Quantum electrodynamics and quantum optics

Fall 2024

Quantum Science

• Quantum theory has affected every day of our lives: atomic clocks for GPS, transistors, optical comm. $H(t) \mid \psi(t) \rangle = i \hbar \frac{d}{dt} \mid \psi(t) \rangle$







transistors

atomic clocks

Photoelectric effect

 Manipulation of quantum systems is unprecedented: atoms, ions, molecules, superconducting circuits, solid state systems to macroscopic systems...





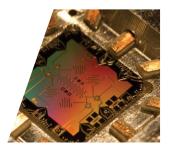




- · Quantum network/communication
- Quantum simulation
- · Quantum metrology







QST potential across disciplines



offer high-speed astronomy



molecules for

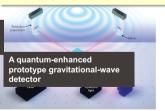


Very active research fields

- Largescale efforts (e.g. EU Flagship on Quantum)
 - Large Quantum Progams at leading institutions (ETHZ. Kavli Delft.
- Nobel Prizes: BEC, Laser Cooling, Quantum Control,...

Quantum across disciplines

- Astronomy
- Gravitational wave detectors
- Biology
- Chemistry

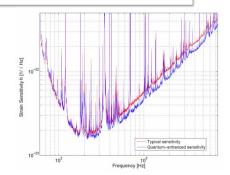


Quantum Science for Precision Measurements

NEWS - 15 FEBRUARY 2019

Gravitational-wave observatory LIGO set to double its detecting power

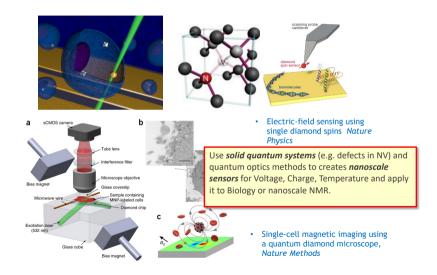
A planned US\$35-million upgrade could enable LIGO to spot one black-hole merger per hour by the mid-2020s.







QST potential across disciplines



Experimental Research in QST at EPFL

Ultracold atoms Quantum Simulations (Brantut)

- Roux Nature Comm 2020
- Brantut Nature, 2015
- **Brantut Science 2013**



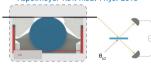
Hybrid Quantum Systems (Scarlino)

Stockklauser, Scarlino, PRX 2017



Quantum measurements (TJK)

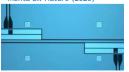
- · Wilson, Nature, 2015
- Aspelmever Rev. Mod. Phys. 2015



$$\frac{d\hat{\rho}}{dt} = -\frac{i}{\hbar} \left[\hat{H}, \hat{\rho} \right] + \mathcal{L}(\hat{\rho})$$

Superconductor Quantum Information (Manucharvan)

Mehta al. Nature (2023)



Superconducting quantum optomechanics and gubits

Youssefi et al. Nature (2022)



Molecular quantum optomechanics (Galland)

· S. Tarrago-Velez, Galland PRX 2019



Course topics

- Quantization of the electromagnetic field
 - Week 1: Quantization of a Harmonic Oscillator, quantization of electrical circuits, field quantization
 - ▶ Week 2-3: Fock states, coherent states and squeezed states
- Measuring the quantum States of Light
 - ▶ Week 4: Phase space representations (Q-function, Wigner function, P-representation)
 - Week 5: Homodyne detection
 - Measurements, photon counting
 - ▶ Photon correlations, HBT effect, g(2) measurements
- Superconducting circuits
 - Week 6: Josephson Junctions
 - Copper pair box and Transmon
 - Circuit quantization

Course topics

Atom field interaction

- ▶ Week 7-8: Light matter interaction, dipole approximation, atom-field interaction Hamiltonian
- ▶ Week 9: Quantum optics of an open cavity, Purcell effect
- ▶ Week 10: Cavity quantum electrodynamics (cQED): strong coupling, dispersive regime
- Applications of cQED: Generation of arbitrary quantum state of a harmonic oscillator, Quantum Metrology, QND measurements of TLS

Introduction to quantum mesaurements

- ▶ Week 11: Quantum non-demolition measurements
- Quantum backaction in linear measurements
- ▶ Week 12: Quantum limits of interferometric measurements
- Week 13: Pondermotive Squeezing
- Week 14: Backaction-Evading Measurements
- Quantum theory of an amplifier

Course rules

- The course will be held in hybrid mode. In person lectures will be held and streamed via zoom.
- Written exam at the end of the semester. The content will be communicated towards the end of the semester.
- Homework is due by the beginning of the next week's exercise session, late submissions will not be graded. Only the starred exercises are graded.
- The exercise session will be held in person in Q&A format.
- Handwritten notes are uploaded to Moodle for reference only. We welcome mistake spotting (feedback to TAs).

Course Structure

- A video lecture will be uploaded to Moodle each week for self learning. In some parts the video quality might not be very good, we apologize for the inconvenience.
- Each week a student will present a paper. The presentation should be around 40 minutes long. Presenters should follow the Beamer template on course Moodle. The slides should be shared with the TAs at least one day before the course.
- Sign up for a presentation/question slot shortly after this lecture (google doc link on Moodle). 13 Topics in total. Send an email to evgenii.guzovskii@epfl.ch
- In week (n+1)'s classroom, first a 30 min summary will be given of week n's lecture video, then the one student will present the paper for one hour.
- ullet Students should both watch the videos and read the paper of week n before next thursday's course.

Grading Policy

Depending on whether you submit homeworks and/or make a presentation, the weight of the final exam towards the final grade might be different:

- Option 1: 100% exam
- Option 2: 90% exam, 10% homework/presentation
- Option 3: 80% exam, 10% homework, 10% presentation

Your final grade will be the maximum between these three options

The assessment of the presentation is binary. The assessment of the homeworks is also binary with an 80% threshold.

Course Comments

- Although this course requires far more than 6 credits of work, which is not a big deal for me, I find that we are left alone and I feel that the teacher does not give any lessons just some summary of the books we have to read and the videos of the course he gave last year, it is a little bit flustrating to have to watch some zoom videos instead of real teaching. Another thing is that we have not access to any corrections to the exercices just some feedbacks from the assistant teachers and I believe it is very difficult to improve our skills and learn from our errors without a thorough corrected version of the exercices.
- . Difficult, but I have better understanding after hours with homework. I feel the course like 8 credit, rather than 6.
- I don't mind graded exercises but not giving a correction is a terrible idea in my opinion. Learning usually happens by making mistakes and correcting them, but with the current system it's hard to know if we even made a mistake in the first place. A grade and a small comment don't only my much information. It's exercisely bard for those who can't on to the everview exercision.
- I like formed in general, but T'm not convinced by the organisation of the exercise session. An assistant show was a way to solve the exercises, but not necessarily the one that we followed, so we cannot know during the exercise session if whe're injudy assistant, but there is not necessarily the contribution of the contri
- Inverted classroom is the worse scum, of course student learn better, it doubles their workload. A tracker can only do it because the other teachers#88217;if down#80217;if worse/body started doing it it would be untenable. And if we already have to watch videos, it would be americalled a start in the research of the workload of the research of the
- . Not particularly fond of the asynchronous teaching style or the "figure it out yourself" approach to exercises. Would prefer a more traditional teaching style for a subject this complex
- The class is very interesting, but a lot of work, even for six credits. As an engineer the loctures are difficult to follow, because we haven't really seen any of the operations used (e.g. the bra-kez notation). It would maybe be helpful to have some sort of cheat sheet that explains some of the basis, that we should know before the class starts. The course lists "Quantum Physics" as a prerequisite, but it should maybe be specified, that it should have been a quantum physics class for physicists and not for engineers. It's difficult to solve the exercises without being able to ask outsetions which led into them, executable for the comprehension of the exercise that?
- The course appears well developed, and the teacher and TA's are good. However, I find the amount of homework, and work in general, to be unfair as reflected by the credits and prerequisites. It easily takes 15-20 hours per week if one wants to actually understand the subject matter, all while indoor, he exercises and two riving to read the week's articles.
- The course is developing very well the themes of quantum electrodynamics and quantum optics. However, the number of credits are not proportional to the workload. Indeed, we get videos of class to watch ourselves in complement of the class. The exercises set are really really long.
- The course is developing very well the themes of quantum electrodynamics and quantum optics. However, the number of credits are not proportional to the workload. Indeed, we get videos of class to watch ourselves in complement of the class. The exercises set are really really long
- the discussion about the article from 10 to 12 is difficult to follow for me, as I don't understand well (I don't have lot's of time during the week to study in details the article(s)).
- . The weekly video lectures are hard to follow because of sound quality and it is sometimes hard to read the blackboard.
- Though I find the lecture interesting. I think it fails to give a soil and clear basis in quantum optics and QED. I think we should take more time to go over the basis: before going into modern research. For some reason, I feel like the lecturer assumes every student has a profound understanding and extensive knowledge of experimental quantum optics. I believe I lack the language and tools to get a grap of the papers we are reading after droing a behaltor which mostly focuses on theory. I see the point that Prof. Kippenberg makes about being waren of the papers we are reading after droing a behaltor which mostly focuses on theory. I see the point that Prof. Kippenberg makes about being waren of the paper we are reading after droing a behaltor which mostly focuses on theory. I see the point that Prof. Kippenberg makes about being waren of the paper was a reading after droing a behaltor which mostly focuses on theory. I see the point that Prof. Kippenberg makes about being waren of the paper was a prof. I see that the subject and failed in the paper was a prof. I see that the subject and after the paper was a prof. I see that Prof. I see that the subject and failed in the paper was a prof. I see that the subject and failed in the paper was a prof. I see that the subject and the subject and failed in the paper was a prof. I see that Prof. I see that Prof. I see that the subject and the subject and failed in the paper was a prof. I see that the subject and the subject and the paper was a prof. I see that the subject and the
- Tremendously interesting but extremely demanding course, probably loser to 8 credits rather than 6. While I agree that the time is well also extend in membrane actually produces high quality learning. I feel that the audio quality of the recorded fectures is too low and I sometimes feel life I don't learn much from them. They don't feel as impactful as they should be a feeding feel with profit and the process of the property of the leight, and they very voluminous preference material; I sepre with Prof, kippoperby's argument about superstar lectures upon a feel see sees of security, but I nonetheless think that the lectures should be a guiding light in the sea of references. Content switching between 5+ different books is not the easiest task. The homeworks also omentiones aren't as useful as they could be. The TAS seem to notice the orablems and listed line immemore by seldent nounce of them.
- Very interesting course, filed with a lot of super interesting content and learning a lot. A lot of work, so only for interested people, the active learning is interesting by the whole would be not to do once every two weeks a full quasa selection and the management of the super interesting by the super int
- Very Interesting, but 6 credits are not nearly enough for the work expected. Inversed classroom is a nice idea, but here I feet it is more like an added classroom, because of the paper presentations, which are demanding to follow aswell. Having a paper presentation week could be left, and a solution shore for the exercices some during me one; than seeing the assistant solving the exercices somes, But overall an extremely interesting course and II like that scentific papers are an important part of the lecture.

Course Comments

- Active learning does require everyone's participation.
- The course recordings are at times not perfect. We are working on re-making the audio.
- This course is a lot of work (more than the credits suggest)
- Handwritten notes are not always well legible but note, they are not replacing the actual primary sources that are referenced.
- Now most of the homework solutions will be uploaded to moodle.

Teaching Philosophy: post COVID

• From: https://www.science.org/doi/epdf/10.1126/science.abj9957

Teaching philosophy

EDUCATION

Active learning: "Hands-on" meets "minds-on"

Widespread disruptions to schooling spurred by COVID-19 have amplified long-standing discussions about what high-quality teaching and learning can be. Growing bodies of research and practice, from early childhood to university classrooms and beyond, demonstrate the benefits of moving beyond traditional lecture-driven approaches in favor of "active learning." Such approaches put students more in the driver's seat through discussions, in-class questions, and feedback; interactive technologies; and other strategies to engage learners and deepen understanding. Beyond cognitive and academic benefits, active-learning approaches can also provide socioemotional support, particularly for students who may not feel at home in or supported by traditional passive learning. But there is no single active-learning approach. Instead, as the experts below describe, we see a rich and developing portfolio of methods and ideas supporting different ways to produce more effective learning.—Brad Wible

Students may learn more than they think

By Louis Deslauriers⁸, Logan McCarty^{8,9}, Kristina Callaghan^{8,10}

Despite strong evidence that active learning based on the principles of deliberate practice produces better educational outcomes (17), traditional lecturing remains the dominant mode of instruction in college STEM courses (18). Why are students and faculty slow to embrace active learning, which seeks to cognitively engage students and opromote peer interactions? In large part, the effortlessness associated with listening to a well-presented lecture can mislead students (and instructors) into thinking that they are learning a lot.

We compared students' perception of learning with their actual learning in college physics classrooms (19). During one class session, half the students were randomly assigned to a class that used active learning (experimental treatment) consisting of students working in small groups on carefully designed in-class activities, followed by instructor feedback tailored to student comments and questions during group work. The other half of the students attended a well-presented lecture (control treatment). The roles were reversed in the subsequent class session. Both experimental and control groups used identical course materials and only the students' active engagement with the material was toggled on and off. We repeated

the same experiment twice in different courses, and the results were the same: Students learned significantly more with active learning (as expected), and they also felt that they learned from it—but their feeling of learning was more pronounced with the well-presented traditional lectures.

These misperceptions have broad implications for STEM education. Course evaluations based on students' perceptions of learning could inadvertently promote inferior methods of instruction—a superstar lecturer can explain things in such a way as to make students feel like they are learning more than they actually are. By contrast, the cognitive effort involved in active learning is a sign of effective learning, even if students may not always perceive it that way. Moreover, these perceptions of learning may also play a role with popular active-learning methods that rely heavily on instructor feedback (17, 20). We recommend that instructors intervene early in the semester to discuss notions of learning versus the feeling of learning and persuade students that they are in fact benefiting from the sustained mental efforts associated with active learning (19). This mismatch between actual learning and the feeling of learning must be addressed and understood by faculty and students for these proven instructional strategies to be more effective and to become widespread.

guidance which certainly belongs after the lecture on rotating systems, but which was, unfortunately, omitted. The fifth and sixth lectures are actually due to Matthew Sands, as I was out of town.

The question, of course, is how well this experiment has succeeded. My own point of view—which, however, does not seem to be shared by most of the people who worked with the students—is pessimistic. I don't think I did very well by the students. When I look at the way the majority of the students handled the problems on the examinations, I think that the system is a failure. Of course, my friends point out to me that there were one or two dozen students who—very surprisingly—understood almost everything in all of the lectures, and who were quite active in working with the material and worrying about the many points in an excited and interested way. These people have now, I believe, a first-rate background in physics—and they are, after all, the ones I was trying to get at. But then, "The power of instruction is seldom of much efficacy except in those happy dispositions where it is almost superfluous." (Gibbons.)."

Still, I didn't want to leave any student completely behind, as perhaps I did. I think one way we could help the students more would be by putting more hard work into developing a set of problems which would elucidate some of the ideas in the lectures. Problems give a good opportunity to fill out the material of the lectures and make more realistic, more complete, and more settled in the mind the ideas that have been exosted.

It think, however, that there isn't any solution to this problem of education other than to realize that the best teaching can be done only when there is a direct individual relationship between a student and a good teacher—a situation in which the student discusses the ideas, thinks about the things, and talks about the things, (18 impossible to learn very much by simply sitting in a lecture, or even by simply diding problems that are assigned. But in our modern times we have so many students to teach that we have to try to find some substitute for the ideal. Perhaps my lectures can make some contribution. Perhaps in some small place where there are individual teachers and students, they may get some inspiration or some ideas from the lectures. Perhaps they will have fun thinking them through—or going on to develop some of the ideas further.

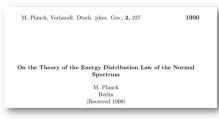
RICHARD P. FEYNMAN

June, 1963

The existence of zero point energy of size $\hbar\omega/2$ is possible.

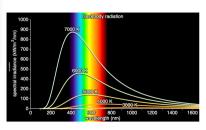
---- Albert Einstein 1913

1900 Planck discovered that spectral distribution of thermal light can be derived from postulating energy of an harmonic oscillator to be quantized.



$$B_v(v, T) = \frac{2hv^3}{c^2} \frac{1}{e^{hv/kT} - 1}$$





1930 The theory of the spontaneous emission under the QED framework was first calculated by Weisskopf and Wigner.





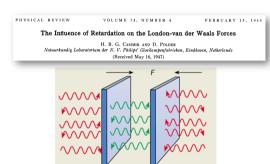
Berechnung der natürlichen Linienbreite auf Grund der Diracschen Lichttheorie*.

Von V. Weisskopf in Göttingen und E. Wigner in Berlin.

Mit 3 Abbildungen. (Eingegangen am 2. Mai 1930.)

Es werden die Diraoschen Gleichungen der Wechselwirkung zwischen Atom und Strahlung in einer von der üblichen verschiedenen Art näherungsweise gelöst. Die Lösungen gelten während der ganzen Zeit, die für die Emission praktisch in Betracht kommt, mit der gleichen Näherung und liefern den Intensitätsverlauf in der Emissionalinien des Atoms.

1948 The Casimir effect was first predicted in 1948 by Hendrik Casimir of Philips Research Laboratories in the Netherlands.





PHYSICAL REVIEW

VOLUME 72, NUMBER 3

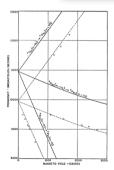
AUGUST 1, 1947

Fine Structure of the Hydrogen Atom by a Microwave Method* **

WILLIS E. LAMB, JR. AND ROBERT C. RETHERFORD

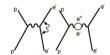
Columbia Radiation Laboratory, Department of Physics, Columbia University, New York, New York

(Received lune 18, 1947)



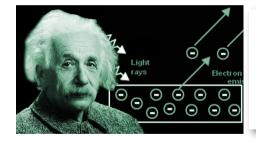
1947

The Lamb shift was first measured in 1947 in the Lamb–Retherford experiment on the hydrogen microwave spectrum and this measurement provided the stimulus for renormalization theory to handle the divergences..





1905 Photoelectric effect could be explained by quantized energy states of light.



6. Über einen
die Erzeugung und Verwandlung des Lichtes
betreffenden heuristischen Gesichtspunkt;
von A. Einstein.

Zwischen den theoretischen Vorstellungen, welche sich die Physiker über die Gase und andere ponderable Körper gebildet haben, und der Maxwellschen Theorie der elektromagnetischen Prozesse im sogenannten leeren Raume besteht ein tiefgreifender formaler Unterschied. Während wir uns mämlich den Zustand eines Körpers durch die Lugen und Geschwindigkeiten einer zwar sehr großen, jedoch endlichen Anzahl von Atomen und Elektronen für vollkommen bestimmt ansehen, bedienen wir uns zur Bestimmung des elektromagne-

1909 G.I. Talyor attempted to find quantum effects of light via optical interference using single photons.

114 Mr Taylor, Interference fringes with feeble light.

Interference fringes with feeble light. By G. I. TAYLOR, B.A., Trinity College. (Communicated by Professor Sir J. J. Thomson, FRS)

[Read 25 January 1909.]

The phenomena of ionisation by light and by Röntgen rays have led to a theory according to which energy is distributed unevenly over the wave-front (J. J. Thomson, Proc. Comb. Phil. Soc. XIV. p. 417, 1997). There are regions of maximum energy widely separated by large undisturbed areas. When the intensity of light is reduced these regions become more widely separated, but the amount of energy in any one of them does not change;



1954

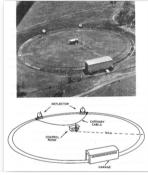
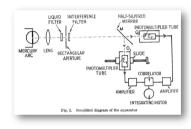


Figure 1. Aerial photo and illustration of the original HBT apparatus, They have been extracted from Ref.[1].



Hanbury-Brown-Twiss experiment realized the measurement of two-time intensity autocorrelation functions which gives photon bunching.

1954 Working with Herbert J. Zeiger and graduate student James P. Gordon, Townes demonstrates the first maser at Columbia University.

1960 Theodore H. Maiman, a physicist at Hughes Research Laboratories in Malibu, Calif., constructs the first laser using a cylinder of synthetic ruby measuring 1 cm in diameter and 2 cm long, with the ends silver-coated to make them reflective and able to serve as a Fabry-Perot resonator. Maiman uses photographic flashlamps as the laser's pump source.



PHYSICAL REVIEW

VOLUME 130, NUMBER 6

15 JUNE 1963

The Quantum Theory of Optical Coherence*

ROY J. GLAUBER

Lyman Laboratory of Physics, Harvard University, Cambridge, Massachusetts

(Received 11 February 1963)



1963 Glauber's quantum theory of coherence predicted anti-bunching of light (classical theory would require negative probabilities)

1975-1976 Prediction and measurement of non-classical light in two level systems (resonance fluorescence) → Quantum Optics

A quantum-mechanical master equation treatment of the dynamical Stark effect

H J Carmichael† and D F Walls
School of Science, University of Waikato, Hamilton, New Zealand

Received 7 November 1975, in final form 28 January 1976

Photon Antibunching in Resonance Fluorescence

H. J. Kimble, ^(a) M. Dagenais, and L. Mandel Department of Physics and Astronomy, University of Rochester, Rochester, New York 14627 (Received 22 July 1976).

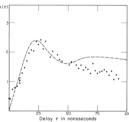
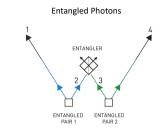


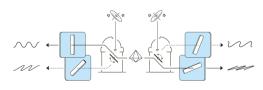
FIG. 3. Values of $1+\lambda(\tau)$ derived from the data. The broken curve shows the theoretically expected form of $(\hat{I}_G(\tau))$ (with $\Omega/\beta=4)$ for a single atom, arbitrarily normalized to the same peak,

Modern Developments of Quantum Optics

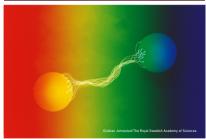
Quantum Entanglement











EPR paradox

MAY 15, 1935 PHYSICAL REVIEW VOLUME 47 Can Quantum-Mechanical Description of Physical Reality Be Considered Complete?

A. EINSTEIN, B. PODOLSKY AND N. ROSEN, Institute for Advanced Study, Princeton, New Jersey
(Received March 25, 1918)

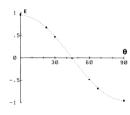
VOLUME 49. NUMBER 2 PHYSICAL REVIEW LETTERS 12 JULY 1982

Experimental Realization of Einstein-Podolsky-Rosen-Bohm Gedankenexperiment: A New Violation of Bell's Inequalities

Alain Aspect, Philippe Grangler, and Gérard Roger
Institut d'Optique Théorique et Appliquée, Laboratoire asucée au Centre National de la Recherche Scientifique,
Université Paris -Sud, F-24.06 Grusy, Prace
(Roccived de December 1996)

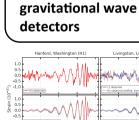






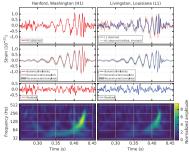
Gravitational wave detection



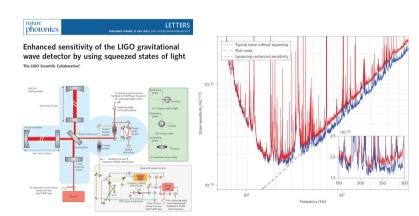


Quantum and thermal noises in





Gravitational wave detection



Cavity quantum electrodynamics



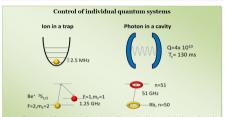


Fig. 1: Historation of the too types of experiments discussed in this scientific background. On the left, an ion is captured in a harmonic trap. Its quantum state (both its internal state mit motion) is controlled by interaction with laser pulses as exemplified for the case of Be-. On the right, a photon is (or several photons are) trapped in a high-Q microwave eavity. The field state is measured and controlled by interaction with highly excited Rb atoms.

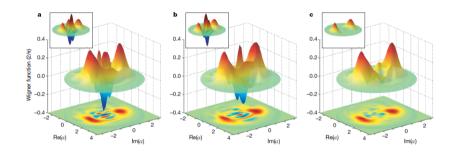
Control of individual quantum system







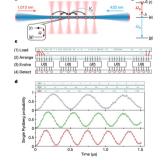
Cavity quantum electrodynamics



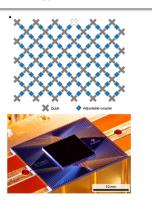
How nonclassical states are prepared and how their decoherence can be measured.

Quantum Computing and Quantum Simulation

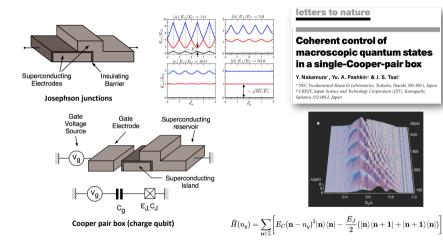




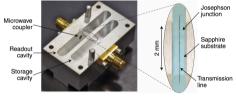
Quantum supremacy using a programmable superconducting processor

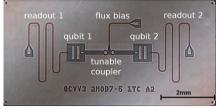


Artificial atoms (qubits) with Josephson junctions



Circuit quantum electrodynamics (cQED) Architectures



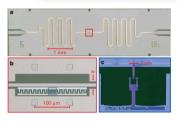


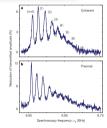
Single qubit coupled to a 3D cavity

Superconducting circuit device with two transmon-type qubits

Dispersive regime

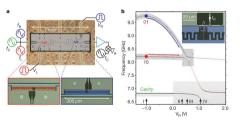


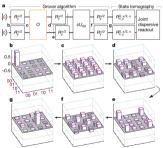




Circuit quantum electrodynamics

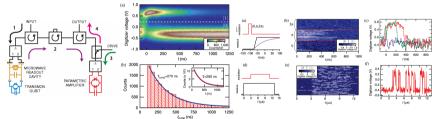




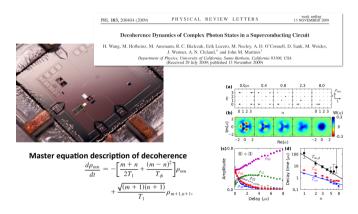


Circuit quantum electrodynamics

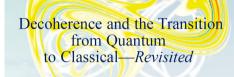




Circuit quantum electrodynamics

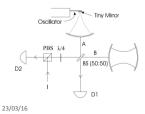


Transition from Quantum to Classical



How to probe decoherence of macroscopic objects

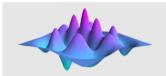
$$H = \hbar \omega_c a^{\dagger} a + \hbar \omega_m b^{\dagger} b - \hbar G a^{\dagger} a (b + b^{\dagger}),$$





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Toolbox



QuTiP

Quantum Toolbox in Python

Features

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Master equation description of decoherence

$$\frac{d\rho_{mn}}{dt} = -\left[\frac{m+n}{2T_1} + \frac{(m-n)^2}{T_{\phi}}\right]\rho_{mn} + \frac{\sqrt{(m+1)(n+1)}}{T_1}\rho_{m+1,n+1}$$

Papers Using QuTiP

80. Lörch et al. "Sub-Poissonian Phonon Lasing in Three-Mode Optomechanics".

79. Dalmonte et al., "Cluster Luttinger liquids and emergent supersymmetric conformal critical points in the one-dimensional soft-shoulder Hubbard model".

78. Weimer, "Variational analysis of driven-dissipative Rydberg gases".

77. Schulte et al., "Quantum Algorithmic Readout in Multi-lon Clocks",

76. Dalmonte et al., "Dipolar Spin Models with Arrays of Superconducting Oubits".

75. Neilinger et al., "Two-photon lasing by a superconducting qubit".

74. Elliott et al., "Driving with squeezed vacuum in circuit quantum electrodynamics",

73. Borregaard et al. "Heralded quantum gates with integrated error detection in optical cavitites".

arXiv:1502.04112

arXiv:1502.00396

arXiv:1501.07284

arXiv:1501.06453

arXiv:1501.03098

arXiv:1501.01009