

Neutron and X-ray Scattering of Quantum Materials

Ellen Fogh

Laboratory for Quantum Magnetism
École Polytechnique Fédérale de Lausanne

Thorsten Schmitt

Spectroscopy of Quantum Materials
Paul Scherrer Institute

Outline for today

- Recap from last week (Chapters 1-2 + 4)
- Neutron diffraction (Chapters 9-10, except 9.1.5-8)
 - Crystals
 - Powders
 - Magnetic diffraction
 - Instruments

From last week: Basic scattering theory

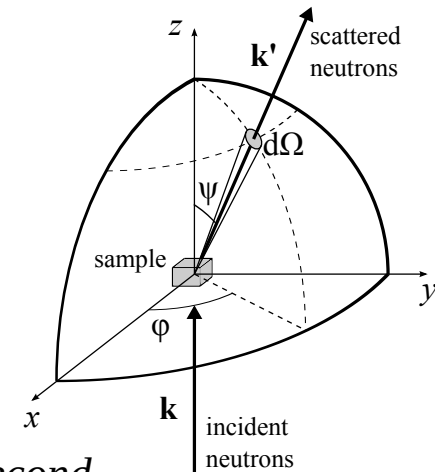
Flux: $\Psi = \frac{\text{number of neutrons hitting a surface per second}}{\text{surface area perpendicular the beam}}$

Cross section: $\sigma = \frac{\text{number of scattered neutrons per second}}{\Psi}$

Differential cross section: $\frac{d\sigma}{d\Omega} = \frac{1}{\Psi} \frac{\text{number of scattered neutrons} \in d\Omega \text{ per second}}{d\Omega}$

Partial differential cross section:

$$\frac{d^2\sigma}{d\Omega dE_f} = \frac{1}{\Psi} \frac{\text{number of scattered neutrons} \in d\Omega \wedge \text{with energies} \in \text{the interval } [E_f, E_f + dE_f] \text{ per second}}{d\Omega dE_f}$$



Absorption and beam attenuation

- Good absorbers: Cd, Gd, ^3He , B
- Useful for shielding and neutron detectors
- Sometimes possible to substitute with less absorbing isotope. Examples
 - $\text{SrCu}_2(\text{BO}_3)_2$: use ^{11}B instead of ^{10}B
 - $\text{Gd}_3\text{Ga}_5\text{O}_{12}$: use ^{160}Gd instead of any of the other Gd isotopes
- Isolating isotopes is expensive

Incoherent scattering

- Creates isotropic scattering (meaning no q -dependence)
- Comes from the fact the scattering cross sections vary over the sample
- Useful for correcting for detector efficiency
- Otherwise it mostly shows up as unwanted background

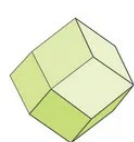
Diffraction

- *Crystalline materials*
- *Bragg's law*
- *Single crystals*
- *Powders*

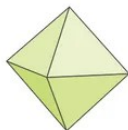
How do we define a crystal?

Crystal symmetries and defining a lattice

Cubic



garnet



spinel



halite



pyrite

Tetragonal



apophyllite



rutile



zircon



wulfenite

Orthorhombic



barite



olivine



topaz



sulfur

Hexagonal or Trigonal



corundum



quartz



ilmenite

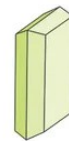


calcite

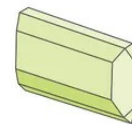
Monoclinic



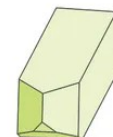
diopside



gypsum



epidote

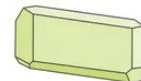


orthoclase

Triclinic



albite



wollastonite

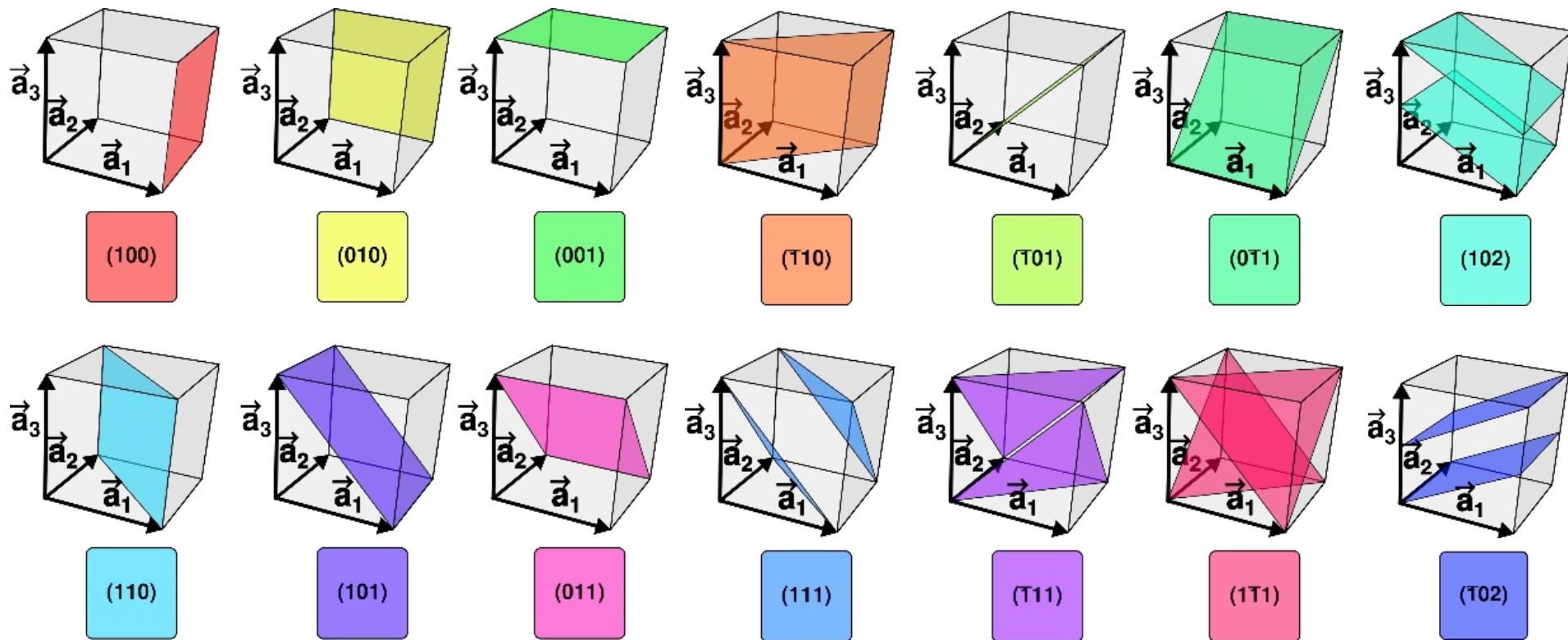


kyanite

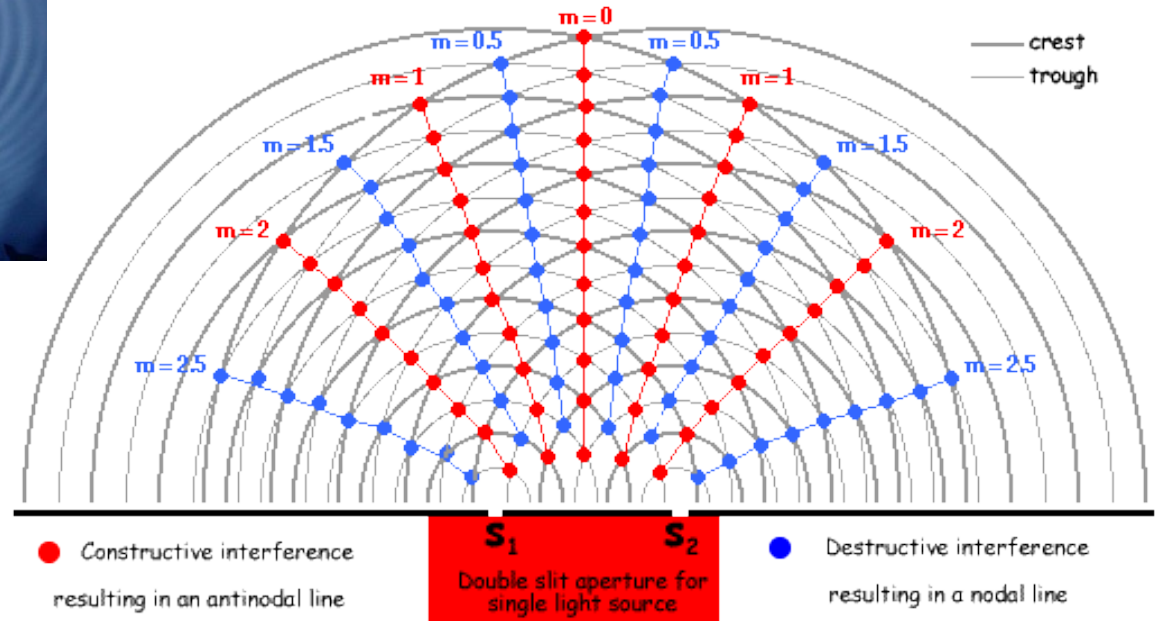


rhodonite

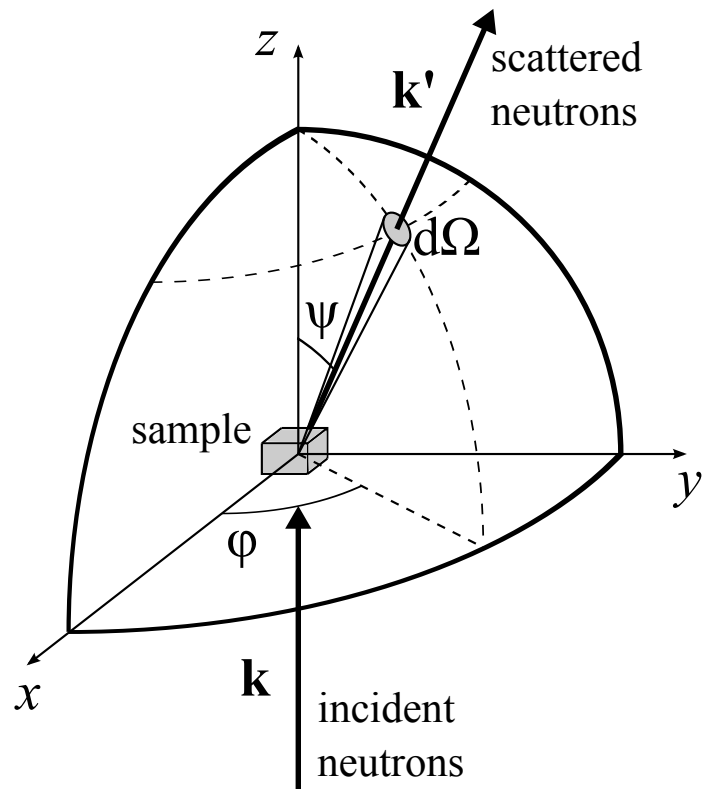
Crystal planes and Miller indices



Interference of waves



Scattering only from reciprocal lattice vectors



Reciprocal lattice vectors:

$$\boldsymbol{\tau} = H\mathbf{a}^* + K\mathbf{b}^* + L\mathbf{c}^*$$

$\boldsymbol{\tau}$ is perpendicular to the (HKL) plane

$$|\boldsymbol{\tau}| = \frac{2\pi}{d}$$

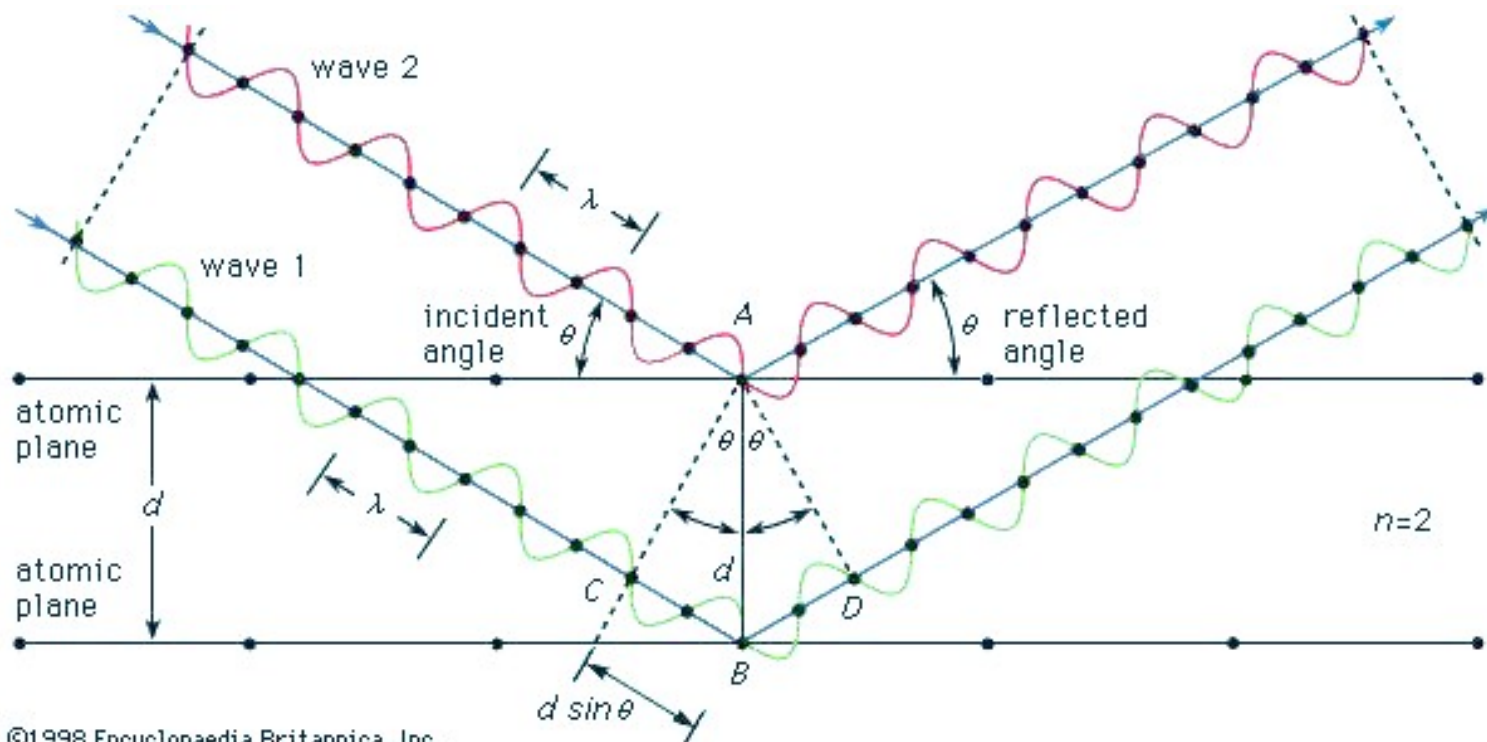
Scattering vector:

$$\mathbf{q} = \mathbf{k} - \mathbf{k}'$$

Diffraction from the lattice planes happens only when $\mathbf{q} = \boldsymbol{\tau}$

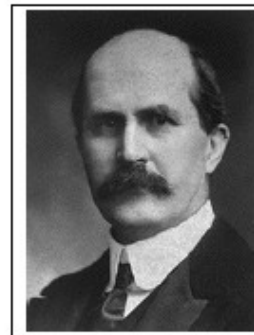
Bragg's law

$$n\lambda = 2d \sin \theta$$

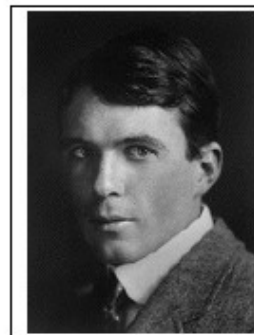


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Nobel Prize 1915

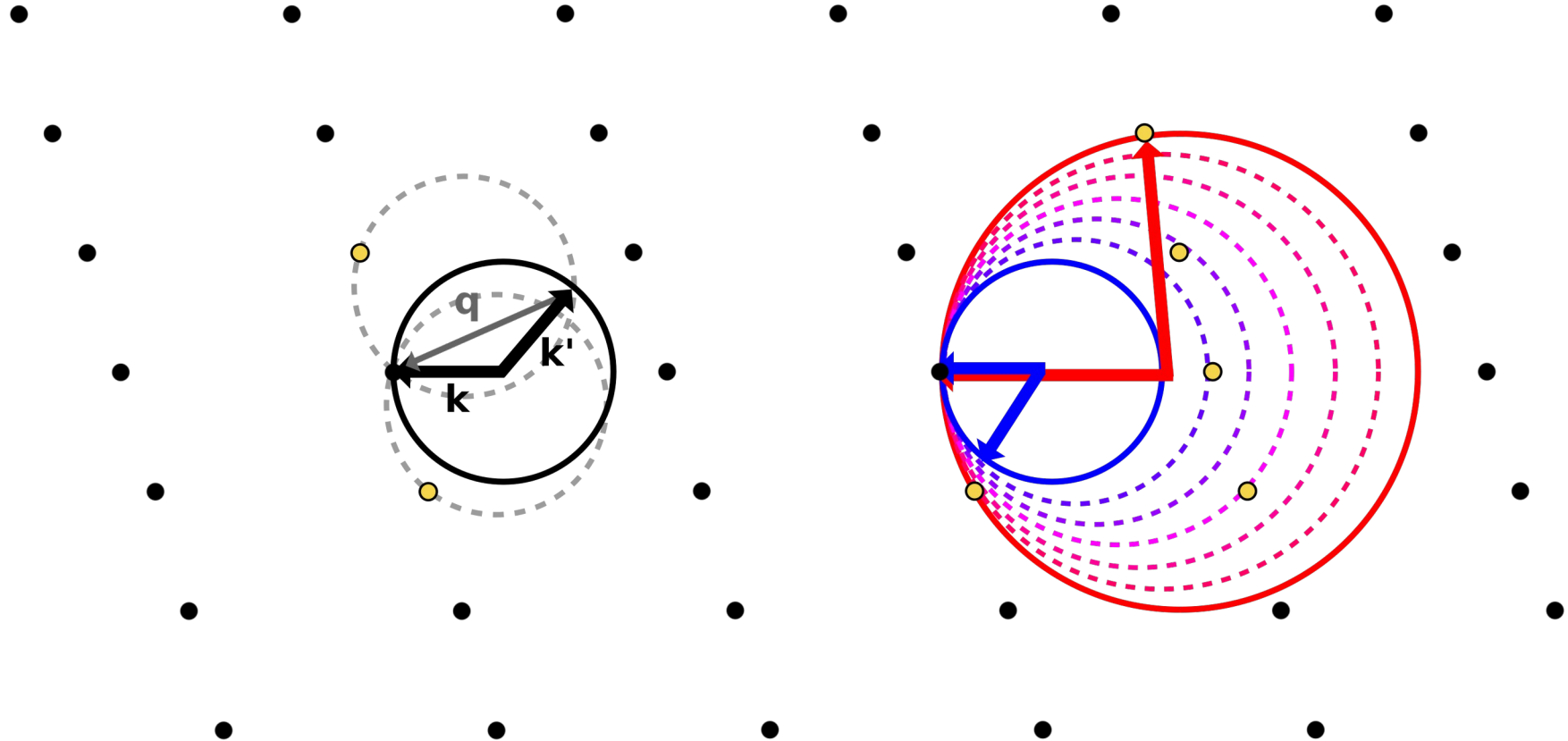


W. H. Bragg

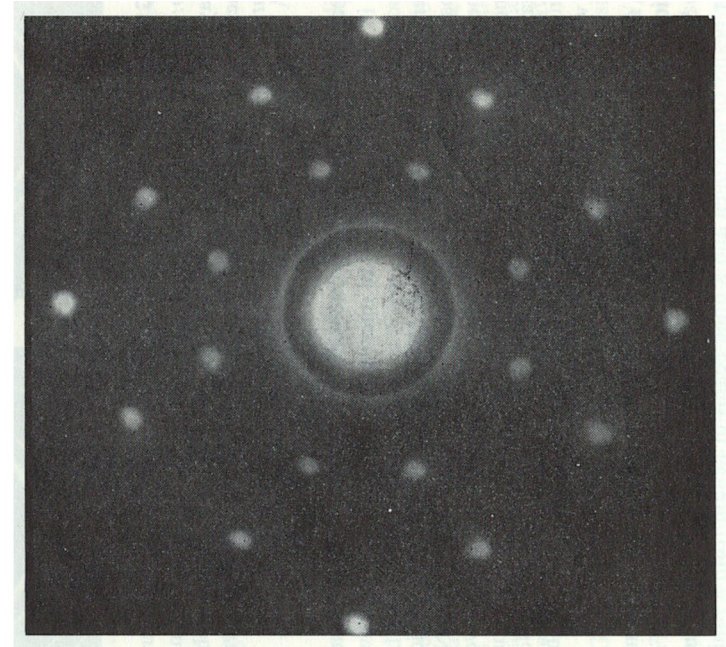
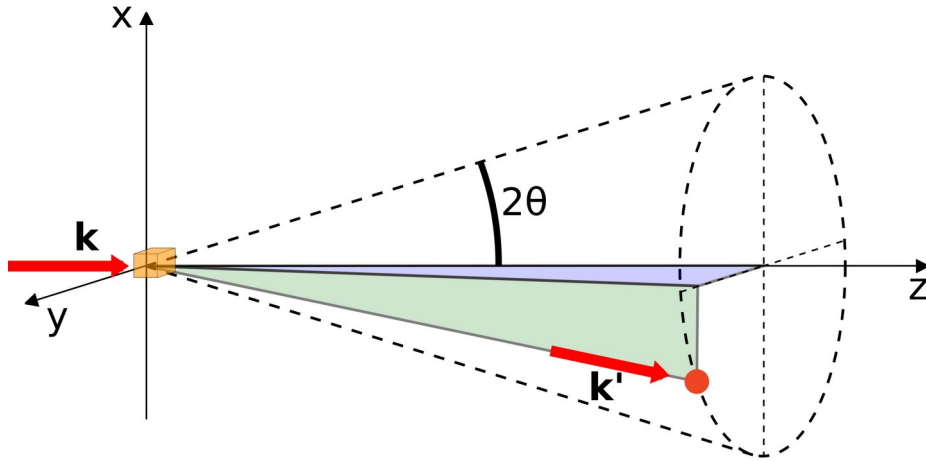


W. L. Bragg

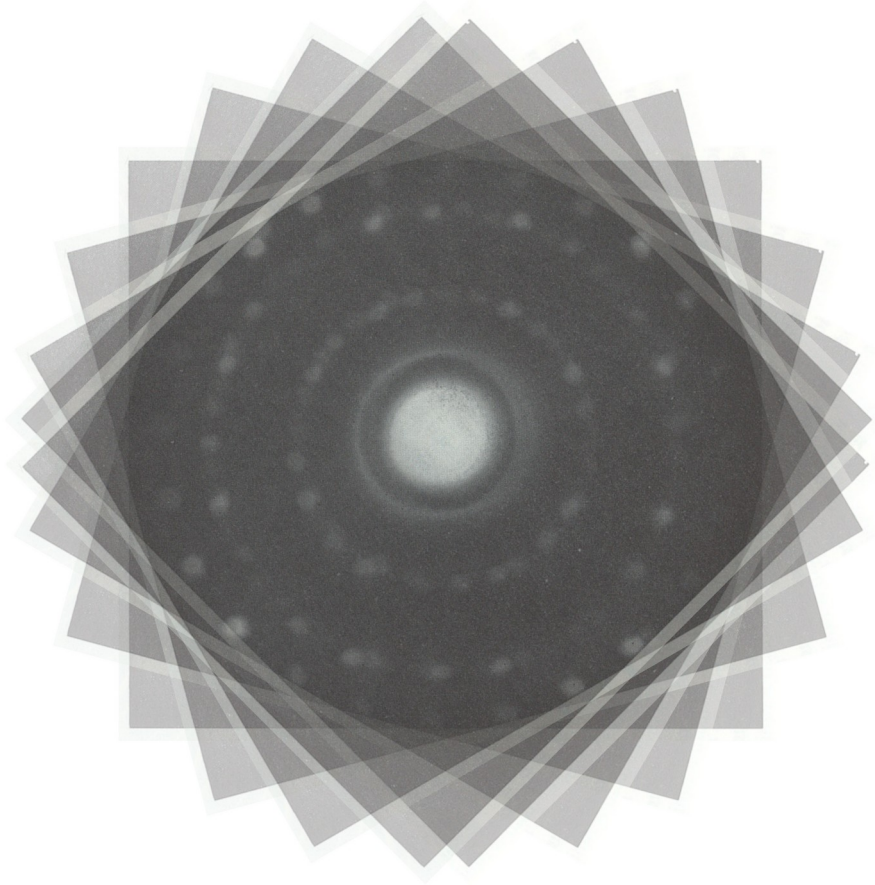
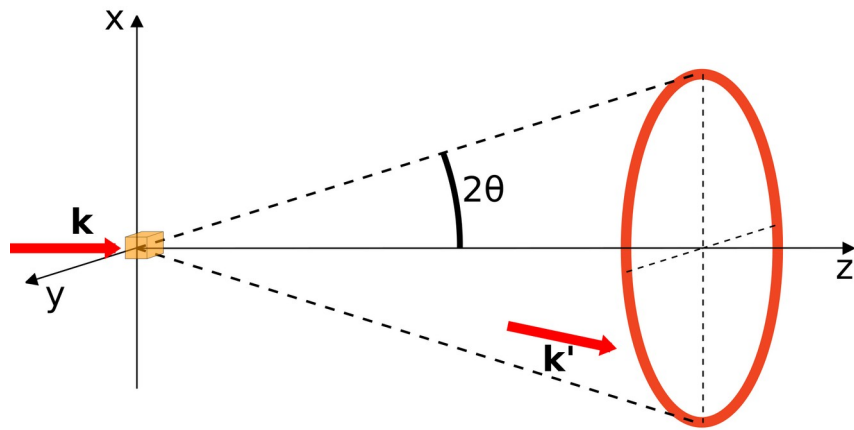
The Laue condition and the Ewald's sphere



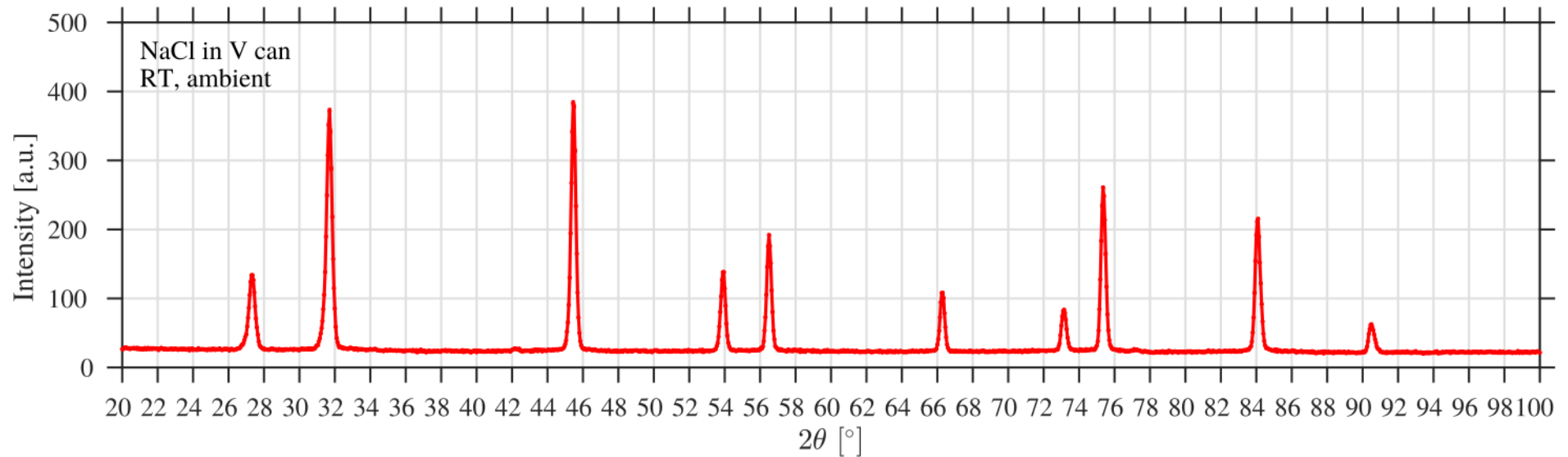
Single-crystal diffraction



Powder diffraction



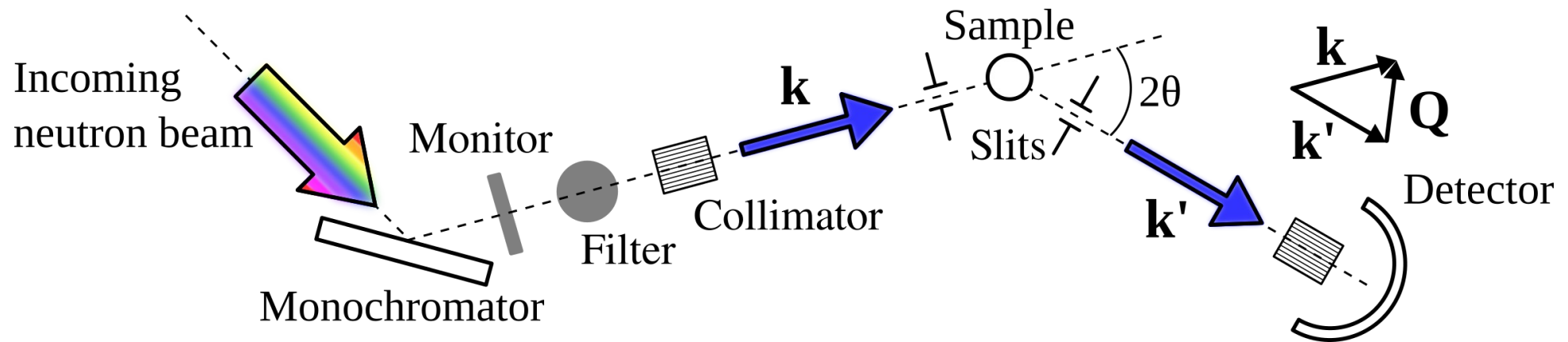
Powder diffraction



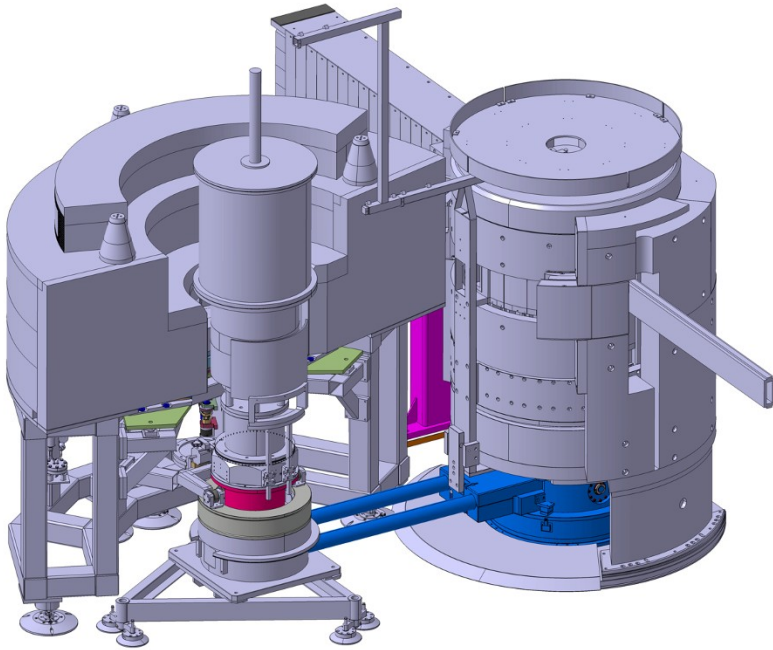
Diffractometers

- *Single-crystal diffractometers*
- *Powder diffractometers*
- *Monochromatic vs. polychromatic beams*
- *Time-of-flight techniques*

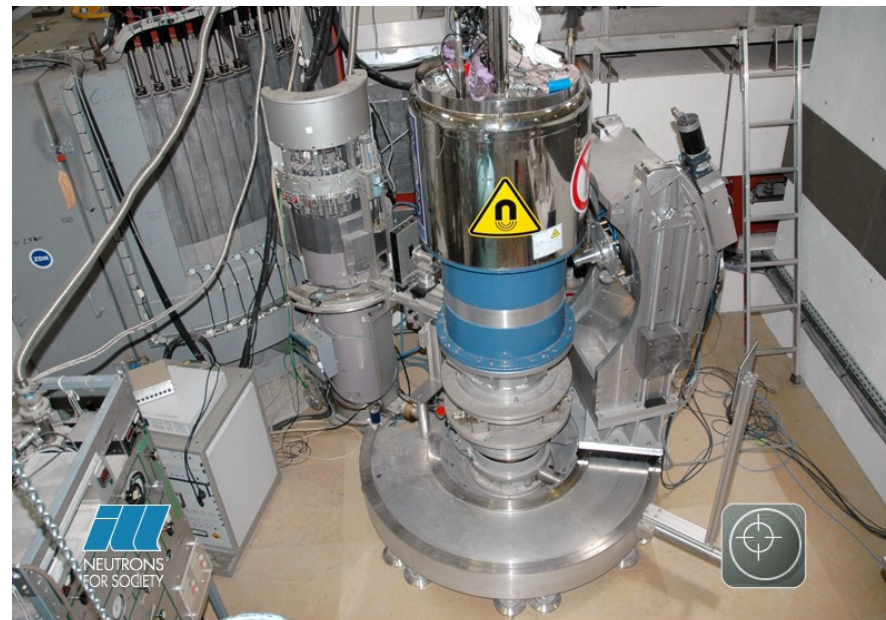
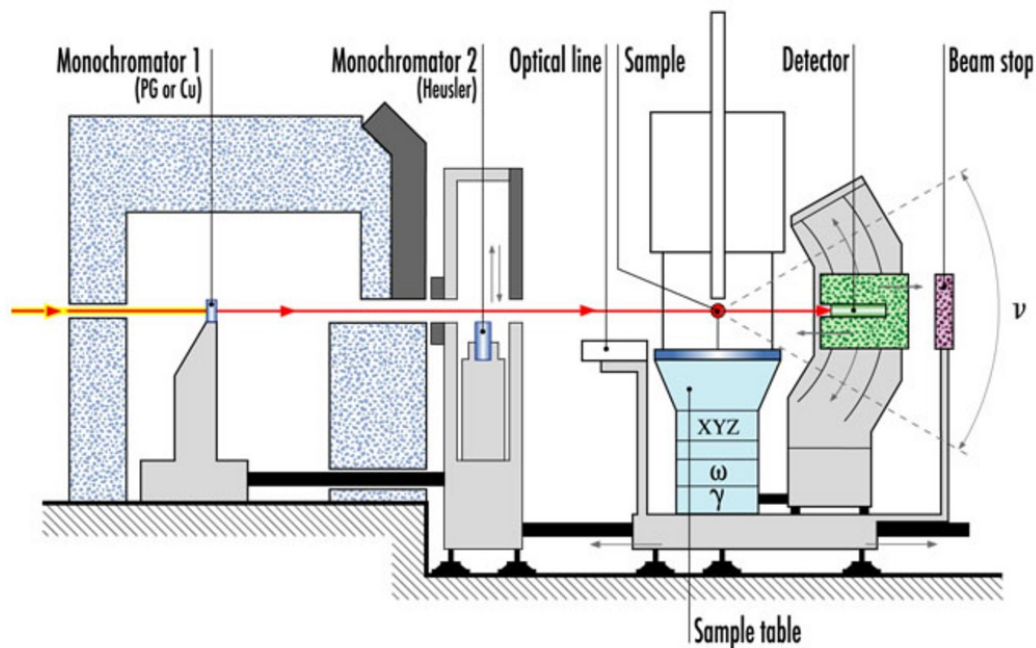
Two-axis neutron diffractometer



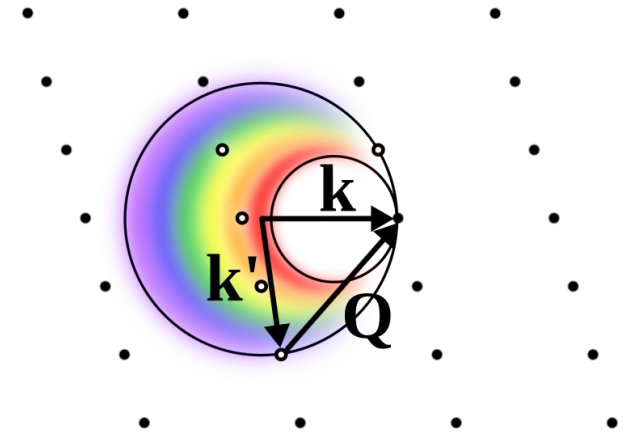
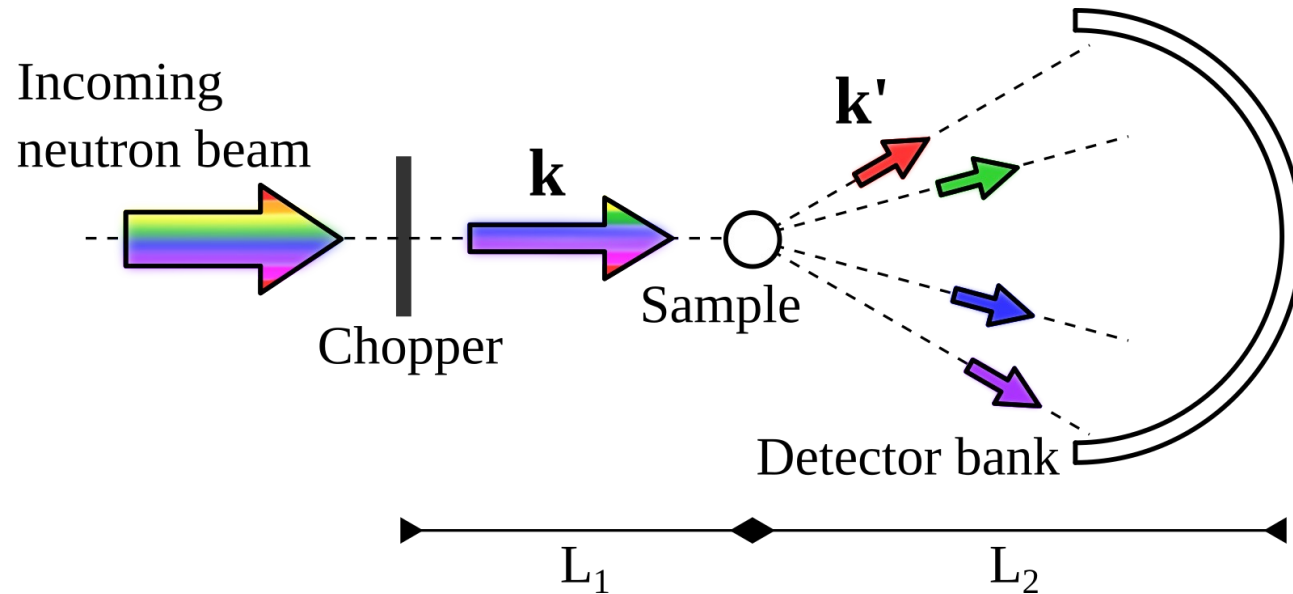
DMC: powder diffractometer at the PSI



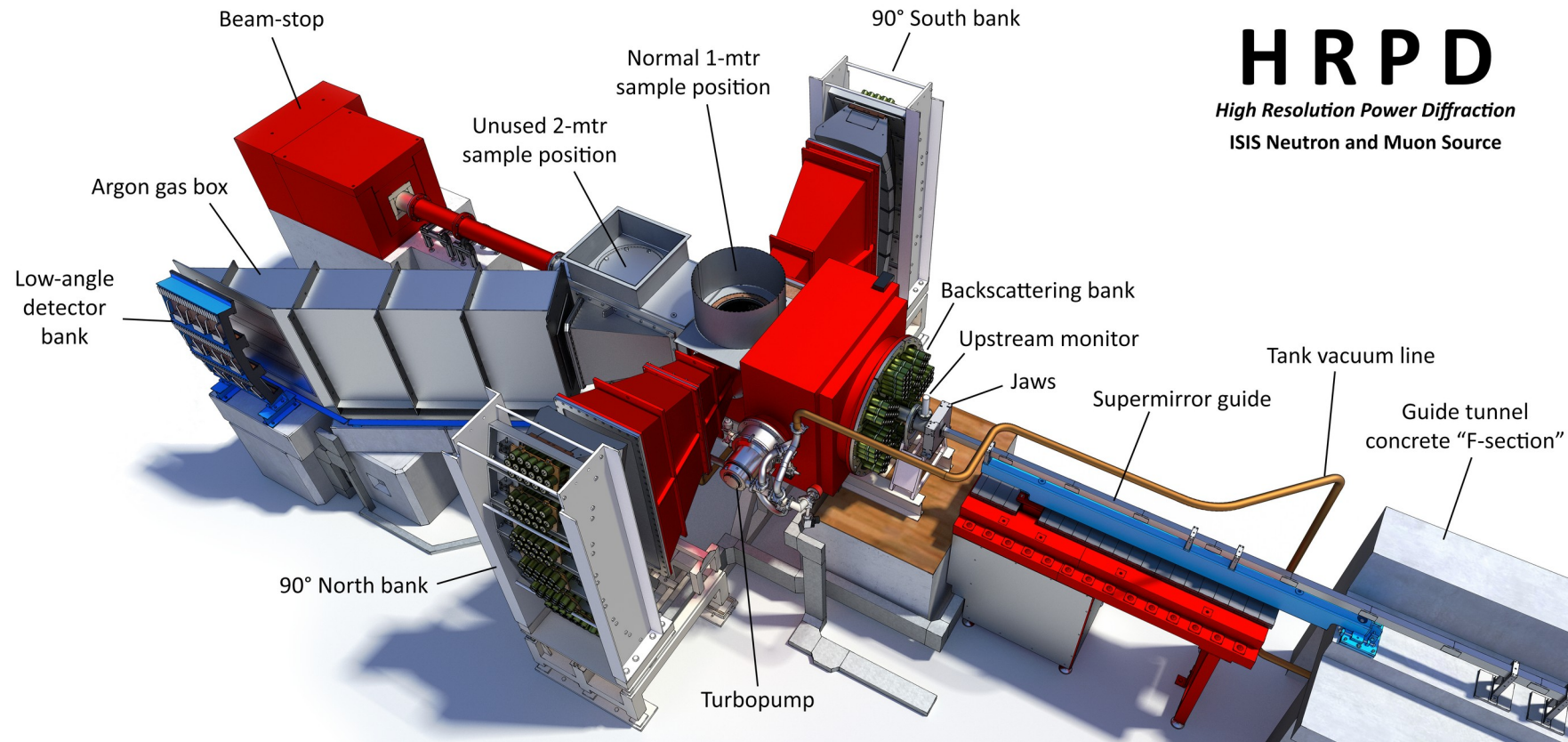
D23: single-crystal diffractometer at the ILL



Time-of-flight neutron diffraction



HRPD: TOF powder diffractometer at ISIS



TOPAZ: single-crystal diffractometer at SNS

