnostic statistics:
  - Loss curves
  - Gradient norms
  - Accuracy / Visual output (generative models)
  - Performance on training vs validation set
  - Other abnormal behaviors

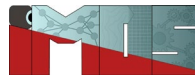


$$\min_{\alpha, \xi, b} \frac{1}{2} \sum_{i \in SV} \sum_{j \in SV} \alpha_i \alpha_j y_i y_j \kappa(\mathbf{x}_i, \mathbf{x}_j) + C \sum_{i=1}^n \xi_i,$$

$$\text{subject to } y_i \left( \sum_{j \in SV} \alpha_i \alpha_j y_i y_j \kappa(\mathbf{x}_i, \mathbf{x}_j) + b \right) \geq 1 - \xi_i, \quad \xi_i \geq 0, \quad \forall i.$$

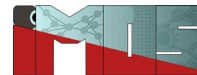


- Grid Search: Exhaustive search over a specified parameter range.
- Random Search: Randomly samples the search space and evaluates sets from a specified probability distribution.
- Bayesian Optimization: Uses a probabilistic model to predict which hyperparameters might lead to better performances.
- Gradient-based Optimization: Adjusts hyperparameters using gradient descent to minimize a predefined loss function.
- Evolutionary Algorithms: Uses mechanisms inspired by biological evolution: reproduction, mutation, recombination, and selection.



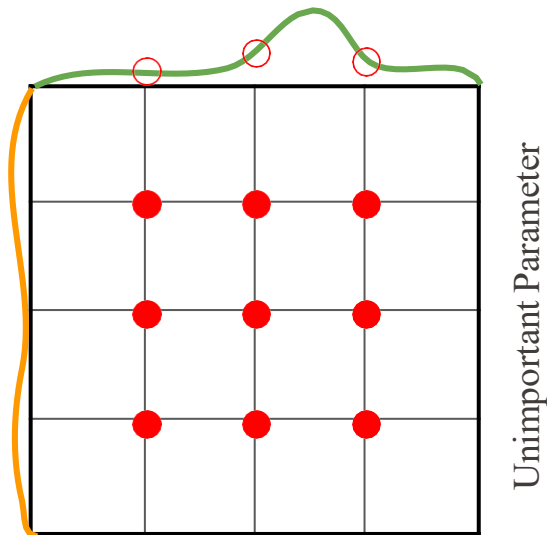
- When tuning parameters, only use a small portion of the dataset for fast iteration.
- Start from a larger learning rate for fast prototyping.
- Cross-validation strategy:
  - coarse  $\rightarrow$  fine: cross-validation in stages
  - First stage: only a few epochs to get rough idea of what parameters work
  - Second stage: longer running time, finer search
  - ... (repeat as necessary)

# Random Search vs. Grid Search



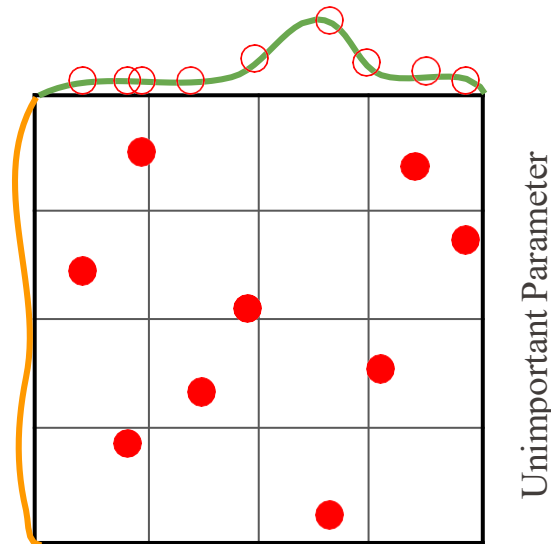
Random Search for:

Grid Layout



Important Parameter

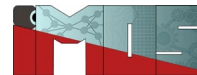
Random Layout



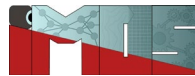
Important Parameter

Hyper-Parameter Optimization  
Bergstra and Bengio, 2012

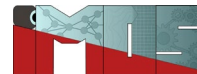
# Can we use Machine Learning instead?



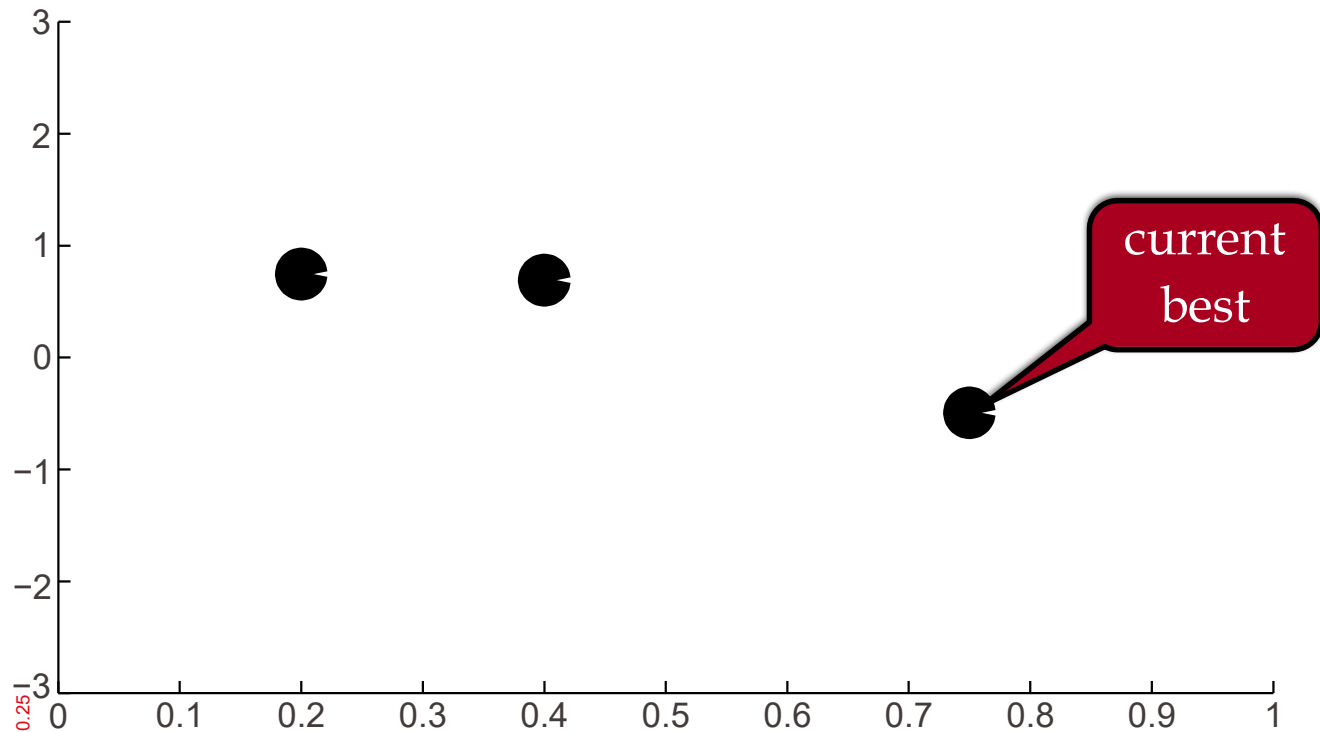
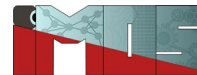
- To predict regions of the hyperparameter space that might give better results.
- To predict how well a new combination of hyperparameters will do and also model the uncertainty of that prediction



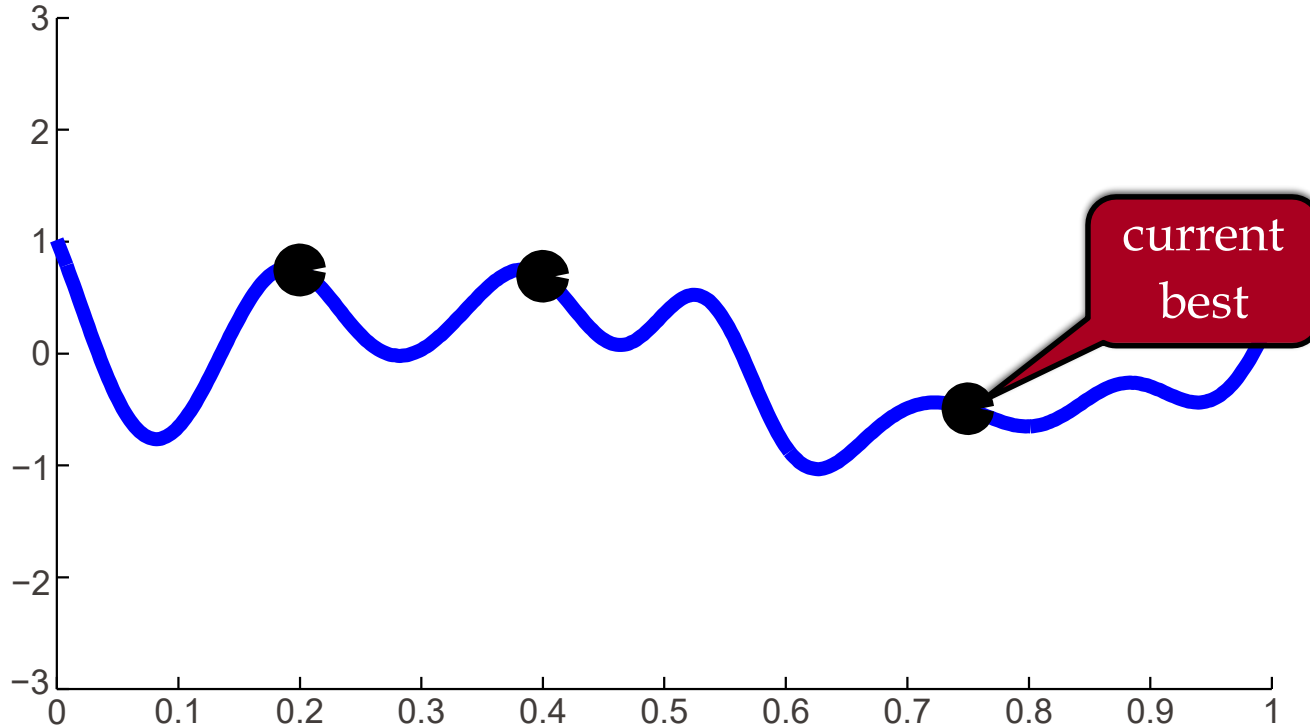
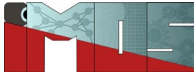
- Build a probabilistic model for the objective.
- Include hierarchical structure about units, etc.
- Compute the posterior predictive distribution.
- Integrate out all the possible true functions.
- Gaussian process regression is often used.
- Optimize a cheap proxy function instead.
- The model is much cheaper than the true objective.
- The main insight:
  - Make the proxy function exploit uncertainty to balance exploration against exploitation.



- Frame Hyperparameter Search as an Optimization Problem
- Model the estimation of the function from hyperparameters to the error metric as a regression problem
- Use Gaussian Process Prior: “Similar inputs have similar outputs” to build a statistical model of the function. Prior is weak but general and effective.
- Use statistics to tell us:
  - Location of expected minimum of the function
  - Expected Improvement of trying other parameters



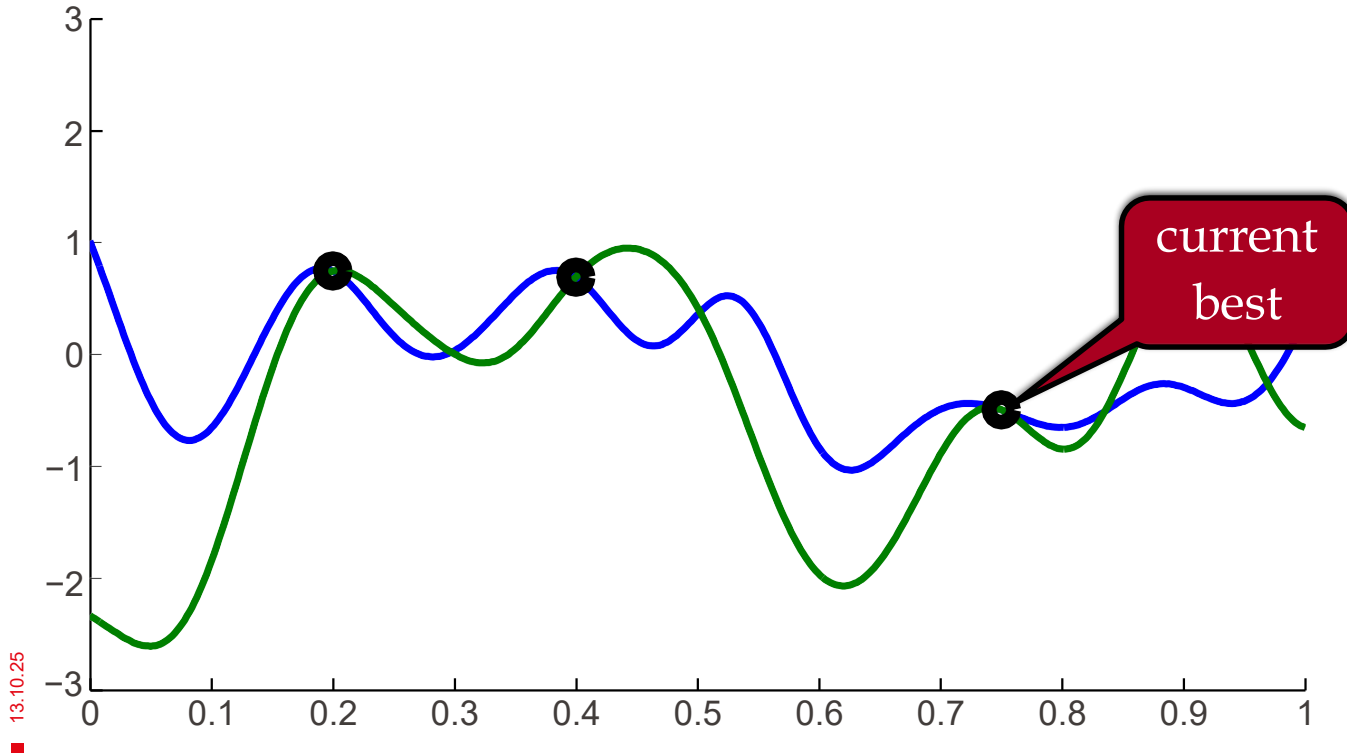
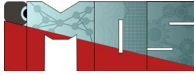
# EPFL The Bayesian Optimization Idea



13.10.25

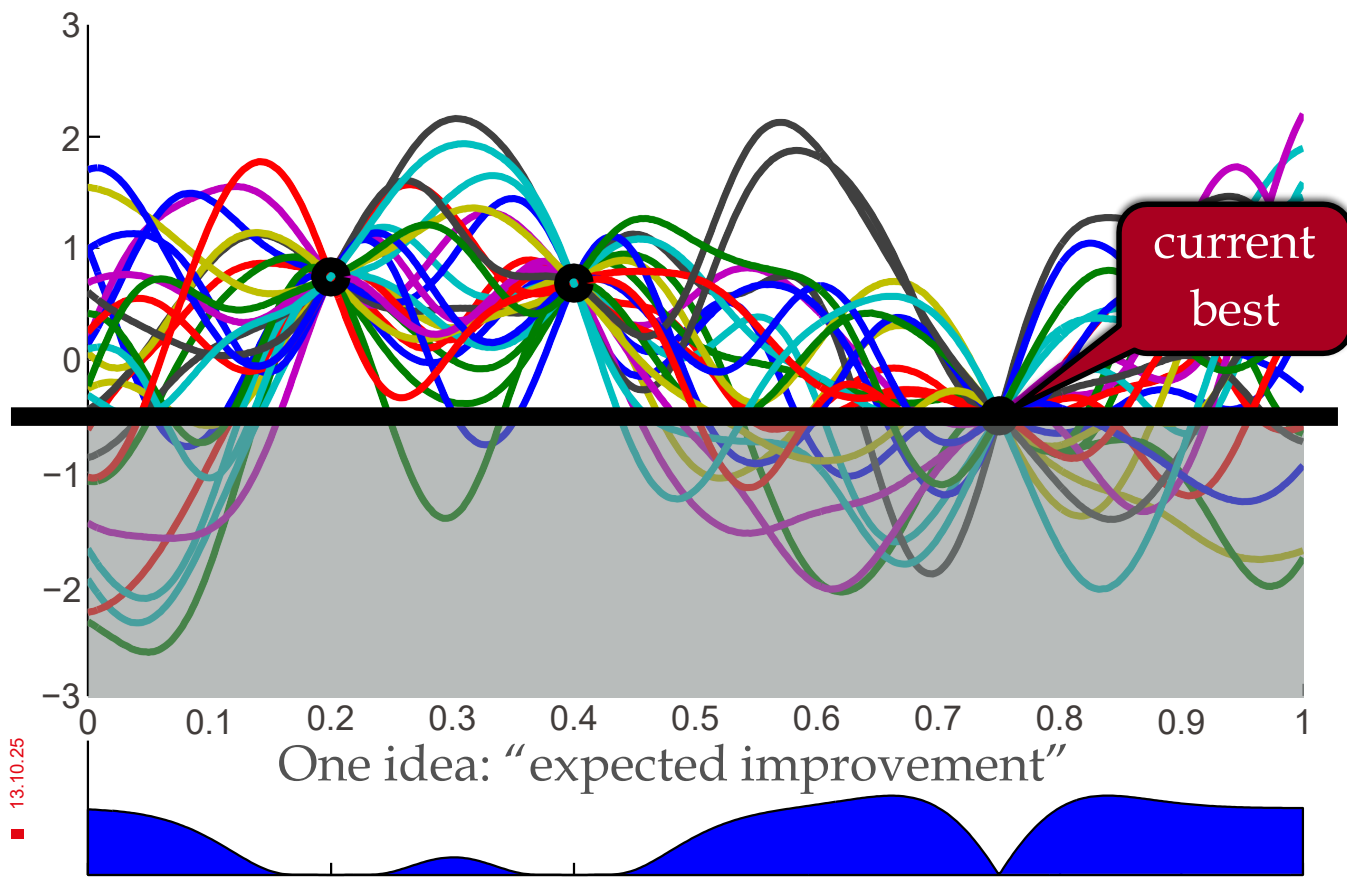
Source: R. Adams, 2017

# EPFL The Bayesian Optimization Idea



■ 13.10.25

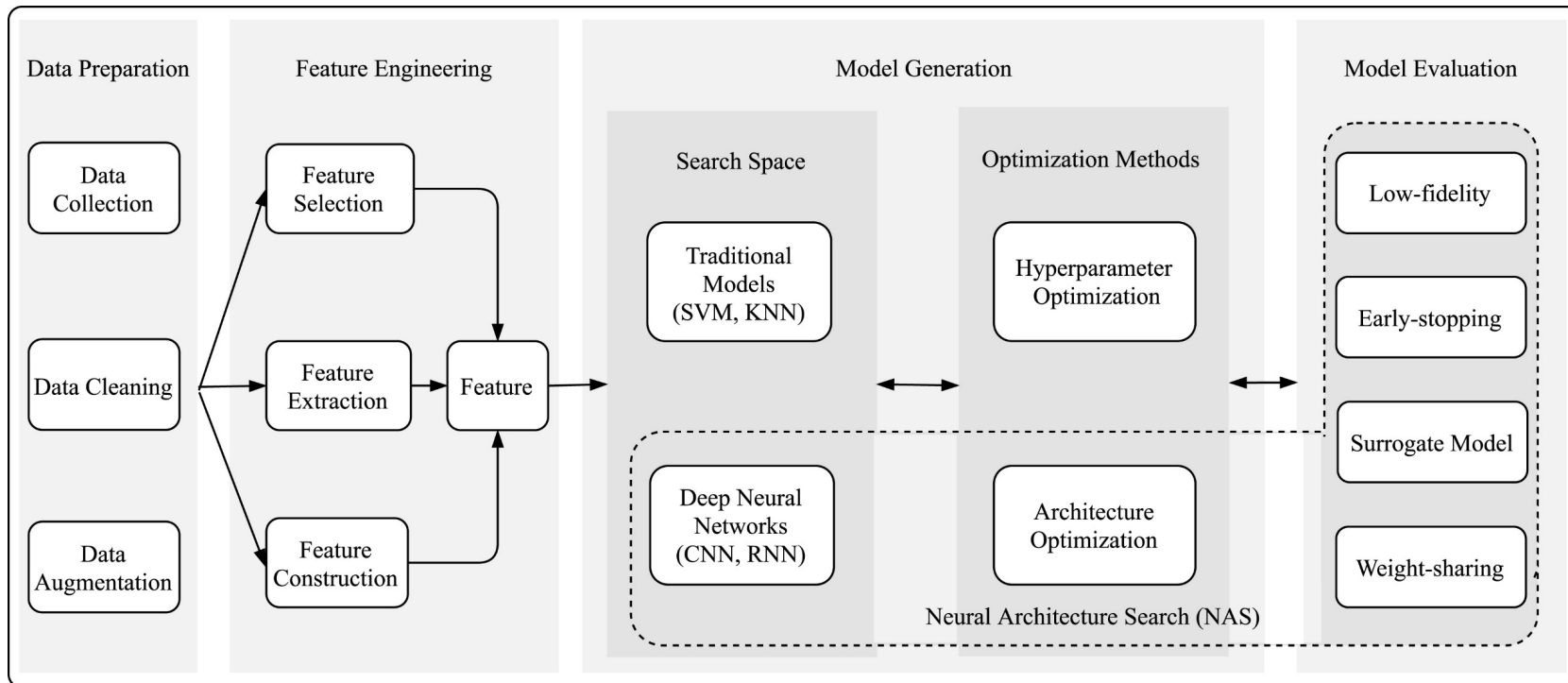
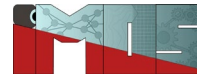
Source: R. Adams, 2017



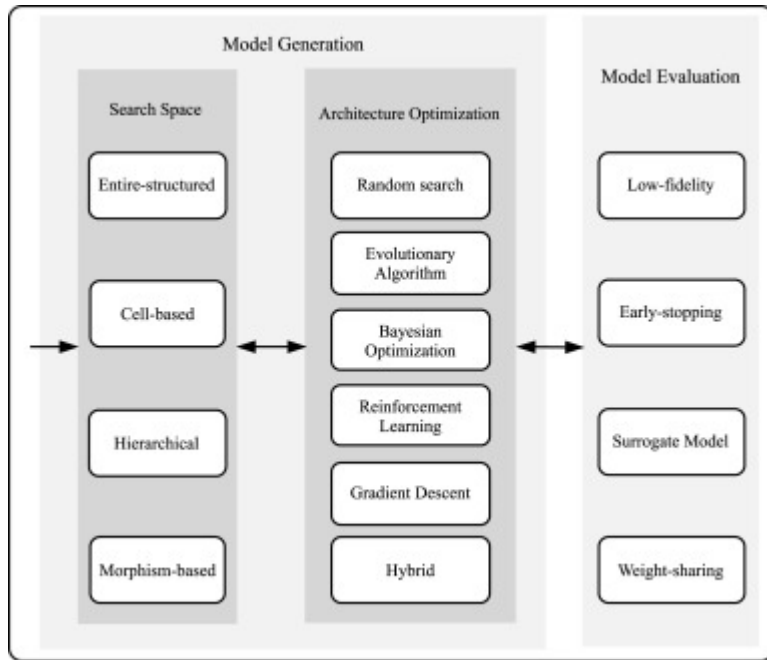
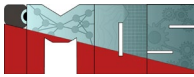
Where should we evaluate next in order to improve the most?

Source: R. Adams, 2017

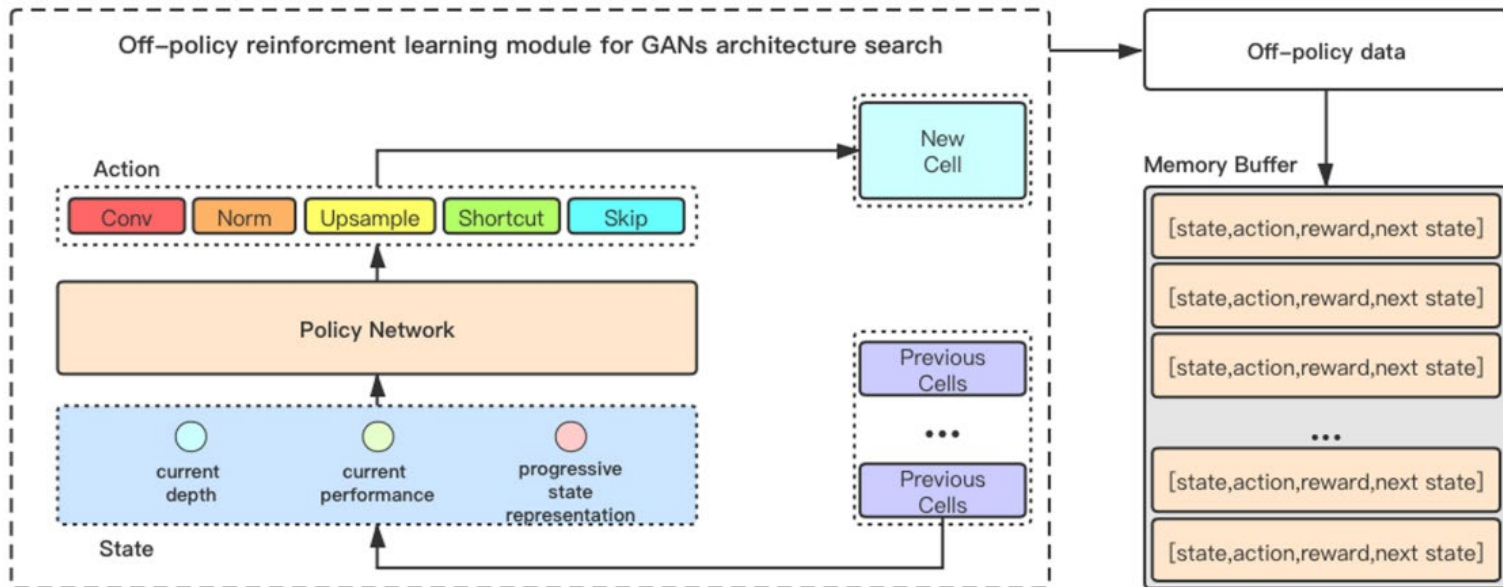
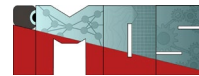
# From hyperparameter search to Neural Architecture Search

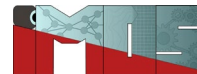


# EPFL An overview of neural architecture search pipeline

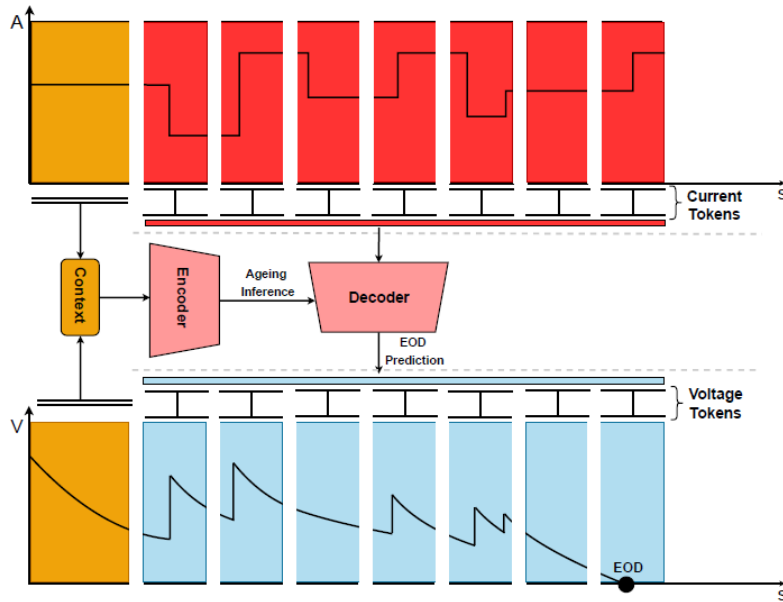
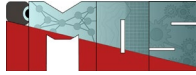


He, Xin, Kaiyong Zhao, and Xiaowen Chu. "AutoML: A Survey of the State-of-the-Art." *Knowledge-Based Systems* 212 (2021): 106622.



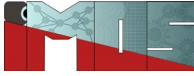


- **Scikit-learn**: Offers grid and random search capabilities.
- **Hyperopt**: Advanced optimization, including Bayesian and random.
- **Optuna**: Framework for automatic hyperparameter optimization, supporting sophisticated algorithms.

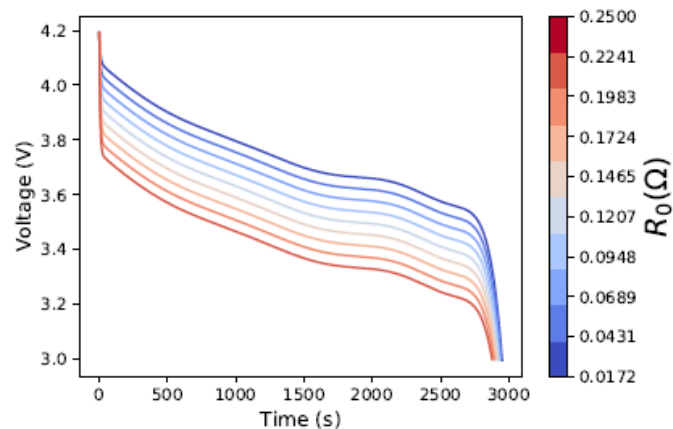
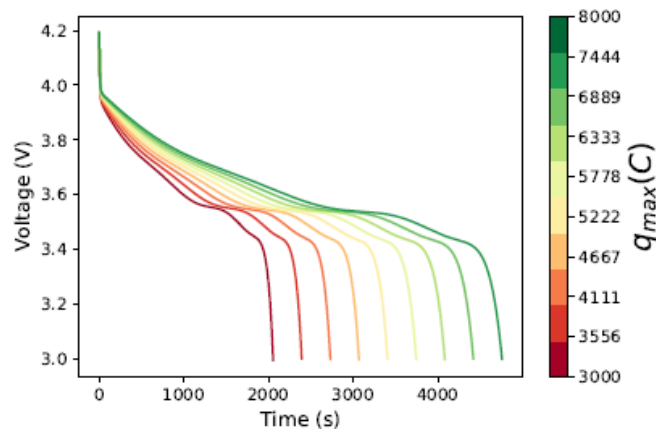
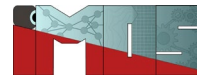


# Ageing-aware Battery Discharge Prediction

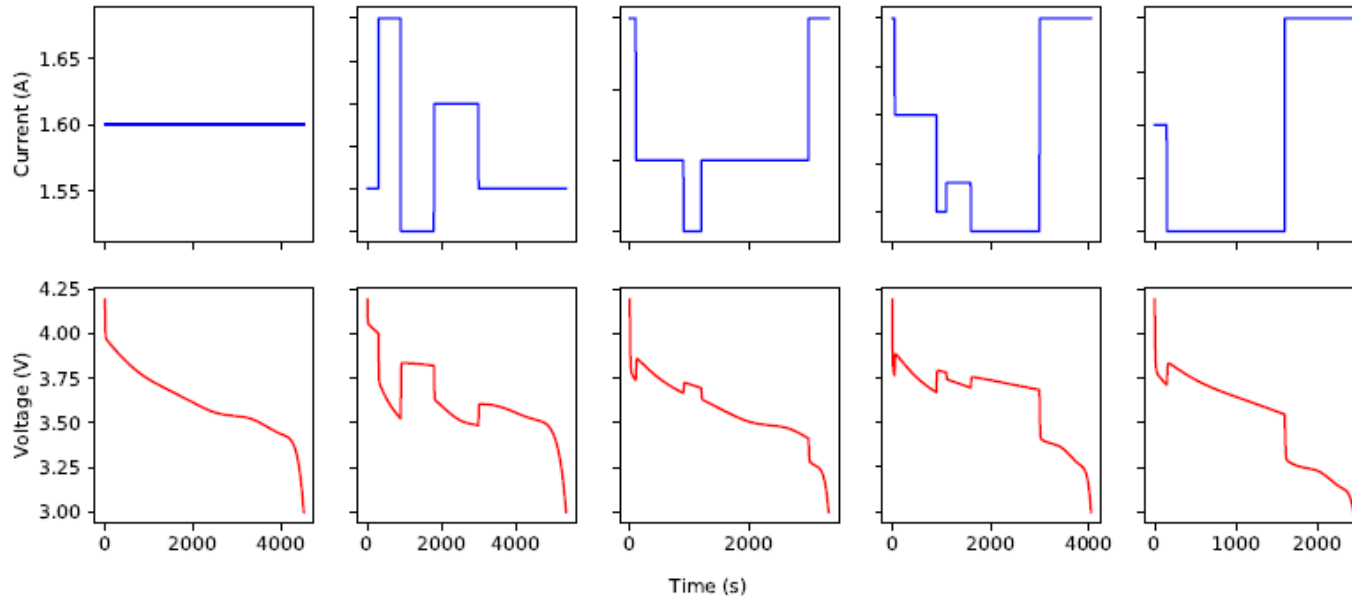
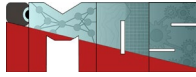
# Degradation of Li-Ion batteries → importance of precise planning

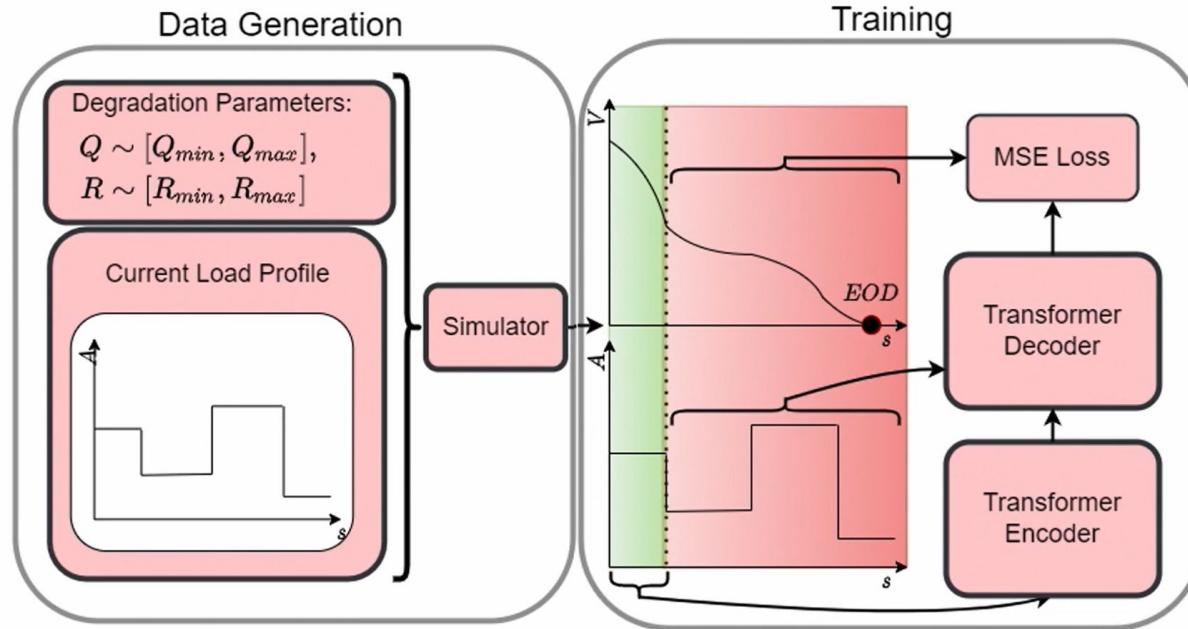
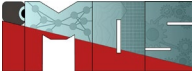


# Effect of varying the degradation parameters on the voltage discharge curve of a Li-ion battery

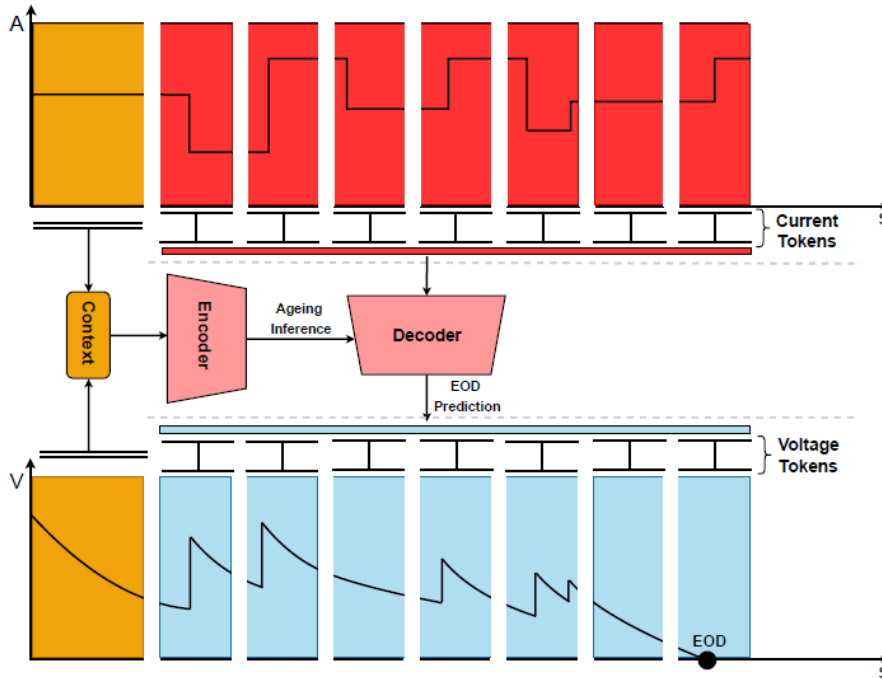
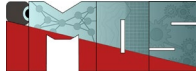


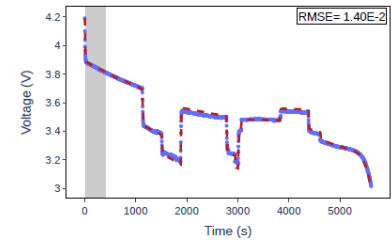
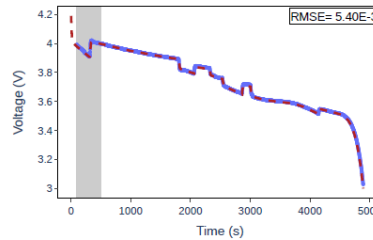
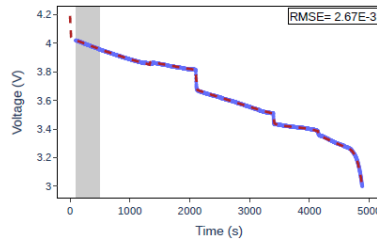
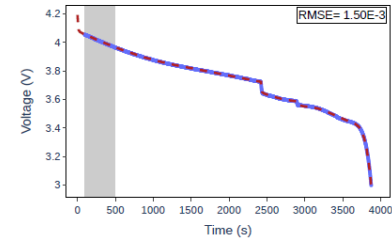
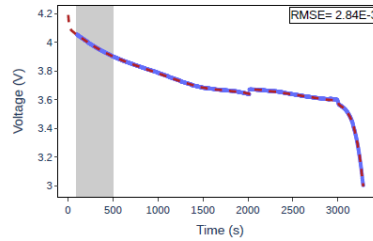
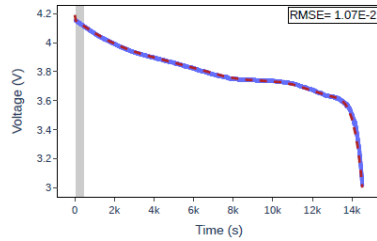
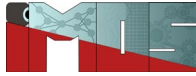
# Discharge behaviors with respect to the different load profiles

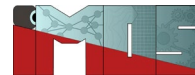




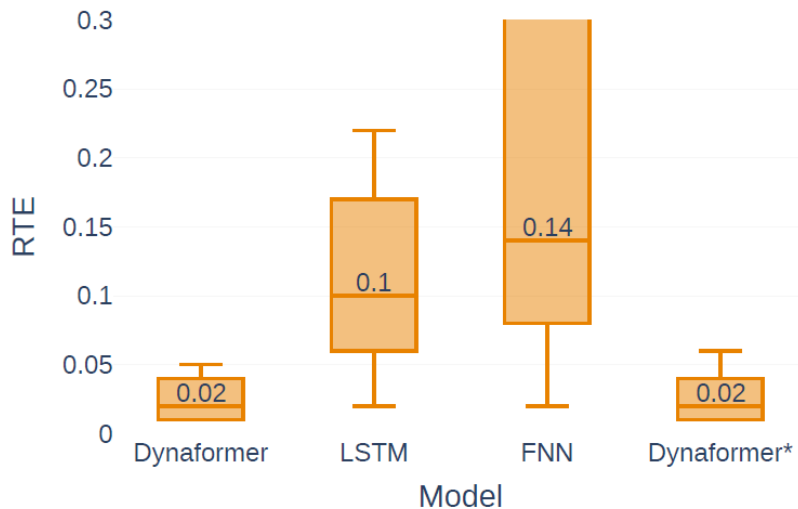
# Transformer-based long-term battery discharge prediction → Dynaformer



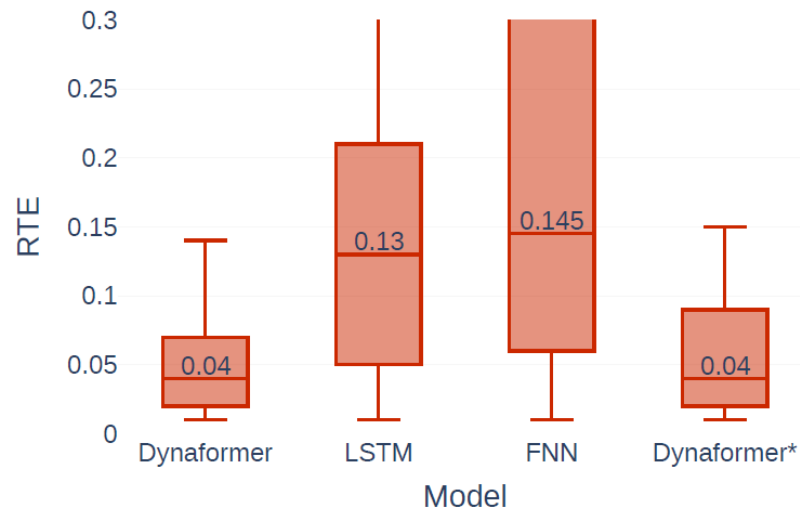




Interpolation



Extrapolation

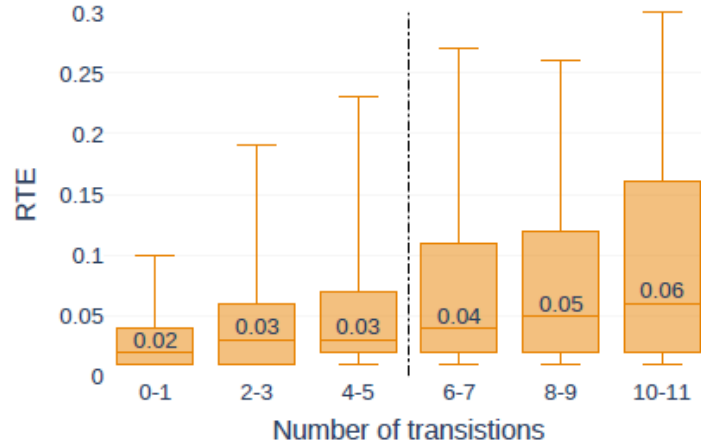
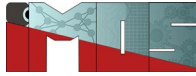


Dynaformer\* → trained with variable current profiles

\*RTE = relative temporal error

Biggio, L., Bendinelli, T., Kulkarni, C., & Fink, O. (2023). Ageing-aware battery discharge prediction with deep learning, Applied Energy

# Performance dependent on the complexity of the the load profiles



# Implicit learning of the degradation parameters in the latent space

